



IIT ROORKEE



NPTEL ONLINE
CERTIFICATION COURSE

MULTIPLE LINEAR REGRESSION Part-4

LECTURES 25

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MULTIPLE LINEAR REGRESSION

- Variable Selection
 - Availability of large no. of variables for selecting a set of predictors
 - Main idea is to select most useful set of predictors for a given outcome variable of interest
 - Selecting all the variables in the model is not recommended
 - Data collection issues in future
 - Measurement accuracy issues for some variables
 - Missing values
 - Parsimony



MULTIPLE LINEAR REGRESSION

- Variable Selection
 - Selecting all the variables in the model is not recommended
 - Multicollinearity: two or more predictors sharing the same linear relationship with the outcome variable
 - Sample size issues: Rule of thumb

$$n > 5*(p+2)$$

Where n=no. of observations

And p=no. of predictors

- Variance of predictions might increase due to inclusion of predictors which are uncorrelated with the outcome variable
- Average error of predictions might increase due to exclusion of predictors which are correlated with the outcome variable



MULTIPLE LINEAR REGRESSION

- Bias-variance trade-off
 - too few vs. too many predictors
 - Few predictors \rightarrow higher bias \rightarrow lower variance
 - Drop variables with ‘coefficient $<$ std. dev. of noise’ and with moderate or high correlation with other variables
 - Lower variance
- Steps to reduce the no. of predictors
 - Domain knowledge
 - Practical reasons



MULTIPLE LINEAR REGRESSION

- Steps to reduce the no. of predictors
 - Summary statistics and graphs
 - Statistical methods using computational power
 - Exhaustive search: all possible combinations
 - Partial-iterative search: algorithm based
- Exhaustive Search
 - Large no. of subsets
 - Criteria to compare models
 - Adjusted R^2



Key References

- Data Science and Big Data Analytics: Discovering, Analyzing, Visualizing and Presenting Data by EMC Education Services (2015)
- Data Mining for Business Intelligence: Concepts, Techniques, and Applications in Microsoft Office Excel with XLMiner by Shmueli, G., Patel, N. R., & Bruce, P. C. (2010)

Thanks...

