

$$V = \{v_1, v_2 \dots v_n\}$$

$$V = \{c_i v_i\}$$

$$\{v_1 \dots v_n\} = \{v\}$$

①

since S is orthonormal,

taking dot product of V with any of the vectors in S .

$$V \cdot v_i = c_1 v_1 \cdot v_i + c_2 v_2 \cdot v_i + \dots + c_i v_i \cdot v_i + \dots + c_n v_n \cdot v_i$$

$$= 0 + 0 + c_i + \dots + 0 = c_i$$

$$= c_i$$

$$\therefore \boxed{c_i = V \cdot v_i}$$

$$\boxed{V \cdot V = 1}$$