

AI1110: Assignment-1

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12.13.6.16 Question: Bag I contains 3 red and 4 black balls and Bag II contains 4 red and 5 black balls. One ball is transferred from Bag I to Bag II and then a ball is drawn from Bag II. The ball so drawn is found to be red in colour. Find the probability that the transferred ball is black.

Answer: $(\frac{16}{31})$

Solution: By Bayes's Theorem we have, for any $i = 1, 2, 3, \dots, n$, where E_1, E_2, \dots, E_n be a set of events associated with a sample space S , where all the events E_1, E_2, \dots, E_n form a partition of S . For an event A associated with S ,

$$P(E_i|A) = \frac{P(E_i)P(A|E_i)}{\sum_{k=1}^{k=n} P(E_k)P(A|E_k)}$$

Let R and B be the events that the ball transferred from Box-1 to Box-2 is Red and Black respectively.

$$P(R) = \frac{\text{No. of Red balls}}{\text{Total Balls}} = \frac{3}{7}$$

$$P(B) = \frac{\text{No. of Black balls}}{\text{Total Balls}} = \frac{4}{7}$$

Let's take the conditional probability for event E , which denotes the outcome of final ball drawn being Red.

When event R occurs, in Box-2 the count of red balls becomes 5 and black balls remains 5.

$$P(E|R) = \frac{5}{10}$$

When event B occurs, in Box-2 the count of red balls remains 4 and black balls becomes 5.

$$P(E|B) = \frac{4}{10}$$

By Bayes Theorem,

$$P(E|B) = \frac{P(E|B).P(B)}{P(E|B).P(B) + P(E|R).P(R)}$$

where $P(E|B)$ is the probability of final ball being red known that the transferred ball is Black, which is our desired final answer.

$$P(E|B) = \frac{\frac{4}{10} \cdot \frac{4}{7}}{\frac{4}{10} \cdot \frac{4}{7} + \frac{5}{10} \cdot \frac{3}{7}}$$

$$P(E|B) = \frac{16}{31}$$

The probability that the transferred ball is Black is $\frac{16}{31}$.