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enaR: Ecosystem Network Analysis with R

Matthew K. Lau
Harvard Forest
Harvard University

Stuart R. Borrett
Department of Biology and Marine Biology
University of North Carolina Wilmington

Pawandeep Singh
Department of Biology and Marine Biology
University of North Carolina Wilmington

and

Duke Network Analysis Center
Social Science Research Institute
Duke University

Abstract

Ecosystem Network Analysis (ENA) provides a framework for investigating the structure, function and dynamics of ecological systems, primarily ecosystem models with physically conserved units. We present the *enaR* package, which provides a broad representation of many of the core tools developed by the ENA community, detailing how to use the primary functions of the package for the analysis of single models or simultaneous, synthetic analysis of multiple ecosystem models.

Keywords: ecology, ENA, ecosystems, species interactions, networks, R.

1. Introduction

Network models have provided an in-road to a variety of complex systems Watts and Strogatz (1998); Newman (2001); Barabási (2012); Newman, Barabási, and Watts (2006); Wasserman and Faust (1994), and although the network approach has deep roots (get old cite from Mutualistic Networks Book), its use has been expanding rapidly in a variety of disciplines including ecology (Borrett, Moody, and Edelmann, 2014; Ings, Montoya, Bascompte, Blüthgen, Brown, Dormann, Edwards, Figueroa, Jacob, Jones, Lauridsen, Ledger, Lewis, Olesen, van Veen, Warren, and Woodward, 2009). This is due in part to the flexibility of the core representation, its utility in answering relational questions, and its applicability to "Big Data" problems. Some scientists are working to build a science of networks (National Research Council, Committee on Network Science for Army Applications, 2006; Brandes, Robins, McCranie, and Wasserman, 2013).

Ecosystem ecologists have developed and used network modeling and analysis for several decades (Borrett, Christian, and Ulanowicz, 2012; Ulanowicz, 1986; Fath and Patten, 1999). From this work, a family of algorithms used to investigate the structure and function of ecological systems has been termed Ecosystem Network Analysis (ENA). For this approach the network models are comprised of transfers of thermodynamically conserved energy or matter (represented by weighted, directed graph edges) between nodes that represent species, groups of species, or non-living components (e.g., dead organic matter) of the ecosystem. The analysis has been used in a variety of ways, including to show the relative importance of indirect effects in ecosystems (Patten, 1983; Higashi and Patten, 1989; Salas and Borrett, 2011) and their capacity to effectively transform the relations among organisms (Ulanowicz and Puccia, 1990; Patten, 1991; Fath and Patten, 1998; Bondavalli and Ulanowicz, 1999). From these applications a new theoretical understanding of ecosystems has emerged (Higashi and Burns, 1991; Belgrano, Scharler, Dunne, and Ulanowicz, 2005; Jørgensen, Fath, Bastianoni, Marques, Müller, Nielsen, Patten, Tiezzi, and Ulanowicz, 2007). Recently, scientists have been applying these methods to understand trophic dynamics in the Sylt-Rømø Bight (Baird, Asmus, and Asmus, 2004a, 2008), biogeochemical cycling in estuaries (Christian and Thomas, 2003; Hines, Lisa, Song, Tobias, and Borrett, 2012), and urban sustainability (Zhang, Yang, and Fath, 2010; Chen and Chen, 2012).

The ENA methodology is an application and extension of economic Input–Output Analysis (Leontief, 1936, 1966) that was first introduced into ecology by Hannon (1973). Since this introduction, two major schools have developed in ENA (Scharler and Fath, 2009). The first is based on Dr. Robert E. Ulanowicz's work with a strong focus on trophic dynamics and a use of information theory (Ulanowicz, 1986, 1997, 2004). The second school has an environment focus and is built on the environ concept introduced by Dr. Bernard C. Patten (Patten, Bosserman, Finn, and Cale, 1976; Patten, 1978; Fath and Patten, 1999). Patten's approach has been collectively referred to separately as *Network Environ Analysis*. At the core the two approaches are very similar; however, they make some different starting assumptions and follow independent yet braided development tracks. One example difference that has historically inhibited collaboration and applications is that the two schools orient their analytical matrices in different ways. The Ulanowicz school orients their matrices as flows from rows-to-columns, which is the most common orientation in the broader field of network science (e.g., Brandes and Erlebach, 2005). In contrast, the Patten School has historically oriented their matricies from column-to-row. Recent research has started to bring the work of the two schools back together (e.g., Scharler and Fath, 2009); we hope this software contributes to this.

Disparate software packages have been created to support ENA. Initially algorithms were developed and distributed as the DOS based NETWRK4 Ulanowicz and Kay (1991), which is still available from `http://www.cbl.umces.edu/~ulan/ntwk/network.html`. Some of these algorithms were re-implemented in an Microsoft Excel based toolbox, WAND Allesina and Bondavalli (2004). The popular Ecopath with Ecosim software that assists with model construction (Christensen and Walters, 2004) also provides multiple ENA algorithms. The algorithms for flow analysis – one component of ENA – were collected into a stand-alone software tool (Latham II, 2006). Fath and Borrett (2006) published NEA.m that collects most of the Patten School ENA algorithms together in a single MATLAB©function. Similarly, the online package by EcoNet (Kazanci 2007) has also made many of the core ENA algorithms available in an easy access framework. Although these packages collectively provide access to a large set of powerful analytical tools, the fragmented distribution of these algorithms has inhibited

the development of theory and the further implementation of important algorithms.

The *enaR* package brings together ENA algorithms into one common software framework that is readily available and extensible. The package is written in the **R** language, which is free and open-source. Due largely to this, **R** is now one of the most widely used analytical programming languages in the biological sciences. *enaR* builds on existing **R** packages for network analysis. For example, it uses the *network* data structure developed by Butts (2008a) and the network analysis tools built into the *network*, *sna* (social network analysis) (Butts, 2008b), and other packages collectively called *statnet* (Handcock, Hunter, Butts, Goodreau, and Morris, 2008). In this article we introduce the user to ENA concepts and algorithms, provide description of how to input ecosystem network models and give detailed description of how to conduct these analyses using *enaR*.

2. Getting Started

In this section we describe the data necessary for the Ecosystem Network Analysis and show how to build the central network data object in **R** that contains the model data for subsequent analysis. To start, the current stable version can be installed from CRAN:

```
> install.packages('enaR')
```

The beta version can be installed from GitHub:

```
> library(devtools)
> install_github('SEELab/enaR',ref='beta')
```

You can now load the package:

```
> library(enaR)
```

2.1. Ecosystem Network Model

ENA is applied to a network model of energy–matter exchanges among system components. The system is modeled as a set of n compartments or nodes that represent species, species-complexes (i.e., trophic guilds or functional groups), or non-living components of the system in which energy–matter is stored. Nodes are connected by L observed fluxes, termed directed edges or links. This analysis requires an estimate of the energy–matter flowing from node i to j over a given period, $\mathbf{F}_{n\times n} = [f_{ij}]$, $i, j = 1, 2, \ldots, n$. These fluxes can be generated by any process such as feeding (like a food web), excretion, and death. As ecosystems are thermodynamically open, there must also be energy or matter inputs into the system $\mathbf{z}_{1\times n} = [z_i]$, and output losses from the system $\mathbf{y}_{1\times n} = [y_i]$. While the Patten School treats all outputs the same, the Ulanowicz School typically partitions outputs into respiration $\mathbf{r}_{1\times n} = [r_i]$ and export $\mathbf{e}_{1\times n} = [e_i]$ to account for differences in energetic quality. Note that $y_i = r_i + e_i, \forall i$. Some analyses also require the amount of energy–matter stored in each node (e.g., biomass), $\mathbf{X}_{1\times n} = [x_i]$. The final required information is a categorization of each node as living or not, which is essential for algorithms from the Ulanowicz School. For our implementation, we have

created a logical vector $\mathbf{Living}_{1\times n}$ that indicates whether the i^{th} node is living (TRUE) or not (FALSE). Together, the model data $\mathcal{M}$ can be summarized as $\mathcal{M} = \{\mathbf{F}, \mathbf{z}, \mathbf{e}, \mathbf{r}, \mathbf{X}, \mathbf{Living}\}$.

Notice the row-to-column orientation of **F**. This is consistent with the Ulanowicz School of network analysis, as well as the orientation commonly used in Social Network Analysis and used in the *statnet* packages. However, this is the opposite orientation typically used in the Patten School of analysis that conceptually builds from a system of differential equations and thus uses the column-to-row orientation common in this area of mathematics. Even though the difference is only a matrix transpose, this single difference may be the source of much confusion in the literature and frustration on the part of users. We have selected to use row-to-column orientation for our primary data structure, as it is the dominant form across network analytics as evidenced by it use in the *statnet* packages. The package algorithms also return the results in the row-to-column orientation by default; however, we have built in functionality with `get.orient` and `set.orient` that allows users to return output in the Patten School row-to-column orientation (see Section 3.13 for details).

There are multiple methods for constructing ecosystem network models and tools for assisting with this process (Fath, Scharler, Ulanowicz, and Hannon, 2007). One approach is to construct a dynamic, processes-based, mathematical model of the system typically using ordinary differential equations. For example, the EcoPath with EcoSim (Christensen and Pauly, 1992; Christensen, 1995) software assists scientists with constructing food-web focused ecosystem models using an underlying bioenergetic approach. Alternatively, Ulanowicz (1986) has called for a more phenomenologial approach to the model construction. This modeling process starts with a conceptual network model of the system and then the node and edge weights are estimated directly from observations. Its phenomenologial in the sense that it focuses on what the flows are, rather than the forms of the mechanistic processes that generate the flows. As this approach is essentially an inverse problem, some have developed inverse linear modeling methods to assist with infering the network weights from data (Vézina and Platt, 1988; van Oevelen, Van den Meersche, Meysman, Soetaert, Middelburg, and Vézina, 2010). The *limSolve* **R**pacakge can assist with this modeling approach (Soetaert, Van den Meersche, and van Oevelen, 2009). Ulanowicz and Scharler (2008) also introduced two least-inference algorithms to assist with this kind of model constuction. These methods focus on constructing models to represent specific empirical systems. Algorithms also exist for constructing simulated ecosystems, including fath04 Cyber Models that use a community assembly type approach. Today, the *enaR* software focuses on the network analysis and assumes that the user has a network model to be analyzed.

2.2. Network Data Class

The *enaR* package stores the model data in the **network** class defined in the *network* package (see Butts, 2008a, for details). In this software, a complete ecosystem network model description includes:

F is the flow matrix, oriented row-to-column

z a vector of inputs

r a vector of respirations

e a vector of exports

y a vector of outputs, which are respirations plus exports

X a vector ofbiomass or storage values

Living = logical vector indicating if the node is living (TRUE) or non-living (FALSE)

2.3. Building a Network Object

Users can assemble the necessary data elements and then use the `pack` function to create the network data object. Here is an example of doing this with hypothetical data.

```
> ## Generate the flow matrix
> flow.mat <- array(abs(rnorm(100,4,2))*sample(c(0,1),100,replace=TRUE),
+                   dim=c(4,4))
> ## Name the nodes
> rownames(flow.mat) <- colnames(flow.mat) <- paste('node',(1:nrow(flow.mat)),sep='')
> ## Generate the inputs
> inputs <- runif(nrow(flow.mat),0,4)
> ## Generate the exports
> exports <- inputs
> ## "Pack" the model into a network object
> fake.model <- pack(flow=flow.mat,
+                    input=inputs,
+                    export=exports,
+                    living=TRUE)

[1] "respiration" "storage"

> ## The model network object contents
> fake.model

 Network attributes:
  vertices = 4
  directed = TRUE
  hyper = FALSE
  loops = TRUE
  multiple = FALSE
  bipartite = FALSE
  balanced = FALSE
  total edges= 8
    missing edges= 0
    non-missing edges= 8

 Vertex attribute names:
    export input living output respiration storage vertex.names

 Edge attribute names:
    flow
```

The individual components can be extracted from the data object using the form specified in the *network* package. For example, we can pull out node of vertex attributes as follows:

```
> fake.model%v%'output'

[1] NA NA NA NA

> fake.model%v%'input'

[1] 3.31224122 0.05082792 0.93603094 2.03415858

> fake.model%v%'living'

[1] TRUE TRUE TRUE TRUE
```

The network flows are stored as edge weights in the network object, which lets users fully manipulate the network object with the `network` functions. The flow matrix can be extracted from the object with:

```
> as.matrix(fake.model,attrname="flow")

        node1    node2    node3    node4
node1 0.00000 0.000000 1.896386 4.077463
node2 0.00000 0.000000 7.811643 2.444950
node3 0.00000 0.000000 4.981009 0.000000
node4 3.50226 4.555268 2.485130 0.000000
```

There are times that it is useful to extract all of the ecosystem model data elements from the network data object. This can be accomplished using the `unpack` function. The `unpack` output is as follows:

```
> unpack(fake.model)

$F
        node1    node2    node3    node4
node1 0.00000 0.000000 1.896386 4.077463
node2 0.00000 0.000000 7.811643 2.444950
node3 0.00000 0.000000 4.981009 0.000000
node4 3.50226 4.555268 2.485130 0.000000

$z
[1] 3.31224122 0.05082792 0.93603094 2.03415858

$r
[1] 0 0 0 0
```

```
$e
[1] 3.31224122 0.05082792 0.93603094 2.03415858

$y
[1] NA NA NA NA

$X
[1] NA NA NA NA

$Living
[1] TRUE TRUE TRUE TRUE
```

Note that we did not specify the storage values. In these instances `pack` produces `NA` values. Although the package is designed to help users navigate missing data issues be sure to check that you are providing the appropriate input for a given function. For more information, see the help file for the function in question.

2.4. Model Library

enaR includes a library of 100 empirically-based previously published ecosystem models that can be categorized into two general classes: trophic and biogeochemical cycling (Christian, Fores, Comin, Viaroli, Naldi, and Ferrari, 1996; Baird *et al.*, 2008; Borrett, Whipple, and Patten, 2010; Borrett, Hines, and Carter, 2015). First, 58 of the models are trophically-based models with food webs at their core (Tables 1). Second, there are 42 models are focused on biogeochemical cycling in ecosystems (Table 2). In summary, these models were originally published for a number of different types of ecosystems, though predominantly aquatic, by a number of author teams. Models in the library range in size from 4 nodes to 125 nodes with connectance values ranging from 7% to 45%.

This collection of models overlaps with other extant data sets. For example, twenty-seven of the models (47%) are included in the set of models compiled and distributed by Dr. Ulanowicz (`http://www.cbl.umces.edu/~ulan/ntwk/network.html`). All 50 of the models analyzed by Borrett and Salas (2010) and Salas and Borrett (2011) and the 45 models analyzed in Borrett (2013) are included in this model library.

The trophic models are grouped as the `troModels` object and the biogeochemically-based models are available as the `bgcModels` object. Both data objects return a list of the model network objects. To use these models simply use the **R** *base* `data` function. This will load the models into the working memory as a named list of network objects:

```
> ## Import the model sets
> data(bgcModels)
> data(troModels)
> ## Check the first few model names
> head(names(bgcModels))

[1] "Hubbard Brook (Ca)(Waide)"     "Hardwood Forest, NH (Ca)"
[3] "Duglas Fir Forest, WA (Ca)"    "Duglas Fir Forest, WA (K)"
[5] "Puerto Rican Rain Forest (Ca)" "Puerto Rican Rain Forest (K)"
```

```
> head(names(troModels))

[1] "Marine Coprophagy (oyster)" "Lake Findley "
[3] "Mirror Lake"                "Lake Wingra"
[5] "Marion Lake"                "Cone Springs"

> ## Isolate a single model
> x <- troModels[[1]]
> x <- troModels$"Marine Coprophagy (oyster)"
> ## Check out the model
> summary(x)

Network attributes:
  vertices = 4
  directed = TRUE
  hyper = FALSE
  loops = TRUE
  multiple = FALSE
  bipartite = FALSE
  balanced = TRUE
 total edges = 4
   missing edges = 0
   non-missing edges = 4
 density = 0.25

Vertex attributes:

 export:
   logical valued attribute
   attribute summary:
   Mode    NA's
logical       4

 input:
   numeric valued attribute
   attribute summary:
   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
   0.00    0.00   62.05   94.90  157.00  255.50

 living:
   logical valued attribute
   attribute summary:
   Mode   FALSE    TRUE    NA's
logical       2       2       0

 output:
   numeric valued attribute
```

```
  attribute summary:
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
  6.60   21.67   64.45   94.90  137.70  244.10

 respiration:
  numeric valued attribute
  attribute summary:
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
  6.60   21.67   64.45   94.90  137.70  244.10

 storage:
  numeric valued attribute
  attribute summary:
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
     1       1       1       1       1       1
 vertex.names:
  character valued attribute
  4 valid vertex names

Edge attributes:

 flow:
  numeric valued attribute
  attribute summary:
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
 15.30   20.25   37.40   42.42   59.58   79.60

Network adjacency matrix:
                         SHRIMP BENTHIC ORGANISMS
SHRIMP                        0                 0
BENTHIC ORGANISMS             0                 0
SHRIMP FECES & BACTERIA       0                 1
BENTHIC FECES & BACTERIA      0                 1
                         SHRIMP FECES & BACTERIA
SHRIMP                                         1
BENTHIC ORGANISMS                              0
SHRIMP FECES & BACTERIA                        0
BENTHIC FECES & BACTERIA                       0
                         BENTHIC FECES & BACTERIA
SHRIMP                                          0
BENTHIC ORGANISMS                               1
SHRIMP FECES & BACTERIA                         0
BENTHIC FECES & BACTERIA                        0
```

2.5. Network Visualization

The *enaR* package uses the *network* package plot tools. Here is one example of how to plot a network model. The figure scaling may need to be adjusted depending on computer and devices. Also note that the graph only shows internal system flows.

```
> ## Load data
> data(oyster)
> m <- oyster
> ## Set the random seed to control plot output
> set.seed(2)
> ## Plot network data object (uses plot.network)
> plot(m)
```

We can use the excellent graphics capabilities of **R** to make fancier plot of the same data (Fig. 1(right)).

```
> ## Set colors to use
> my.col <- c('red','yellow',rgb(204,204,153,maxColorValue=255),'grey22')
> ## Extract flow information for later use.
> F <- as.matrix(m,attrname='flow')
> ## Get indices of positive flows
> f <- which(F!=0, arr.ind=T)
> opar <- par(las=1,bg=my.col[4],xpd=TRUE,mai=c(1.02, 0.62, 0.82, 0.42))
> ## Set the random seed to control plot output
> set.seed(2)
> plot(m,
+  ## Scale nodes with storage
+       vertex.cex=log(m%v%'storage'),
+  ## Add node labels
+       label= m%v%'vertex.names',
+       boxed.labels=FALSE,
+       label.cex=0.65,
+  ## Make rounded nodes
+       vertex.sides=45,
+  ## Scale arrows to flow magnitude
+       edge.lwd=log10(abs(F[f])),
+       edge.col=my.col[3],
+       vertex.col=my.col[1],
+       label.col='white',
+       vertex.border = my.col[3],
+       vertex.lty = 1,
+       xlim=c(-4,1),ylim=c(-2,-2))
> ## Lastly, remove changes to the plotting parameters
> rm(opar)
```

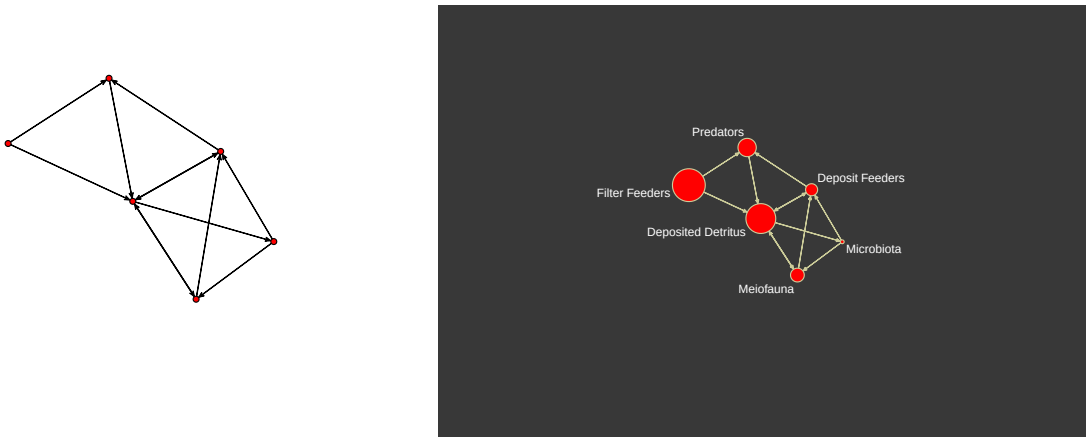

Figure 1: Two networks for the Oyster Reef model (Dame and Patten, 1981) showing a simple (left) and more elaborate (right) implementation of the network plotting function.

2.6. Data Input: Reading Common Data File Formats

Several software packages exist in the literature for running ENA. For convenience, we have written functions to read in a few of the more common data formats used by these software.

SCOR

The `read.scor` function reads in data stored in the SCOR format specified by Ulanowicz and Kay (1991) that is the input to the NETWRK4 programs. This function can be run as follows.

```
> scor.model <- readLines('../../data/oyster.dat')
> m <- read.scor(scor.model,from.file=FALSE)
```

This constructs the network data object from the SCOR file that stores the ecosystem model data for an oyster reef model (Dame and Patten, 1981). The individual model elements are

```
> unpack(m)

$F
                  Filter Feeders Microbiota Meiofauna Deposit Feeders
Filter Feeders                 0     0.0000    0.0000          0.0000
Microbiota                     0     0.0000    1.2060          1.2060
Meiofauna                      0     0.0000    0.0000          0.6609
Deposit Feeders                0     0.0000    0.0000          0.0000
Predators                      0     0.0000    0.0000          0.0000
Deposited Detritus             0     8.1721    7.2745          0.6431
                  Predators Deposited Detritus
Filter Feeders       0.5135            15.7910
Microbiota           0.0000             0.0000
Meiofauna            0.0000             4.2403
```

```
Deposit Feeders       0.1721             1.9076
Predators             0.0000             0.3262
Deposited Detritus    0.0000             0.0000

$z
[1] 41.47  0.00  0.00  0.00  0.00  0.00

$r
[1] 25.1650  5.7600  3.5794  0.4303  0.3594  6.1759

$e
[1] 0 0 0 0 0 0

$y
[1] 25.1650  5.7600  3.5794  0.4303  0.3594  6.1759

$X
[1] 2000.0000    2.4121   24.1210   16.2740   69.2370 1000.0000

$Living
[1]  TRUE  TRUE  TRUE  TRUE  TRUE FALSE
```

This same data is stored as a network data object that is distributed with this package, which can be accessed as:

```
> data(oyster)
> m <- oyster
```

WAND

In part to make ENA more accessible to biologists, Allesina and Bondavalli (2004) recoded some of Ulanowicz's NETWRK4 algorithms into a Microsoft Excel based tool called WAND. For this tool, the model data is stored as a separate Excel file with two worksheets. The first contains many of the node attributes and the second contains the flow matrix. The `read.wand` function will create an **R** network data object from a WAND model file. An example WAND file can be found at `http://people.uncw.edu/borretts/data/MDmar02_WAND.xls`.

```
> m <- read.wand('../../data/MDmar02_WAND.xls')
```

This code creates a network data object for *enaR* from the WAND formatted Mdloti ecosystem model data (Scharler, 2012). This data is courtesy of U.M. Scharler.

NEA

For their Matlab function to perform network environ analysis (Patten School), Fath and Borrett (2006) packaged the model flows, inputs, outputs, and storage values into what they

called a system matrix $\mathrm{S} = \begin{bmatrix} \mathbf{F} & \vec{z} & \vec{X} \\ \vec{y} & 0 & 0 \end{bmatrix}_{(n+1)\times(n+2)}$. Flows in the system matrix are oriented from column to row.

The *enaR* function `read.nea` reads in data with this format stored as a comma separated value file. The function `write.nea()` will write any network model to a CSV file with this format.

While convenient, this data format does not enable inclusion of the full range of model information included in the *enaR* network data object. This format does not partition outputs into exports and respiration values, nor does it identify the node labels are their living status. This missing information will prevent the use of some *enaR* functions.

Here is an example of using these functions:

```
> data(oyster)
> ## Write oyster reef model to a csv file
> write.nea(oyster, file.name="oyster.csv")
```

```
        [,1]  [,2]   [,3]   [,4]   [,5]   [,6]  [,7]      [,8]
[1,]  0.0000 0.000 0.0000 0.0000 0.0000 0.0000 41.47 2000.0000
[2,]  0.0000 0.000 0.0000 0.0000 0.0000 8.1721  0.00    2.4121
[3,]  0.0000 1.206 0.0000 0.0000 0.0000 7.2745  0.00   24.1210
[4,]  0.0000 1.206 0.6609 0.0000 0.0000 0.6431  0.00   16.2740
[5,]  0.5135 0.000 0.0000 0.1721 0.0000 0.0000  0.00   69.2370
[6,] 15.7910 0.000 4.2403 1.9076 0.3262 0.0000  0.00 1000.0000
[7,] 25.1650 5.760 3.5794 0.4303 0.3594 6.1759  0.00    0.0000
```

```
> ## Read in oyster reef model data from NEA.m formatted CSV file
> m <- read.nea("oyster.csv")
```

```
[1] "export" "living"
```

```
>
> ## Again, this model object does NOT contain all
> ## of the information in the "oyster" data object.
```

ENAM

Another commonly used data format stores the necessary model data in a csv or Excel formatted file. We include an example Excel file of the Mdloti estuary stored in this form ("MDMAR02.xlsx", courtesy of U. M. Scharler). This format has not been described technically in the literature nor has it been named. We refer to it as ENAM as it is the ENA model data stored primarily as a square matrix with several preliminary rows that include meta-data, the number of nodes, and number of living nodes (similar to SCOR). The data format is generally similar in concept, if not exact form, to the data system matrix used as the input to the NEA.m function (Fath and Borrett, 2006). However, the ENAM format includes information on whether nodes are living and partitions output into respiration and exports.

Using an example data file, http://people.uncw.edu/borretts/data/MDMAR02.xlsx, this data format can be read into the *enaR* package as:

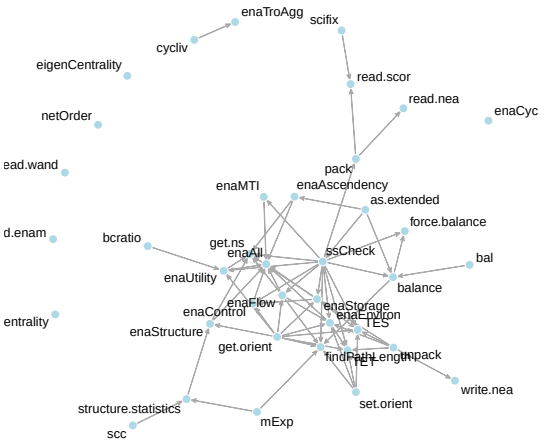

Figure 2: A plot of the *enaR* function relationships. Edges point *from* a function that provides information *to* the function that receives that information.

```
>   m <- read.enam('../../data/MDMAR02.xlsx')
```

The current read.enam function assumes the data are stored on the first worksheet of an Excel file. In the future, we expect to expand this function's capabilities to read the data from a CSV file.

3. Analyzing Ecosystem Models

ENA is often applied to investigate the structure and function of a single ecosystem model. Here, we walk through an example of applying multiple ENA algorithms to the South Carolina oyster reef model (Dame and Patten, 1981). Table 3 summarizes the main ENA algorithms encoded in *enaR*, and Figure 2 illustrates the interdependecy of all of the the functions in the package.

Again, in this package results are reported in the row-to-column orientation by default – including the algorithms from the Patten school. Please see Section 3.13 for how to change this default if needed.

3.1. Balancing for Steady-State

Many of the ENA functions assume that the network model is at steady-state (node inputs equal node outputs). Thus, this package has functions for (1) checking to see if the assumption is met and (2) automatically balancing the model so that input equal outputs.

To determine if the model is balanced and then balance it if necessary:

```
> ## Check to see if the model is balanced
> ssCheck(fake.model)

[1] FALSE

> ## To BALANCE a model if needed
> fake.model <- balance(fake.model,method="AVG2")

[1] AVG2

> ## To FORCE BALANCE a model if needed
> fake.model <- force.balance(fake.model)
```

The automated balancing routines are based on those presented in Allesina and Bondavalli (2003) and include Input, Output, AVG, and AVG2. These authors compare these alternative balancing algorithms and further discuss the implications of using automated procedures. Caution is warranted when using these techniques, as they indiscriminately alter the model flow rates. A more neuanced appraoch may be desired when the uncertainty in estimates of model fluxes are known.

3.2. Structural Network Analysis

Structural network analysis is common to many types of network analysis. The structural analyses applied here are based on those presented in NEA.m (Fath and Borrett, 2006) following the Patten School. Output of the enaStructure function is summarized in Table 4

```
> St <- enaStructure(m)
> attributes(St)

$names
[1] "A"  "ns"

> St$ns

     n  L         C LD      ppr    lam1A mlam1A      rho         R
[1,] 6 12 0.3333333  2 2.147899 2.147899      1 2.147899 0.4655712
            d no.scc no.scc.big      pscc
[1,] 0.147899      2          1 0.8333333
```

The number of nodes, number of links, link density, and connectance (density) are common statistics used to describe networks like food webs (Martinez, 1992; Dunne, Williams, and Martinez, 2002; Eklöf and Ebenman, 2006; Estrada, 2007; Brandes and Erlebach, 2005). The pathway proliferation rate quantifies if and how fast the number of pathways increases with path length in the network (Borrett and Patten, 2003; Borrett *et al.*, 2007). This rate is equivalent to the dominant eigenvalue of the adjacency matrix ($\lambda_1(A)$) if the network is comprised of a single strongly connected component (Borrett *et al.*, 2007).

The structural network statistics for the oyster reef model shows that it has 6 nodes, a pathway proliferation rate of 2.14 (ppr), and that the model is comprised of two strongly connected components (no.scc) but that only one has more than one node (no.scc.big). Thus, 83% of the nodes are participating in a strongly connected component (pscc).

3.3. Flow Analysis

Flow analysis is one of the core ENA analyses for both the Ulanowicz and Patten Schools (Fath and Patten, 1999; Latham II, 2006; Fath and Borrett, 2006; Schramski, Kazanci, and Tollner, 2011). The *enaR* implementation `enaFlow` mostly follows the NEA.m function, with small updates (e.g. calculating the ratio of indirect-to-direct flows Borrett and Freeze, 2011; Borrett, Freeze, and Salas, 2011). Results returned by `enaFlow` are summarized in Table 5

Here, we extract the flow statistics and then isolate and remove the output-oriented direct flow intensity matrix $\mathbf{G}$ matrix. Recall that ENA is partially derived from Input–Output analysis; the input and output orientations provide different information about the system. We also show the input-oriented integral flow matrix $\mathbf{N}'$.

```
> F <- enaFlow(m)
> attributes(F)

$names
[1] "T"  "G"  "GP" "N"  "NP" "ns"

> F$ns

     Boundary     TST TSTp      APL       FCI       BFI       DFI
[1,]    41.47 83.5833   NA 2.015512 0.1101686 0.4961517 0.1950689
          IFI     ID.F   ID.F.I   ID.F.O    HMG.I    HMG.O AMP.I AMP.O
[1,] 0.3087794 1.582925 1.716607 1.534181 2.051826 1.891638     3     1
     mode0.F  mode1.F  mode2.F  mode3.F mode4.F
[1,]   41.47 32.90504 9.208256 32.90504   41.47

> ## Output-oriented direct flow matrix
> G <- F$G
> rm(G)
> ## Input-oriented integral flow matrix
> F$NP

  1         2         3         4         5         6
1 1 1.0000000 1.0000000 1.0000000 1.0000000 1.0000000
2 0 1.1018630 0.2440716 0.6197856 0.1555792 0.1018630
3 0 0.2971032 1.2971032 0.5604100 0.1406747 0.2971032
4 0 0.1240688 0.1240688 1.1240688 0.2821649 0.1240688
5 0 0.0203426 0.0203426 0.0203426 1.0051064 0.0203426
6 0 1.3885039 1.3885039 1.3885039 0.3485436 1.3885039
```

Note that you can use the `attach` function to have access to the objects nested within an object. Since some objects may conflict in name, it's best to `detach` an object once it's not in use.

```
> attach(F)
> G

  1         2         3          4          5         6
1 0 0.0000000 0.0000000 0.00000000 0.01238245 0.3807813
2 0 0.0000000 0.1475753 0.14757529 0.00000000 0.0000000
3 0 0.0000000 0.0000000 0.07793173 0.00000000 0.5000059
4 0 0.0000000 0.0000000 0.00000000 0.06856574 0.7600000
5 0 0.0000000 0.0000000 0.00000000 0.00000000 0.4757876
6 0 0.3670363 0.3267221 0.02888377 0.00000000 0.0000000

> detach(F)
```

Matrix powers – raising a matrix to a power is not a native operation in **R** . Thus, the *enaR* package includes a function `mExp` to facilitate this matrix operation commonly used in ENA.

```
> mExp(F$G,2)

  1         2          3          4           5           6
1 0 0.1397606 0.12440966 0.01099840 0.000000000 0.005891414
2 0 0.0000000 0.00000000 0.01150080 0.010118608 0.185945731
3 0 0.1835203 0.16336297 0.01444205 0.005343446 0.059228112
4 0 0.2789476 0.24830879 0.02195166 0.000000000 0.032622730
5 0 0.1746313 0.15545033 0.01374254 0.000000000 0.000000000
6 0 0.0000000 0.05416549 0.07962750 0.001980437 0.185314635
```

To validly apply flow analysis, the network model must meet two analytical assumptions. First, the model must trace a single, thermodynamically conserved currency, such as energy, carbon, or nitrogen. Second, the model must be at steady-state for many of the analyses.

Flow analysis has been used in a variety of ways. For example, Finn (1980) used ENA flow analysis to compare the cycling of multiple nutrients through the Hubbard Brook Ecosystem, New Hampshire, USA, and van Oevelen, Duineveld, Lavaleye, Mienis, Soetaert, and Heip (2009) used the technique to show how different marine canyon conditions change the flow of carbon through the food webs in Nazaré Canyon. Gattie, Schramski, Borrett, Patten, Bata, and Whipple (2006) applied the analysis to characterize N cycling in the Neuse River Estuary (North Carolina, USA), and Zhang *et al.* (2010) used flow analysis to help assess the sustainability of the urban water metabolism of Beijing, China. Borrett (2013) showed that the throughflow vector T can be considered as a type of centrality measure that indicates the relative importance of each node to the generation of the total system throughflow or activity.

3.4. Ascendency

A key contribution of the Ulanowicz School to ENA is the Ascendency concept and the development of several information based network-level statistics (Ulanowicz, 1986, 1997).

This analysis is based on all of the flows in the system and does not assume the modeled system is at steady-state. The `enaAscendency` function returns several of these information based measures (Table 6). This is run as follows:

```
>   enaAscendency(oyster)

          AMI      ASC       OH      CAP   ASC.CAP    OH.CAP robustness
[1,] 1.330211 166.3473 211.0979 377.4452 0.4407191 0.5592809  0.3611021
         ELD       TD
[1,] 1.79506 2.514395
```

3.5. Storage Analysis

Storage ENA was developed in the Patten School (Barber, 1978b,a). It is similar to flow ENA, but divides the flows by storage (e.g., biomass) instead of throughflow. Several papers provide an overview of this methodology Fath and Patten (1999); Gattie *et al.* (2006); Schramski *et al.* (2011). Output of this function is summarized in Table 7. What follows is an example of applying the storage analysis to the oyster reef model.

```
> S <- enaStorage(m)
> attributes(S)

$names
 [1] "X"  "C"  "P"  "S"  "Q"  "CP" "PP" "SP" "QP" "dt" "ns"

> S$ns

          TSS       CIS         BSI         DSI       ISI     ID.S
[1,] 3112.044 0.9940252 0.003331412 0.003320932 0.9933477 299.1171
      ID.S.I   ID.S.O  HMG.S.O  HMG.S.I NAS NASP mode0.S  mode1.S
[1,] 454.227 294.1527 1.115985 1.464503  20   21 10.3675 8.226261
     mode2.S  mode3.S mode4.S
[1,] 3093.45 8.226261      NA
```

This storage analysis of the oyster reef model indicates that the total energy stored in the system on an average day is 3112 kcal m−2, and that 99.3% of this storage is generated by energy flowing over indirect pathways (ISI).

Whipple, Patten, and Borrett (2014) provides a detailed example of applying storage analysis to characterize the dynamic organization of an ecosystem. They investigated how the storage analysis properties changed across sixteen consecutive seasonal N cycling models of the Neuse River Estuary. They found that from this storage perspective NOx was the dominant compartment, and thus a primary controller of the system dynamics. Note that this work provides an example of applying this analysis at multiple levels of analysis (e.g., Hines and Borrett, 2014).

3.6. Utility Analysis

Utility analysis describes the relationship between node pairs in the ecosystem model when considering both direct and indirect interactions. It developed in the Patten School (Patten, 1991; Fath and Patten, 1999) and is similar to yet distinct from the Ulanowicz School mixed trophic impacts analysis (Ulanowicz and Puccia, 1990). Utility analysis can be conducted from both the flow and storage perspectives, so the "type" argument needs to be set to suit the users needs. This is again implemented as in NEA.m. Table 8 summarizes the function output for the flow and storage versions. These analyses are executed as:

```
> UF <- enaUtility(m,eigen.check=TRUE,type="flow")
> US <- enaUtility(m,eigen.check=TRUE,type="storage")
> attributes(UF)

$names
[1] "D"  "U"  "Y"  "ns"
```

Please note the function argument "eigen.check=TRUE". For this analysis to work, the power series of the direct utility matrices must converge, which is only true if the dominant eigenvalue of the direct utility matrix is less than 1. The function default prevents the analysis from being performed if this condition is not met. Users that wish to perform the analysis anyway can set "eigen.check=FALSE". Care should be used when doing this, as the meaning of the underlying mathematics is uncertain.

3.7. Environ Analysis

Environ Analysis finds the *n unit* input and output environs for the model (Patten, 1978; Fath and Patten, 1999). These unit environs are returned by the *environ* function as in NEA.m. They indicate the flow activity in each subnetwork generated by pulling a unit out of a node (input environs) or pushing a unit into a node (output environ). These unit environs can be converted into "realized" environs by multiplying each by the relevant observed input or output (Borrett and Freeze, 2011; Whipple, Borrett, Patten, Gattie, Schramski, and Bata, 2007; Whipple *et al.*, 2014).

```
> E <- enaEnviron(m)
> attributes(E)

$names
[1] "input"  "output"

> E$output[1]

$`1`
   1          2           3           4           5           6
1 -1  0.0000000  0.00000000  0.00000000  0.012382445  0.380781288
2  0 -0.1970605  0.02908126  0.02908126  0.000000000  0.000000000
3  0  0.0000000 -0.20449723  0.01593682  0.000000000  0.102249819
```

```
4  0  0.0000000  0.00000000 -0.06052568  0.004149988  0.045999518
5  0  0.0000000  0.00000000  0.00000000 -0.016532433  0.007865927
6  0  0.1970605  0.17541596  0.01550760  0.000000000 -0.536896552
z  1  0.0000000  0.00000000  0.00000000  0.000000000  0.000000000
            y
1 0.606836267
2 0.138897999
3 0.086310586
4 0.010376176
5 0.008666506
6 0.148912467
z 0.000000000
```

The `TET` function returns vectors of the unit and realized input and output total environ throughflow. The realized total environ throughflow is an environ based partition of the total system throughflow (Whipple *et al.*, 2007).

```
> tet <- TET(m)
> show(tet)

$realized.input
[1] NA NA NA NA NA NA

$realized.output
[1] 83.5833  0.0000  0.0000  0.0000  0.0000  0.0000

$unit.input
[1] 1.000000 3.931882 4.074090 4.713111 2.932069 2.931882

$unit.output
[1] 2.015512 1.836089 2.540670 3.124836 2.234317 2.594261
```

The `TES` functions returns the both the realized and unit total environ storage for the input and output environs. Again, the realized TES is a partition of the total system storage (TSS).

```
> tes <- TES(m)
> show(tes)

$realized.input
 1  2  3  4  5  6
NA NA NA NA NA NA

$realized.output
[1] 3112.044    0.000    0.000    0.000    0.000    0.000

$unit.input
```

```
          1           2           3           4           5           6
289.3658066   0.6561948   7.3735209  11.5308112 109.7205293 265.1036470

$unit.output
        1         2         3         4         5         6
 75.04326  16.06273  41.03146  65.81279 132.44451  66.11575
```

Realized TET and TES might be considered network centrality measures that indicate the relative importance of the environs in generating the observed flow or storage, respectively.

3.8. Control Analysis

Control analysis was implemented as in the original NEA.m function, but we also include recent updates to control analysis (e.g., Schramski, Gattie, Patten, Borrett, Fath, Thomas, and Whipple, 2006; Schramski, Gattie, Patten, Borrett, Fath, and Whipple, 2007). In general, these analyses determine the pairwise control relationships between the nodes in the network. Table 9 summarizes the function output.

```
> C <- enaControl(m)
> attributes(C)

$names
[1] "CN" "CQ" "CR" "CD" "sc"

> C$sc

          1           2           3           4           5
 0.120569086 -0.063395416 -0.042707703  0.002631762 -0.069124796
          6
 0.052027067
```

The elements of the sc vector indicate the relative control exherted by each node on the system functioning.

3.9. Mixed Trophic Impacts

Mixed Trophic Impacts is a popular analysis from the Ulanowicz School of ENA (Ulanowicz and Puccia, 1990). The `enaMTI` function generates comparable results to the calculations in Ulanowicz and Puccia (1990). These are implemented as follows; Table 10 summarizes the function output.

```
> mti <- enaMTI(oyster)
> attributes(mti)

$names
[1] "G"  "FP" "Q"  "M"
```

```
> mti$M

[1] NA
```

In this case, the power series of the direct trophic impacts matrix does not converge (dominant eigenvalue is greater than one). Thus, the function returns the mti$M = NA. Like with Utility analysis, however, we can use the eigen.check argument to do the calculation despite the mathematical problem.

```
> mti <- enaMTI(oyster,eigen.check=FALSE)
> attributes(mti)

$names
[1] "G"  "FP" "Q"  "M"

> mti$M

                  Filter Feeders  Microbiota    Meiofauna
Filter Feeders      -0.0250635283  0.16956382  0.431493557
Microbiota          -0.0015848556 -0.30675078 -0.182458391
Meiofauna           -0.0001241781 -0.47413204 -0.070959618
Deposit Feeders     -0.0069255188 -0.26769125 -0.007062628
Predators           -0.0301817448  0.02000515 -0.004028911
Deposited Detritus  -0.0034657973  0.21795628  0.612654910
                  Deposit Feeders    Predators Deposited Detritus
Filter Feeders         0.26144106  0.795834137        0.516016759
Microbiota             0.20520368  0.050323410       -0.295378609
Meiofauna              0.01607831  0.003942987       -0.001592286
Deposit Feeders       -0.10329881  0.219903765        0.177109591
Predators             -0.07586335 -0.041648786       -0.019939324
Deposited Detritus     0.44874394  0.110048344       -0.251366300
```

The mixed trophic impacts analysis has been usefully applied to discover interesting and sometimes unexpected ecological relationships. For example, although alligators directly eat frogs in the Florida Everglades (USA), it appears that their net relationship when considering the whole food web is actually mutualistic Bondavalli and Ulanowicz (1999). This is in part because the alligators also eat other key predators of the frogs such as snakes.

3.10. Cycle Analysis

The Cycle Analysis provides the detailed account of the cycling present in the network. It follows the algorithm by the DOS-based NETWRK 4.2b software by Ulanowicz (Ulanowicz and Kay, 1991; Ulanowicz, 1983) and provides results similar to NETWRK's 'Full Cycle Analysis'. Cycles in a network are grouped together into disjoint nexuses and each nexus is characterized by a weak arc. This function gives details of the individual cycles along with the disjoint nexuses present in the network. Table 11 summarizes the function output.

```
>   cyc <- enaCycle(m)
> attributes(cyc)

$names
[1] "Table.cycle"      "Table.nexus"      "CycleDist"
[4] "NormDist"         "ResidualFlows"    "AggregatedCycles"
[7] "ns"

> ## The individual cycles
> names(cyc$Table.cycle)

[1] "CYCLE" "NEXUS" "NODES"

> ## The disjoint nexuses
> names(cyc$Table.nexus)

[1] "NEXUS"      "CYCLES"     "W.arc.From" "W.arc.To"   "W.arc.Flow"
```

3.11. Trophic Aggregations

The Trophic Aggregation algorithm identifies the trophic structure of the given network based on the Lindeman's trophic concepts (Lindeman, 1942). The algorithm is implemented as in NETWRK 4.2b by Ulanowicz (Ulanowicz and Kemp, 1979) and provides similar results as NETWRK's 'Lindeman Trophic Aggregations' (Ulanowicz and Kay, 1991). It apportions the nodes into integer trophic levels and estimates the corresponding inputs, exports, respirations and the grazing chain and trophic spine which represent the transfers between integer trophic levels. This analysis assumes that the ecosystem network model being analyzed represents a food web.

It is crucial for this algorithm that the cycles among the nl living nodes of the network (Feeding Cycles) be removed beforehand to assign trophic levels to nodes. Hence the output for this function contains the Cycle Analysis output for the Feeding cycles in the network.

Following Ulanowicz and Kay (1991), the non-living nodes are grouped together for this analysis and referred to as the detrital pool.

Table 12 summarizes the function output except the outputs for the feeding cycles which are similar to the enaCycle outputs.

```
> trop <- enaTroAgg(m)
> attributes(trop)

$names
 [1] "Feeding_Cycles" "A"              "ETL"            "CE"
 [5] "CR"             "GC"             "RDP"            "LS"
 [9] "TE"             "ns"

> ## Cycle analysis output for Feeding Cycles
> trop$Feeding_Cycles
```

```
$ResidualFlows
                Filter Feeders Microbiota Meiofauna Deposit Feeders
Filter Feeders               0          0     0.000          0.0000
Microbiota                   0          0     1.206          1.2060
Meiofauna                    0          0     0.000          0.6609
Deposit Feeders              0          0     0.000          0.0000
Predators                    0          0     0.000          0.0000
                Predators
Filter Feeders     0.5135
Microbiota         0.0000
Meiofauna          0.0000
Deposit Feeders    0.1721
Predators          0.0000
```

3.12. Other Analyses

There are a number of additional tools in the package. Here selected a subset of these to highlight.

Quickly Return Multiple Analyses

There are two functions that aggregate multiple analyses and report selected results. A quick way to get a list of the global network statistics reported in Structure, Flow, Ascendency, Storage, and Utility analysis is to use the `get.ns` function.

```
> ns <- get.ns(m)
> ## Examine the structure of ns
> str(ns)

'data.frame':        1 obs. of  65 variables:
 $ n          : num 6
 $ L          : num 12
 $ C          : num 0.333
 $ LD         : num 2
 $ ppr        : num 2.15
 $ lam1A      : num 2.15
 $ mlam1A     : num 1
 $ rho        : num 2.15
 $ R          : num 0.466
 $ d          : num 0.148
 $ no.scc     : num 2
 $ no.scc.big : num 1
 $ pscc       : num 0.833
 $ Boundary   : num 41.5
 $ TST        : num 83.6
 $ TSTp       : num 125
 $ APL        : num 2.02
```

```
$ FCI         : num 0.11
$ BFI         : num 0.496
$ DFI         : num 0.195
$ IFI         : num 0.309
$ ID.F        : num 1.58
$ ID.F.I      : num 1.72
$ ID.F.O      : num 1.53
$ HMG.I       : num 2.05
$ HMG.O       : num 1.89
$ AMP.I       : num 3
$ AMP.O       : num 1
$ mode0.F     : num 41.5
$ mode1.F     : num 32.9
$ mode2.F     : num 9.21
$ mode3.F     : num 32.9
$ mode4.F     : num 41.5
$ AMI         : num 1.33
$ ASC         : num 166
$ OH          : num 211
$ CAP         : num 377
$ ASC.CAP     : num 0.441
$ OH.CAP      : num 0.559
$ robustness  : num 0.361
$ ELD         : num 1.8
$ TD          : num 2.51
$ TSS         : num 3112
$ CIS         : num 0.994
$ BSI         : num 0.00333
$ DSI         : num 0.00332
$ ISI         : num 0.993
$ ID.S        : num 299
$ ID.S.I      : num 454
$ ID.S.O      : num 294
$ HMG.S.O     : num 1.12
$ HMG.S.I     : num 1.46
$ NAS         : num 20
$ NASP        : num 21
$ mode0.S     : num 10.4
$ mode1.S     : num 8.23
$ mode2.S     : num 3093
$ mode3.S     : num 8.23
$ mode4.S     : num 10.4
$ lam1D       : num 0.899
$ synergism.F: num 4.92
$ mutualism.F: num 2.27
$ lam1DS      : num 0.302
$ synergism.S: num 13.1
```

```
 $ mutualism.S: num 2.6
```

It is also possible to instantly return all of the main ENA output with `enaAll`:

```
> oyster.ena <- enaAll(oyster)
> names(oyster.ena)
```

```
[1] "ascendency" "control"    "environ"    "flow"       "mti"
[6] "storage"    "structure"  "utility"
```

Centrality

Centrality analysis is a large topic in network science Brandes and Erlebach (2005); Wasserman and Faust (1994). In general the goal is to describe the relative importance of parts of the networks (nodes, edges, environs). Many different types of centrality measures exist in network science Freeman (1979); Freeman, Borgatti, and White (1991); Borgatti and Everett (2006); Brandes and Erlebach (2005). Environ centrality is unique to ENA Fann and Borrett (2012), but like eigenvector centrality, it is a degree-based centrality measure that considers the equilibrium effect of all pathways of all lengths in the system and as such can be classified as a global centrality measure. Both of these centralities can be calculated in *enaR* as follows:

```
> F <- enaFlow(oyster)
> ec <- environCentrality(F$N)
> show(ec)
```

```
$ECin
    Filter Feeders         Microbiota          Meiofauna
         0.1404961          0.1279889          0.1771034
   Deposit Feeders          Predators Deposited Detritus
         0.2178241          0.1557484          0.1808391

$ECout
    Filter Feeders         Microbiota          Meiofauna
        0.06970737         0.19108709         0.20595483
   Deposit Feeders          Predators Deposited Detritus
        0.12350944         0.07903903         0.33070223

$AEC
    Filter Feeders         Microbiota          Meiofauna
         0.1051017          0.1595380          0.1915291
   Deposit Feeders          Predators Deposited Detritus
         0.1706668          0.1173937          0.2557707
```

```
> eigenCentrality(F$G)
```

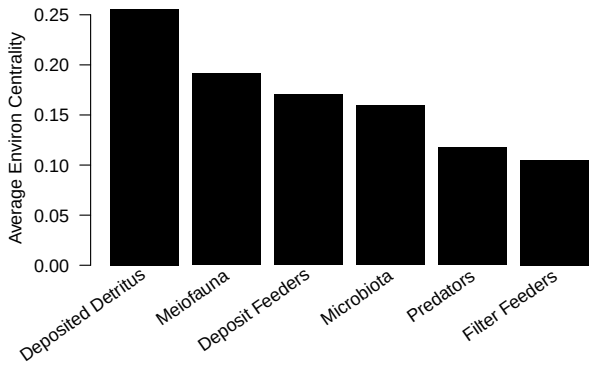

Figure 3: Bar plot of the Oyster Reef model Average Environ Centralities.

```
$EVCin
[1] 0.1207568 0.1093625 0.1876329 0.2518905 0.1470501 0.1833072

$EVCout
[1] 0.00000000 0.23325048 0.26566843 0.11130122 0.01286707 0.37691280

$AEVC
[1] 0.06037842 0.17130647 0.22665067 0.18159586 0.07995858 0.28011000
```

These centrality values have been normalized to sum to one.

Figure 3 shows one way to visualize the Average Environ Centralities.

```
> ## Set plotting parameters
> opar <- par(las=1,mar=c(7,5,1,1),xpd=TRUE,bg="white")
> ## Find centrality order
> o <- order(ec$AEC,decreasing=TRUE)
> ## Creating a barplot
> bp <- barplot(ec$AEC[o],
+               names.arg=NA,
+               ylab="Average Environ Centrality",
+               col="black",border=NA)
> ## Adding labels
> text(bp,-0.008,
+       labels=names(ec$AEC)[o],
+       srt=35,adj=1,cex=1)
> ## Remove the plotting parameters
> rm(opar)
```

As mentioned previously, the throughflow vector from flow analysis, the total environ throughflow, and total environ storage vectors might also be considered centrality metrics.

3.13. Output Orientation

To facilitate package use by the existing ENA community, some of which use the column-to-row orientation (e.g. the Patten School), we have created orientation functions that enable the user to set the expected output orientation for functions written in a particular "school" of analysis. Thus, functions from either school will receive network models with the standard row-to-column, but will return output with flow matrices oriented in the column-to-row orientation when appropriate (i.e. Patten school functions) and return them in that same orientation.

Here is an example of how to use the model orientation functions to re-orient the output from `enaFlow`:

```
> ## Check the current orientation
> get.orient()

[1] "rc"

> ## enaFlow output in row-column
> flow.rc <- enaFlow(oyster)$G
> ## Set the global orientation to school
> set.orient('school')
> ## Check that it worked
> get.orient()

[1] "school"

> ## enaFlow output in column-row
> flow.cr <- enaFlow(oyster)$G
> ## Check. Outputs should be transposed from each other.
> all(flow.rc == flow.cr)

[1] FALSE

> all(flow.rc == t(flow.cr))

[1] TRUE

> ## Now change back to the default orientation ('rc')
> set.orient('rc')
```

4. Multi-Model Analyses (Batch Processing)

While many investigators analyze single models, much of ENA is used to compare ecosystem models (e.g., Baird *et al.*, 1991; van Oevelen, Soetaert, Middelburg, Herman, Moodley, Hamels, Moens, and Heip, 2006; Christian and Thomas, 2003; Niquil, Chaumillon, Johnson,

Bertin, Grami, David, Bacher, Asmus, Baird, and Asmus, 2012; Hines *et al.*, 2015). Investigators have also analyzed large set of models to determine the generality of hypothesized ecosystem properties (e.g., Christensen, 1995; Borrett and Salas, 2010; Salas and Borrett, 2011). For both of these applications, investigators need to analyze multiple models. One advantage of the *enaR* **R** package is that it simplifies this batch processing. Here we illustrate how to batch analyze a selection of models.

Our first step is to build an **R** list data object with ecosystem network models to batch analyze as the elements of the list. To illustrate batch processing, we will use a subset of the trophic models distributed with textitenaR, which are already stored as a list.

```
> data(troModels)
```

Now that we have the models loaded, we can start to manipulate them. The first step is to balance the models. Then we can run the flow analysis. We are using the `lapply` function to apply the analysis across the list of models stored in model.list.

```
> # balance models as necessary
> m.list <- lapply(troModels[1:10],balance)

[1] BALANCED
[1] BALANCED
[1] BALANCED
[1] BALANCED
[1] BALANCED
[1] BALANCED
[1] BALANCED
[1] BALANCED
[1] BALANCED
[1] BALANCED

> # check that models are balanced
> unlist(lapply(m.list,ssCheck))

Marine Coprophagy (oyster)              Lake Findley
                      TRUE                      TRUE
               Mirror Lake               Lake Wingra
                      TRUE                      TRUE
               Marion Lake              Cone Springs
                      TRUE                      TRUE
            Silver Springs           English Channel
                      TRUE                      TRUE
              Oyster Reef               Baie de Somme
                      TRUE                      TRUE

> ## If balancing fails, you can use force.balance
> ## to repeatedly apply the balancing procedure
```

```
> ## although this is not the case with our model set
>
> m.list <- lapply(m.list,force.balance)
> ## Check that all the models are balanced
> all(unlist(lapply(m.list,ssCheck)))

[1] TRUE

> ## Example Flow Analysis
> F.list <- lapply(m.list, enaFlow)
> ## The full results of the flow analysis is now stored in the elements
> ## of the F.list.  To get the results for just the first model:
> F.list[[1]]

$T
                  SHRIMP        BENTHIC ORGANISMS
                   124.1                    323.7
 SHRIMP FECES & BACTERIA BENTHIC FECES & BACTERIA
                    21.9                     79.6

$G
                         SHRIMP BENTHIC ORGANISMS
SHRIMP                        0         0.0000000
BENTHIC ORGANISMS             0         0.0000000
SHRIMP FECES & BACTERIA       0         0.6986301
BENTHIC FECES & BACTERIA      0         0.6645729
                         SHRIMP FECES & BACTERIA
SHRIMP                                 0.1764706
BENTHIC ORGANISMS                      0.0000000
SHRIMP FECES & BACTERIA                0.0000000
BENTHIC FECES & BACTERIA               0.0000000
                         BENTHIC FECES & BACTERIA
SHRIMP                                 0.0000000
BENTHIC ORGANISMS                      0.2459067
SHRIMP FECES & BACTERIA                0.0000000
BENTHIC FECES & BACTERIA               0.0000000

$GP
                         SHRIMP BENTHIC ORGANISMS
SHRIMP                        0        0.00000000
BENTHIC ORGANISMS             0        0.00000000
SHRIMP FECES & BACTERIA       0        0.04726599
BENTHIC FECES & BACTERIA      0        0.16342292
                         SHRIMP FECES & BACTERIA
SHRIMP                                         1
BENTHIC ORGANISMS                              0
SHRIMP FECES & BACTERIA                        0
```

```
BENTHIC FECES & BACTERIA                        0
                        BENTHIC FECES & BACTERIA
SHRIMP                                          0
BENTHIC ORGANISMS                               1
SHRIMP FECES & BACTERIA                         0
BENTHIC FECES & BACTERIA                        0

$N
                        SHRIMP BENTHIC ORGANISMS
SHRIMP                       1         0.1473716
BENTHIC ORGANISMS            0         1.1953471
SHRIMP FECES & BACTERIA      0         0.8351055
BENTHIC FECES & BACTERIA     0         0.7943953
                        SHRIMP FECES & BACTERIA
SHRIMP                                0.1764706
BENTHIC ORGANISMS                     0.0000000
SHRIMP FECES & BACTERIA               1.0000000
BENTHIC FECES & BACTERIA              0.0000000
                        BENTHIC FECES & BACTERIA
SHRIMP                                0.03623966
BENTHIC ORGANISMS                     0.29394387
SHRIMP FECES & BACTERIA               0.20535805
BENTHIC FECES & BACTERIA              1.19534712

$NP
                        SHRIMP BENTHIC ORGANISMS
SHRIMP                       1        0.05649926
BENTHIC ORGANISMS            0        1.19534712
SHRIMP FECES & BACTERIA      0        0.05649926
BENTHIC FECES & BACTERIA     0        0.19534712
                        SHRIMP FECES & BACTERIA
SHRIMP                                        1
BENTHIC ORGANISMS                             0
SHRIMP FECES & BACTERIA                       1
BENTHIC FECES & BACTERIA                      0
                        BENTHIC FECES & BACTERIA
SHRIMP                                0.05649926
BENTHIC ORGANISMS                     1.19534712
SHRIMP FECES & BACTERIA               0.05649926
BENTHIC FECES & BACTERIA              1.19534712

$ns
     Boundary   TST  TSTp     APL       FCI       BFI       DFI
[1,]    379.6 549.3 928.9 1.44705 0.1199863 0.6910614 0.1542493
           IFI     ID.F    ID.F.I    ID.F.O    HMG.I    HMG.O AMP.I
[1,] 0.1546893 1.002852 0.3603839 0.6126851 2.014161 1.891504     1
     AMP.O mode0.F  mode1.F  mode2.F  mode3.F mode4.F
```

```
[1,]     0   379.6 103.7915 65.90846 103.7915   379.6
```

We can use the same technique to extract specific information, like just the ratio of Indirect-to-Direct flow for each model.

```
> ## Example of extracting just specific information - Indirect Effects Ratio
> IDs <- unlist(lapply(m.list, function(x) enaFlow(x)$ns[9]))
> ## Look at the first few ID's
> head(IDs)
```

```
Marine Coprophagy (oyster)              Lake Findley
                  1.002852                  1.723221
              Mirror Lake                Lake Wingra
                  1.861121                  1.861719
              Marion Lake               Cone Springs
                  2.175878                  1.023016
```

We can also collect the set of output-oriented integral flow matrices.

```
> ## Here is a list containing only the
> ## output-oriented integral flow matrices
> N.list <- lapply(m.list,function(x) enaFlow(x)$N)
```

We can also apply the `get.ns` function to extract all of the network statistics for each model. We then use the `do.call` function to reshape the network statistics into a single data frame.

```
> ## Collecting and combining all network statistics
> ns.list <- lapply(m.list,get.ns) # returns as list
> ns <- do.call(rbind,ns.list)  # ns as a data.frame
> ## Let's take a quick look at some of the output
> colnames(ns)    # return network statistic names.
```

```
 [1] "n"           "L"           "C"           "LD"
 [5] "ppr"         "lam1A"       "mlam1A"      "rho"
 [9] "R"           "d"           "no.scc"      "no.scc.big"
[13] "pscc"        "Boundary"    "TST"         "TSTp"
[17] "APL"         "FCI"         "BFI"         "DFI"
[21] "IFI"         "ID.F"        "ID.F.I"      "ID.F.O"
[25] "HMG.I"       "HMG.O"       "AMP.I"       "AMP.O"
[29] "mode0.F"     "mode1.F"     "mode2.F"     "mode3.F"
[33] "mode4.F"     "AMI"         "ASC"         "OH"
[37] "CAP"         "ASC.CAP"     "OH.CAP"      "robustness"
[41] "ELD"         "TD"          "TSS"         "CIS"
[45] "BSI"         "DSI"         "ISI"         "ID.S"
[49] "ID.S.I"      "ID.S.O"      "HMG.S.O"     "HMG.S.I"
[53] "NAS"         "NASP"        "mode0.S"     "mode1.S"
[57] "mode2.S"     "mode3.S"     "mode4.S"     "lam1D"
[61] "synergism.F" "mutualism.F" "lam1DS"      "synergism.S"
[65] "mutualism.S"
```

```
> dim(ns)         # show dimensions of ns matrix

[1] 74 65

> ns[1:5,1:5]     # show selected results

                           n  L     C  LD      ppr
Marine Coprophagy (oyster) 4  4 0.250 1.0 1.000000
Lake Findley               4  6 0.375 1.5 1.004975
Mirror Lake                5  9 0.360 1.8 1.324718
Lake Wingra                5 10 0.400 2.0 2.000000
Marion Lake                5  9 0.360 1.8 1.324718
```

Given this data frame of network statistics, we can construct interesting plots for further analysis. Here we focus on results of the St. Marks Seagrass ecosystem (Baird *et al.*, 1998).

```
> opar <- par(las=1,mar=c(9,7,2,1),xpd=TRUE,mfrow=c(1,2),oma=c(1,1,0,0))
> ## Number of models
> x=dim(ns)[1]
> m.select <- 26:31
> bp=barplot(ns$ID.F[m.select],ylab="Indirect-to-Direct Flow Ratio (I/D, Realized)",
+          col="darkgreen",border=NA,ylim=c(0,2))
> ## Add labels
> text(bp,-0.05,
+       labels=rownames(ns)[m.select],
+         srt=45,adj=1,cex=0.85)
> opar <- par(xpd=FALSE)
> abline(h=1,col="orange",lwd=2)
> #
> plot(ns$FCI,ns$ID.F,pch=20,col="blue",cex=2,
+       ylab="Indirect-to-Direct Flow Ratio (I/D, Realized)",
+       xlab="Finn Cycling Index (FCI)",
+       xlim=c(0,0.8),ylim=c(0,8))
> ## Remove the plotting parameters
> rm(opar)
```

A strength of this software is the ease with which users can apply ENA to multiple models. We expect that this will simplify users analytic workflows and reduce the time required to conduct the work.

5. Connecting to Other Useful Packages

Another advantage of building the *enaR* package in **R** is that it lets ecologists take advantage of other types of network analysis and statistical tools that already exist in **R**. We highlight three examples here.

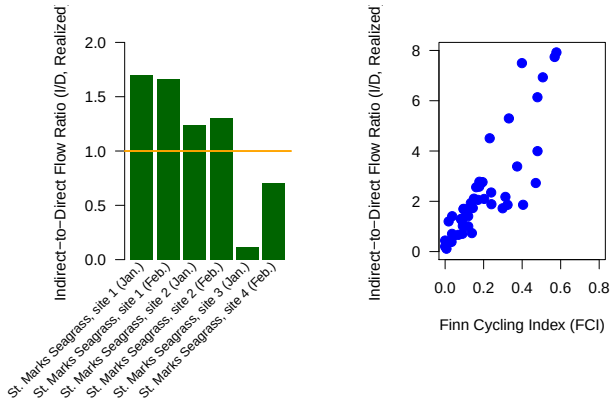

Figure 4: Ratio of Indirect-to-Direct Flow for six ecosystem models (left) and relationship between the Finn Cycling Index and the ratio of Indirect-to-Direct flow in the 74 ecosysetm models.

5.1. network

enaR uses the network data object introduced in the *network* package (Butts, 2008a). One advantage of using this data object is that analysts can then use the tools for network construction and manipulation that are part of the *network* package. For example, *network* can import network models form Pajek project files, which is another widely used network modeling and analysis software Batagelj and Mrvar (2007). The package also includes functions to seamlessly add and delete nodes (edges). It also provides the capability to visualize the network shown previously.

5.2. sna: Social Network Analysis

The *sna* package for Social Network Analysis is bundled in the *statnet* package and uses the same network data object defined in *network*. Thus, the design decision to use the network data object gives users direct access to *sna* tools.

As an example, the *sna* package provides a way of calculating several common centrality measures. Thus, ecologists can now use the *sna* algorithms to determine different types of centrality for their models. This includes betweenness and closeness centrality as follows:

```
> betweenness(oyster)

[1] 0.0 0.0 0.5 3.5 0.0 9.0

> closeness(oyster)

[1] 0.625 0.000 0.000 0.000 0.000 0.000
```

The *sna* package introduced new graphical capabilities as well. For example, it will create a target diagram to visualize the centralities.

```
> m <- m.list[[17]]  # Okefenokee Food Web
> ## Calculate betweenness centrality
> b <- betweenness(m)
> ## Get vertex names
> nms <- m%v%'vertex.names'
> show(nms)

 [1] "Peat decomposers"
 [2] "Detritus decomposers"
 [3] "Nitrogen fixing and nitrifying bacteria"
 [4] "Autotrophic macrophytes"
 [5] "Carnivorous macrophytes"
 [6] "Phytoplankton"
 [7] "Periphyton"
 [8] "Filamentous algae"
 [9] "Herbivorous microinvertebrates"
[10] "Predaceaous microinvertebrates"
[11] "Saprotrophic microinvertebrates"
[12] "Algae-eating macroinvertebrates"
[13] "Macrophyte-eating macroinvertebrates"
[14] "Microinvertebrate-eating macroinvertebrates"
[15] "Macroinvertebrate-eating macroinvertebrates"
[16] "Vertebrate-eating macroinvertebrates"
[17] "Saprotrophic macroinvertebrates"
[18] "Algae-eating vertebrates"
[19] "Macrophyte-eating vertebrates"
[20] "Microinvertebrate-eating vertebrates"
[21] "Macroinvertebrate-eating vertebrates"
[22] "Vertebrate-eating vertebrates"
[23] "Saprotrophic vertebrates"
[24] "Superficial peat"
[25] "Non-peat detritus"
[26] "Nutrients"

> ## Exclude less central node names
> nms[b<=(0.1*max(b))] <- NA
> set.seed(2)
> opar <- par(xpd=TRUE,mfrow=c(1,1))
> ## Create target plot showing only
> ## labels of most central nodes
> gplot.target(m,b,
+              circ.lab=FALSE,
+              edge.col="grey",
+              label=nms)
> ## Remove plot settings
> rm(opar)
```

In addition to the node-level measures, *sna* includes graph-level indices.

```
 [1] "Peat decomposers"
 [2] "Detritus decomposers"
 [3] "Nitrogen fixing and nitrifying bacteria"
 [4] "Autotrophic macrophytes"
 [5] "Carnivorous macrophytes"
 [6] "Phytoplankton"
 [7] "Periphyton"
 [8] "Filamentous algae"
 [9] "Herbivorous microinvertebrates"
[10] "Predaceaous microinvertebrates"
[11] "Saprotrophic microinvertebrates"
[12] "Algae-eating macroinvertebrates"
[13] "Macrophyte-eating macroinvertebrates"
[14] "Microinvertebrate-eating macroinvertebrates"
[15] "Macroinvertebrate-eating macroinvertebrates"
[16] "Vertebrate-eating macroinvertebrates"
[17] "Saprotrophic macroinvertebrates"
[18] "Algae-eating vertebrates"
[19] "Macrophyte-eating vertebrates"
[20] "Microinvertebrate-eating vertebrates"
[21] "Macroinvertebrate-eating vertebrates"
[22] "Vertebrate-eating vertebrates"
[23] "Saprotrophic vertebrates"
[24] "Superficial peat"
[25] "Non-peat detritus"
[26] "Nutrients"
```

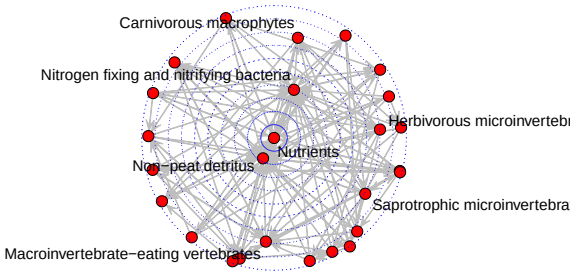

Figure 5: Target plot of node betweenness centrality for the Okefenokee Swamp trophic model.

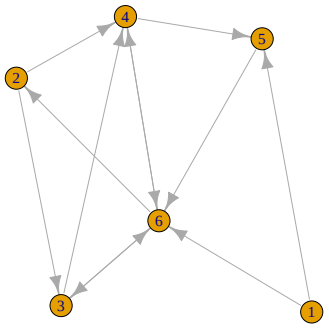

Figure 6: Plot of Oyster reef model using *iGraph*

```
> centralization(oyster, degree)

[1] 0.45

> centralization(oyster,closeness)

[1] 0.75

> centralization(oyster,betweenness)

[1] 0.41
```

5.3. iGraph

The *iGraph* package can also be useful for analyzing network data. Here are a few examples of using the package. Note that some functions in *iGraph* conflict with other functions already defined, so care is required when using *iGraph*.

```
> library(igraph)
> ## The adjacency matrix
> A <- St$A
> ## Creating an iGraph graph
> g <- graph.adjacency(A)
> plot(g)
```

iGraph has a different set of visualization tools and generates a different looking graph (Fig. 6).

```
> ## Betweenness centrality (calculated by iGraph and sna)
> betweenness(g)
```

```
  1   2   3   4   5   6
0.0 0.0 0.5 3.5 0.0 9.0

> ## Shortest path between any two nodes
> shortest.paths(g)

  1 2 3 4 5 6
1 0 2 2 2 1 1
2 2 0 1 1 2 1
3 2 1 0 1 2 1
4 2 1 1 0 1 1
5 1 2 2 1 0 1
6 1 1 1 1 1 0

> ## Average path length in the network (graph theory sense)
> average.path.length(g,directed=TRUE)

[1] 1.52

> ## Diameter of the graph
> diameter(g)

[1] 2

> ## Connectivity of the group and sub-components
> vertex.connectivity(g)  # connectivity of a graph (group cohesion)

[1] 0

> subcomponent(g,1,'in')  # subcomponent reachable from 1 along inputs

+ 1/6 vertex, named:
[1] 1

> subcomponent(g,2,'in')  # subcomponent reachable from 2 along inputs

+ 6/6 vertices, named:
[1] 2 6 1 3 4 5

> subcomponent(g,1,'out') # subcomponent reachable from 1 along outputs

+ 6/6 vertices, named:
[1] 1 5 6 2 3 4

> subcomponent(g,2,'out') # subcomponent reachable from 2 along output
```

```
+ 5/6 vertices, named:
[1] 2 3 4 6 5

> edge.connectivity(g)

[1] 0

> ## Detach igraph package
> detach(package:igraph)
```

5.4. EcoNet

The *EcoNet* software is an online, web-interface that provides a tool box for dynamic modeling and ENA analytics Kazanci (2007). We have provided a write function that enables *enaR* users to output models for easy input into the *EcoNet* interface. The *EcoNet* package and details on the model input syntax can be found at `http://eco.engr.uga.edu`. Here is an example of how to use the `write.EcoNet` function in *enaR* in your current working directory:

```
> data(oyster)
> write.EcoNet(oyster,file='oyster.txt',mn='oyster_model')
```

6. Conclusion

These examples show how to use the key features of the *enaR* package that enables scientists to perform Ecosystem Network Analysis in **R**. The vision for this package is that it provides access to ENA algorithms from both the Ulanowicz and Patten Schools to facilitate theoretical synthesis and broader application. In its current form it replicates, updates, and extends the functionality of the NEA.m function (Fath and Borrett, 2006). Through the connections that *enaR* provides to other **R** packages users can connect to other network analyses provided by packages, such as *sna* and *iGraph*. There are other **R** packages that have graph and network analysis tools, like *Bioconductor*, *WGCNA*, *tnet* and *rmangal*, that might also be useful for ecologists. Our aim is for *enaR* to serve as a nexus for the introduction of analyses from the broader field of network theory into ecology. In addition, we would like to invite users to connect, collaborate and contribute to development of ENA theory and *enaR*. Programmers that are interested can visit `https://github.com/SEELab/enaR_development` for more information on how to contribute to development of the *enaR* package.

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Affiliation:

Matthew K. Lau
Harvard Forest
Harvard University
324 N Main St, Petersham, MA 01366, USA
E-mail: matthewklau@fas.harvard.edu
URL: https://github.com/MKLau

Stuart R. Borrett
Department of Biology and Marine Biology
University of North Carolina Wilmington
601 South College Road, Wilmington, NC 28403, USA
E-mail: borretts@uncw.edu
URL: http://people.uncw.edu/borretts/

Pawandeep Singh
Department of Biology and Marine Biology
University of North Carolina Wilmington
601 South College Road, Wilmington, NC 28403, USA
E-mail: @uncw.edu
URL: http://people.uncw.edu/borretts/

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Table 1: Trophic ecosystem networks (58) included in the *enaR* model library.

Models	Units	$n^{\dagger}$	$C^{\dagger}$	$Input^{\dagger}$	$TST^{\dagger}$	$FCI^{\dagger}$	
Marine Coprophagy (oyster)	kcal m^{-2} yr^{-1}	4	0.25	379	549	0.12	
Lake Findley	gC m^{-2} yr^{-1}	4	0.38	21	50	0.30	
Mirror Lake	gC m^{-2} yr^{-1}	5	0.36	72	217	0.32	
Lake Wingra	gC m^{-2} yr^{-1}	5	0.40	478	1517	0.40	
Marion Lake	gC m^{-2} yr^{-1}	5	0.36	87	242	0.31	
Cone Springs	kcal m^{-2} yr^{-1}	5	0.32	11819	30626	0.09	
Silver Springs	kcal m^{-2} yr^{-1}	5	0.28	21296	29175	0.00	
English Channel	kcal m^{-2} yr^{-1}	6	0.25	1096	2280	0.00	
Oyster Reef	kcal m^{-2} yr^{-1}	6	0.33	41	83	0.11	
Baie de Somme	mgC m^{-2} d^{-1}	9	0.30	876	2034	0.14	
Bothnian Bay	gC m^{-2} yr^{-1}	12	0.22	44	183	0.23	
Bothnian Sea	gC m^{-2} yr^{-1}	12	0.24	117	562	0.31	
Ythan Estuary	gC m^{-2} yr^{-1}	13	0.23	1258	4181	0.24	
Sundarban Mangrove (virgin)	kcal m^{-2} yr^{-1}	14	0.22	111317	440931	0.19	
Sundarban Mangrove (reclaimed)	kcal m^{-2} yr^{-1}	14	0.22	38484	103056	0.05	
Baltic Sea	mg C m^{-2} d^{-1}	15	0.17	603	1973	0.13	
Ems Estuary	mg C m^{-2} d^{-1}	15	0.19	282	1067	0.32	
Swartkops Estuary 15	mg C m^{-2} d^{-1}	15	0.17	3544	13996	0.47	
Southern Benguela Upwelling	mg C m^{-2} d^{-1}	16	0.23	714	2545	0.31	
Peruvian Upwelling	mg C m^{-2} d^{-1}	16	0.22	14927	33491	0.04	
Crystal River (control)	mg C m^{-2} d^{-1}	21	0.19	7357	15062	0.07	
Crystal River (thermal)	mg C m^{-2} d^{-1}	21	0.14	6018	12032	0.09	
Charca de Maspalomas Lagoon	mg C m^{-2} d^{-1}	21	0.12	1486230	6010331	0.18	
Northern Benguela Upwelling	mg C m^{-2} d^{-1}	24	0.21	2282	6611	0.05	
Swartkops Estuary	mg C m^{-2} d^{-1}	25	0.17	2859	8949	0.27	
Sunday Estuary	mg C m^{-2} d^{-1}	25	0.16	4440	11937	0.22	
Kromme Estuary	mg C m^{-2} d^{-1}	25	0.16	2571	11087	0.38	
Okefenokee Swamp	g dw m^{-2} y^{-1}	26	0.20	2533	12855	0.48	
Neuse Estuary (early summer 1997)	mg C m^{-2} d^{-1}	30	0.09	4385	13827	0.12	
Neuse Estuary (late summer 1997)	mg C m^{-2} d^{-1}	30	0.11	4639	13035	0.13	
Neuse Estuary (early summer 1998)	mg C m^{-2} d^{-1}	30	0.09	4568	14025	0.12	
Neuse Estuary (late summer 1998)	mg C m^{-2} d^{-1}	30	0.10	5641	15031	0.11	
Gulf of Maine	g ww m^{-2} yr^{-1}	31	0.35	5053	18381	0.15	Link, Overholtz, O'Reilly, Green, Dow, Pa
Georges Bank	g ww m^{-2} yr^{-1}	31	0.35	4380	16889	0.18	
Middle Atlantic Bight	g ww m^{-2} yr^{-1}	32	0.37	4869	17916	0.18	
Narragansett Bay	mgC m^{-2} yr^{-1}	32	0.15	693845	3917246	0.51	
Southern New England Bight	g ww m^{-2} yr^{-1}	33	0.35	4717	17597	0.16	
Chesapeake Bay	mg C m^{-2} yr^{-1}	36	0.09	888791	3227453	0.19	
Mondego Estuary (*Zostera* sp. Meadows)	g AFDW m^{-2} yr^{-1}	43	0.19	4030	6822	0.03	
St. Marks Seagrass, site 1 (Jan.)	mg C m^{-2} d^{-1}	51	0.08	514	1315	0.13	
St. Marks Seagrass, site 1 (Feb.)	mg C m^{-2} d^{-1}	51	0.08	601	1590	0.11	
St. Marks Seagrass, site 2 (Jan.)	mg C m^{-2} d^{-1}	51	0.07	602	1383	0.09	
St. Marks Seagrass, site 2 (Feb.)	mg C m^{-2} d^{-1}	51	0.08	800	1921	0.08	
St. Marks Seagrass, site 3 (Jan.)	mg C m^{-2} d^{-1}	51	0.05	7809	12651	0.01	
St. Marks Seagrass, site 4 (Feb.)	mg C m^{-2} d^{-1}	51	0.08	1432	2865	0.04	
Sylt-Rømø Bight	mg C m^{-2} d^{-1}	59	0.08	683448	1781028	0.09	
Graminoids (wet)	g C m^{-2} yr^{-1}	66	0.18	6272	13676	0.02	
Graminoids (dry)	g C m^{-2} yr^{-1}	66	0.18	3472	7519	0.04	
Cypress (wet)	g C m^{-2} yr^{-1}	68	0.12	1418	2571	0.04	
Cypress (dry)	g C m^{-2} yr^{-1}	68	0.12	1035	1919	0.04	
Lake Oneida (pre-ZM)	g C m^{-2} yr^{-1}	74	0.22	1034	1697	0.00	
Lake Oneida (post-ZM)	g C m^{-2} yr^{-1}	76	0.22	810	1462	0.00	
Bay of Quinte (pre-ZM)	g C m^{-2} yr^{-1}	74	0.21	984	1509	0.00	
Bay of Quinte (post-ZM)	g C m^{-2} yr^{-1}	80	0.21	1129	2039	0.01	
Mangroves (wet)	g C m^{-2} yr^{-1}	94	0.15	1531	3265	0.10	
Mangroves (dry)	g C m^{-2} yr^{-1}	94	0.15	1531	3272	0.10	
Florida Bay (wet)	mg C m^{-2} yr^{-1}	125	0.12	738	2720	0.14	
Florida Bay (dry)	mg C m^{-2} yr^{-1}	125	0.13	547	1778	0.08	

† n is the number of nodes in the network model, $C = L/n^2$ is the model connectance when L is the number of direct links or energy–matter transfers, $Input = sum z_i$ is the total amount of energy–matter flowing into the system, $TST = \sum\sum f_{ij} + \sum z_i$ is the total system throughflow, and FCI is the Finn Cycling Index (Finn, 1980). Flow based network statistics ($Input$, TST, and FCI) were calculated after models were balanced using the AVG2 algorithm.

Table 2: Biogeochemical ecosystem networks (42) included in the *enaR* model library.

Model	Units	$n^{\dagger}$	$C^{\dagger}$	$Input^{\dagger}$	$TST^{\dagger}$	$FCI^{\dagger}$	Referen
Hubbard Brook (Waide)	kg Ca Ha^{-1} yr^{-1}	4	0.25	11	168	0.76	Waide, Krebs, Clarkson, and Setzler (197
Hardwood Forest, NH	kg Ca Ha^{-1} yr^{-1}	4	0.31	11	200	0.80	Jordan, Kline, and Sasscer (197
Douglas Fir Forest, WA	kg Ca Ha^{-1} yr^{-1}	4	0.31	4	54	0.74	Jordan *et al.* (197
Douglas Fir Forest, WA	kg K Ha^{-1} yr^{-1}	4	0.31	0	45	0.97	Jordan *et al.* (197
Puerto Rican Rain Forest	kg Ca Ha^{-1} yr^{-1}	4	0.31	43	274	0.57	Jordan *et al.* (197
Puerto Rican Rain Forest	kg K Ha^{-1} yr^{-1}	4	0.31	20	433	0.86	Jordan *et al.* (197
Puerto Rican Rain Forest	kg Mg Ha^{-1} yr^{-1}	4	0.31	10	70	0.58	Jordan *et al.* (197
Puerto Rican Rain Forest	kg Cu Ha^{-1} yr^{-1}	4	0.31	0	2	0.37	Jordan *et al.* (197
Puerto Rican Rain Forest	kg Fe Ha^{-1} yr^{-1}	4	0.31	0	7	0.95	Jordan *et al.* (197
Puerto Rican Rain Forest	kg Mn Ha^{-1} yr^{-1}	4	0.38	0	7	0.98	Jordan *et al.* (197
Puerto Rican Rain Forest	kg Na Ha^{-1} yr^{-1}	4	0.31	64	140	0.24	Jordan *et al.* (197
Puerto Rican Rain Forest	kg Sr Ha^{-1} yr^{-1}	4	0.31	0	1	0.71	Jordan *et al.* (197
Tropical Rain Forest	g N m^{-2} d^{-1}	5	0.24	10	71	0.48	Edmisten (197
Neuse River Estuary (AVG)	mmol N m^{-2} $season^{-1}$	7	0.45	795	41517	0.89	Christian and Thomas (200
Neuse River Estuary (Spring 1985)	mmol N m^{-2} $season^{-1}$	7	0.45	133	9120	0.91	Christian and Thomas (200
Neuse River Estuary (Summer 1985)	mmol N m^{-2} $season^{-1}$	7	0.45	119	20182	0.96	Christian and Thomas (200
Neuse River Estuary Fall 1985)	mmol N m^{-2} $season^{-1}$	7	0.45	181	8780	0.88	Christian and Thomas (200
Neuse River Estuary Winter 1986)	mmol N m^{-2} $season^{-1}$	7	0.43	187	6880	0.85	Christian and Thomas (200
Neuse River Estuary (Spring 1986)	mmol N m^{-2} $season^{-1}$	7	0.45	128	12915	0.94	Christian and Thomas (200
Neuse River Estuary (Summer 1986)	mmol N m^{-2} $season^{-1}$	7	0.45	165	11980	0.91	Christian and Thomas (200
Neuse River Estuary (Fall 1986)	mmol N m^{-2} $season^{-1}$	7	0.45	100	9863	0.94	Christian and Thomas (200
Neuse River Estuary (Winter 1987)	mmol N m^{-2} $season^{-1}$	7	0.45	691	7907	0.62	Christian and Thomas (200
Neuse River Estuary (Spring 1987)	mmol N m^{-2} $season^{-1}$	7	0.45	334	11533	0.84	Christian and Thomas (200
Neuse River Estuary (Summer 1987)	mmol N m^{-2} $season^{-1}$	7	0.45	90	15621	0.96	Christian and Thomas (200
Neuse River Estuary (Fall 1987)	mmol N m^{-2} $season^{-1}$	7	0.45	85	7325	0.93	Christian and Thomas (200
Neuse River Estuary (Winter 1988)	mmol N m^{-2} $season^{-1}$	7	0.45	171	8680	0.89	Christian and Thomas (200
Neuse River Estuary (Spring 1988)	mmol N m^{-2} $season^{-1}$	7	0.45	176	6898	0.85	Christian and Thomas (200
Neuse River Estuary (Summer 1988)	mmol N m^{-2} $season^{-1}$	7	0.45	132	16814	0.95	Christian and Thomas (200
Neuse River Estuary (Fall 1988)	mmol N m^{-2} $season^{-1}$	7	0.45	128	5732	0.87	Christian and Thomas (200
Neuse River Estuary (Winter 1989)	mmol N m^{-2} $season^{-1}$	7	0.45	291	5739	0.75	Christian and Thomas (200
Cape Fear River Estuary (Oligohaline)	nmol N cm^{-3} d^{-1}	8	0.36	3802	7088	0.20	Hines *et al.* (201
Cape Fear River Estuary (Polyhaline)	nmol N cm^{-3} d^{-1}	8	0.36	3068	5322	0.17	Hines, Lisa, Song, Tobias, and Borrett (201
Lake Lanier (AVG)	mg P m^{-2} day^{-1}	11	0.21	95	749	0.40	Borrett and Osidele (200
Baltic Sea	mg N m^{-3} day^{-1}	16	0.15	2348	44510	0.67	Hinrichsen and Wulff (199
Chesapeake Bay	mg N m^{-2} yr^{-1}	36	0.12	73430	484325	0.33	Baird, Ulanowicz, and Boynton (199
Chesapeake Bay	mg P m^{-2} yr^{-1}	36	0.12	9402	101091	0.51	Ulanowicz and Baird (199
Chesapeake Bay (Winter)	mg P m^{-2} $season^{-1}$	36	0.08	1009	11926	0.53	Ulanowicz and Baird (199
Chesapeake Bay (Spring)	mg P m^{-2} $season^{-1}$	36	0.10	1932	27325	0.57	Ulanowicz and Baird (199
Chesapeake Bay (Summer)	mg P m^{-2} $season^{-1}$	36	0.12	4184	42935	0.46	Ulanowicz and Baird (199
Chesapeake Bay (Fall)	mg P m^{-2} $season^{-1}$	36	0.10	2276	18904	0.40	Ulanowicz and Baird (199
Sylt-Rømø Bight	mg N m^{-2} yr^{-1}	59	0.09	99613	363693	0.23	Baird *et al.* (200
Sylt-Rømø Bight	mg P m^{-2} yr^{-1}	59	0.09	2508	57739	0.66	Baird *et al.* (200

† n is the number of nodes in the network model, $C = L/n^2$ is the model connectance when L is the number of direct links or energy–matter transfers, $Input = sum z_i$ is the total amount of energy–matter flowing into the system, $TST = \sum\sum f_{ij} + \sum z_i$ is the total system throughflow, and FCI is the Finn Cycling Index (Finn, 1980). Flow based network statistics ($Input$, TST, and FCI) were calculated after models were balanced using the AVG2 algorithm.

Table 3: Primary Ecosystem Network Analysis algorithms in *enaR*.

Analysis	**Function Name**	**School**
Structure	`enaStructure`	foundational, Patten
Flow	`enaFlow`	foundational, Patten
Ascendency	`enaAscendency`	Ulanowicz
Storage	`enaStorage`	Patten
Utility	`enaUtility`	Patten
Mixed Trophic Impacts	`enaMTI`	Ulanowicz
Control	`enaControl`	Patten
Environ	`enaEnviron`	Patten
Cycle Basis	`enaCycle`	Ulanowicz
Canonical Trophic Aggregation	`enaTroAgg`	Ulanowicz

Table 4: Resultant matrices and network statistics returned by the `enaStructure` function in *enaR*.

Label	**Description**
Matrices	
A	$n \times n$ adjacency matrix
Network statistics	
n	number of nodes
L	number of directed edges
C	connectance ($C = L/n^2$); the proportion of possible directed edges connected.
LD	Link Density (L/n)
ppr	estimated rate of pathway proliferation (Borrett and Patten, 2003)
lam1A	dominant eigenvalue of A ($lambda_1(\mathbf{A})$), which is the asymptotic rate of pathway proliferation (Borrett, Fath, and Patten, 2007)
mlam1A	multiplicity of the dominant eigenvalue (number of times repeated)
rho	damping ratio, an indicator of how quickly $[a_{ij}]^{(m)}/[a_{ij}]^{(m-1)}$ goes to $lam_1(\mathbf{A})$ (Caswell, 2001, , p. 95)
R	distance of $lam_1(\mathbf{A})$ from the bulk of the eigen spectrum (Farkas, Derenyi, Barabasi, and Vicsek, 2001)
d	difference between dominant eigenvalue and link density (expected value for random graph)
no.scc	number of strongly connected components (SCC)
no.scc.big	number of SCC with more than one node
pscc	fraction of network nodes included in a big SCC

Table 5: Matrices and network statistics returned by the `enaFlow` function in *enaR*.

***enaR* label**	**Description**
Matrices	
T	$n \times 1$ vector of node throughflows (M L^{-2} or $^{-3}$ T^{-1})
G	output-oriented direct throughflow intensity matrix
GP	input-oriented direct throughflow intensity matrix
N	output-oriented integral throughflow intensity matrix
NP	input-oriented integral throughflow intensity matrix
Network statistics	
Input	Total input boundary flow
TST	Total System ThroughFLOW
TSTp	Total System ThroughPUT
APL	Average Path Length (Finn, 1976)
FCI	Finn Cycling Index (Finn, 1980)
BFI	Boundary Flow Intensity, *Boundary/TST*
DFI	Direct Flow Intensity, *Direct/TST*
IFI	Indirect Flow Intensity, *Indirect/TST* (Borrett, Whipple, Patten, and Christian, 2006)
ID.F	Ratio of Indirect to Direct Flow Borrett and Freeze (2011); Borrett *et al.* (2011)
ID.F.I	input oriented ratio of indirect to direct flow intensity (as in Fath and Borrett, 2006)
IF.F.O	output oriented ratio of indirect to direct flow intensity (as in Fath and Borrett, 2006)
HMG.F.I	input oriented network homogenization to direct flow intensity
HMG.F.O	output oriented network homogenization to direct flow intensity
AMP.F.I	input oriented network amplification
AMP.F.O	output oriented network amplification
mode0.F	Boundary Flow
mode1.F	Internal First Passage Flow
mode2.F	Cycled Flow
mode3.F	Dissipative Equivalent to mode1.F
mode4.F	Dissipative Equivalent to mode0.F

Table 6: Graph-level network statistics returned by the *enaR* `enaAscendency` function (see Ulanowicz, 1986, 1997, for interpretations).

Label	**Description**
AMI	average mutual information (bits)
ASC	ascendency, AMI × TSTp
OH	overhead
CAP	capacity
ASC.CAP	ascendency-to-capacity ratio (dimensionless)
OH.CAP	overhead-to-capacity ratio (dimensionless)
robustness	robustness of the network as in Fath (2014)
ELD	effective link density of the network Ulanowicz, Holt, and Barfield (2014)
TD	trophic depth of the network as in Ulanowicz *et al.* (2014)

Table 7: Matrices and graph-level network statistics returned by the *enaR* `enaStorage` function.

Label	Description
Matrices	
X	$n \times 1$ vector of storage values [M L^{-2}]
C	$n \times n$ donor-storage normalized output-oriented direct flow intensity matrix (T^{-1})
P	$n \times n$ storage-normalized output-oriented direct flow matrix (dimensionless)
S	$n \times n$ donor-storage normalized output-oriented integral flow intensity matrix (T^{-1})
Q	$n \times n$ output-oriented integral flow intensity matrix (dimensionless)
CP	$n \times n$ recipient-storage normalized input-oriented direct flow intensity matrix (T^{-1})
PP	$n \times n$ storage-normalized input-oriented direct flow matrix (dimensionless)
SP	$n \times n$ donor-storage normalized input-oriented integral flow intensity matrix (T^{-1})
QP	$n \times n$ input-oriented integral flow intensity matrix (dimensionless)
dt	discrete time step
Network statistics	
TSS	Total System Storage
CIS	Storage Cycling Index
BSI	Boundary Storage Intensity
DSI	Direct Storage Intensity
ISI	Indirect Storage Intensity
ID.S	Ratio of Indirect-to-Direct storage (realized)
ID.S.I	storage-based input-oriented indirect-to-direct ratio (as in Fath and Borrett, 2006)
ID.S.O	storage-based input-oriented indirect-to-direct ratio (as in Fath and Borrett, 2006)
HMG.S.I	input-oriented storage network homogenization
HMG.S.O	output-oriented storage network homogenization
AMP.S.I	input-oriented storage network amplification
AMP.S.O	output-oriented storage network amplification
mode0.S	Storage from Boundary Flow
mode1.S	Storage from Internal First Passage Flow
mode2.S	Storage from Cycled Flow
mode3.S	Dissipative Equivalent to mode1.S
mode4.S	Dissipative Equivalent to mode0.S

Table 8: Matrices and graph-level network statistics returned by the *enaR* `enaUtility` function.

Label	Description
Matrices	
$D_{n\times n}$	throughflow-normalized direct utility intensity (dimensionless)
$U_{n\times n}$	integral flow utility (dimensionless)
$Y_{n\times n}$	integral flow utility scaled by original throughflow (M $L^{-2 \text{ or } -3}$ T^{-1})
$DS_{n\times n}$	storage-normalized direct utility intensity (dimensionless)
$US_{n\times n}$	integral storage utility (dimensionless)
$YS_{n\times n}$	integral storage utility scaled by original throughflow (M $L^{-2 \text{ or } -3}$ T^{-1})
Network Statistics	
lam1D	dominant eigenvalue of D
synergism.F	benefit-cost ratio or network synergism (flow)
mutualism.F	positive to negative interaction ratio or network mutualism (flow)
lam1DS	dominant eigenvalue of DS
synergism.S	benefit-cost ratio or network synergism (storage)
mutualism.S	positive to negative interaction ratio or network mutualism (storage)

Table 9: Matrices returned by the *enaR* `enaControl` function, which are based on (Dame and Patten, 1981; Patten and Auble, 1981; Schramski *et al.*, 2006, 2007).

Label	Description
Matrices	
$CN_{n\times n}$	Control matrix using flow values
$CQ_{n\times n}$	Control matrix using storage values
$CR_{n\times n}$	Schramski's Control Ratio Matrix
$CD_{n\times n}$	Schramski's Control Difference Matrix
$sc_{n\times 1}$	Schramski's System Control vector

Table 10: Matrices returned by the *enaR* `enaMTI` function, which are based on (Ulanowicz and Puccia, 1990).

Label	Description
Matrices	
$G_{n\times n}$	positive effect of prey on its predator
$F_{n\times n}$	negative impact of the predator on its prey
$Q_{n\times n}$	direct net impact of one node on another
$M_{n\times n}$	total impact of i on j (direct and indirect)

Table 11: Data frames, matrices and graph-level network statistics returned by the *enaR* `enaCycle` function, which is based on (Ulanowicz, 1983).

Label	**Description**
Data frames	
Table.cycle	Data frame of cycles in the network. Up to 50 cycles are returned per nexus.
Table.nexus	Data frame with details of the disjoint nexuses present in the network
Matrices	
$\text{CycleDist}_{n\times 1}$	Vector of flows cycling in loops of increasing length (i.e., 1, 2, ...).
$\text{NormDist}_{n\times 1}$	Vector of Cycle Distributions normalized by the total system throughput
$\text{ResidualFlows}_{n\times n}$	Matrix of straight-through flows or the underlying acyclic graph
$\text{AggregatedCycles}_{n\times n}$	Matrix of all the cycled flows or the underlying cyclic graph
Network Statistics	
NCYCS	Number of cycles detected in the network
NNEX	Number of disjoint nexuses detected in the network
CI	Cycling index of the network based on flow matrix

Table 12: Matrices and graph-level network statistics returned by the *enaR* `enaTroAgg` function, which are based on Ulanowicz and Kemp (1979).

Label	**Description**
Matrices	
$A_{nl \times nl}$	Lindeman transformation matrix that apportions nodes to integer trophic levels
$ETL_{n \times 1}$	Vector of the effective trophic levels of different nodes
$M.Flow_{nl \times 1}$	Migratory flows in living nodes (if present)
$CI_{n \times 1}$	Vector of canonical inputs to integer trophic levels (if migratory flows present)
$CE_{n \times 1}$	Canonical Exports. Vector of exports from Integer trophic levels
$CR_{n \times 1}$	Canonical Respirations. Vector of respiration from Integer trophic levels
$GC_{nl \times 1}$	Grazing Chain. Vector of inputs to Integer trophic levels from preceding level
$RDP_{nl \times 1}$	Vector of returns from each level to the detrital pool
$LS_{nl \times 1}$	Vector representing the Lindeman Spine
$TE_{nl \times 1}$	Vector of the trophic efficiencies for integer trophic levels
Network Statistics	
Detritivory	Flow from the detrital pool (non-living nodes) to the second trophic level
DetritalInput	Exogenous inputs to the detrital pool
DetritalCirc	internal circulation within the detrital pool
NCYCS	number of feeding cycles removed from the network
NNEX	number of disjoint nexuses detected for the feeding cycles
CI	cycling index of the living component of the network based on flow matrix