

```
In [1]: from __future__ import print_function
        %matplotlib inline
        # import ganymede
        # ganymede.configure('uav.beaver.works')
        import matplotlib.pyplot as plt
        import numpy as np
        import sympy as sym
        from IPython.display import YouTubeVideo, HTML
        sym.init_printing(use_latex = "mathjax")
```

Enter your name below and run the cell:

Individual cells can be run with Ctrl + Enter

```
In [2]: # # ganymede.name('YOUR NAME HERE')
        # def check(p):
        #     ganymede.update(p, True)
        # check(0)
```

```
In [3]: YouTubeVideo('9vKqVkmQHk', width=560, height=315) # Video by http://www..
```

Out[3]:

The paradox of the derivative | Chapter 2, Essence of calcul...



```
In [4]: YouTubeVideo('bRZmfc1YFsQ', width=560, height=315) #Note: All Khan Academ
```

Out[4]:

Power rule | Derivative rules | AP Calculus AB | Khan Acade...



Power Rule

The derivative of x^n is nx^{n-1}

[Read more](#)

[Other derivative rules](#)

```
In [5]: # Creating algebraic symbols
x = sym.symbols('x')
x
```

Out[5]: x

```
In [6]: x = sym.symbols('x')
expr = x ** 2
expr
```

Out[6]: x^2

```
In [7]: sym.Derivative(expr) # does not actually compute the derivative
```

Out[7]: $\frac{d}{dx}x^2$

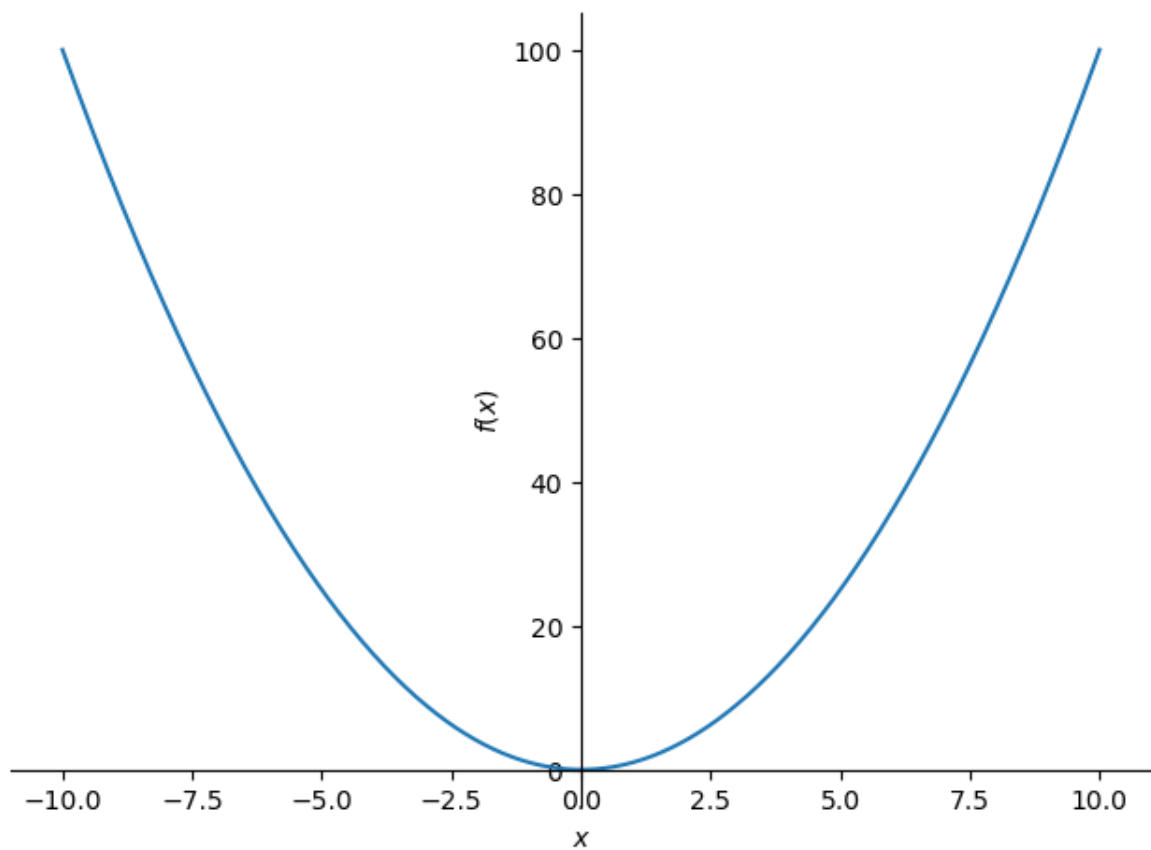
```
In [8]: sym.Derivative(expr).doit()
```

Out[8]: $2x$

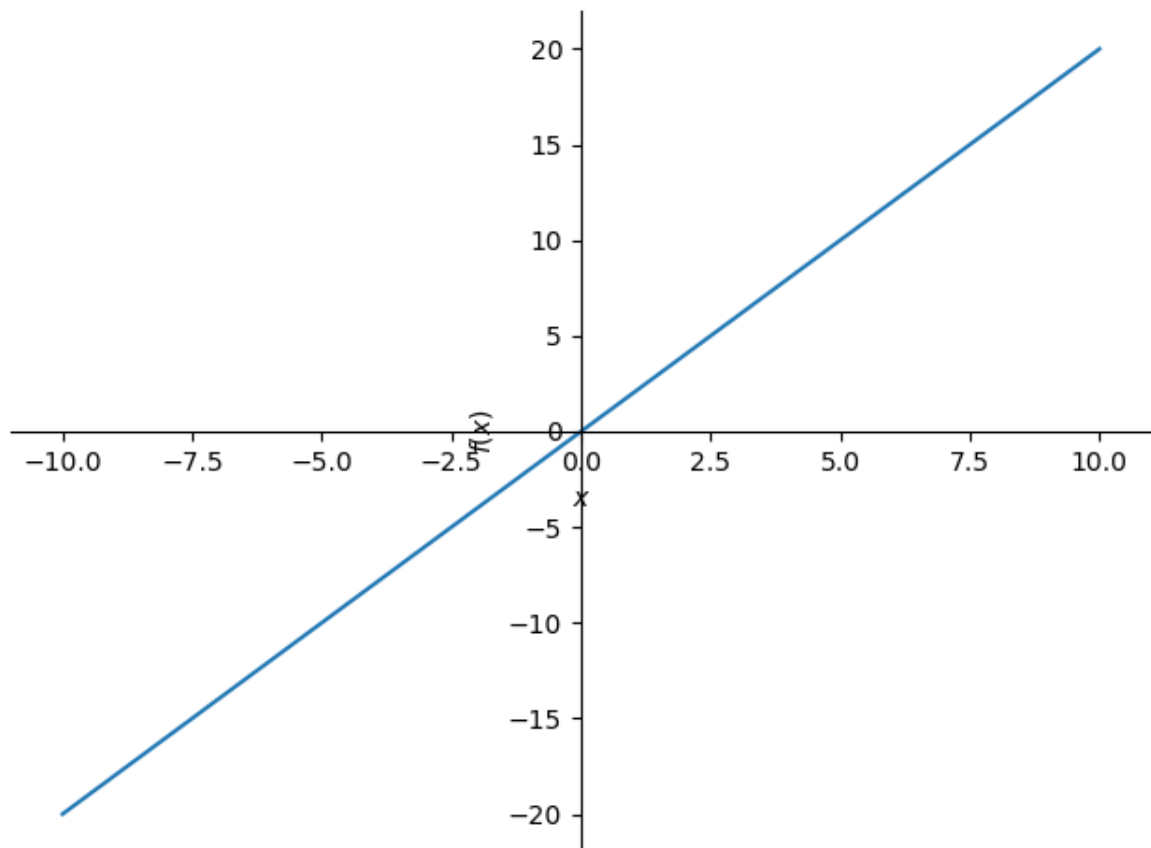
```
In [9]: sym.diff(expr) #equivalent to doit()
```

Out[9]: $2x$

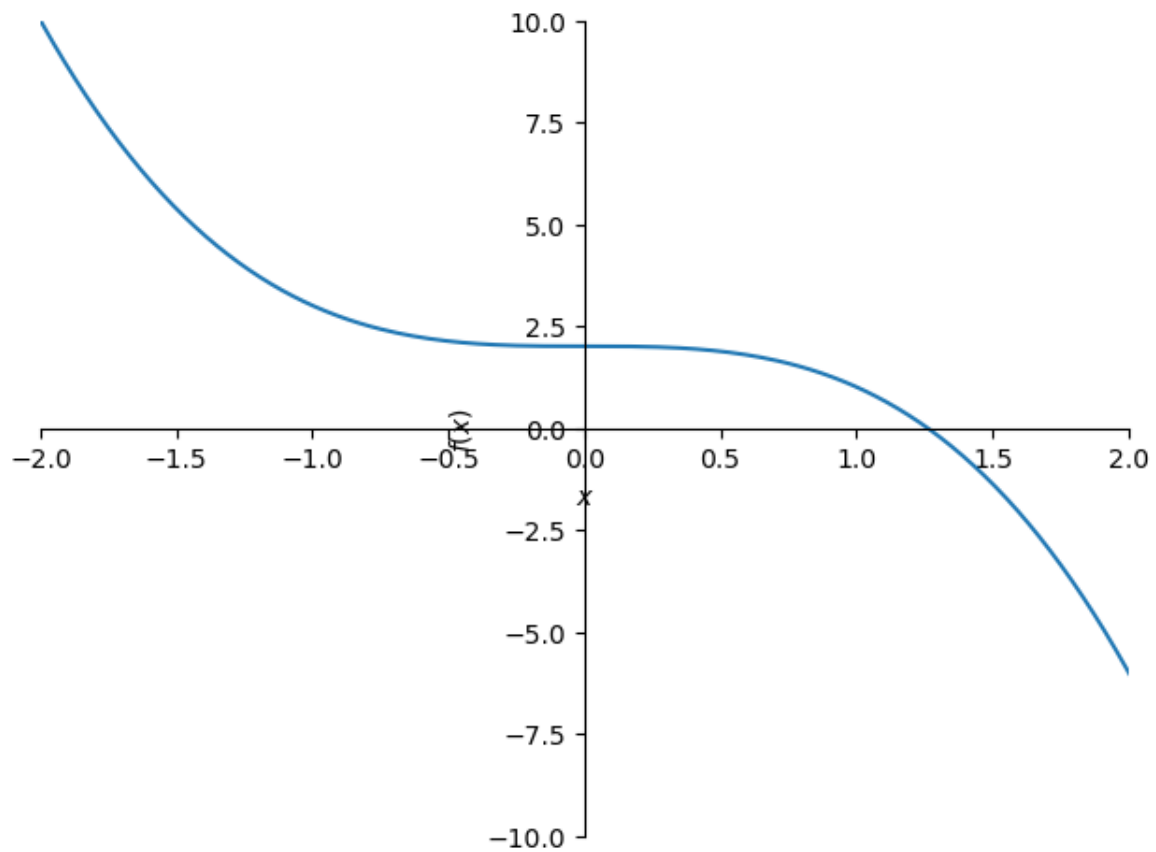
```
In [10]: sym.plot(expr);
```



```
In [11]: sym.plot(sym.diff(expr));
```



```
In [12]: x = sym.symbols('x')
expr = -x ** 3 + 2
sym.plot(expr, xlim=(-2, 2), ylim=(-10, 10));
```



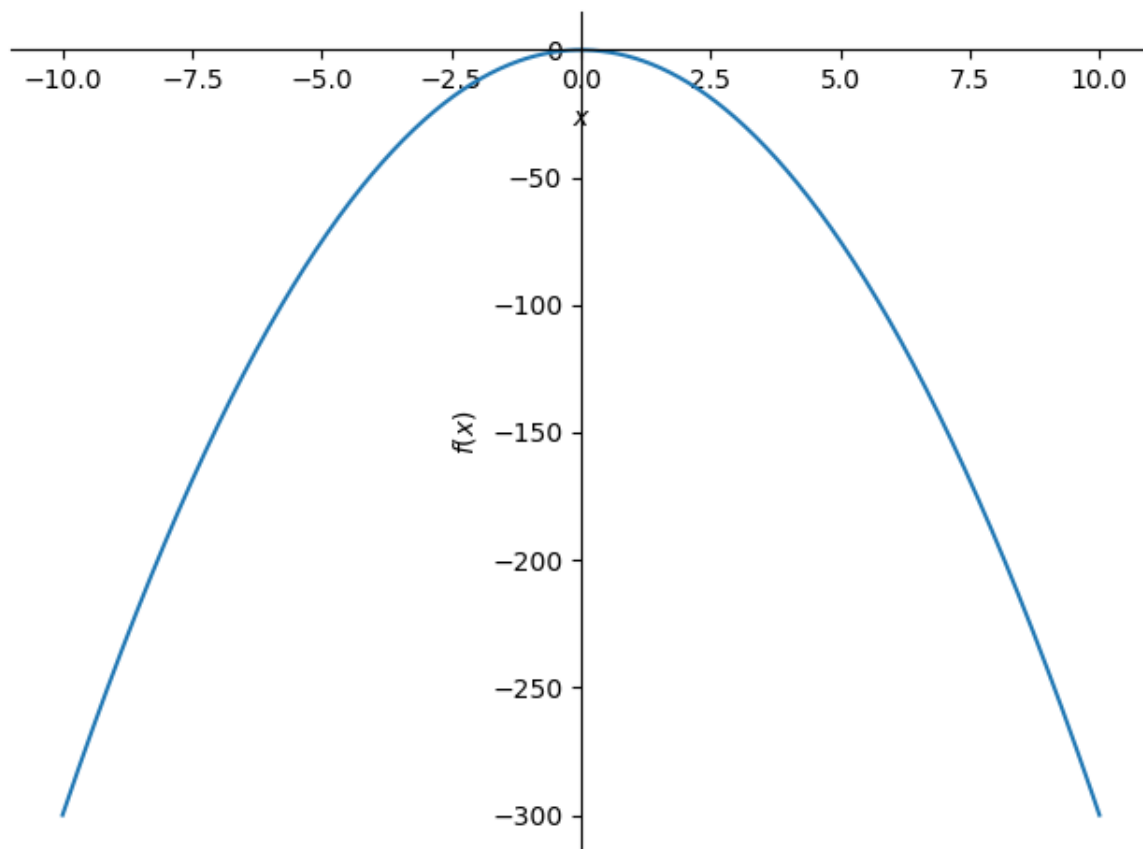
```
In [13]: sym.Derivative(expr)
```

```
Out[13]:  $\frac{d}{dx}(2 - x^3)$ 
```

```
In [14]: sym.Derivative(expr).doit()
```

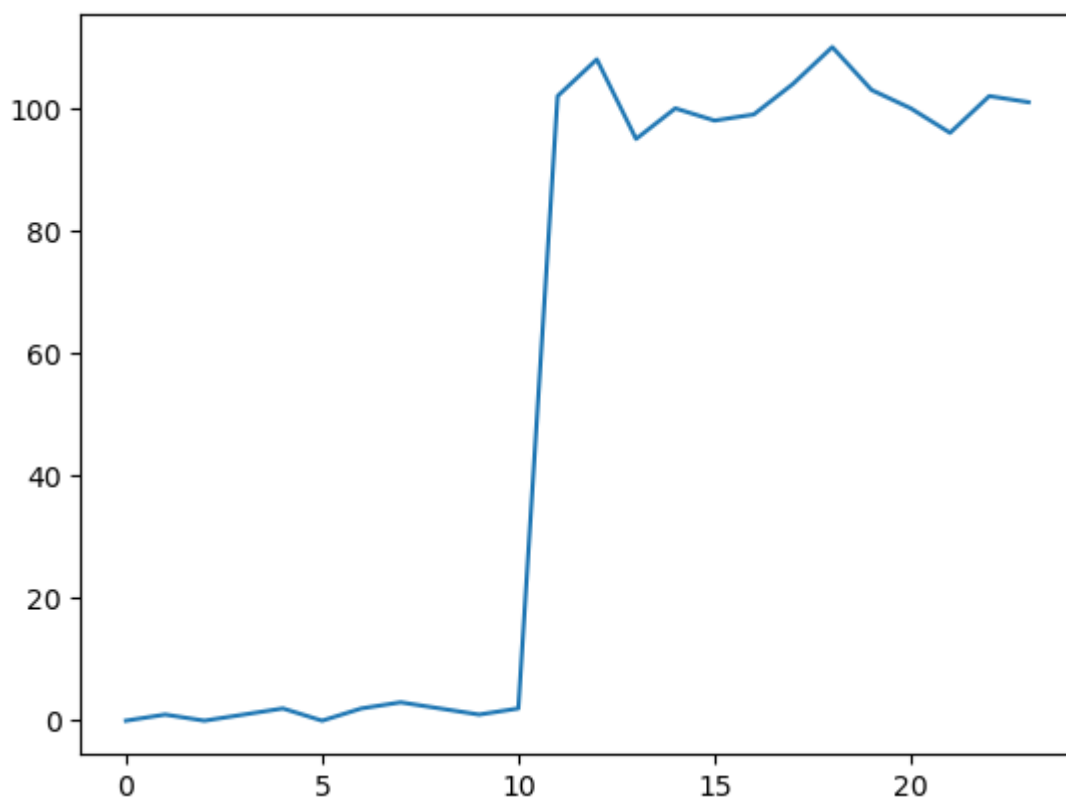
```
Out[14]:  $-3x^2$ 
```

```
In [15]: sym.plot(sym.diff(expr));
```



Now, let's generate a fake one-dimensional signal:

```
In [16]: ys = np.array([0, 1, 0, 1, 2, 0, 2, 3, 2, 1, 2, 102, 108, 95, 100, 98,
fig,ax = plt.subplots()
ax.plot([i for i in range(len(ys))], ys);
# check(1)
```



Next, let's look at small chunks of our fake signal:

```
In [17]: chunks = np.split(ys, len(ys)//2)
print(chunks)
# check(2)
```

```
[array([0, 1]), array([0, 1]), array([2, 0]), array([2, 3]), array([2,
1]), array([ 2, 102]), array([108, 95]), array([100, 98]), array([ 99,
104]), array([110, 103]), array([100, 96]), array([102, 101])]
```

Question: Which one of these chunks would you say is the most "interesting"?

The chunk around $x = 10$ because the y value suddenly increased by around 100.

Question If we always divide up the signal as we did above, will we always find something "interesting"?

Yes, because we can compare the numbers to find some outliers.

Convolutions

Derivatives and convolutions are one technique to help us tackle the above problem.

First, you'll need to generate windows into the signal. Write a function that can generate windows with a user-supplied window size, and print them out.

An example signal with 3 window sizes is shown below. Your output does not need to replicate the formatting shown, but they should produce the same windows. E.g., given an input signal of `[10,20,30]` and a `window size=2`, your function should return `[[10,20], [20,30]]`.

A window size of 1:

```
signal:
      0  1  0  2  1  0  1 101 100 98 102 101
0:      0
1:      1
2:      0
3:      2
4:      1
5:      0
6:      1
7:      101
8:      100
9:      98
10:     102
11:     101
```

```
.....
```

```
i:    0 | i + window size:    1 | window: [  0]
i:    1 | i + window size:    2 | window: [  1]
```

```
i: 2 | i + window size: 3 | window: [ 0]
i: 3 | i + window size: 4 | window: [ 2]
i: 4 | i + window size: 5 | window: [ 1]
i: 5 | i + window size: 6 | window: [ 0]
i: 6 | i + window size: 7 | window: [ 1]
i: 7 | i + window size: 8 | window: [101]
i: 8 | i + window size: 9 | window: [100]
i: 9 | i + window size:10 | window: [ 98]
i:10 | i + window size:11 | window: [102]
i:11 | i + window size:12 | window: [101]
```

A window size of 2:

```
signal:
      0  1  0  2  1  0  1 101 100  98 102 101
0:      0  1
1:      1  0
2:      0  2
3:      2  1
4:      1  0
5:      0  1
6:      1 101
7:      101 100
8:      100  98
9:      98 102
10:     102 101
```

```
::::::::::::::::::::::::::::::::::::::::::::::::::::::
```

```
i: 0 | i + window size: 2 | window: [ 0, 1]
i: 1 | i + window size: 3 | window: [ 1, 0]
i: 2 | i + window size: 4 | window: [ 0, 2]
i: 3 | i + window size: 5 | window: [ 2, 1]
i: 4 | i + window size: 6 | window: [ 1, 0]
i: 5 | i + window size: 7 | window: [ 0, 1]
i: 6 | i + window size: 8 | window: [ 1,101]
i: 7 | i + window size: 9 | window: [101,100]
i: 8 | i + window size:10 | window: [100, 98]
i: 9 | i + window size:11 | window: [ 98,102]
i:10 | i + window size:12 | window: [102,101]
```

A window size of 3

```
signal:
      0  1  0  2  1  0  1 101 100  98 102 101
0:      0  1  0
1:      1  0  2
2:      0  2  1
3:      2  1  0
4:      1  0  1
5:      0  1 101
6:      1 101 100
7:      101 100  98
```

8: _____ 100 98 102
9: _____ 98 102 101

.....

i:	0		i + window size:	3		window:	[0,	1,
0]									
i:	1		i + window size:	4		window:	[1,	0,
2]									
i:	2		i + window size:	5		window:	[0,	2,
1]									
i:	3		i + window size:	6		window:	[2,	1,
0]									
i:	4		i + window size:	7		window:	[1,	0,
1]									
i:	5		i + window size:	8		window:	[0,	1,
101]									
i:	6		i + window size:	9		window:	[1,	101,
100]									
i:	7		i + window size:	10		window:	[101,	100,
98]									
i:	8		i + window size:	11		window:	[100,	98,
102]									
i:	9		i + window size:	12		window:	[98,	102,
101]									

The below resources may be helpful::

List Comprehensions

https://www.pythonlikeyoumeanit.com/Module2_EssentialsOfPython/Generators_and_Comprehensions.html#List-&Tuple-Comprehensions

Numpy indexing with slices

http://www.pythonlikeyoumeanit.com/Module3_IntroducingNumpy/AccessingDataAlongMultipleDimensions.html#Slice-Indexing

Formatting numbers in python

<https://pyformat.info/#number>

```
input: '{:4d}'.format(42)
```

output: 4 2

```
input: '{:06.2f}'.format(3.141592653589793)
```

output: 003.14

String concatenation

```
>>> print('a' + 'b' + 'c')
abc
>>> print(''.join(['a', 'b', 'c']))
abc
>>> print(''.join(['a', 'b', 'c']))
a,b,c
```

```
In [36]: def make_windows(sequence, windowsize):
# raise NotImplementedError # TODO
my_list = []
# new_seq = enumerate(sequence)
# for s in new_seq:
#     for w in range(windowsize):
#         seq = s[0]
#         x = []
#         if not (seq + w) >= len(sequence):
#             x.append(sequence[seq + w])
#             my_list.append(x)

# return my_list

place = len(sequence) - windowsize + 1
for i in range(place):
    my_list.append(sequence[i:i + windowsize])

return my_list
```

```
In [37]: series = [0, 1, 0, 2, 1, 0, 1, 101, 100, 98, 102, 101]

make_windows(sequence=series, windowsize=1)
make_windows(sequence=series, windowsize=2)
make_windows(sequence=series, windowsize=3)

# check(3)
```

```
Out[37]: [[0, 1, 0], [1, 0, 2], [0, 2, 1], [2, 1, 0], [1, 0, 1], [0, 1, 101], [1, 101, 100], [101
```

When you are done:

Generate some example outputs in this notebook.

1. Double-check that you filled in your name at the top of the notebook!
2. Click File -> Export Notebook As -> PDF
3. Email the PDF to YOURTEAMNAME@beaver.works