

$$\hat{x} = D(E(x)) \quad \mathcal{L} = \text{MSE}(x, \hat{x})$$

$$\text{MAE}(x, \hat{x})$$

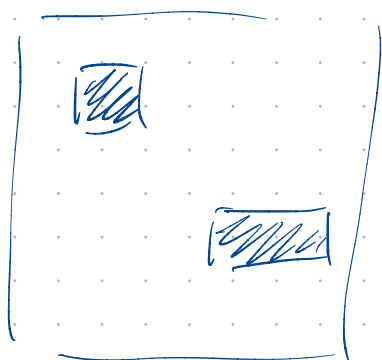
$$\text{MAPE}(x, \hat{x})$$

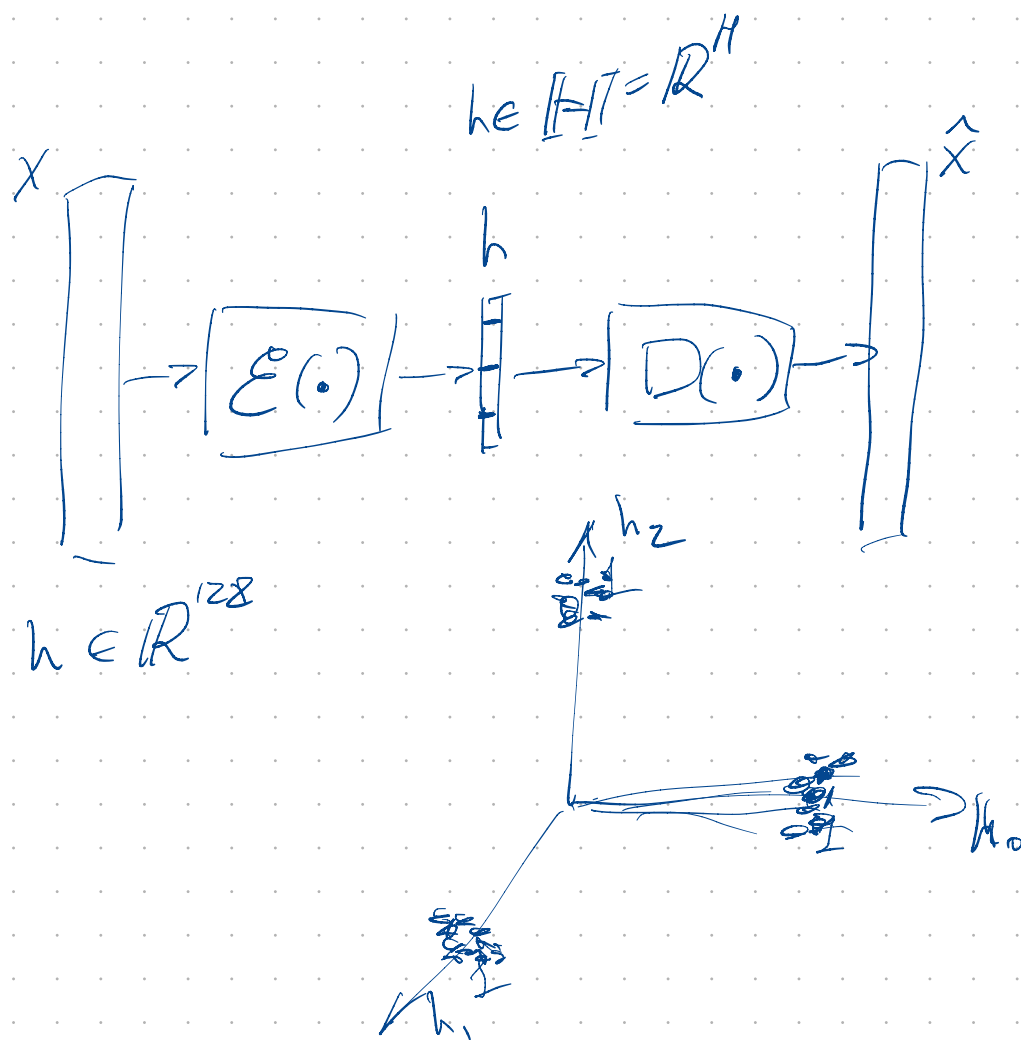
$$\text{BCE}(x, \hat{x})$$

Denoising:

$$\mathcal{L} = \text{MSE}(x, D(E(x + \epsilon)))$$

$$\epsilon \sim \mathcal{N}(0, \sigma^2)$$

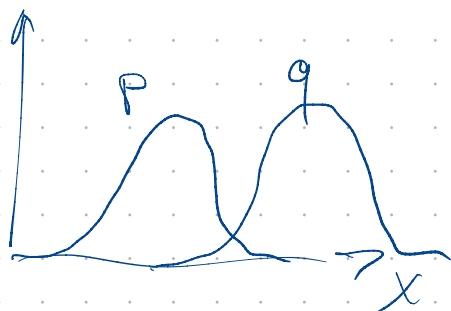




$$\mathcal{L} = \text{MSE}(x, \hat{x}) + \lambda \cdot \text{reg}$$

$$\text{reg} = \sum_{i=1}^N \sum_{j: h_j \geq c} (1 - h_j)^2 + \sum_{i=1}^N \sum_{j: h_j < c} h_j^2$$

P, q $\mathbb{KL}(p \parallel q) = \int p(x) \log \frac{p(x)}{q(x)} dx$
 $x \sim \mathcal{X}$



$$\mathbb{KL}(p \parallel q) \neq \mathbb{KL}(q \parallel p)$$

$$\text{KL}(p \parallel q) = - \sum p \log \frac{q}{p}$$

$$h \in \mathbb{R}^H$$



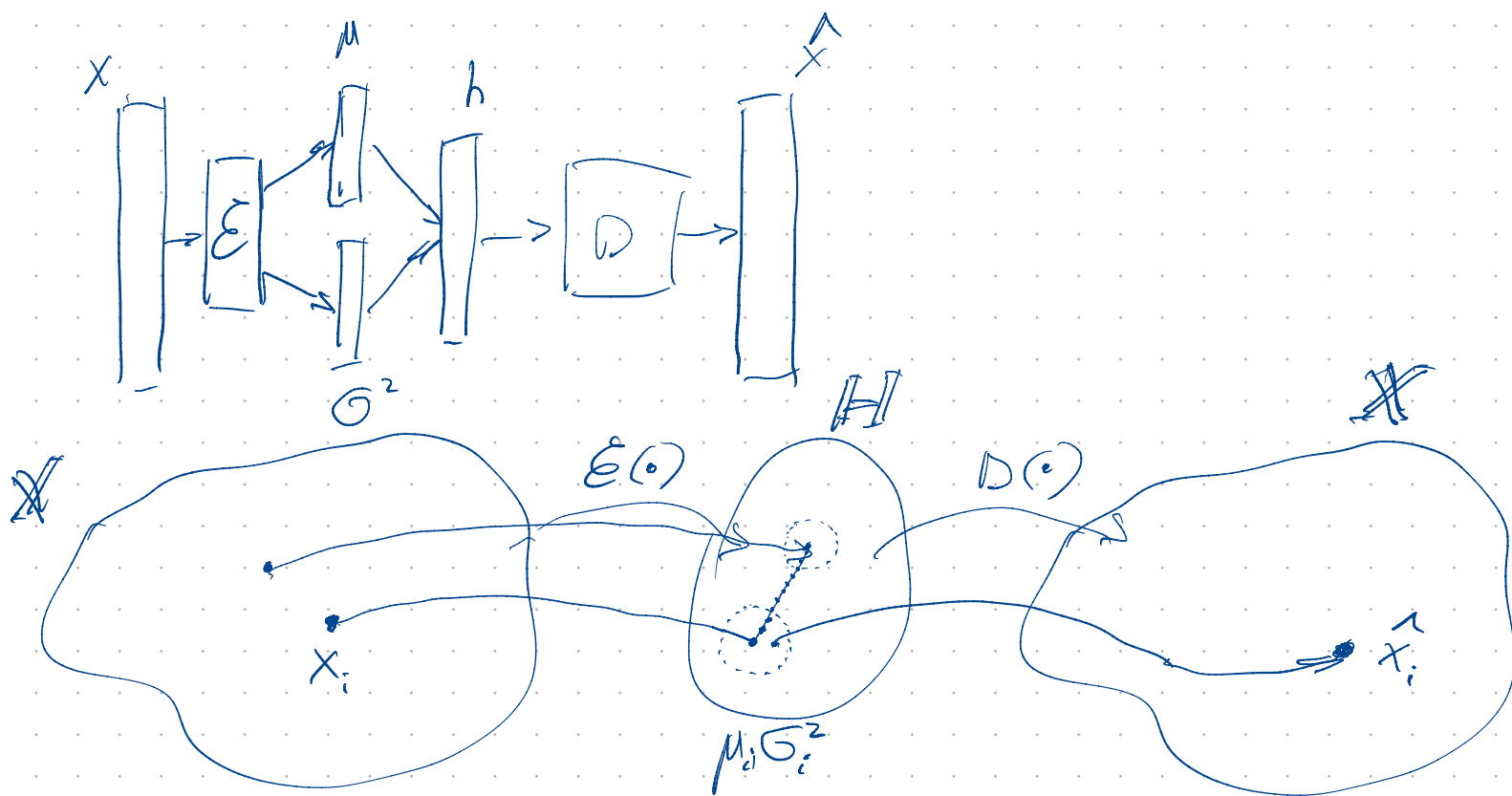
$$\text{KL}(p \parallel h) = - \sum p \log \frac{h}{p}$$

$$p = \text{Ber}(p) \quad p \in [0, 1]$$

$$\text{KL}(\text{Ber}_H(p), h) = - \sum_{i=1}^N \sum_{j=1}^H (p \log \frac{p}{h_j} + (1-p) \log \frac{1-p}{1-h_j})$$

$$h = \hat{E}(x) \quad \text{reg} = \text{KL}(\text{Ber}_H(p), h)$$

$$\mathcal{L} = \text{MSE}(x, \hat{x}) + \lambda \text{KL}(\text{Ber}_H(p), \hat{E}(x))$$



$$\mathcal{L} = \text{MSE}(x, \hat{x}) + \lambda \cdot \text{reg}_{\text{VAE}}$$

$$\mu_i, \sigma_i^2 = E(x_i)$$

$$h_i \sim \mathcal{N}(\mu_i, \sigma_i^2)$$

$$\mu, \sigma^2 \in \mathbb{R}^H$$

$$p_{\text{H}}(\sigma^2) \propto e^{-\ln \sigma^2}$$

$$\xi \sim \mathcal{N}(0, 1)$$

$$h_i = \xi \cdot \sigma_i + \mu_i$$

$$\hat{x}_i = D(h_i)$$

$$\text{reg}_{\text{VAE}} = \mathbb{E}[\mathcal{L}(h, \mathcal{N}(\mu, \sigma^2))]$$

$$= \frac{1}{2} \left[\sum_{i=1}^H \mu_i^2 + \sum_{i=1}^H \sigma_i^2 \right] - \sum_{i=1}^H (\log \sigma_i^2 + 1)$$