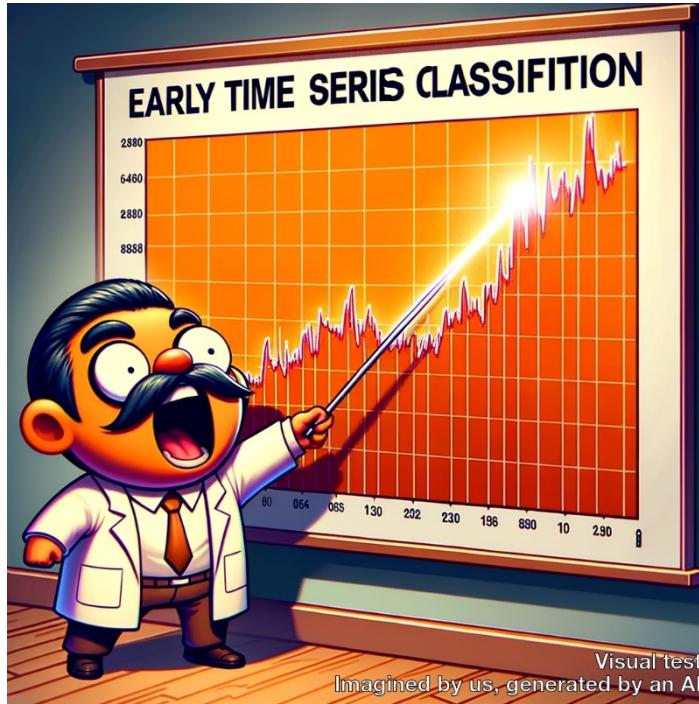


Early Decision Making

Tutorial PFIA 2024



Visual test
Imagined by us, generated by an AI



Our research history and team



Antoine
Cornuéjols



Alexis
Bondu



Vincent
Lemaire



Asma
Dachraoui



Youssef
Achenchabe



Aurélien
Renault

- 2012 : start working on **Early Classification of Time Series** (@EDF) with *Asma Dachraoui*, Phd student
- 2015 : development of the first **non-myopic** approach
- 2019 : second Phd student, *Youssef Achenchabe* (@Orange)
- 2020 : improvement of **non-myopic** approaches
- 2022 : - extension to **revocable** decisions
 - extension to **open time series** (i.e. data stream)
- 2023 : Extension of ECTS to a more general problem, called **ML-EDM**
- 2024 : third Phd student, *Aurélien Renault* (@Orange) working on **non-stationary** environment



Albert
Bifet



Joao
Gama



Georges
Hébrail



Pierre-François
Marteau



Fabrice
Clérot

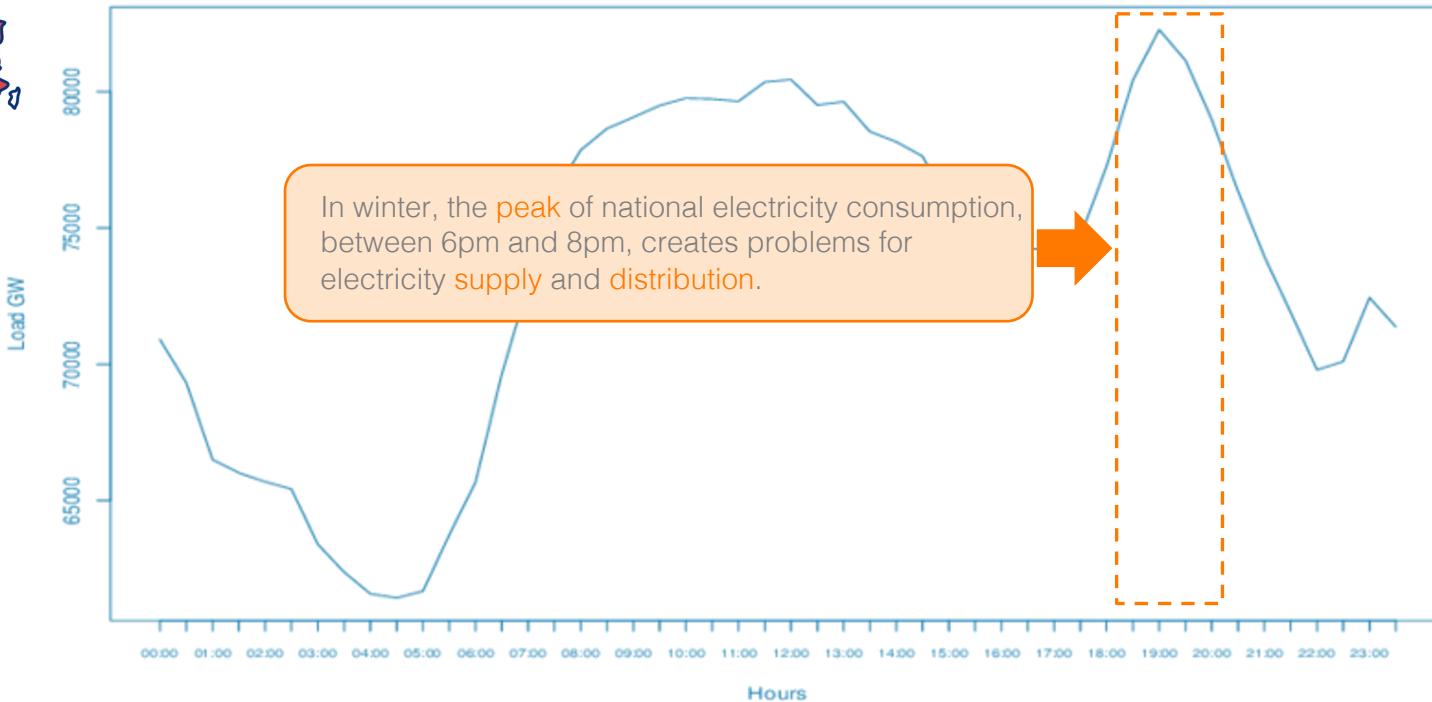
Motivations



EDF's original target application

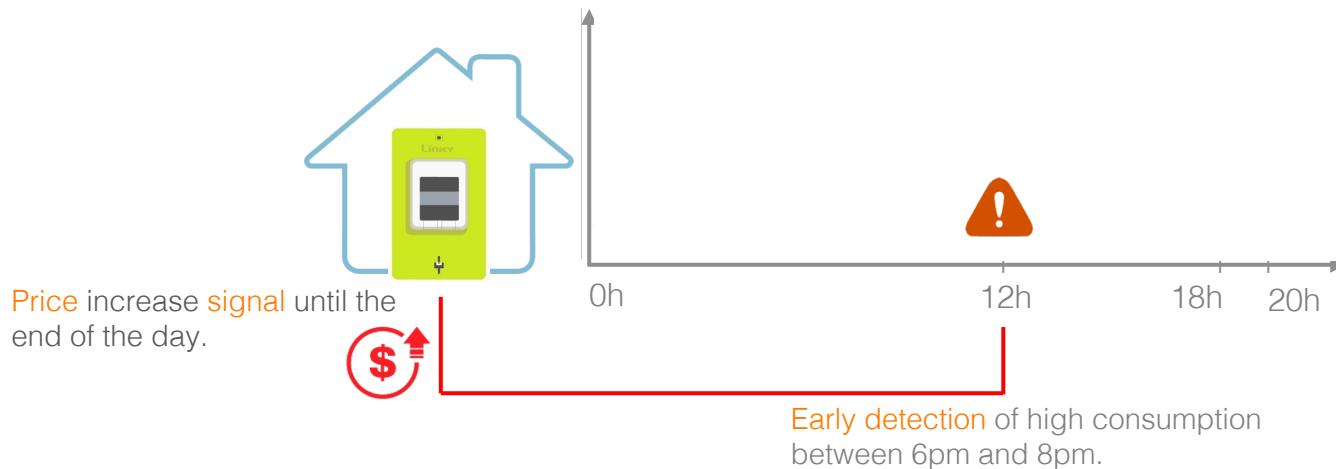


French daily load on the 29th January 2014

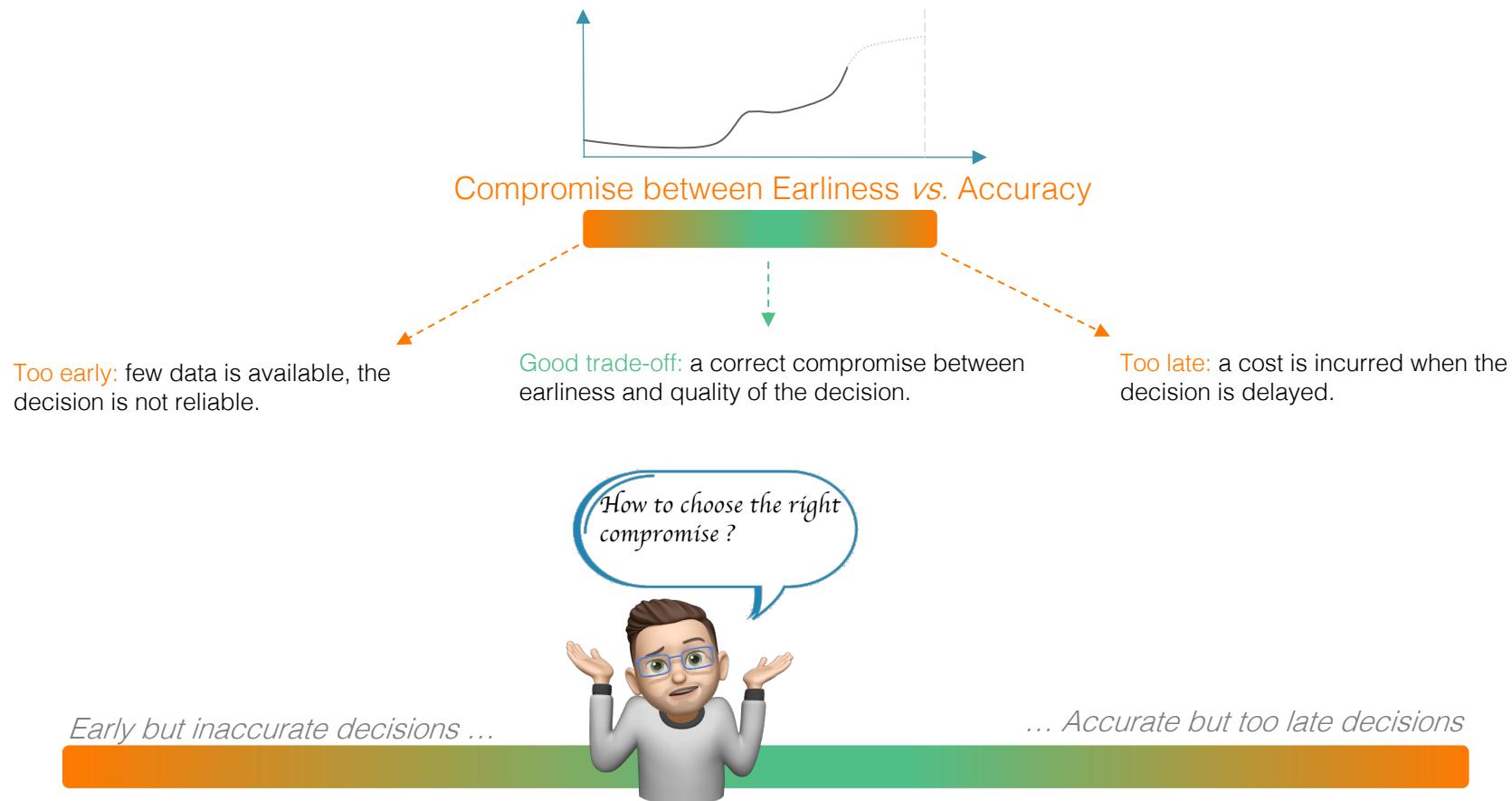


EDF's original target application

Early targeting of households involved in the evening peak, between 18pm and 20pm.



The question is: When to make a decision ?



Many applications with time pressure to decide



Churn: when to contact potential churners?

Waiting for further information ... before they leave Orange.



Fraud: when to block a bank card?

Waiting for further information ... before the bank account is empty.

This compromise is
everywhere !



Network monitoring: when to detect a malfunction?

Waiting for further information ... before the breakdown is established.

Outline



#1 Introduction to ECTS



#2 Proposed taxonomy



#3 State of the art



#4 Experiments



#5 Tutorial



#6 Generalization to ML-EDM

We provide :



Python library:

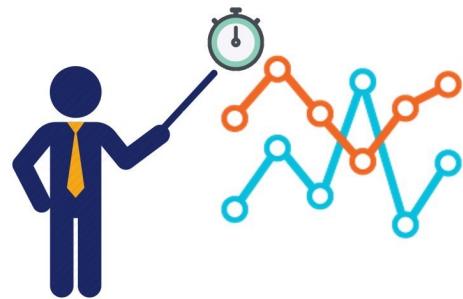
- 10 competing approaches,
- 3 baselines.



Collection of 35 datasets:

- non-z-normalized
- stratified train / test split

#1 Introduction to ECTS



Bibliographic origins

- First publication to mention the ECTS problem in 2008 [1]
- But, ECTS is rooted in the optimal stopping problem [2] (1969)
 - Here, the online decision to make is simply to stop receiving new pieces of information.
 - A value is observed at each time step and a reward is received.
 - The objective is to maximize the reward by stopping receiving new values at proper time.

e.g. 1 – The Shepp's urn problem

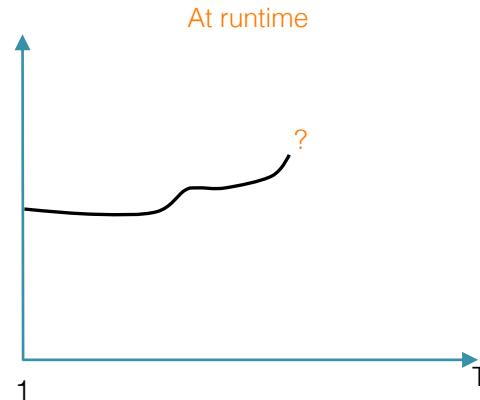
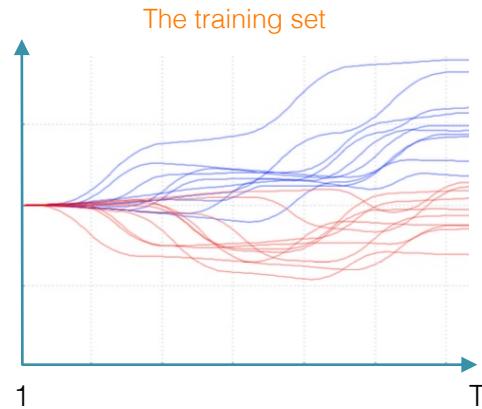


e.g. 2 – The secretary problem

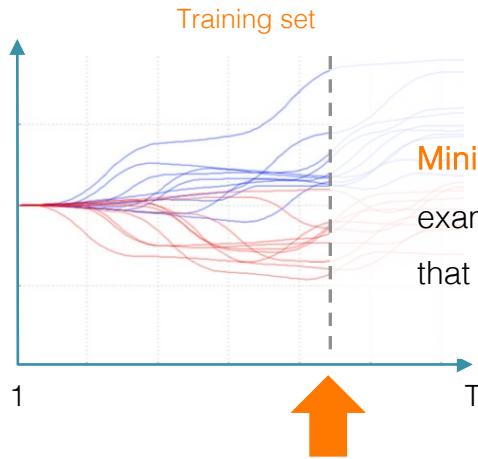


ECTS is an Optimal Stopping problem coupled with a classification task

- The training set is made up of time series of the **same length**
 - The full length, **T**, corresponds to the **maximum time horizon** to trigger the decision
 - Each **label** is assigned to a **full length** time series
 - At **runtime**, the input time series is **progressively observed** (with non i.i.d measurements)
 - The objective is to **trigger** a reliable decision as soon as possible, **before the time T**
 - A single **irrevocable** decision can be triggered



Back to the first “ECTS” approach



Minimal Prediction Length, defined of all training examples, such that the predictions are the same that the ones using the **full-length** time series.

Shortcomings

- There is **no adaptation** of the trigger moment to the observed time series
- **No trade-off** between Accuracy and Earliness

Ground truth

Two decision **costs** are considered :

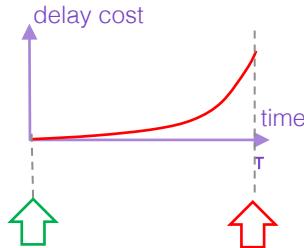
1 - miss-classification cost;

$$C_m(\hat{y}|y) : \mathcal{Y} \times \mathcal{Y} \rightarrow \mathbb{R}$$

\hat{y}/y	1	0
1	10	5
0	100	0

2 - and the cost of delaying the decision.

$$C_d(t) : \mathbb{R} \rightarrow \mathbb{R}$$



The example of fraud detection:



The **worst** case scenario would be to miss an anomaly and trigger the prediction at the last moment.



In the **best** case, the potential for an anomaly is ruled out as soon as possible.

Ground truth

Two decision **costs** are considered :

- 1 - miss-classification cost;

$$C_m(\hat{y}|y) : \mathcal{Y} \times \mathcal{Y} \rightarrow \mathbb{R}$$

\hat{y}/y	1	0
1	10	5
0	100	0

- 2 - and the cost of delaying the decision.

$$C_d(t) : \mathbb{R} \rightarrow \mathbb{R}$$



- Considering the following ‘time dependent’ Loss Function:

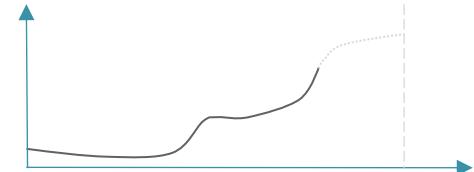
$$\mathcal{L}(\hat{y}, y, \hat{t}) = C_m(\hat{y}|y) + C_d(\hat{t})$$

- The **Empirical Risk** is defined as:

$$AvgCost = \frac{1}{N} \sum_{i=0}^N C_m(\hat{y}_i|y_i) + C_d(\hat{t}_i)$$

General form of ECTS models

Incomplete time series: $\mathbf{x}_t = \langle x_1, \dots, x_t \rangle$



ECTS model: $s(\mathbf{x}_t)$

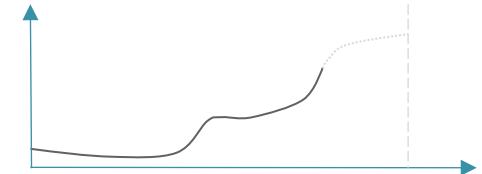
Trigger time: $\hat{t} \in [1, T]$

Predicted class: $\hat{y} \in \mathcal{Y}$

General form of ECTS models

An ECTS function involves a predictor :

$$\hat{y}(\mathbf{x}_t)$$



The optimal triggering time depends on this predictor : $t^* = \arg \min_{t \in [1, T]} \mathcal{L}(\hat{y}(\mathbf{x}_t), t, y)$

Optimal time requires a complete knowledge of the time series!

The optimal triggering function is defined as follows :

$$s^*(\mathbf{x}_t) = \begin{cases} \emptyset & \text{if extra measures are queried;} \\ y^* = \hat{y}(x_{t^*}) & \text{when prediction is triggered at } t = t^* \end{cases}$$

The objective is to minimize the true risk by finding the best triggering function, such that :

$$\arg \min_{s \in \mathcal{S}} \mathbb{E}_{\mathbf{x} \sim \mathbb{P}_{\mathcal{X}}} [\mathcal{L}(\hat{y}(\mathbf{x}_{\hat{t}}), y, \hat{t})]$$

Triggering predictions is an online problem!

Proxy metrics exist in the literature

- The **Harmonic Mean**:

$$HM = \frac{2 \times Accuracy \times (1 - Earliness)}{Accuracy + (1 - Earliness)}$$
 with $Accuracy = \frac{1}{M} \sum_{i=1}^M \mathbb{1}(\hat{y}_i = y_i)$ and $Earliness = \frac{1}{M \times T} \sum_{i=1}^M \hat{t}_i$

- The **Cost Function**:

$$CF = \alpha \times (1 - Accuracy) + (1 - \alpha) \times Earliness$$

Witch equals to **AgvCost** when $C_m(\hat{y}, y) = \mathbb{1}(\hat{y} = y)$, $C_d(t) = \hat{t}/T$ and $\alpha = 1$



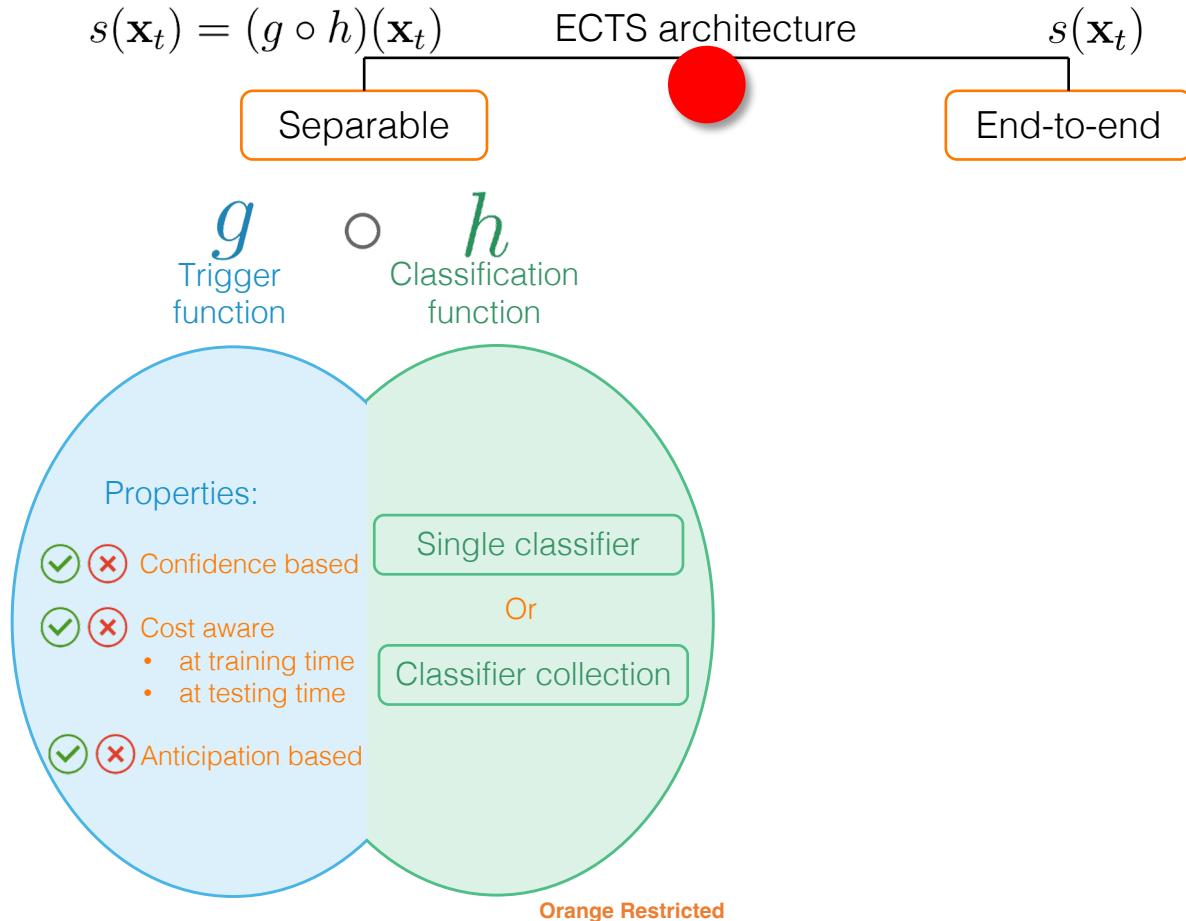
Why do certain approaches to literature fail to use empirical risk ?



#2 Proposed taxonomy



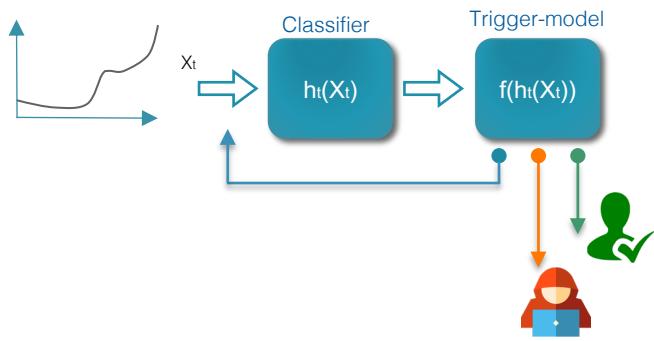
A new ECTS taxonomy



Types of architecture :

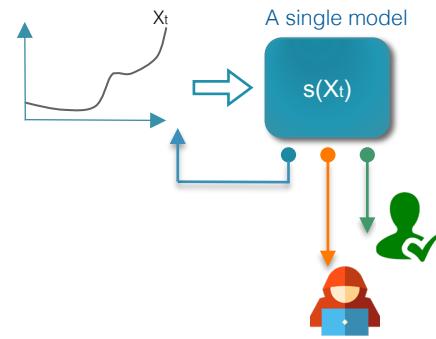
Separable

$$s(\mathbf{x}_t) = (g \circ h)(\mathbf{x}_t)$$



End-to-end

$$s(\mathbf{x}_t)$$



- A baseline example: **Proba_Threshold** consists in triggering the prediction as soon as the estimated class probability exceeds a certain threshold.

- Example: Early Distinctive Shapelet Classification (EDSC) finds a set of **sub-series** (i.e. shapelets) that allow for early discrimination between different classes..

Types of architecture :

Separable

$$s(\mathbf{x}_t) = (g \circ h)(\mathbf{x}_t)$$

- The major part of the literature.
- Involves two independent training.
- The trigger function is fed from the classifier output.

End-to-end

$$s(\mathbf{x}_t)$$

- RL and Deep Learning (sometime mixed)

Separable RL approaches

Set of actions:

{‘decide now’, ‘postpone decision’}

End-to-end RL approaches

Set of actions:

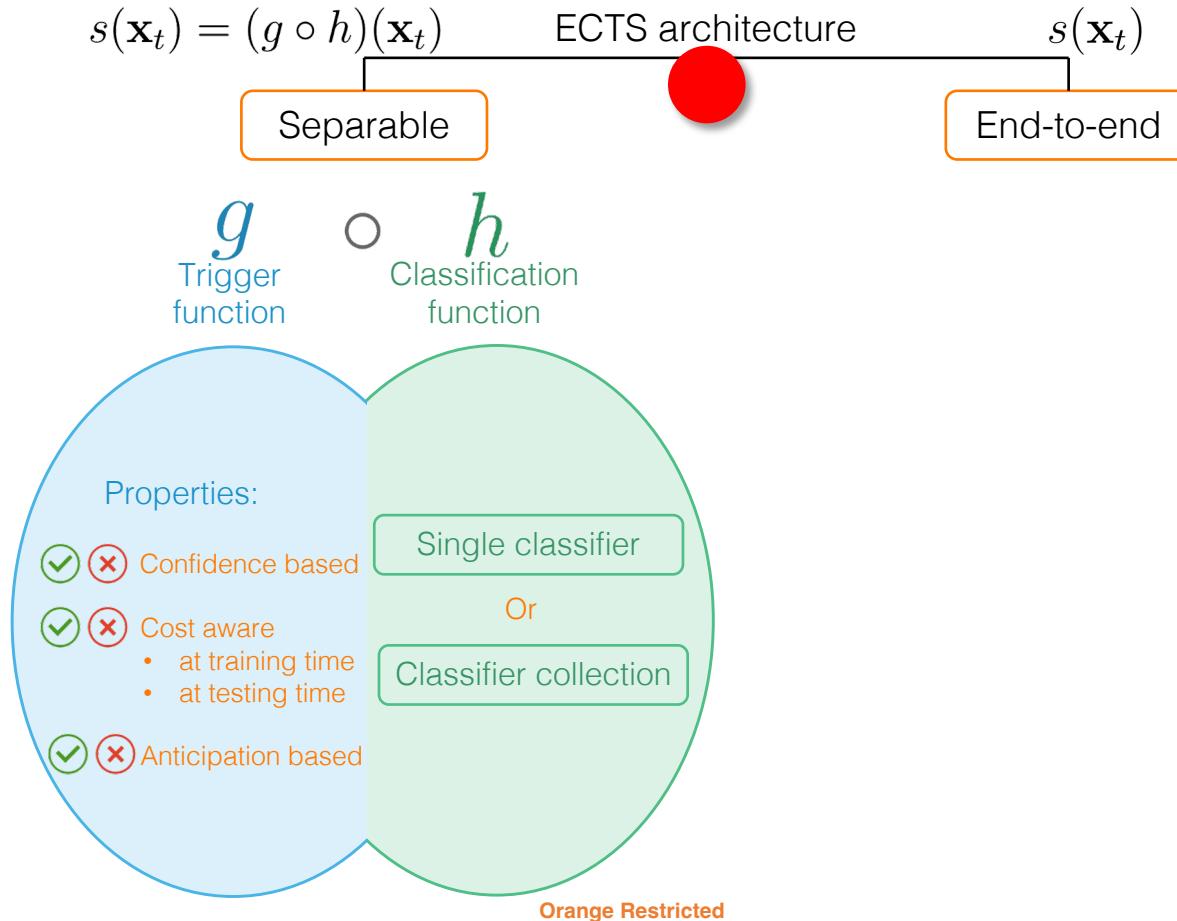
{‘postpone decision’, c_1, \dots, c_N }



We focus now on **separable** approaches

Two distinct functions (or modules),
but one common training stage.

Outline

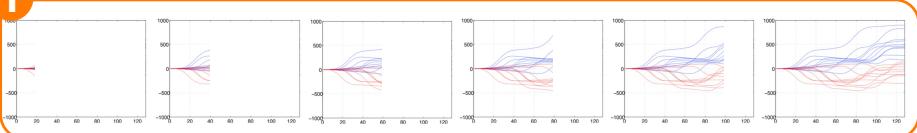


Classification function

Training a collection of time-indexed classifiers

- The **most used** in the literature.

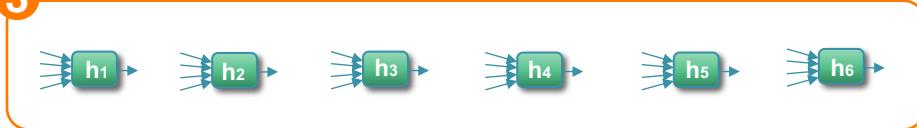
1 Building a collection of truncated datasets



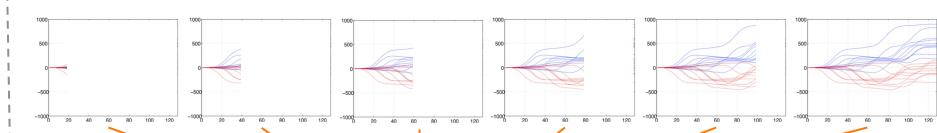
2 Independent **features** extraction (*or representations*)



3 Independent classifier training



Training a single classifier



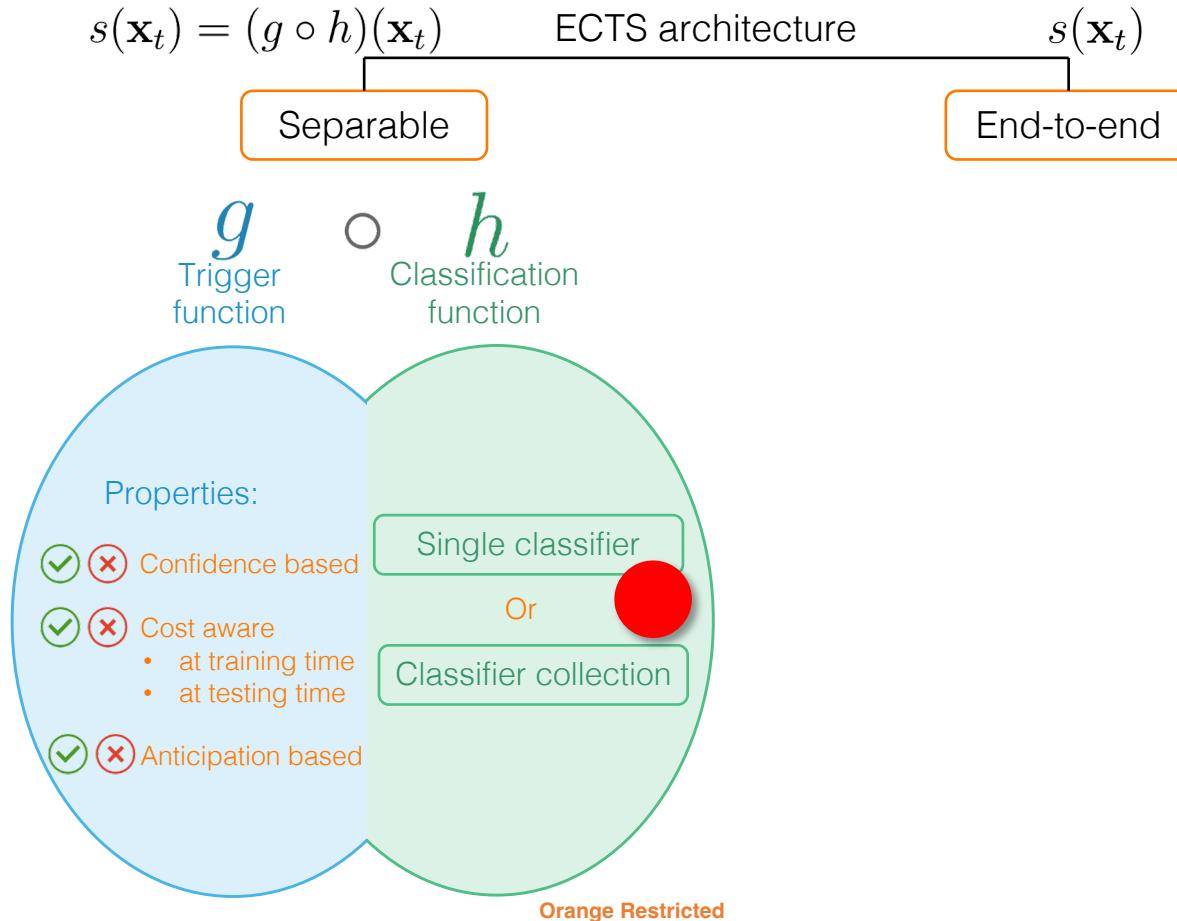
A single
feature
space

- Specific **feature** engineering
- Or **learning** a representation (deep)



- Training a **single** classifier

Outline

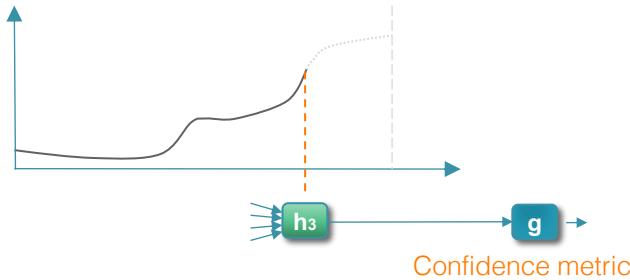


Confidence based approaches



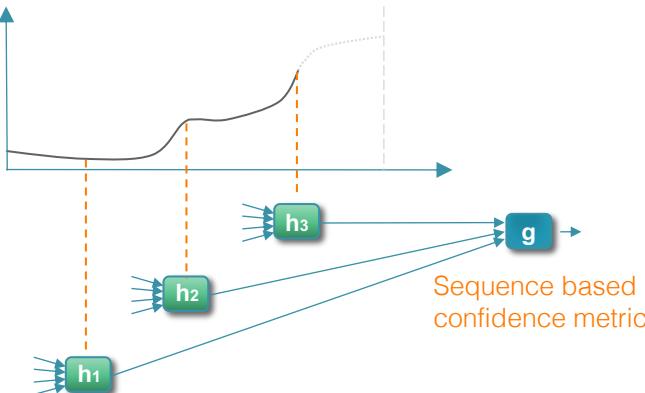
1 Instant-based trigger function

- The most used in the literature.
- Monitor a confidence metric over time;
- By considering only the last value classifier output.
- Trigger prediction when a threshold is reached.
- A baseline example: Proba_Threshold.



sequence-based trigger function

- Considering the sequence of classifier outputs.
- Specifically designed confidence metric for ECTS.



Cost awareness

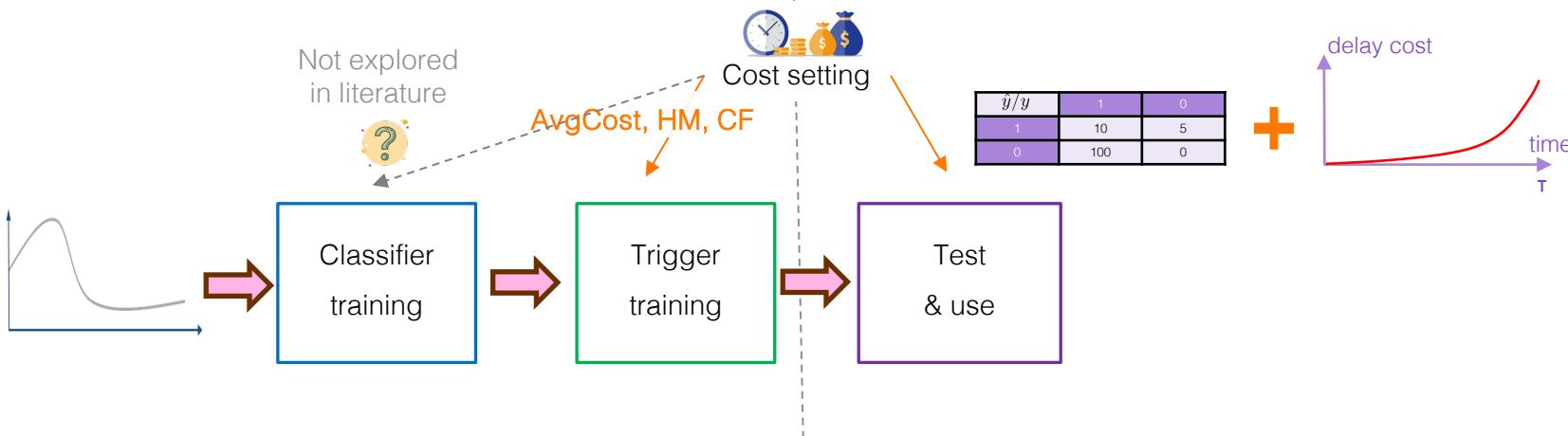
Approaches in the literature differ in the requirement (*or not*) to be informed of costs, at two different stages:

At training time

- A scalar metric is available which combines the two objectives of **accuracy** and **earliness**.
- This **metric** is often used to optimize the trigger **parameters**.

At testing time

- The **cost functions** themselves are available (i.e. C_m and C_d)



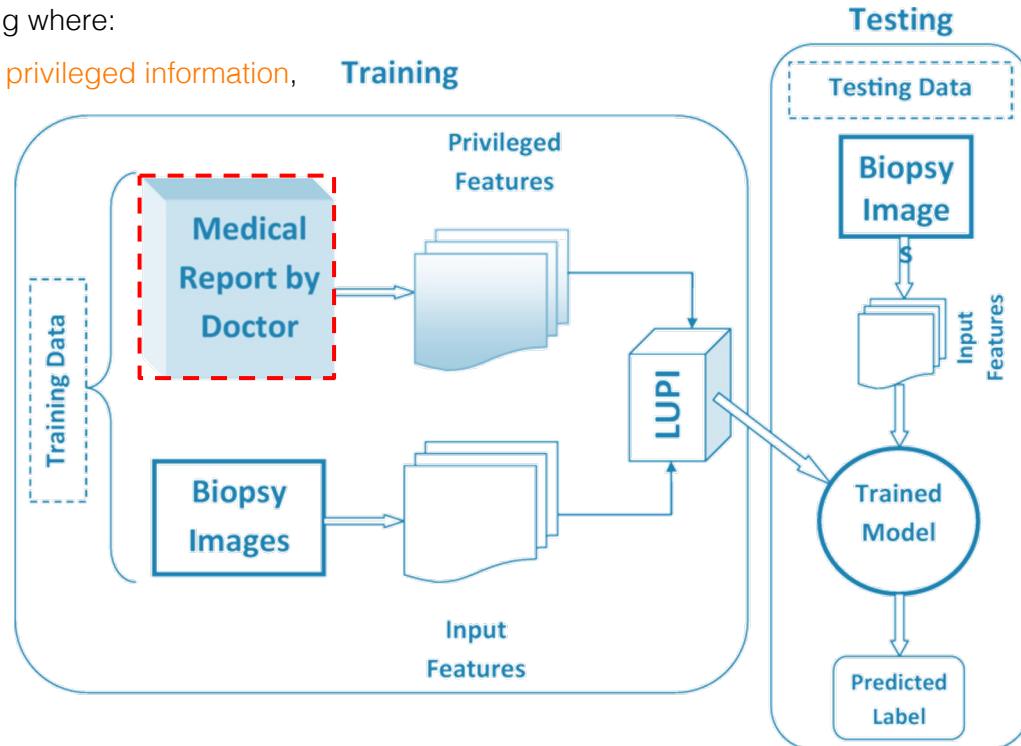
Anticipation-based

Is the current time step is better than all the future ones ?

ECTS can be cast as a LUPI problem [1]

Learning Using Privileged Information is a setting where:

- The learner can benefit at the **training** time of **privileged information**,
- That will not be available at **test** time.

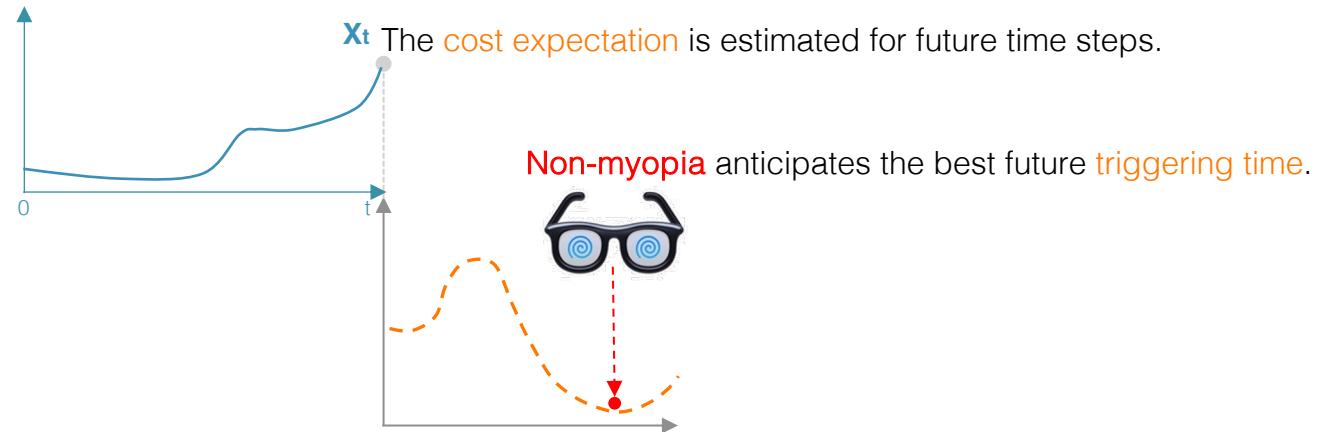


Anticipation-based

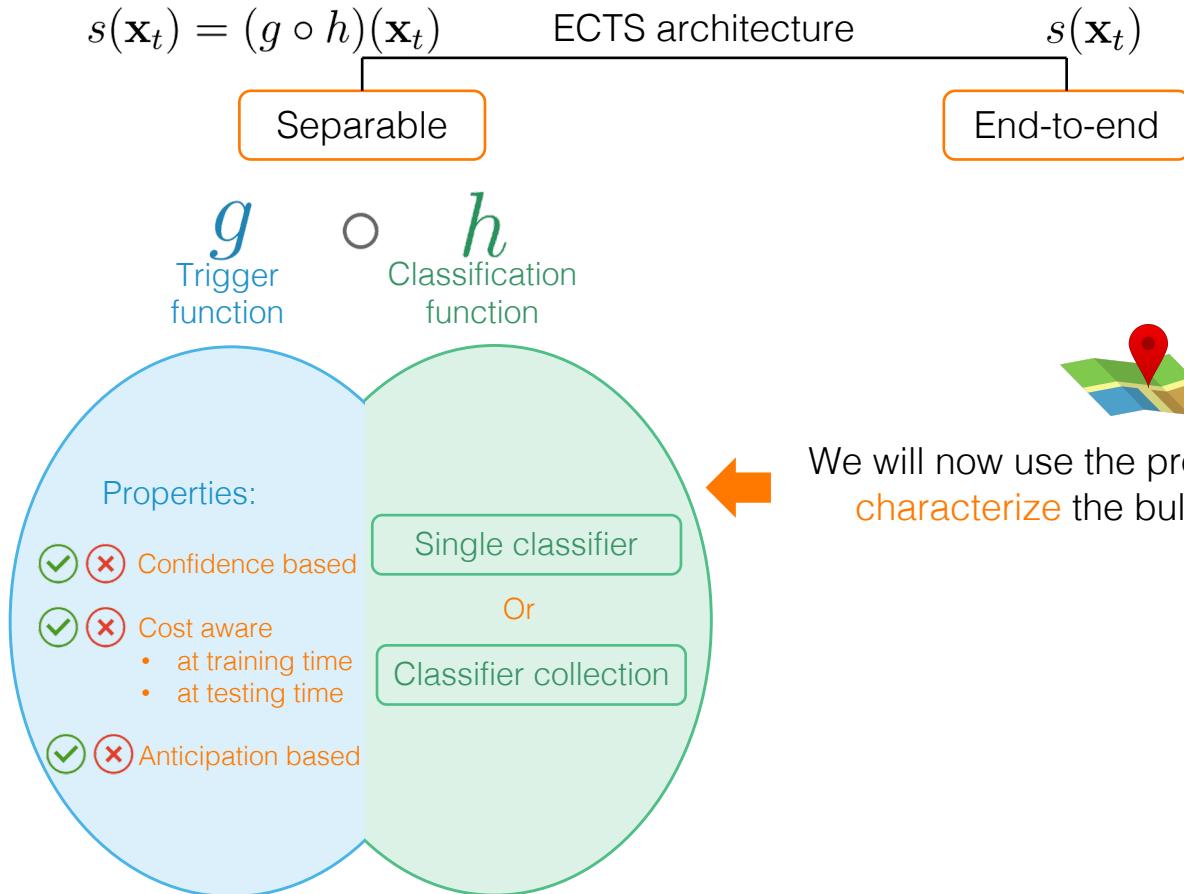
Is the current time step is better than all the future ones ?

In the ECTS problem

- LUPI makes possible to learn what are the likely future of an incoming time series;
- For example, to estimate the cost expectation for all future time steps.



Proposed ECTS taxonomy



#3 State of the art



Literature approaches

References	Classifier(s) (collection ✓)	End2end	Confidence	Anticipation	Cost awareness
EDSC (Xing et al., 2011)	Shapelet	✓	✓		✗
ECTS' (Xing, Pei, & Yu, 2012)	1NN		✓	✓	✗
Reject (Hatami & Chira, 2013)	SVM		✓		✗
RelClass (Parrish et al., 2013)	QDA, Linear SVM		✓	✓	✗
iHMM (Antonucci et al., 2015)	HMM		✓		✗
2step/NoCluster (Tavenard & Malinowski, 2016)	Linear SVM (✓)			✓	train & test
ECDIRE (Mori et al., 2017b)	Gausian Process (✓)		✓		✗
Stopping Rule (Mori et al., 2017a)	Gaussian Process (✓)		✓		train
EARLIEST (Hartvigsen et al., 2019)	LSTM	✓			train
ECEC (Lv et al., 2019)	WEASEL (✓)		✓		train
DDQN (Martinez et al., 2020)	MLP?	✓		✓	train
TEASER (Schäfer & Leser, 2020)	WEASEL (✓)		✓		train
ECONOMY- γ -max (Zafar et al., 2021)	XGBoost + tsfel (✓)			✓	train & test
DETSCNet (Chen et al., 2022)	TCN	✓			train
CALIMERA (Bilski & Jastrzebska, 2023)	MiniROCKET (✓)			✓	train
ELECTS (Rußwurm et al., 2023)	LSTM	✓			train
SOCN (Lv et al., 2023)	FCN		✓		train

The ASAP and ALAP baselines



- **ASAP** triggers all predictions at the first time step.
- **ALAP** triggers all predictions at the last time step.



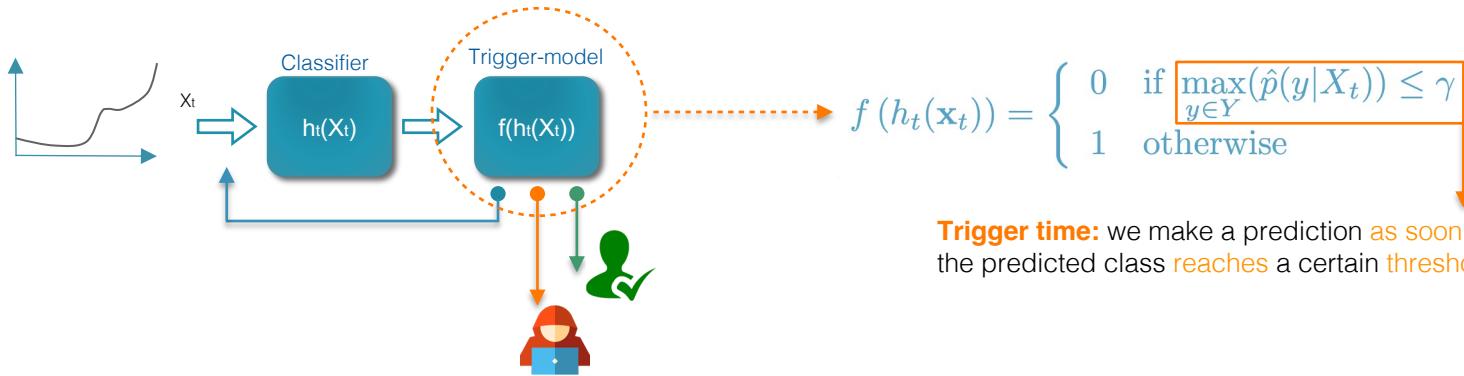
Do these baseline approaches disqualify some literature approaches?

- Not **well studied** in the literature !
- However, the performance of these baselines is an essential **point of comparison**.

Proba Threshold baseline



- Separable ✓
- Collection of classifiers ✓
- Confidence based ✓
- Anticipation based ✗
- Cost aware ✓ @train @test



Trigger time: we make a prediction as soon as the probability of the predicted class reaches a certain threshold.

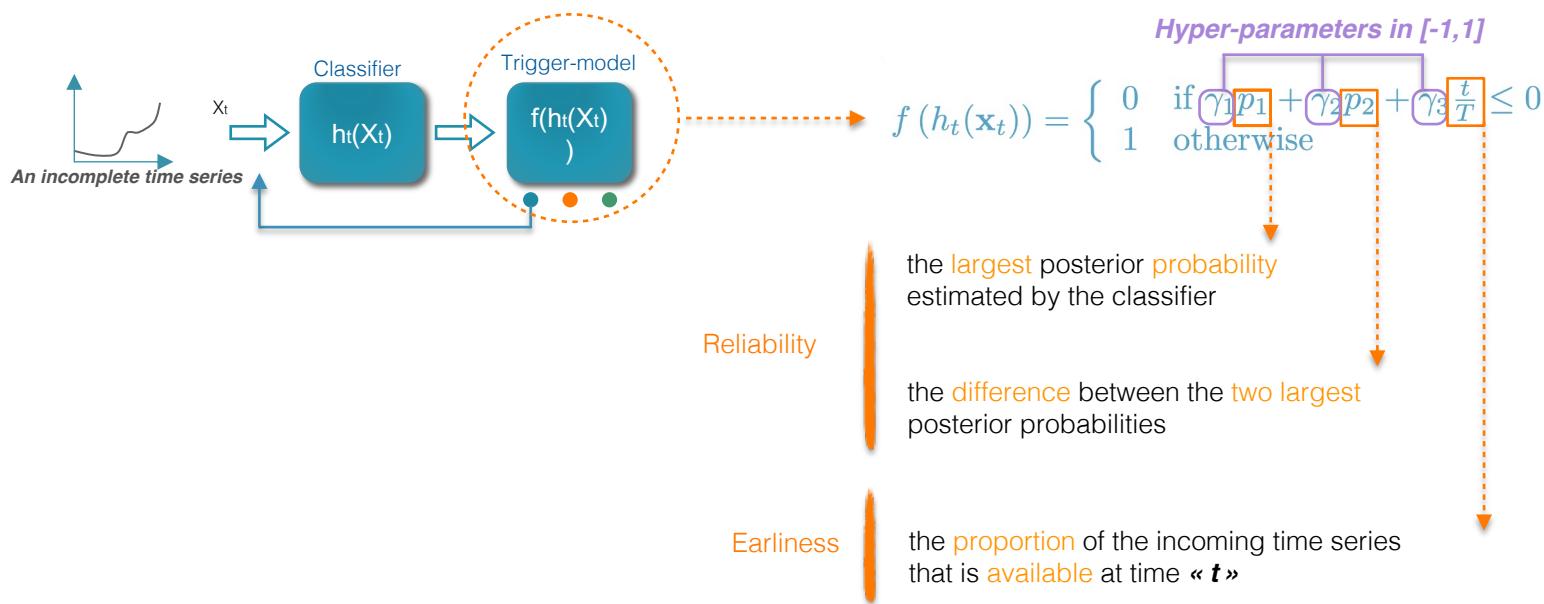


Can we perform better than this simple confidence based approach ?

- Not well studied in the literature !
- Seems to be a natural idea for datascientists

The Stopping Rule approach [1]

- Separable ✓
- Collection of classifiers ✓
- Confidence based ✓
- Anticipation based ✗
- Cost aware ✓ @train @test

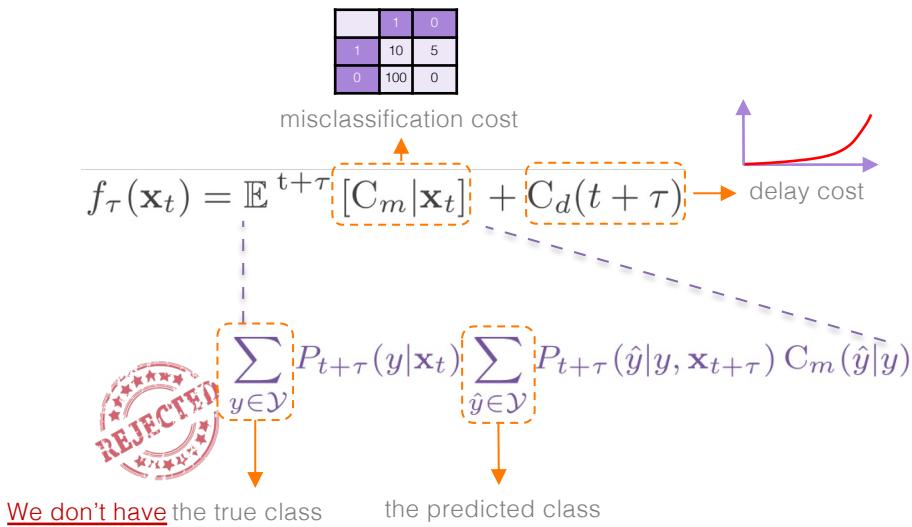


The ECONOMY approach

1/3



Non-myopia: The objective is to estimate the cost expectation at a fixed future potential triggering time $t + \tau$



The best future triggering moment:

$$\tau^* = \underset{\tau \in \{0, \dots, T-t\}}{\text{ArgMin}} f_\tau(\mathbf{x}_t)$$

Triggering condition:



$$\tau^* = 0$$

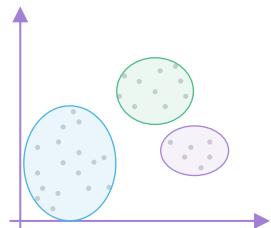
Tractable formalization

$$f_{\tau}(\mathbf{x}_t) = \sum_{g_k \in \mathcal{G}} [P_t(g_k | \mathbf{x}_t)] \sum_{y \in \mathcal{Y}} [P_t(y | g_k)] \sum_{\hat{y} \in \mathcal{Y}} [P_{t+\tau}(\hat{y} | y, g_k)] C_m(\hat{y} | y) + C_d(t + \tau)$$

We need to build a partition of data

Prior of the class y within the group g^k

Tractable using the confusion matrices of the classifiers, within each group, and for each time horizon



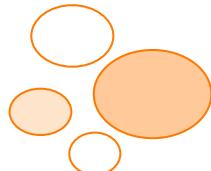
The ECONOMY approach

3/3



- Separable ✓
- Collection of classifiers ✓
- Confidence based ✗
- Anticipation based ✓
- Cost aware ✓ @train @test

$$f_{\tau}(\mathbf{x}_t) = \sum_{\mathbf{g}_k \in \mathcal{G}} P_t(\mathbf{g}_k | \mathbf{x}_t) \sum_{y \in \mathcal{Y}} P_t(y | \mathbf{g}_k) \sum_{\hat{y} \in \mathcal{Y}} P_{t+\tau}(\hat{y} | y, \mathbf{g}_k) C_m(\hat{y} | y) + C_d(t + \tau)$$



1. How to build the data partition ?
2. How to estimate the probability of belonging to each group ?

Best design choices

Among all the tested algorithms [2], the best one is ECONOMY- γ

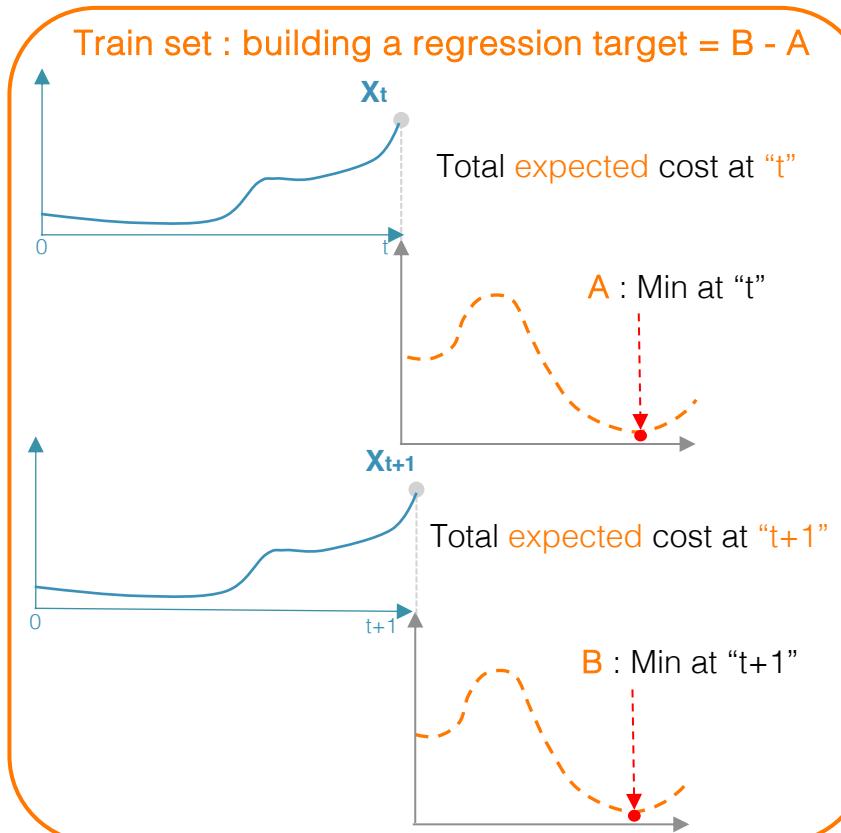


1. It build a data partition by discretizing the output confidence level of each classifier
2. It estimates the probability of belonging to each group at a future time step $t + \tau$ by using a Markov Chain model.



The best ECTS approach !

The CALIMERA approach



Key ideas :

- Separable ✓
- Collection of classifiers ✓
- Confidence based ✗
- Anticipation based ✓
- Cost aware ✓ @train @test

1. This is a non-myopic approach
2. That uses a well defined regression problem
3. A collection of time indexed regression models is trained
4. In order to detect when the min value is being exceeded.

Shortcoming : when estimating the expected cost

- The misclassification cost matrix is not fully browsed
- Only the predicted class is considered

The ECEC approach



- The objective is to **limit variation** in the sequence of predicted class values.
- **Precision** is used as a confidence measure (probability of the true class, given the predicted class)

$$r_H(y|\hat{y}) = \frac{\|\{X_i | H(X_i) = \hat{y} \& Y_i = y\}\|}{\|\{X_i | H(X_i) = \hat{y}\}\|}$$

Number of examples with predicted class \hat{y} and true class y
Number of examples with predicted class \hat{y}

- Confidence in the sequence of predictions is estimated using the **independence assumption**:

$$C_t(H_t(X)) = 1 - \prod_{k=1}^t (1 - r_{H_k}(y = H_t(X) | H_k(X)))$$

Probability that the i th prediction will differ from the last one.

 independence assumption within the sequence of predictions.

- A decision **threshold** is applied to this sequential confidence measure



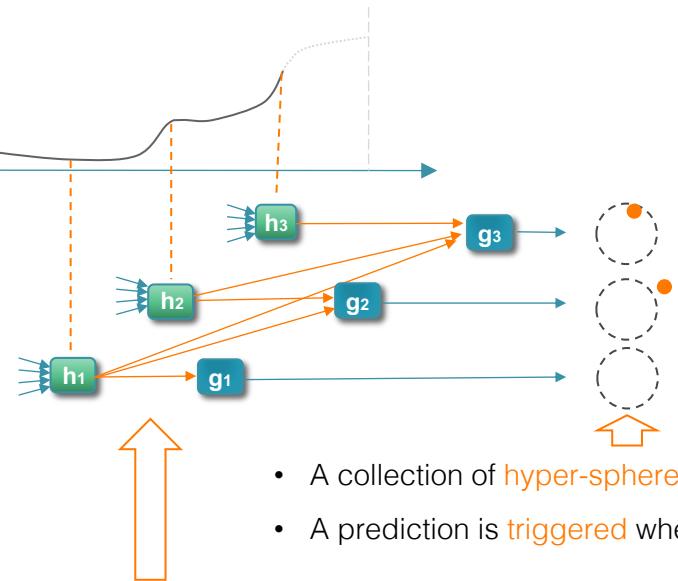
- Separable ✓
- Collection of classifiers ✓
- Confidence based ✓
- Anticipation based ✗
- Cost aware ✓ @train @test

The TEASER approach



- Separable ✓
- Collection of classifiers ✓
- Confidence based ✓
- Anticipation based ✗
- Cost aware ✓ @train @test

- Triggering (or not) the predictions becomes a **classification** problem,
- Aiming to discriminate between **good** and **bad** predictions.
- But, the **balance** of the problem drastically changes depending on the triggering **time**.
- Thus, the authors proposed to use a **collection of one-class SVM**.



- A collection of **hyper-spheres** is learned, representing good predictions.
- A prediction is **triggered** when an observation **falls within** it.

The **input space** dimension of one-class SVMs increases with time.

#4 Experiments



All implemented approaches in the provided library



References	Classifier(s) (collection ✓)	End2end	Confidence	Anticipation	Cost awareness
EDSC (Xing et al., 2011)	Shapelet	✓	✓		✗
ECTS' (Xing, Pei, & Yu, 2012)	1NN	✓		✓	✗
Reject (Hatami & Chira, 2013)	SVM	✓			✗
RelClass (Parrish et al., 2013)	QDA, Linear SVM	✓		✓	✗
iHMM (Antonucci et al., 2015)	HMM	✓			✗
2step/NoCluster (Tavenard & Malinowski, 2016)	Linear SVM (✓)			✓	train & test
ECDIRE (Mori et al., 2017b)	Gausian Process (✓)		✓		✗
Stopping Rule (Mori et al., 2017a)	Gaussian Process (✓)		✓		train
EARLIEST (Hartvigsen et al., 2019)	LSTM	✓			train
ECEC (Lv et al., 2019)	WEASEL (✓)		✓		train
DDQN (Martinez et al., 2020)	MLP?	✓		✓	train
TEASER (Schäfer & Leser, 2020)	WEASEL (✓)		✓		train
ECONOMY- γ -max (Zafar et al., 2021)	XGBoost + tsfel (✓)			✓	train & test
DETSCNet (Chen et al., 2022)	TCN	✓			train
CALIMERA (Bilski & Jastrzebska, 2023)	MiniROCKET (✓)			✓	train
ELECTS (Rußwurm et al., 2023)	LSTM	✓			train
SOCN (Lv et al., 2023)	FCN		✓		train

Four additional approaches, including two that have not been used in experiment due to scalability or performance issues.

Motivation: common pitfalls in the literature

- **Variety of setups:** with different levels of cost awareness.
- **Thus, evaluation issues:**
 - Globally hard to define what is « good » ECTS approach.
 - No agreement on evaluation metrics,
 - No baselines comparison
 - Copy-paste of the published results
 - Very simple cost setting
 - Unfair comparisons (e.g. comparing trigger functions, with different classifiers)
- **And numerous methodology shortcoming :**
 - Z-normalization
 - Biased train/test split
 - No calibration

➔ big accumulated debt
➔ no clear vision of the performance of existing approaches

Reproducibility, Protocol and Evaluation

Trigger function : we provide a modular **python library** implementing **10** competing approaches and **3** baselines.

Classifier : this choice is **fixed**, and a collection of **calibrated** Minirocket estimators is used.

Datasets : UCR Archive for time series classification **AND** a new non z-normalized collection.

Baselines : blind baselines **ASAP** and **ALAP** and **proba_threshold**.

Evaluation is performed using the **AvgCost** metric which represents the ground truth.

$$\text{AvgCost} = \frac{1}{N} \sum_{i=0}^N \alpha \times C_m(\hat{y}_i^t | y_i) + (1 - \alpha) \times C_d(\hat{t}_i)$$

We **use** an additional parameter **alpha** to control the relative importance of both costs

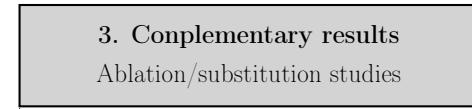
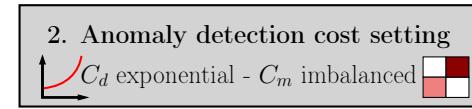
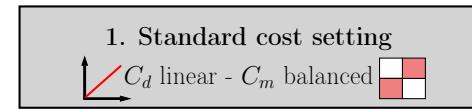
We can find in the literature ...

A rather simple costs definition :

$$C_m(\hat{y}|y) = \mathbb{1}(\hat{y} \neq y)$$
$$C_d(t) = t/T$$

That simplifies the metric: $\text{AvgCost} = \alpha \times (1 - \text{Accuracy}) + (1 - \alpha) \times \text{Earliness}$

Extensive experiments



Derived from 1.



- 1.2 Removing calibration
- 1.3 Impact of base classifier
- 1.5 Impact of z -normalization

Derived from 2.



- 2.1 Exponential delay cost only
- 2.2 Imbalanced cost only
- 2.3 Standard cost setting

Used datasets:



Classically used datasets collection



Proposed, non z normalized, datasets collection



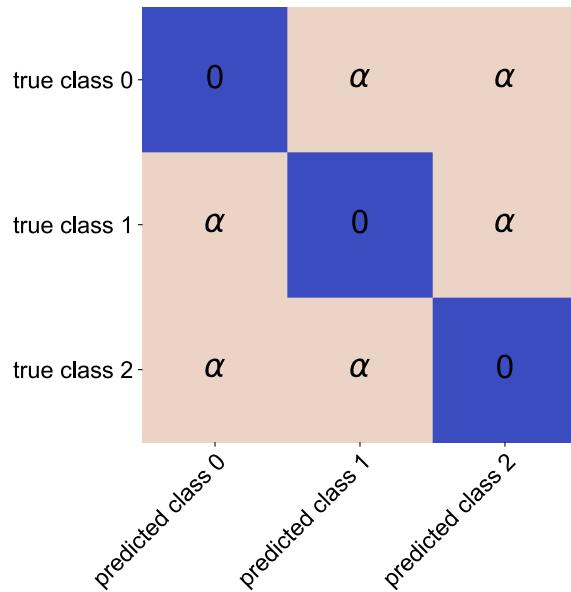
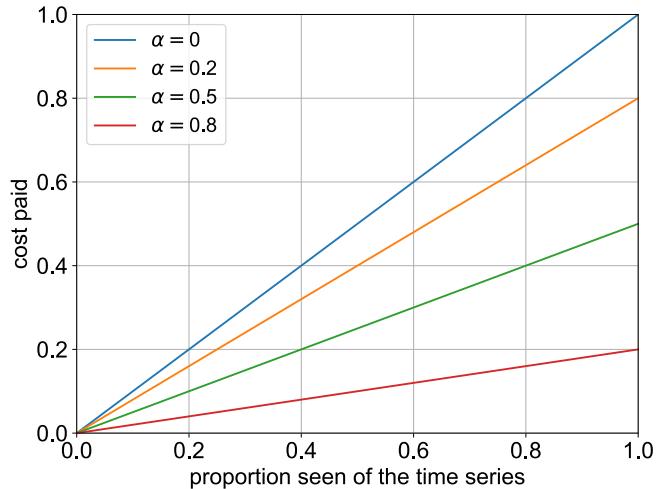
Z normalized version of the proposed datasets collection



Imbalanced version of datasets collection

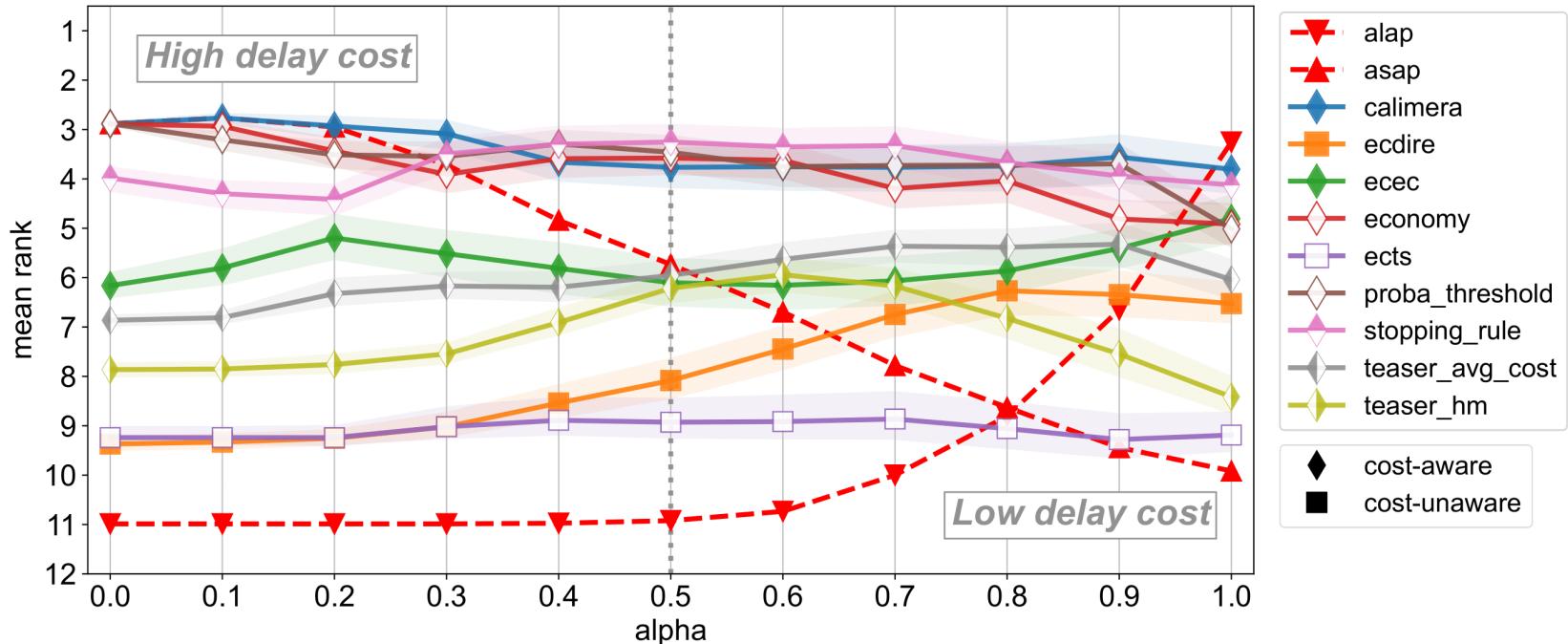
Experiments :

Balanced misclassification and linear delay costs



Experiments :

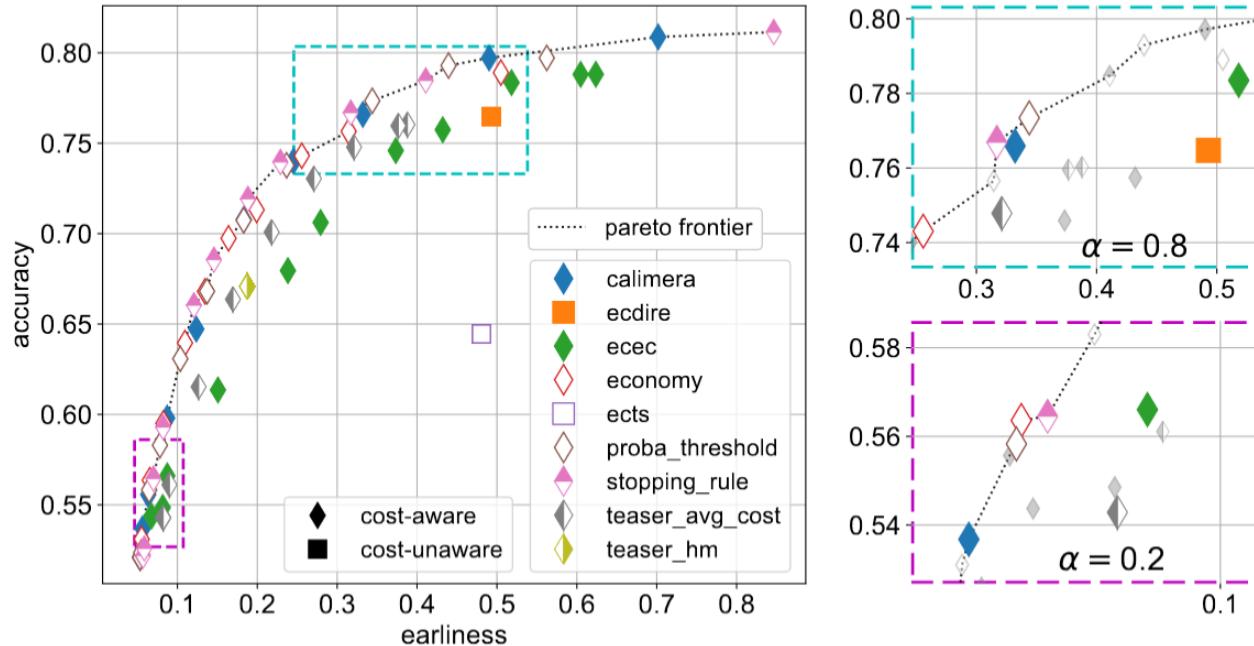
Balanced misclassification and linear delay costs



- The ASAP and ALAP baselines disqualify numerous approaches for a large range of alpha.
- Proba_threshold belongs to the top group in this balanced cost setting.

Experiments :

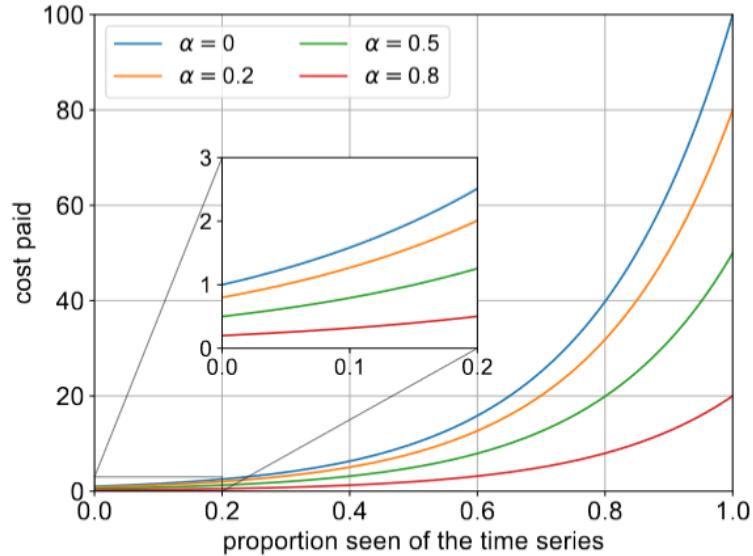
Balanced misclassification and linear delay costs



- Different compromise between earliness and accuracy are reached by competing approaches.
- Most of approaches are close to the Pareto front.

Experiments :

Unbalanced misclassification and exponential delay costs



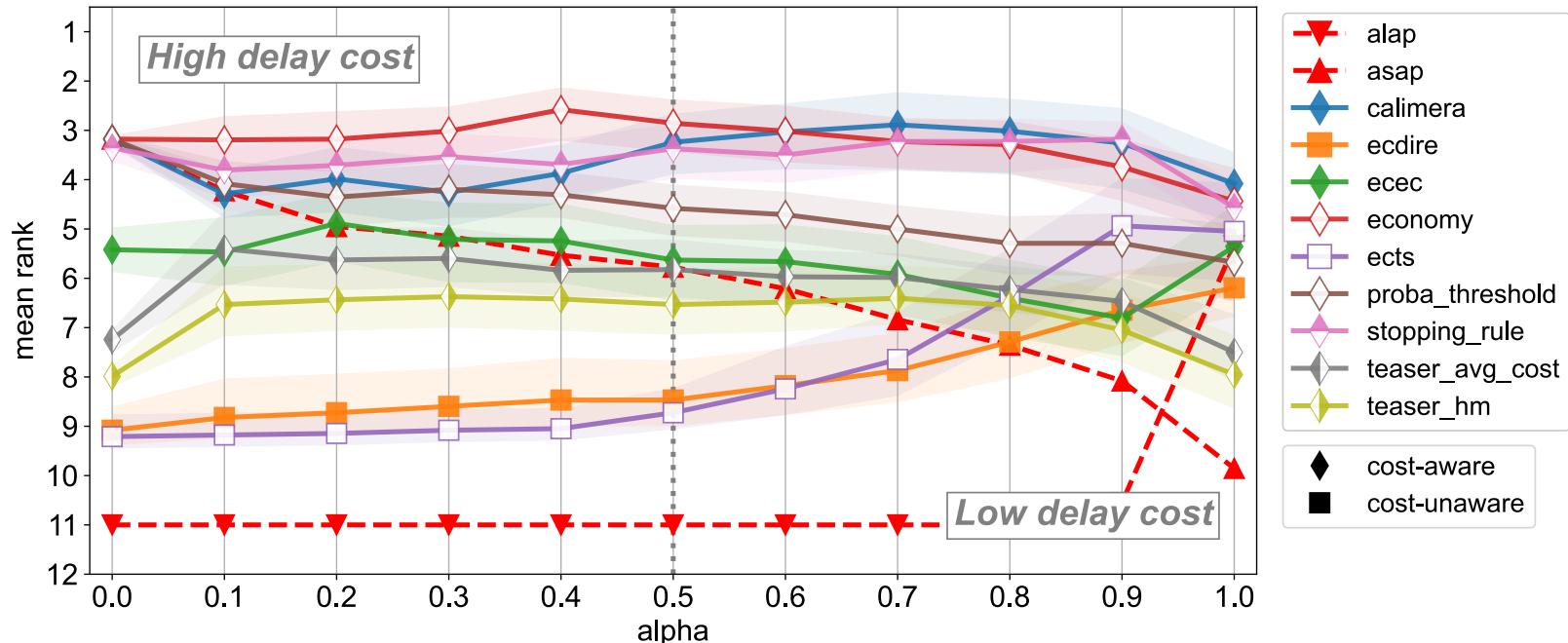
(a) Exponential delay cost

	predicted class 0	predicted class 1	predicted class 2
true class 0	0	α	α
true class 1 (anomaly)	100α	0	100α
true class 2	α	α	0

(b) Misclassification cost matrix

Experiments :

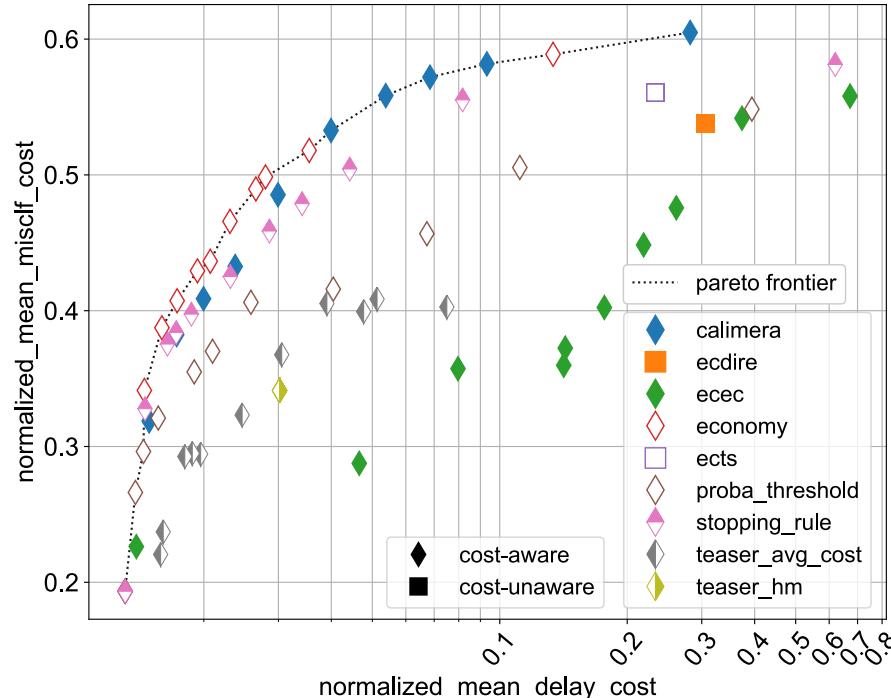
Unbalanced misclassification and exponential delay costs



- Proba_threshold becomes easier to beat in this unbalanced cost setting.
- The non-myopia seems to be an advantageous property (see the top group)

Experiments :

Unbalanced misclassification and exponential delay costs



- The Pareto front confirms the advantage of non-myopia

Other experiments :

Intermediary results
<i>Derived from 1.</i>
1.1 Removing calibration
1.2 Impact of base classifier
1.3 Impact of stratified train/test splits
1.4 Impact of z -normalization
<i>Derived from 2.</i>
2.1 Exponential delay cost only
2.2 Imbalanced cost only
2.3 Standard cost setting



→ The baseline proba_threshold is penalized



→ Low impact of classifier choice



→ Less significance in statistical tests

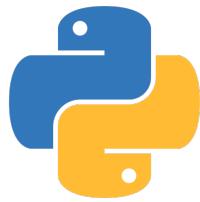


→ No significant temporal leakage revealed



Future works :

- Evaluate competing approaches for additional cost setting
 - Cost drift
 - Noisy costs
- Cost sensitive classification stage
- Improve existing ECTS approaches (ex: Calimera).
- Generalization of the ECTS problem ... (see next slides)



#5 Python Library

Open source library



https://github.com/ML-EDM/ml_edm/



#6 ML based Early Decision Making



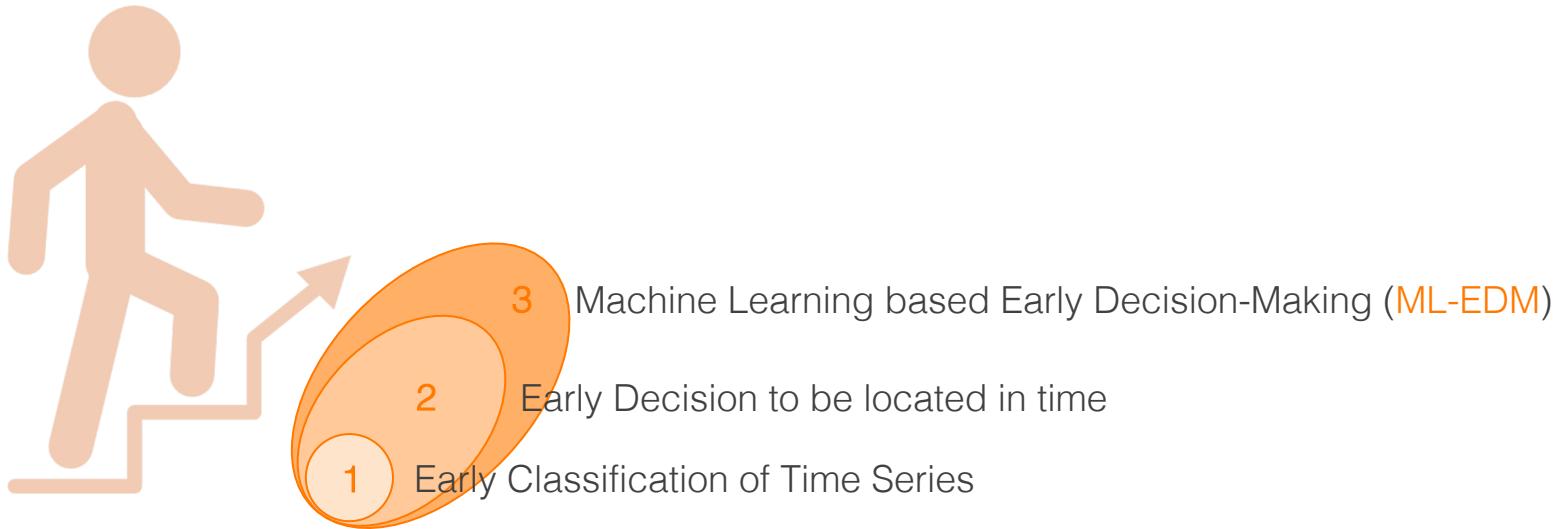
video playlist



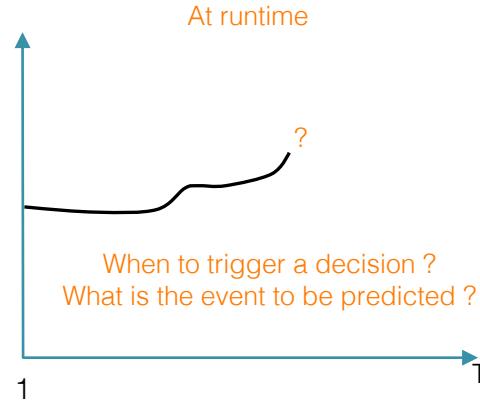
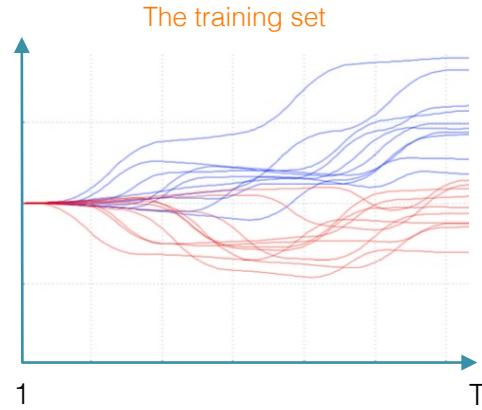
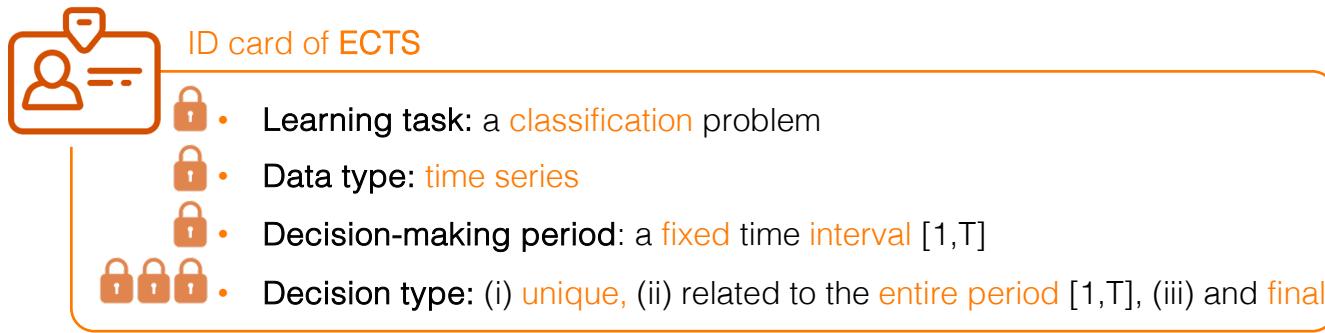
Open challenges for machine learning based early decision-making research.
Bondu, A., Achenchabe, Y., Bifet, A., Clérot, F., Cornuéjols, A., Gama, J., ... &

ACM SIGKDD Explorations Newsletter, 24(2), 12-31.
Marteau, P. F. (2022).

Let's present a progression of three problems, toward ML-EDM



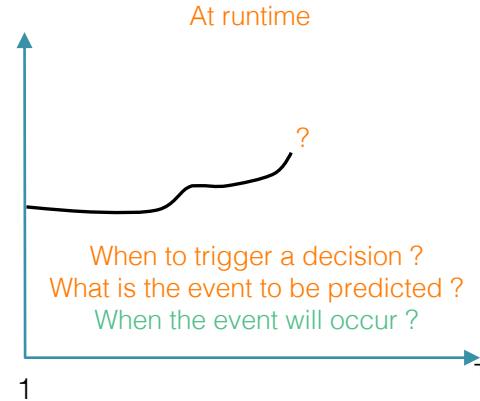
Problem #1 : ECTS is our starting point



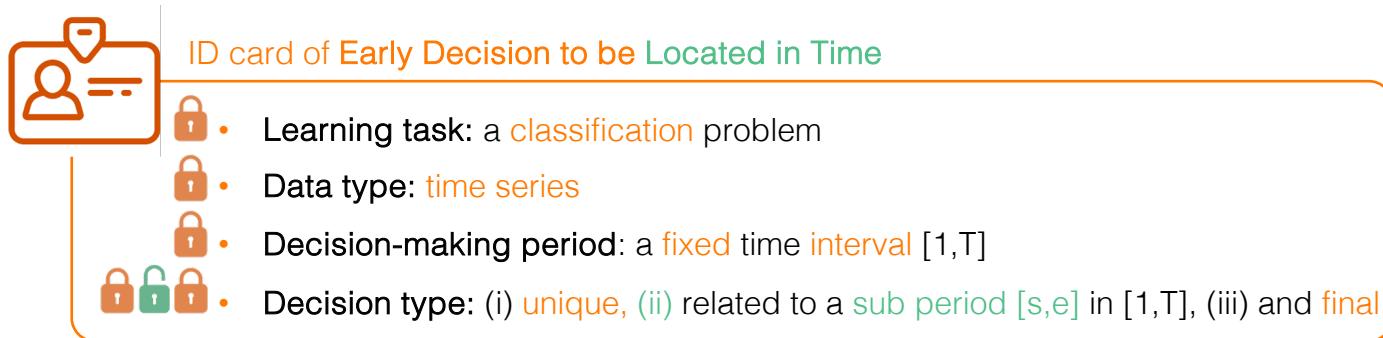
Problem #2 : Let's localize our decisions, while keeping them early ...

ID card of Early Decision to be Located in Time

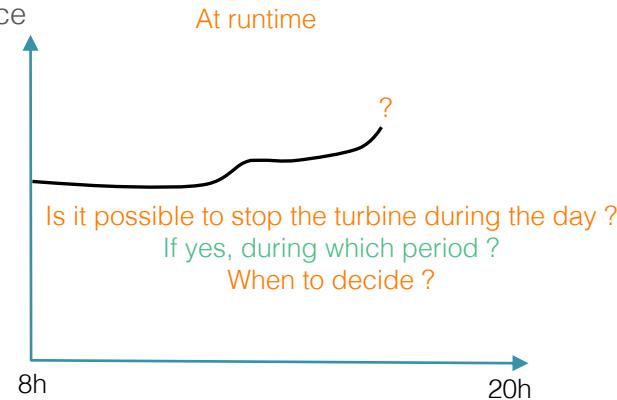
- Learning task: a classification problem
- Data type: time series
- Decision-making period: a fixed time interval $[1, T]$
- Decision type: (i) unique, (ii) related to a sub period $[s, e]$ in $[1, T]$, (iii) and final.



Problem #2 : Let's localize our decisions, while keeping them early ...



Example: In a hydroelectric dam, turbines can be stopped for maintenance operations, only if the electricity demand is low enough.



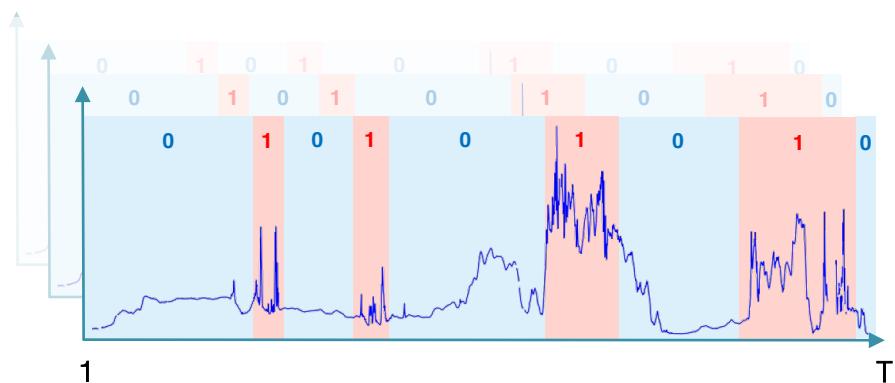
Problem #3 : Let's consider multiple early decisions with ML-EDM



ID card of ML-EDM: Early Multiple Decision to be Located in Time

- Learning task: a classification problem
- Data type: time series
- Decision-making period: a fixed time interval $[1, T]$
- Decision type: (i) multiple, (ii) related to a sub period $[s, e]$ in $[1, T]$, (iii) and final.

The training set made of such examples:

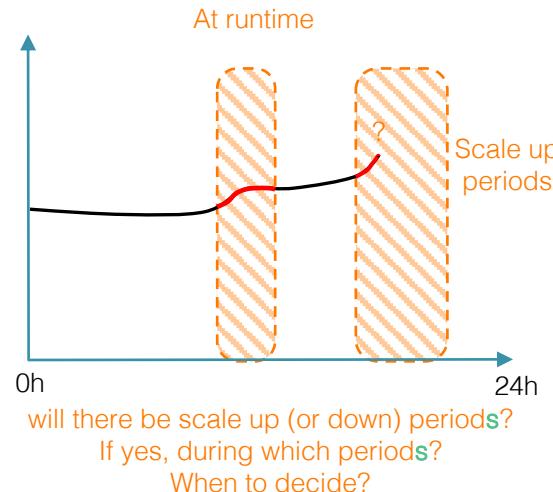
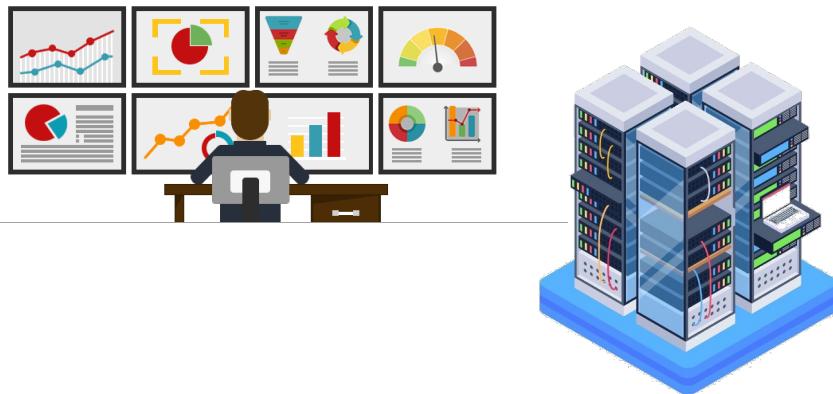
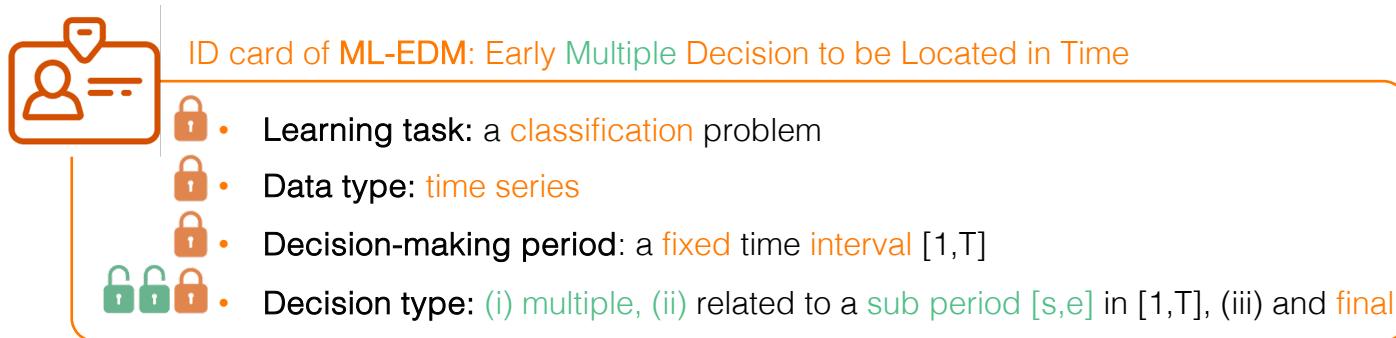


At runtime

When to trigger a new decision ?
What is the new event to be predicted ?
When each event will occur ?



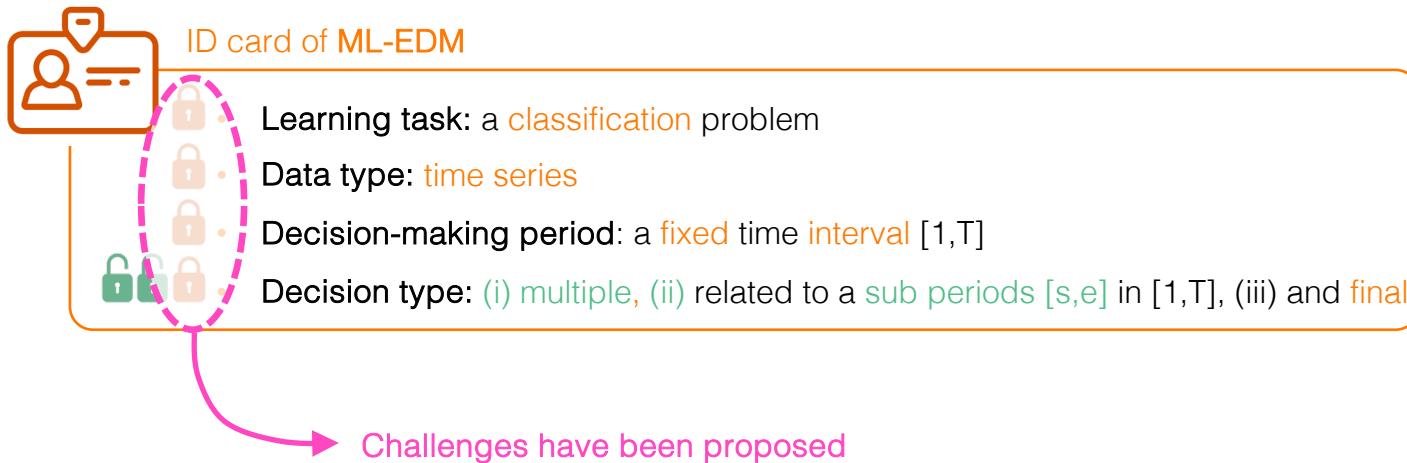
Problem #3 : Let's consider multiple early decisions with ML-EDM



Example: Using a cloud platform, identify as soon as possible the periods when it is necessary to scale up or down the number of nodes.

Overview of the proposed ML-EDM Challenges

We have defined what the ML-EDM problem is



Conclusion : overview of the proposed challenges

#1- Extending non-myopia to unsupervised approaches

#5 – Online prediction to be located in time

#8 – Reactivity vs. stability dilemma for revocable decisions

#2- Addressing other supervised learning tasks

#6 – Online accuracy vs. earliness trade-off

#9 – Non-myopia to revocation risk

#3- Early Weakly Supervised Learning

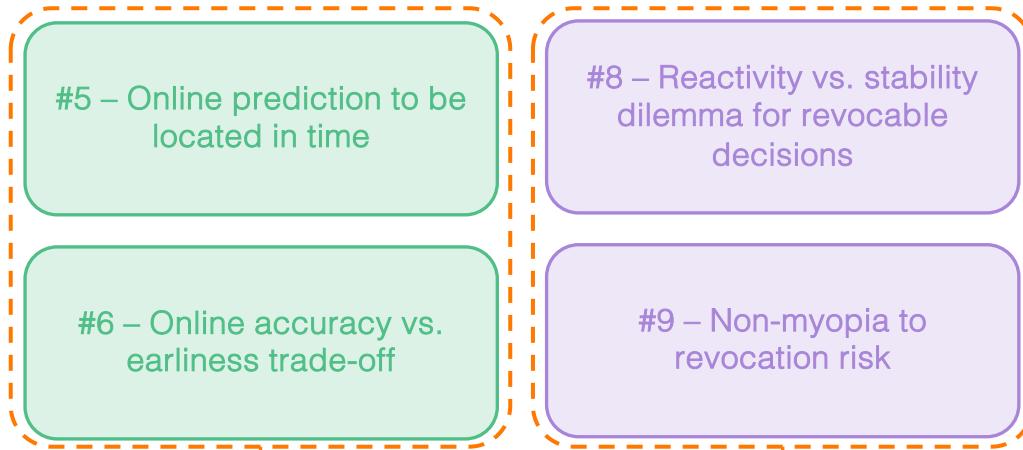
#7 – Management of non-stationarity in ML-EDM

#10 – Time-dependent decision costs

#4 – Data type agnostic ML-EDM

- Related to the learning task
- Related to the online setting
- Related to revocable decisions

One more thing ?



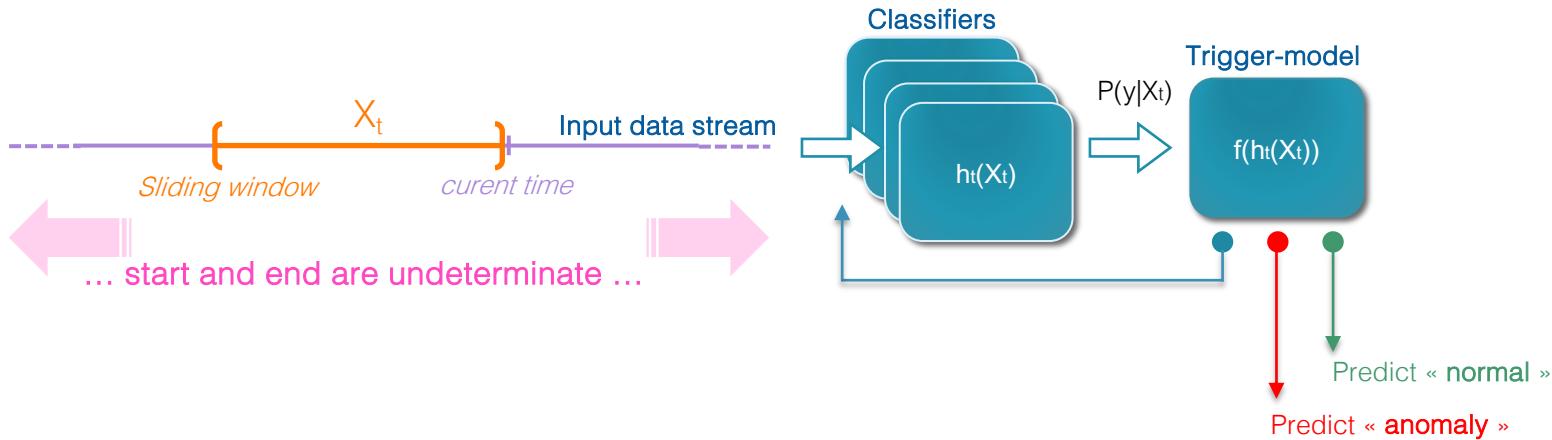
#2 ECTS with revocable decisions

#1 Early decision on open time series

Appendix #1

Early decision on open time series

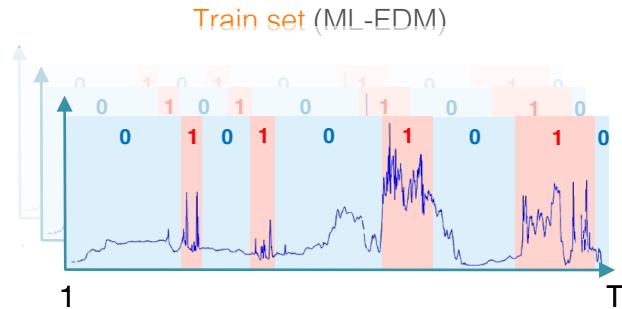
Data stream can be considered



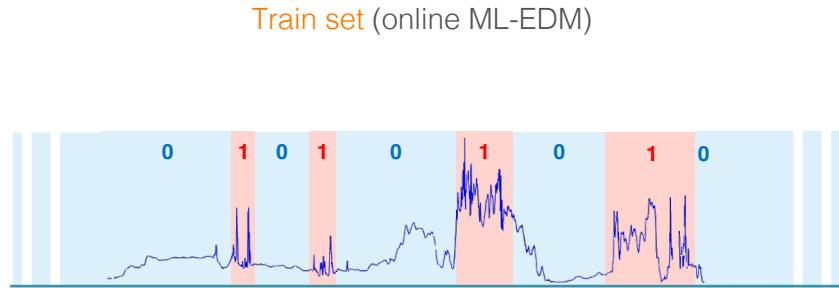
Data stream should be considered, to enable important applications



Example: continuous monitoring.

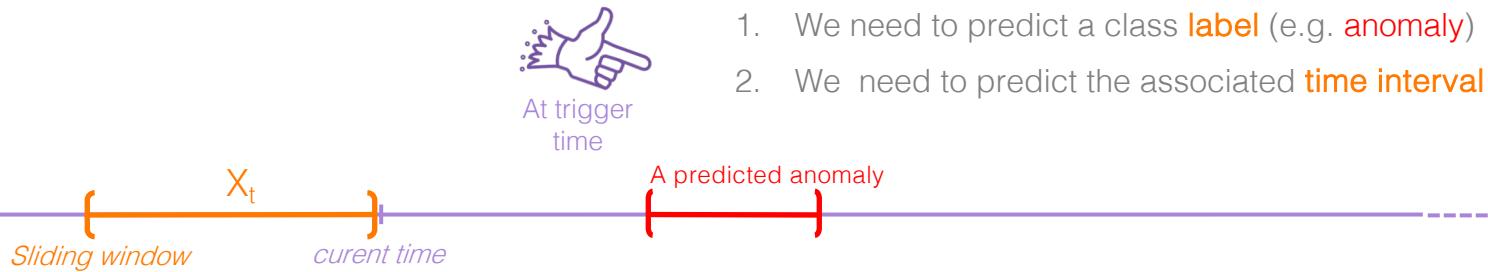


Historical data is split into periods of size T to form a collection of training examples



Historical data is considered in its fullness, in a continuous way (i.e. without any a priori splitting)

A complex kind of prediction

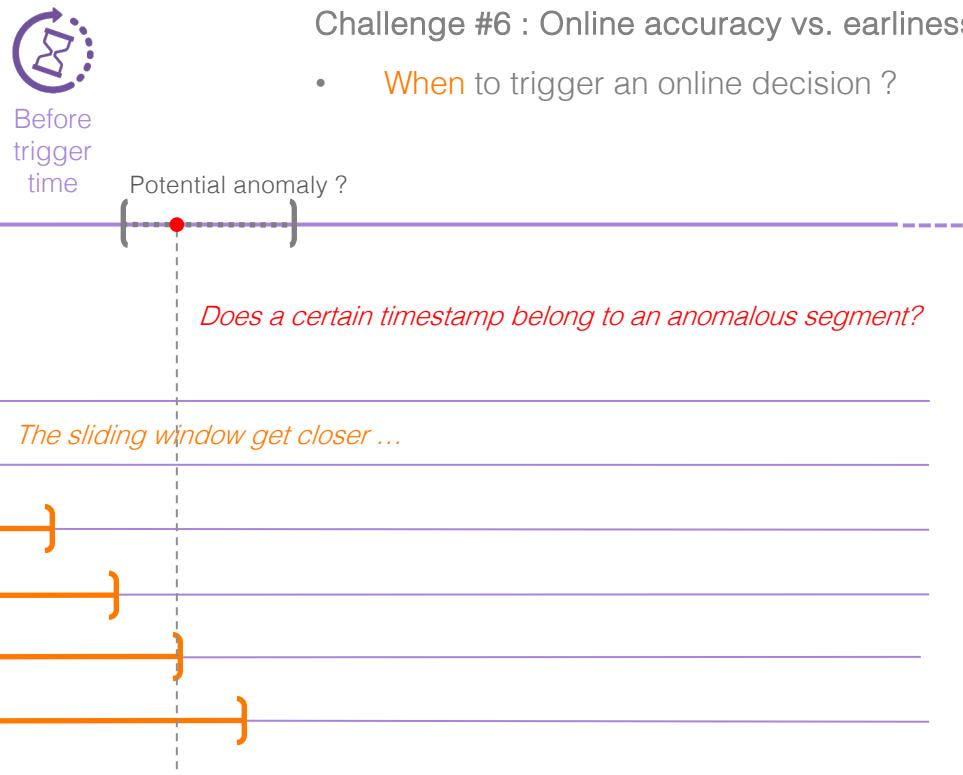


Challenge #5 : Online prediction to be located in time

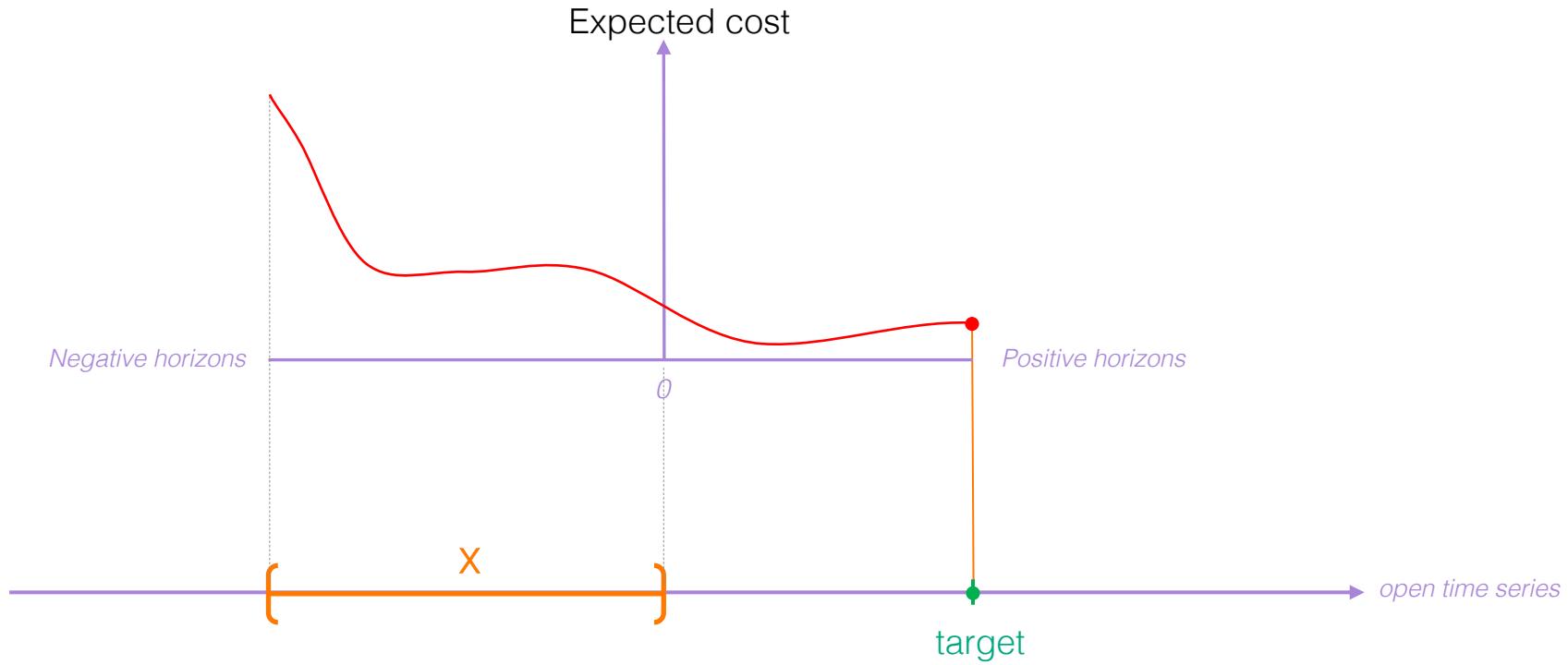
1. We need to predict a class **label** (e.g. **anomaly**)
2. We need to predict the associated **time interval**



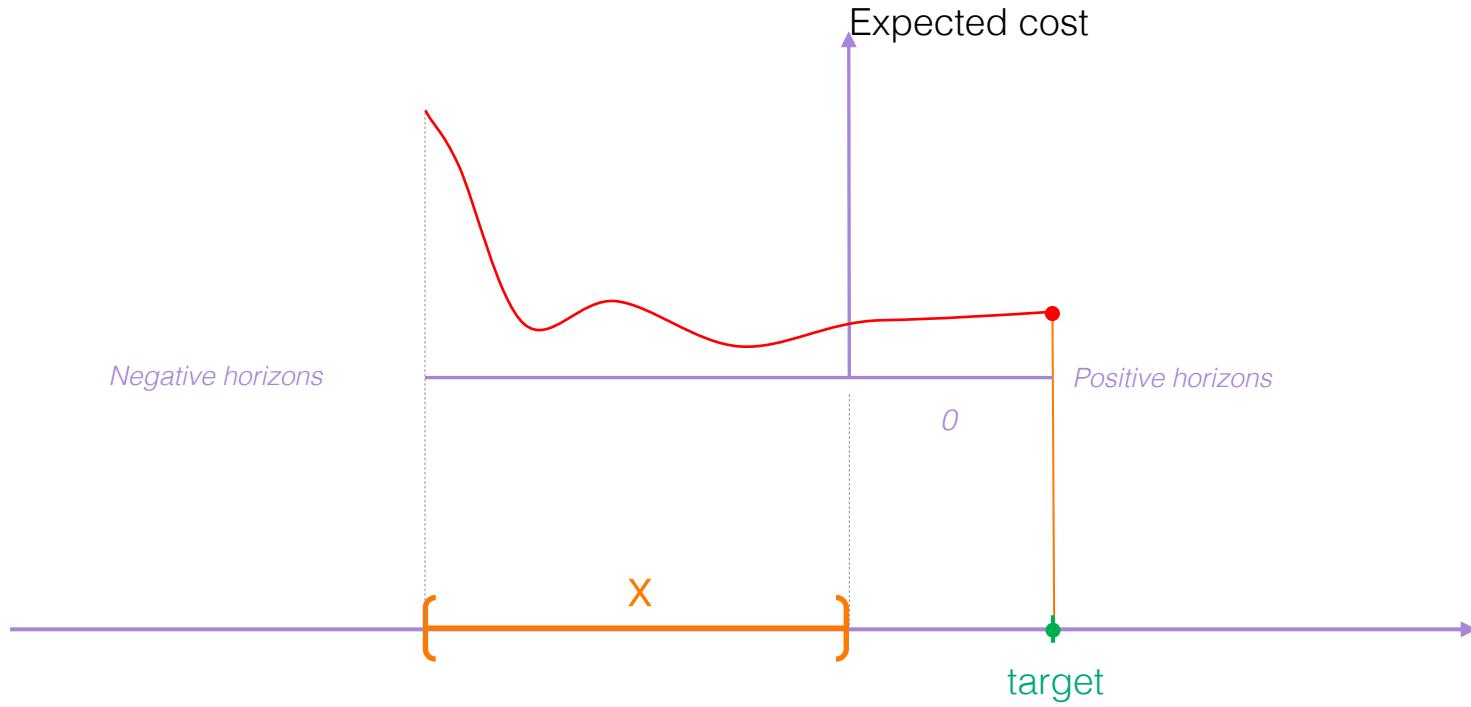
What is precocity in this case?



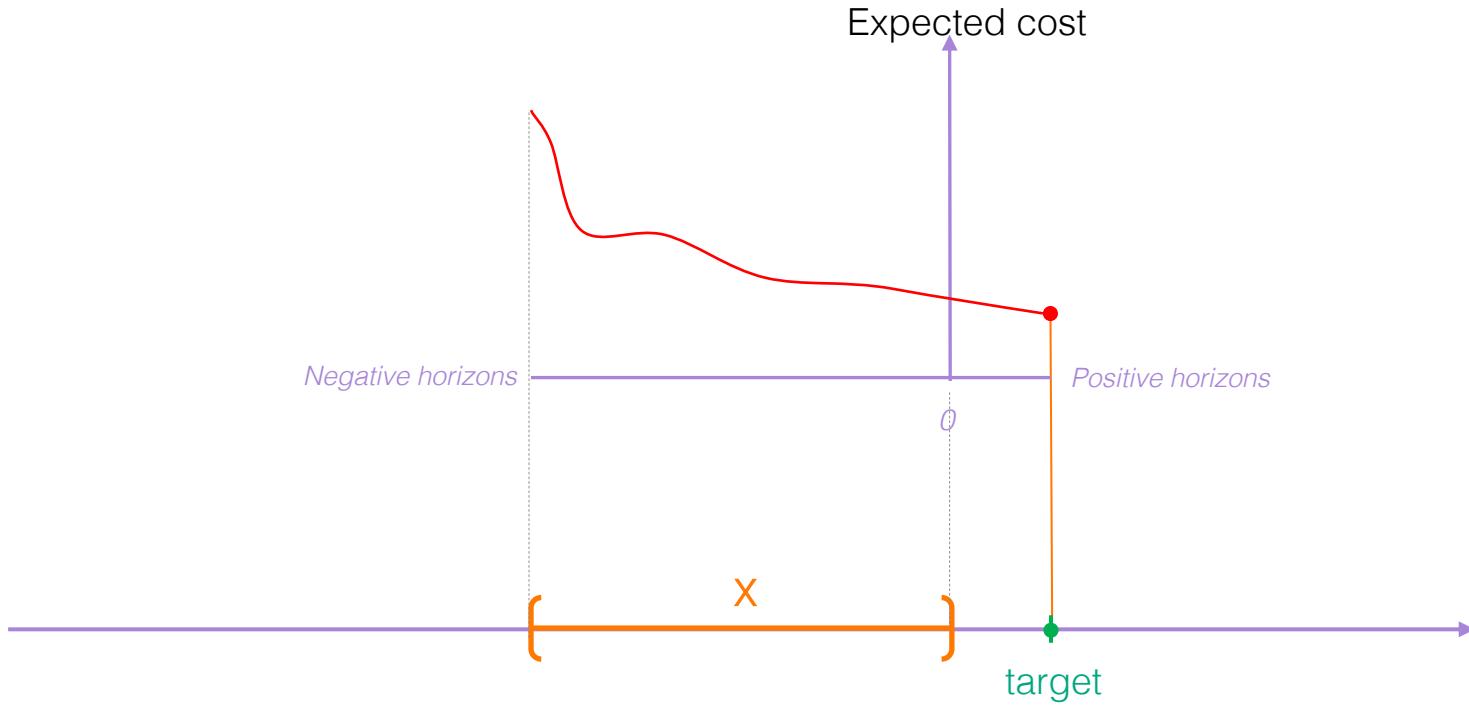
What is non-myopia in this case?



What is non-myopia in this case?



What is non-myopia in this case?



Experiments : Dataset

- Real dataset from one of the **schwan's** Factories (Frozen food industry corporation).
- 100 multivariate open time series associated with **100 machines** monitored for a period of 1 year, labeled periods of failure.
- **Features** include pressure, rotation, voltage, vibration, presence of a device error.



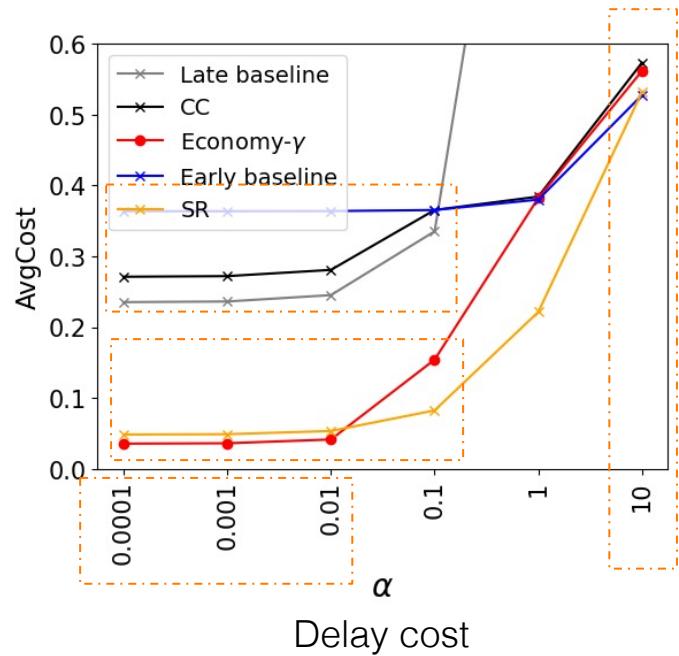
Source: Google images

Experiments : Competing approaches

- Baselines:
 - Late baseline
 - Early baseline
- Adapted methods from ECTS:
 - Economy- γ [Achenchabe et al.]
 - SR [Mori et al.]
- CC (Consecutive classifiers): basic threshold based approach

Experimental results

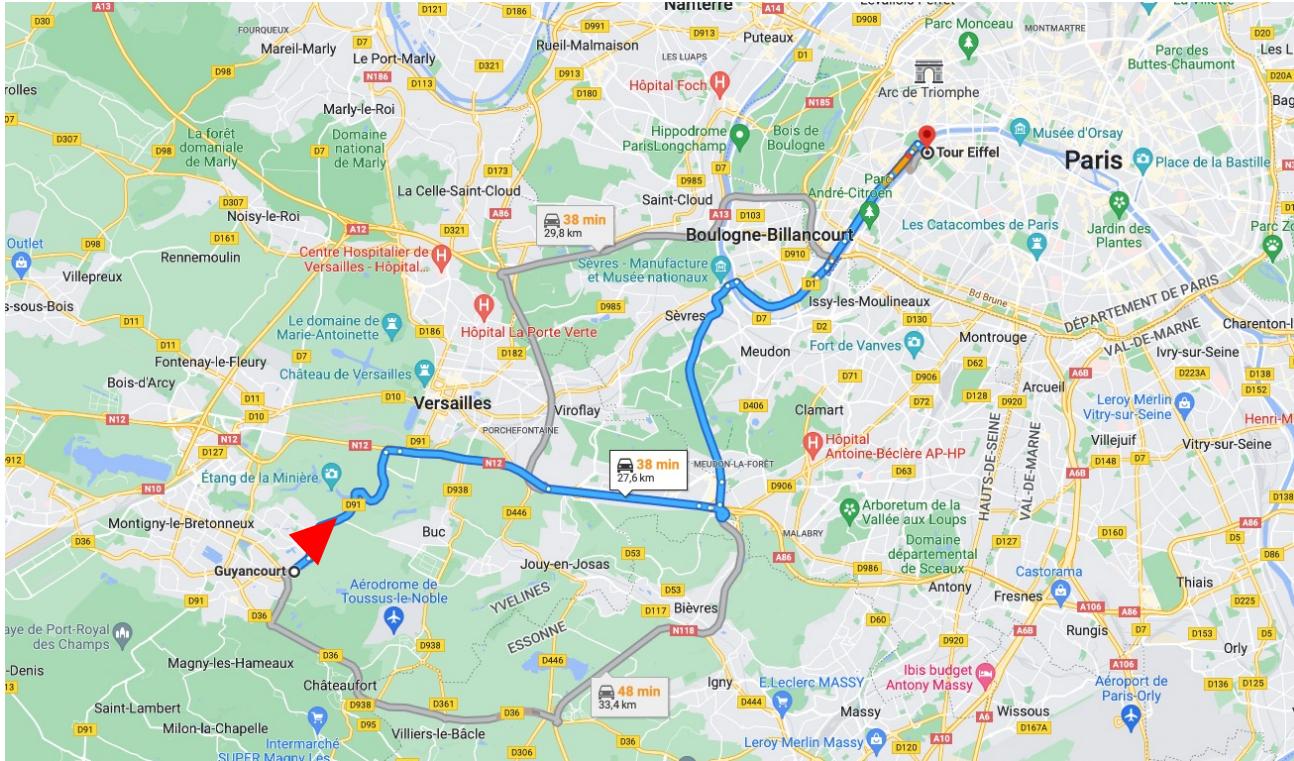
- When the cost of delaying decision is high, the optimal strategy is the ``early'' baseline.
- When the delay cost is low, taking late decisions is a good strategy even though it is not optimal.
- The CC method essentially switches from one baseline strategy to the other one as the delay cost increases.
- Both methods adapted from ECTS: Economy- γ and SR, noticeably overcome CC.



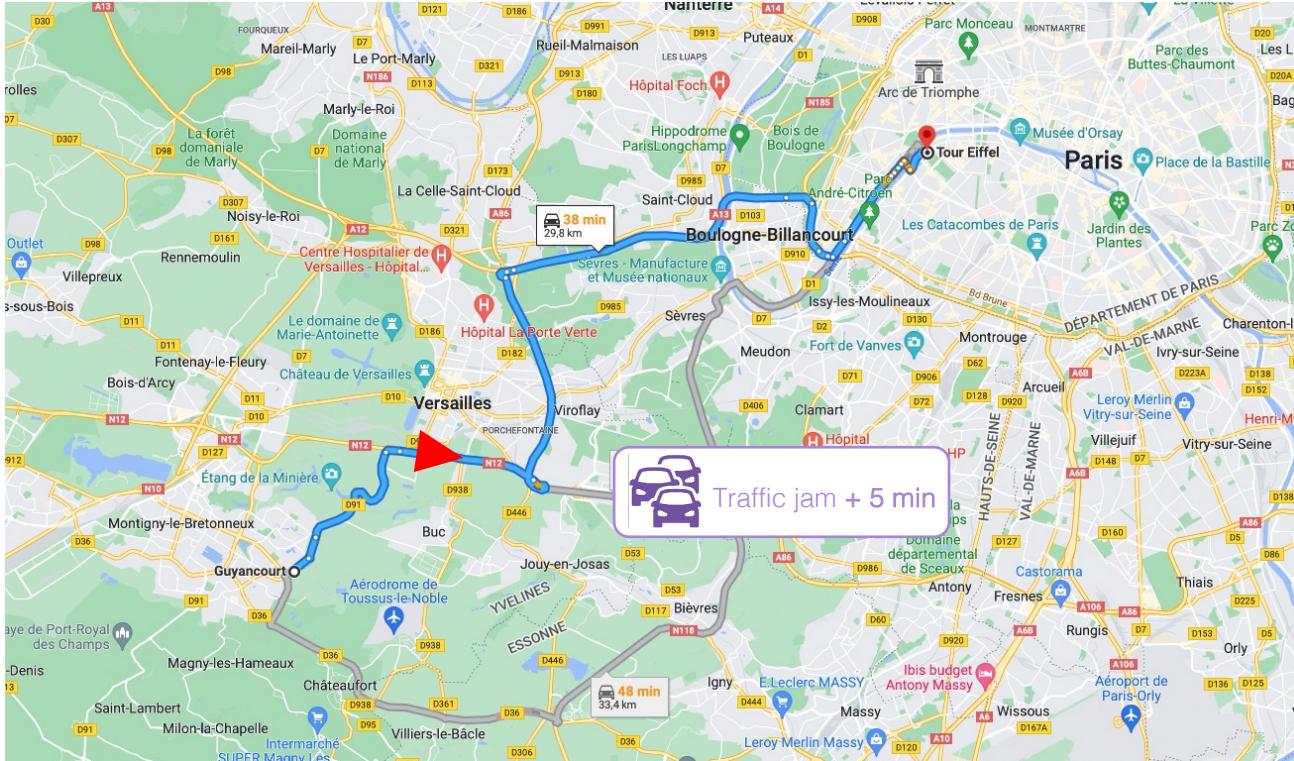
Appendix #2

ECTS with revocable decisions

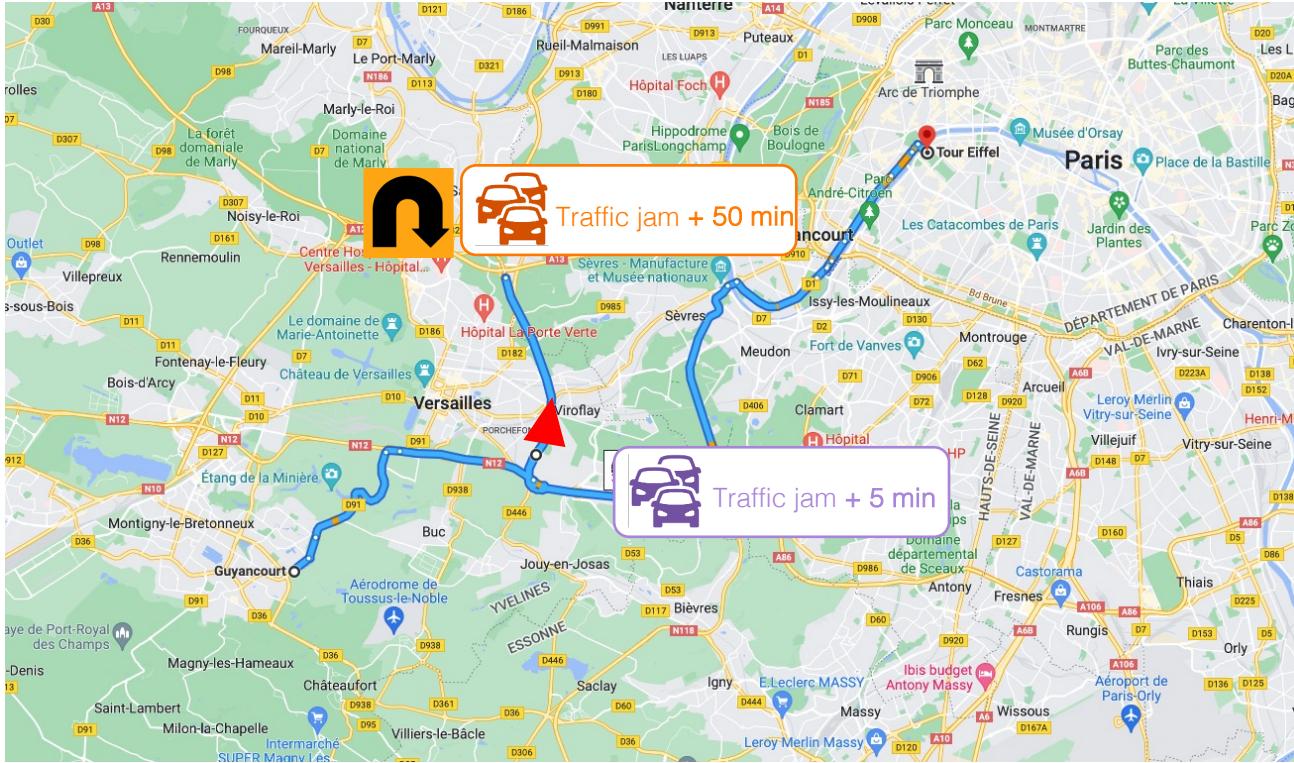
What is revoking a decision?



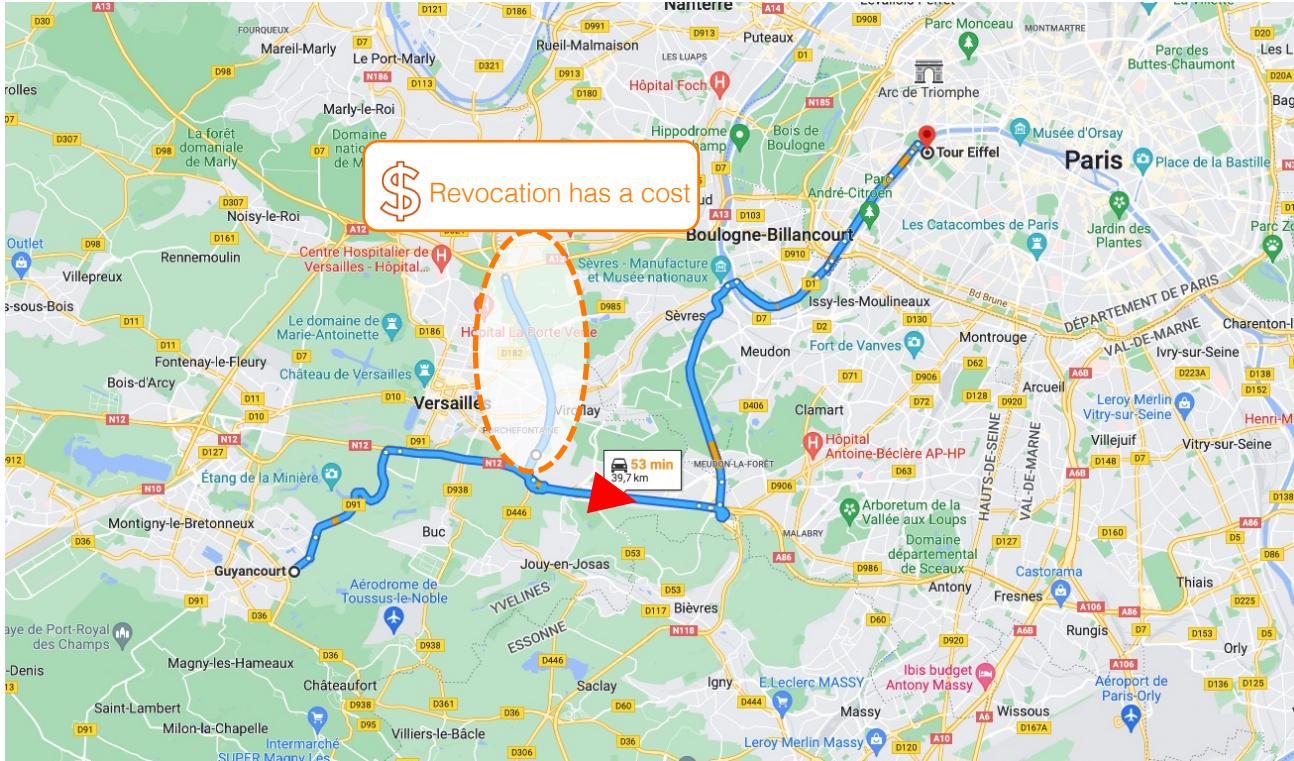
What is revoking a decision?



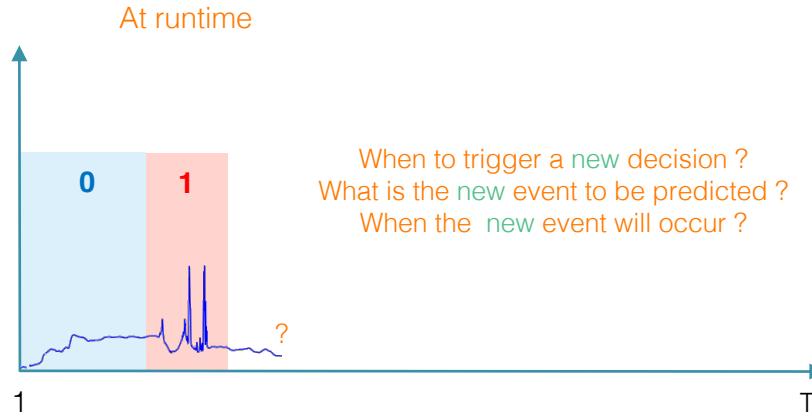
What is revoking a decision?



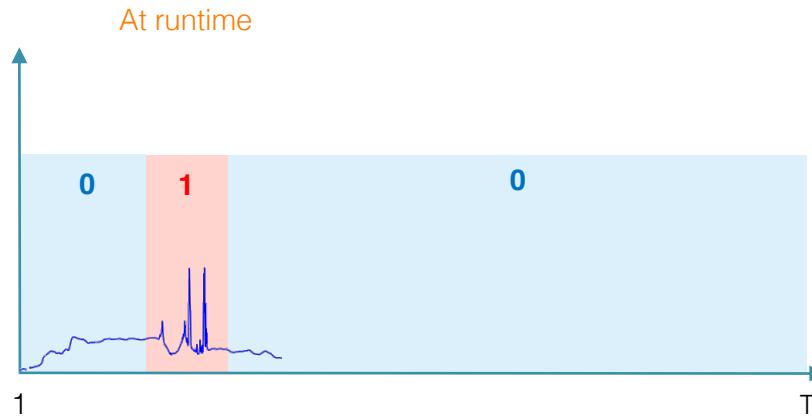
What is revoking a decision?



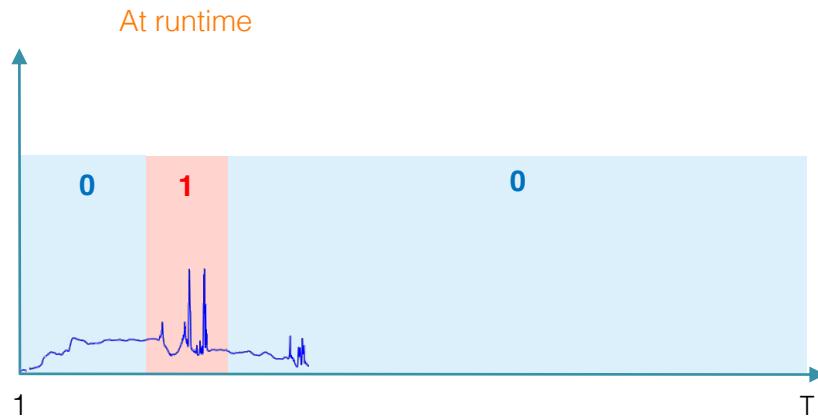
Back to ML-EDM, with revocable decisions



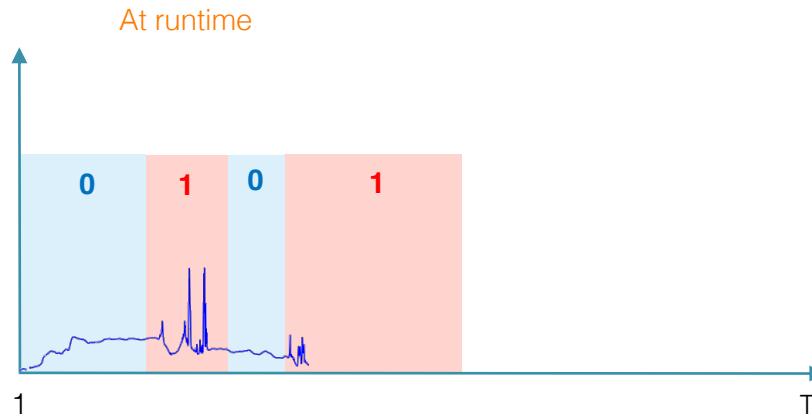
Back to ML-EDM, with revocable decisions



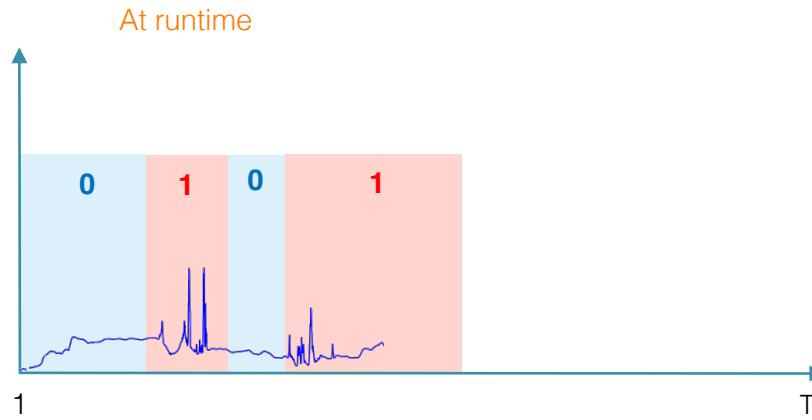
Back to ML-EDM, with revocable decisions



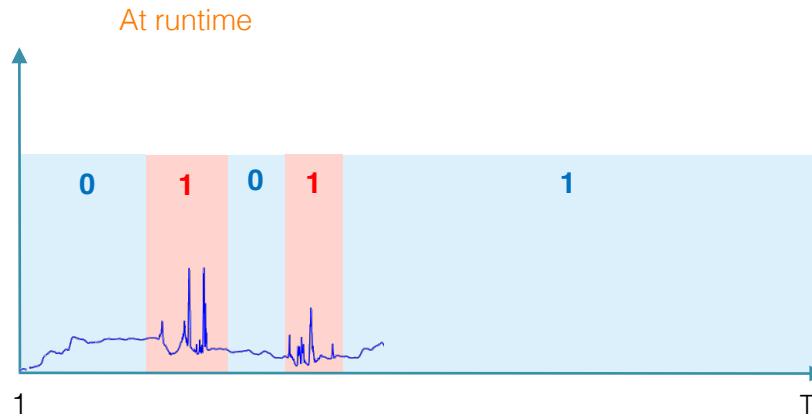
Back to ML-EDM, with revocable decisions



Back to ML-EDM, with revocable decisions



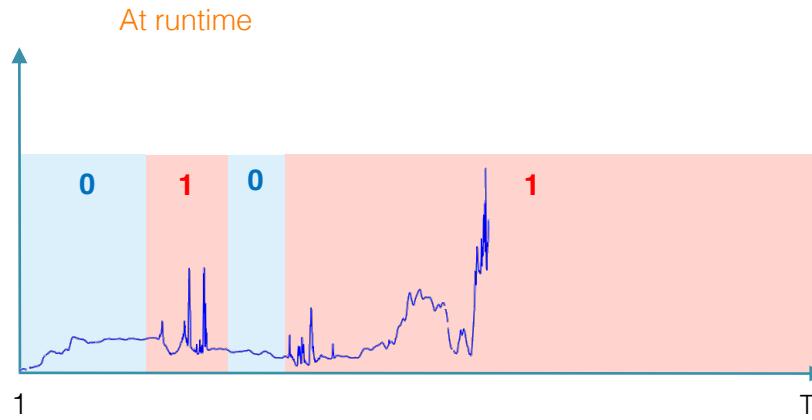
Back to ML-EDM, with revocable decisions



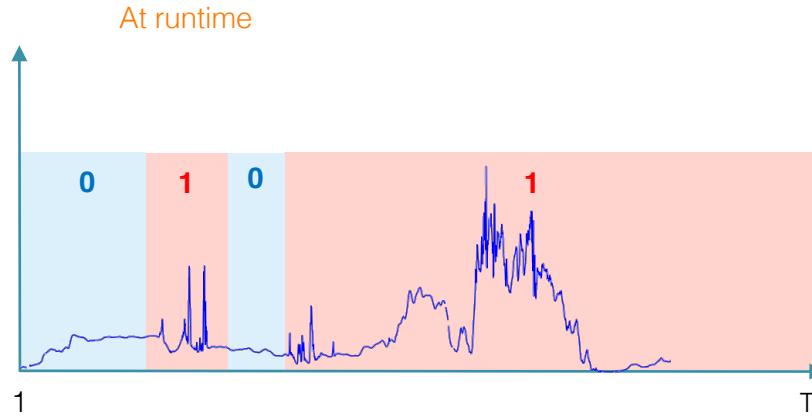
Back to ML-EDM, with revocable decisions



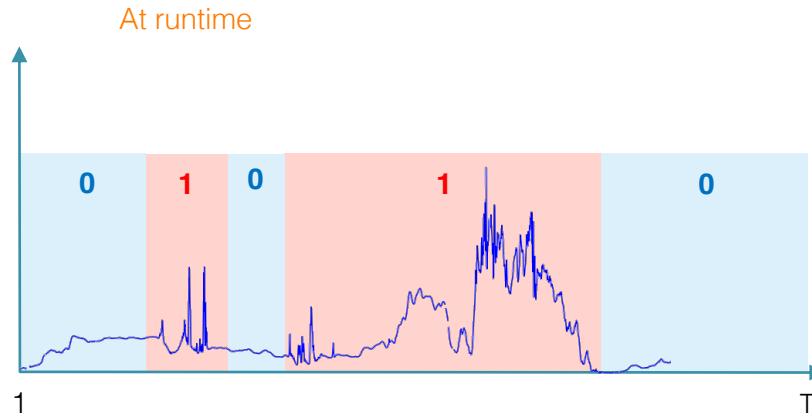
Back to ML-EDM, with revocable decisions



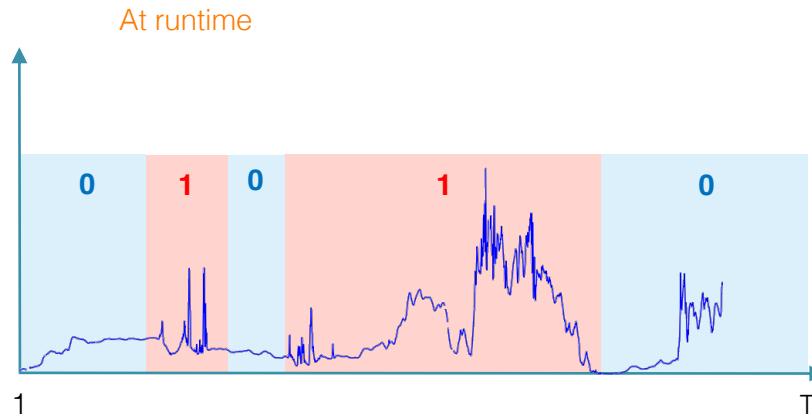
Back to ML-EDM, with revocable decisions



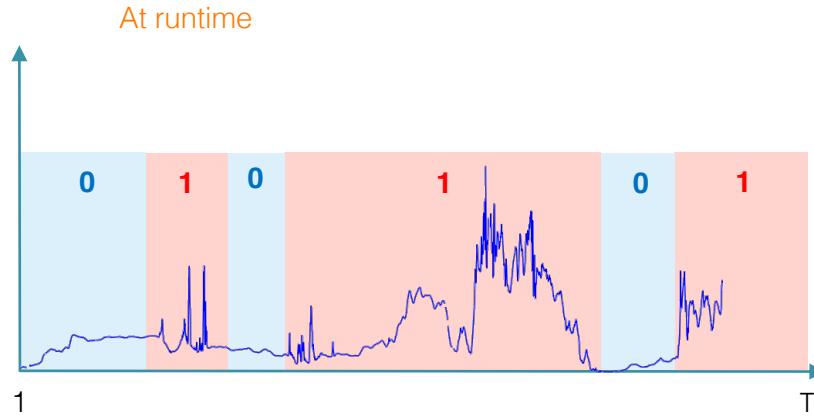
Back to ML-EDM, with revocable decisions



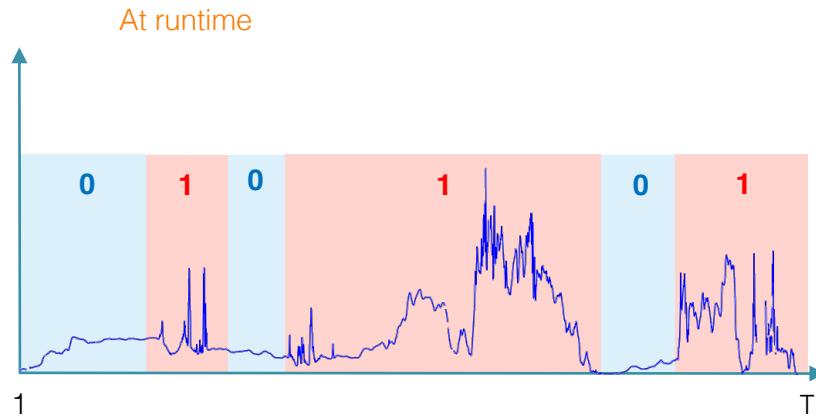
Back to ML-EDM, with revocable decisions



Back to ML-EDM, with revocable decisions



Back to ML-EDM, with revocable decisions



Back to the simple case of ECTS, with the ECONOMY approach extended to revocable decisions

Miss classification costs

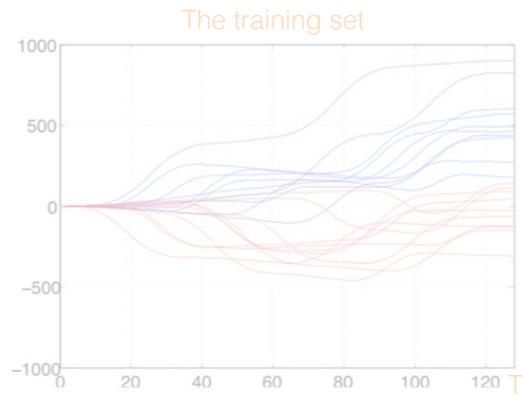
\hat{y}/y	1	0
1	10	5
0	100	0

Cost of changing a decision

$\hat{y}_1 \hat{y}_2$	1	0
1	0	5
0	1	0

$$C_{cd}(\hat{y}_1|\hat{y}_2) : \mathcal{Y} \times \mathcal{Y} \rightarrow R$$

An additional input :



Challenge #8: Reactivity vs. stability dilemma for revocable decisions

- How to combat **too frequent** changes and **unstable** decisions?



Back to the simple case of ECTS, with the ECONOMY approach extended to revocable decisions

What's new in the decision criterion ?

$$f_{\tau}^{\text{rev}}(\mathcal{D}_k, \tilde{t} | \mathbf{x}_t) = \mathbb{E}_{\substack{(\hat{y}, y) \in \mathcal{Y}^2}}^{t+\tau} [C_m(\hat{y}|y)| \mathbf{x}_t] + \sum_{\substack{i=1 \\ \hat{y}_{t_i}, \hat{y}_{t_{i+1}} \in \mathcal{D}_k}}^{k-1} C_{cd}(\hat{y}_{t_{i+1}}|\hat{y}_{t_i}) + \mathbb{E}_{\hat{y} \in \mathcal{Y}}^{t+\tau} [C_{cd}(\hat{y}|\hat{y}_{t_k})| \mathbf{x}_t] + C_d(\tilde{t})$$

Expected misclassification cost at $t+\tau$

The cost of **past** decision changes

Expected cost of changing a decision at the **future** time steps « $t+\tau$ »

Delay cost

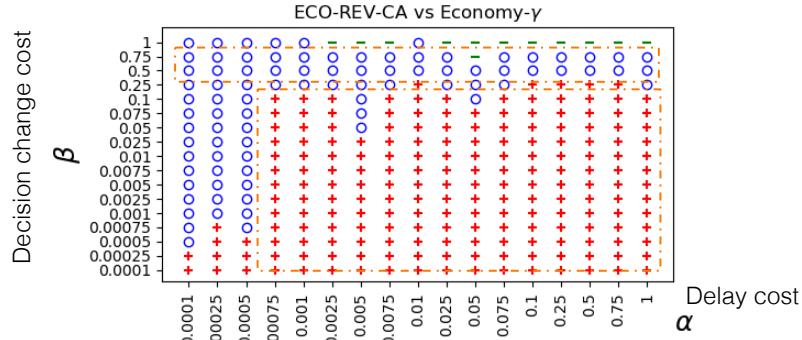
We consider the entire sequence of decisions

Challenge #9: Non-myopia to revocation risk

- How to **delay** a decision that **risks** being **revoked** later?

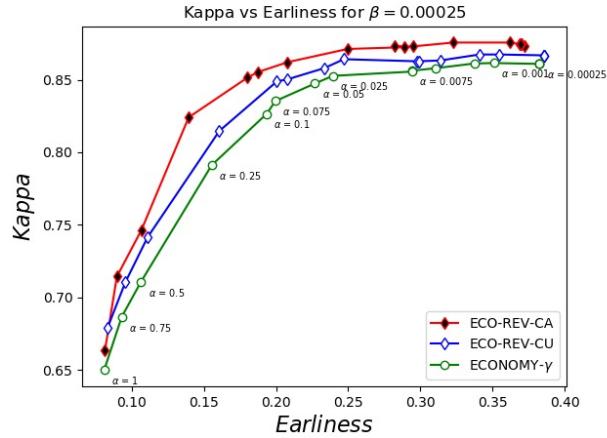


Back to the simple case of ECTS, with the ECONOMY approach extended to revocable decisions



- +: Statistically significant difference in favor ECO-REV-CA
- : Statistically significant difference in favor of ECO-gamma
- o: No significant difference

Results of statistical testing significance for multiple combinations of delay and misclassification costs



Predictive performance against earliness
for multiple values of the delay cost

