

NOVEMBER

22

326-39

THURSDAY

DIP

23

327-38

FRIDAY

24

328-37

SATURDAY

Pubs in England open 24 hours as new licensing law takes effect 2005

Chapter:

- 3 → Lecture Slide : 4, 5, 6, 7
- 6 → Lecture : 15 (HSI model দ্রুত বাস করে আছে)
- 8 → Lecture : 13, 14
- 9 → Lecture : 11, 12 (thinning & thickening এর আগে পর্যন্ত)
- 10 → Lecture : 8

25

329-36

SUNDAY

Lionel Messi becomes the UEFA Champions League all-time top scorer 2014

A'2

* Chapter : 3 (Intensity Transformations)

④ Enhancement

Lecture : 4

④ Intensity transformation functions

- Linear

- Logarithmic

- Power law

④ Piecewise-Linear Transformation Function

- Contrast stretching

- Intensity-level slicing

- Bit-plane slicing

Image Enhancement:

* Process/manipulate an image so that the result is more suitable than the original image for a specific application.

Methods :

- ⇒ Spatial Domain

- ⇒ Frequency Domain

- ⇒ Combination Methods

We will only learn about this

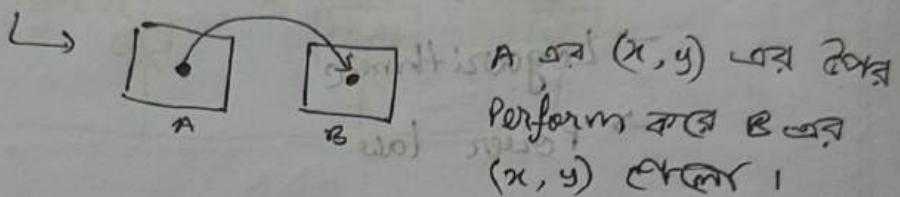
Spatial Domain Process:

Spatial Domain:

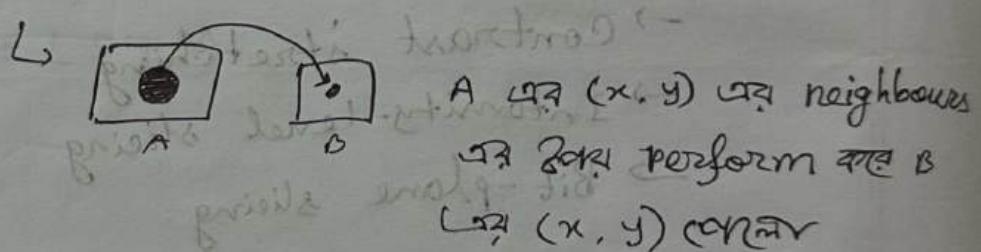
Direct manipulation
of pixels in an image

Types of img enhancement operations

① Point/Pixel operation



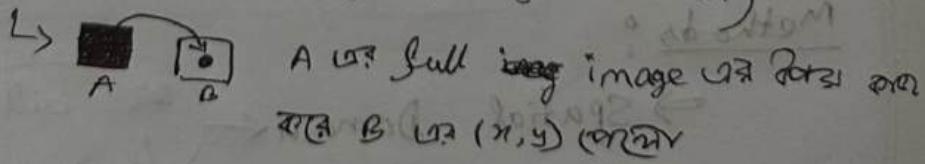
② Local operation



Spatial Filters: by mask, kernel, template or window

Intensity Transformation: Point operation

③ Global operation (Frequency Domain)



* input, output image of size same 2x2!

Intensity transformations functions:

- ① Basic
 - Linear
 - Logarithmic
 - Power-law

② Piecewise Linear

- Contrast stretching, thresholding
- Gray-level slicing
- Bit-plane slicing

$$g(x,y) = T[f(x,y)]$$

Gray-level/
intensity transformation/
mapping function

$$s = T(r)$$

r = Gray level of f at (x,y)

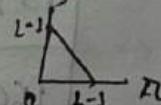
s = Gray level of g at (x,y)

T = A function that maps
 r to s .

* 8 bit img $\rightarrow k=8$ so, $L-1 = 2^8 - 1$
 $= 256 - 1$
 $= 255$

③ Linear Functions:

- Negative



$$\text{inverse of } r \quad s = (L-1) - r$$

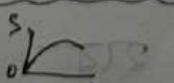
- Identity



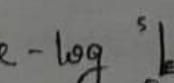
$$s = r \quad (\text{input, output same})$$

④ Logarithmic Functions:

- Log

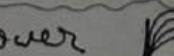


- Inverse-log



⑤ Power-Law Functions:

- nth power



- nth root



(Linear)

■ Negative Transformation:

8-bit image

$$L = 2^8$$

$$= 256$$

$$L-1 = 256 - 1$$

$$= 255$$

We know,

$$S = (L-1) - r$$

So, For first pixel $r = 100$

$$\therefore S = 255 - 100 \\ = 155$$

For second pixel $r = 110$

$$\therefore S = 255 - 110 \\ = 145$$

For third pixel $r = 90$

$$\therefore S = 255 - 90 \\ = 165$$

Now each pixel count S , then output image $g(x,y)$.

Input

100	110	90	95
98	110	105	135
89	90	88	85
102	105	99	115

$f(x,y)$

Output

155	195	165	160
157	115	110	120
166	165	167	170
153	150	156	140

$g(x,y)$

Thresholding:

* যেকোনো gray level image or binary image -এ

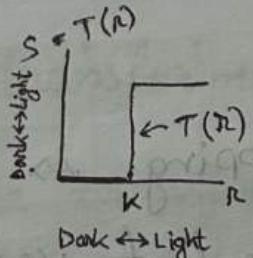
নিচে thresholding use করা হয়।

Threshold value এরে বড় value প্রস্তাবে, > এবং
ছোট value প্রস্তাবে ০ করে ফেলবে,

* contrast enhancement এর জন্য thresholding use

করা হয়।

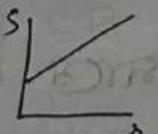
* Function:



$$S = T(R)$$

Intensity Scaling:

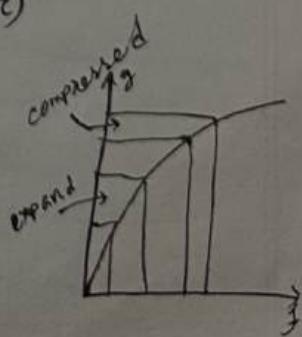
$$S = T(R) = \alpha \cdot R$$



Log Transformation:

$$S = C * \log(1+R)$$

* input image এর lower amplitudes গুরুত্বে gray level এxpand করে।



* input image এর higher amplitudes গুরুত্বে gray level compressed করে।

* Also called "dynamic-range compression/expansion".

Power-Law transformation:

Gamma Transformation

$$S = C * I^\gamma \quad \leftarrow C \text{ & } \gamma \text{ constant}$$

C = 1 এর জন্য
usually by default

$\gamma < 1 \Rightarrow$ the mapping is weighted toward brighter output values.

$\gamma = 1 \Rightarrow$ the mapping is linear.
(default)

$\gamma > 1 \Rightarrow$ the mapping is weighted toward darker output values.

* MRI \rightarrow Power-Law use করে রয়ে, γ এর value
থাইমে কর্মসূলি detailing করে MRI \rightarrow ,

$$(n+1)^\gamma * 2 = 2$$

: non-linear relationship



Piecewise Linear Transformation Functions:

→ Advantage: Some important transformations can be formulated only as a piecewise function.

→ Disadvantage: Their specification requires more user input than previous transformations.

* 3 types Piecewise transformation:

1. Contrast Stretching:

→ In contrast stretching we main the dynamic range to increase the.

$$* I_{\text{new}} = (I - \text{Min}) \frac{\text{NewMax} - \text{NewMin}}{\text{Max} - \text{Min}} + \text{NewMin}$$

↳ I = Input Intensity

NewMax = 255, NewMin = 0

Max = 150, min = 80

I_{new} = Output Intensity
after contrast
stretching

If, input image: 8bit have
range [80-150]

After contrast
stretching the new range
becomes : [0 - 255]

then

Exercise:

110	120	90	130
91	94	98	200
90	91	99	100
82	90	85	90

8-bit image

So the range is (0-255)

Given, $m = 95$ [threshold]

Output image:

255	255	0	255
0	0	255	255
0	0	255	255
0	255	0	0

95 മേൽ കൂട്ട്

value ദിനാംഗ എഡ്

മാത്രം, ഏഴ് 95

മേൽ വരുന്ന value

ദിനാംഗ എഡ്

മാത്രം, ഫണി 95

ബാക്കി ജീവിച്ചുപെട്ട

0 എഡ് മേഡ്.



2. Gray / Intensity Level Slicing:

↳ Highlights a specific range of Intensities levels in an image.

Example: যদি, $(100 \rightarrow 200)$ অন এই range দ্বাৰা

আচে, এখন, $(100 \rightarrow 200)$ অৱ মধ্যেৰ সব Pixel
শূলো 255 (white) কৈ ফুলে, বাকি সব pixel
আচে শূলো 0 (black) কৈ নিয়ে,

3. Bit - Plane Slicing:

↳ Three main goals are:

① Converting gray level image to a binary image.

② compression

③ Enhancing the image by focusing.

* Far Left side is MSB.

* Far Right side is LSB.

* The n th plane in the pixels are multiplied by the constant 2^{n-1}

Exercise:

8-bit image:

10100111	10000101	01101111
10010000	10001100	10000111
10011111	10011010	10010100

decimal - 2
binary
convert to binary

* bit-plane slicing করলে 8x8 matrix পাওয়া

যাবে, LSB এর position থেকে matrix create

শুধু করতে হবে,

bit-plane Slicing:

matrix-1

1	1	1
0	0	1
1	0	0

matrix-2

1	0	1
0	0	1
1	1	0

matrix-3

1	1	1
0	1	1
1	0	1

matrix-4

0	0	1
0	1	0
1	1	0

matrix-5

0	0	0
1	0	0
1	1	1

matrix-6

1	0	1
0	0	0
0	0	0

matrix-7

0	0	1
0	1	0
0	0	0

matrix-8

1	1	0
1	1	1
1	1	1

Reconstruct the image: (using 5th and 4th bit planes)

$(2^{n-1}) \leftarrow$ used here

$0 \times 2^{5-1} + 0 \times 2^{4-1}$ $= 0 \times 2^4 + 0 \times 2^3$ $= 0$	$0 \times 2^{5-1} + 0 \times 2^{4-1}$ $= 0$	$0 \times 2^{5-1} + 1 \times 2^{4-1}$ $= 0 + 1 \times 2^3$ $= 8$
$1 \times 2^{5-1} + 0 \times 2^{4-1}$ $= 1 \times 2^4 + 0$ $= 16$	$0 \times 2^{5-1} + 1 \times 2^{4-1}$ $= 0 + 1 \times 2^3$ $= 8$	$0 \times 2^{5-1} + 0 \times 2^{4-1}$ $= 0$
$1 \times 2^{5-1} + 1 \times 2^{4-1}$ $= 1 \times 2^4 + 1 \times 2^3$ $= 16 + 8$ $= 24$	$1 \times 2^{5-1} + 1 \times 2^{4-1}$ $= 1 \times 2^4 + 1 \times 2^3$ $= 16 + 8$ $= 24$	$1 \times 2^{5-1} + 0 \times 2^{4-1}$ $= 1 \times 2^4 + 0$ $= 16$

Final Result: (Enheched image) Also, it is a compressed image.

0	0	8
16	8	0
24	24	16

(contd)

Slide exercise

2	1	2	1	0
7	1	4	3	2
2	9	1	3	7
1	3	4	6	3
1	4	1	3	4

→ 3-bit image

→ 3-bit image এবং
highest value হচ্ছে
7. এবং lowest 0.

Digital Negative

7-2 = 5	7-1 = 6	5	6	7
7-7 = 0	6	3	4	5
5	3	6	9	0
6	4	3	1	4

Digital negative

বললে max

value হচ্ছে

OR ক্ষেত্রে

certain pixel

এর value ২৪

বিঘাতা করে

then ০.

position - ১

হয়ে ফিরে।

Bit-plane:

- * Firstly decimal value থেকে binary করে নিয়ে
একটি matrix তৈরী। যেখানে 3-bit image
এর binary value থেকে 3 bit এর হবে।
- * Then এই matrix থেকে bit-plane করলে new
3 bit matrix তৈরী। এজন্মেই এভাবে সেগুলো
bit-plane. Reconstruction করার প্রস্তাৱ
নেই এখন কোণ বলে বাই কৰতে।

Thresholding with $T = 3$:

- * Pixel এর value 3 বা 3 থেকে ছুটে হলে 0 (black) বজাবো।
- * Pixel এর value 3 থেকে বড় হলে 1 (white) বজাবো।

0	0	0	0	0
7	0	7	0	0
0	7	0	0	7
0	0	7	7	0
0	7	0	0	7

* 3-bit image তাই
max value 7 র হলো।
* এই 1-bit/binarized
image বলতে উল্লেখ
7 এর ছয়গাম 1 হলো।

Intensity slicing with both approaches,

when $a = 3$, $b = 5$; up the level to 5;

First approach:

- * range এর জন্যে না থাকলে 0 করে দিব,
- * range এর জন্যে থাকলে 5 করে দিব,

0	0	0	0	0
0	0	5	5	0
0	5	0	5	0
0	5	5	0	5
0	5	0	5	5

Second approach:

- * range এর জন্যে না থাকলে যা আছে তার বসতে,
- * range এর জন্যে থাকলে 5 করে দিব,

2	1	2	1	0
7	1	5	5	2
2	5	1	5	7
1	5	5	6	5
1	5	1	5	5

Histogram

Lecture : 5

Histogram: Histogram is a graphical representation showing a visual impression of the distribution of data.

Image Histogram: Image histogram is a type of histogram that acts as a graphical representation of the lightness/color distribution in a digital image. It plots the number of pixels for each value.

Example:

a 3-bit 4×4 image. So, $L = 2^n = 2^3 = 8 \rightarrow (0 - 7)$

~~original~~

An image

5	5	3	3
9	3	3	3
0	6	7	2
1	7	2	2

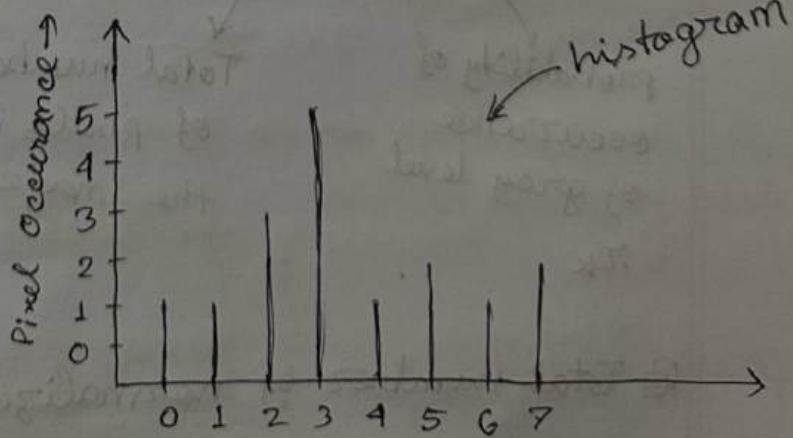
2^b-1

$$\sum_{n=0}^{2^b-1} h(n) = \text{area of the image}$$

total no. of pixels

Intensity Level

Position	0	1	2	3	4	5	6	7
h	1	1	3	5	1	2	1	2



histogram

↪ Gray level r_k in $[0, L-1]$: range of

then,

$$h(r_k) = n_k$$

Here,

r_k = k^{th} gray level

n_k = no. of pixels with having gray level r_k

↪ different image but no. of pixel same also
they are gray level images then their
histogram must same तरीके

Histogram Normalization:

$$P(r_k) = \frac{n_k}{n} \quad \begin{matrix} \xrightarrow{\text{certain gray}} \\ \text{value of Total} \\ \text{no. of pixel} \end{matrix} \quad \text{where } n = \sum_k n_k$$

probability of occurrence of gray level r_k

Total number of pixels in the image

↪ Total number of normalized histogram is 1 for an image.

④ No ~~color~~ indication of location of pixels.

⑤ Can we reconstruct image from histogram?

Ans: No.

Color img Histogram:

2 ways:

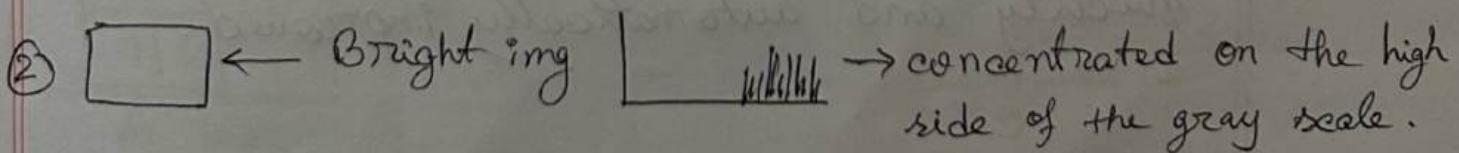
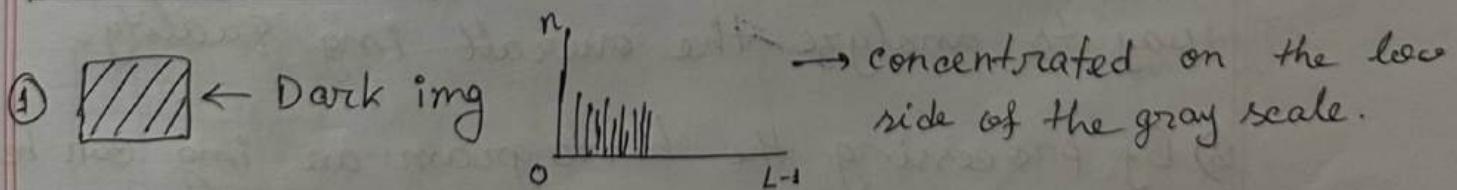
① Convert color img to gray scale. Then display histogram of gray scale.

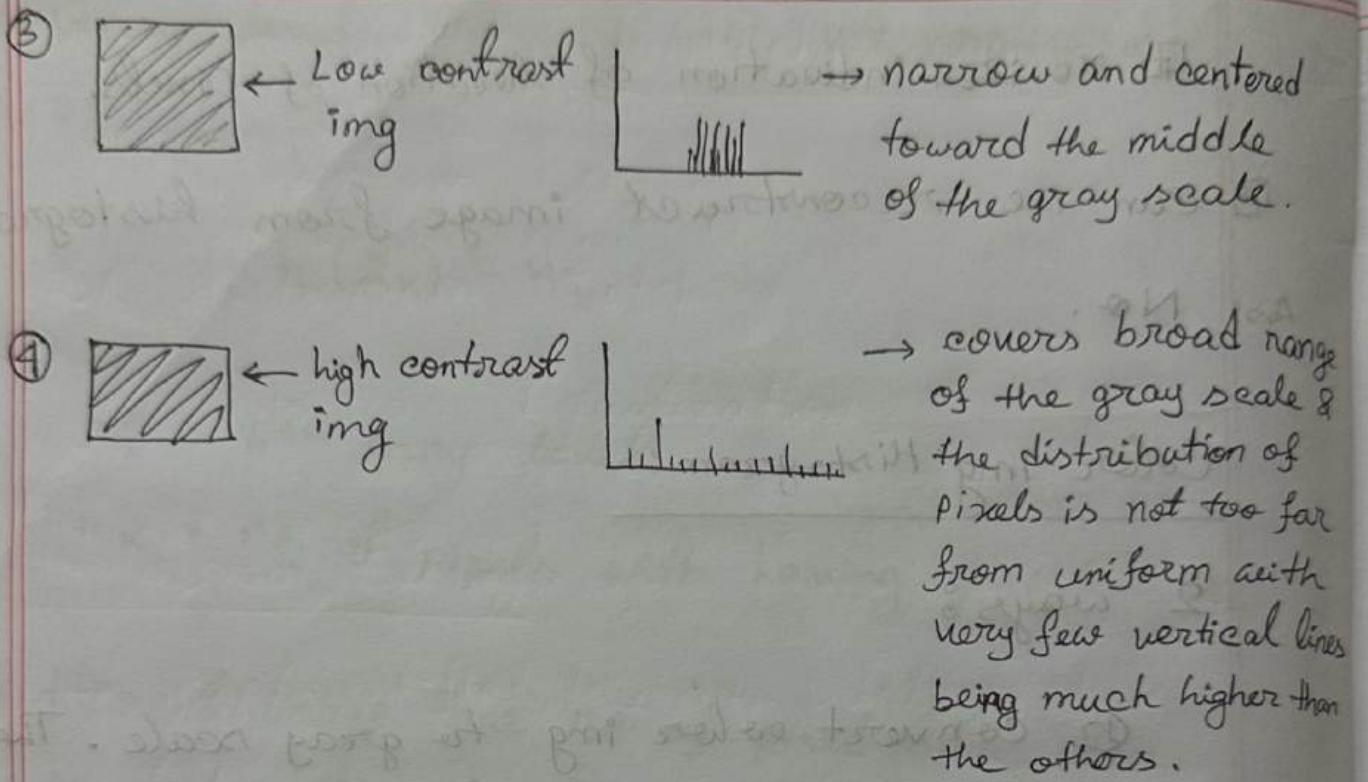
② 3 histograms (R, G, B).

1 for Red, 1 for Green, 1 for Blue.

Four basic type of imgs and their corresponding

histograms:





Q Why is the img histogram important?

Ans) Histogram (उस शैर्प फॉर्म की जानकारी प्रदान करता है।

- The overall quality of the img.

- The possibility for enhancement.

3) Visual inspection of the histogram is a fast way to analyze the overall img quality.

3) By processing the histogram an img can be quickly and automatically improved.

Uses of Histogram:

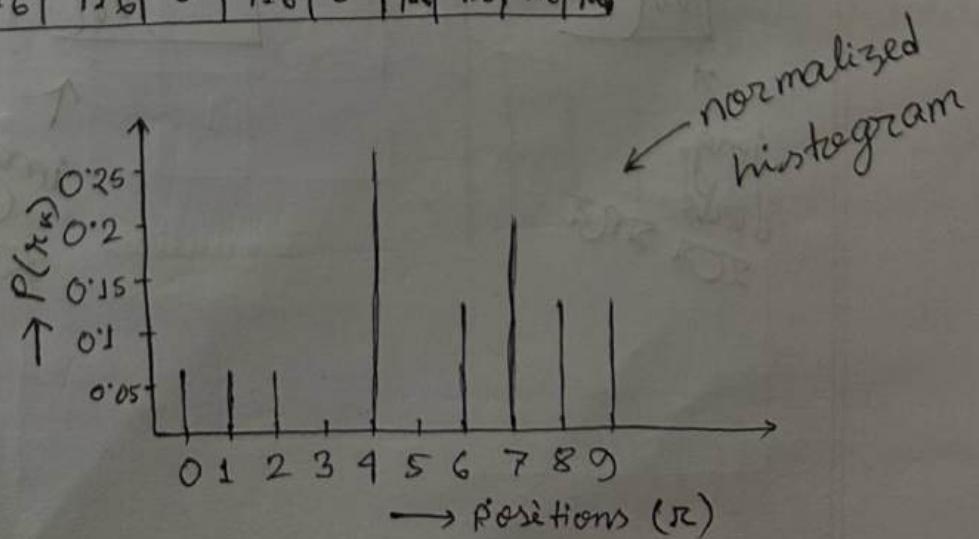
- 1) whether img was scanned properly or not.
- 2) idea about tonal distribution
- 3) to improve appearance, Histogram equalization can be applied.
- 4) tells us about the objects of the img.
- 5) to select threshold value for obj detection.
- 6) can be used for managed segmentation.

Normalized img Histogram:

position	0	1	2	3	4	5	6	7	8	9
$h(r_k)$	1	1	1	0	4	0	2	3	2	2
$p(r_k)$	$1/16$	$1/16$	$1/16$	0	$9/16$	0	$2/16$	$3/16$	$2/16$	$2/16$

9	8	9	8
2	7	4	7
6	4	6	1
4	0	7	4

An img

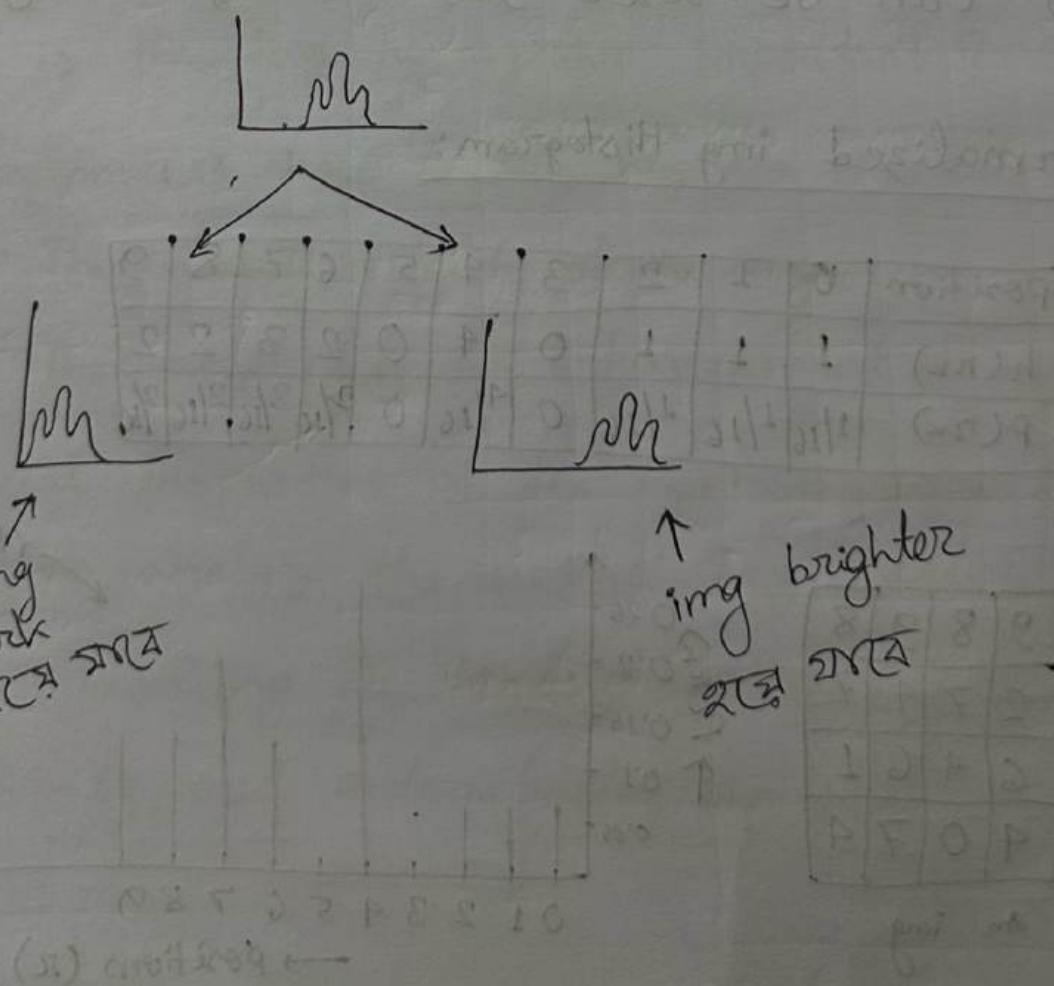


Histogram processing techniques:

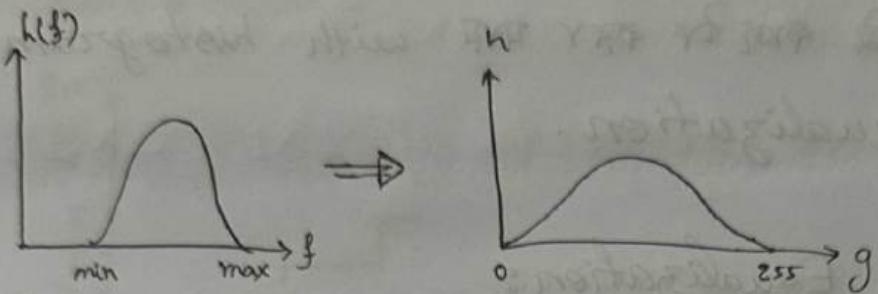
- ① Histogram Sliding
 - ② Histogram Stretching
 - ③ Histogram Equalization

Histogram Sliding:

→ simply shifted towards rightwards or leftwards.

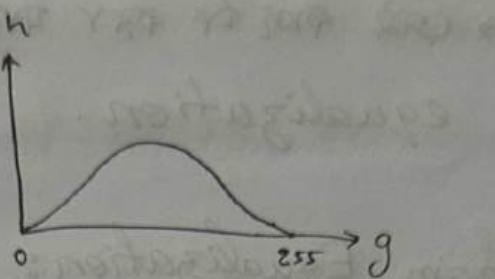


Histogram Stretching :



Rescale to

$[0, 255]$ range

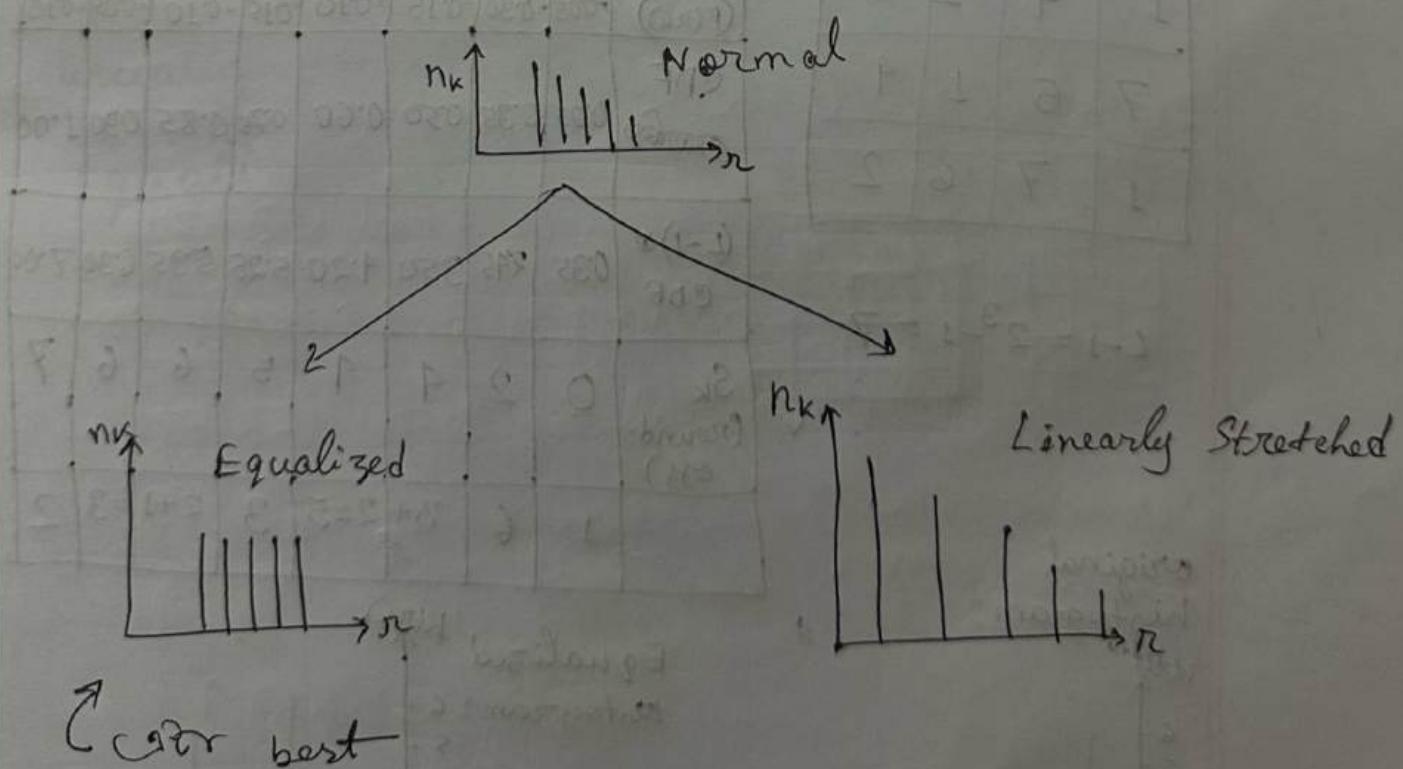


Slide histogram down to 0

$$g = \frac{255}{\max - \min} (f - \min)$$

Normalized histogram to
 $[0, 1]$ range.

Stretch. করলে enhance হচ্ছে স্বার্থ।



most of the time we need a flat histogram.

↪ इसे करने का पथ with histogram equalization.

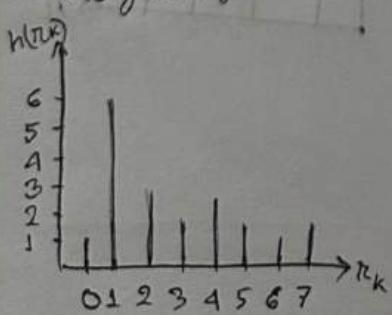
Histogram Equalization:

Target → contrast enhance प्रक्रिया

0	1	2	1
3	1	4	5
1	4	2	3
7	5	1	9
1	7	6	2

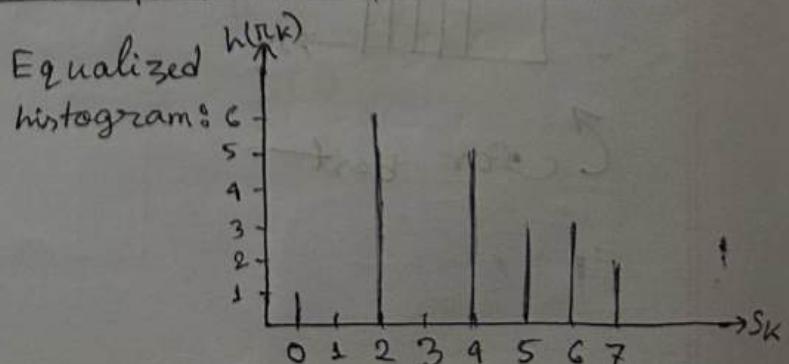
$$L-1 = 2^3 - 1 = 7$$

original histogram:

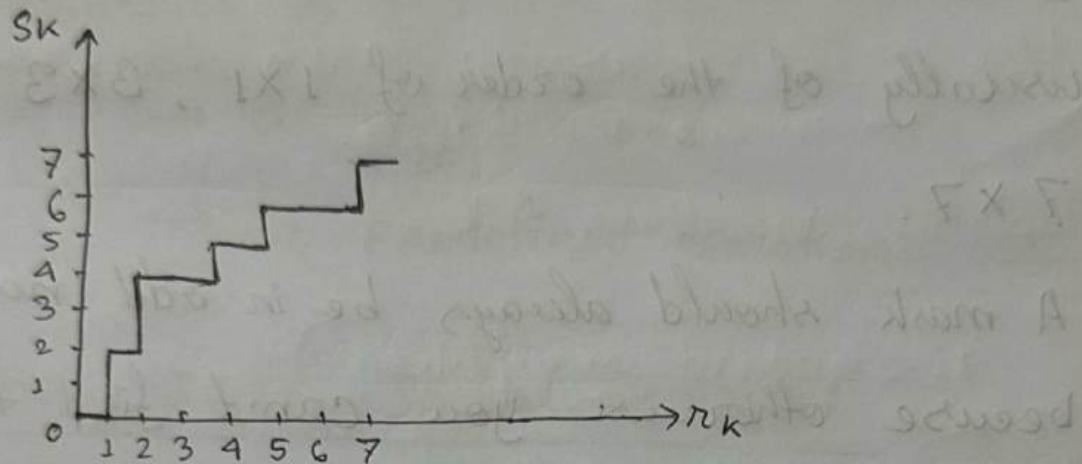


r_k	0	1	2	3	4	5	6	7	Total = 20
$h(r_k)$	1	6	3	2	3	2	1	2	
PDF ($P(r_k)$)	$\frac{1}{20}$	$\frac{6}{20}$	$\frac{3}{20}$	$\frac{2}{20}$	$\frac{3}{20}$	$\frac{2}{20}$	$\frac{1}{20}$	$\frac{2}{20}$	
CDF	0.05	0.35	0.50	0.60	0.75	0.85	0.90	1.00	
$(L-1) \times$ CDF	0.35	2.95	3.50	4.20	5.25	5.95	6.30	7.00	
s_k (round-off)	0	2	4	4	5	6	6	7	
	1	6	$3+2=5$	3	$2+1=3$	2			

Equalized histogram:



Transformation
function & curve :



Histogram Equalization Algorithm:

usually ଅର୍ଜ କର , ସହ ଅର୍ଜିତେ just
 equalization ଏବଂ process କେ ନିଷୟଲେଖ
 enough . Slide-ଏବେ ଉପରେ ନିଷୟ

Q What is kernel / mask ?

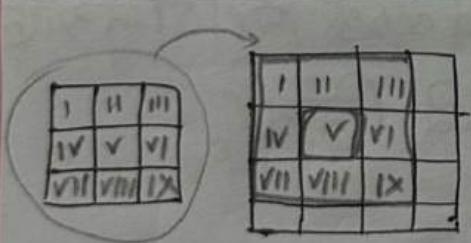
Lecture: 6

Ans: 2 - dimensional matrix. The mask is usually of the order of 1×1 , 3×3 , 5×5 , 7×7 .

A mask should always be in odd number because otherwise you can't find the mid of the mask.

Also known as filter / mask / window / box / kernel.

Convolution Process:



element wise dot
product .

একটি pixel এর মধ্যে input
img টির project করে
value শূলো এবং রয়ে , And
each pixel এর মধ্যে matrix
হয়ে এবং finally একটি output
img আঙুরো মাছে ,

Spatial Filtering:

consists of :

- a neighborhood
- a predefined operation

Filtering in the Spatial Domain:

2 types : ① Smoothing Spatial filter [Low Pass].

② Sharpening Spatial filter [High Pass]

Q Why filters are used ??

A → For blurring and noise reduction

→ For edge detection and sharpness.

→ For enhancing img

→ For extract info from img

→ For detecting patterns.

Smoothing Spatial Filters:

Use: → for blurring and → noise reduction.
 → remove fine details.

Types of smoothing filter:

- 1. Standard avg / Mean } linear
- 2. Weighted avg } Order Statistic
- 3. Median filter } (Non-linear)

① Standard Avg / Mean Filter: (Linear)

→ kernel ওর সবগুলি element এর value same
 এতে এবং একই value ধূলি করে Total
 । মাঝে রয়ে ।

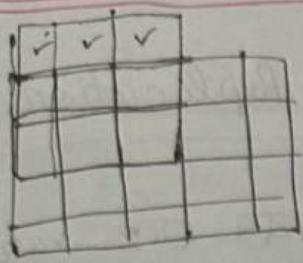
basic
mean
filter →

1	1	1
1	1	1
1	1	1

চেতে 3x3 img ওর
 অপর ~~৩~~ $\frac{1}{9}$ গুণ
 করে নিল kernel এর
 each pixel value - (3
 same করে plus
 মেজাজন্তে 1 হয় ।

1/9	1/9	1/9
1/9	1/9	1/9
1/9	1/9	1/9

মোটে 1/9
 common নিয়ে
 সমন্বয় রয়েছে



✓ - এই ক্ষেত্রে img এর value
নাই, সেক্ষেত্রে padding দিব
নিতে হবে।

Padding 3 types :

① Zero padding : (mostly used)

img প্রে চৰপথৰ দিকে ০ বজাব্বো,

এতে কুৱা img প্ৰে চৰপথৰ মাঝে
black border ভালবে,

0	0	0	0	0	0
0					0
0					0
0					0
0					0
0	0	0	0	0	0



② Border padding / Pixel Replication:

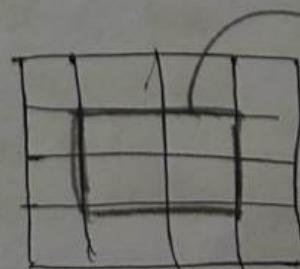
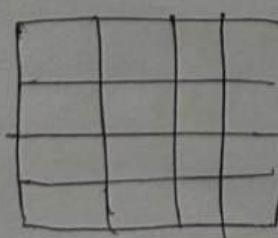
img এর border করব যেই value

গুলো এবং অঙ্গুল বসান্ত দিব।

2	2	5	1	0	0
2	2	5	1	0	0
6	6			2	2
4	4			1	1
3	3	7	8	9	9
3	3	7	8	9	9

③ Discard solution:

মনে রেখা pixel - টা ব্যালে kernel
বাইরে চলে যাবে তা পেরি এখন
calculate - টি করতে না, Discard
করে দিবো।



only calculate
এতে

Q) What does Mean or Box filter do?

- Ans:
- ① Replaces each pixel with an avg of its neighborhood
 - ② Achieve smoothing effect.
(remove sharp features).
 - ③ Adds a 'softer' look to an image.

② Weighted Avg Smoothing Filter: (Linear)

kernel ও স্যুন্দর pixel ও value same হবে
বি, But মোট করলে 1 অসত হবে,

1	2	1
2	4	2
1	2	1

যেকোনো 3×3 kernel
ৰে $\frac{1}{16}$ ফিল্টার
করাতে element
wise then স্যুন্দর
ফোর্ম ।

$1/16$	$2/16$	$1/16$
$2/16$	$4/16$	$2/16$
$1/16$	$2/16$	$1/16$

মুসলিম $1/16$
common ফিল্টার
নিবৃত্ত হয়।

Weighted filter হচ্ছে mainly Gaussian Filter.

③ Median Filter:

(Non-linear)

- কেন্দ্র অলম্বন kernel use করা হয় না,
- image এর তিতারেই kernel size এর position
ধৰণ বিশ্লেষণ করা হয়।

Example:

110	120	90	130
91	94	98	200
90	95	99	100
82	96	85	90



110	120	90	130
91	95	98	200
90	95	99	100
82	96	85	90

Sort করে দেখো যেকো বড় :

90, 90, 91, 94, 95, 95, 98, 99, 110, 120

Same way কো, যদি min filter বলে then sort করে
~~বেশি~~ minimum value দ্বা বজাবে।

যদি max filter বলে then sort করে
maximum value দ্বা বজাবে।

■ $\text{gray} - \text{black}$ dots পরালে image - \rightarrow then গুলকে
বলে Salt and Pepper' noise.

এখি 'Salt and Pepper' noise হুব করা ~~হয়ে~~
অন্য median filter use করা best.

Cross co-relation and template matching:

Slide এর মাণ্ডি সুন্দর
মতে দেয়া আছে।

Sharpening Spatial Filter:

Lecture: 7

- seek to highlight fine details
- Remove blurring
- Highlight edges
- useful for emphasizing transitions in image intensity.

Spatial Derivation:

1st Derivation

2nd Derivation

both has forward
and backward

details in slide

Types of Sharpening Spatial Filters:

① Laplacian filter

↳ uses 2nd derivative of Image

Enhancement

~~Process~~

② Sobel (Gradient Operators)

↳ uses 1st derivative of Image

Enhancement.

① Laplacian Filter:

4 types :

0	1	0
1	-4	1
0	1	0

Forward 4-neighbor

0	-1	0
-1	4	-1
0	-1	0

Backward 4-neighbor

1	1	1
1	-8	1
1	1	1

Forward 8-neighbor

-1	-1	-1
-1	8	-1
-1	-1	-1

Backward 8-neighbor

original img + Laplacian filter = Enhanced
applied img with Image
Laplace filter

Sharpening filter এর টাই - এই অপারেটর
enhanced img এর

But Smoothing এর টাই - এই just
filter apply করলেই enhanced image
পেতে পারিলাম।

Sobel operator:

-1	0	+1
-2	0	+2
-1	0	+1

G_x

+1	+2	+1
0	0	0
-1	-2	-1

G_y

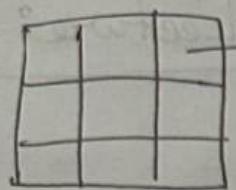
Prewitt operator: (Sobel ওর স্টেপের উন্নয়ন)

-1	0	+1
-1	0	+1
-1	0	+1

G_x

+1	+1	+1
0	0	0
-1	-1	-1

G_y



এই একটি pixel-এর মতো Sobel কে
জের, একবার $G_{x,x}$ এর করাতে,
একবার $G_{y,y}$ এর করাতে, Then,

$$M = |G_{x,x}| + |G_{y,y}|$$

$= \boxed{\quad}$ → এই value-র আবেদনে
প্রাণীটি যেখানে একটি certain pixel-এ বসতে,

সেখানে সুস্থিতি হবে এবং এখানে
সেখানে সুস্থিতি হবে এবং

সেখানে সুস্থিতি হবে

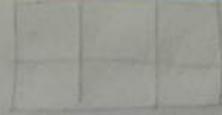
সুস্থিতির মুল ভাব

Chapter: 6 (Color Image Processing)

Human eye range:

Lecture: 15

400 nm to 700 nm



Color Model:

$$|x_1| + |x_2| = m$$

→ human eye combines 3 primary colors by using the 3 different types of cones to discern all possible colors.

→ colors are just different light frequencies:

red → 700 nm wavelength

green → 546.1 nm wavelength

blue → 435.8 nm wavelength

→ Higher frequencies are cooler colors.

↳ 700 nm ~~at~~ red.

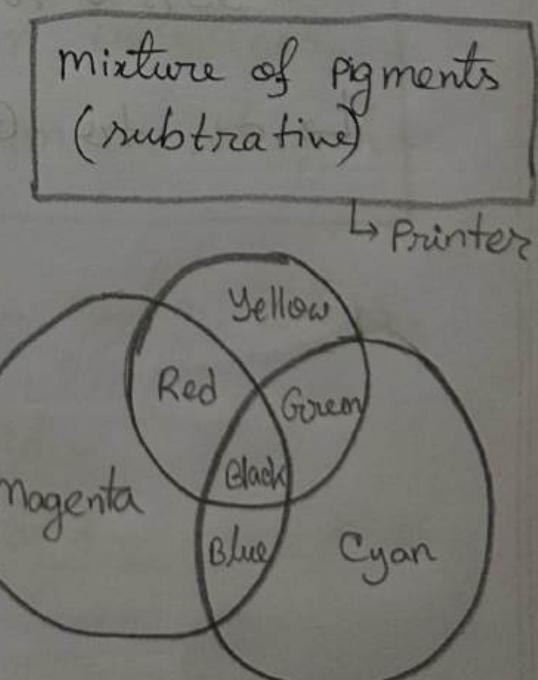
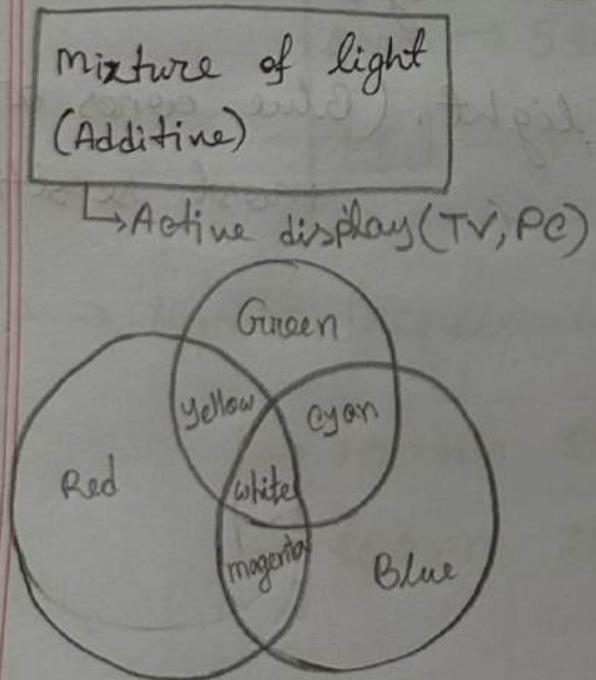
↳ 400 nm ~~at~~ violet.

Human Color Vision:

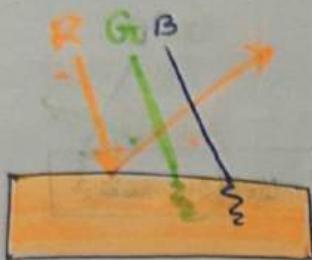
- Retina contain 2 types of Photo receptors
 - ↳ Cones (color sensitive)
 - ↳ Rods (more numerous, insensitive to color)
- 6 to 7 million cones in each eye are responsible for colour vision.
 - ↳ 65% of these are sensitive to Red light.
 - ↳ 33% to Green light
 - ↳ 2% to Blue light. (Blue cones are the most sensitive.)

Primary Colors:

- ⇒ Primary colors of light are additive
- ↳ Primary Colors: Red, Green, Blue
 - ↳ combining red + green + blue yields white.
- ⇒ Primary colors of pigment are subtractive
- ↳ Primary Colors: Cyan, Magenta, Yellow
 - ↳ Combining cyan + magenta + yellow yields black.

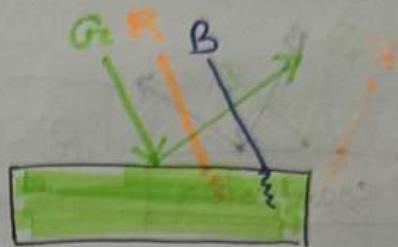


Red pigment :

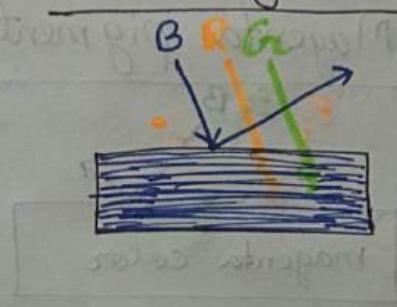


Red
color
বর্মাৰ রঁজ
প্ৰক্ৰিয়া

Green pigment :



Blue pigment :



Red-Green pigment :



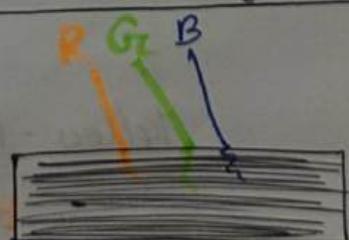
Black
(no light reflected)

Red-Blue pigment :



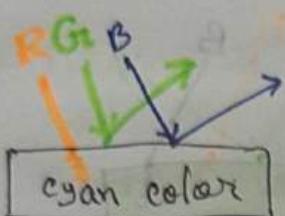
Black
(no light reflected)

Green-Blue pigment :

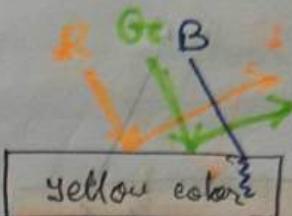


Black
(no light reflected)

Cyan pigment :



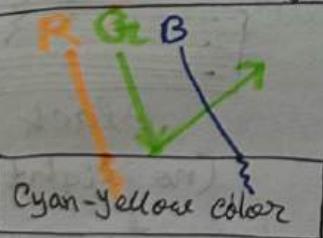
Yellow pigment :



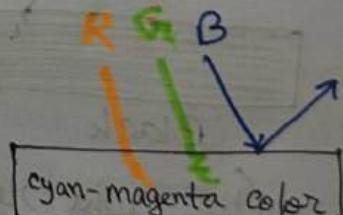
Magenta pigment :



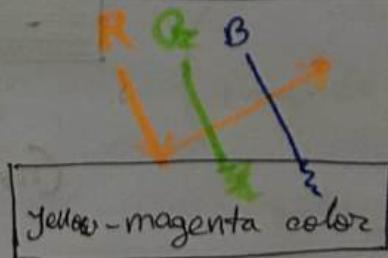
Cyan-Yellow pigment :



Cyan-Magenta pigment :



Yellow - Magenta pigment :



Primary and Secondary colors:

Additive Primaries
of Light

$$\text{Red} + \text{Green} + \text{Blue} = \text{White}$$

$$\text{Red} + \text{Green} = \text{Yellow}$$

$$\text{Red} + \text{Blue} = \text{Magenta}$$

$$\text{Green} + \text{Blue} = \text{Cyan}$$

Subtractive Primaries
of Pigments

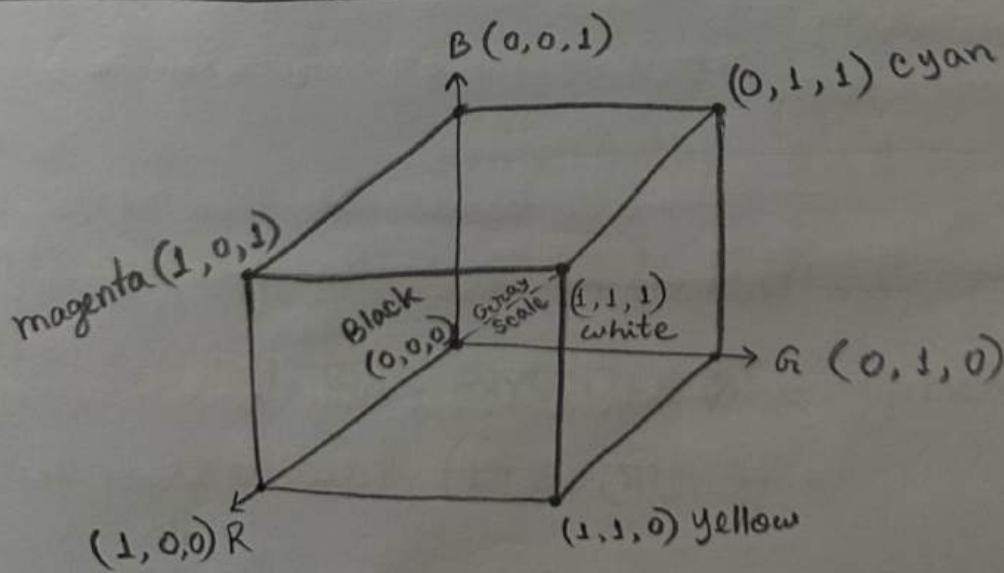
$$\text{Cyan} + \text{Magenta} + \text{Yellow} = \text{Black}$$

$$\text{Cyan} = \text{White} - \text{Red}$$

$$\text{Magenta} = \text{White} - \text{Green}$$

$$\text{Yellow} = \text{White} - \text{Blue}$$

RGB color model:



RGB 24-bit color cube

- pixel depth = 24 bits (8 bit per plane)
- Total no. of colors = $(2^8)^3$ = 16,777,216

Light Intensity :

$$\text{intensity} = 0.299 * \text{Red} + 0.587 * \text{Green} + 0.111 * \text{Blue}$$

Green portion (for human eye)

$$\text{Red} - \text{Blue} = \text{Red}$$

$$\text{Red} = \text{Red} + \text{Blue}$$

$$\text{Green} - \text{Blue} = \text{Green}$$

$$\text{Green} = \text{Red} + \text{Blue}$$

$$\text{Blue} - \text{Red} = \text{Blue}$$

$$\text{Blue} = \text{Red} + \text{Green}$$

: Debbaran Saha 02/2021

(1,0,0)

Chapter : 10 (Image Segmentation)

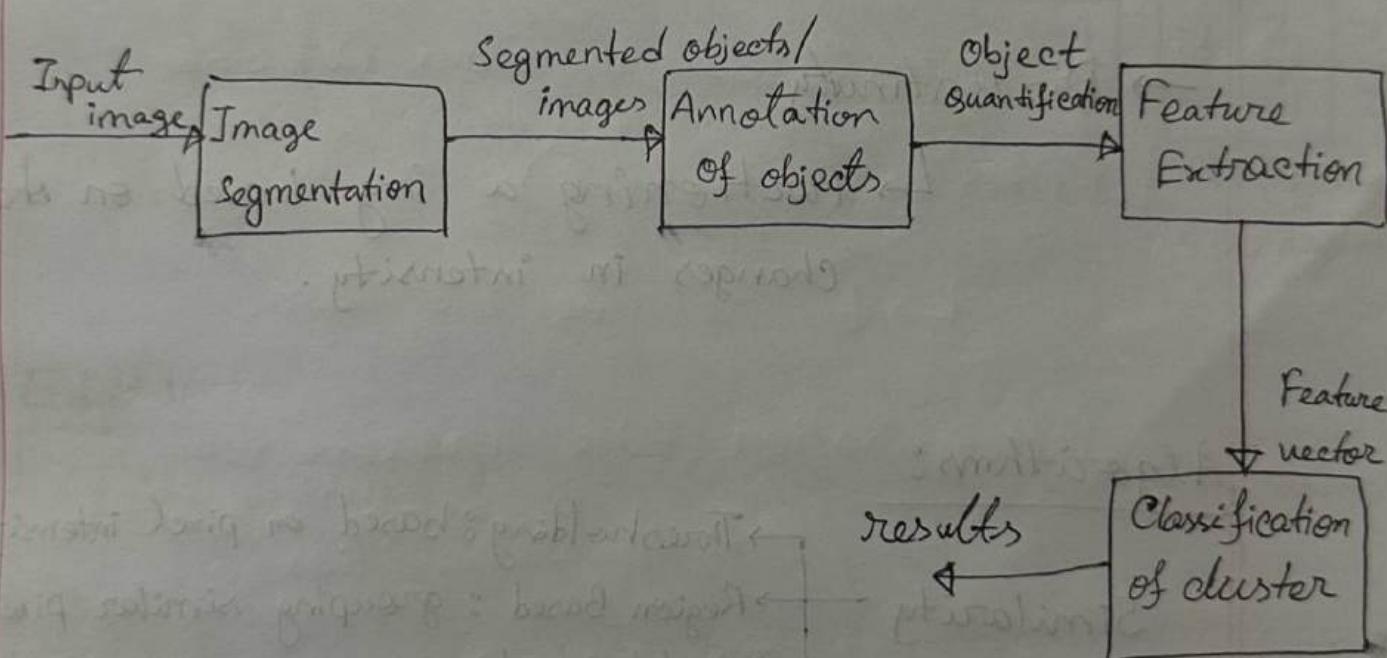
Q What is image segmentation?

Lecture : 8

Ans: → an aspect of img processing

→ a computer vision process

→ the first step in image analysis



Q What does img segmentation do?

⇒ কেবল img কে different different way করে analysis

ক্ষেত্র গঠনের জন্য বিস্তারকে segmentation

process এবং প্রক্রিয়া মতে হবে,

Principal approaches of segmentation:

→ Similarity

↳ Partitioning an img into regions that are similar according to a set of predefiner criteria .

→ Discontinuity

↳ Partitioning a img based on sharp changes in intensity .

Algorithms:

Similarity →

- Thresholding : based on pixel intensities
- Region Based : grouping similar pixels
- Match Based : comparison to a given template

Discontinuity →

- Edge based : detection of edges that separate regions from each other .
- Watershed : find regions corresponding to local minima in intensity

Point detection:

$$R = \sum w_k z_k \xrightarrow{\text{kernel/filter}}$$

↓
img

Line detection:

-1	-1	-1
2	2	2
-1	-1	-1

Horizontal

-1	-1	2
-1	2	-1
2	-1	-1

+45° (positive diagonal)

-1	2	-1
-1	2	-1
-1	2	-1

Vertical

2	-1	-1
-1	2	-1
-1	-1	2

-45° (negative diagonal)

Edge:

↪ the boundary between two homogeneous regions

types:

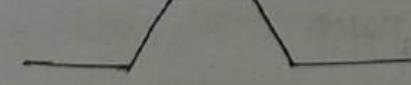
- Step edge :



- Ramp edge :



- Ridge :



- Roof :



Edge detection:

→ Identifying sudden change in image intensity

usage:

- extract imp features of an img (corners, lines, curves).

④ Three main steps in Edge Detection:

1. Filtering (Smoothing)

↳ to remove the noise.

2. Differentiation (Edge sharpening using derivatives)

↳ detects discontinuities

3. Detection (Thresholding)

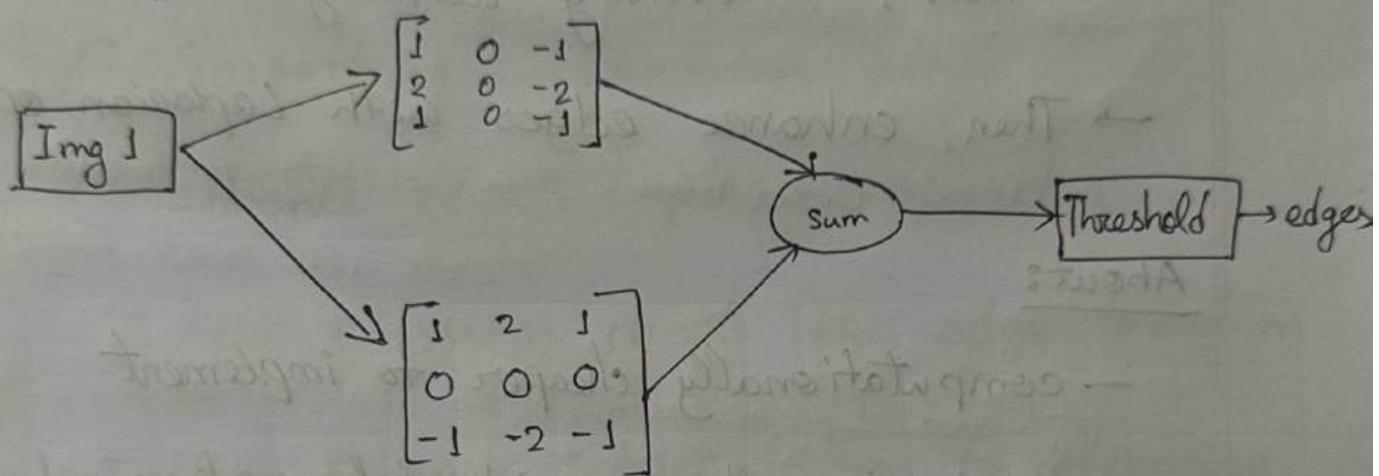
↳ take decision on the edge pixel
where the changes are significant.

Extra 4. Localization

↳ determine the exact location of an edge.

Gradient based edge Detection:

By sobel,



- simple to implement
- capable of detecting edges and their direction
- sensitive to noise
- not accurate in locating edges.

Problems:

- too much details
 - one way to overcome this is to smooth images prior to edge detection.
 - LOG

LOG (Laplacian of Gaussian):

- First, smoothing with gaussian filter
- Then, enhance edges with Laplacian operator

About:

- computationally cheaper to implement
 - But doesn't provide information about the direction of the edge.
 - Also probability of false and missing edges remain
- Localization is better than Gradient operators.

LOC for Marr Hildreth Algorithm:

Steps:

{ - Smoothing : Gaussian filter

- Enhance edges : Laplacian operator

- Zero crossings denote the edge location

- Use linear interpolation to determine
the sub-pixel location of the edge.

$$\rightarrow g(x, y) = \nabla^2 [G(x, y) * f(x, y)]$$

The Canny Edge Detector:

~~Three~~ 3 main criteria :

- Good Detection : the ability to locate and mark all real edges.

- Good Localization : minimal distance between the detected edge and

edges with similar gradients.

- Clear Response : only one response per edge.

Algo runs in 5 steps:

1. Smoothing

2. Finding gradients

3. Non - maximum suppression

4. Double thresholding

5. Edge tracking by Hysteresis

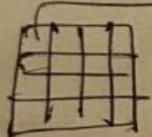
এবং কিছি strong edge
গুলোকে ঘূর্ণ নিয়ে
যাবো

Step 1: (smoothing / noise reduction).

$$f_s(x, y) = G_r(x, y) * f(x, y)$$

↓
filtered img ↓
gaussian filter → original img

Step 2: (finding gradient operator).


$$\rightarrow G_{rx} \& G_{ry} \text{ calculate} \rightarrow \sqrt{G_{rx}^2 + G_{ry}^2} = M(x, y)$$

Step 3: (non-maximum suppression)

2↑	3↑	5↑	9↑	6↑
9↑	5↑	7↑	6↑	7↑
5↑	6↑	9↑	3↑	2↑
3↑	4↑	3↑	1↑	1↑

Step 4 : (Hysteresis Thresholding)

$$G_{NH}(x, y) = G_N(x, y) \geq T_H$$

$$G_{NL}(x, y) = G_N(x, y) \geq T_L$$

and

$$G_N(x, y) = G_{NL}(x, y) - G_{NH}(x, y)$$

Step 5 : (connectivity Analysis)

200	0	0
0	0	101
0	0	0

$g_{NH}(x, y)$

0	0	57
0	45	0
50	0	0

$g_{NL}(x, y)$

200	0	57
0	45	101
0	0	0

$g(x, y)$

(threshold segment based approach) e - work

④ In Hysteresis thresholding, we set two thresholds 'High' and 'Low'.

— If the threshold is set too Low, there will still be some false edge which is called False Positive.

— If the threshold is set too high, then actual valid edge points will be eliminated which is called False Negative.

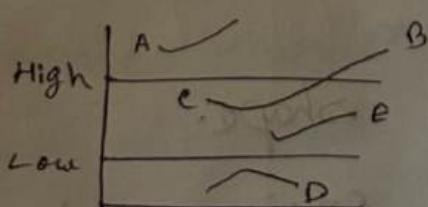
\Rightarrow High \rightarrow sure edge

\Rightarrow Low \rightarrow non-edges

\Rightarrow between 'High' and 'Low' \rightarrow High \rightarrow sure edge

if \rightarrow connected \rightarrow then counted \rightarrow otherwise

discard \rightarrow if \rightarrow 1 sure edge \rightarrow neighbor



Chapter - 9 (Morphological Image Processing)

- pixel shape based analysis

Lecture - 11

- basic morphology operations :

1. Dialation → grow img regions

2. Erosion → shrink img regions

3. Opening → structured removal of img
region boundary pixels.

4. Closing → structured filling in of img
region boundary pixels.

Binary Image :

representation 0, 1

→ foreground, object = 1 (white)

→ background = 0 (black)

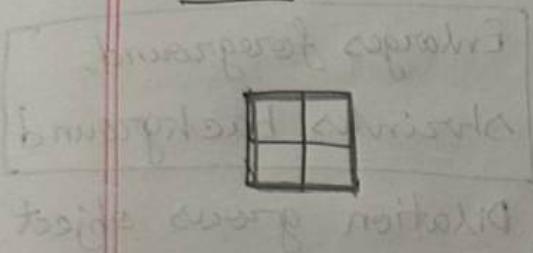
Structuring Element:

- can be any shape.

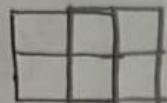
- has an origin. Origin can be in any position.

~~Operations~~

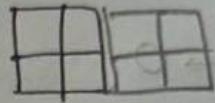
Fit: $A \oplus A$



Hit:



Miss:



Erosion:

Fit $\rightarrow 1$

Hit $\rightarrow 0$

Miss $\rightarrow 0$

$$A \ominus B = \{ z \mid (B)_z \subseteq A \}$$

Shrinks Foreground,
enlarges Background

Erosion shrinks objects

Effect:

- Shrinks the size of foreground (1-valued) objects
- smoothes object boundaries
- Removes small objects

Dilation:

Fit \rightarrow 1

Hit \rightarrow 1

Miss \rightarrow 0

$$A \oplus B = \{z \mid (\hat{B})_z \cap A \neq \emptyset\}$$

Enlarges foreground,
shrink's background

Dilation grows object

Effects:

- Fills in holes
- Smoothens object boundaries
- Adds an extra outer ring of pixels onto object boundary then object ~~boundary~~ becomes slightly larger.
- Expands the size of foreground (1-valued) objects.

For Erosion,

$$A - \{A \ominus B\} = \text{Border} \quad (\text{object } \nwarrow \text{ inner line})$$

foreground pixel \nwarrow

For Dilation,

$$\{A \oplus B\} - A = \text{Border} \quad (\text{object } \nwarrow \text{ outer line})$$

background pixel \nwarrow

Dilation and erosion are duals of each other :

$$(A \ominus B)^c = A^c \oplus \hat{B}$$

Same way $\ominus (A \oplus B) = A \ominus B$

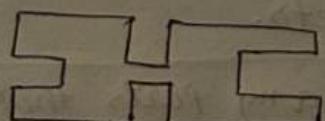
$$(A \oplus B)^c = A^c \ominus \hat{B}$$

Opening :

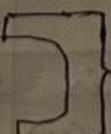
→ img এর প্রথম firstly erosion perform করবে।

→ Then এই result এর পুরোপুরি dilation
perform করবে।

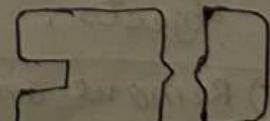
$$A \ominus B = \{A \ominus B\} \oplus B$$



A
binary



$A \ominus B$

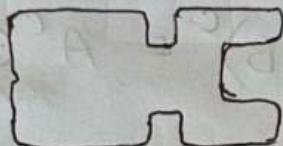
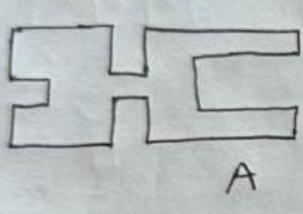


$\{A \ominus B\} \oplus B$

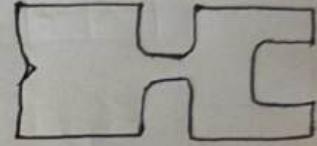
Closing :

- img पर फॉर्म के बाहरी कंपोनेंट्स को हटाने के लिए, firstly dilation perform करता है।
- Then इसके result पर फॉर्म के अंदरी कंपोनेंट्स को हटाने के लिए erosion perform करता है।

$$A \bullet B = (A \oplus B) \ominus B$$



$A \oplus B$



$(A \oplus B) \ominus B$

Opening	Closing
1) Removes small objects/noise from the foreground of an img.	1) Fill small holes and gaps in the foreground of an img.
2) Erosion followed by dilation.	2) Dilation followed by erosion.
3) Make objects smaller	3) Make objects larger
4) Useful for separating objects.	4) Useful for connecting objects.
5) Remove any parts that is smaller than the shape (SE) used.	5) Fill any parts that is touched by the shape (SE) used.
6) Denoted as: $A \circ B = (A \ominus B) \oplus B$	6) Denoted as: $A \bullet B = (A \oplus B) \ominus B$

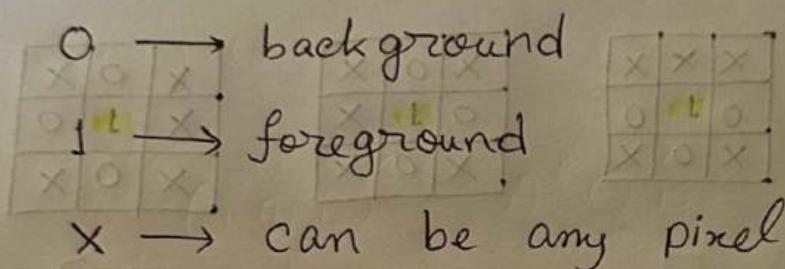
Hit and Miss Transformation:

Lecture: 12

Hit and Miss Structure element contains :

0 , 1 and X (Don't care).

Here,



WATCH OUT: We actually look for "fits" but we will be calling them "hits" when talking about Hit and Miss Transformation.

Structuring Elements representing 4 corners:

X	1	X
0	1	1
0	0	X

X	0	0
1	1	0
X	1	X

0	0	X
0	1	1
X	1	X

X	1	X
1	1	0
X	0	0

21)

Equation:

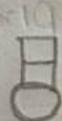
$$A \circledast B = (A \ominus B_1) - (A \oplus \hat{B}_2)$$

Structuring Elements representing end points:

x	o	x
o	1	o
x	x	x



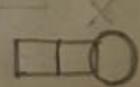
x	x	x
o	1	o
x	o	x



x	o	x
o	1	x
x	o	x



x	o	x
x	1	o
x	o	x



x	1	x
o	1	o
x	1	x

x	o	o
1	o	o
x	1	x

o	o	x
o	1	o
x	1	x

x	1	x
1	o	o
x	1	x