

# Exercise Computational Learning Theory: Boosting

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**a.**

Let  $x \geq 0$ . then  $e^{-x} \geq (1 - x)$ .

**Proof:**

Note that  $e^{-x} \geq 0$  and  $e^0 = 1$ , so that the result is trivial for  $x \geq 1$  and  $x = 0$ . We assume  $x \in (0, 1)$ . Then we have, using the series representation of  $e^{-x}$ :

$$\begin{aligned} e^{-x} - (1 - x) &= \sum_{n=0}^{\infty} \frac{(-x)^n}{n!} - (1 - x) \\ &= \sum_{n=2}^{\infty} \frac{(-x)^n}{n!} \\ &= \sum_{n=1}^{\infty} \frac{x^{2n}}{(2n)!} - \frac{(x)^{2n+1}}{(2n+1)!} \\ &= \sum_{n=1}^{\infty} \frac{x^{2n}}{(2n)!} \left( 1 - \frac{x}{2n+1} \right) \\ &\geq 0 \end{aligned}$$

Where in the last step it was used that each term of the sum is positive.