Numpy for High Energy Physics

Romain Madar[1]

[1]Laboratoire de Physique de Clermont-Ferrand

January 3, 2019

Abstract

These notes describe the material presented in a numpy tutorial in the context of a working group at Laboratoire de Physique de Clermont related to machine learning and applications in physics. This tutorial is split into three parts, going from first principles to some limitations for High Energy Physics (HEP), and some possible workarounds. This tutorial reflects my current understanding and some newer/better approach might exist (feel free to contact me!). This tutorial assumes some basic knowledge of python. The code and these notes are accessible in https://github.com/MLatCezeaux/intro_numpy

Contents

1 Short introduction to `numpy`

```
import numpy as np
```

1.1 1. Motivations

Why `numpy`**?** Because it's very well optimized (and then fast) for numerical computations in python

Why python? Many tools available

1.2 2. The core object: arrays

1.2.1 2.1 Main differences with usual python lists

Addition of lists/arrays and multiplication by a number:

```
# Python list and numpy arrays to play with
l1, l2 = [1, 2, 3], [3, 4, 5]
a1, a2 = np.array([1, 2, 3]), np.array([3, 4, 5])


# helper function to print title
def print_title(title):
    print('-'*len(title))
    print(title)
    print('-'*len(title))


print_title('obj1+obj2')
print('  python lists: {}'.format(l1+l2))
print('  numpy arrays: {}'.format(a1+a2))
print('\n')
print_title('obj*2')
print('  python list: {}'.format(l1*2))
print('  numpy array: {}'.format(a1*2))
```

```
-----
obj1+obj2
-----
  python lists: [1, 2, 3, 3, 4, 5]
```

```
  numpy arrays: [4 6 8]


---
obj*2
---
  python list: [1, 2, 3, 1, 2, 3]
  numpy array: [2 4 6]
```

Slicing and indexing:

```
print_title('Indexing with an integer: obj[1]')
print('  python list: {}'.format(l1[1]))
print('  numpy array: {}'.format(a1[1]))
print('\n')

print_title('Indexing with a slicing: obj[slice(1,3))]')
print('  python list: {}'.format(l1[slice(1,3)]))
print('  numpy array: {}'.format(l1[slice(1,3)]))
print('\n')

print_title('Indexing with a list of integers: obj[[0,2]]')
print('  python list: IMPOSSIBLE')
print('  numpy array: {}'.format(a1[[0,2]]))
```

```
----------------
Indexing with an integer: obj[1]
----------------
  python list: 2
  numpy array: 2


---------------------
Indexing with a slicing: obj[slice(1,3))]
---------------------
  python list: [2, 3]
  numpy array: [2, 3]


---------------------
Indexing with a list of integers: obj[[0,2]]
---------------------
  python list: IMPOSSIBLE
  numpy array: [1 3]
```

1.2.2 2.2 Main caracteristics of a `np.array`

- `a.dtype`: type of data contained in the array
- `a.shape`: number of elements along each dimension
- `a.size`: total number of elements
- `a.ndim`: number of dimensions

```
a = np.array([[ 0,  1,  2,  3],
              [ 4,  5,  6,  7],
              [ 8,  9, 10, 11]])

print('a.dtype = {}'.format(a.dtype))
print('a.shape = {}'.format(a.shape))
print('a.size  = {}'.format(a.size))
print('a.ndim  = {}'.format(a.ndim))
```

```
a.dtype = int64
a.shape = (3, 4)
a.size  = 12
a.ndim  = 2
```

1.3 3. The three key features of `numpy`

1.3.1 3.1 Vectorization

The *Vectorization* is a way to make computations on numpy array **without explicit loops**, which are very slow in python. The idea of vectorization is to compute a given operation *element-wise* while the operation is called on the array itself. An example is given below to compute the inverse of 100000 numbers, both with explicit loop and vectorization.

```
a = np.random.randint(low=1, high=100, size=100000)

def explicit_loop_for_inverse(a):
    inv_a = []
    for element in a:
        inv_a.append(1./element)
    return np.array(inv_a)
```

```
# Using explicit loop
%timeit explicit_loop_for_inverse(a)
```

```
160 ms ± 3.82 ms per loop (mean ± std. dev. of 7 runs, 10 loops each)
```

```
# Using list comprehension
%timeit [1/x for x in a]
```

```
15.1 ms ± 328 µs per loop (mean ± std. dev. of 7 runs, 100 loops each)
```

```
# Using vectorization
%timeit 1.0/a
```

```
116 µs ± 7.77 µs per loop (mean ± std. dev. of 7 runs, 10000 loops each)
```

Many standard functions are implemented in a vectorized way, they are call the *universal functions*, or `ufunc`. Few examples are given below but the full description can be found in numpy documentation.

```
a = np.random.randint(low=1, high=100, size=3)
print('a         : {}'.format(a))
print('a^2       : {}'.format(a**2))
print('a/(1-a^a): {}'.format(a/(1-a**a)))
print('cos(a)    : {}'.format(np.cos(a)))
print('exp(a)    : {}'.format(np.exp(a)))
```

```
a         : [90 74 55]
a^2       : [8100 5476 3025]
a/(1-a^a): [ 9.00000000e+01  7.40000000e+01 -1.81472871e-17]
cos(a)    : [-0.44807362  0.17171734  0.02212676]
exp(a)    : [1.22040329e+39 1.37338298e+32 7.69478527e+23]
```

All these ufunct can work for n-dimension arrays and can be used in a very flexible way depeding on the axis you are refering too. Indeed the mathematical operation can be performed over a different axis of the array, having a totally different meaning. Let's give a simple concrete example with a 2D array of shape (5,2), *i.e.* 5 vectors of three coordinates (x, y, z) Much more examples will be discussed in the section 2.

```
# Generate 5 vectors (x,y,z)
positions = np.random.randint(low=1, high=100, size=(5, 3))

# Average of the coordinate over the 5 observations
```

```
pos_mean = np.mean(positions, axis=0)
print(pos_mean)

# Distance to the origin sqrt(x^2+ y^2 + z^2)for the 5 observations
distances = np.sqrt(np.sum(positions**2, axis=1))
print(distances)
```

```
[42.6 55.4 57. ]
[113.08846095  97.55511263 107.42904635  86.46386528  81.64557551]
```

1.3.2 3.2 Broadcasting

The *broadcasting* is a way to compute operation between arrays of having different sizes in a implicit (and consice) manner. Few examples are given below but more details are give in this documentation.

```
# operation between shape (3) and (1)
a = np.array([1, 2, 3])
b = np.array([5])
a+b
```

```
array([6, 7, 8])
```

```
# operation between shape (3) and (1,2)
a = np.array([1, 2, 3])
b = np.array([
              [4],
              [5],
             ])
a+b
```

```
array([[5, 6, 7],
       [6, 7, 8]])
```

```
# Operation between shapes (5,3) and (3), e.g. adding an origin r0 to 10 2D
↪  vectors
data = np.random.normal(size=(5, 2))
r0 = np.array([1, 4])
print('data:\n {}\n'.format(data))
print('data+r0:\n {}'.format(data+r0))
```

```
data:
 [[-1.02127235 -0.53024222]
 [-0.54934453 -0.17206173]
 [ 0.9895191  -1.2826329 ]
 [ 2.34814196 -0.97768543]
 [-1.13020269  0.65844848]]

data+r0:
 [[-0.02127235  3.46975778]
 [ 0.45065547  3.82793827]
 [ 1.9895191   2.7173671 ]
 [ 3.34814196  3.02231457]
 [-0.13020269  4.65844848]]
```

1.3.3 3.3 Working with sub-arrays: slicing, indexing and mask (or selection)

Slicing and indexing are ways to access sub-arrays in a smart way. Python allows slicing with `Slice()` object but `numpy` allows to push it much further with fancy indexing. Few examples are given below and for more details, please have a look to this documentation page.

The basic synthax is `a[i]` to access the ith element. It is also possible to go from the last element using negative indices: `a[-1]` is the last element. Numpy also support array of indices. If the index array is multi-dimensional, the result will have the same dimension as the indices array.

```
a = np.random.randint(low=1, high=100, size=10)
print('a = {}'.format(a))
print('a[2] = {}'.format(a[2]))
print('a[-1] = {}'.format(a[-1]))
print('a[[1, 2, 5]] = {}'.format(a[[1, 2, 5]]))
```

```
a = [49 47 65 50  1 61 27 15  9  5]
a[2] = 65
a[-1] = 5
a[[1, 2, 5]] = [47 65 61]
```

```
# Playing with a small n-dimensional indices array: 5 arrays of 2 elements
 ↪  each
indices = np.arange(10).reshape(5,2)
print('indices = {}'.format(indices))
print('a[indices] = {}'.format(a[indices]))
print('\n')
```

```
# Playing with n-dimensional indices array: 2 arrays of (10, 10) arrays
indices_big = np.random.randint(low=0, high=10, size=(2, 10, 10))
print('indices_big = {}'.format(indices_big))
print('a[indices_big] = {}'.format(a[indices_big]))
```

```
indices = [[0 1]
 [2 3]
 [4 5]
 [6 7]
 [8 9]]
a[indices] = [[49 47]
 [65 50]
 [ 1 61]
 [27 15]
 [ 9  5]]


indices_big = [[[9 2 3 7 5 1 9 2 2 8]
  [7 6 1 2 5 8 0 0 3 0]
  [8 3 0 1 4 4 8 9 7 1]
  [4 6 6 9 9 3 9 2 9 7]
  [3 4 0 5 1 3 5 8 2 4]
  [6 6 4 0 0 0 1 4 9 3]
  [2 7 8 5 4 3 7 5 2 5]
  [1 4 1 1 0 5 8 0 5 9]
  [3 5 0 9 2 5 4 4 0 9]
  [3 1 7 1 6 9 4 2 4 5]]

 [[0 1 9 2 1 4 0 0 8 4]
  [9 7 8 3 4 0 0 1 8 9]
  [4 3 4 4 4 7 1 2 9 1]
  [1 5 5 3 8 2 8 3 9 6]
  [1 8 6 7 2 8 2 3 6 9]
  [1 6 2 9 0 1 2 6 3 1]
  [7 0 2 0 3 2 7 3 0 0]
  [7 9 0 1 0 5 6 2 4 8]
  [7 5 1 8 1 6 5 9 3 3]
  [2 0 5 5 8 3 3 3 3 6]]]
a[indices_big] = [[[ 5 65 50 15 61 47  5 65 65  9]
  [15 27 47 65 61  9 49 49 50 49]
  [ 9 50 49 47  1  1  9  5 15 47]
  [ 1 27 27  5  5 50  5 65  5 15]
  [50  1 49 61 47 50 61  9 65  1]
  [27 27  1 49 49 49 47  1  5 50]
```

```
  [65 15  9 61  1 50 15 61 65 61]
  [47  1 47 47 49 61  9 49 61  5]
  [50 61 49  5 65 61  1  1 49  5]
  [50 47 15 47 27  5  1 65  1 61]]

 [[49 47  5 65 47  1 49 49  9  1]
  [ 5 15  9 50  1 49 49 47  9  5]
  [ 1 50  1  1  1 15 47 65  5 47]
  [47 61 61 50  9 65  9 50  5 27]
  [47  9 27 15 65  9 65 50 27  5]
  [47 27 65  5 49 47 65 27 50 47]
  [15 49 65 49 50 65 15 50 49 49]
  [15  5 49 47 49 61 27 65  1  9]
  [15 61 47  9 47 27 61  5 50 50]
  [65 49 61 61  9 50 50 50 50 27]]]
```

There is a quite powerful smart way to access sub-array with the synthax `a[min:max:step]`. In that way, it's very easy to take one element over two (`step=2`), or reverse the order of the array (`step=-1`). This synthax works also for n-dimensional array, where each dimension is sperated by a coma. An example is given for a 1D array and for a 3D array of (5, 2, 3) shapes (that can though of 5 observations containing each 2 3D vectors).

```
a = np.random.randint(low=1, high=100, size=10)
print('full array a              = {}'.format(a))
print('from 0 to 1: a[:2]        = {}'.format(a[:2]))
print('from 4 to end: a[4:]      = {}'.format(a[4:]))
print('reverse order: a[::-1]    = {}'.format(a[::-1]))
print('all even elements: a[::2] = {}'.format(a[::2]))
```

```
full array a              = [74  7 97 54 43 33  3 53 52 67]
from 0 to 1: a[:2]        = [74  7]
from 4 to end: a[4:]      = [43 33  3 53 52 67]
reverse order: a[::-1]    = [67 52 53  3 33 43 54 97  7 74]
all even elements: a[::2] = [74 97 43  3 52]
```

```
a = np.random.randint(low=0, high=100, size=(5, 2, 3))
print('a = {}'.format(a))

# Taking only the y,z values of the first vector for all observation
#  - first dimension (=5 observations): `:` means takes all
#  - second dimension (=2 vectors): `1` means only the 2nd element
#  - third dimensio (=3 coordinates): `0:2` means from 0 to 2-1, so only
 ↪  (x,y)
```

```
print('\nTaking only the y,z values of the first vector for all
 ↪  observation:')
print('a[:, 0, 0:2] = {}'.format(a[:, 0, 0:2]))

print('\nReverse the order of the 2 vector for each observation:')
print('a[:, ::-1, :] = {}'.format(a[:, ::-1, :]))
```

```
a = [[[73 66 21]
  [21 54 62]]

 [[38 20 70]
  [53 34 17]]

 [[68 93 64]
  [26 10 81]]

 [[83 67 98]
  [96 51 18]]

 [[82 77  8]
  [81 68 94]]]

Taking only the y,z values of the first vector for all observation:
a[:, 0, 0:2] = [[73 66]
 [38 20]
 [68 93]
 [83 67]
 [82 77]]

Reverse the order of the 2 vector for each observation:
a[:, ::-1, :] = [[[21 54 62]
  [73 66 21]]

 [[53 34 17]
  [38 20 70]]

 [[26 10 81]
  [68 93 64]]

 [[96 51 18]
  [83 67 98]]

 [[81 68 94]
  [82 77  8]]]
```

The last part of of indexing is about array *masking* or *selection*. This allows to get only element based on a give criteria, exploiting the indexing technics shown above. Indeed, a condition an array such as `a>0` will directly return an array of boolean for which each element is `True` or `False` depending on the condition. This is also very useful to replace all element with a given value. Some examples are given below.

```
a = np.random.randint(low=-100, high=100, size=(5, 3))
mask = a>0
print('a        = {}'.format(a))
print('mask     = {}'.format(mask))
print('a[mask]  = {}'.format(a[mask]))  # this cannot keep the dimension, by
 ↪  construction
print('a*mask   = {}'.format(a*mask))   # this preserve the dimension
 ↪  (replacing False by 0)
print('a[~mask] = {}'.format(a[~mask])) # The symbol ~make reverse the
 ↪  conditions
print('a*~mask  = {}'.format(a*~mask))  # which work for a produc too.
```

```
a        = [[ 15  89 -68]
 [-22 -97 -76]
 [-20 -14 -74]
 [-41   1   7]
 [ 86 -42 -61]]
mask     = [[ True  True False]
 [False False False]
 [False False False]
 [False  True  True]
 [ True False False]]
a[mask]  = [15 89  1  7 86]
a*mask   = [[15 89  0]
 [ 0  0  0]
 [ 0  0  0]
 [ 0  1  7]
 [86  0  0]]
a[~mask] = [-68 -22 -97 -76 -20 -14 -74 -41 -42 -61]
a*~mask  = [[  0   0 -68]
 [-22 -97 -76]
 [-20 -14 -74]
 [-41   0   0]
 [  0 -42 -61]]
```

```
# Replacement of all negative values by their square
a = np.random.randint(low=-100, high=100, size=(5, 3))
print('Before: a={}'.format(a))

a[a<0] = a[a<0]**2
print('\nAfter: a={}'.format(a))
```

```
Before: a=[[ 99  21  78]
 [ 29  10  58]
 [ 31 -43 -46]
 [-91 -77 -88]
 [ 66   7 -64]]

After: a=[[  99   21   78]
 [  29   10   58]
 [  31 1849 2116]
 [8281 5929 7744]
 [  66    7 4096]]
```

1.4 4. A powerfull plotting tool: `matplotlib`

`matplolib` is an extremely rich pacakge for data visualization and there is no way to cover all its features here. The goal of this section is just to give you short and practical example to plot data. Much more details can be obtained on the webpage.

```
import matplotlib.pyplot as plt
%matplotlib inline
```

1.4.1 4.1 Example of 1D plots and histograms

```
# Data generation
x = np.random.normal(loc=[-1, 1], scale=[0.5, 0.5], size=(1000,2))
y = np.sin(x)

# Figure creation
fig = plt.figure(figsize=(24, 10))

# First subplot (1 line, 2 column, 1st plot)
plt.subplot(121)
ax = plt.plot(x, y, marker='o', markersize=5, linewidth=0.0)
```

```
# Second subplot (1 line, 2 column, 2nd plot)
plt.subplot(122)
ax = plt.hist(x, bins=20) # x.shape = (1000, 2), interpreted as 2 histos of
 ↪  1000 entries
```

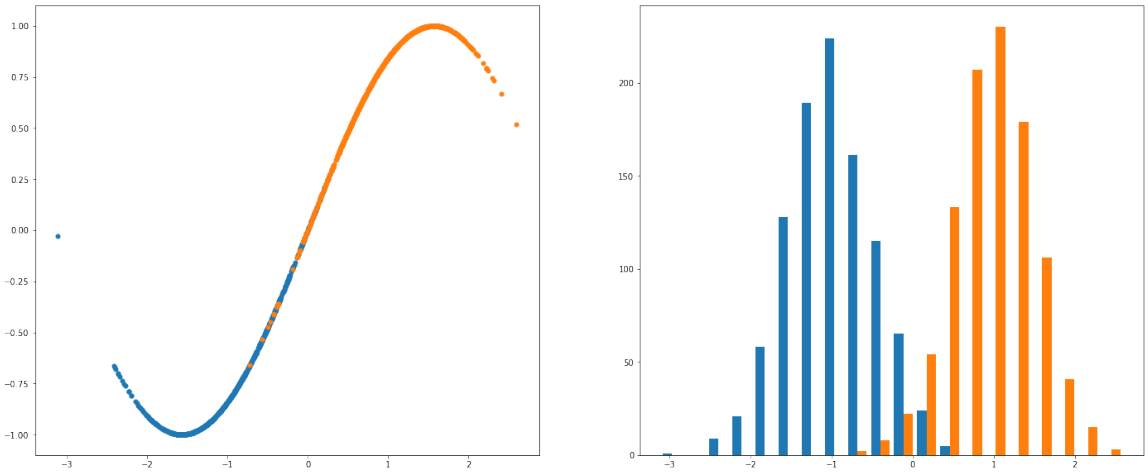

Figure 1: png

1.4.2 4.2 Example of 2D scatter plot

```
# Data generation
points = np.random.normal(loc=[0, 0.0], scale=[0.5, 0.8], size=(5000,2))

# plotting 2D points (x, y) with a circle size of 100*sin(x)^2
x, y = points[:, 0], points[:, 1]
fig = plt.figure(figsize=(10,7))
ax = plt.scatter(x, y, s=100*(np.sin(x))**2, marker='o', alpha=0.3)
ax = plt.xlim(-3, 3)
ax = plt.ylim(-3, 3)
```

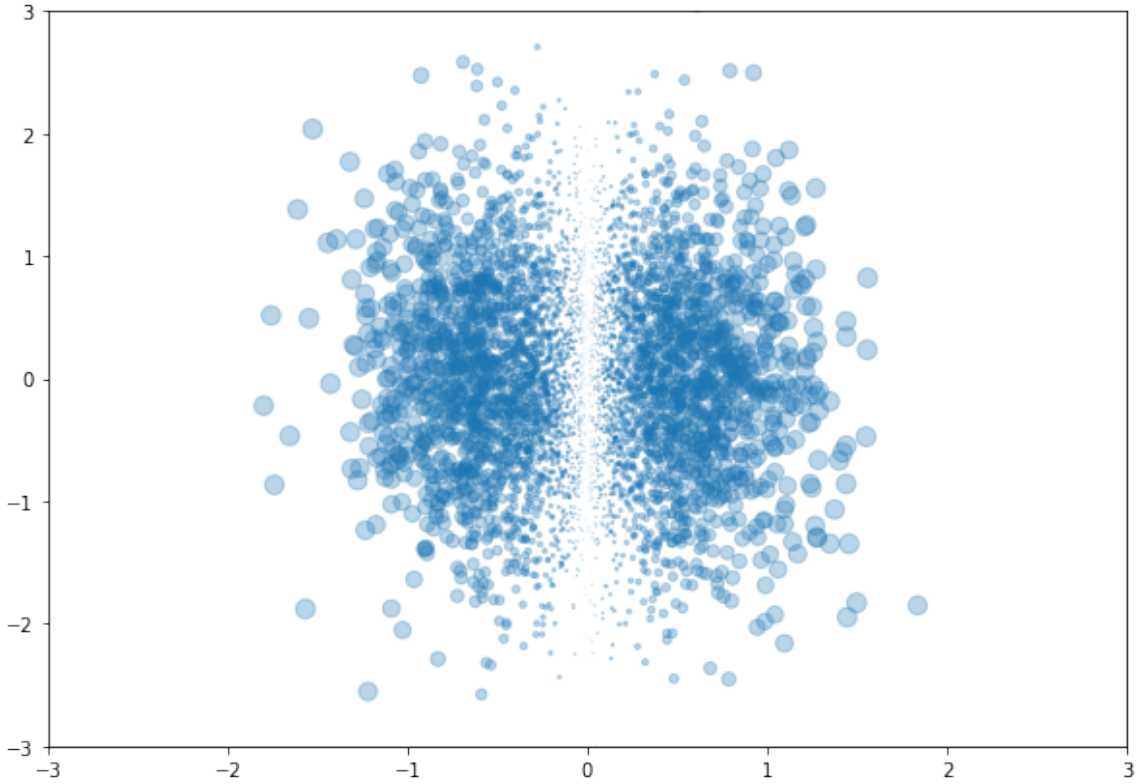

Figure 2: png

1.4.3 4.3 Example of 3D plots

```
# Making 3D positions and translate them using broadcasting
data = np.random.normal(size=(1000, 3))
r0 = np.array([1, 4, 2])
data_trans = data + r0

# import the needed extension to plot in 3D
from mpl_toolkits import mplot3d

# Plotting the data before and after translation
fi = plt.figure(figsize=(12,10))
ax = plt.axes(projection='3d')
_ = ax.scatter3D(data[:,0], data[:,1], data[:,2], alpha=0.4, label='before
↪  translation')
_ = ax.scatter(data_trans[:,0], data_trans[:,1], data_trans[:,2], alpha=0.4,
↪  label='after translation')
_ = ax.set_xlabel('x')
_ = ax.set_ylabel('y')
```

```
_ = ax.set_zlabel('z')
_ = ax.legend(frameon=False, fontsize=18)
```

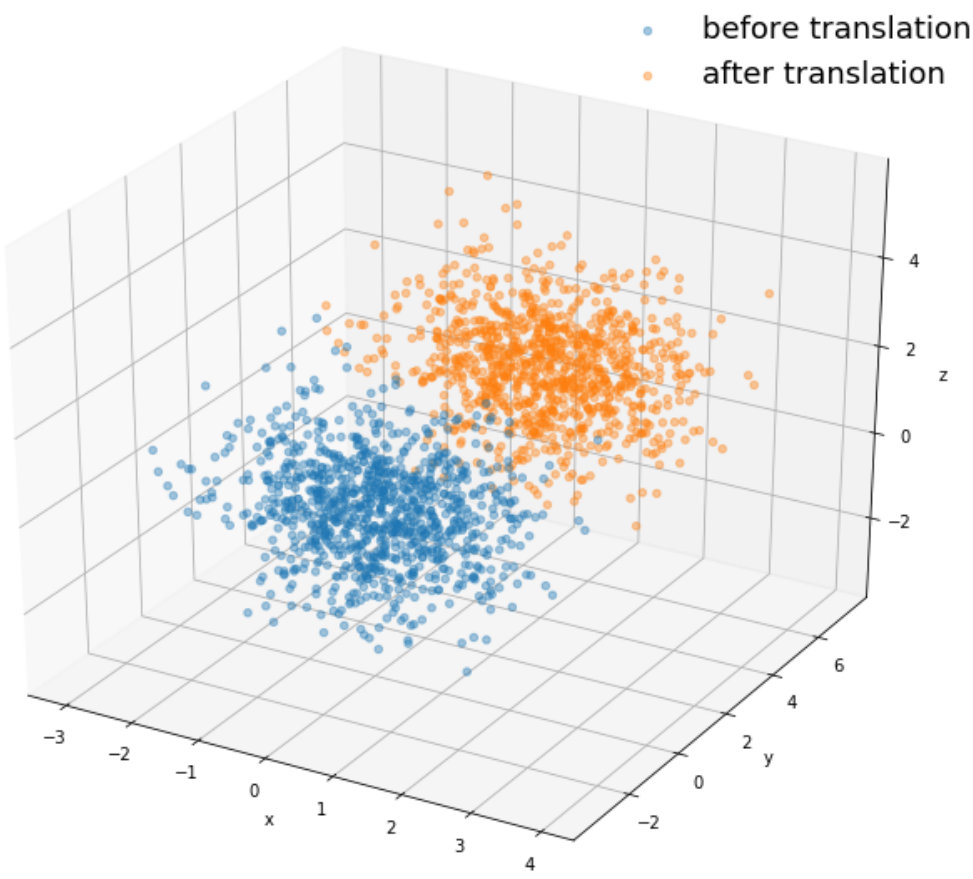

Figure 3: png

1.5 5. Import and manipulate data as `numpy` array via `pandas`

The package `pandas` is an very rich interface to read data from different format and produce a `pandas.dataframe` that can be based on `numpy` (but contanining a lot more features). There is no way to fully desribe this package here, the goal is simply to give functional and concrete example easily usable. More more details, please check the pandas webpage

```
import pandas as pd
cols_to_keep = ['HT', 'nlep', 'njet', 'pt_1st_bjet', 'pt_2nd_bjet',
↪  'pt_3rd_bjet', 'pt_4th_bjet']
df = pd.read_csv('ttW.csv', usecols=cols_to_keep)
df.head()
```

```
<tr style="text-align: right;">
  <th></th>
  <th>HT</th>
  <th>njet</th>
  <th>nlep</th>
  <th>pt_1st_bjet</th>
  <th>pt_2nd_bjet</th>
  <th>pt_3rd_bjet</th>
  <th>pt_4th_bjet</th>
</tr>

<tr>
  <th>0</th>
  <td>262.100311</td>
  <td>2</td>
  <td>2</td>
  <td>48.112684</td>
  <td>-99.000000</td>
  <td>-99.0</td>
  <td>-99.0</td>
</tr>
<tr>
  <th>1</th>
  <td>447.937225</td>
  <td>4</td>
  <td>4</td>
  <td>118.460391</td>
  <td>28.788586</td>
  <td>-99.0</td>
  <td>-99.0</td>
</tr>
<tr>
  <th>2</th>
  <td>1287.348022</td>
  <td>6</td>
  <td>6</td>
  <td>89.715039</td>
  <td>42.138535</td>
  <td>-99.0</td>
  <td>-99.0</td>
</tr>
<tr>
  <th>3</th>
  <td>453.677887</td>
  <td>6</td>
```

```
  <td>6</td>
  <td>88.535555</td>
  <td>82.532266</td>
  <td>-99.0</td>
  <td>-99.0</td>
</tr>
<tr>
  <th>4</th>
  <td>268.445099</td>
  <td>2</td>
  <td>2</td>
  <td>116.625023</td>
  <td>-99.000000</td>
  <td>-99.0</td>
  <td>-99.0</td>
</tr>
```

```
# Get a numpy arrays
ht = df['HT'].values

# Get derived quantities
ht_mean = np.mean(ht)
ht_rms = np.sqrt(np.mean((ht-ht_mean)**2))

# Add them into the pandas dataframe
df['HT_centered'] = ht-ht_mean
df['HT_normalized'] = (ht-ht_mean)/ht_rms
df.head()
```

```
<tr style="text-align: right;">
  <th></th>
  <th>HT</th>
  <th>njet</th>
  <th>nlep</th>
  <th>pt_1st_bjet</th>
  <th>pt_2nd_bjet</th>
  <th>pt_3rd_bjet</th>
  <th>pt_4th_bjet</th>
  <th>HT_centered</th>
  <th>HT_normalized</th>
</tr>

<tr>
  <th>0</th>
```

```
  <td>262.100311</td>
  <td>2</td>
  <td>2</td>
  <td>48.112684</td>
  <td>-99.000000</td>
  <td>-99.0</td>
  <td>-99.0</td>
  <td>-254.826585</td>
  <td>-0.895919</td>
</tr>
<tr>
  <th>1</th>
  <td>447.937225</td>
  <td>4</td>
  <td>4</td>
  <td>118.460391</td>
  <td>28.788586</td>
  <td>-99.0</td>
  <td>-99.0</td>
  <td>-68.989671</td>
  <td>-0.242554</td>
</tr>
<tr>
  <th>2</th>
  <td>1287.348022</td>
  <td>6</td>
  <td>6</td>
  <td>89.715039</td>
  <td>42.138535</td>
  <td>-99.0</td>
  <td>-99.0</td>
  <td>770.421127</td>
  <td>2.708646</td>
</tr>
<tr>
  <th>3</th>
  <td>453.677887</td>
  <td>6</td>
  <td>6</td>
  <td>88.535555</td>
  <td>82.532266</td>
  <td>-99.0</td>
  <td>-99.0</td>
  <td>-63.249009</td>
  <td>-0.222371</td>
```

```
</tr>
<tr>
  <th>4</th>
  <td>268.445099</td>
  <td>2</td>
  <td>2</td>
  <td>116.625023</td>
  <td>-99.000000</td>
  <td>-99.0</td>
  <td>-99.0</td>
  <td>-248.481797</td>
  <td>-0.873612</td>
</tr>
```

```
plt.figure(figsize=(20, 6))

plt.subplot(121)
ax = plt.hist(df['HT'], bins=100, alpha=0.5)
ax = plt.hist(df['HT_centered'], bins=100, alpha=0.5)

plt.subplot(122)
ax = plt.hist(df['HT_normalized'], bins=100, alpha=0.5)
```

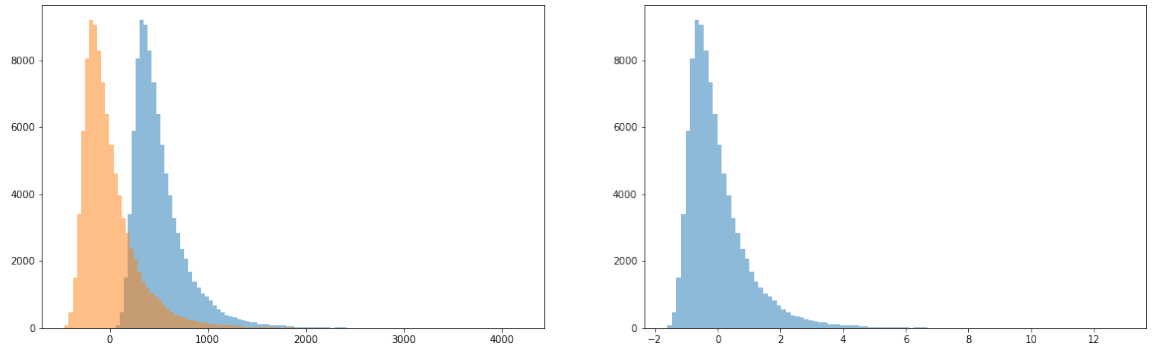

Figure 4: png

```
from pandas.plotting import scatter_matrix
df_scatter = df[['HT_normalized', 'njet', 'nlep', 'pt_1st_bjet']]
_ = scatter_matrix(df_scatter, alpha=0.2, figsize=(12, 12), diagonal='hist')
```

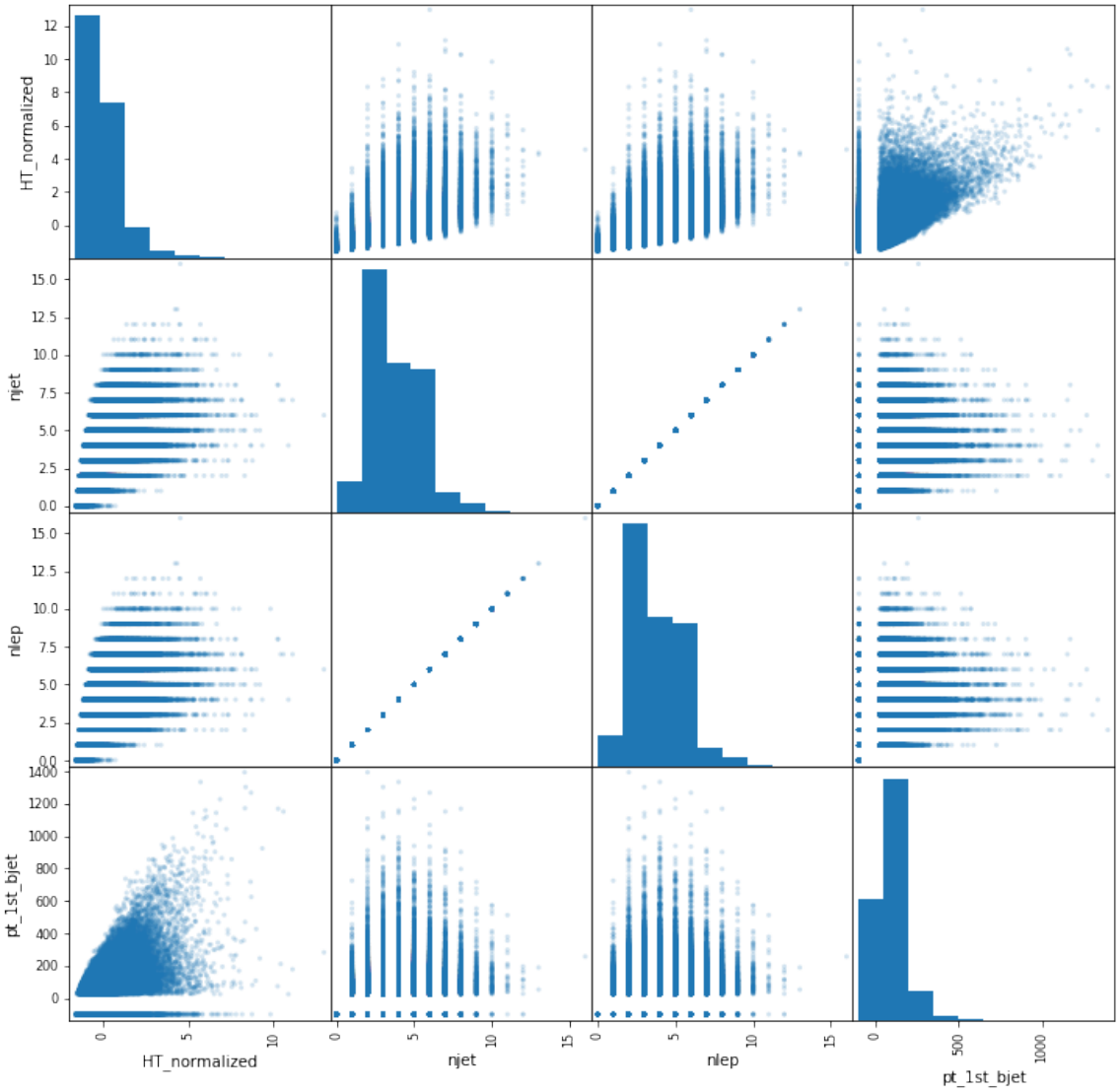

Figure 5: png

2 Typical use cases in high energy physics

```
# Imports
import numpy as np
import itertools
import matplotlib.pyplot as plt
import matplotlib as mpl
```

```
%matplotlib inline

# Plot settings
mpl.rcParams['legend.frameon'] = False
mpl.rcParams['legend.fontsize'] = 'xx-large'
mpl.rcParams['xtick.labelsize'] = 16
mpl.rcParams['ytick.labelsize'] = 16
mpl.rcParams['axes.titlesize'] = 18
mpl.rcParams['axes.labelsize'] = 18
mpl.rcParams['lines.linewidth'] = 2.5
mpl.rcParams['figure.figsize'] = (10, 7)
```

2.1 1. Data model and goals

We consider 1 millions of "observations", each defined by ten 3D vectors $(r_0, ..., r_9)$ where $r_i = (x, y, z)$. These pseudo data can represent position in space or RGB colors. This is just an example to play with and apply numpy concepts for both simple computations (element-by-element functions, statistics calculations) and more complex calculations exploiting the multi-dimensional structure of the data. For example, one might want to compute the distance between all pairs (r_i, r_j), which has to be done without loop.

2.2 2. Generation of pseudo-data

Using the `np.random` module, it is possible to generate n-dimensional arrays easily. In our case, the array containing our observation will have 3 dimensions (or **axis** in `numpy` language), and the size along each of these axis will have the following size and meaning: + `axis=0`: over 1.5 events + `axis=1`: over 10 vectors + `axis=2`: over 3 coordinates

```
r = np.random.random_sample((1000000, 10, 3))
print(r[0:2, ...])
```

```
[[[0.34436731 0.53107072 0.26815523]
  [0.91108107 0.4570885  0.00702956]
  [0.32093231 0.24713113 0.83575452]
  [0.47213206 0.19990225 0.38265613]
  [0.76153726 0.04433562 0.22878573]
  [0.10192781 0.78294055 0.31604284]
  [0.52889256 0.52907432 0.94869321]
  [0.30725522 0.52849071 0.12516978]
  [0.21245529 0.24189646 0.6371295 ]
```

```
  [0.56123822 0.04453289 0.74059217]]

 [[0.05499102 0.03072383 0.61919756]
  [0.15099051 0.37395727 0.4230077 ]
  [0.97925116 0.82085132 0.90825113]
  [0.33902785 0.80294261 0.10205408]
  [0.57943954 0.61033554 0.171087  ]
  [0.56197849 0.71818245 0.59397004]
  [0.47305503 0.88798201 0.12895532]
  [0.16396314 0.0010218  0.25188666]
  [0.13043163 0.17845942 0.72213101]
  [0.10597685 0.66827465 0.8475888 ]]]
```

2.3 3. Mean over the differents axis

2.3.1 3.1 Mean over `axis=0`

This mean will average all observations over the first dimension, returning an array of dimension `(10, 3)` corresponding to the average $r_i = (x_i, y_i, z_i)$ over the 1 millions observations. The histogram distribution results into three separate histograms (one for each x, y, x) each having 10 entries (one per r_i)

```
%timeit np.mean(r, axis=0)
m0 = np.mean(r, axis=0)
print(m0.shape)
ax = plt.hist(m0, label=['$<x>_{evts}$', '$<y>_{evts}$', '$<z>_{evts}$'])
ax = plt.title('10 entries, one for each $r_i$')
ax = plt.legend()
```

```
36.4 ms ± 10.9 ms per loop (mean ± std. dev. of 7 runs, 10 loops each)
(10, 3)
```

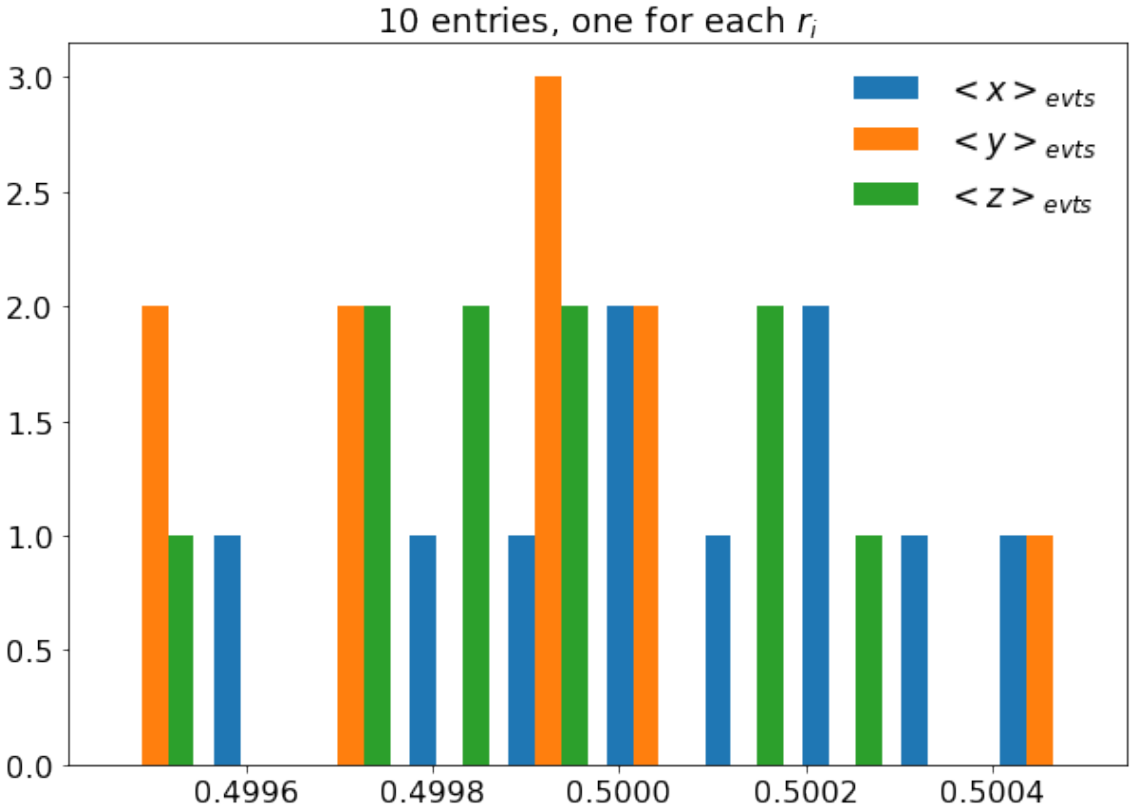

Figure 6: png

2.3.2 3.2 Mean over `axis=1`

This one will compute the average over the 10 vectors, for each of 1 million observations, reducing into a `(1000000, 3)` shape array, as seen below.

```
%timeit np.mean(r, axis=1)
m1 = np.mean(r, axis=1)
print(m1.shape)
ax = plt.hist(m1, label=['$<x>_{i}$', '$<y>_{i}$', '$<z>_{i}$'])
ax = plt.title('$10^6$ entries, one per event')
ax = plt.legend()
```

```
275 ms ± 28.3 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)
(1000000, 3)
```

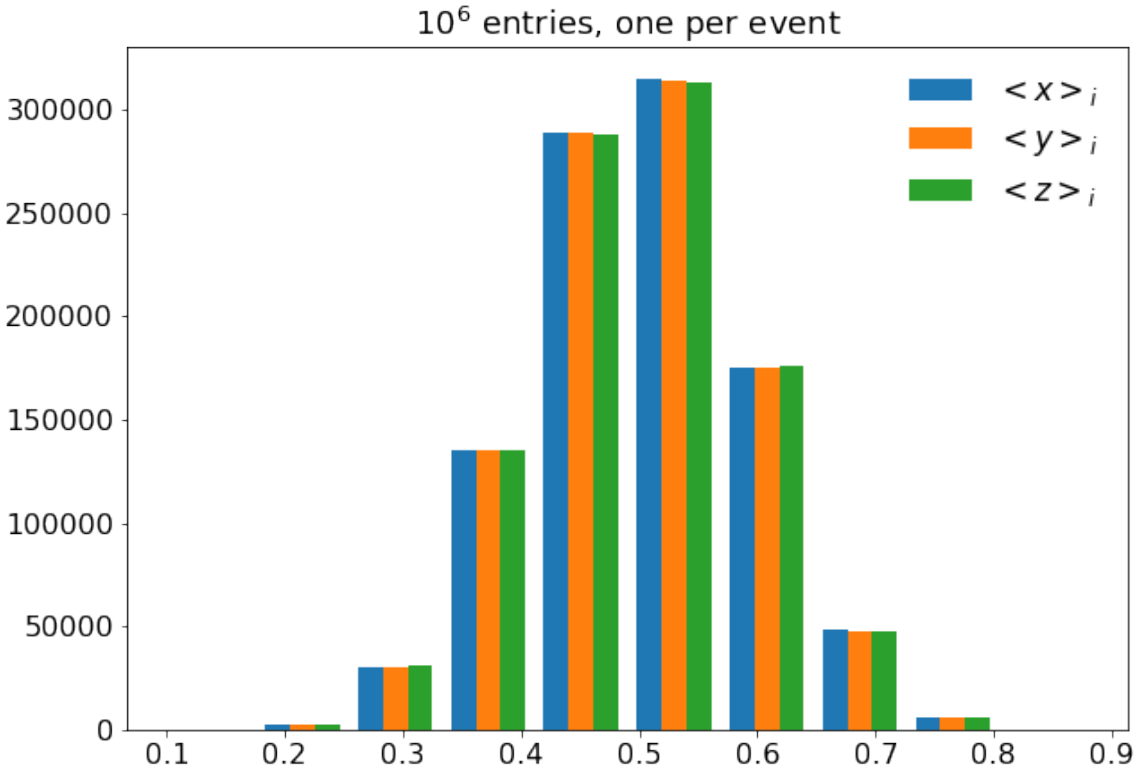

Figure 7: png

2.3.3 3.2 Mean over `axis=2`

This directly computes the average over the three coordinates for each vector of each event, in other words, the barycenter $(x + y + z)/3$.

```
%timeit np.mean(r, axis=2)
m2 = np.mean(r, axis=2)
print(m2.shape)
ax = plt.hist(m2, label=['$(x+y+z)/3|_{'+'{}'.format(i)+'}$' for i in
 ↪  range(1, 11)])
ax = plt.title('$10^6$ entries, one per event')
ax = plt.legend()
```

```
241 ms ± 45.9 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)
(1000000, 10)
```

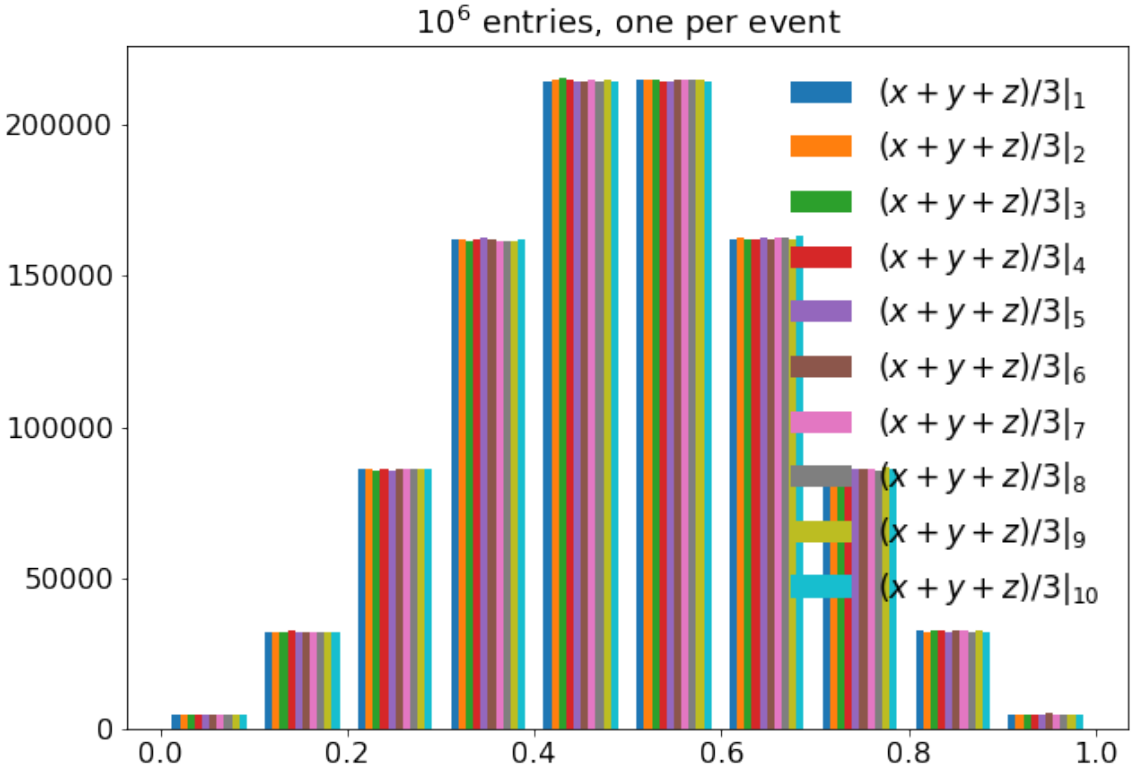

Figure 8: png

2.4 4. Distance computation

2.4.1 4.1 Distance to a reference r_0

```
# Reference definition
r0 = np.array([1, 2, 1])

# Compute all 10 differences for all the events
%timeit np.sum(((r-r0)**2)**0.5, axis=2)
d = np.sum(((r-r0)**2)**0.5, axis=2)
print(d.shape)
ax = plt.hist(d, label=['$d(r_{'+'{}'.format(i)+'},r_0)$' for i in range(1,
↪  11)])
ax = plt.title('$10^6$ entries, one per event')
ax = plt.legend()
```

```
475 ms ± 39.2 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)
(1000000, 10)
```

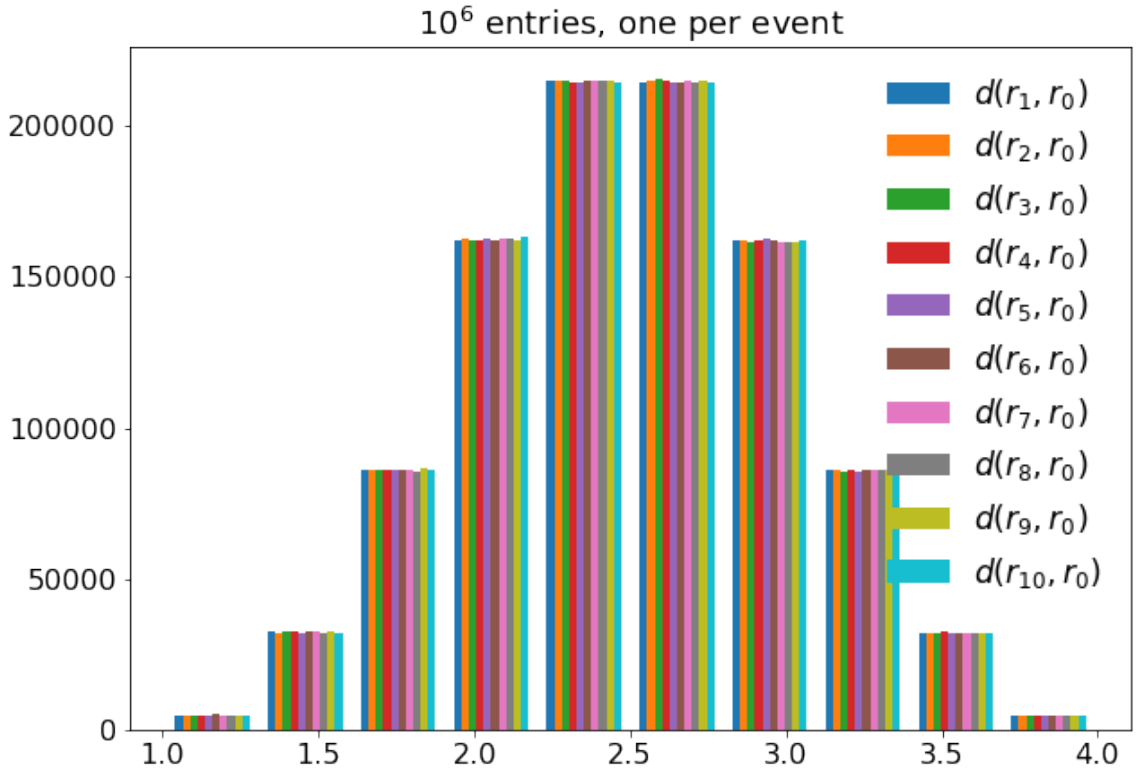

Figure 9: png

2.4.2 4.2 Distance between the two first vectors r_0 and r_1 for each event

```
# Condensed expression
%timeit np.sum(((r[:, 0, :]-r[:, 1, :])**2)**0.5, axis=1)

# More readable expression
r1, r2 = r[:, 0, :], r[:, 1, :]
d12 = np.sum(((r1-r2)**2)**0.5, axis=1)
print(d12.shape)

# Plotting
ax = plt.hist(d12, label='$d(r_1,r_2)$', bins=100)
ax = plt.title('$10^6$ entries, one per event')
ax = plt.legend()
```

```
64.8 ms ± 9.86 ms per loop (mean ± std. dev. of 7 runs, 10 loops each)
(1000000,)
```

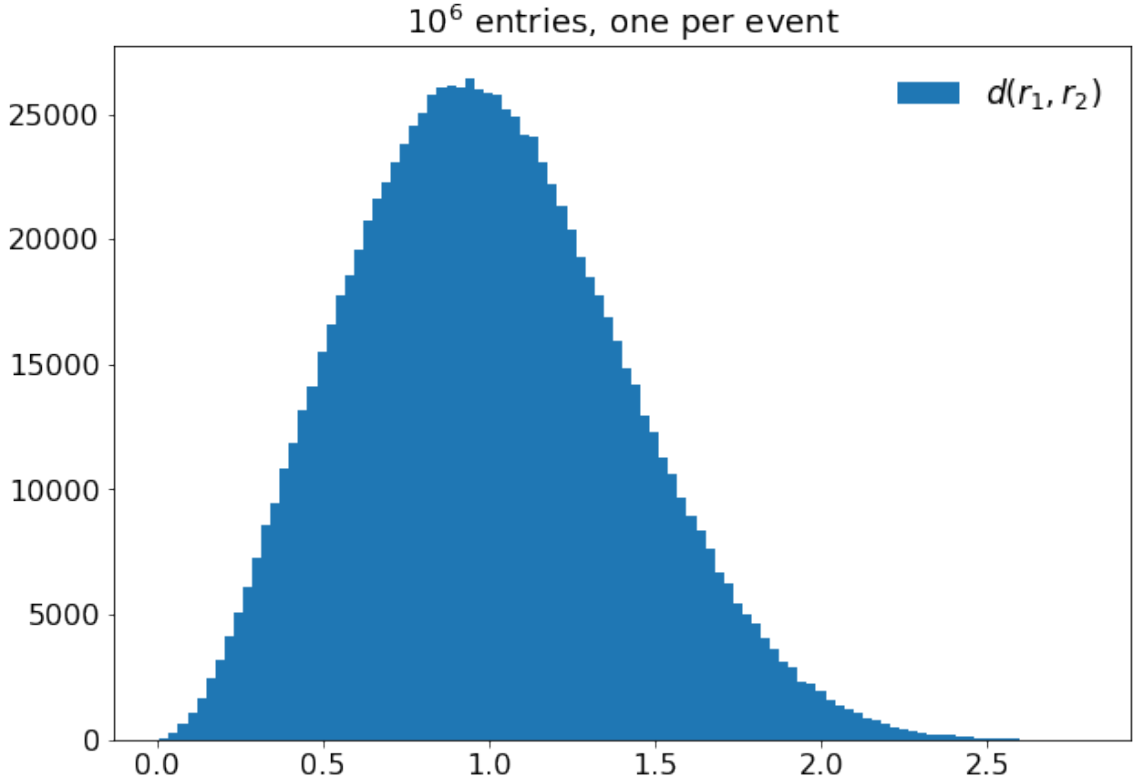

Figure 10: png

2.5 5. Pairing 3D vectors for each observation, without a loop

2.5.1 5.1 Finding all possible (r_i, r_j) pairs for all events

```
def combs_nd(a, n, axis=0, info=False):
    '''
    Solution found on
↪   https://stackoverflow.com/questions/16003217/n-d-version-of-itertools-combinations-in-nu

    The idea here is to simply work on indices to build the pairs
    since it doesn't really matter what are the nature of the objects ...
    '''

    # 1. Initialisation of indices array along the axis we want to pair
    indices = np.arange(a.shape[axis])
    if info:
        print('initialisation -> indices={}'.format(indices))

    # 2. Datatype of index array ([int,int] for a pair)
```

```
    dt = np.dtype([('', np.intp)]*n)
    if info:
        print('datatype: {}'.format(dt))

    # 3. Use itertool to compute combinations and overwite indices
    indices = np.fromiter(itertools.combinations(indices, n), dt) # [(0,1),
↪   (0,2), .. ]
    if info:
        print('np.fromiter -> indicies={}'.format(indices))
    indices = indices.view(np.intp) # [0 1 0 2 ...]
    if info:
        print('indices.view -> indicies={}'.format(indices))
    indices = indices.reshape(-1, n) # [[0 1], [0 2], ...]
    if info:
        print('indices.reshape -> indicies={}'.format(indices))

    # 4. Take all elements in a defined by indices along a given axis
    # the dimension of the array is changed because indices has (n,2) shape
    return np.take(a, indices, axis=axis)


# Trying on the 2 first observations considering only the 5 first vectors ri:
↪   r[0:1, 0:5]
result = combs_nd(a=r[0:1,0:5], n=2, axis=1, info=True)
```

```
initialisation -> indices=[0 1 2 3 4]
datatype: [('f0', '<i8'), ('f1', '<i8')]
np.fromiter -> indicies=[(0, 1) (0, 2) (0, 3) (0, 4) (1, 2) (1, 3) (1, 4) (2,
3) (2, 4) (3, 4)]
indices.view -> indicies=[0 1 0 2 0 3 0 4 1 2 1 3 1 4 2 3 2 4 3 4]
indices.reshape -> indicies=[[0 1]
 [0 2]
 [0 3]
 [0 4]
 [1 2]
 [1 3]
 [1 4]
 [2 3]
 [2 4]
 [3 4]]
```

2.5.2 5.2 Computing (minimum) distances on these pairs

```
# Time and get the pair function
print('\nGetting all pairs')
%timeit combs_nd(r, 2, axis=1)
pairs = combs_nd(r, 2, axis=1)
print(pairs.shape)

# Time and Get the euclidien distance of all pair
print('\nGetting all euclidian distances')
dp = pairs[:, :, 0, :]-pairs[:, :, 1, :]
%timeit(np.sum(dp**2, axis=2))**0.5
diff_pairs = (np.sum(dp**2, axis=2))**0.5
print(dp.shape)
print(diff_pairs.shape)

# Time and get the minimum
print('\nGetting the minimum distances')
%timeit np.min(diff_pairs, axis=1)
closest_pair = np.min(diff_pairs, axis=1)
print(closest_pair.shape)
```

```
Getting all pairs
936 ms ± 169 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)
(1000000, 45, 2, 3)

Getting all euclidian distances
1.14 s ± 26.4 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)
(1000000, 45, 3)
(1000000, 45)

Getting the minimum distances
87.1 ms ± 8.68 ms per loop (mean ± std. dev. of 7 runs, 10 loops each)
(1000000,)
```

```
def compute_dr_min(a):
    pairs = combs_nd(a, 2, axis=1)

    # Get the axis of the pair index to build p1, p2 = a[...,0], a[...,1]
    d = pairs.ndim
    i1 = tuple([None if i != d-2 else 0 for i in range(0, d)])
    i2 = tuple([None if i != d-2 else 1 for i in range(0, d)])
```

```
    return np.min(np.sum((pairs[i1]-pairs[i2])**2, axis=2)**0.5, axis=1)


# Time and get the minimum from r directly
print('\nGetting the minimum distances from r directly using one function')
%timeit compute_dr_min(r)
```

```
Getting the minimum distances from r directly using one function
1.09 s ± 188 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)
```

```
ax = plt.hist(diff_pairs)
```

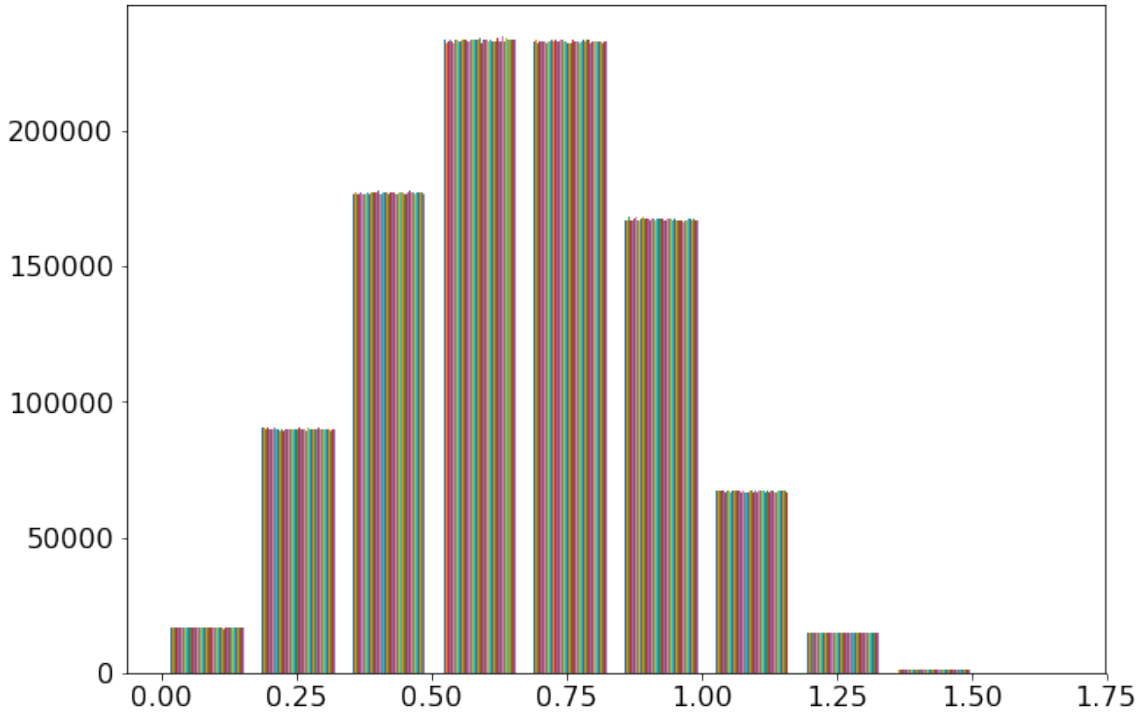

Figure 11: png

```
ax = plt.hist(diff_pairs.flatten(), bins=100)
```

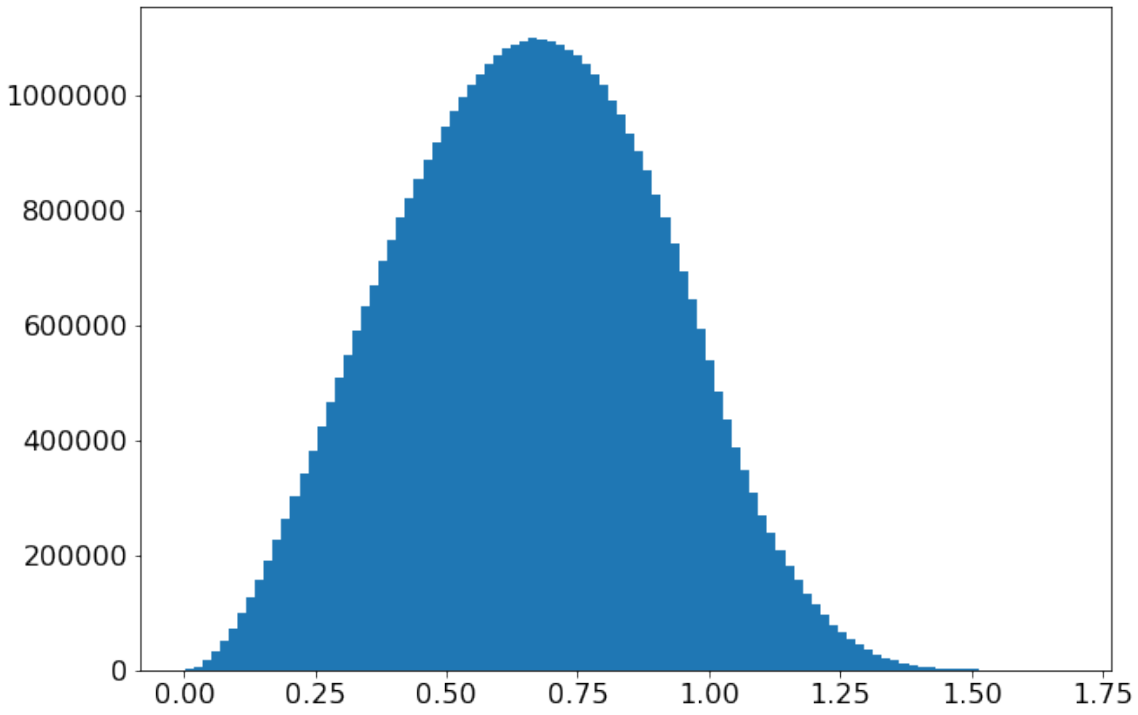

Figure 12: png

```
ax = plt.hist(closest_pair, bins=100)
```

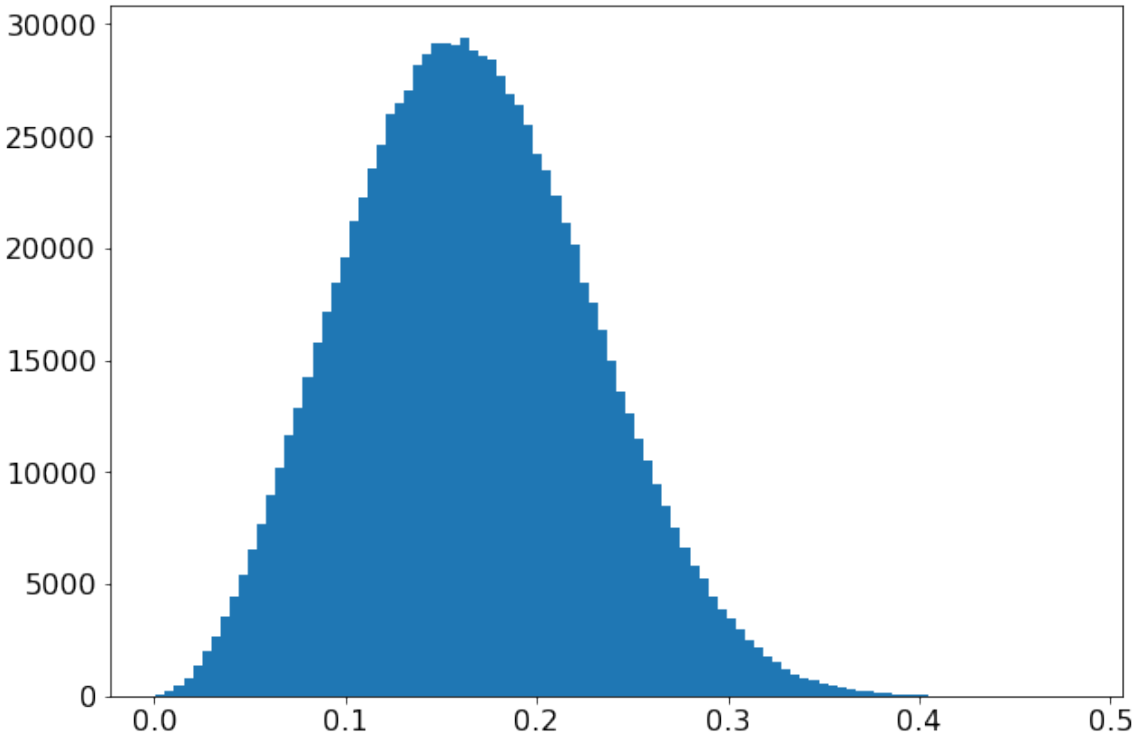

Figure 13: png

2.6 6. Selecting a subset of r_i based on (x, y, z) values, without loop

```
x, y, z = r[:, :, 0], r[:, :, 1], r[:, :, 2]
ax = plt.hist(x**2+y**2+z**2, bins=10)
```

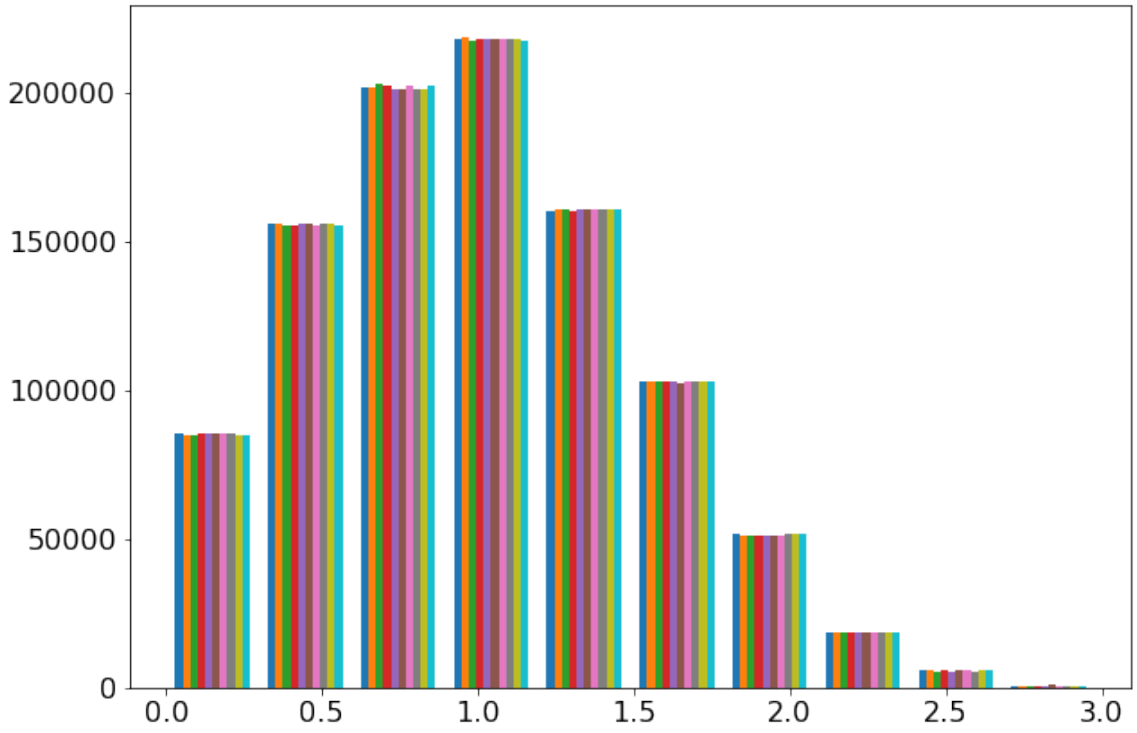

Figure 14: png

```
ax = plt.hist(np.sum(r**2, axis=2), bins=10)
```

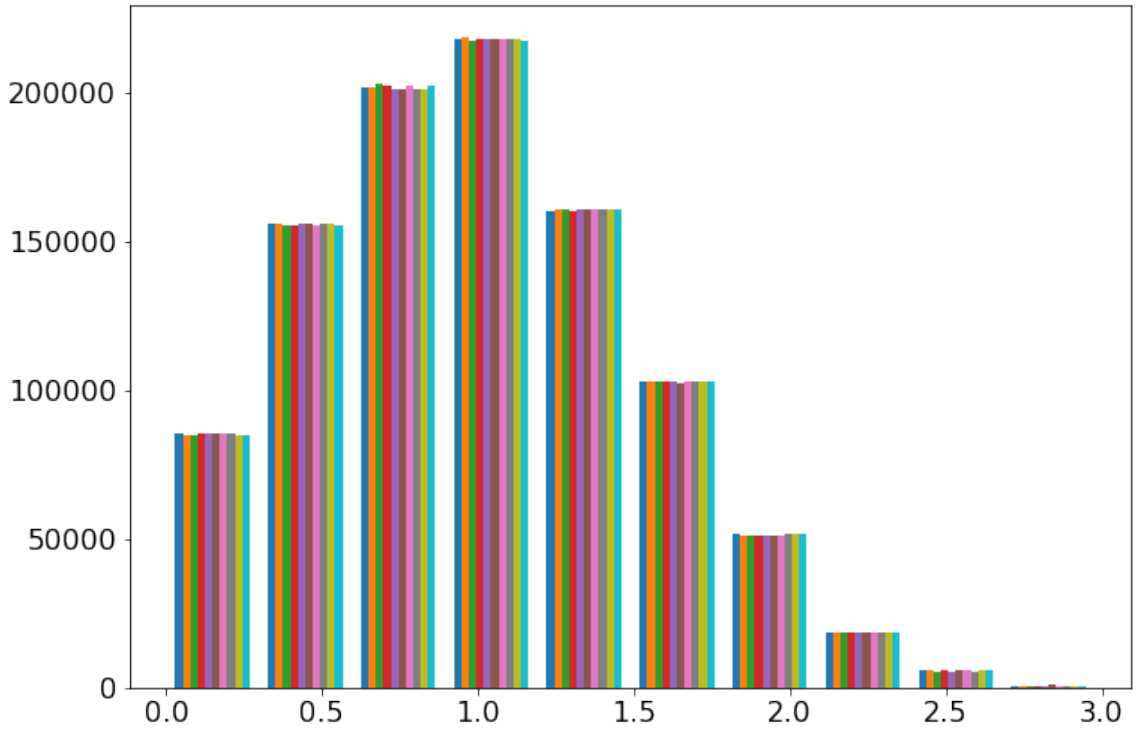

Figure 15: png

2.6.1 6.1 Counting number of points amont the 10 with $x_i > y_i$ in each event

```
# define the selection
idx = x > y
print(idx.shape)

# Checkout the distribution of x,y,z for the selected points
ax = plt.hist(x[idx], bins=100, alpha=0.2)
ax = plt.hist(y[idx], bins=100, alpha=0.2)
ax = plt.hist(z[idx], bins=100, alpha=0.3)
```

```
(1000000, 10)
```

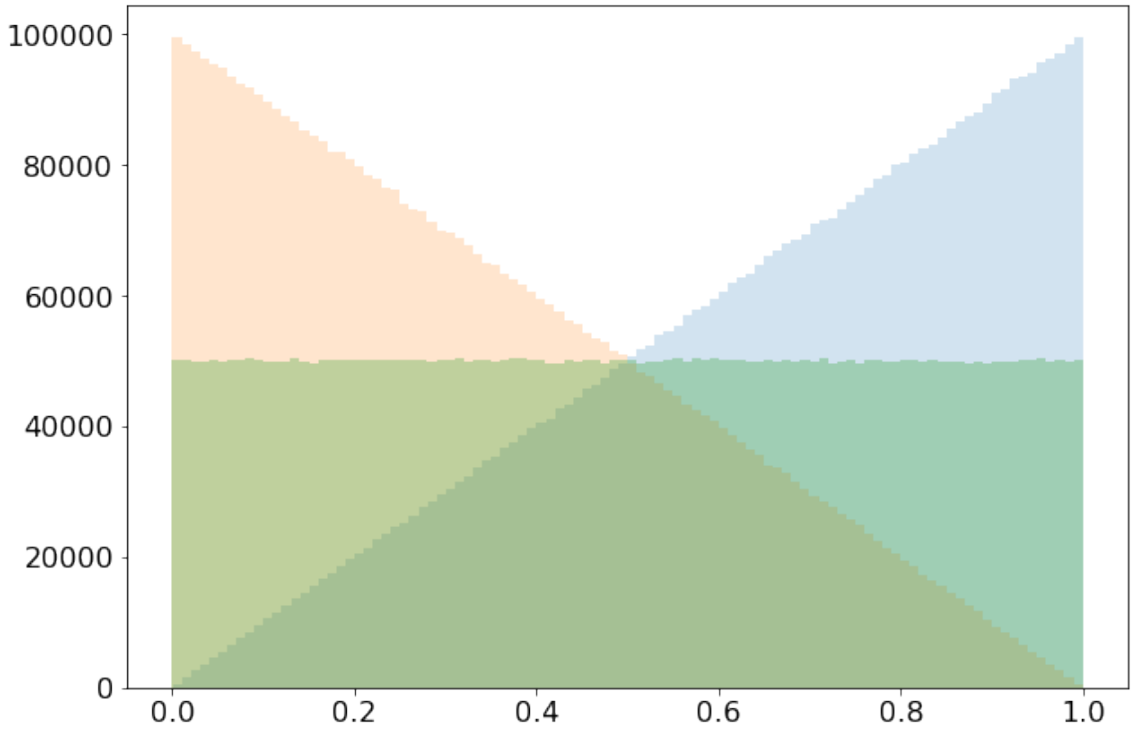

Figure 16: png

```
# Count the number of r per event satisfying x>y
c = np.count_nonzero(idx, axis=1)
print(c.shape)

# Plot the distribution of the count
ax = plt.hist(c, bins=20, alpha=0.5)
```

```
(1000000,)
```

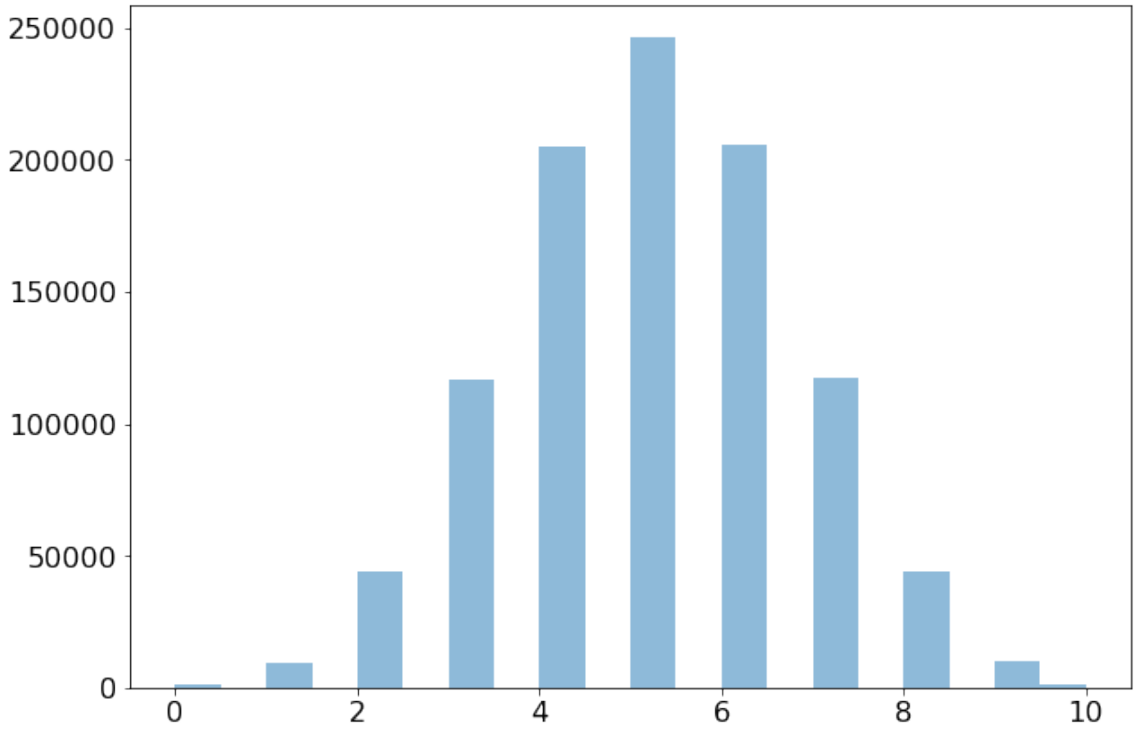

Figure 17: png

2.6.2 6.2 Plotting z for the two types of population ($x > y$ and $x < y$)

```
# Access xi and yi which satisfy xi>yi and xi<xi for each events (over 500
 ↪  events)
# using proper indexing
sx, sy, sz = x[0:500, ...], y[0:500, ...], z[0:500, ...]
sidx_gt, sidx_lt = sx > sy, sx < sy

# Taking the proper indexing will flatten the array
print('\n -> Full array shape    = {}'.format(sx.shape))
print(' -> Indexed array shape = {}'.format(sx[sidx_gt].shape))
print(' -> Counting *all* selected pairs:
 ↪  {}'.format(np.count_nonzero(sidx_gt)))

# Plotting x vs z for the two populations (marker size is 1/(z+0.001))
ax = plt.scatter(sx[sidx_gt], sy[sidx_gt], s=(sz[sidx_gt]+1e-3)**-1)
ax = plt.scatter(sx[sidx_lt], sy[sidx_lt], s=(sz[sidx_lt]+1e-3)**-1)
```

```
 -> Full array shape    = (500, 10)
 -> Indexed array shape = (2593,)
```

```
-> Counting *all* selected pairs: 2593
```

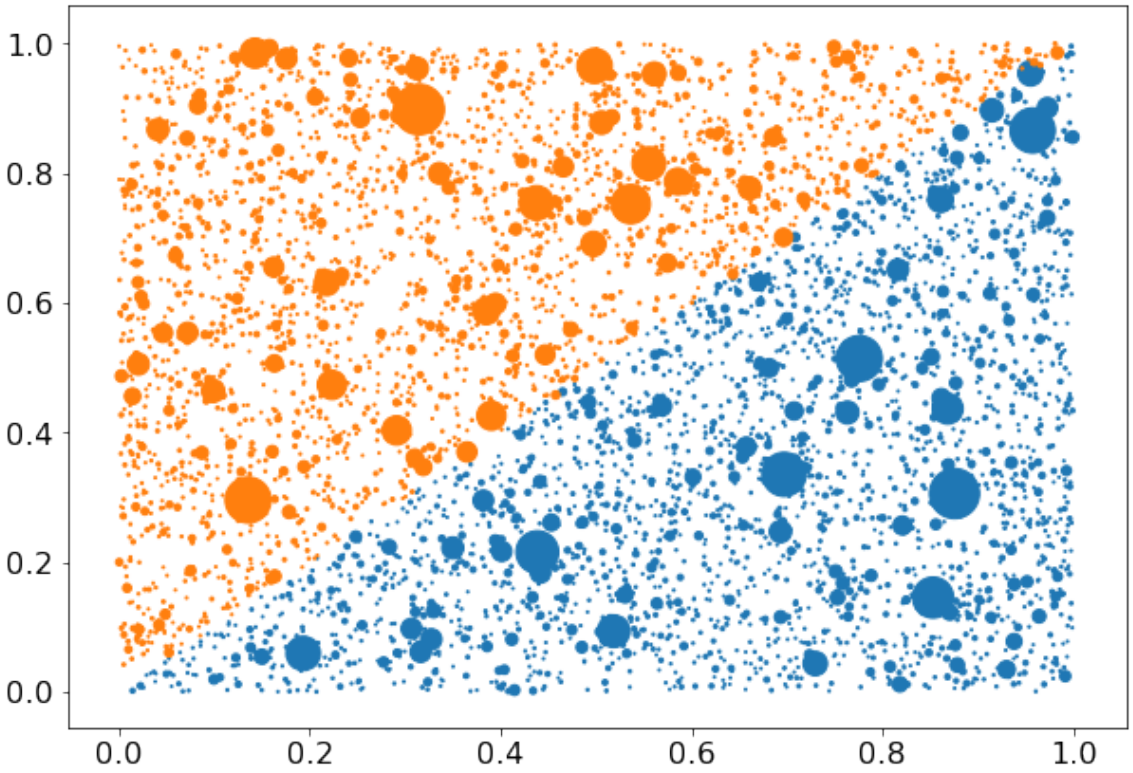

Figure 18: png

2.6.3 6.3 Compute $x_i + y_i + z_i$ sum over the collection of 10 r_i including only points that have $x_i > y_i$?

```
# First step: basic sum over 10 points, ie sum_{i=1..10}(xi+yi+zi) for each
↪  event.
ht1 = np.sum(x+y+z, axis=1)
print(ht1.shape)
ax = plt.hist(ht1, bins=100, alpha=0.4)

# Second step: doing the proper sum, ie only with points verifying x>y.
# 'x*selection' replace xi by 0 in [x0,...,x9]_evt where x<y for all
# events evt. They must have the same shape to be multiplied element
# by element.
selection = x>y
ht2 = np.sum((x+y+z)*selection, axis=1)
print(x.shape, selection.shape, ht2.shape)
ax = plt.hist(ht2[ht2 > 0], bins=100, alpha=0.4)
```

```
(1000000,)
(1000000, 10) (1000000, 10) (1000000,)
```

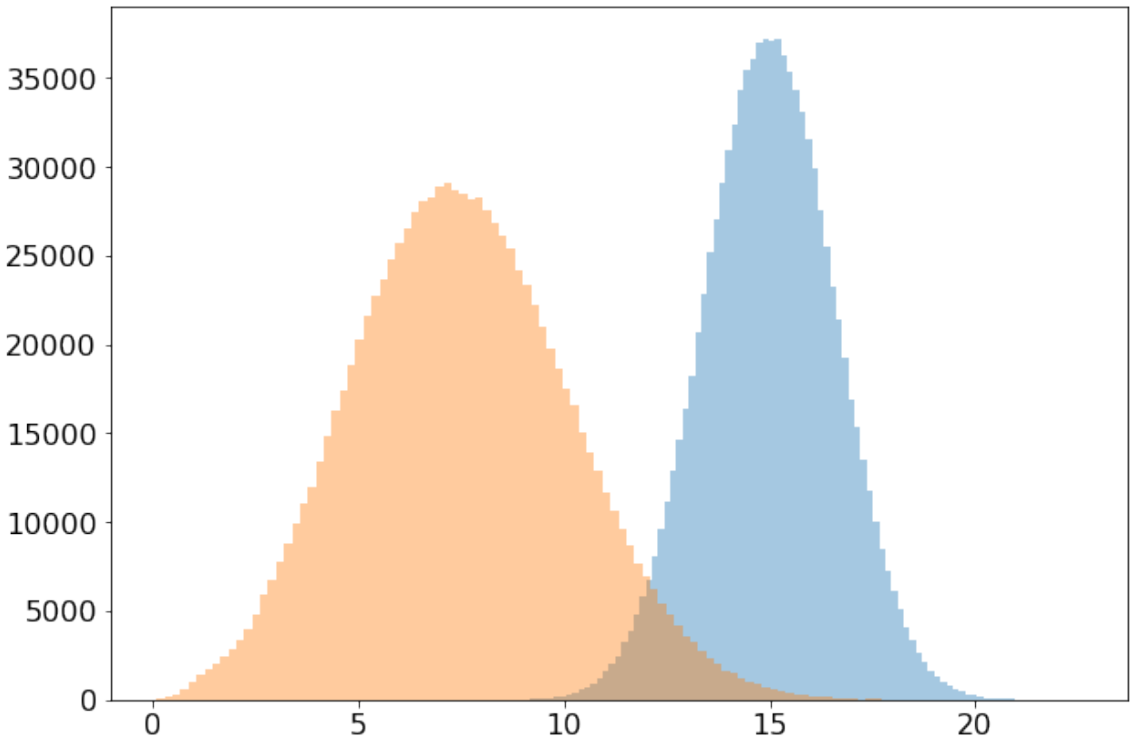

Figure 19: png

2.6.4 6.4 Pairing with a subset of r_i verifying $x_i > y_i$ only

```
# define index of selected points
selection = x > y

# add an empty dimension to make broadcasting possible
selected_r = r*selection[:, :, None]

# replace all 0 (False) by nan so that any combinaison with one of those
# will be nan - and be filtered
selected_r[selected_r == 0] = np.nan

# Print the two first events
print(selected_r[:2])
```

```
[[[       nan        nan        nan]
```

```
  [0.91108107 0.4570885  0.00702956]
  [0.32093231 0.24713113 0.83575452]
  [0.47213206 0.19990225 0.38265613]
  [0.76153726 0.04433562 0.22878573]
  [       nan        nan        nan]
  [       nan        nan        nan]
  [       nan        nan        nan]
  [       nan        nan        nan]
  [0.56123822 0.04453289 0.74059217]]

 [[0.05499102 0.03072383 0.61919756]
  [       nan        nan        nan]
  [0.97925116 0.82085132 0.90825113]
  [       nan        nan        nan]
  [       nan        nan        nan]
  [       nan        nan        nan]
  [       nan        nan        nan]
  [0.16396314 0.0010218  0.25188666]
  [       nan        nan        nan]
  [       nan        nan        nan]]]
```

```
pairs = combs_nd(selected_r, n=2, axis=1)  # get all the possible pairs
print(pairs.shape)
```

```
(1000000, 45, 2, 3)
```

```
# get the first and second element of the pair
p1, p2 = pairs[:, :, 0, :], pairs[:, :, 1, :]

# compute the distance (summed over x,y,z, is axis=2)
dp = np.sum((p1-p2)**2, axis=2)**0.5

# set a default value of irrelevant pairs
dp[np.isnan(dp)] = 999
print(dp.shape)
```

```
(1000000, 45)
```

```
ax = plt.hist(dp.flatten(), bins=np.linspace(0, 2, 200), alpha=0.3,
↪  label='$|r_i-r_j|$ for all pairs')
ax = plt.hist(np.min(dp, axis=1), bins=np.linspace(0, 2, 200), alpha=0.3,
↪  label='min$(|r_i-r_j|)$')
ax = plt.legend()
```

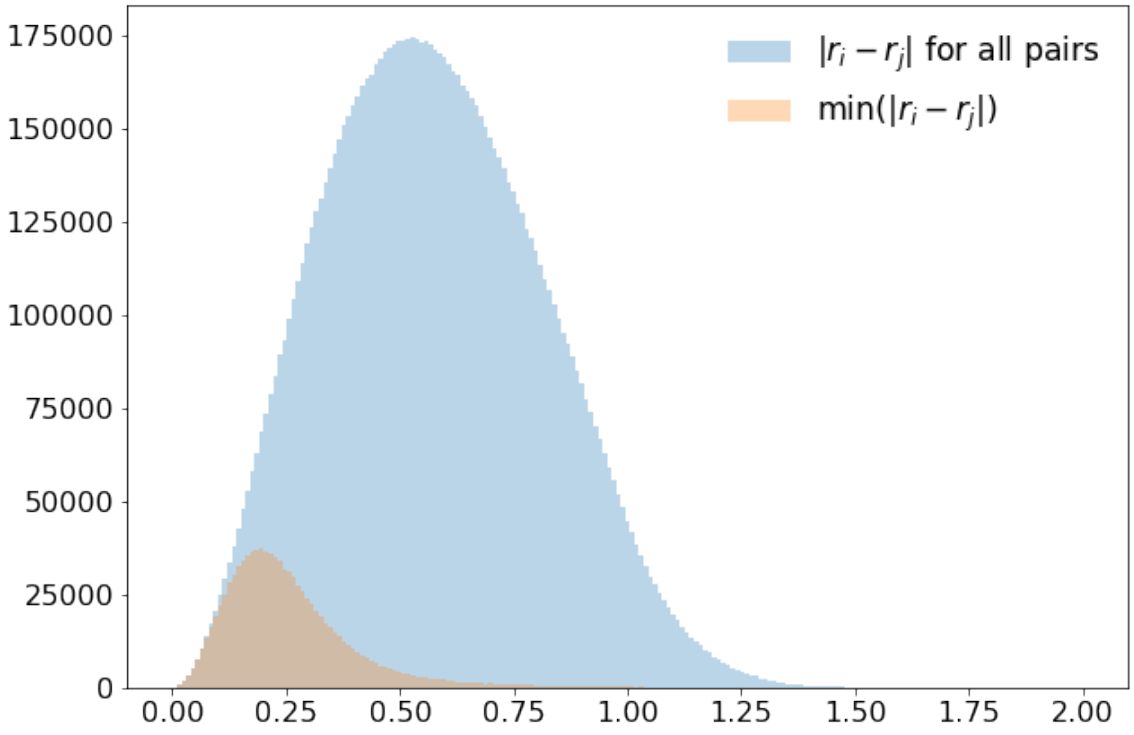

Figure 20: png

2.7 7. Play with two collections of vectors with different size $\{r_i\}_{10}$ and $\{q_i\}_6$

```
q = np.random.random_sample((1000000, 6, 3))
print(q[0:2])
```

```
[[[0.18273329 0.88919754 0.94533167]
  [0.14130847 0.60501287 0.76631964]
  [0.01727239 0.31589769 0.77674801]
  [0.43584386 0.03698427 0.65843665]
  [0.65640608 0.82857438 0.36795615]
  [0.53113251 0.10629633 0.24452858]]

 [[0.6427692  0.17845751 0.12196744]
  [0.23347984 0.48754658 0.96964187]
  [0.75710888 0.999534   0.2420504 ]
  [0.44541921 0.45561578 0.80811487]
  [0.95508582 0.34944633 0.84320844]
  [0.34801462 0.32696285 0.51270624]]]
```

```
def all_pairs_nd(a, b, axis=0):

    # Sanity check
    good_shape = np.array_equal(
        np.delete(a.shape, axis), np.delete(b.shape, axis))
    if not good_shape:
        err = 'The shape along all dimensions but the one of axis={}'.format(
            axis)
        err += ' should be equal, while here:\n'
        err += '  -> shape of a is {} \n'.format(a.shape)
        err += '  -> shape of b is {} \n'.format(b.shape)
        raise NameError(err)

    # Individual indices
    a, b = np.asarray(a), np.asarray(b)
    ia, jb = np.arange(a.shape[axis]), np.arange(b.shape[axis])

    # Pairs of indicies
    dt = np.dtype([('', np.intp)]*2)
    if np.array_equal(a, b):
        ij = np.fromiter(itertools.combinations(ia, 2), dtype=dt)
    else:
        ij = np.fromiter(itertools.product(ia, jb), dtype=dt)
    ij = ij.view(np.intp).reshape(-1, 2)

    # Array of all pairs
    ipair, jpair = ij[:, 0], ij[:, 1]
    return np.stack([a.take(ipair, axis=axis), b.take(jpair, axis=axis)],
     ↪  axis=axis+1)
```

```
p = all_pairs_nd(r, q, axis=1)
print(p.shape)
```

```
(1000000, 60, 2, 3)
```

```
pairs = all_pairs_nd(r, r, axis=1)
print(pairs.shape)
```

```
(1000000, 45, 2, 3)
```

```
# Case where it will crash
p = all_pairs_nd(r, q, axis=2)
```

```
---------------------------------------

NameError                                 Traceback (most recent call last)

<ipython-input-51-b06c074af0d9> in <module>()
      1 # Case where it will crash
--> 2 p = all_pairs_nd(r, q, axis=2)


<ipython-input-48-3ff98aab2b79> in all_pairs_nd(a, b, axis)
     10         err += '  -> shape of a is {} \n'.format(a.shape)
     11         err += '  -> shape of b is {} \n'.format(b.shape)
--> 12         raise NameError(err)
     13
     14     # Individual indices


NameError: The shape along all dimensions but the one of axis=2 should be
equal, while here:
  -> shape of a is (1000000, 10, 3)
  -> shape of b is (1000000, 6, 3)
```

2.8 Appendix: explanation of the function `all_pairs_nd(a,b,axis)`

```
axis = 1

a = np.array([
    [[1, 2], [3, 4]],
    [[5, 6], [7, 8]]
])

b = np.array([
    [[9, 10], [11, 12], [13, 14]],
    [[15, 16], [17, 18], [19, 20]]
])
```

```
a
```

```
array([[[1, 2],
        [3, 4]],

       [[5, 6],
        [7, 8]]])
```

```
b
```

```
array([[[ 9, 10],
        [11, 12],
        [13, 14]],

       [[15, 16],
        [17, 18],
        [19, 20]]])
```

```
# Get the indices of all pairs
ia, jb = np.arange(a.shape[axis]), np.arange(b.shape[axis])
dt = np.dtype([('', np.intp)]*2)
ij = np.fromiter(itertools.product(ia, jb), dtype=dt)
print(ij)
ij = ij.view(np.intp)
print(ij)
ij = ij.reshape(-1, 2)
print(ij)
```

```
[(0, 0) (0, 1) (0, 2) (1, 0) (1, 1) (1, 2)]
[0 0 0 1 0 2 1 0 1 1 1 2]
[[0 0]
 [0 1]
 [0 2]
 [1 0]
 [1 1]
 [1 2]]
```

```
ipair = ij[:, 0]  # fisrt element of ij is the index of a
pairs_a = np.take(a, ipair, axis=1)
pairs_a
```

```
array([[[1, 2],
        [1, 2],
        [1, 2],
        [3, 4],
        [3, 4],
        [3, 4]],

       [[5, 6],
        [5, 6],
        [5, 6],
        [7, 8],
        [7, 8],
        [7, 8]]])
```

```
jpair = ij[:, 1]  # second element of ij is the index of b
pairs_b = np.take(b, jpair, axis=1)
pairs_b
```

```
array([[[ 9, 10],
        [11, 12],
        [13, 14],
        [ 9, 10],
        [11, 12],
        [13, 14]],

       [[15, 16],
        [17, 18],
        [19, 20],
        [15, 16],
        [17, 18],
        [19, 20]]])
```

```
pairs = np.stack([pairs_a, pairs_b], axis=2)
print(pairs.shape)
pairs
```

```
(2, 6, 2, 2)
```

```
array([[[[ 1,  2],
```

```
         [ 9, 10]],

        [[ 1,  2],
         [11, 12]],

        [[ 1,  2],
         [13, 14]],

        [[ 3,  4],
         [ 9, 10]],

        [[ 3,  4],
         [11, 12]],

        [[ 3,  4],
         [13, 14]]],


       [[[ 5,  6],
         [15, 16]],

        [[ 5,  6],
         [17, 18]],

        [[ 5,  6],
         [19, 20]],

        [[ 7,  8],
         [15, 16]],

        [[ 7,  8],
         [17, 18]],

        [[ 7,  8],
         [19, 20]]]])
```

3 Analysis of typical collider data and `numpy` limitation

Caution: this notebook needs to have ROOT installed with python and `root_numpy`.

TODO: print the exact conda environement setup

```
# Disable warnings
import warnings
warnings.filterwarnings('ignore')

# Usual library
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
%matplotlib inline

# Plot settings
import matplotlib as mpl
mpl.rcParams['legend.frameon'] = False
mpl.rcParams['legend.fontsize'] = 'xx-large'
mpl.rcParams['xtick.labelsize'] = 16
mpl.rcParams['ytick.labelsize'] = 16
mpl.rcParams['axes.titlesize'] = 18
mpl.rcParams['axes.labelsize'] = 18
mpl.rcParams['lines.linewidth'] = 2.5

# Time profiling
from timeit import default_timer
import cProfile

# Combinatorics tool
import itertools

# root_numpy (http://scikit-hep.org/root_numpy)
from root_numpy import root2array
```

3.1 1. Loading a `TTree` as a `DataFrame`

Load a TTree and *view* it as a `recarray` (ie a *structured array* with fields accessible as attribute), then convert it into a pandas dataframe very easily. Our collider data are now in a pandas dataframe.

```
ar = root2array('collisions.root', 'event_tree').view(np.recarray)
df = pd.DataFrame(ar)
df.head()
```

```
<tr style="text-align: right;">
  <th></th>
```

```
  <th>jet_pt</th>
  <th>jet_eta</th>
  <th>jet_phi</th>
  <th>jet_mv2c10</th>
  <th>jet_isbtagged_77</th>
  <th>el_pt</th>
  <th>el_eta</th>
  <th>el_phi</th>
  <th>mu_pt</th>
  <th>mu_eta</th>
  <th>mu_phi</th>
  <th>mu</th>
</tr>

<tr>
  <th>0</th>
  <td>[169695.5, 122250.03]</td>
  <td>[-0.39637992, 1.6006567]</td>
  <td>[1.4989699, -1.4390093]</td>
  <td>[0.9628408, 0.99954563]</td>
  <td>[1, 1]</td>
  <td>[55366.094, 38978.633]</td>
  <td>[1.9268323, 0.13278118]</td>
  <td>[-3.0938299, -0.1095593]</td>
  <td>[]</td>
  <td>[]</td>
  <td>[]</td>
  <td>3.5</td>
</tr>
<tr>
  <th>1</th>
  <td>[92278.93, 70800.66, 69653.164, 27776.486]</td>
  <td>[0.40425044, 0.96515447, 0.5671447, 0.6175964]</td>
  <td>[-1.6717116, 1.0977219, -1.2310998, 0.40548608]</td>
  <td>[0.99883986, 0.999752, -0.897119, -0.8301639]</td>
  <td>[1, 1, 0, 0]</td>
  <td>[]</td>
  <td>[]</td>
  <td>[]</td>
  <td>[65079.883, 37495.855]</td>
  <td>[1.3351973, 0.3574057]</td>
  <td>[2.9533806, 3.1300983]</td>
  <td>26.5</td>
</tr>
<tr>
```

```
  <th>2</th>
  <td>[56349.285, 43751.82, 36588.938, 35095.082, 27...</td>
  <td>[0.56248516, 2.4351118, -1.7529668, 1.2876523,...</td>
  <td>[-0.38178313, 1.3481613, -2.3859453, -2.722344...</td>
  <td>[0.9999337, -0.7246226, -0.7773614, -0.9201909...</td>
  <td>[1, 0, 0, 0, 0]</td>
  <td>[76494.64]</td>
  <td>[-0.31438547]</td>
  <td>[-1.9961401]</td>
  <td>[49808.887]</td>
  <td>[-0.17943819]</td>
  <td>[-3.1100628]</td>
  <td>27.5</td>
</tr>
<tr>
  <th>3</th>
  <td>[59820.547, 41592.062]</td>
  <td>[-2.302116, -2.218402]</td>
  <td>[1.9511205, 0.5742027]</td>
  <td>[-0.82315505, 0.9919272]</td>
  <td>[0, 1]</td>
  <td>[39917.418]</td>
  <td>[-1.3356979]</td>
  <td>[2.6993954]</td>
  <td>[103460.734]</td>
  <td>[-2.07254]</td>
  <td>[-1.3708612]</td>
  <td>9.5</td>
</tr>
<tr>
  <th>4</th>
  <td>[196711.52, 123898.07, 87307.625, 82197.49, 41...</td>
  <td>[-2.2168732, -0.5487006, -1.6435306, -1.037495...</td>
  <td>[-0.24934195, 0.61117375, 1.870176, -2.149553,...</td>
  <td>[-0.97217584, -0.9577969, -0.88246375, 0.99995...</td>
  <td>[0, 0, 0, 1, 0, 0]</td>
  <td>[197385.73]</td>
  <td>[-0.749733]</td>
  <td>[-2.845913]</td>
  <td>[34190.586]</td>
  <td>[-1.418337]</td>
  <td>[-1.6127276]</td>
  <td>12.5</td>
</tr>
```

```
print('Number of events: {:.0f}'.format(len(df)))
```

```
Number of events: 250000
```

3.2 2. Variable-size arrays and "squared" arrays

Pandas is very nice and powerful for flat numbers (*i.e.* no arrays), while in collider physics we have various collections of physics objects (of various size) for each events. This means two things: 1. it's very common to have arrays per event and not only numbers 2. the size of the array will change from an event to another (those are called *jagged arrays*).

Doing pure python is not a problem with jagged arrays but it's impossible to benefit from `numpy` vectorization since this requires well defined shape. In practice, the numpy array obtained by `df.values` is a 1D-array of arrays, and not a n-dimenional array:

```
array_jet_pt = df['jet_pt'].values
print('shape: {}'.format(array_jet_pt.shape))
```

```
shape: (250000,)
```

```
# Comprehensive loop for Njets
%timeit Njets=[len(j) for j in array_jet_pt]
```

```
10 loops, best of 3: 53.9 ms per loop
```

3.2.1 2.1 Squaring arrays

In order to work around this issue, one can "square jagged arrays" by setting the variable size to the maximum number of objects among all events, and fill empty values with a dummy value (to be carefully chosen depending on your computation). This is exactly what the function `square_jagged_2Darray(a,val=value,nobj=Nmax)` does, as illustrated below. The cell below prints the jet p_T array for the three first event, for different formating of the array. The construction of this function is detailed (and timed) after.

```
# Utils function to manipulate jagged arrays
import np_utils as npu
```

```
# Main function
help(npu.square_jagged_2Darray)
```

```
Help on function square_jagged_2Darray in module np_utils:

square_jagged_2Darray(a, **kwargs)
    Give the same dimension to all raws of a jagged 2D array.

    This function equalizes the the size of every raw (obj collection)
    using a default value 'val' (nan if nothing specifed) using either
    the maximum size of object collection among all column (events) or
    using a maximum size 'size'. The goal of this function is to fully
    use numpy vectorization which works only on fixed size arrays.

    Parameters
    -----
    a: array of arrays with different sizes this is the jagged 2D
    array to be squared

    keyword arguments
    ---------
    dtype: string
        data type of the variable-size array. If not specified,
        it is 'float32'. None means dt=data.dt.
    nobj: int
        max size of the array.shape[1]. if not specified (or None),
        this size is the maximum size of all raws.
    val: float32
        default value used to fill empty elements in order to get
        the proper size. If not specified (or None), val is np.nan.

    Returns
    ----
    out: np.ndarray
        with a dimension (ncol,nobj).

    Examples
    ----
    >> import numpy as np
    >> a=np.array([
        [1,2,3,4,5],
        [6,7],
        [8],
        [9,10,11,12,13]
```

```
    ])
    »>
    »> square_jagged_2Darray(a)
    array([[  1.,   2.,   3.,   4.,   5.],
       [  6.,   7.,  nan,  nan,  nan],
       [  8.,  nan,  nan,  nan,  nan],
       [  9.,  10.,  11.,  12.,  13.]], dtype=float32)
    »>
    »> square_jagged_2Darray(a,nobj=2,val=-999)
    »> array([[   1.,    2.],
       [   6.,    7.],
       [   8., -999.],
       [   9.,   10.]], dtype=float32)
```

```
# Raw numbers (ie before squaring)
print('\n\nBefore squaring:')
print('================')
jet_pt_df = df['jet_pt'].values
print('shape: {}'.format(jet_pt_df.shape))
for pt in jet_pt_df[0:3]:
    print(len(pt), pt)

# After squaring
print('\n\nAfter squaring:')
print('===============')
jet_pt_np = npu.square_jagged_2Darray(jet_pt_df, val=-999)
print('shape: {}'.format(jet_pt_np.shape))
for pt in jet_pt_np[0:3]:
    print(len(pt), pt)

# After squaring with Nmax=3
print('\n\nAfter squaring with Nmax=3:')
print('============================')
jet_pt_np = npu.square_jagged_2Darray(jet_pt_df, val=-999, nobj=3)
print('shape: {}'.format(jet_pt_np.shape))
for pt in jet_pt_np[0:3]:
    print(len(pt), pt)
```

```
Before squaring:
================
shape: (250000,)
(2, array([169695.5 , 122250.03], dtype=float32))
(4, array([92278.93 , 70800.66 , 69653.164, 27776.486], dtype=float32))
(5, array([56349.285, 43751.82 , 36588.938, 35095.082, 27441.059],
```

```
      dtype=float32))


After squaring:
===============
shape: (250000, 11)
(11, array([169695.5 , 122250.03,   -999.  ,   -999.  ,   -999.  ,   -999.  ,
         -999.  ,   -999.  ,   -999.  ,   -999.  ,   -999.  ],
      dtype=float32))
(11, array([92278.93 , 70800.66 , 69653.164, 27776.486,  -999.   ,  -999.   ,
        -999.   ,  -999.   ,  -999.   ,  -999.   ,  -999.   ],
      dtype=float32))
(11, array([56349.285, 43751.82 , 36588.938, 35095.082, 27441.059,  -999.   ,
        -999.   ,  -999.   ,  -999.   ,  -999.   ,  -999.   ],
      dtype=float32))


After squaring with Nmax=3:
===========================
shape: (250000, 3)
(3, array([169695.5 , 122250.03,   -999.  ], dtype=float32))
(3, array([92278.93 , 70800.66 , 69653.164], dtype=float32))
(3, array([56349.285, 43751.82 , 36588.938], dtype=float32))
```

3.2.2 2.2 Typical timing

```
# Getting the array directly
%timeit df['jet_pt'].values

# Squaring the array
%timeit npu.square_jagged_2Darray(jet_pt_df, val=-999)

# # Squaring the array with max 3 objects
%timeit npu.square_jagged_2Darray(jet_pt_df, val=-999, nobj=3)
```

```
The slowest run took 11.50 times longer than the fastest. This could mean
that an intermediate result is being cached.
100000 loops, best of 3: 2.78 µs per loop
1 loop, best of 3: 214 ms per loop
1 loop, best of 3: 245 ms per loop
```

3.2.3 2.3 Detail of `square_jagged_2Darray()` function

As it was probably noted, the `square_jagged_2Darray()` is longer than directly taking the numpy array. This is mostly due to two steps: scanning to find the max of object numbers, and the concatenation of all individual arrays. At the end, loading the squared numpy array takes 0.2 seconds for 250 kEvents. The timing and the details of operation is shown below:

```
# 0. Getting the 1D array of arrays
jet_pt_df = df['jet_pt'].values

# 1. Getting all the sub-array length
%timeit lens = np.array([len(i) for i in jet_pt_df])
lens = np.array([len(i) for i in jet_pt_df])
print('lens:\n {}'.format(lens[:3]))

# 2. Create a mask to know which value should be filled
%timeit mask = np.arange(lens.max()) < lens[:, None]
mask = np.arange(lens.max()) < lens[:, None]
print('mask:\n {}'.format(mask[:3]))

# 3. Initialize the final squared array
%timeit out = np.zeros(mask.shape, dtype='float32')
out = np.zeros(mask.shape, dtype='float32')
print('out:\n {}'.format(out[:3]))

# 4. Fill the default values where needed
%timeit out.fill(999)
out.fill(999)
print('out:\n {}'.format(out[0:3]))

# 5. Fill the 1D array (out[mask]) of all jet pT with the values using
 ↪  concatenate
%timeit out[mask] = np.concatenate(jet_pt_df)
jet_pt_1d = np.concatenate(jet_pt_df)
out[mask] = jet_pt_1d
print(('out:\n {}'.format(out[0:3])))
```

```
10 loops, best of 3: 63.4 ms per loop
lens:
 [2 4 5]
100 loops, best of 3: 4.15 ms per loop
mask:
 [[ True  True False False False False False False False False False]
 [ True  True  True  True False False False False False False False]
```

```
 [ True  True  True  True  True False False False False False False]]
1000 loops, best of 3: 640 µs per loop
out:
 [[0. 0. 0. 0. 0. 0. 0. 0. 0. 0.]
 [0. 0. 0. 0. 0. 0. 0. 0. 0. 0.]
 [0. 0. 0. 0. 0. 0. 0. 0. 0. 0.]]
1000 loops, best of 3: 727 µs per loop
out:
 [[999. 999. 999. 999. 999. 999. 999. 999. 999. 999. 999.]
 [999. 999. 999. 999. 999. 999. 999. 999. 999. 999. 999.]
 [999. 999. 999. 999. 999. 999. 999. 999. 999. 999. 999.]]
10 loops, best of 3: 108 ms per loop
out:
 [[169695.5   122250.03     999.       999.       999.       999.
     999.       999.       999.       999.       999.    ]
 [ 92278.93   70800.66   69653.164  27776.486    999.       999.
     999.       999.       999.       999.       999.    ]
 [ 56349.285  43751.82   36588.938  35095.082  27441.059    999.
     999.       999.       999.       999.       999.    ]]
```

Another function called `df2array()` allows to load several columns (with the same maximum size) into a given nd array. This is needed if one wants to make computations based on all those columns. The best example is the dR variable which involves both η and ϕ. These two variables can be grouped in a big numpy array of dimension `(Nevts,Njets,2)`, where 2 corresponds to the number of variables. This function is internally call the np.stack() method (on top of some checks):

```
jets_kin = npu.df2array(df,['jet_pt','jet_eta','jet_phi'])
```

is equivalent to

```
jets_pt  = npu.square_jagged_2Darray(df['jet_pt'].values)
jets_eta = npu.square_jagged_2Darray(df['jet_eta'].values)
jets_phi = npu.square_jagged_2Darray(df['jet_phi'].values)
jets_kin = np.concatenate([jets_pt,jets_eta,jets_phi],axis=2)
```

```
jets_kin = npu.df2array(df[0:1000], ['jet_pt', 'jet_eta', 'jet_phi'])
print(jets_kin.shape)

jets_btg = npu.df2array(df[0:1000], ['jet_mv2c10', 'jet_isbtagged_77'])
print(jets_btg.shape)
```

```
jets = npu.df2array(df[0:1000], ['jet_pt', 'jet_eta',
                                 'jet_phi', 'jet_mv2c10',
                                  ↪  'jet_isbtagged_77'])
print(jets.shape)
```

```
(1000, 8, 3)
(1000, 8, 2)
(1000, 8, 5)
```

```
# Load jet array for all events
jets = npu.df2array(df, ['jet_pt', 'jet_eta', 'jet_phi',
                         'jet_mv2c10', 'jet_isbtagged_77'])
```

3.3 3. Producing some non-trivial plots using numpy arrays

Everything which is based on flat number can be directly done pandas columns directly, *e.g.* the following code will be similarly efficient as with a `TTree->Draw()` command.

```
plt.figure(figsize=(10,7))
ax=plt.hist(df['mu'])
```

But the more tricky part is what to do with python to make some more complex computations **without doing an explicit event loop**? The next sub-sections give some examples.

```
plt.figure(figsize=(10, 7))
ax = plt.hist(df['mu'])
```

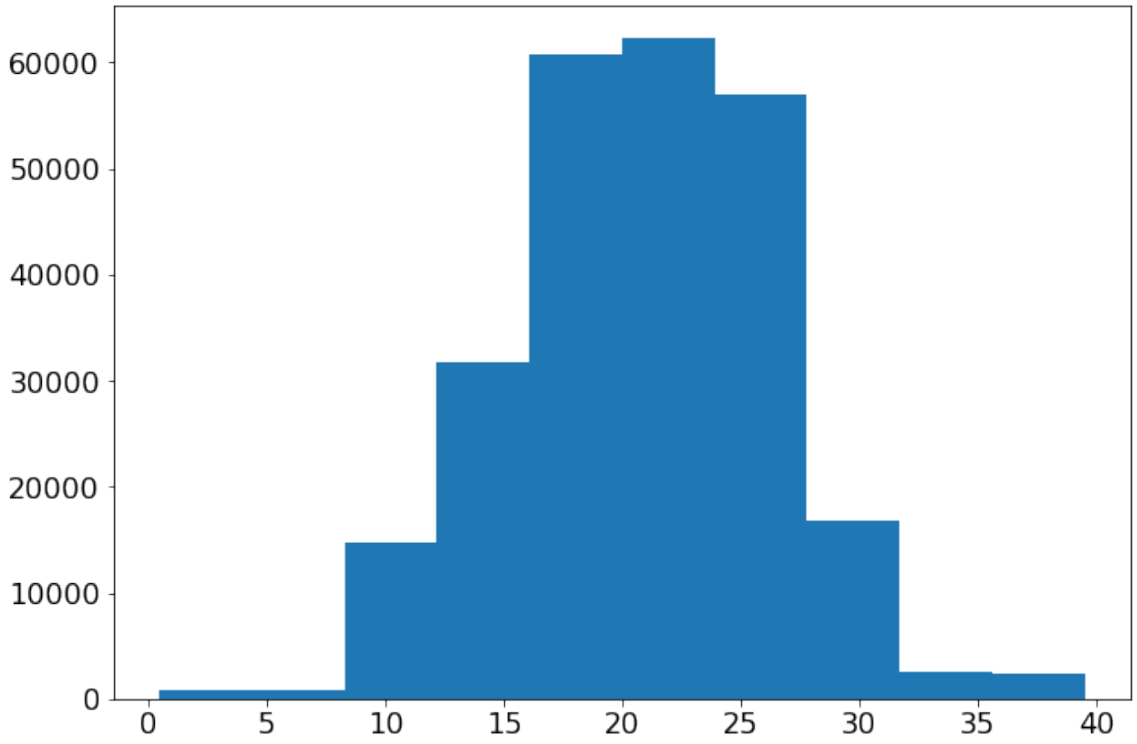

Figure 21: png

3.3.1 3.1 Jet multiplicity for different p_T thresholds

Looking at the jet multiplicity depending on the p_T threshold: + `jets[...:0]` means that all dimention but the last one is inclusive (here it means all events and all jets for each events), while the 0 means first variable (*i.e.* the p_T since it comes first in the command `df2array(df, ['jet_pt', 'jet_eta', 'jet_phi', 'jet_mv2c10', 'jet_isbtagged_77']);` + `jets[...,0]>pt` is a 2D arrays filled of shape (Nevts,Njets) with `True` and `False` depending on wether the element is above `pt` or not; + `np.count_nonzero(jets[...,0]>pt, axis=1)` is 1D array of shape (Nevts) which counts the number of `True` along the Njets axis (so per event).

```
plt.figure(figsize=(10, 7))
for pt in np.linspace(25, 100, 4)*1000:
    ax = plt.hist(np.count_nonzero(jets[..., 0] > pt, axis=1),
                  label='$p_T>{:.0f}$ GeV'.format(pt/1000.),
                  alpha=0.8, histtype='step', linewidth=3,
                  bins=np.linspace(0, 15, 15), log=True)
ax = plt.legend()
ax = plt.xlabel('$N_{jets}(p_T>X)$')
ax = plt.ylabel('Event count')
```

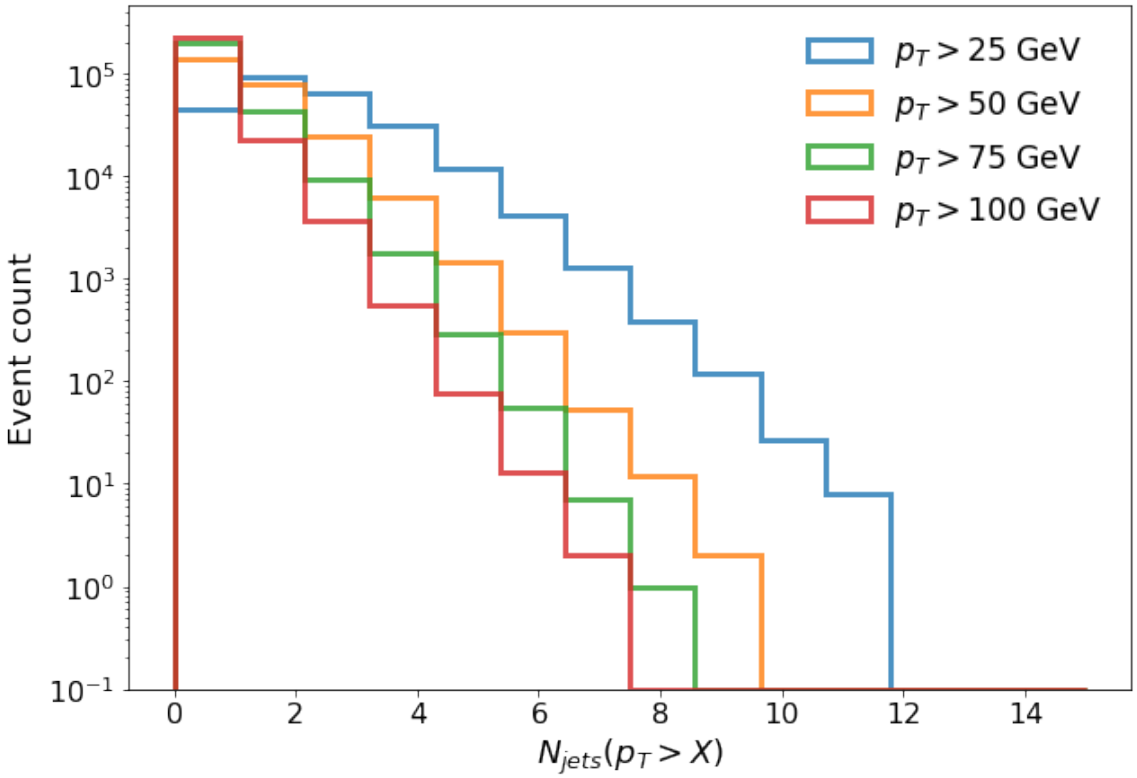

Figure 22: png

3.3.2 3.2 Jet p_T distribution for every jets in the event

This is also very easy to look at the p_T distributions of the leading, sub-leading, ... jets. For this, one first needs to replace all `nan` (not a number) by a appropriate default value (0 for instance), otherwise the plotting step will crash (cannot plot `nan`). Then a loop over all the jets is performed (the number of jets is the size of the dimension 2, *i.e.* `shape[1]`).

```
jets_pt_plots = npu.replace_nan(jets[..., 0], value=0)

fig = plt.figure(figsize=(10, 7))
Njets = jets_pt_plots.shape[1]
for i in np.arange(Njets):
    ax = plt.hist(jets_pt_plots[:, i]/1000., alpha=0.3, linewidth=3,
                  bins=np.linspace(25, 2000, 100), log=True, label='jet
↪  {}'.format(i+1))
ax = plt.legend()
ax = plt.xlabel('$p^{jets}_T$ [GeV]')
ax = plt.ylabel('Unweighted events')
```

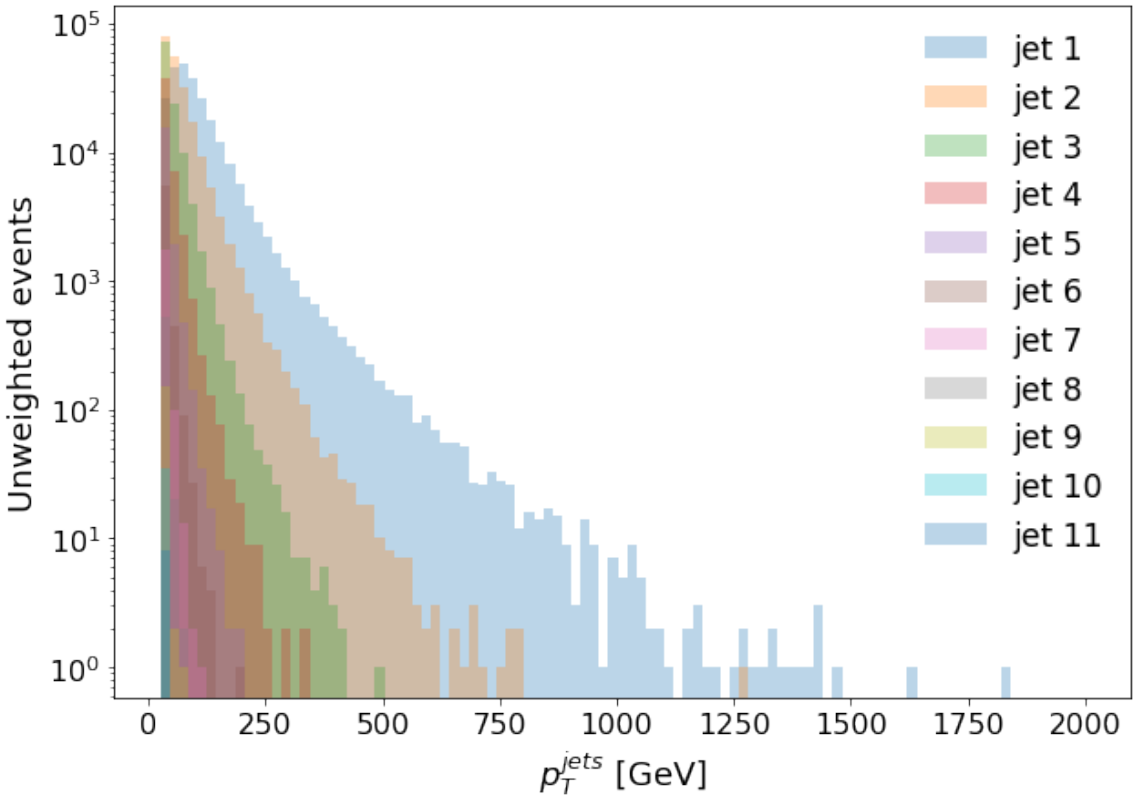

Figure 23: png

3.3.3 3.3 *Apparte:* difference between `a*(a>x)` and `a[a>x]`

First of all `a>x` is an array filled with `True` or `False` depending on whether the condition is true or false (in numpy, it is called a *mask*). What do the two diffent commands is: + `a[a>x]` return all elements of a which pass the condition. In practice, it removes the other elements from the array. **This is always a 1D array**. + `a*(a>x)` return the product of `a` and `a>x` converted into a `int` (so 0 or 1). In practice, it replaces the values not passing the condition by by `False` or `0`. + if `a` is multi-dimentional, `a[a>x]` will be a flat (1D) array. This is unavoidable since the output would be a jagged array. Indeed, for a 2D array, the number of elements per line might depends on the line.

This is illustrated with examples below for both 1D and 2D arrays.

```
# 1D arrays
a = np.arange(12)
print('a       = {}'.format(a))
print('a>4     = {}'.format(a > 4))
print('a*(a>4) = {}'.format(a*(a > 4)))
print('a[a>4]  = {}'.format(a[a > 4]))
```

```
a       = [ 0  1  2  3  4  5  6  7  8  9 10 11]
a>4     = [False False False False False  True  True  True  True  True  True
True]
a*(a>4) = [ 0  0  0  0  0  5  6  7  8  9 10 11]
a[a>4]  = [ 5  6  7  8  9 10 11]
```

```
# 2D arrays
a = np.arange(12).reshape(6, 2)
print('a       = {}'.format(a))
print('a>4     = {}'.format(a > 4))
print('a*(a>4) = {}'.format(a*(a > 4)))
print('a[a>4]  = {}'.format(a[a > 4]))
```

```
a       = [[ 0  1]
 [ 2  3]
 [ 4  5]
 [ 6  7]
 [ 8  9]
 [10 11]]
a>4     = [[False False]
 [False False]
 [False  True]
 [ True  True]
 [ True  True]
 [ True  True]]
a*(a>4) = [[ 0  0]
 [ 0  0]
 [ 0  5]
 [ 6  7]
 [ 8  9]
 [10 11]]
a[a>4]  = [ 5  6  7  8  9 10 11]
```

3.3.4 3.4 H_T distribution in different configurations

One can also recompute observables using only objects passing certain selections (this is not so easy to do with `TTree->Draw()` commands). Let's take the example of H_T defined as the scalar sum of p_T over the jets (probing the "hardness" of the collision): + Usual case: `jet_pt_ht` is the p_T array with a shape (Nevt,Njets), so sum over axis=1 will give the H_T array with shape (Nevts). `HTjets[HTjets>0]` means removing events with $H_T = 0$ (if not jets at all for example); + Compte H_T only with central jets: `jet_pt_ht*(np.abs(jet_eta)<1.0)` is an array containing only p_T of jets with $|\eta| < 1.0$, then the logic remains the same; + Compte H_T

only with b-tagged jets: `jet_pt_ht*(jet_btagw>0.67)` is an array containing only p_T of jets with $w_b > 0.67$.

```
jet_pt_ht = npu.replace_nan(jets[..., 0], value=0)/1000.
jet_eta = jets[..., 1]
jet_btagw = jets[..., 3]
```

```
fig = plt.figure(figsize=(10, 7))

# Compute usual HT jets
HTjets = np.sum(jet_pt_ht, axis=1)
ax = plt.hist(HTjets[HTjets > 0], alpha=0.5, bins=np.linspace(
    0, 2000, 100), label='$|eta|<2.5$', log=True)

# Compute HT only with central jets
central_jet_pt_ht = jet_pt_ht*(np.abs(jet_eta) < 1.0)
HTjets_central = np.sum(central_jet_pt_ht, axis=1)
ax = plt.hist(HTjets_central[HTjets_central > 0], alpha=0.5,
↪  bins=np.linspace(
    0, 2000, 100), label='$|eta|<1$', log=True)

# Compute HT only with b-jets
bjets_pt_ht = jet_pt_ht*(jet_btagw > 0.67)
HTbjets = np.sum(bjets_pt_ht, axis=1)
ax = plt.hist(HTbjets[HTbjets > 0], alpha=0.5, bins=np.linspace(
    0, 2000, 100), label='b-jets', log=True)

ax = plt.title('All jets vs central jets $|\eta|<1$')
ax = plt.xlabel('$H_T$ [GeV]')
ax = plt.ylabel('Unweighted events')
ax = plt.legend(title='$t\\bar{t}$')
```

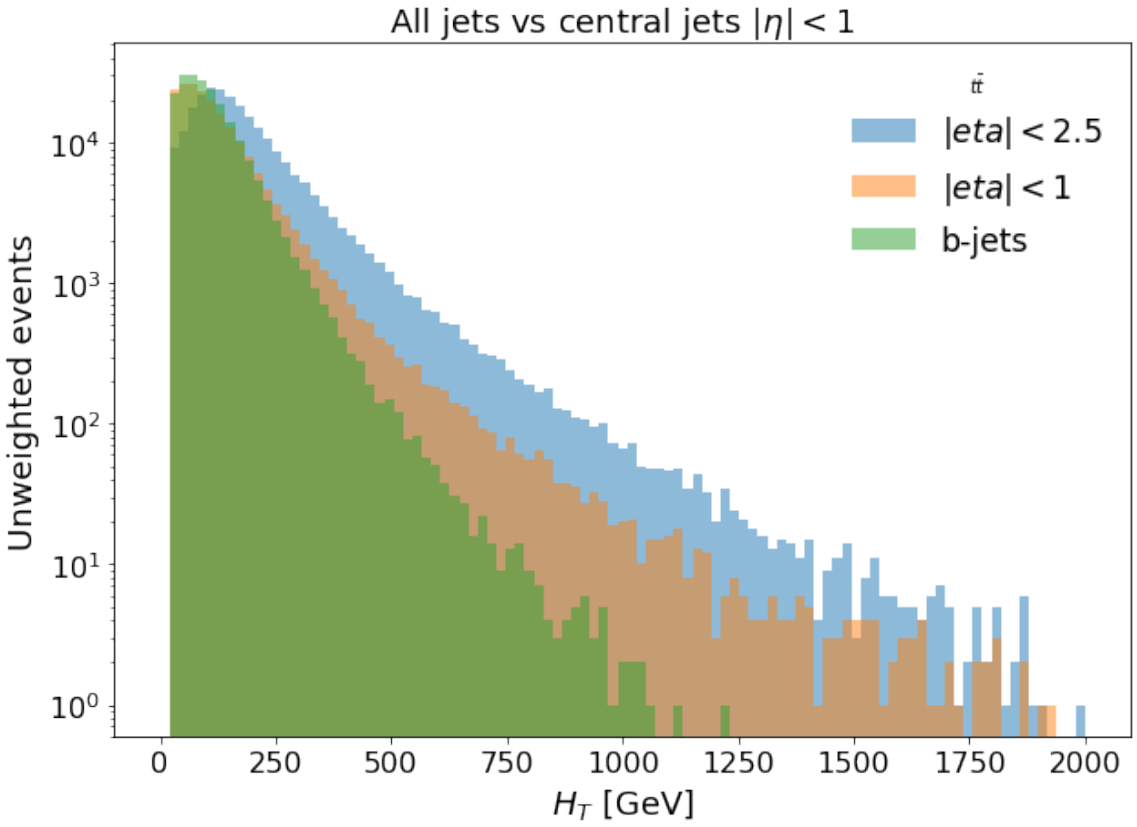

Figure 24: png

3.4 4. Perform computations that would normally be done in an event loop

There are many obvious use cases of doing these typical operations: + identify the jet which is the closest of a given lepton (minimum ΔR computation) + compute invariant mass between all possible electrons and find the combination corresponding to a Z decay + find the jet pair which best match a hadronic W decay

In principle, the same methodology could be applied to combination having more than 2 objects (rough decay reconstruction). But this can be quite long to compute - depending on the number of events - because we have to deal with large number of objects (the max one, in order to get fixed-size array). One option though, is to limit the number of object participating to the combination, by taking for example the 5th first leading p_T jets. In our current example, this would reduce the number of jets from 13 to 5 (in term of N(N-1)/2 combinations: 78 to 10).

3.4.1 4.1 Getting all possible pairs of jets

```
jet_pairs = npu.all_pairs_nd(jets)
print(jet_pairs.shape)
```

```
(250000, 55, 2, 5)
```

3.4.2 How to select only events with at least two objects?

In the case of making pairs of the two same objects, one needs to make sure there are at least two! Let's take the example of jets:

1. we need to compute the number of jets, *i.e.* the number of not `nan` per event (since empty elements are set to `nan`), which can be done for any variable (here p_T): `python nj=npu.count_nonnan(jets[...,0],axis=1)`
2. Select all jets and all variables for events with `nj>1`: `python jets_atl2 = jets[nj>1,...]`

```
nj=npu.count_nonnan(jets[...,0],axis=1)
print('There are {} events without any jets'.format(np.count_nonzero(nj==0)))
is_0j = nj==0
print(is_0j.shape)
jets_atl2 = jets[~is_0j]
print(jets_atl2.shape)
```

```
There are 4803 events without any jets
(250000,)
(245197, 11, 5)
```

3.4.3 4.2 Compute pair-related observables

Once the pairs are formed, we can do any computation with it. For convenience, you can make two variables being the first jet `j1` and the second jet `j2` of the pair. Those will be array of shape (Nevt,Npair,Nvar):

```
j1, j2 = jet_pairs[:, :, 0, :], jet_pairs[:, :, 1, :]
print(j1.shape, j2.shape)
```

```
((250000, 55, 5), (250000, 55, 5))
```

3.4.3.1 Minimum $\Delta R(j,j)$

We can then take the sum, the difference, the invariant mass or anthing else based on `j1` and `j2`. Below, we form the array of $(\Delta\eta, \Delta\phi)$ for each pair, having a shape (Nevt,Npair,2):

```
# keep only eta,phi to compute dR=sqrt(deta^2+dphi^2)
dj_etaphi = j1[..., 1:3] - j2[..., 1:3]

# remove nan by a relevant default values (outside plots)
dj_etaphi = npu.replace_nan(dj_etaphi, value=999)

# print the 5th first pair of the 3rd event
print(dj_etaphi.shape, dj_etaphi[2, 0:5])
```

```
((250000, 55, 2), array([[-1.8726265e+00, -1.7299445e+00],
       [ 2.3154519e+00,  2.0041623e+00],
       [-7.2516710e-01,  2.3405614e+00],
       [-1.8223300e+00,  2.6417046e+00],
       [ 9.9900000e+02,  9.9900000e+02]], dtype=float32))
```

```
dR = np.sum(dj_etaphi**2, axis=2)**0.5
print(dR.shape, dR[0, 0:5])

dR = npu.replace_val(dR, (2**0.5)*999., 999)
print(dR.shape, dR[0, 0:5])
```

```
((250000, 55), array([   3.5524466, 1412.7993   , 1412.7993   , 1412.7993   ,
       1412.7993   ], dtype=float32))
((250000, 55), array([  3.5524466, 999.       , 999.       , 999.       ,
999.       ],
      dtype=float32))
```

```
fig = plt.figure(figsize=(10, 7))
ax = plt.hist(dR.flatten(), bins=np.linspace(
    0, 8, 100), alpha=0.5, label='All jet pairs')
ax = plt.hist(np.min(dR, axis=1), bins=np.linspace(
    0, 8, 100), alpha=0.5, label='Minimal $\Delta R$')
ax = plt.xlabel('$\Delta R(j,j$)')
ax = plt.ylabel('Unweighted events')
ax = plt.legend()
```

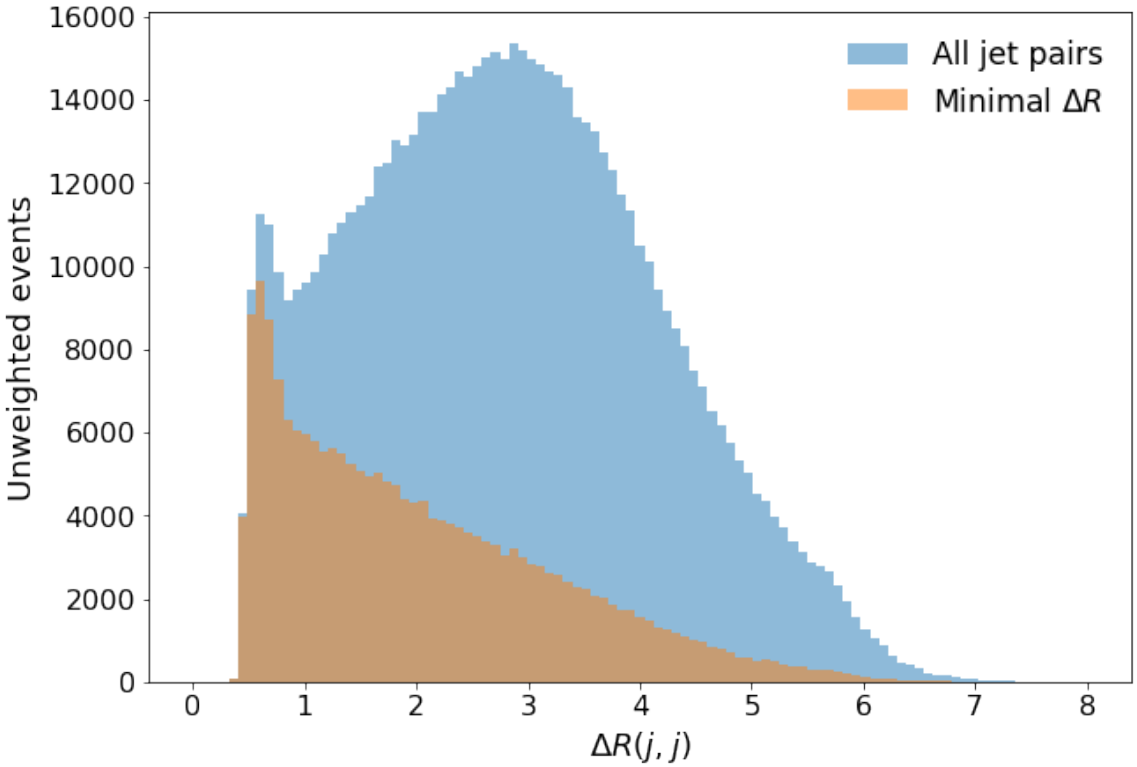

Figure 25: png

3.4.3.2 Minimum $\Delta R(j,e)$

```
jet_direction = jets[:, :, 1:3]
ele_direction = npu.df2array(df, ['el_eta', 'el_phi'])
```

```
jet_ele_pairs_direction = npu.all_pairs_nd(jet_direction, ele_direction)
```

```
dej = jet_ele_pairs_direction[:, :, 0, :]-jet_ele_pairs_direction[:, :, 1, :]
dRej = npu.replace_nan(np.sum(dej**2, axis=2)**0.5, value=999)
dRmin = np.min(dRej, axis=1)
```

```
fig = plt.figure(figsize=(10, 7))
style = {
    'bins': np.linspace(0, 8, 100),
    'alpha': 0.5,
    'density': True,
    'log': True,
}
```

```
ax = plt.hist(dRej.flatten(), label='All jet-electron pairs', **style)
ax = plt.hist(dRmin, label='Minimal $\Delta R$', **style)
ax = plt.xlabel('$\Delta R(j,e)$')
ax = plt.ylabel('Unweighted events')
ax = plt.legend()
```

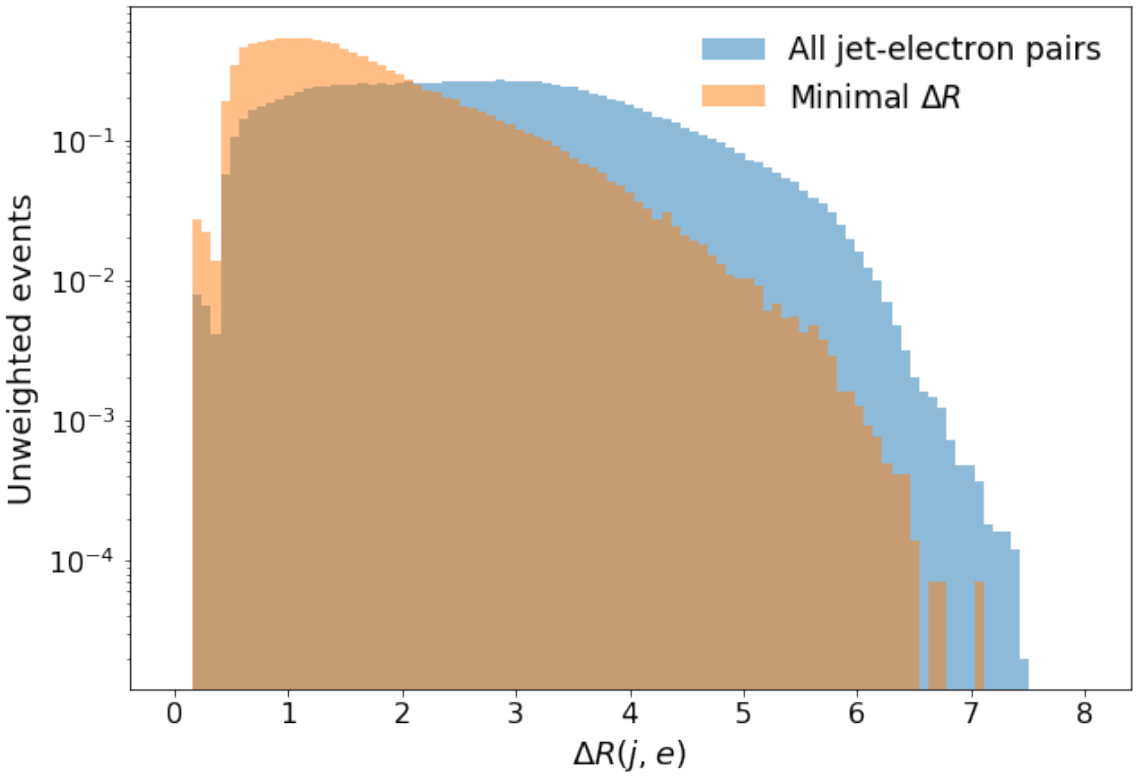

Figure 26: png

3.4.4 Di-jet invariant masses

Let's take the example of the invariant mass betwee `j1` and `j2`:

$$m^2 = p_{T1}^2 p_{T2}^2 (\cosh(\eta_1 - \eta_2) - \cos(\phi_1 - \phi_2))$$

```
deta, dphi = dj_etaphi[..., 0], dj_etaphi[..., 1]
pt1, pt2 = j1[..., 0], j2[..., 0]
print(pt1.shape, deta.shape)
```

```
((250000, 55), (250000, 55))
```

```
m = np.sqrt(pt1*pt2 * (np.cosh(deta)-np.cos(dphi))) / 1000.
m = npu.replace_nan(m, 1e10)
print(m.shape)
```

```
(250000, 55)
```

```
fig = plt.figure(figsize=(10, 7))

style = {
    'bins': np.linspace(0, 500, 100),
    'alpha': 0.8,
    'density': True,
    'log': False,
    'histtype': 'step',
    'linewidth': 3.0
}

ax = plt.hist(m.flatten(), label='All pairs', **style)
ax = plt.hist(np.min(m, axis=1), label='Min $M(j,j)$', **style)
ax = plt.hist(np.max(npu.replace_val(m, 1e10, -1e10), axis=1),
              label='Max M$(j,j)$', **style)
ax = plt.xlabel('$M(j,j)$ [GeV]')
ax = plt.ylabel('Unweighted events')
ax = plt.legend()
```

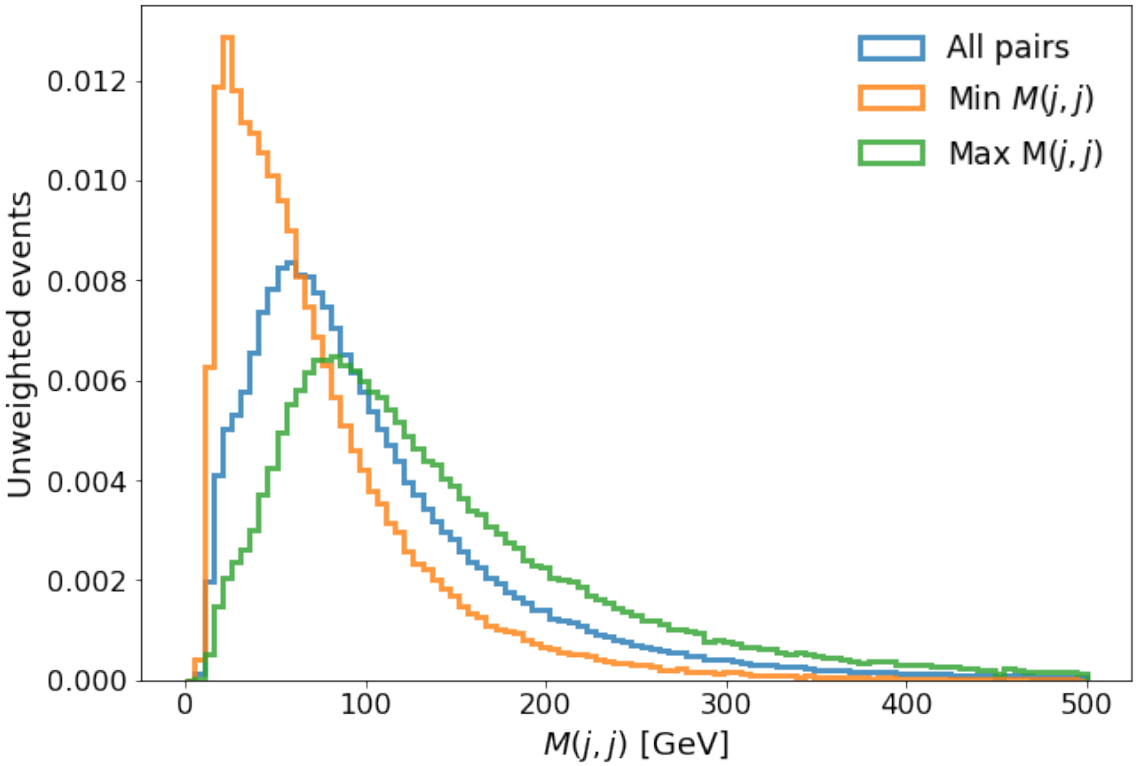

Figure 27: png

3.5 5. Build up system of several collections (e.g. electrons and jets)

Explain what is it ... basically building a colletion made of several entities: *e.g.* `lep={el+mu}` or `EMobj={jets+ele}`

3.5.1 5.1 Preamble: implementing default values like `df2array(df,['var1','var2','999'])`

This would be useful to work around the constrain of having the same number of variable per object. For example, if one want to make all possible pairs of electrons and jets or simply group the collection together, we need to have the same dimension along the variable axis (*i.e.* axis=3). Of course, variables for jets might not exist for electrons (or the opposit). Concretely, the following code

```
jets      =
↪  df2array(df,['jet_pt','jet_eta','jet_phi','jet_mv2c10','jet_isbtagged_77'])
electrons = df2array(df,['el_pt' ,'el_eta' ,'el_phi'])
ele_jets  = all_pairs_nd(jets,electrons)
```

will not work and will return something like

```
NameError: The shape along all dimensions but the one of axis=1 should be
equal, while here:
  -> shape of a is (1000, 8, 5)
  -> shape of b is (1000, 3, 3)
```

The adopted possibility is to be able to set a default value just to have the proper number of variable for both object **and** remember that this is a dummy value, like

```
jets      =
↪  df2array(df,['jet_pt','jet_eta','jet_phi','jet_mv2c10','jet_isbtagged_77'])
electrons = df2array(df,['el_pt' ,'el_eta' ,'el_phi' ,      '-999',
↪  'nan'])
ele_jets  = all_pairs_nd(jets,electrons)
```

Since `jets` currently contains 5 variables, one needs to build up a collection of electrons with 5 variables. But the btagg weight is not defined for electron, se we put a dummy value (otherwise the stacking cannot work).

```
print(jets.shape)
```

```
(250000, 11, 5)
```

```
eles = npu.df2array(df, ['el_pt', 'el_eta', 'el_phi', 'nan', 'nan'])
```

```
jets_eles = npu.stack_collections([jets, eles])
print(jets.shape, eles.shape, jets_eles.shape)
```

```
((250000, 11, 5), (250000, 3, 5), (250000, 14, 5))
```

```
jet_el_pt = npu.replace_nan(jets_eles[:, :, 0])
jet_el_HT = np.sum(jet_el_pt/1000., axis=1)
print(jet_el_HT.shape)
```

```
(250000,)
```

```
fig = plt.figure(figsize=(10, 7))
plt.hist(jet_el_HT[jet_el_HT > 0], bins=np.linspace(0, 1000, 100), alpha=0.5)
ax = plt.xlabel('$\sum_{e,j} \; p_T$ [GeV]')
ax = plt.ylabel('Unweighted events')
```

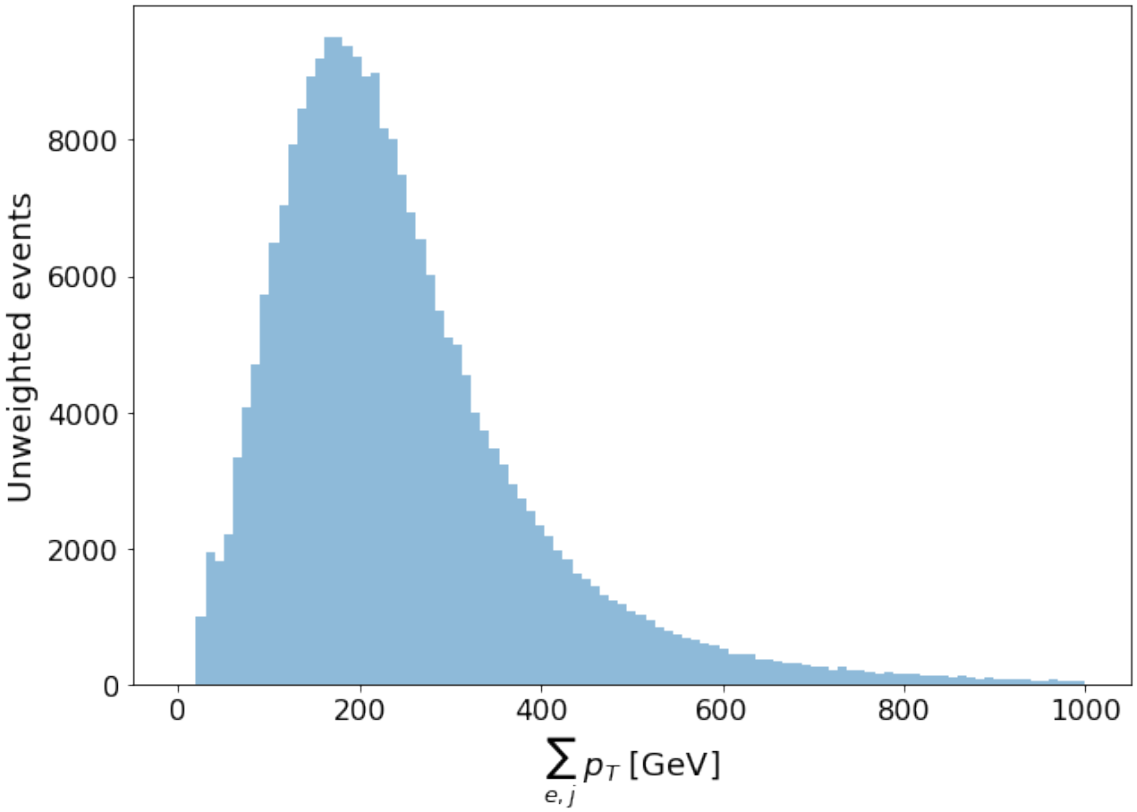

Figure 28: png

3.5.2 5.3 Select an object based on event-based criteria (distance, invariant mass, etc ...)

The goal of this section is to look at say the isolation of the leptons which form a pair having $M(e,e) \sim M(Z)$.

3.5.2.1 E.g. 1: compare the b-tagging weight of the jet closest to an electron and the others

We reform all the pair here, but not only with the direction but all needed variables:

```
jets_elec_pairs = npu.all_pairs_nd(jets, eles)
print(jets.shape, eles.shape, jets_elec_pairs.shape)
```

```
((250000, 11, 5), (250000, 3, 5), (250000, 33, 2, 5))
```

Then we need to isolate an array of shape (Nevt,Npair) contanining the btagg weight (3rd variable) of the first element (*i.e.* the jet) for any pair: `btagw=jets_ele[:,:,0,3]`

```
jet_btag_w = npu.replace_nan(jets_elec_pairs[:, :, 0, 3], value=999)
```

Reminder of $dR(e,j)$ and min$dR(e,j)$ distribution (already computed from before):

```
fig = plt.figure(figsize=(20, 7))
plt.subplot(121)
ax = plt.hist(dRmin, bins=np.linspace(0, 8, 100), alpha=0.5,
              density=True, log=True, label='Smallest $dR$')
ax = plt.hist(dRej.flatten(), bins=np.linspace(0, 8, 100),
              alpha=0.5, density=True, log=True, label='All pairs')
ax = plt.xlabel('$dR(j,e)$')
ax = plt.ylabel('PDF')
ax = plt.legend()

plt.subplot(122)
ax = plt.hist(dRmin, bins=np.linspace(0, 0.5, 50), alpha=0.5, density=True)
ax = plt.xlabel('min $dR(j,e)$')
ax = plt.ylabel('PDF')
```

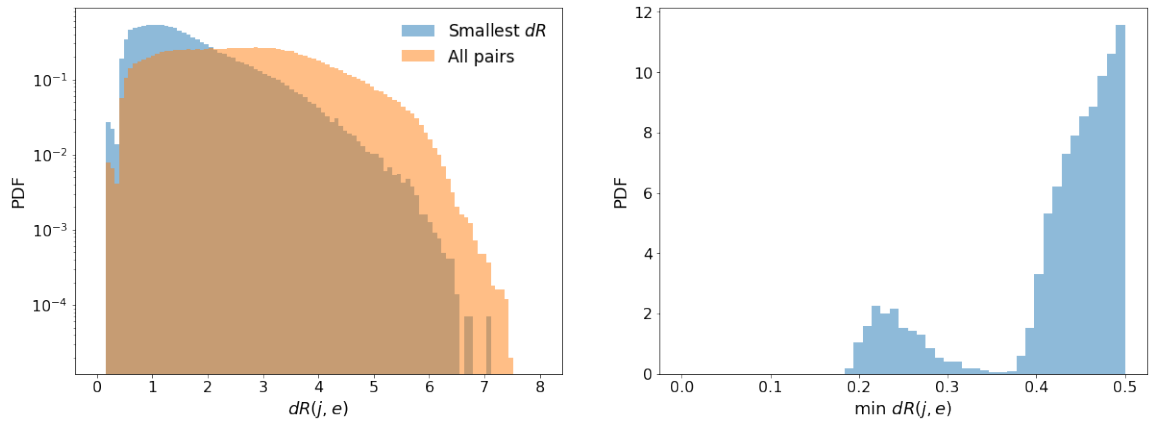

Figure 29: png

Getting now the index of the pair having the minimal dR using the command `np.argmin(dRej,axis=1)` which return a 1D array of shape (Nevt) containing the wanted index for each event. Then one can use the functions `get_indexed_value()` and `get_all_but_indexed_value()` to get either the btag weight of the minimal dR or all the others.

```
idRmin = np.argmin(dRej, axis=1)
jet_btag_w_dRmin = npu.get_indexed_value(jet_btag_w, idRmin)
jet_btag_w_other = npu.get_all_but_indexed_value(jet_btag_w, idRmin)
```

```
fig = plt.figure(figsize=(20, 7))
plt.subplot(121)
ax = plt.hist(jet_btag_w_dRmin, bins=np.linspace(-1, 1, 50),
              alpha=0.5, density=True, log=True, label='Closest jet')
ax = plt.hist(jet_btag_w_other.flatten(), bins=np.linspace(-1, 1, 50),
              alpha=0.5, density=True, log=True, label='Not the closest
 ↪  jets')
ax = plt.xlabel('$w_{b-tagging}$ of the jet')
ax = plt.ylabel('PDF')
ax = plt.legend()
```

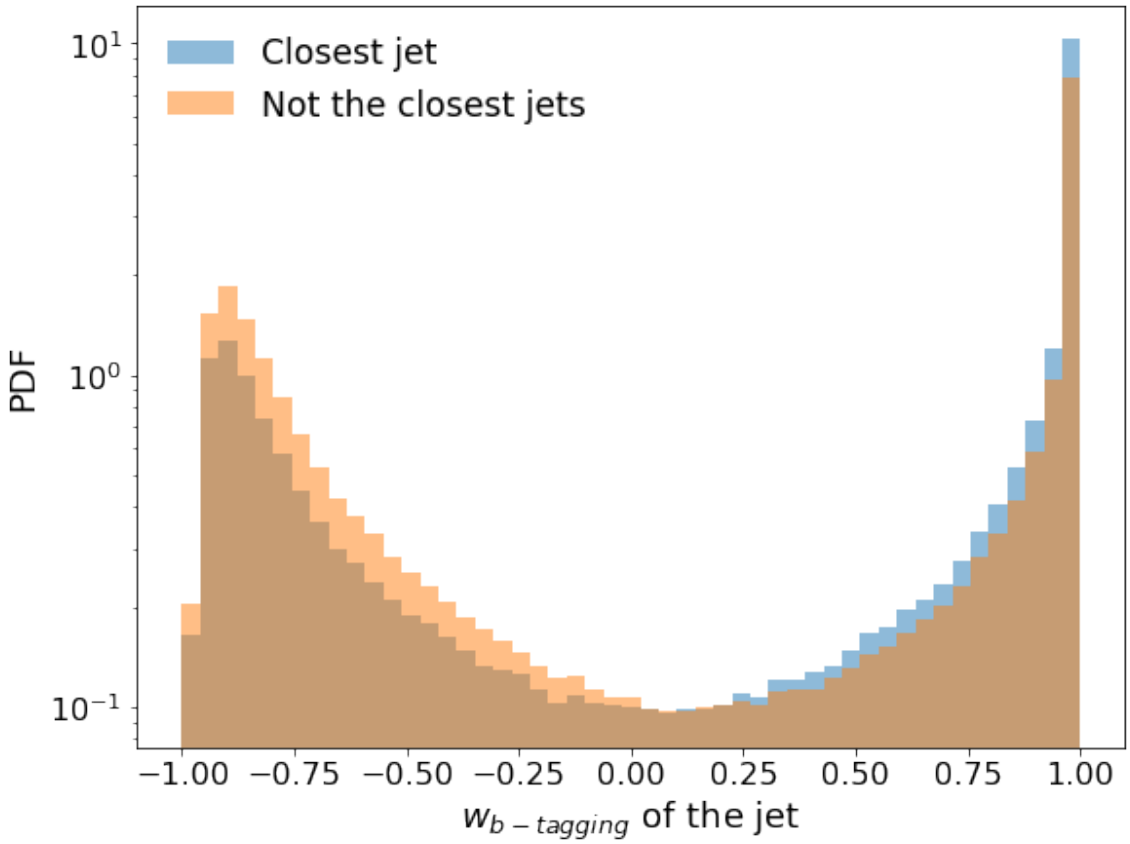

Figure 30: png

```
fig = plt.figure(figsize=(17, 10))
style = {
    'bins': np.linspace(-1, 1, 50),
    'alpha': 0.8,
    'density': True,
    'log': True,
```

```
    'histtype': 'step',
    'linewidth': 3.0
}
for i, cut in enumerate([0.35, 0.5, 1.0, 3.0]):
    plt.subplot(2, 2, i+1)
    dRgt_btag = jet_btag_w_dRmin*(dRmin>cut)
    dRgt_btag[dRgt_btag == 0] = 999
    dRlt_btag = jet_btag_w_dRmin*(dRmin<cut)
    dRlt_btag[dRlt_btag == 0] = 999
    ax = plt.hist(dRgt_btag, label='$dR_{min}>'+'{:.2f}$'.format(cut),
↪   **style)
    ax = plt.hist(dRlt_btag, label='$dR_{min}<'+'{:.2f}$'.format(cut),
↪   **style)
    ax = plt.xlabel('$w_{b-tagging}$ of the closest jet')
    ax = plt.ylabel('PDF')
    ax = plt.legend()
plt.tight_layout()
```

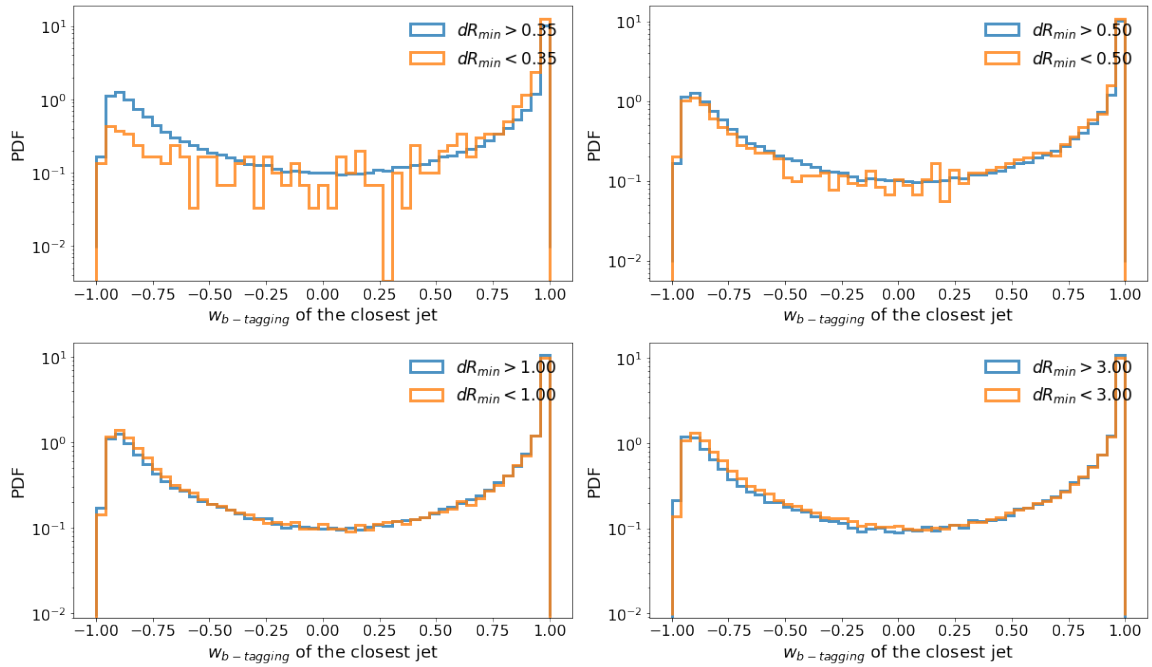

Figure 31: png

3.5.2.2 E.g. 2: p_T distribution for jets forming the highest $M(j,j)$

```
j1, j2 = jet_pairs[:, :, 0, :], jet_pairs[:, :, 1, :]
deta, dphi = j1[..., 1]-j2[..., 1], j1[..., 2]-j2[..., 2]
```

```
pt1, pt2 = j1[..., 0], j2[..., 0]
mjj = npu.replace_nan(
    np.sqrt(pt1*pt2 * (np.cosh(deta)-np.cos(dphi)))/1000., -1e10)
```

```
i_mjj_max = np.argmax(mjj, axis=1)
pt_mjj_max = np.concatenate([
    npu.get_indexed_value(pt1, i_mjj_max)/1000,
    npu.get_indexed_value(pt2, i_mjj_max)/1000]
)
```

```
fig = plt.figure(figsize=(10, 7))
style = {
    'bins': np.linspace(0, 2000, 100),
    'alpha': 0.8,
    'log': True,
}
ax = plt.hist(npu.replace_nan(pt_mjj_max, -999), **style)
ax = plt.xlabel('Jet $p_T$ [GeV] for the two jets having max $M(j,j)$')
ax = plt.ylabel('Unweighted events')
```

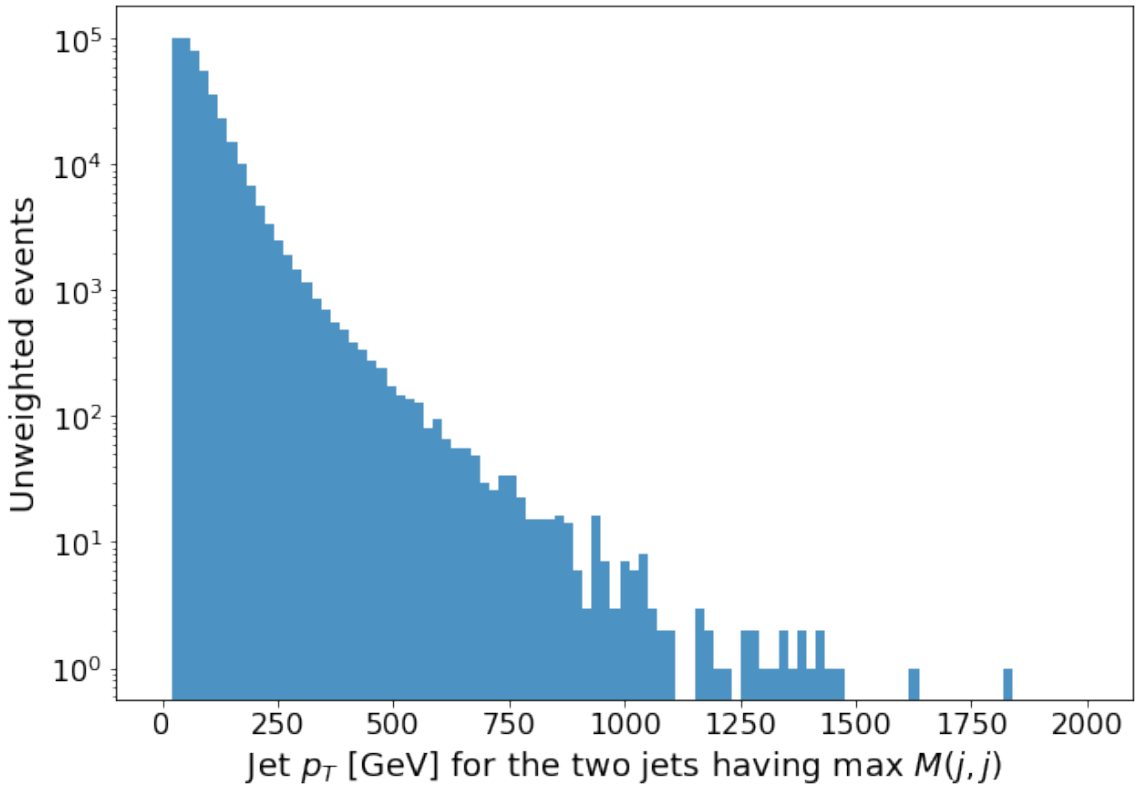

Figure 32: png

3.6 6 IO between panda/numpy and ROOT

3.6.1 6.1 Save some variables back into a ROOT file

This is possible that one wants to save and share the obtained variables in a ROOT file. This is possible to do using a *structured array*, numpy object accepting both field different shape for each "column". This goes through a data type (which in for instance the event model) and then each column can be filled. This is in principle a simplified pandas dataframe (simplified but interfaced with TTree via root_numpy). **Note that every** np.nan **will manifest in** tree->Draw() **as 0.0**

```
from root_numpy import array2root

# Define the event model with ('name','type','shape') for each column
event_model = np.dtype([
    ('n_jets', 'i4'),
    ('jet_pt', 'f8', (jets.shape[1],)),
    ('jet_eta', 'f8', (jets.shape[1],)),
    ('jet_phi', 'f8', (jets.shape[1],)),
    ('ht', 'f8'),
    ('ht_cent', 'f8'),
])

# Create the giant structured array
events = np.zeros(jets.shape[0], dtype=event_model)
events['n_jets'] = npu.count_nonnan(jets[..., 0], axis=1)
events['jet_pt'] = jets[..., 0]
events['jet_eta'] = jets[..., 1]
events['jet_phi'] = jets[..., 2]
events['ht'] = HTjets
events['ht_cent'] = HTjets_central

# Convert it into a TTree stored in a ROOT file
array2root(events, 'ttbar_jets.root', 'tree_jets', mode='recreate')
```

3.6.2 6.2 Read back the created file with root_numpy *WIP*

```
ar_new = root2array('ttbar_jets.root', 'tree_jets',
                    branches=['jet_pt']).view(np.recarray)
df_new = pd.DataFrame(ar_new, index=np.arange(len(ar_new)))
```

```
ExceptionTraceback (most recent call last)

<ipython-input-115-8eeaafb6cd3f> in <module>()
      1 ar_new = root2array('ttbar_jets.root', 'tree_jets',
      2                     branches=['jet_pt']).view(np.recarray)
--> 3 df_new = pd.DataFrame(ar_new, index=np.arange(len(ar_new)))


/home/rmadar/anaconda3/envs/root_env/lib/python2.7/site-packages/pandas/core/frame.pyc
in __init__(self, data, index, columns, dtype, copy)
    371                 if columns is None:
    372                     columns = data_columns
-> 373                 mgr = self._init_dict(data, index, columns,
dtype=dtype)
    374             elif getattr(data, 'name', None) is not None:
    375                 mgr = self._init_dict({data.name: data}, index,
columns,


/home/rmadar/anaconda3/envs/root_env/lib/python2.7/site-packages/pandas/core/frame.pyc
in _init_dict(self, data, index, columns, dtype)
    457             arrays = [data[k] for k in keys]
    458
-> 459         return _arrays_to_mgr(arrays, data_names, index, columns,
dtype=dtype)
    460
    461     def _init_ndarray(self, values, index, columns, dtype=None,
copy=False):


/home/rmadar/anaconda3/envs/root_env/lib/python2.7/site-packages/pandas/core/frame.pyc
in _arrays_to_mgr(arrays, arr_names, index, columns, dtype)
   7357
   7358     # don't force copy because getting jammed in an ndarray anyway
-> 7359     arrays = _homogenize(arrays, index, dtype)
   7360
   7361     # from BlockManager perspective


/home/rmadar/anaconda3/envs/root_env/lib/python2.7/site-packages/pandas/core/frame.pyc
in _homogenize(data, index, dtype)
   7667                 v = lib.fast_multiget(v, oindex.values,
default=np.nan)
   7668             v = _sanitize_array(v, index, dtype=dtype, copy=False,
-> 7669                                 raise_cast_failure=False)
```

```
   7670
   7671         homogenized.append(v)


/home/rmadar/anaconda3/envs/root_env/lib/python2.7/site-packages/pandas/core/series.pyc
in _sanitize_array(data, index, dtype, copy, raise_cast_failure)
   4163     elif subarr.ndim > 1:
   4164         if isinstance(data, np.ndarray):
-> 4165             raise Exception('Data must be 1-dimensional')
   4166         else:
   4167             subarr = com._asarray_tuplesafe(data, dtype=dtype)


Exception: Data must be 1-dimensional
```