

SREE VIDYANIKETHAN ENGINEERING COLLEGE

(An Autonomous Institution, Affiliated to JNTUA, Ananthapuramu)

I B.Tech II Semester (SVEC-16) Supplementary Examinations December - 2018**TRANSFORMATION TECHNIQUES AND PARTIAL DIFFERENTIAL EQUATIONS**

[Civil Engineering, Electrical and Electronics Engineering, Mechanical Engineering,
Electronics and Communication Engineering, Computer Science and Engineering,
Electronics and Instrumentation Engineering, Information Technology,
Computer Science and Systems Engineering]

Time: 3 hours

Max. Marks: 70

Answer One Question from each Unit
All questions carry equal marks

UNIT-I

- 1 If $f(x) = \begin{cases} 0, & -\pi \leq x \leq 0 \\ \sin x, & 0 \leq x \leq \pi \end{cases}$ then show that 14 Marks

$$f(x) = \frac{1}{\pi} + \frac{\sin x}{2} - \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{\cos 2nx}{4n^2 - 1}, \text{ and hence establish that}$$

$$\frac{1}{1.3} - \frac{1}{3.5} + \frac{1}{5.7} - \dots = \frac{1}{4}(\pi - 2).$$

(OR)

- 2 Write Fourier series of $f(x)$ in the interval $(0, 2\ell)$ and develop the series for 14 Marks

$$f(x) = 2x - x^2 \text{ in } (0, 3) \text{ and hence deduce that } \frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi}{12}.$$

UNIT-II

- 3 State Fourier sine transform of $f(x)$ and develop a Fourier sine transform of 14 Marks

$$e^{-|x|} \text{ and hence show that } \int_0^{\infty} \frac{x \sin mx}{1+x^2} dx = \frac{\pi e^{-m}}{2}, m > 0.$$

(OR)

- 4 State Fourier cosine transform of $f(x)$. Find the Fourier cosine transform of 14 Marks

$$f(x) = \frac{1}{1+x^2} \text{ and applying it find Fourier sine transform of } \phi(x) = \frac{x}{1+x^2}.$$

UNIT-III

- 5 Find the value of; 14 Marks

$$\text{i) } L\left(\int_0^t te^{-t} \sin 4tdt\right), \quad \text{ii) } \int_0^{\infty} \frac{e^{-t} - e^{-2t}}{t} dt.$$

(OR)

- 6 a) Find $L(f(t))$ where $f(t) = \begin{cases} \sin t, & 0 < t < \pi \\ 0, & \pi < t < 2\pi \end{cases}$ 7 Marks

b) Find: i) $L^{-1}\left(\frac{s-2}{s^2-5s+6}\right)$, ii) $L^{-1}\left(\frac{1}{s(s+1)(s+2)}\right)$. 7 Marks

UNIT-IV

- 7 a) Calculate u_2 and u_3 , if $U(z) = \frac{2z^2 + 4z + 12}{(z-1)^4}$. 7 Marks

b) Applying Z-transforms, solve $\mathbf{u}_{n+2} + 2\mathbf{u}_{n+1} + \mathbf{u}_n = \mathbf{0}$, given that $\mathbf{u}_0 = \mathbf{u}_1 = \mathbf{0}$. 7 Marks

(OR)

- 8 a) State the convolution theorem and applying it find the inverse Z - transform of $\frac{z^2}{(z-4)(z-5)}$. 7 Marks

- b) Find $Z^{-1}\left[\frac{z}{z^2 + 11z + 24}\right]$ by using partial fractions method. 7 Marks

UNIT-V

- 9 a) Determine the partial differential equation by eliminating arbitrary constants **a, b** and **c** from $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$. 7 Marks

- b) By the technique of separation of variables, solve $y^3 z_x + x^2 z_y = 0$. 7 Marks

(OR)

- 10 Design a solution for the differential equation $\frac{\partial^2 u}{\partial x^2} = \frac{\partial u}{\partial y} + 2u$ in the form $u = f(x) g(y)$ satisfying the conditions $u = 0$, $\frac{\partial u}{\partial x} = 1 + e^{-3y}$ when $x = 0$ for all values of y . 14 Marks

