

a. Best model based on accuracy:

From my results:

- **Linear Regression:** 0.96
- **Polynomial Regression (degree 2):** 0.9733
- **Polynomial Regression (degree 3):** 0.9467
- **Naive Bayes (GaussianNB):** 0.9667
- **kNN (k=5):** 0.9467
- **LDA:** 0.98
- **QDA:** 0.9733

Thus, the best model is **Linear Discriminant Analysis (LDA)** with an accuracy of **0.98**.

b. Why other models perform slightly worse

1. Linear Regression (0.96)

- Regression is not designed for classification; it predicts continuous values that must be rounded.
- This rounding may misclassify borderline samples.
- It does not model class boundaries directly, so it underperforms compared to LDA/QDA.

2. Polynomial Regression (degree 2) (0.9733)

- Very close to QDA and almost as good as LDA.
- However, polynomial regression can **overfit** on training folds, which may reduce its ability to generalize perfectly to the test fold.

3. Polynomial Regression (degree 3) (0.9467)

- Higher degree polynomials introduce **too much flexibility**.
- The model captures noise and overfits, which hurts generalization.

- Accuracy drops because the class decision boundaries become too complex.

4. **Naive Bayes (0.9667)**

- Assumes **feature independence** given the class, which isn't true for the iris dataset (e.g., petal length and width are correlated).
- Still performs well, but not as high as LDA which models covariance between features.

5. **kNN (0.9467)**

- Relies on local neighborhoods.
- Sensitive to class overlap and the chosen value of **k**.
- With $k=5$, some misclassifications happen when neighbors belong to multiple classes, especially between versicolor and virginica (which are harder to separate).

6. **QDA (0.9733)**

- Slightly worse than LDA.
- QDA allows each class to have its own covariance matrix, which increases flexibility.
- This flexibility can backfire on small datasets like Iris (150 samples), where covariance estimates may not be stable → leading to minor misclassifications.