Multi-objective Model-Predictive Control for Dielectric Elastomer Wave Harvesters.

Matthias K. Hoffmann* Lennart Heib* Giacomo Moretti** Gianluca Rizzello*** Kathrin Flaßkamp*

* Systems Modeling and Simulation,
(e-mail: {matthias.hoffmann, kathrin.flasskamp}@uni-saarland.de,
lennartheib@gmail.com)

** Università degli Studi di Trento, (e-mail: giacomo.moretti@unitn.it)

*** Intelligent Material Systems Lab,
(e-mail: gianluca.rizzello@imsl.uni-saarland.de)

* and *** from Saarland University, Saarbrücken, Germany.

Abstract:

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1. INTRODUCTION

2. MODEL AND PROBLEM STATEMENT

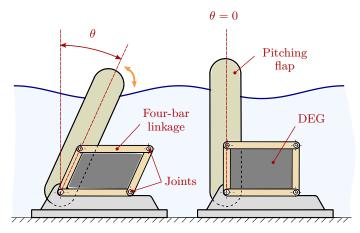


Fig. 1. Wave surge converter: A flap mounted to the sea floor is tilted by the wave motion. It is displayed in a generic (left) and the vertical equilibrium position (right).

2.1 Background

In this work, we investigate the Model-predictive Control (MPC) of the wave surge converter (see, e.g. Whittaker and Folley (2012)), displayed in Fig. 1. The device is pivoted to the sea, such that incoming waves excite an oscillatory motion. This motion distorts a dielectric elastomer generator (DEG) mounted to a deformable parallelogram Moretti et al. (2014). Through this parallelogram, the DEG applies a torque to the flap towards the equilibrium position $\theta=0$. Applying a voltage to the DEG adds an electrostatically-induced torque in the same angular direction, making the system stiffer.

When a voltage is applied to the DEG, charge carrier accumulate in the DEG. By deforming the parallelogram

to a smaller area, the charge density increases, such that energy can be extracted. As we showed in our previous work Hoffmann et al. (2022), controlling the input to maximise the energy extracted from the system requires application of large voltages, damaging the DEG-material over time, and resulting in system failure after too much damage accumulated Chen et al. (2019). For that reason, we also took the damage into consideration as a second control goal, resulting in lower electric fields in the DEG.

2.2 Model

The dynamics of the wave surge

$$\begin{bmatrix} \dot{\theta} \\ \dot{\delta} \\ \dot{z} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0^{1 \times n} \\ -I_h^{-1} K_h & -I_h^{-1} B_h & -I_h^{-1} C_r \\ 0^{n \times 1} & B_r & A_r \end{bmatrix} \begin{bmatrix} \theta \\ \delta \\ z \end{bmatrix} + \\ + \begin{bmatrix} 0 \\ I_h^{-1} \\ 0^{n \times 1} \end{bmatrix} (d - C_0 \theta u),$$
(1)

contain the equation of angular motion and the wave loads generated by the interaction of the waves with the flap. Here, $\delta = \dot{\theta}$ describes the flap's angular velocity and $z \in \mathbb{R}^n$ the *n*-dimensional state vector for wave radiation (Yu and Falnes (1995)). The input u is the electrostatic force generated by the DEG when a voltage v is applied. Since the DEG's electrostatic force is proportional to the v^2 , u is restricted to be positive.

2.3 Cost functions

Our aim is the simultaneous minimisation of damage and maximisation of extracted energy, which we will employ in a multi-objective Optimal Control (MOOCP) setting. The extracted energy cost function is modelled as the negative generated energy

$$J_{1} = \Psi(t_{f}) - \Psi(0) + \int_{0}^{t_{f}} \left(B_{h} \dot{\theta}^{2} + z^{\mathsf{T}} S_{r} z + \frac{u}{R_{0}} - d\dot{\theta} \right) dt$$
with $\Psi = \frac{1}{2} I_{h} \dot{\theta}^{2} + \frac{1}{2} K_{h} \theta^{2} + \frac{1}{2} z^{\mathsf{T}} Q_{r} z + \frac{1}{2} C_{0} \left(1 - \theta^{2} \right) u,$
(2)

with the storage function ψ including kinematic, potential, electrostatic, and hydrodynamic energy contributions. Dissipations due to viscous, hydrodynamic, and electrical losses, and the power input by the incident wave are considered via the integral terms. more explanations?, see mathmod paper

Under the assumption, that damage only starts accumulating after the applied electric field exceeds a threshold $E_{\rm th}$, the cost function can be formulated as

$$J_2 = \alpha \int_0^{t_f} \left(\max \{ \cos^2(\theta) u - E_{th}^2 h_l^2, 0 \} \right)^{n_d} dt.$$
 (3)

3. METHODS

3.1 Model-predictive Control

MPC arose from optimal control as one answer on how to "close the loop" (Rawlings et al. (2017)). In optimal control, a system's behaviour is predicted into the future, while optimising the inputs to the system, such that a cost function is minimised. The working principle of MPC is repeatedly solving an Optimal Control Problem (OCP), only applying the first of the calculated inputs, and measuring the system's state.

4. NUMERICAL RESULTS

The following simulations were done using MATLAB. The optimisation problems were formulated and solved using the CasADi package by Andersson et al. (2019) and the Ipopt solver by Wächter and Biegler (2006).

- 4.1 Fractional Brownian Motion Noise
- 4.2 Multi-objective Optimal Control

Methods from Hoffmann et al. (2022).

4.3 Model-predictive Control

5. CONCLUSION

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