1)Removal of Recursion

Write a program to implement removal of recursion for-

a)Finding maximum from array.

```
#include <iostream>
using namespace std;
int findMax(int arr[], int n) {
    int max = arr[0];
    for (int i = 1; i < n; i++) {
        if (arr[i] > max)
            max = arr[i];
    }
    return max;
}
int main() {
    int arr[] = {5, 3, 9, 2, 8, 10};
    int n = sizeof(arr) / sizeof(arr[0]);
    cout << "Maximum element: " << findMax(arr, n);
    return 0;
}</pre>
```

Output:

```
C:\Users\MCM\Documents\1.exe

Maximum element: 10

Process exited after 0.01334 seconds with return value 0

Press any key to continue . . .
```

b) Binomial Coefficient B(n,m)=B(n-1,m-1)+B(n-1,m),B(n,n)=B(n,0)=1.

```
#include <iostream>
using namespace std;
int binomialCoeff(int m, int n) {
  int C[m + 1][n + 1];
  for (int i = 0; i \le m; i++) {
     for (int j = 0; j \le min(i, n); j++) {
       if (j == 0 || j == i)
          C[i][j] = 1;
       else
          C[i][j] = C[i-1][j-1] + C[i-1][j];
     }
  }
  return C[m][n];
}
int main() {
  int m = 5, n = 2;
  cout << "Binomial Coefficient C(" << m << "," << n << ") is " << binomial Coeff(m, n);
  return 0;
}
```

```
C:\Users\MCM\Documents\2.exe

Binomial Coefficient C(5,2) is 10

Process exited after 0.01428 seconds with return value 0

Press any key to continue . . .
```

c)Searching element from array.

```
#include <iostream>
using namespace std;
int linearSearch(int arr[], int n, int x) {
  for (int i = 0; i < n; i++) {
     if (arr[i] == x)
        return i;
  }
  return -1;
}
int main() {
  int arr[] = \{5, 7, 2, 8, 4\};
  int n = sizeof(arr) / sizeof(arr[0]);
  int x = 8;
  int result = linearSearch(arr, n, x);
  if (result != -1)
     cout << "Element found at index: " << result;</pre>
  else
     cout << "Element not found";</pre>
  return 0;
}
```

```
C:\Users\MCM\Documents\3.exe

Element found at index: 3

Process exited after 0.02206 seconds with return value 0

Press any key to continue . . .
```

2)Elementary data structure-Tree

a)Write a program for creating max/min heap using INSERT.

```
#include <iostream>
using namespace std;
void insertMaxHeap(int heap[], int& size, int value) {
  size++;
  heap[size] = value;
  int i = size;
  while (i > 1 \&\& heap[i / 2] < heap[i]) {
     swap(heap[i], heap[i / 2]);
     i = i / 2;
  }
}
void printHeap(int heap[], int size) {
  for (int i = 1; i \le size; i++)
     cout << heap[i] << " ";
  cout << endl;
}
int main() {
  int heap[100], size = 0;
  int elements[] = {10, 20, 15, 30, 40};
  for (int i = 0; i < 5; i++)
     insertMaxHeap(heap, size, elements[i]);
cout << "Max Heap: ";</pre>
  printHeap(heap, size);
  return 0;}
```

b)Write a program for creating max/min heap using ADJUST/HEAPIFY.

```
#include <iostream>
using namespace std;
void heapify(int arr[], int n, int i) {
  int largest = i;
  int left = 2 * i + 1;
  int right = 2 * i + 2;
  if (left < n && arr[left] > arr[largest])
     largest = left;
  if (right < n && arr[right] > arr[largest])
     largest = right;
  if (largest != i) {
     swap(arr[i], arr[largest]);
     heapify(arr, n, largest);
  }
}
void buildMaxHeap(int arr[], int n) {
  for (int i = n / 2 - 1; i \ge 0; i--)
     heapify(arr, n, i);
}
void printArray(int arr[], int n) {
  for (int i = 0; i < n; ++i)
     cout << arr[i] << " ";
  cout << endl;</pre>
}
int main() {
  int arr[] = {4, 10, 3, 5, 1};
  int n = sizeof(arr) / sizeof(arr[0]);
  buildMaxHeap(arr, n);
  cout << "Heapified Array: ";</pre>
  printArray(arr, n);
  return 0;
}
```

```
C:\Users\MCM\Documents\5.exe

Heapified Array: 10 5 3 4 1

Process exited after 0.02298 seconds with return value 0

Press any key to continue . . . _
```

c)Write a program for sorting given array in ascending /descending order with n=1000,2000,3000.find exact time of execution using heap sort.

```
#include <iostream>
#include <cstdlib> // ? For rand() and srand()
#include <ctime>
using namespace std;
void heapify(int arr[], int n, int i) {
  int largest = i;
  int l = 2 * i + 1;
  int r = 2 * i + 2;
          if (1 \le n \&\& arr[1] \ge arr[largest])
     largest = l;
  if (r < n \&\& arr[r] > arr[largest])
     largest = r;
  if (largest != i) {
     swap(arr[i], arr[largest]);
     heapify(arr, n, largest);
  }
}
void heapSort(int arr[], int n) {
  for (int i = n / 2 - 1; i \ge 0; i--)
     heapify(arr, n, i);
  for (int i = n - 1; i > 0; i--) {
     swap(arr[0], arr[i]);
     heapify(arr, i, 0);
  }
}
int main() {
  int sizes[] = {1000, 2000, 3000};
          for (int s = 0; s < 3; s++) {
     int n = sizes[s];
     int* arr = new int[n];
```

```
for (int i = 0; i < n; i++)
    arr[i] = rand();
        clock_t start = clock();
    heapSort(arr, n);
    clock_t end = clock();
        cout << "Time taken for n = " << n << ": "
        << (double)(end - start) / CLOCKS_PER_SEC << " seconds\n";
    delete[] arr;
}
return 0;</pre>
```

}

d)Write a program to implement Weighted UNION and Collapsing FIND operation.

```
#include <iostream>
using namespace std;
const int MAX = 1000;
int parent[MAX], size[MAX];
void makeSet(int n) {
  for (int i = 0; i < n; i++) {
     parent[i] = i;
     size[i] = 1;
  }
}
int find(int x) {
  if (x != parent[x])
     parent[x] = find(parent[x]); // Path compression
  return parent[x];
}
void unionSets(int a, int b) {
  int rootA = find(a);
  int rootB = find(b);
  if (rootA != rootB) {
     if (size[rootA] < size[rootB])</pre>
       swap(rootA, rootB);
     parent[rootB] = rootA;
     size[rootA] += size[rootB];
  }
}
int main() {
  int n = 5;
  makeSet(n);
  unionSets(0, 1);
  unionSets(1, 2);
  unionSets(3, 4);
  cout << "Find(2): " << find(2) << endl;</pre>
```

```
cout << "Find(4): " << find(4) << endl;
return 0;
}</pre>
```

```
C:\Users\MCM\Documents\7.exe

Find(2): 0
Find(4): 3
-----

Process exited after 0.01553 seconds with return value 0
Press any key to continue . . .
```

3)Divide and Conquer.

a) Write a program for searching element from given array using binary search for n=1000,2000,3000. Find exact time of execution .

```
#include <iostream>
#include <ctime>
using namespace std;
int binarySearch(int arr[], int l, int r, int x) {
  while (l \le r) {
     int mid = 1 + (r - 1) / 2;
     if (arr[mid] == x) return mid;
     if (arr[mid] < x) l = mid + 1;
     else r = mid - 1;
  return -1;}
int main() {
  int sizes[] = \{1000, 2000, 3000\};
  for (int s = 0; s < 3; s++) {
     int n = sizes[s];
     int* arr = new int[n];
     for (int i = 0; i < n; i++) arr[i] = i * 2;
     int key = arr[n - 1]; // Last element for worst case
     clock_t start = clock();
     int index = binarySearch(arr, 0, n - 1, key);
     clock_t end = clock();
     cout << "n = " << n << ", Time: "
        << (double)(end - start) / CLOCKS_PER_SEC << " seconds\n";
     delete[] arr;
  }
  return 0;}
```

```
C:\Users\MCM\Documents\8.exe

n = 1000, Time: 0 seconds
n = 2000, Time: 0 seconds
n = 3000, Time: 0 seconds
Process exited after 0.01516 seconds with return value 0
```

b)Write a program to find maximum and minimum from given array using MAXMIN.

```
#include <iostream>
#include <utility> // for std::pair
#include <algorithm> // for std::max and std::min
using namespace std;
pair<int, int> maxMin(int arr[], int low, int high) {
  int maxVal, minVal;
  if (low == high)
     return make_pair(arr[low], arr[low]);
  if (high == low + 1) {
     if (arr[low] > arr[high])
       return make_pair(arr[low], arr[high]);
     else
       return make_pair(arr[high], arr[low]);
  }
  int mid = (low + high) / 2;
  pair<int, int> left = maxMin(arr, low, mid);
  pair<int, int> right = maxMin(arr, mid + 1, high);
  maxVal = max(left.first, right.first);
  minVal = min(left.second, right.second);
  return make_pair(maxVal, minVal);}
int main() {
  int arr[] = \{100, 200, 5, 2, 999, 21, 67\};
  int n = sizeof(arr) / sizeof(arr[0]);
  pair<int, int> result = maxMin(arr, 0, n - 1);
  cout << "Max: " << result.first << ", Min: " << result.second << endl;</pre>
  return 0;
}
```

c) Write a program for sorting given array in ascending/descending order with n=1000,2000,3000 Find exact time of execution using -

d)Merge sort

```
#include <iostream>
#include <cstdlib>
#include <ctime>
using namespace std;
void merge(int arr[], int beg, int mid, int end) {
int n1=mid-beg+1;
int n2=end-mid;
int leftarray[n1];
int rightarray[n2];
for(int i=0;i<n1;i++)
leftarray[i]=arr[beg+i];
for(int j=0; j< n2; j++)
rightarray[j]=arr[mid+1+j];
int i=0,j=0,k=beg;
while(i<n1 && j<n2){
if(leftarray[i]<=rightarray[j]){</pre>
         arr[k]=leftarray[i];
         i++;
else{
   arr[k]=rightarray[j];
         j++;
}k++;
\wedge while (i \le n1) {
arr[k]=leftarray[i];
         i++;
         k++;
 }
 while(j \le n2){
         arr[k]=rightarray[j];
```

```
j++;
         k++;
 }
}
void mergesort(int arr[],int beg,int end){
if(beg<end){
         int mid=(beg+end)/2;
         mergesort(arr,beg,mid);
         mergesort(arr,mid+1,end);
         merge(arr,beg,mid,end);
}
int main() {
 int sizes[] = {1000, 2000, 3000};
 for (int s = 0; s < 3; s++) {
 int n = sizes[s];
 int* arr = new int[n];
for (int i = 0; i < n; i++) arr[i] = rand() % 10000;
clock_t start = clock();
mergesort(arr, 0, n - 1);
clock_t end = clock();
cout << "Merge Sort Time for n = " << n << ": "
        << (double)(end - start) / CLOCKS_PER_SEC << " seconds\n";
 delete[] arr;
  }
return 0;
```

e)Quick sort

```
#include <iostream>
#include <cstdlib>
#include <ctime>
using namespace std;
int partition(int arr[], int low, int high) {
  int pivot = arr[high], i = low - 1;
  for (int j = low; j < high; j++) {
     if (arr[j] < pivot) {</pre>
       i++;
       swap(arr[i], arr[j]);
     }
  }
  swap(arr[i + 1], arr[high]);
  return i + 1;
}
void quickSort(int arr[], int low, int high) {
  if (low < high) {
     int pi = partition(arr, low, high);
     quickSort(arr, low, pi - 1);
     quickSort(arr, pi + 1, high);
  }
}
int main() {
  int sizes[] = {1000, 2000, 3000};
  for (int s = 0; s < 3; s++) {
     int n = sizes[s];
     int* arr = new int[n];
     for (int i = 0; i < n; i++) arr[i] = rand() % 10000;
     clock_t start = clock();
     quickSort(arr, 0, n - 1);
     clock_t end = clock();
     cout << "Quick Sort Time for n = " << n << ": "
```

```
      << (double)(end - start) / CLOCKS_PER_SEC << " seconds\n";
      delete[] arr;
    }
    return 0;
}</pre>
```

```
Quick Sort Time for n = 1000: 0 seconds
Quick Sort Time for n = 2000: 0 seconds
Quick Sort Time for n = 3000: 0.002 seconds
Quick Sort Time for n = 3000: 0.002 seconds

Process exited after 0.02681 seconds with return value 0
Press any key to continue . . .
```

f)Write a program for matrix multiplication using Strassen's Matrix Multiplication.

```
#include <iostream>
using namespace std;
void add(int A[2][2], int B[2][2], int C[2][2]) {
  for (int i = 0; i < 2; i++)
     for (int j = 0; j < 2; j++)
       C[i][j] = A[i][j] + B[i][j];
}
void subtract(int A[2][2], int B[2][2], int C[2][2]) {
  for (int i = 0; i < 2; i++)
     for (int j = 0; j < 2; j++)
        C[i][j] = A[i][j] - B[i][j];
}
void strassen(int A[2][2], int B[2][2], int C[2][2]) {
  int M1 = (A[0][0] + A[1][1]) * (B[0][0] + B[1][1]);
  int M2 = (A[1][0] + A[1][1]) * B[0][0];
  int M3 = A[0][0] * (B[0][1] - B[1][1]);
  int M4 = A[1][1] * (B[1][0] - B[0][0]);
  int M5 = (A[0][0] + A[0][1]) * B[1][1];
  int M6 = (A[1][0] - A[0][0]) * (B[0][0] + B[0][1]);
  int M7 = (A[0][1] - A[1][1]) * (B[1][0] + B[1][1]);
  C[0][0] = M1 + M4 - M5 + M7;
  C[0][1] = M3 + M5;
  C[1][0] = M2 + M4;
  C[1][1] = M1 - M2 + M3 + M6;
}
int main() {
  int A[2][2] = \{\{1, 2\}, \{3, 4\}\};
  int B[2][2] = \{\{5, 6\}, \{7, 8\}\};
  int C[2][2];
  strassen(A, B, C);
  cout << "Result Matrix:\n";</pre>
  for (int i = 0; i < 2; i++) {
```

```
Result Matrix:
19 22
43 50

Process exited after 0.01809 seconds with return value 0
Press any key to continue . . .
```

4) GREEDY ALGORITHM

a) Write a Program to find solution of Fractional Knapsack instance.

```
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
// Structure to represent an item
struct Item {
  int weight;
  int profit;
  double ratio;
  // Constructor
  Item(int w, int p) {
     weight = w;
     profit = p;
     ratio = (double)p / w;
  }
};
// Comparison function to sort items by ratio
bool compare(Item a, Item b) {
  return a.ratio > b.ratio;
}
// Function to solve Fractional Knapsack
double fractionalKnapsack(vector<Item> items, int capacity) {
  // Sort items by value-to-weight ratio
  sort(items.begin(), items.end(), compare);
  double total Profit = 0.0;
  int currWeight = 0;
  for (int i = 0; i < items.size(); ++i) {
     if (currWeight + items[i].weight <= capacity) {</pre>
       currWeight += items[i].weight;
       totalProfit += items[i].profit;
     } else {
```

```
int remain = capacity - currWeight;
        totalProfit += items[i].ratio * remain;
        break;
     }
  }
  return totalProfit;
}
// Main function
int main() {
  int n, capacity;
  cout << "Enter number of items: ";</pre>
  cin >> n;
  vector<Item> items;
  cout << "Enter weight and profit of each item:\n";</pre>
  for (int i = 0; i < n; ++i) {
     int w, p;
     cin >> w >> p;
     items.push_back(Item(w, p));
  }
  cout << "Enter capacity of knapsack: ";</pre>
  cin >> capacity;
  double maxProfit = fractionalKnapsack(items, capacity);
  cout << "Maximum profit: " << maxProfit << endl;</pre>
  return 0;
}
```

```
Enter number of items: 3
Enter weight and profit of each item:
10 60
20 100
30 120
Enter capacity of knapsack: 50
Maximum profit: 240

Process exited after 48.33 seconds with return value 0
Press any key to continue . . .
```

b) Write a program to find Minimum Spanning Tree using Prim's Algorithm.

```
#include <iostream>
#include <vector>
#include <climits> // for INT_MAX
using namespace std;
const int MAX = 100;
int findMinKey(int key[], bool mstSet[], int V) {
  int min = INT_MAX, minIndex;
  for (int v = 0; v < V; v++)
     if (!mstSet[v] \&\& key[v] < min)
       min = key[v], minIndex = v;
  return minIndex;
}
void printMST(int parent[], int graph[MAX][MAX], int V) {
  cout << "Edge \tWeight\n";</pre>
  for (int i = 1; i < V; i++)
     cout << parent[i] << " - " << i << "\t" << graph[i][parent[i]] << "\n";</pre>
}
void primMST(int graph[MAX][MAX], int V) {
  int parent[V]; // Stores MST
  int key[V]; // Used to pick minimum weight edge
  bool mstSet[V]; // To represent included vertices
  // Initialize keys
  for (int i = 0; i < V; i++)
     key[i] = INT_MAX, mstSet[i] = false;
  key[0] = 0; // Start from first vertex
  parent[0] = -1; // Root of MST
  for (int count = 0; count < V - 1; count++) {
     int u = findMinKey(key, mstSet, V);
     mstSet[u] = true;
     for (int v = 0; v < V; v++) {
       if (graph[u][v] \&\& !mstSet[v] \&\& graph[u][v] < key[v])
          parent[v] = u, key[v] = graph[u][v];
```

```
}
  }
  printMST(parent, graph, V);
}
int main() {
  int V;
  cout << "Enter number of vertices: ";</pre>
  cin >> V;
  int graph[MAX][MAX];
  cout << "Enter the adjacency matrix (use 0 if no edge):\n";</pre>
  for (int i = 0; i < V; i++)
     for (int j = 0; j < V; j++)
       cin >> graph[i][j];
  cout << "\nMinimum Spanning Tree using Prim's Algorithm:\n";</pre>
  primMST(graph, V);
  return 0;
}
```

```
Enter number of vertices: 5
Enter the adjacency matrix (use 0 if no edge):
1 0 3 4 2
2 3 1 0 2
3 4 1 0 6
1 3 4 2 0
0 2 1 4 5

Minimum Spanning Tree using Prim's Algorithm:
Edge Weight
4 - 1 2
4 - 2 6
0 - 3 1
0 - 4 0

Process exited after 55.4 seconds with return value 0
Press any key to continue . . .
```

c)Write a program to find Minimum Spanning Tree using Kruskal's algorithm.

```
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
struct Edge {
  int u, v, weight;
};
bool compare(Edge a, Edge b) {
  return a.weight < b.weight;
}
class DisjointSet {
public:
  vector<int> parent;
  DisjointSet(int n) {
     parent.resize(n);
     for (int i = 0; i < n; ++i)
       parent[i] = i;
  }
  int find(int i) {
     if (parent[i] != i)
       parent[i] = find(parent[i]);
     return parent[i];
  }
  void unionSet(int u, int v) {
     int set_u = find(u);
     int set_v = find(v);
     if (set_u != set_v)
       parent[set_u] = set_v;
  }};
void kruskalMST(int V, vector<Edge>& edges) {
  sort(edges.begin(), edges.end(), compare);
  DisjointSet ds(V);
```

```
vector<Edge> mst;
  int totalWeight = 0;
  for (int i = 0; i < edges.size(); ++i) {
     Edge e = edges[i];
     if (ds.find(e.u) != ds.find(e.v)) {
        mst.push_back(e);
        totalWeight += e.weight;
       ds.unionSet(e.u, e.v);
     } }
cout << "Minimum Spanning Tree using Kruskal's Algorithm:\n";</pre>
  cout << "Edge\tWeight\n";</pre>
  for (int i = 0; i < mst.size(); ++i)
     cout << mst[i].u << " - " << mst[i].v << "\t" << mst[i].weight << "\n";
  cout << "Total weight of MST: " << totalWeight << "\n";</pre>
}
int main() {
  int V, E;
  cout << "Enter number of vertices and edges: ";</pre>
  cin >> V >> E;
  vector<Edge> edges(E);
  cout << "Enter each edge as: u v weight\n";</pre>
  for (int i = 0; i < E; ++i)
     cin >> edges[i].u >> edges[i].v >> edges[i].weight;
kruskalMST(V, edges);
  return 0;
}
```

```
Enter number of vertices and edges: 4 5
Enter each edge as: u v weight
1 0 2
2 3 4

1 0 4
2 0 98
2 3 1
Minimum Spanning Tree using Kruskal's Algorithm:
Edge Weight
2 - 3 1
1 - 0 2
2 - 0 98
Total weight of MST: 101
```

d)Write a program to find Single Source Shortest Path using Dijkstra's algorithm

```
#include <iostream>
#include <vector>
#include inits>
using namespace std;
#define INF 99999 // Representing infinity
void dijkstra(int graph[10][10], int V, int src) {
  vector<int> dist(V, INF); // Distance from source to each vertex
  vector<bool> visited(V, false); // Track visited vertices
  dist[src] = 0; // Distance to source is 0
  for (int count = 0; count < V - 1; ++count) {
     // Find the minimum distance vertex from the set of unvisited vertices
     int u = -1;
     int minDist = INF;
     for (int i = 0; i < V; ++i) {
       if (!visited[i] && dist[i] < minDist) {</pre>
          minDist = dist[i];
          u = i;
       }
     }
     if (u == -1) break; // No reachable vertex left
     visited[u] = true;
     // Update distances to neighboring vertices
     for (int v = 0; v < V; ++v) {
       if (!visited[v] && graph[u][v] && dist[u] + graph[u][v] \leq dist[v])
          dist[v] = dist[u] + graph[u][v];
     }
  }
  // Print the result
  cout << "Vertex\tDistance from Source " << src << endl;</pre>
  for (int i = 0; i < V; ++i)
     cout << i << "\t" << dist[i] << endl;}
```

```
int main() {
  int V;
  cout << "Enter number of vertices: ";
  cin >> V;
  int graph[10][10];
  cout << "Enter the adjacency matrix (0 if no edge, >0 for weight):" << endl;
  for (int i = 0; i < V; ++i)
     for (int j = 0; j < V; ++j)
        cin >> graph[i][j];
  int src;
  cout << "Enter the source vertex: ";
  cin >> src;
  dijkstra(graph, V, src);
  return 0;
}
```

```
Enter number of vertices: 5
Enter the adjacency matrix (0 if no edge, >0 for weight):
1 0 10 3 2
0 2 12 5 2
1 2 3 4 5
0 3 4 2 4
0 1 1 0 3
Enter the source vertex: 0
Vertex Distance from Source 0
0 0
1 3
2 3
3 3
4 2
Process exited after 43.6 seconds with return value 0
Press any key to continue . . .
```

5) Dynamic Programming

a) Write a program to find solution of Knapsack Instance (0/1).

```
#include <iostream>
#include <vector>
using namespace std;
int knapsack(int W, vector<int>& weights, vector<int>& values, int n) {
  vector<vector<int> > dp(n + 1, vector<int>(W + 1, 0));
  for (int i = 1; i \le n; i++) {
     for (int w = 1; w \le W; w++) {
       if (weights[i - 1] <= w) {
          dp[i][w] = max(values[i-1] + dp[i-1][w - weights[i-1]],
                    dp[i - 1][w]);
       } else {
          dp[i][w] = dp[i - 1][w];
       }
     }
  }
  return dp[n][W];
}
int main() {
  int n, W;
  cout << "Enter number of items: ";</pre>
  cin >> n;
  vector<int> weights(n), values(n);
  cout << "Enter weights of items: ";</pre>
  for (int i = 0; i < n; i++) cin >> weights[i];
  cout << "Enter values of items: ";</pre>
  for (int i = 0; i < n; i++) cin >> values[i];
  cout << "Enter capacity of knapsack: ";</pre>
  cin >> W;
  int maxValue = knapsack(W, weights, values, n);
  cout << "Maximum value that can be obtained = " << maxValue << endl;</pre>
  return 0;}
```

```
Enter number of items: 4
Enter weights of items: 2 3 4 5
Enter values of items: 6 2 3 1
Enter capacity of knapsack: 3
Maximum value that can be obtained = 6

Process exited after 32.84 seconds with return value 0
Press any key to continue . . .
```

b)Write a program to find solution of matrix chain multiplication.

```
#include <iostream>
#include imits.h>
using namespace std;
// Function to compute minimum number of multiplications
int matrixChainMultiplication(int p[], int n) {
  int m[n][n];
 // m[i][j] = Minimum number of multiplications needed to compute A[i]A[i+1]...A[j] = A[i..j]
  for (int i = 1; i < n; i++) {
     m[i][i] = 0; // cost is 0 when multiplying one matrix
  }
  // l is chain length
  for (int l = 2; l < n; l++) {
     for (int i = 1; i < n - l + 1; i++) {
       int j = i + l - 1;
        m[i][j] = INT\_MAX;
        for (int k = i; k < j; k++) {
          int q = m[i][k] + m[k + 1][j] + p[i - 1]*p[k]*p[j];
          if (q \le m[i][j])
             m[i][j] = q;
       }
     }
  }
  return m[1][n - 1];
}
int main() {
  int n;
  cout << "Enter number of matrices: ";</pre>
  cin >> n;
  int p[n + 1];
  cout << "Enter dimensions (array of size " << n + 1 << "): ";
  for (int i = 0; i \le n; i++) {
     cin >> p[i];
```

```
}
int result = matrixChainMultiplication(p, n + 1);
cout << "Minimum number of multiplications is: " << result << endl;
return 0;
}</pre>
```

c)Write a program to find shortest path using all pair shortest path algorithm.

```
#include <iostream>
using namespace std;
#define INF 99999
#define V 100 // Maximum number of vertices
void floydWarshall(int graph[V][V], int n) {
  int dist[V][V];
  // Initialize the solution matrix same as input graph matrix
  for (int i = 0; i < n; i++)
     for (int j = 0; j < n; j++)
       dist[i][j] = graph[i][j];
  // Floyd-Warshall Algorithm
  for (int k = 0; k < n; k++) {
     for (int i = 0; i < n; i++) {
       for (int j = 0; j < n; j++) {
          // Update the distance if going through vertex k is shorter
          if (dist[i][k] + dist[k][j] < dist[i][j])
             dist[i][j] = dist[i][k] + dist[k][j];
       }
     }
  }
  // Print the shortest distance matrix
  cout << "\nShortest distances between every pair of vertices:\n";</pre>
  for (int i = 0; i < n; i++) {
     for (int j = 0; j < n; j++) {
       if (dist[i][j] == INF)
          cout << "INF ";
       else
          cout << dist[i][j] << " ";
     cout << endl;
  }
}
```

```
int main() {
  int n;
  cout << "Enter number of vertices: ";
  cin >> n;
  int graph[V][V];
  cout << "Enter the adjacency matrix (use " << INF << " for no direct path):\n";
  for (int i = 0; i < n; i++)
      for (int j = 0; j < n; j++)
      cin >> graph[i][j];
  floydWarshall(graph, n);
  return 0;
}
```

```
Enter number of vertices: 4
Enter the adjacency matrix (use 99999 for no direct path):
1 0 6666 2
9999 2 3 4444
1 2222 3 1111
0 66666 2 3
Shortest distances between every pair of vertices:
1 0 3 2
4 2 3 6
1 1 3 3
0 0 2 2

Process exited after 37.34 seconds with return value 0
Press any key to continue . . . .
```

d)Write a program to Traverse Graph-Depth First Search, Breadth First Search.

```
#include <iostream>
#include <vector>
#include <queue>
using namespace std;
#define MAX 100
vector<int> adj[MAX];
bool visited[MAX];
// Depth First Search (DFS)
void DFS(int node) {
  visited[node] = true;
  cout << node << " ";
  for (int i = 0; i < adj[node].size(); i++) {
     int neighbor = adj[node][i];
     if (!visited[neighbor])
       DFS(neighbor);
  }
}
// Breadth First Search (BFS)
void BFS(int start) {
  for (int i = 0; i < MAX; i++)
     visited[i] = false;
  queue<int> q;
  visited[start] = true;
  q.push(start);
  while (!q.empty()) {
     int node = q.front();
     q.pop();
     cout << node << " ";
     for (int i = 0; i < adj[node].size(); i++) {
       int neighbor = adj[node][i];
       if (!visited[neighbor]) {
          visited[neighbor] = true;
```

```
q.push(neighbor);
        }
     }
  }
}
int main() {
  int vertices, edges, u, v, start;
  cout << "Enter number of vertices and edges: ";</pre>
  cin >> vertices >> edges;
  cout << "Enter edges (u v):\n";
  for (int i = 0; i < edges; i++) {
     cin >> u >> v;
     adj[u].push_back(v);
     adj[v].push_back(u); // for undirected graph
  }
  cout << "Enter starting node for traversal: ";</pre>
  cin >> start;
  // DFS
  for (int i = 0; i < MAX; i++)
     visited[i] = false;
  cout << "\nDFS Traversal: ";</pre>
  DFS(start);
  // BFS
  cout << "\nBFS Traversal: ";</pre>
  BFS(start);
  return 0;}
```

```
Enter number of vertices and edges: 6 7
Enter edges (u v):
1 0
2 0
1 6
2 3
1 0
1 5
5 6
Enter starting node for traversal: 0

DFS Traversal: 0 1 6 5 2 3
BFS Traversal: 0 1 2 6 5 3
```

6)BackTracking

a) Write a program to find all solutions for N-Queen problem using backtracking.

```
#include <iostream>
#include <vector>
#include <cmath>
using namespace std;
#define MAX 20
int board[MAX], count = 0;
// Function to check if position is safe
bool isSafe(int row, int col, int n) {
  for (int i = 1; i < row; i++) {
     // Check column and diagonals
     if (board[i] == col \parallel abs(board[i] - col) == abs(i - row))
       return false;
  }
  return true;
}
// Recursive backtracking function
void solveNQueens(int row, int n) {
  if (row > n) {
     count++;
     cout << "Solution " << count << ": ";
     for (int i = 1; i \le n; i++)
       cout << "(" << i << "," << board[i] << ") ";
     cout << endl;</pre>
     return;
  for (int col = 1; col \leq n; col++) {
     if (isSafe(row, col, n)) \{
       board[row] = col;
       solveNQueens(row + 1, n);
     }
  }}
```

```
int main() {
  int n;
  cout << "Enter value of N (size of board): ";
  cin >> n;
  if (n < 1 || n > MAX) {
    cout << "Invalid board size. Use N between 1 and " << MAX << ".\n";
    return 0;
  }
  solveNQueens(1, n);
  if (count == 0)
    cout << "No solution exists for N = " << n << endl;
  else
    cout << "Total solutions: " << count << endl;
  return 0;
}</pre>
```

```
Enter value of N (size of board): 4
Solution 1: (1,2) (2,4) (3,1) (4,3)
Solution 2: (1,3) (2,1) (3,4) (4,2)
Total solutions: 2

Process exited after 1.589 seconds with return value 0
Press any key to continue . . .
```

b)Write a program for Graph Coloring using backtracking.

```
#include <iostream>
using namespace std;
#define MAX 20
int graph[MAX][MAX]; // Adjacency matrix
int color[MAX]; // Color assigned to each vertex
int V, M;
                // V = number of vertices, M = number of colors
// Check if the current color assignment is safe
bool isSafe(int v, int c) {
  for (int i = 0; i < V; i++) {
     if (graph[v][i] == 1 \&\& color[i] == c)
       return false;
  }
  return true;
}
// Backtracking function to assign colors
bool graphColoring(int v) {
  if (v == V) // All vertices are assigned
     return true;
  for (int c = 1; c \le M; c++) {
     if (isSafe(v, c)) {
       color[v] = c;
       if (graphColoring(v + 1))
          return true;
       // Backtrack
       color[v] = 0;
     }
  }
  return false;
}
int main() {
  cout << "Enter number of vertices: ";</pre>
  cin >> V;
```

```
cout << "Enter number of colors: ";</pre>
cin >> M;
cout << "Enter adjacency matrix (" << V << "x" << V << "):\n";
for (int i = 0; i < V; i++)
  for (int j = 0; j < V; j++)
     cin >> graph[i][j];
for (int i = 0; i < V; i++)
  color[i] = 0; // Initialize all colors to 0
if \ (graphColoring(0)) \ \{\\
  cout << "Solution Exists. Assigned colors:\n";</pre>
  for (int i = 0; i < V; i++)
     cout << "Vertex " << i << " --> Color " << color[i] << endl;
} else {
  cout << "No solution exists with " << M << " colors.\n";
}
return 0;}
```