

# SOLUTION FOR HOMEWORK ASSIGNMENT NO. 09

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## Exercise 9.1

In this exercise we have to do a simple hypothesis testing on our own. The test statistic to use is defined by the Neyman-Pearson lemma,

$$\Lambda(\{x\}) = \frac{\mathcal{L}(\{x\} | H_1)}{\mathcal{L}(\{x\} | H_0)} \quad (1)$$

where  $\{x\}$  stands for the data set,  $H_0$  for the hypothesis for *background-only* signal and  $H_1$  for the *background+signal* hypothesis.

The theory predicts the following parameters:

The particle mass of 751 GeV,  
a peak-width of 30 GeV,  
an exponential background  $e^{-a \cdot x}$  with  $a = 1 \times 10^{-3} \text{ GeV}^{-1}$  and  
an production rate of 3 signal events for 10 background events.

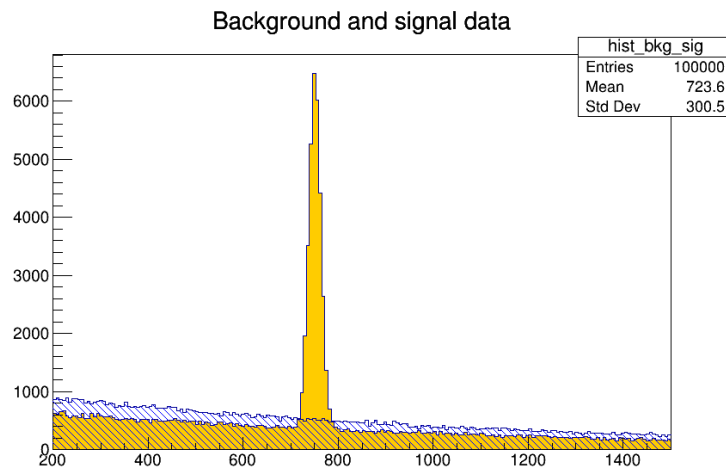
First, we generate Monte Carlo data. As said before we use an exponential function for the background and an exponential function plus a gaussian function for background and signal

$$f_{\text{bkg}} = A_{\text{bkg}} \cdot \exp(-a \cdot x) \quad (2)$$

$$f_{\text{sig}} = A_{\text{sig}} \cdot \exp\left(-\frac{(x - \mu)^2}{\sigma^2}\right) \quad (3)$$

with the amplitudes  $A_{\text{bkg}}$  and  $A_{\text{sig}}$ .

We generate 1000 times  $1 \times 10^5$  datapoints for the *background-only* and the *background+signal* hypothesis. You can find a visualisation of the first iteration of datapoints in figure 1.



**Figure 1:** Visualisation of datapoints for the *background-only* (blue, dashed) and *background+signal* (orange, filled) hypothesis. Each histogram contains  $1 \times 10^5$  datapoints.

Next, we calculate the test statistic  $\Lambda$  for every iteration. The histograms for  $H_0$  and  $H_1$  can be found in figure 1.