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Authors: Stuart R. Borrett, Matthew K. Lau

Addresses:

SRB: Department of Biology and Marine Biology, University of North Carolina Wilmington, Wilmington, NC, 28403

• MKL: Department of Biological Sciences and the Merriam-Powell Center for Environmental Research, Northern Arizona University, 617 S. Beaver St., Flagstaff, AZ, 86011

Contact Details:

• Email: borretts@uncw.edu

Phone: 910.962.2411Fax: 910.962.4066

enaR: An R package for Ecosystem Network Analysis

Stuart R. Borrett a,* and Matthew K. Lau^b

^a Department of Biology and Marine Biology,

University of North Carolina Wilmington, Wilmington, NC, 28403

b Department of Biological Sciences and the Merriam-Powell Center for Environmental Research, Northern Arizona University, 617 S. Beaver St., Flagstaff, AZ, 86011

* Corresponding author, borretts@uncw.edu

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1 Abstract

- Network analysis is a useful approach for complex, relational datasets in many biological
- fields, including ecology and molecular and evolutionary biology.
- Here, we introduce enaR, an R package for conducting Ecosystem Network Analysis (ENA),
- an analytical tool set rooted in ecosystem ecology with over 30 years of development, which
- examines the structure and dynamics of matter and energy movement between discrete eco-
- logical compartments (e.g., a food web).
- In addition to describing the primary functionality of the package, we also highlight several
- value added features, including a library of 100 empirical ecosystem models, the ability to
- analyze and compare multiple models simultaneously, and connections to useful ecological
- network analysis tools in R.
- KEYWORDS: network analysis, ecosystem, open-source software, network environ analysis,
- ascendency, input-output analysis, food web, urban metabolism, Ecopath, WAND

14 1 Introduction

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Network Ecology – the study of ecological systems using network models and analyses to characterize their structure, function, and evolution – is a large and rapidly growing area of ecology (Proulx et al., 2005). For example, Ings et al. (2009) discovered that a notable fraction of 2008 publications 17 in 11 select journals were related to food webs ($\approx 2.4\%$), mutualistic networks ($\approx 0.9\%$), and hostparasitoid networks ($\approx 0.06\%$). Likewise, Borrett et al. (2014) found that the percent of ecology and 19 evolutionary biology papers indexed by Web of Science that could be classified as Network Ecology 20 increased from 1.3% in 1991 to more than 5% in 2012. This rise of Network Ecology contributes 21 to, mirrors, and builds on the more general growth of network sciences (Barabási, 2012; Borgatti & Foster, 2003; Freeman, 2004; Newman, 2003; Wasserman & Faust, 1994). Ecosystem Network Analysis (ENA) is a branch of Network Ecology that has been used to 24 address a range of key ecosystem questions (Borrett et al., 2012; Fath & Patten, 1999; Ulanowicz, 1986). For example, in the food web of Big Cypress National Preserve (Florida, USA) Bondavalli & Ulanowicz (1999) found evidence of an indirect mutualism between the American alligator and some of its previtems. Applications of ENA have also lead to new insights into the classic trophic questions of "What limits food-chain length?" (Ulanowicz et al., 2014) and "Are food webs modular?" (Allesina et al., 2005; Borrett et al., 2007; Krause, 2004). Hines et al. (2012) used ENA to quantify the relative importance of coupling between biogeochemical processes (e.g., nitrification) in the Cape Fear River estuary sedimentary nitrogen cycle. Further, scientists have used ENA to investigate differences in urban sustainability (Bodini & Bondavalli, 2002; Bodini et al., 2012; Chen & Chen, 2012; Zhang et al., 2010). Collectively, this work consistently shows the power of a transactional network to generate unexpected ecological relationships that then influence the system function and evolution (Jørgensen et al., 2007; Patten, 1991; Ulanowicz, 1997).

enaR is an open-source software to facilitate ENA. Extant ENA software (Allesina & Bondavalli,

2004; Christensen & Walters, 2004; Fath & Borrett, 2006; Kazanci, 2007; Ulanowicz & Kay, 1991) each have critical limitations, which led us to three primary design objectives for enaR. The first objective was to collect the major ENA functions into a single software package. While multiple 40 investigators have contributed to algorithmic development (e.g., Allesina & Bondavalli, 2003; Fath & Patten, 1999; Finn, 1976; Ulanowicz, 1986; Ulanowicz & Kay, 1991), the broad set of tools is not available in a single existing software. The second objective was to increase the availability and extensibility of the software. We chose to use R in part because of its increasing popularity as an analytical tool in the biological sciences (e.g., Dixon, 2003; Metcalf et al., 2012; Revell, 2012). Further, users can freely download a stable version of the package from the CRAN website (http://cran.r-project.org/web/packages/enaR/), and the code for every function in R is available from within R (e.g., edit(function_name)). In addition, enaR development is being managed via GitHub (https://github.com/TheSeeLab/enaR) to encourage collaborative development. The third design objective was to enable enaR users access to network analysis tools from other disciplines. To enable this, enaR was designed to work directly with two existing R network 51 analysis packages: network (Butts, 2008a) and sna (Butts, 2008b). In summary, the aim of the 52 enaR package is to make ENA tools more available and easier to use, adapt, and extend. 53 In this paper, we present an overview of enaR and highlight some of its functionality. A full 54 description of the ENA algorithms and their use and interpretation is beyond the scope of this short paper, but we refer interested readers to a selection of reviews as an entry point to ENA (Fath & Borrett, 2006; Fath & Patten, 1999; Jørgensen et al., 2007; Schramski et al., 2011; Ulanowicz, 1997). For a more comprehensive description on how to use the enaR package, please refer to the package vignette: http://cran.r-project.org/web/packages/enaR/vignettes/enaR.pdf.

60 2 Overview of enaR

ENA is an agglomeration of algorithms developed to analyze network models of energy or matter
movement in ecosystems (e.g., Fath & Patten, 1999; Hannon, 1973; Ulanowicz, 1986), but it can
generally be applied to any Input-Output system that follows a thermodynamically conserved
unit among the compartments. Thus, it is a family of related algorithms to analyze the ecosystem
from several perspectives including its structure, flow, storage, and utility. Together, these analyses
function as a "macroscope" to investigate (1) whole system organization, (2) the direct and indirect
effects among system components, and (3) the processes that create and sustain ecological systems.
In this section we provide an overview of these algorithms and tools include in the enaR software.

After describing the required model information, we highlight the primary ENA algorithms included
in enaR. We then walk through an example application of the enaR Flow analysis.

71 2.1 Data Requirements and Input

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ENA is a data-intensive methodology. The system is modeled as a set of compartments or network nodes that represent species, species-complexes (i.e., trophic guilds or functional groups), or non-living components of the system in which energy or matter is stored. These nodes are connected by a set of direct energy or matter transactions among the nodes, termed directed edges or links. These models also have energy—matter inputs into the system and output losses from the system. In summary, the full set of data required includes: (1) internal flows, (2) boundary inputs, (3) boundary exports, (4) boundary respiration, (5) boundary outputs, which may be the sum of exports and respiration, (6) biomass or storage values, and (7) designation of living status of each node. While all seven elements are required for a full analysis, the specific data requirements varies among the ENA algorithms.

The primary ENA algorithms in enaR assume the model data is presented as an R network data

object defined in the network package. Given the data elements, users can use the pack function to combine the data elements into the R network data object. While a standard data format for an ENA model does not yet exist, there are two commonly used formats. First, there is the Scientific Committee for Ocean Research (SCOR) format that is the required input to NETWRK (Ulanowicz & Kay, 1991), and the second format is the Excel sheet formatted data that is the input to WAND (Allesina & Bondavalli, 2004). The enaR package includes a read.scor and a read.wand function to read in these common data formats (Table 1).

90 2.2 Visualization

Visualization of network models can be an essential analytical tool (Lima, 2011; Moody et al., 2005). Because enaR is built specifically to use the network package and data type, it is possible to quickly create network plots of the model internal structure. Fig. 1a shows an example visualization of Dame & Patten's (1981) Oyster Reef ecosystem model. The network package includes three network layout algorithms: circle, Fruchterman-Reingold, and Kamada-Kawai. The Fruchterman-Reingold algorithm used here is the default. The R script to generate this visualization is included in the online supplementary information.

98 2.3 Algorithm Overview

enaR includes many of the most commonly used ENA algorithms (Table 2), along with a number of
work flow tools and specialty analyses (Tables 1 and 3). Note that the nine primary ENA functions
begin with the prefix 'ena' followed by the specific analysis name (see Table 2). There are a total
of 34 functions in the enaR package.

Scharler & Fath (2009) identify two schools of ENA. The first school is based on the work of Robert Ulanowicz and colleagues at the University of Maryland (Ulanowicz, 1986, 1997, 2009).

Primarily focused on trophic ecology, this approach uses information theory and the ascendency concept that characterizes ecosystem growth and development Ulanowicz (1986, 1997). This work is often referred to as "Ecological Network Analysis" as it predates many other types of network 107 ecology. The second school is based on the work of Bernard Patten at the University of Georgia 108 (Fath & Patten, 1999; Matis & Patten, 1981; Patten, 1982; Patten et al., 1976). Steeped in dynamic 109 equations, simulations, and systems analysis, this approach developed around the environ concept 110 that formalizes the concept of environment (Patten, 1978), and has often been referred to as "Net-111 work Environ Analysis." enaR currently captures all of the Patten School algorithms previously 112 implemented in NEA.m (Fath & Borrett, 2006). Presently, the Ulanowicz School algorithms are 113 more limited, including the ascendency calculations (Ulanowicz, 1997) and mixed trophic impacts 114 analyses (Ulanowicz & Puccia, 1990); however, we expect the package capabilities to continue to 115 grow, especially with the assistance of new users. This combination of the Patten and Ulanowicz 116 schools of analyses is rare in extant software. 117

118 2.4 Example Application

Given a network model, applying ENA algorithms with enaR is straight forward. We demonstrate how to use the package with an example Flow analysis on Dame & Patten's (1981) model of energy flow in an Oyster Reef ecosystem. Table 4 shows the example script. The analysis involves: (1) loading the model data, (2) checking and balancing the model if necessary, and (3) inputing the balanced model into the analysis function. The final step is interpreting the analytical output. This is a typical workflow for ENA.

After loading the enaR package, the next step is to enter the model data. Here, we have extracted the model information from the paper and created a vector of node names, the flow matrix (F), inputs (z), outputs (y), and the logical vector indicating whether or not the nodes

are living (Table 4). We then use the pack function to create the required network data object. The next step is to apply the ssCheck function ensure that the model is at steady-state, which is 129 one of the assumptions of the flow analysis (Fath & Borrett, 2006; Finn, 1976). If the model had 130 not been at steady-state, we could have then applied one of four automated balancing algorithms 131 (AVG, Input-Output, Output-Input, AVG2; Allesina & Bondavalli, 2003) to force the model into a 132 steady-state. We then apply the enaFlow function to the model to perform the desired ENA flow 133 analysis. As shown with the attributes function, this analysis returns 4 matrices (G, GP, N, 134 **NP**) and two vectors (throughflow, T, and a vector of 20 whole-network statistics, ns). 135 Interpreting the ENA results is the final challenge. Here, we provide a few illustrative interpre-136

tations of the Flow analysis. Starting with the whole-network flow statistics, we see that the total 137 system throughflow (TST) of the oyster reef model is 83.6 Kcal m⁻² d⁻¹. TST is a measure of 138 the total activity of the system, which is often referred to as the size or power of the system. The 139 Finn Cycling Index (FCI) indicates that 11% of this activity was generated by recycling. Further, the average path length (APL = 2.02) shows that an average input passes over two paths before 141 exiting the system, and the ratio of indirect to direct flows (ID.F = 1.58) indicates that the indirect 142 flow exceeds the direct flow in this system. Together, these whole network indicators show the 143 importance of indirect interactions in the system. A next analytical step might be to apply the Utility or Mixed Trophic Impacts analyses to determine the net relationships among the ecosystem 145 components when we consider the direct and indirect interactions, but this is beyond our analysis 146 here. More detailed guidance for how to interpret ENA results can be found in previously published 147 literature (Fath & Borrett, 2006; Jørgensen et al., 2007; Schramski et al., 2011).

3 Value Added Features

There are several features of the enaR package beyond the core analyses that add substantive value for users. In this section, we highlight several value added features, including a library of 100 ecosystem network models, methods for conducting batch analysis (i.e., simultaneous analysis of multiple models), and connections to other analytical software.

154 3.1 Model Library

To facilitate new systems ecology and network science, we included a library of 100 previously 155 published ecosystem network models with the enaR package. These models each trace a thermo-156 dynamically conserved unit (e.g., C, N, P) through a particular ecosystem. The models in this set 157 are empirically-based in that the authors attempted to model a specific system and parameterized the model to some degree with empirical estimates. While the library includes models used pre-159 viously to test several systems ecology hypotheses (Borrett, 2013; Borrett & Salas, 2010; Borrett 160 et al., 2010; Salas & Borrett, 2011), and the set has a 47% overlap with the set of models previously 161 collected by Dr. Ulanowicz (http://www.cbl.umces.edu/~ulan/ntwk/network.html), the full set has not previously been collected and distributed together. 163

We have tentatively split these models into two classes. The most abundant class is the trophic network models. These models tend to have a food web at their core, but also include non-trophic fluxes generated by processes like death and excretion. The annual carbon flux model for the meso-haline region of the Chesapeake Bay is a typical example (Baird & Ulanowicz, 199). The second class of models focuses on biogeochemical cycling. In contrast to the trophic networks, the biogeochemical cycling models tend to have more highly aggregated nodes (more species grouped into a compartment), include more abiotic nodes that could represent chemical species (e.g., ammonia in a nitrogen cycle), have a lower dissipation rate, and therefore they tend to have more recycling

(Borrett *et al.*, 2010; Christian *et al.*, 1996). Christian & Thomas's (2003) models of nitrogen cycling in the Neuse River Estuary are good examples of the class. The package vignette has a full listing of the models included along with references to their original publications (Lau *et al.*, 2013).

175 3.2 Batch Analysis

Advances in ecosystem ecology have been made by comparing network metrics across multiple 176 ecosystem models. For example, Christensen (1995) applied ENA to identify and compare the 177 maturity of 41 ecosystem models, and van Oevelen et al. (2011) compared the the organic matter processing of food webs in three sections of the Nazaré submarine canyon. The enaR tool simplifies 179 the work flow for these types of comparison. Given a list of models like the model library, it is 180 possible to quickly analyze multiple models using R's lapply function (see help("lapply")). This 181 facilitates the kind of comparative network analysis often of interest to ecologists (Christian et al., 182 2005; Monaco & Ulanowicz, 1997; Whipple et al., 2007). 183 Batch analysis can be used in several additional ways. One application is for meta-analyses, 184 such as tests of the generality of hypothesized ecosystem properties like network non-locality (Salas 185 & Borrett, 2011), or to investigate how physical features might influence ENA results (Niquil et al., 186 2012). Fig. 1b illustrates the rank-ordered network homogenization statistic for the 56 trophic-187 based ecosystem models in the library. Notice that the homogenization statistic is greater than one 188 in all of these models indicating that the network of indirect interactions tend to more uniformly distribute the resources than is obvious from the direct interactions, which extends previous results 190 of Borrett & Salas (2010) to include several new models. A second kind of application is the 191 exploration of new ENA inter-relationships. With the collection of algorithms and the library of 192 models, we can now investigate possible relationships among ENA indicators from different schools (Fig. 1c). The R script to generate Fig. 1 is available as an online enhancment. A third application of batch analysis is to investigate the previously unknown empirical ranges of ENA whole-network statistics, which may be useful for interpreting results from specific applications. Fig. 2 shows the observed distribution of values for selected network statistics from the 100 models in the library easily analyzed using lapply and the associated enaR functions.

A third added benefit of the enaR package design is that it enables network ecologists easier access to

199 3.3 New Connections

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other network tools and analyses that might be useful. The enaR package uses the R network data 201 structure defined in the network package (Butts, 2008a). This means that network ecologists using 202 enaR can also use the network manipulation functions and visualization features of the network 203 package. Further, the R Social Network Analysis (SNA) package, sna, (Butts, 2008b) also uses this 204 network data object. This means that network ecologists can apply many of the SNA algorithms 205 directly to their ecological network models. Fig. 1d illustrates applying the betweenness centrality 206 function to the Chesapeake Bay trophic model (Baird & Ulanowicz, 199) and visualizing the results 207 using a target centrality plot (Brandes et al., 2003). This analysis highlights the central role of 208 Sedimentary Particulate Carbon and bacteria in the Sediment Particulate Organic Carbon (POC) 200 in the carbon flux of the estuary. 210 In addition, enaR can be a starting point for ecosystem network ecologists to use other R 211 network tools. For example, the iGraph package provides functions to apply classic graph theory 212 (Csardi & Nepusz, 2006). The limSolve package provides capabilities to infer network model fluxes 213 from empirical data by linear inverse modeling (Soetaert et al., 2009), which can also be used for 214 uncertainty analyses of ENA (Kones et al., 2009). There are a wealth of additional R package that 215 network ecologists may find useful including bipartite (Dormann et al., 2008), vegan (Dixon, 2003), Cheddar (Hudson et al., 2013), and packages in the statnet family (Handcock et al., 2008).

²¹⁸ 4 Conclusion and Future Development

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ENA software and facilitate wide development and use. It does this by (1) providing greater 220 accessibility to the code (e.g., free and open source software available on multiple OS), (2) collecting 221 a broad set of available ENA algorithms and workflow management functions, and (3) creating the 222 potential for collaborative development (via GitHub and CRAN). Further, the software is extensible for individual needs and it lets users integrate ENA into a broader workflow in R in a way that 224 is not possible in web based tools like EcoNet (Kazanci, 2007; Schramski et al., 2011). Finally, it 225 lets users have access to other network and statistical analysis tools (e.g., social network analysis) 226 that are already part of R. These benefits come at the cost of having a steeper learning curve (e.g., users must know R), which may make enaR more suited to advanced practitioners. 228 In the near future, we anticipate two initial lines of continued development for the enaR package. 229 The first is to increase the connections between the enaR package and other modeling and analytical tools. For example, we are currently working with colleagues to enable users of Ecopath with Ecosim 231 (Christensen & Walters, 2004) to apply the enaR tools in a seamless way. We are also developing 232 functions to connect between enaR and the R limSolve package (Soetaert et al., 2009) for creating 233 models using Linear Inverse Modeling and to enable uncertainty analysis (Kones et al., 2009). The second line of development is to extend the package's capabilities. While it currently contains 235 most of the many commonly used ENA algorithms used by ecologists, it is far from complete. For 236 example, Ulanowicz's (1983) decomposition of cycles is not yet included nor is his construction 237 for the Lindeman trophic spine (Ulanowicz & Kemp, 1979). Network model construction tools, such as least-inference methods for building models from empirical data (Ulanowicz & Scharler, 239 2008) and Fath's (2004) algorithm for constructing plausible ecosystems models are also possible 240 enhancments.

The enaR package encodes exiting ENA algorithms, and is designed to address limitations of current

In conclusion, enaR is an R package intended to facilitate the use and the collaborative development of Ecosystem Network Analysis, a branch of field of Network Ecology. This domain is rapidly
growing in part because the tools and techniques let ecologists address a wide range of relational
questions at the core of ecology. We look forward to seeing new ecological discoveries made through
the use of enaR.

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6 Tables

Table 1: Selected data input, management, and export functions in enaR.

Function	Description	Example Reference			
pack	This function lets the user combine model elements into a network data object	none			
unpack	Extracts the invidual model elements (e.g., flows, inputs, outputs) from the network data object	none			
read.scor	Creates a network data object from a SCOR formatted data file	Ulanowicz & Kay (1991)			
read.wand	Creates a network data object from a WAND formatted data file	Allesina & Bondavalli (2004)			
ssCheck	Checks to see if the model is at steady-state				
balance	Applies one of four balancing algorithms to a model not at steady-state	Allesina & Bondavalli (2003)			
force.balance	Runs balancing algorithm as many times as necessary to balance the model				
write.nea	Writes the model data to the file format used as input for NEA.m	Fath & Borrett (2006)			

Table 2: Ecosystem Network Analysis functions in ${\tt enaR}.$

Function	Description	Example Reference		
enaStructure	ENA Structural analysis returns the adjacency matrix and multiple common descriptive statistics (e.g., number of nodes, connectance, pathway proliferation rate)	Borrett <i>et al.</i> (2007)		
enaFlow	Calculates node throughflow and input and output oriented direct and integral flow intensity matrices. It also returns multiple whole network descriptive statistics including Total System Throughflow, Finn Cycling Index, and Average Path Length	Finn (1976)		
enaAscendency	Performs ascendency analysis on the model flows and returns whole-network statistics including the average mutual information, Ascendency, Capacity, and Overhead.	Ulanowicz (1997)		
enaStorage	ENA Storage analysis considers how the model fluxes generate the node storage (e.g., biomass) in the system. This function returns the input and output oriented direct and integral storage matrices.	Matis & Patten (1981)		
enaUtility	ENA Utility analysis investigates the direct relation- ships among the network nodes as well as the integral relationships when all of the indirect interactions are also considered.	Patten (1991)		
enaMTI	Mixed Trophic Impacts assesses the net relationships among species in a food web.	Ulanowicz & Puccia (1990)		
enaControl	Control analysis determines the relative control one node exerts on another through the transaction net- work.	Dame & Patten (1981)		
enaEnviron	Returns the n unit and n realized input and output environs of the model.	Patten (1978)		

Table 3: Selected ${\tt enaRauxiliary}$ functions and analyses.

Function	Description	Example Reference					
Specialty Analyses							
enaAll	Runs all of the primary ENA algorithms						
get.ns	Returns the whole-network statistics from enaStruc-						
	ture, enaFlow, enaAscendency, enaStorage, and enaU-						
	tility						
eigenCentrality	Calculates the average eigenvalue centrality for any						
	input matrix						
environCentrality	Returns the input, output, and average environ cen-	Fann & Borrett (2012)					
	tralities for a matrix						
TET	Returns the total environ throughflows	Whipple $et \ al. \ (2007)$					
TES	Returns the total enivron storages	Matis & Patten (1981)					
Auxiliary Functions							
get.orient	Determine the orientation of the results (row-to-						
	column vs. School)						
set.orient	Set the orientation of the results (row-to-column vs.						
	School)						
mExp	This function les users calculate matrix exponents.						

Table 4: Example code for applying enaR Flow analysis to Dame & Patten's (1981) oyster reef model.

```
library(enaR)
                # load enaR package
> # -- ENTER MODEL DATA -- from Dame and Patten (1981)
> # node names
> names <- c("Filter Feeders", "Microbiota", "Meiofauna",</pre>
                        "Deposit Feeders", "Predators", "Deposited Detritus")
> # Internal Flows of model, as matrix (oriented row to column)
+
                 0, 0, 8.1721, 0, 1.2060, 0, 0, 0, 7.2745,
                 0, 1.2060, 0.6609, 0, 0, 0.6431, 0.5135, 0, 0,
                 0.1721, 0, 0, 15.7910, 0, 4.2403, 1.9076, 0.3262, 0),
             ncol=6)
> rownames(F) <- names # add node names to rows
> colnames(F) <- names # add node names to cols
> # boundary flows
> inputs <- c(41.47,0, 0, 0, 0, 0)
> outputs <- c(25.1650, 5.76, 3.5794, 0.4303, 0.3594, 6.1759)
> # Living
> Living <- c(TRUE, TRUE, TRUE, TRUE, TRUE, FALSE)
> # pack the model data into the R network data object
> m <- pack(flow=F,input=inputs, respiration=outputs, outputs=outputs, living=Living);</pre>
> ssCheck(m)
                            # check to see if the model is at steady-state
[1] TRUE
> # perform flow analysis
> F <- enaFlow(m)
                                # perform ENA flow analysis
> attributes(F)
                                 # show analysis objects created
$names
[1] "T" "G" "GP" "N" "NP" "ns"
> F$ns
                                # show flow analysis network statistics
                                          FCT
                                APL
                                                    BFI
                                                              DFT
    Boundary
                  TST TSTp
       41.47 83.5833
                       NA 2.015512 0.1101686 0.4961517 0.1950689 0.3087794
[1,]
                                            HMG.O AMP.I AMP.O modeO.F mode1.F
         ID.F
                ID.F.I
                        ID.F.O
                                   HMG.I
[1,] 1.582925 1.716607 1.534181 2.051826 1.891638
                                                     3
                                                            1
                                                               41.47 32.90504
      mode2.F mode3.F mode4.F
[1,] 9.208256 32.90504
> F$T
   Filter Feeders
                          Microbiota
                                               Meiofauna
                                                            Deposit Feeders
           41.4700
                                                  8.4805
                                                                     2.5100
                               8.1721
        Predators Deposited Detritus
            0.6856
                              22.2651
```

7 Figures

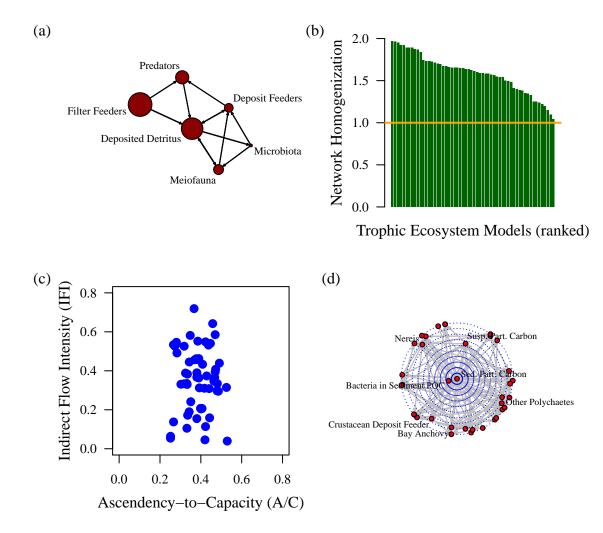


Figure 1: Example of analysis and visualizations created with enaR (a) network digraph of the internal flows of an oyster reef ecosystem model (Dame & Patten, 1981), (b) network homogenization statistic for 56 trophic ecosystem models (rank-ordered), (c) scatter plot showing the relationship between the ascendency-to-capacity ratio and the indirect flow index for the 56 trophic ecosystem models included in the package, and (d) target plot of the betweenness centrality from social network analysis calculated for the xx nodes of the Chesapeake Bay ecosystem model (Baird & Ulanowicz, 199).

Statistic	Min	Distribution	Max	Median	Mean	CV
n	4	L	125	15	26.66	1.02
C	0.05	أحلحت	0.45	0.22	0.25	0.51
LD	1		16.91	3.14	4.58	0.89
lam1A	0		14.17	3.27	4.27	0.76
FCI	0		0.98	0.26	0.38	0.86
APL	1.37	L	186.25	3.67	20	1.91
IFI	0.04	أسريفيا	0.99	0.53	0.56	0.52
HMG.O	1.04	_	13.07	1.78	2.3	0.83
AMP.O	0	L	323	6.5	19.77	1.91
AMI	1	44.44	2.25	1.57	1.58	0.21
ASC.CAP	0.25	بطاقات	0.75	0.39	0.42	0.28
synergism.F	2.41		60.51	3.95	5.69	1.1
mutualism.F	0.6		4	1.16	1.43	0.5

Figure 2: Distributions of selected ENA network statistics from the 100 empirically-based ecosystem models included in enaR. The results are summarized using a histogram showing the distribution of the values of each network statistic between the observed minimum and maximum values. The median, mean, and coefficient of variation (ratio of standard deviation and mean) values are also reported. The network statistics are the number of nodes (n), the connectance $(C = L/n^2)$, link density (LD = L/n), pathway proliferation rate (lam1A), Finn cycling index (FCI), average path length (APL), indirect flow intensity (IFI), output oriented network homogenization ratio (HMG.O), output-oriented network amplification ratio (AMP.O), average mutual information (AMI), the ascendency-to-capacity ratio (ASC.CAP), flow-based network synergism (synergism.F) and mutualism (mutualism.F).