Presentation of Assignment 1

Henri Bunting, Martin Lundfall, Malte Siemers

November 4, 2015

2.1

a

Linear functions can always be concatenated and a network with linear transfer functions can only approximate linear functions. Given enough layers and neurons with nonlinear transfer functions, the network can model any function within a certain accuracy.
Examples, that need nonlinear transfer functions include image classification or speech recognition.

b

Consider a simple neural network with two input neurons that can both either be 0 or 1 and one output layer. We want to construct an AND gate with our network, so without bias our quest would be to find $w = (w_1, w_2)$ such that:

$$\begin{aligned} 0 &\leq 0 \\ w_1 &\leq 0 \\ w_2 &\leq 0 \\ w_1 + w_2 &> 0 \end{aligned}$$

which is impossible. We can easily however create the network with a bias, if we have the weights $w = (1, 1)$ and the bias $\theta = \frac{3}{2}$. Then $sgn(w^T x - \theta)$ would give us AND.

w_0							1.5
w_1		0	1	0	1		1
w_2		0	0	1	1		1
0 0	-	-	-	-	-		-
0 1	-	-	-	+	+		-
1 0	-	-	+	-	+		-
1 1	+	-	+	+	+		+

c

Point and edge filters are for example a connectionist neuron which gets values of a scalar field as input, that represent the color of each pixel or the color gradient or even a higher derivative and has weights in the following form: In the simple case of two colors (0 and 1) this point filter would

-1	-1	-1
-1	+8	-1
-1	-1	-1

point filter

-1	0	+1
−2	0	+2
-1	0	+1

+1	+2	+1
0	0	0
-1	−2	-1

edge filter (Sobel filter)

return zero for no point, 1 or -1 for a point in the outer region and 8 or -8 if the point is in the middle. This goes analogously for the other filter.

d

The first is deterministic and the second has a noise parameter and can return different states for set parameters and a given input.

2.2

The following two figures refer to exercise parts a and b.

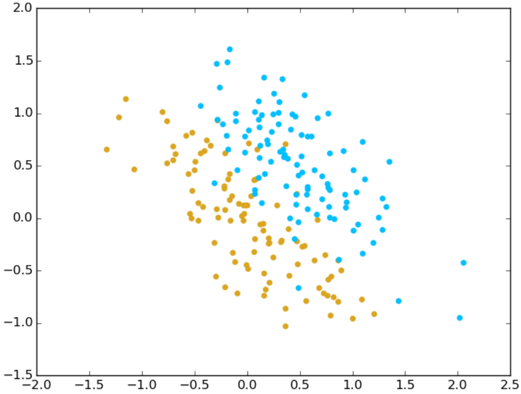

Figure 1: Plot where Y=1 (blue) and Y=0 (gold).

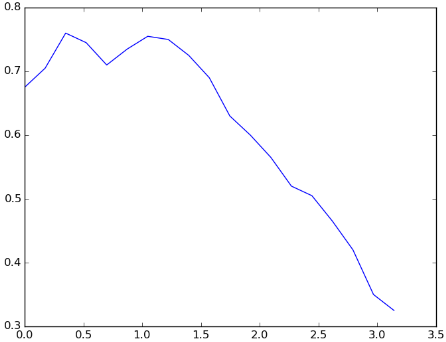

Figure 2: Classification performance given by $sign(w \cdot x)$ for varying angles determining w

c

The weight vector giving us the best performance is $w = (0.93969262, 0.34202014)$ if we optimize it without respect to θ.

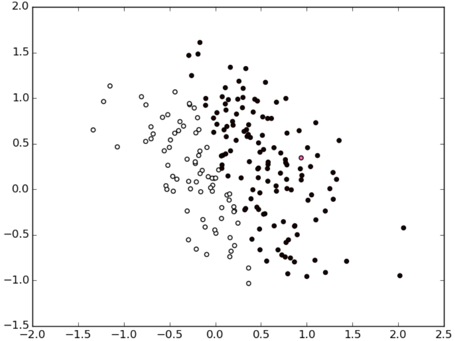

Figure 3: Classification performance with w and $theta$ optimized separately

e

If we optimize w and theta simultaneously we get a $p = 0.915$ classification rate with optimal parameters $w = (0.64278761, 0.76604444)$ and $\theta = 0.339339339339$

2.3

a

A MLP could decide between a horizontal and a vertical edge, whereas a perceptionist neuron would either be able to differ between vertical edge or no vertical edge OR horizontal edge or no horizontal edge.

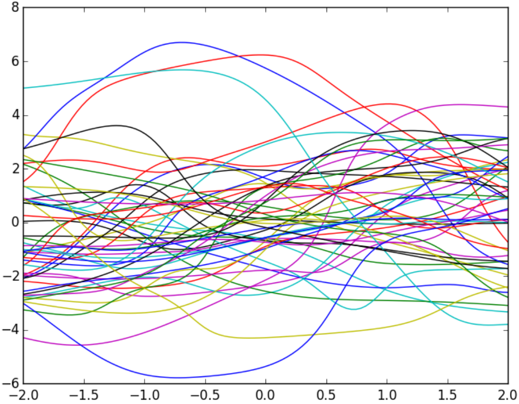

Figure 4: functions computed with normally distributed a_i with a standard deviation of 2

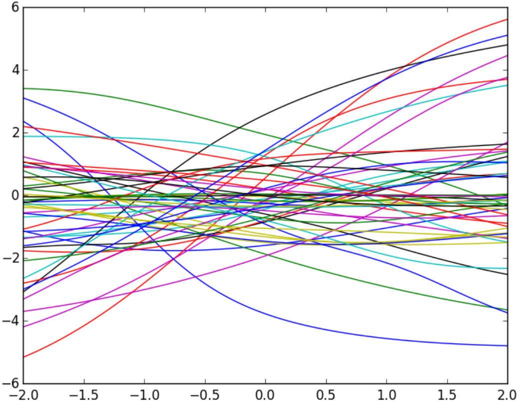

Figure 5: functions computed with normally distributed a_i with a standard deviation of 0.5

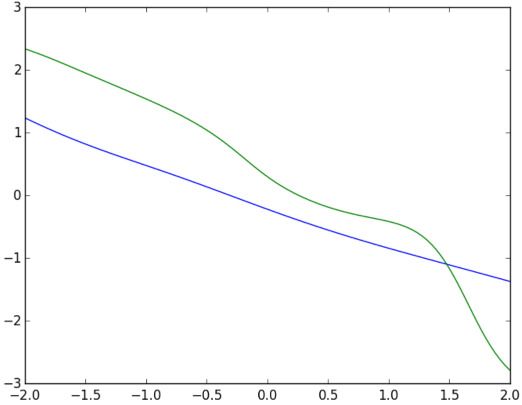

Figure 6: functions with least mean square error from f(x)=-x, computed with an std of 2 (green) and 0.5 (blue)

Questions?