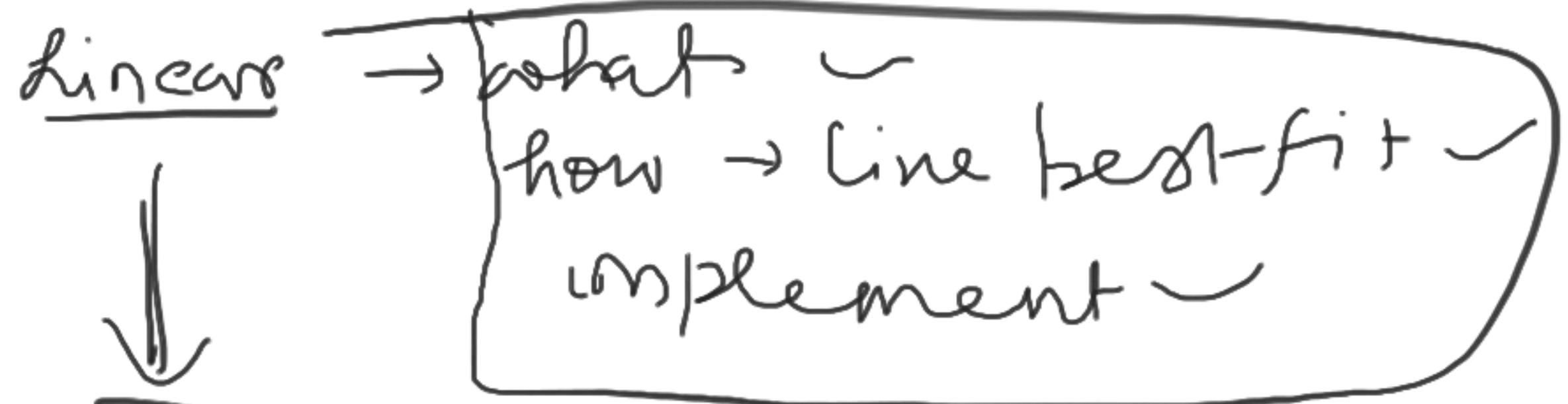


# → Logistic Regression

## Agenda



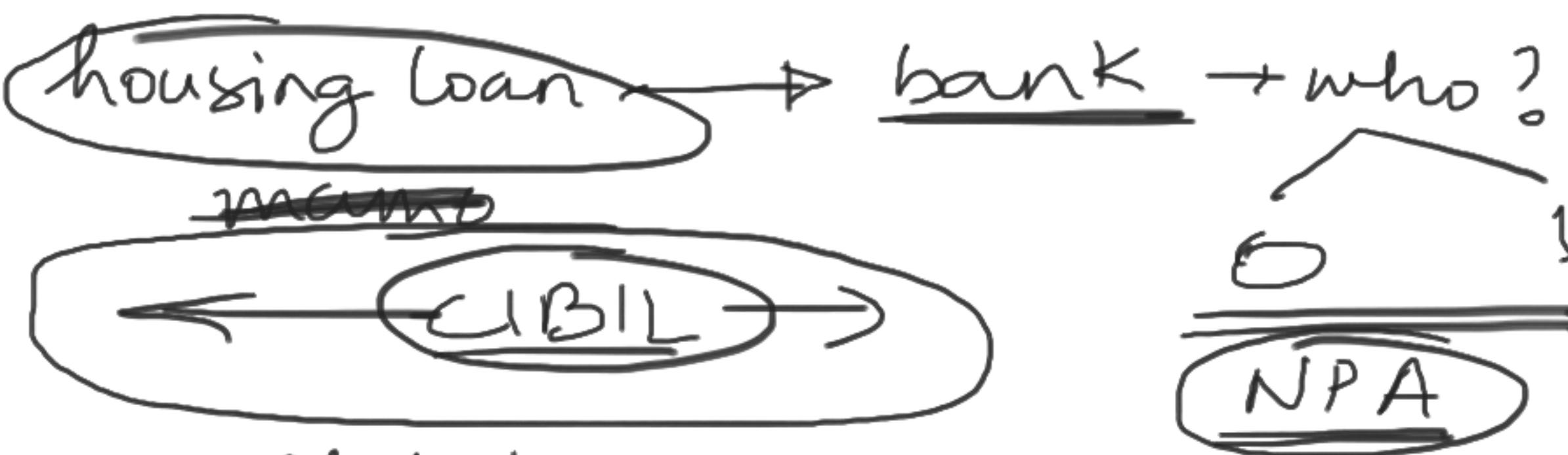
logistic → analogous

- ↳ ↗
- ↳ ↗

image → truck, cars —

Reg cont	Class <u>discrete</u> ↓ <u>binary</u>
	<del>3 classes</del>
	<del>weak</del>
	<u>Labels</u>
	<u>target</u>
	→ <u>0 or 1</u>
	<u>doubt/clear</u>

use-case?



SB → ~~SR~~

what has user  
history →



cont-

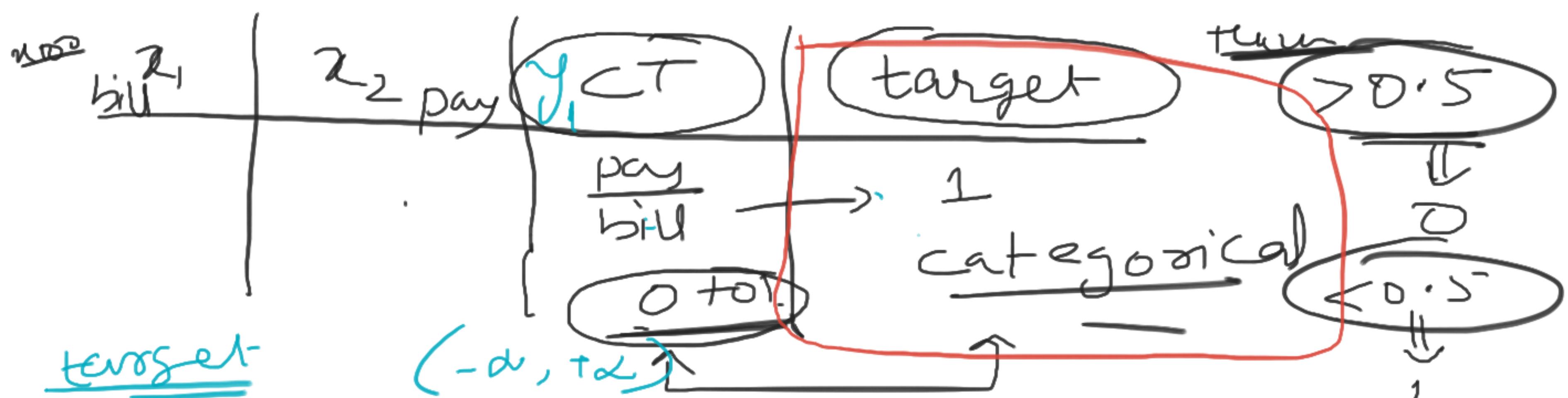
categorical

credit → Month

pay

pay  
bill

history repeat  
itself  
target  
o ✓  
o  
→ def  
o  
|  
analogous



target

CT

Linear reg

$\boxed{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_{100} x_{100}$

$\downarrow$  transform  
categorical

C5

$$\text{Bob Fraud} = 0 \cdot 3 = P$$

~~out~~

$$NF = 0 \cdot 7 = 1 - P$$

~~linear~~  $z = \sum_{i=0}^n \beta_i x_i$   $\rightarrow$  ~~sigmoid f^n~~  $\ell_0 = 1$

$$\text{Bob} \rightarrow y = \frac{1}{1 + e^{-z}}$$

$$z = -\alpha \text{ to } +\alpha$$

• class A →  $\frac{1}{1 + e^{-\alpha}} = 0$

class B →  $\frac{1}{1 + e^{-\alpha}} = 1$

$$\log\left(\frac{P}{1-P}\right) = z$$

$$z \in \mathbb{R}$$

$$\frac{P}{1-P} = e^z$$

$$\Rightarrow \frac{1-P}{P} = e^{-z}$$

$$= \frac{1}{P} - 1 = e^{-z}$$

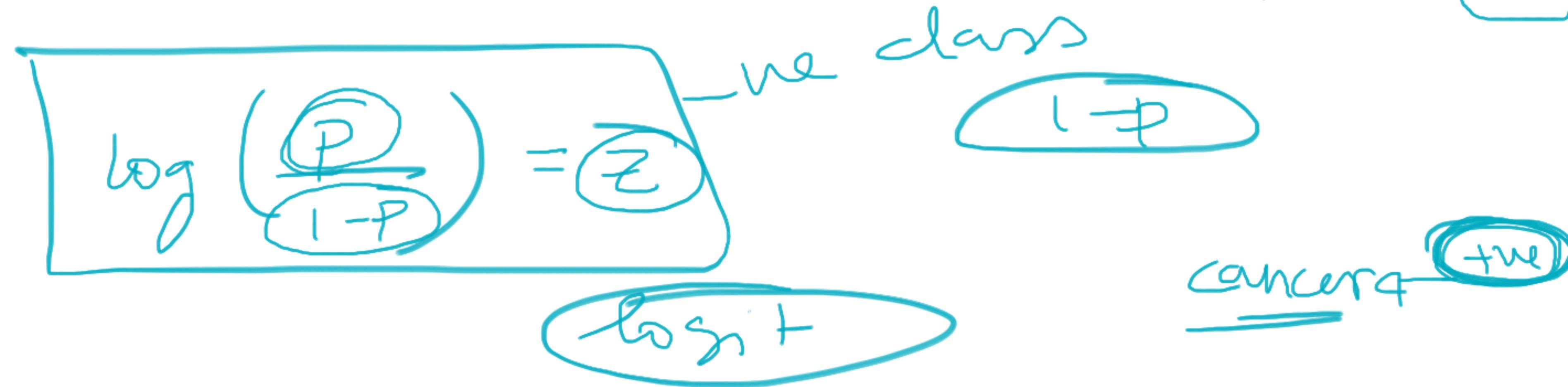
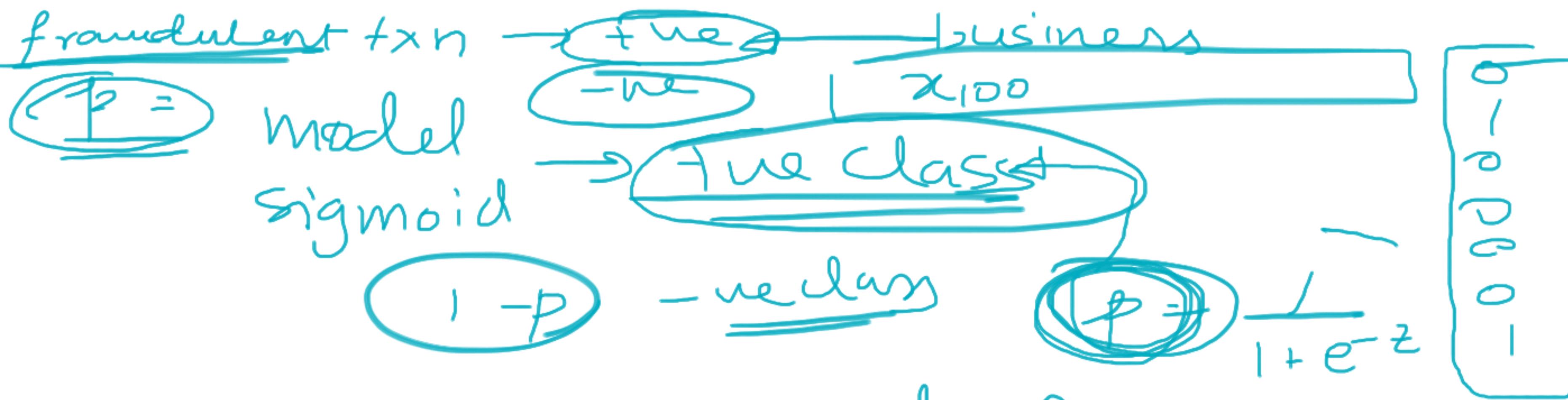
$$\frac{1}{1 + \frac{1}{e^z}}$$

$$\Rightarrow \frac{1}{P} = 1 + e^{-z}$$

$$\Rightarrow P =$$

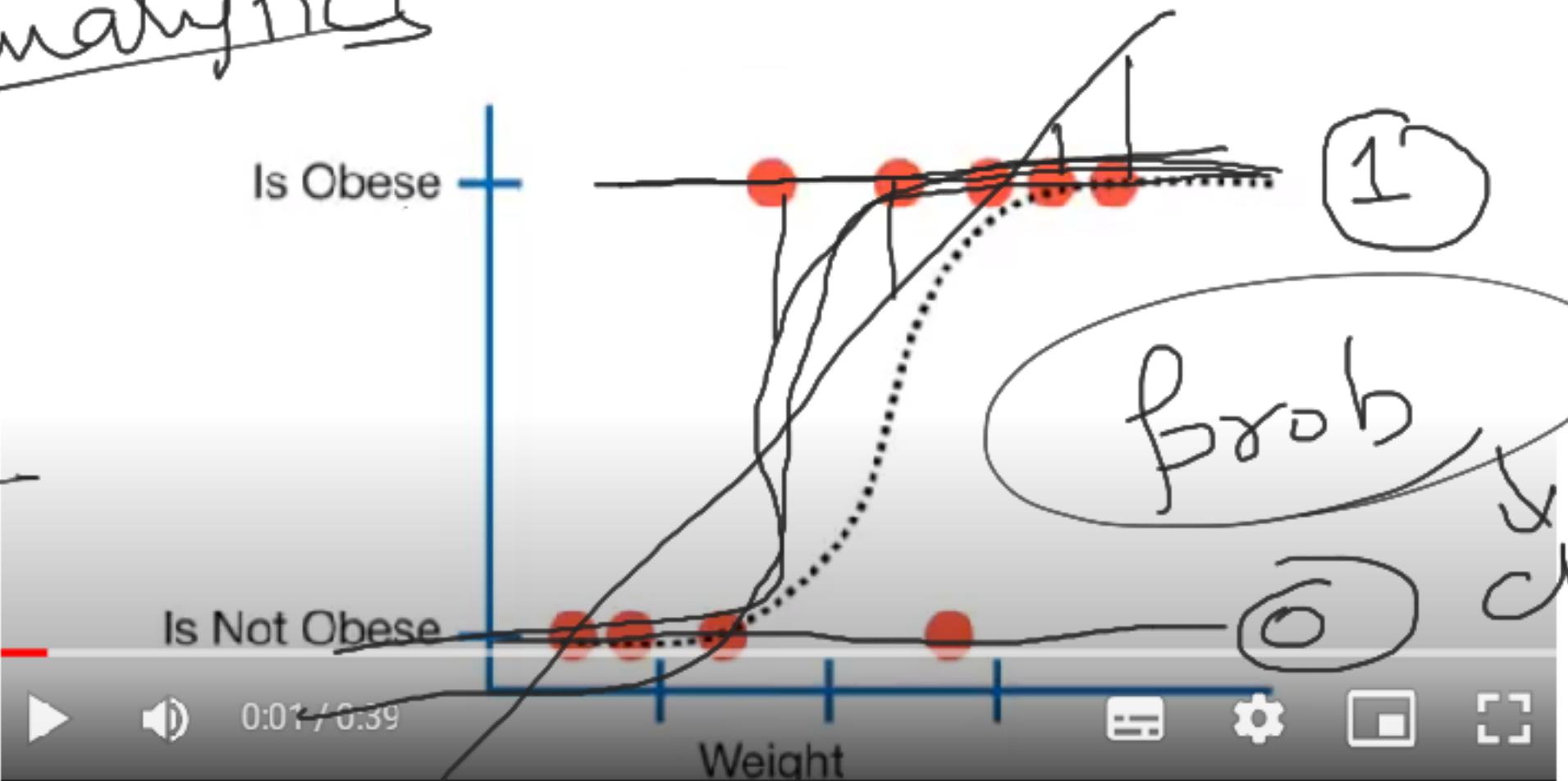
$$\frac{1}{1 + e^{-z}}$$

$$\frac{1}{1 + e^{-z}}$$



fraud analytics

~~conf 150~~



logistic  
Regression

1 → true class

$$Z = -\alpha, \alpha$$

$$\frac{1}{1 + e^{-Z}}$$

$$\hat{y} = \frac{1}{1 + e^{-Z}}$$

$$\hat{y} = \frac{1}{1 + e^{-\alpha}} = 1$$

Linear reg

Sigmoid

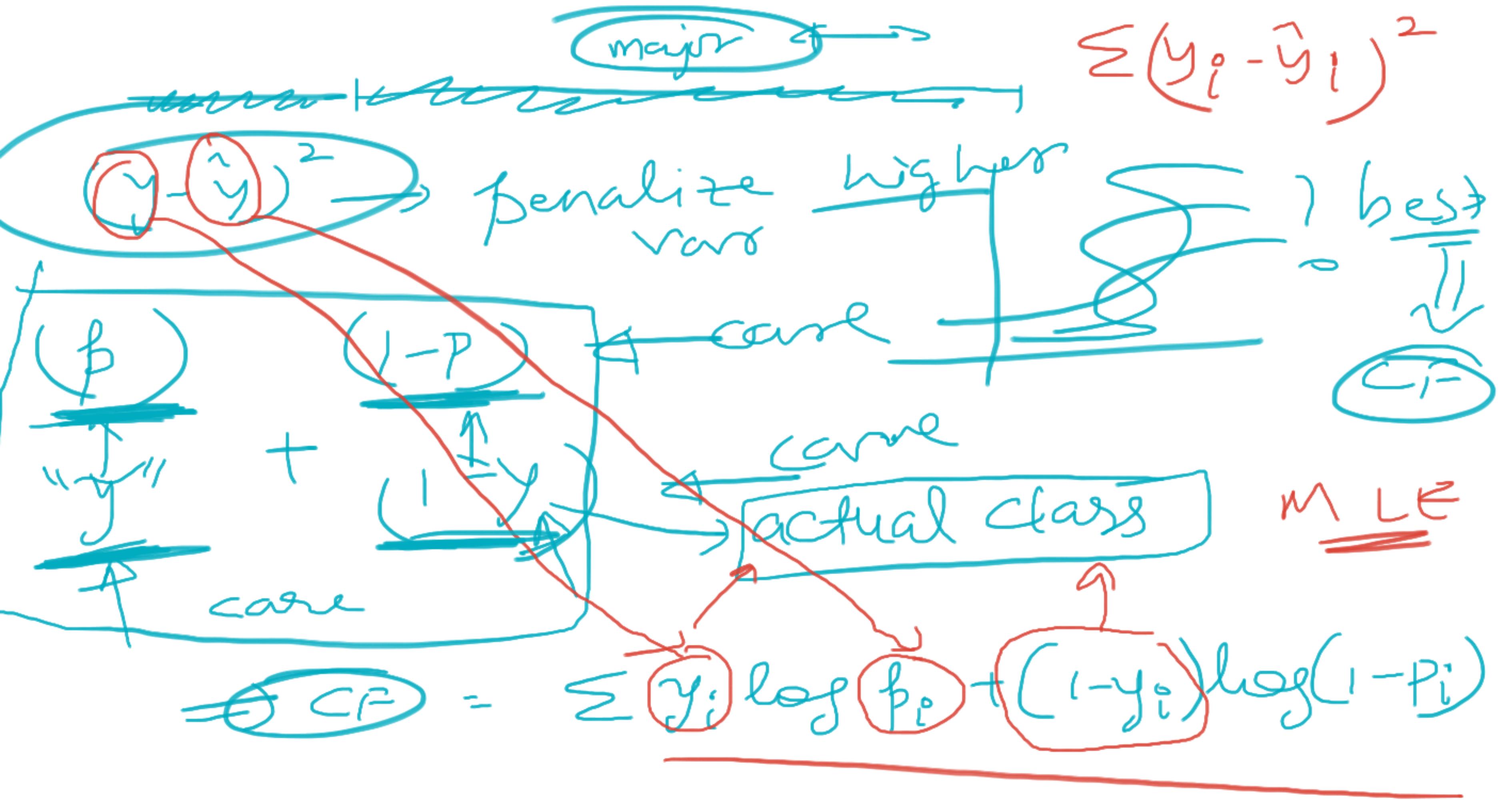
$$Z = \sum w_i x_i \rightarrow \text{linear reg}$$

$$(0, 1)$$

$$Z = \alpha$$

$$Z = -\alpha$$

$$\begin{pmatrix} 0 & 5 \\ 0 & 5 \end{pmatrix}$$



$$\text{cost}_F = \sum_i [y_i \log p_i + (1-y_i) \log(1-p_i)]$$

$y_i$

$p_i$

$\beta_i$

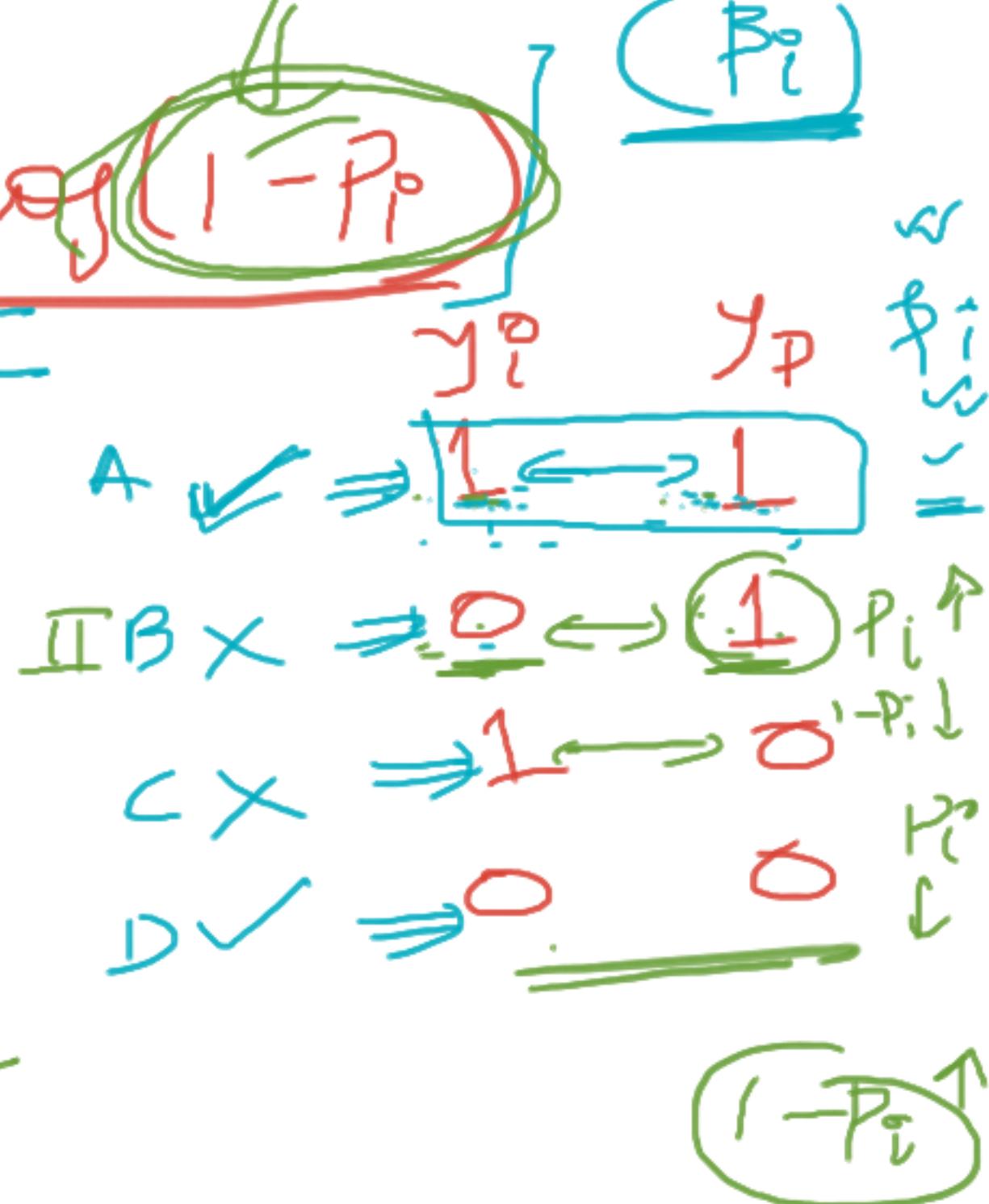
$\downarrow$   $y_i = \begin{cases} 1 & \text{if } p_i > 0.5 \\ 0 & \text{otherwise} \end{cases}$

A → more -ve → good < 0

D → more -ve → good < 0

B → less -ve → penalizing < 0

C → less -ve → penalizing < 0



$$\ell(w) = \sum_{i=1}^N y_i \log(h_w(x_i)) + (1 - y_i) \log(1 - h_w(x_i))$$

$$\log\left(\frac{e^{-z}}{1+e^{-z}}\right)$$

$$= \sum_{i=1}^N y_i \log\left(\frac{1}{1 + e^{-w^T x_i}}\right) + (1 - y_i) \log\left(\frac{e^{-w^T x_i}}{1 + e^{-w^T x_i}}\right)$$

$$\log e^{-z} - \log(1 + e^{-z})$$

$$= \sum_{i=1}^N -y_i \log(1 + e^{-w^T x_i}) + (1 - y_i) \left( -w^T x_i - \log(1 + e^{-w^T x_i}) \right)$$

$$= \boxed{\sum_{i=1}^N (y_i - 1)(w^T x_i) - \log(1 + e^{-w^T x_i})}$$

$(y_i - 1)z - \log(1 + e^{-z})$

$$w_i^o = w_p + \alpha \frac{\partial L}{\partial w_i^o}$$

$$Z = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$

$$\xrightarrow{\quad} \beta_0 + \frac{1}{\epsilon e^{\epsilon}}$$

$$\frac{\partial \ell(w)}{\partial w_j} = \sum_{i=1}^N(x_{ij})\left(y_i - \frac{1}{1+e^{-w^Tx_i}}\right)$$

$$\sum_{i=1}^n\Big(\,y-\big(\,\beta_0+\beta_1x\big)\,\Big).x$$

~~60~~ 1000 80:20

train

test  
200

least error

train

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$

GD

fit (feature target)

parameters

pred (f-er)

linear

Logisit

$$y - \text{pred}$$

x-train

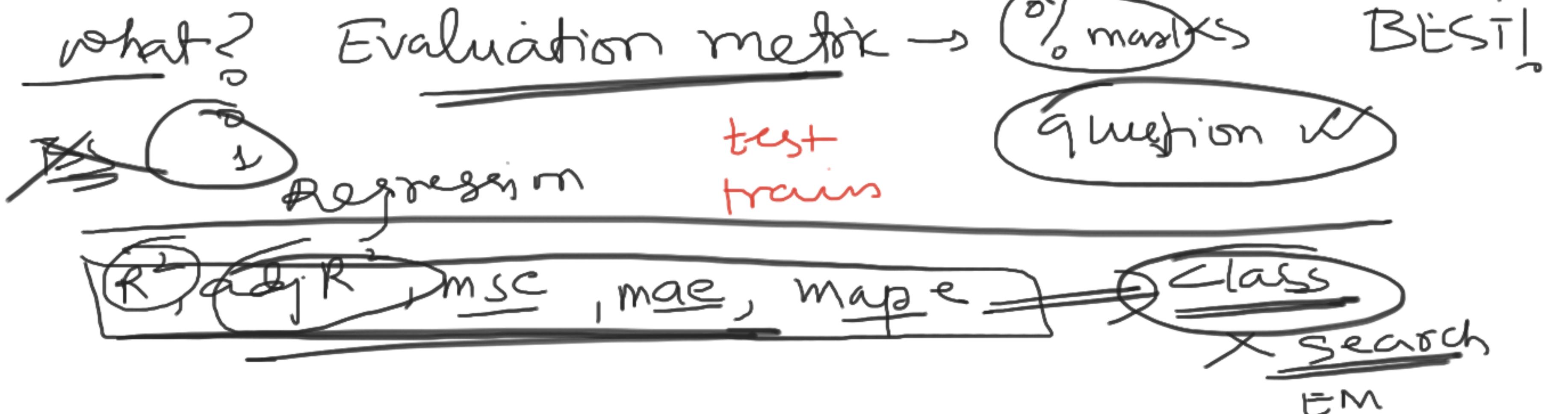
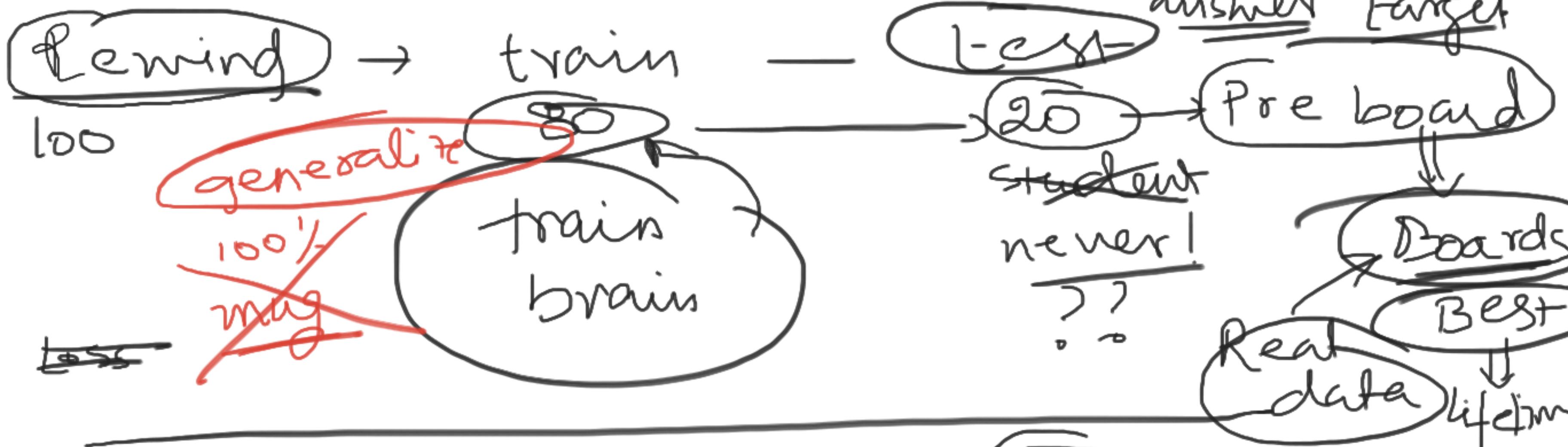
y-train

pred train

pred test

pred (x-train)  $\rightarrow$  brain trains

pred (x-test)  $\rightarrow$  pre

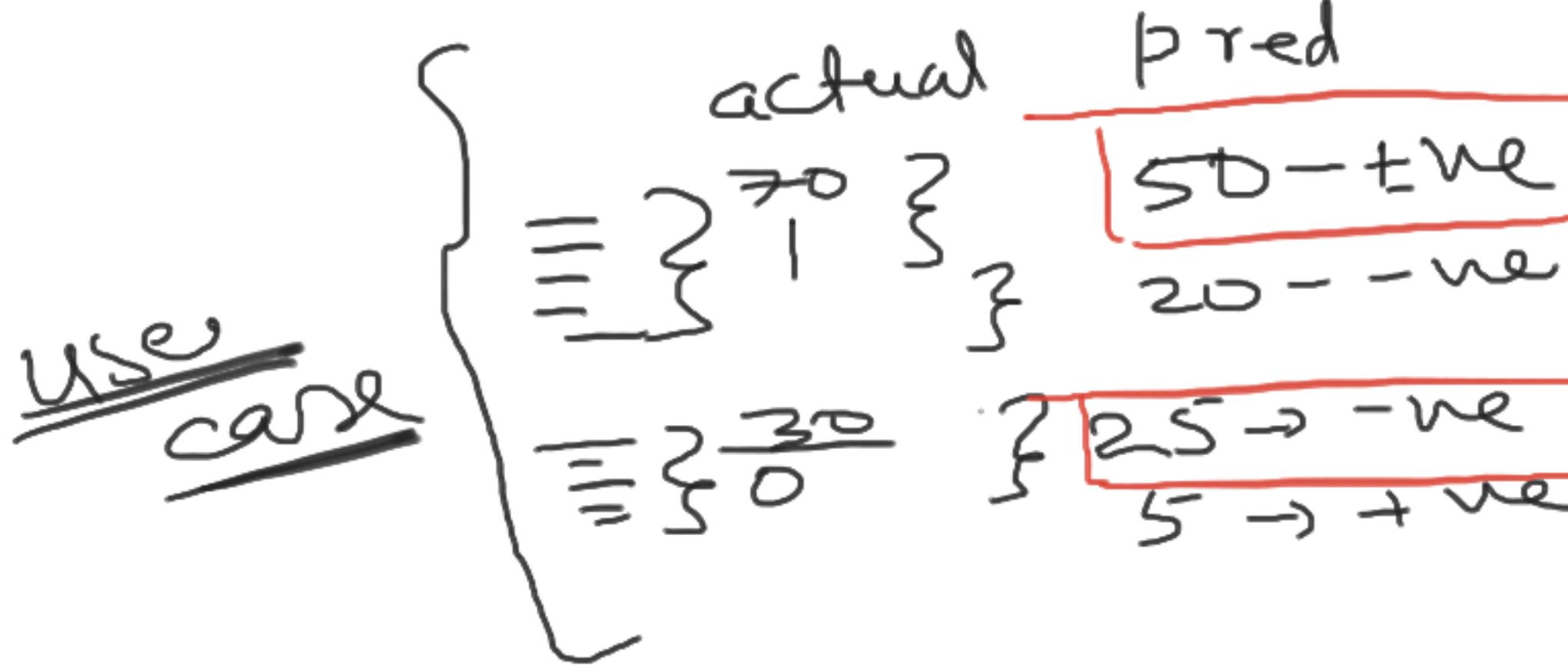


~~-ve  $\rightarrow$  0  
+ve  $\rightarrow$  1  
act pred~~

bias

	1	1 $\approx$ 50
50	1 $\times$	5
10	0 $\times$	20
50	0 $\approx$	25

$$= \{ 0\%, 0\%$$



accuracy  $\rightarrow$

$\frac{50 + 25}{100}$

Class  $\rightarrow$  0 | 1

Confusion

Predict +

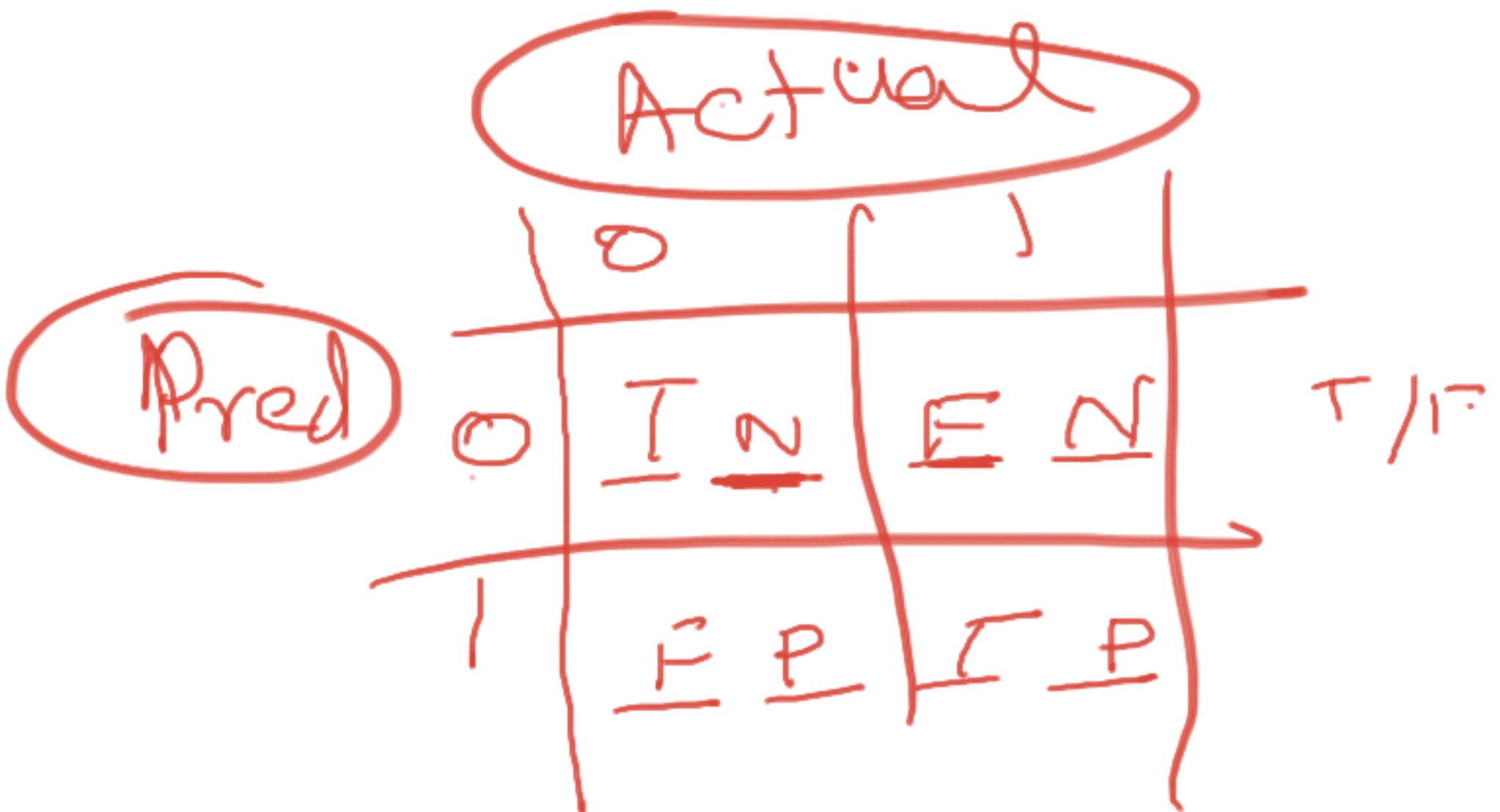
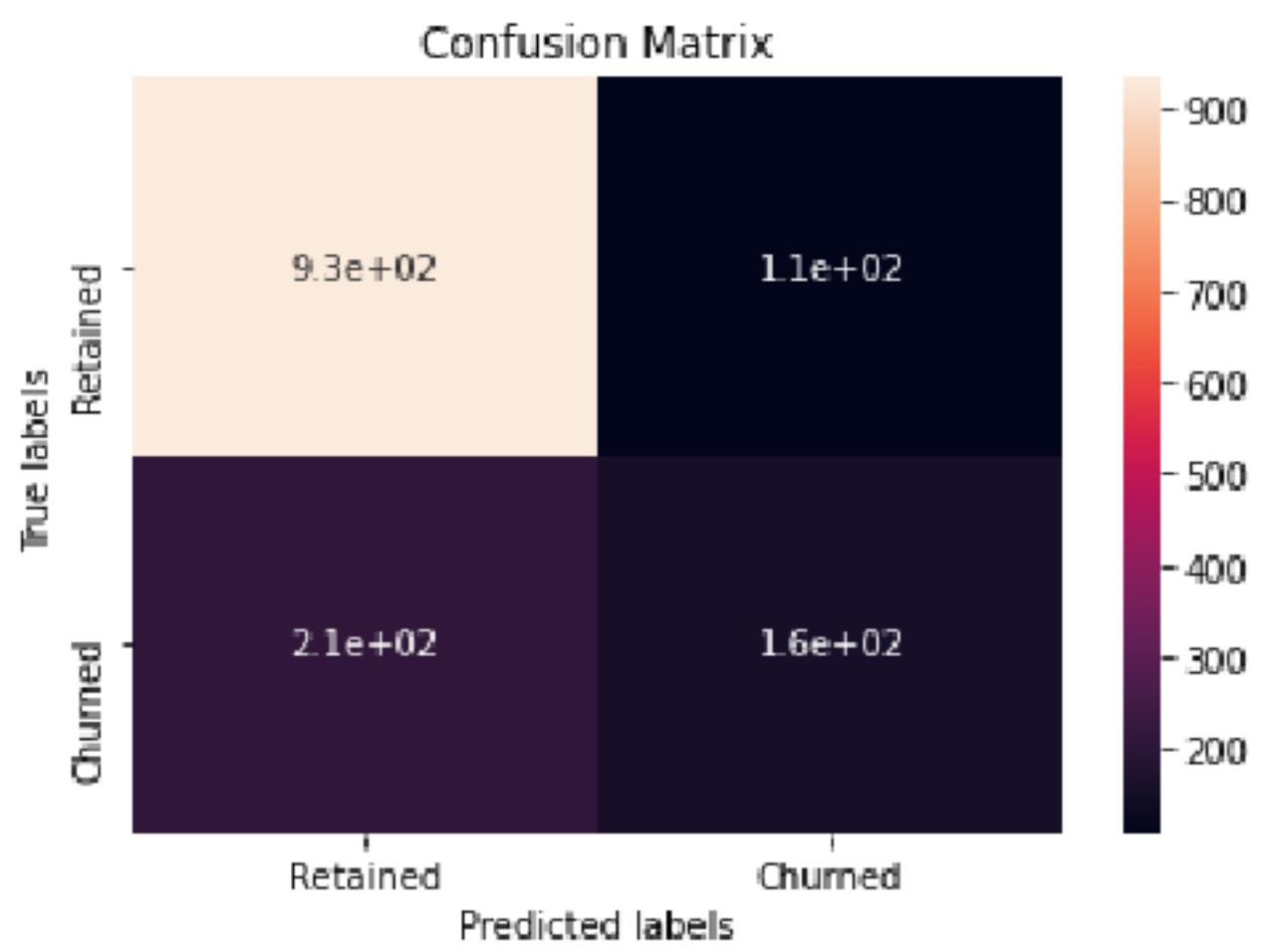
		Predicted 0	Predicted 1
		Actual 0	Actual 1
Actual 0	TN	FP	
Actual 1	FN	TP	

$$\frac{T/F}{4}$$

$$P/N$$

wrong  
Predicted class model  
+ve/-ve

$O \rightarrow -ve$



$$\text{Accuracy} = \frac{TN + TP}{TN + FP + FN}$$

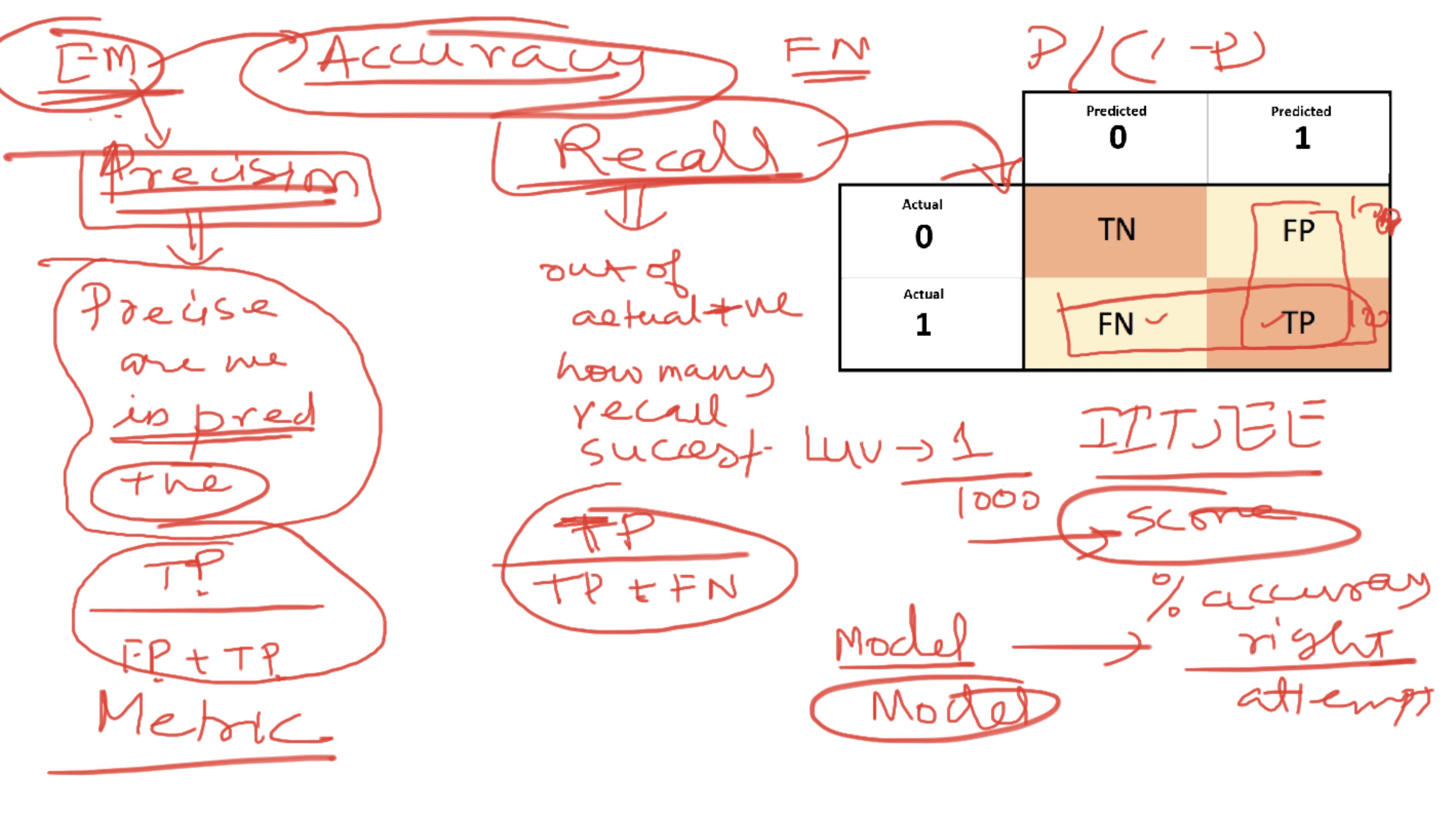
$\bar{r}$

$D_B$  pool

$\sqrt{\lambda}$

$\tau_F$

Pred





$P \downarrow$

$\uparrow$

P, R

Actual +ve class

		Predicted 0	Predicted 1
Actual	0 - ve	TN	FP
	1 + ve	FN	TP

Precision

$\downarrow$  train

↓ test

underfit

↑ train

↓ test

overfit

\* error

$$\frac{P+R}{2} = \frac{1}{P} + \frac{1}{R}$$

Recall =  $\frac{TP}{TP+FN}$

$FN + TP$

$$F1 = \frac{2PR}{P+R}$$