

$$\frac{\partial SSE}{\partial \beta_0} = \boxed{-2(y - \beta_0 - \beta_1 x) = 0} \quad \frac{\partial SSE}{\partial \beta_0} = \boxed{(y - \beta_0 - \beta_1 x)^2}$$

$$= 2(y - \beta_0 - \beta_1 x)$$

β_0 / β_1

$$\beta_0 = ?$$

$$f = \boxed{f(g(x))}$$

$$\beta_0, \beta_1 \rightarrow SSE \downarrow$$

$$\frac{\partial f}{\partial \beta_0} = \underline{y - \beta_0 - \beta_1 x} \quad \neq \underline{-1}$$

$$\frac{\partial SSE}{\partial \beta_1} = \boxed{-2x(y - \beta_0 - \beta_1 x) = 0}$$

$$\frac{\partial \text{const}}{\partial x} = n x^{n-1}$$

$$x^2 = 2x^{2-1}$$

$$\beta_0' = 1 \quad = \underline{\underline{2x}}$$

$$\frac{\partial SSE}{\partial \beta_0} = \text{eq 1} = 0 \quad \underline{\underline{2(y - \beta_0 - \beta_1 x) = 0}}$$

$$\frac{\partial SSE}{\partial \beta_1} = \text{eq 2} = 0 \Rightarrow \underline{\underline{2x(y - \beta_0 - \beta_1 x) = 0}}$$

$\beta_0 \& \beta_1$

$$\beta_0 + \beta_1 x = y$$

2 variable \rightarrow 150 variable \rightarrow 750

150 eqn ()

OLS

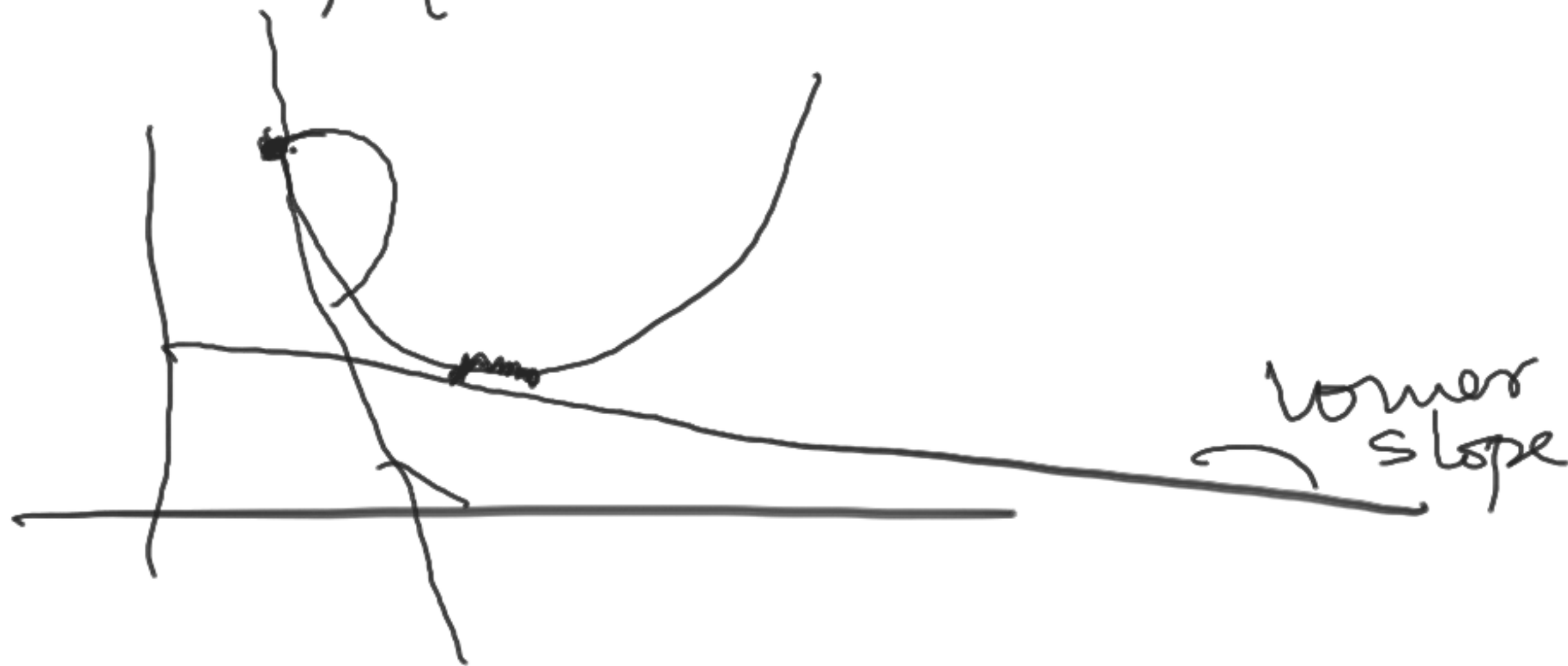
n
equ = Lgo \rightarrow $\beta_0 \beta_1 \dots \beta_m$

GD

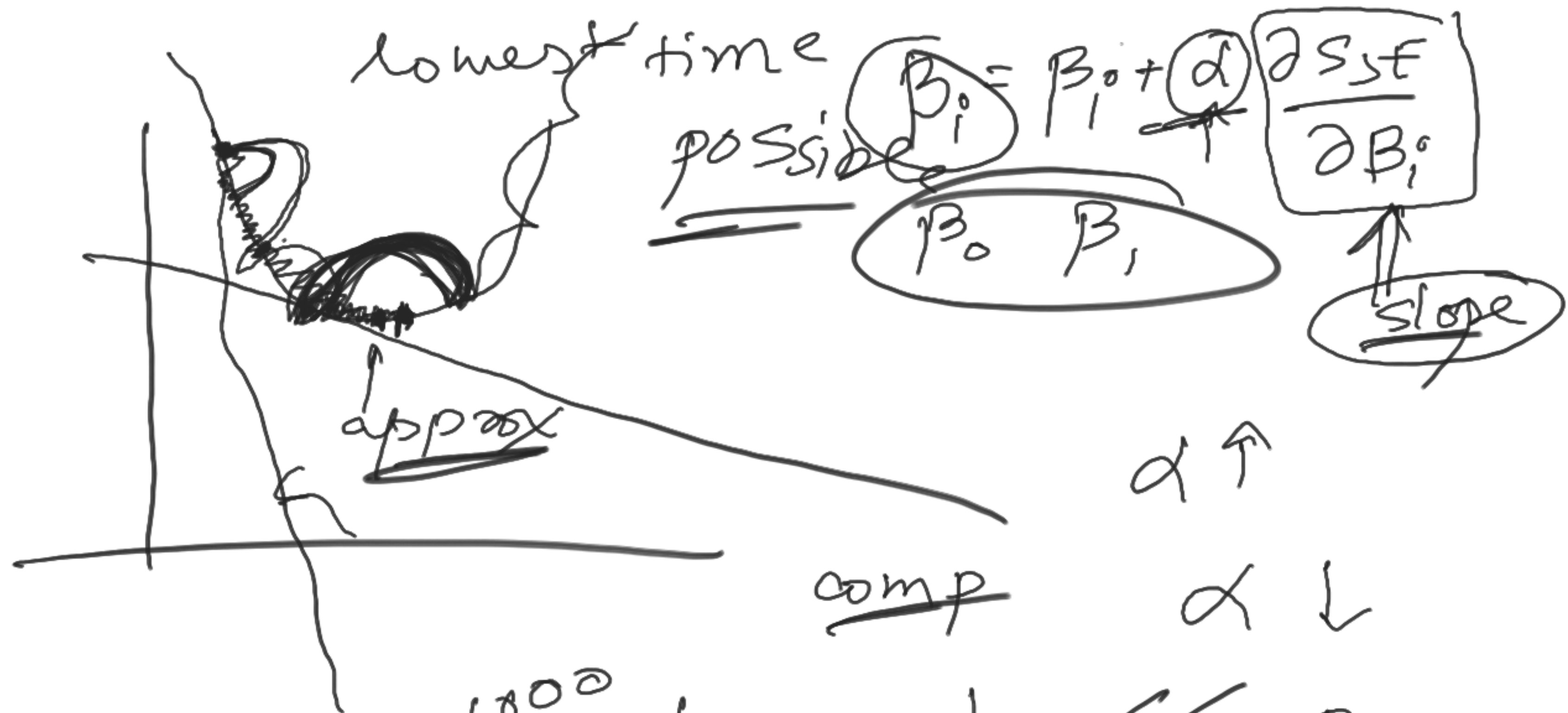
$\beta_i = \underline{\text{random}}$

iter = $\beta_i + \frac{2SSE}{n\beta_i}$

updating



$\frac{dy}{dx}$



iterations = 1000 elements ✓✓

~~if~~ $SSE_i - SSE_{i-1} < \epsilon$

~~hetero~~

p no.

errors can be model

Boosting

X_{boost}

$\epsilon_{error} = f(\sin)$

homosceda

linear

Algo \rightarrow Best outcome \rightarrow model
residual SS E linear

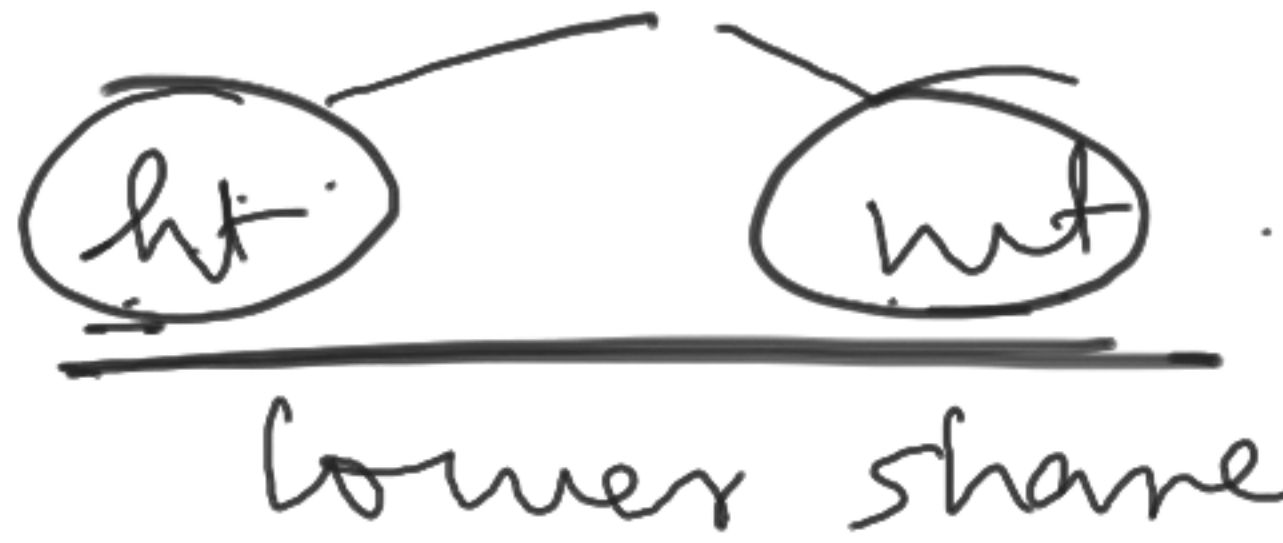
$$\sum (y - \hat{y})^2 =$$

$$\begin{pmatrix} 0 & 1 \\ 1/2 & 2 \\ \sqrt{2} & 2 \\ \sqrt{3} & 1 \\ 1 & 1 \\ \sqrt{3} & 0 \\ 2/3 & 0 \end{pmatrix}$$

$k_1 = 2/3$ $k_2 = 1$

Let's go

100%
 $y =$

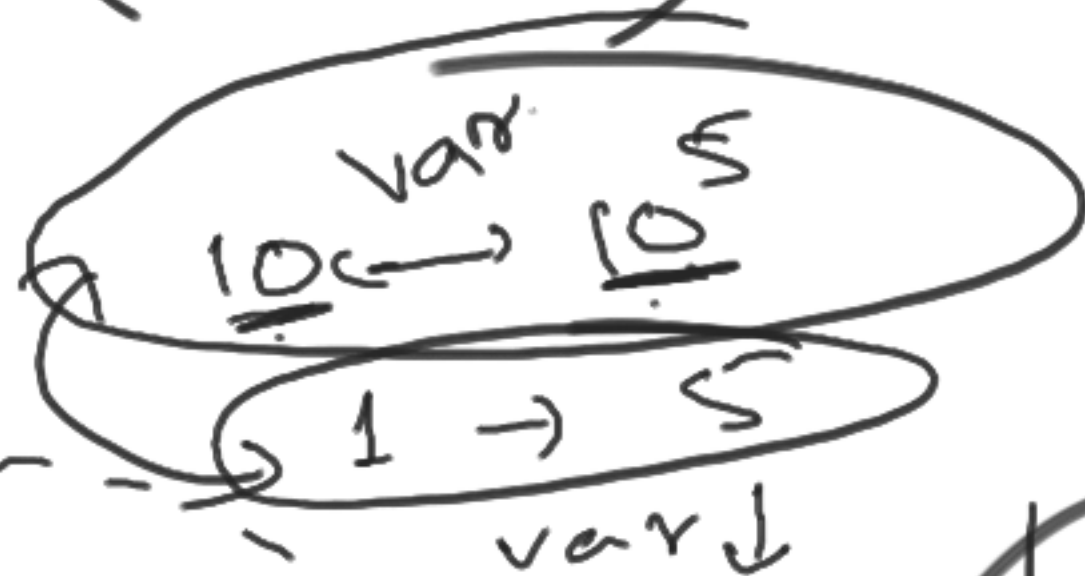


$\beta(M) = f(ht, wt)$
 Sharpe

$y = m_1 ht + m_2 wt + m_3 \frac{ht}{wt}$
 $= m_1 ht \left(1 + \frac{m_3}{m_1} \frac{1}{wt} \right)$

multicollinear \rightarrow 2 indep

sin (

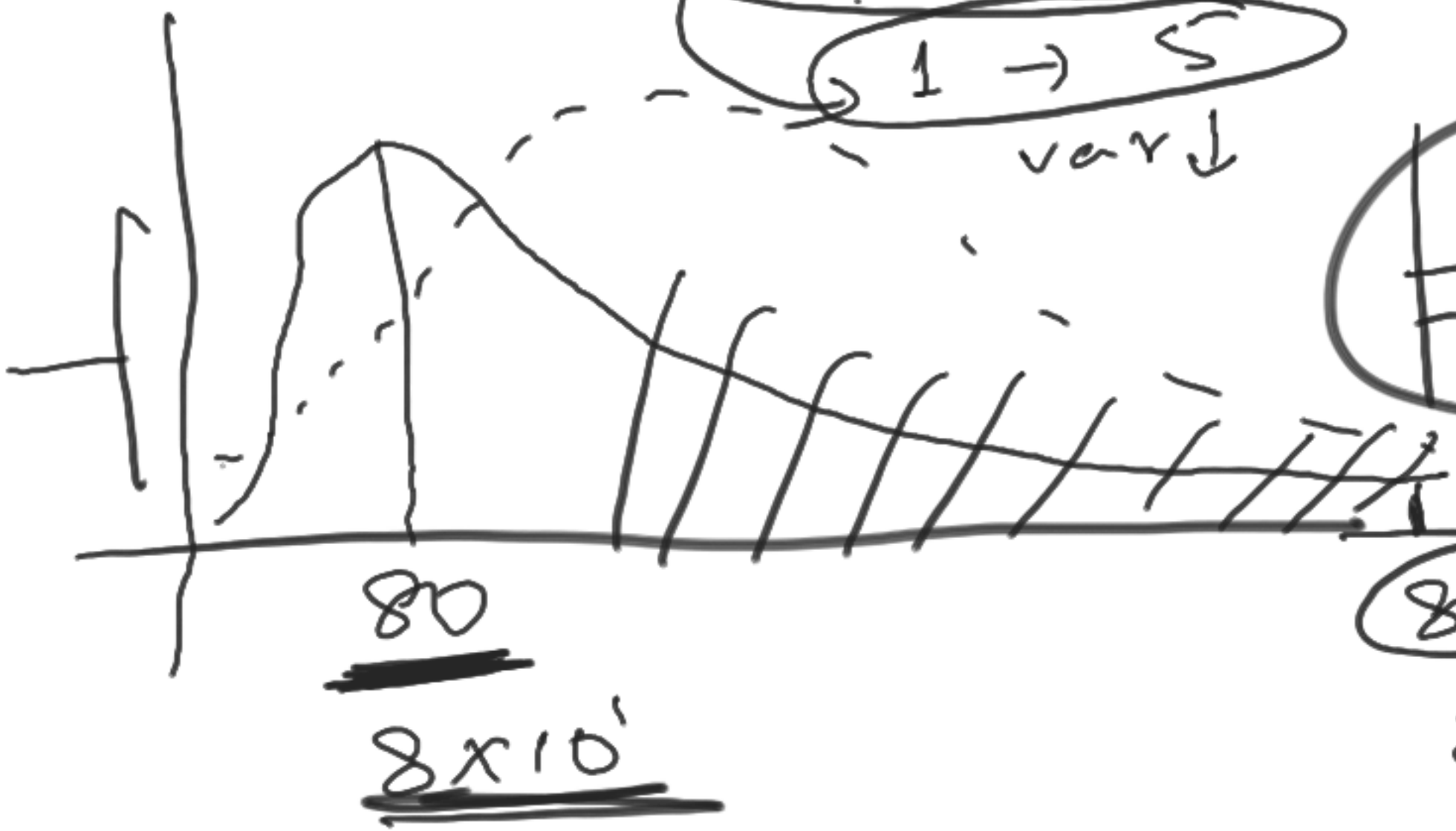


$$y = \beta_0 + \beta_1 x + \beta_2 x^2 + \beta_3 x^3$$

$$\log(x+1)$$

$$\log_{10} 10^5 = 5$$

$$\log_{10} 10 = 1$$



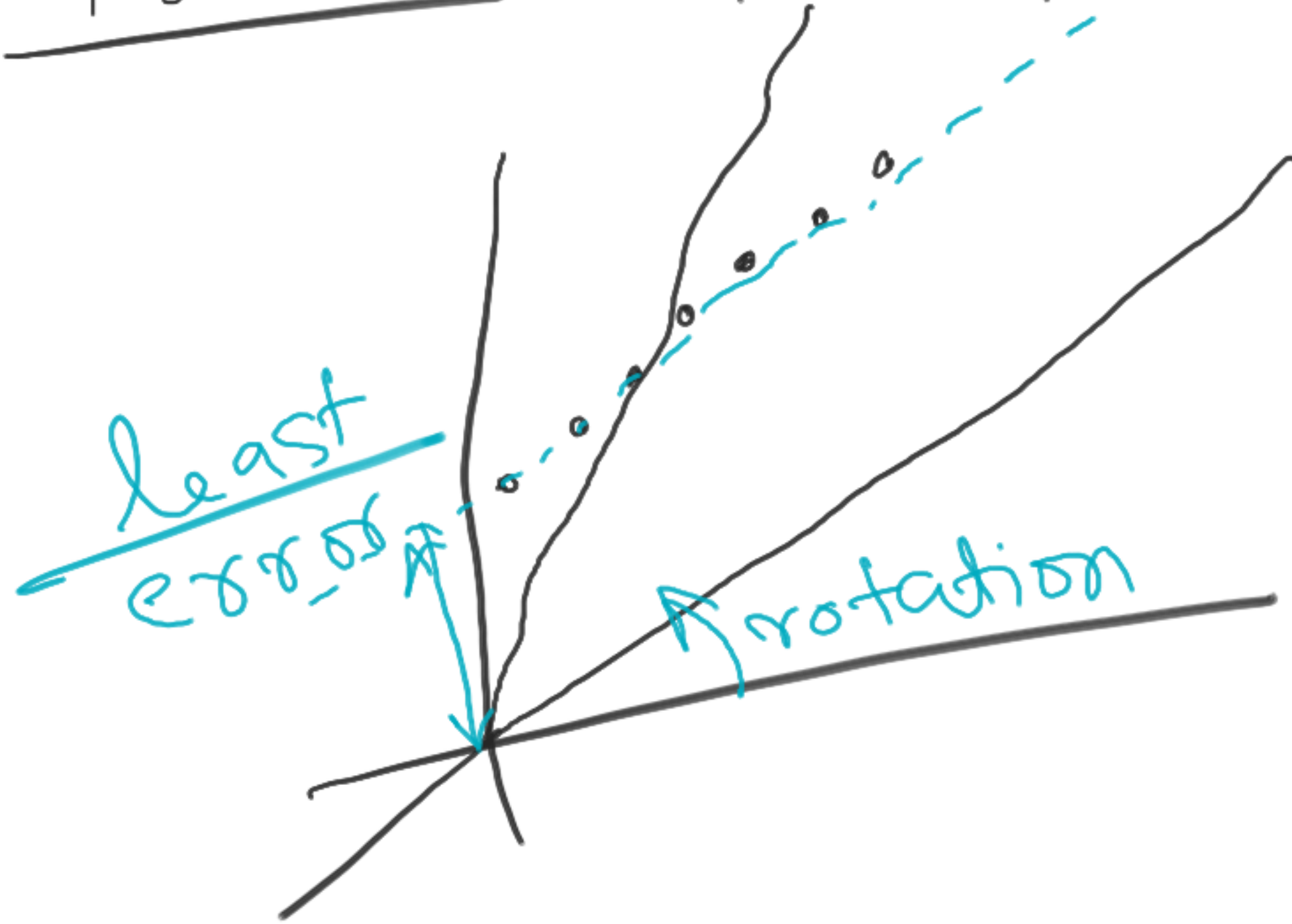
$$80,000$$

$$8 \times 10^4$$

Guided \leftrightarrow VIF

$\beta_0 = 0$ \rightarrow func passes through origin

$$\beta = 0$$



minimize error

salary
 $\hat{y} =$

$\hat{y} = \underline{\underline{B_0}} + \underbrace{\beta x_1}_{\substack{\text{projects} \\ \downarrow \\ \text{+ve}}} + \underbrace{\beta x_2}_{\substack{\text{-ve} \\ \uparrow \\ \text{complaints}}}$

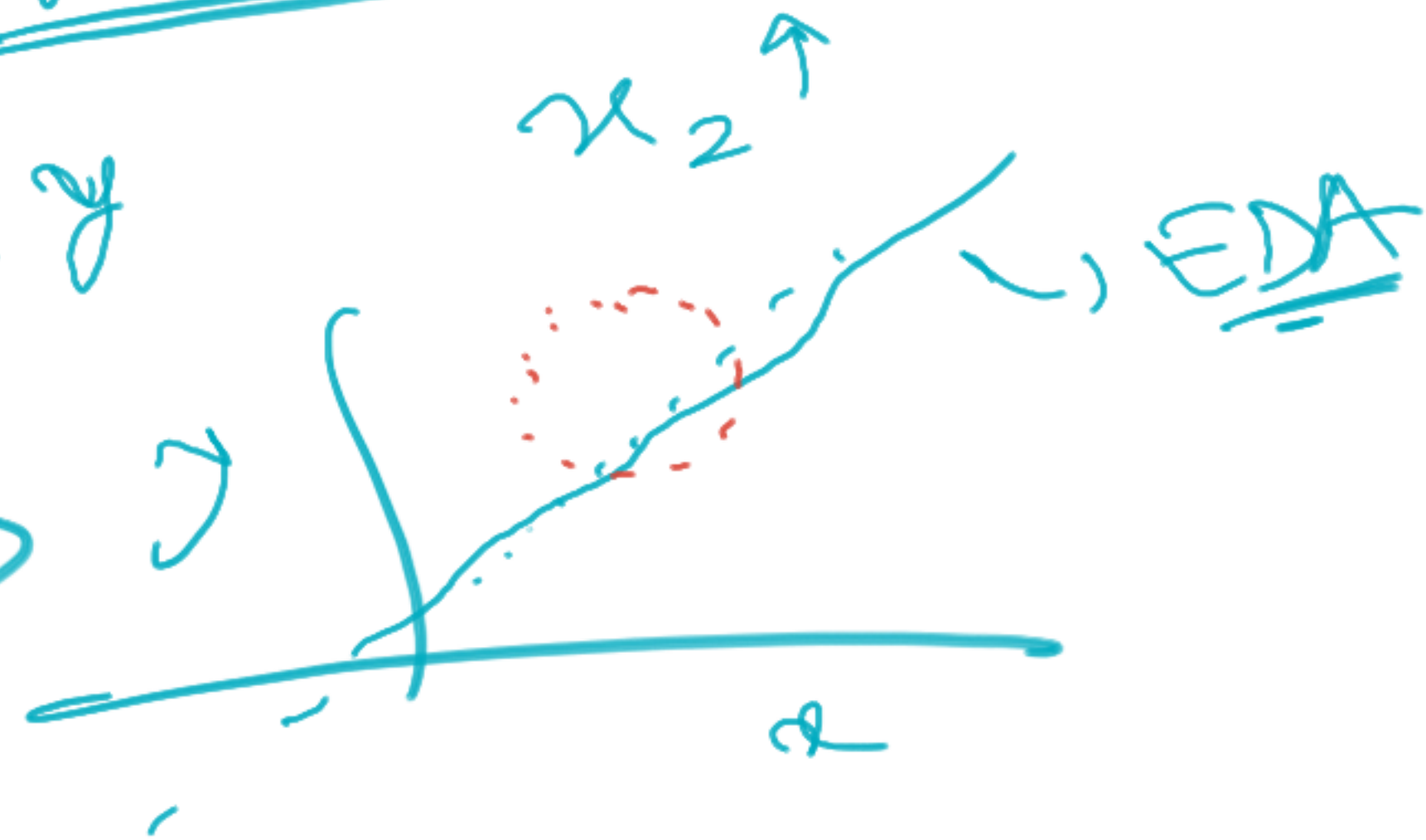
Base Salary

$\uparrow y \propto \uparrow$ \rightarrow +ve correla

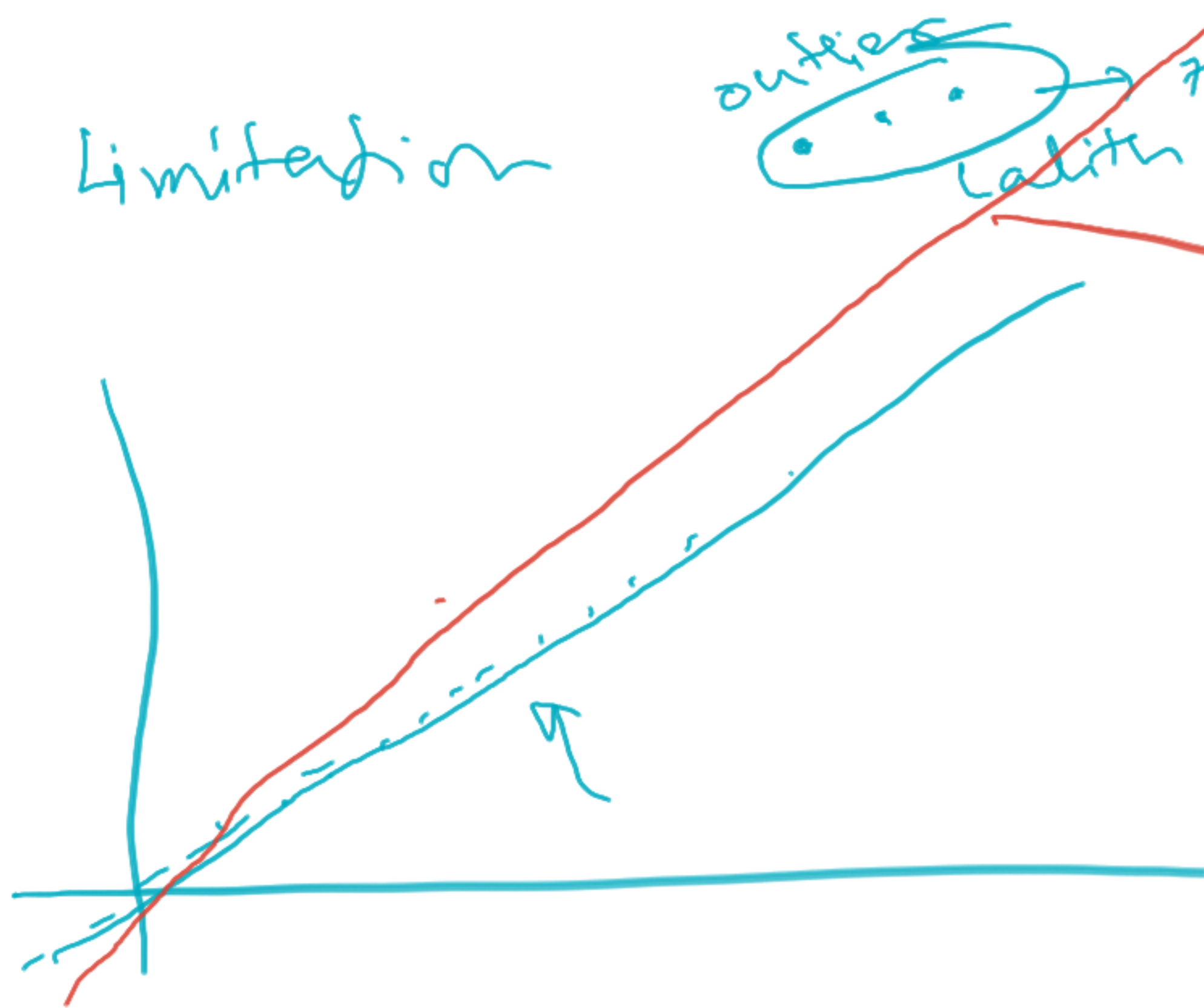


$\downarrow y$

y lin x



Limitation

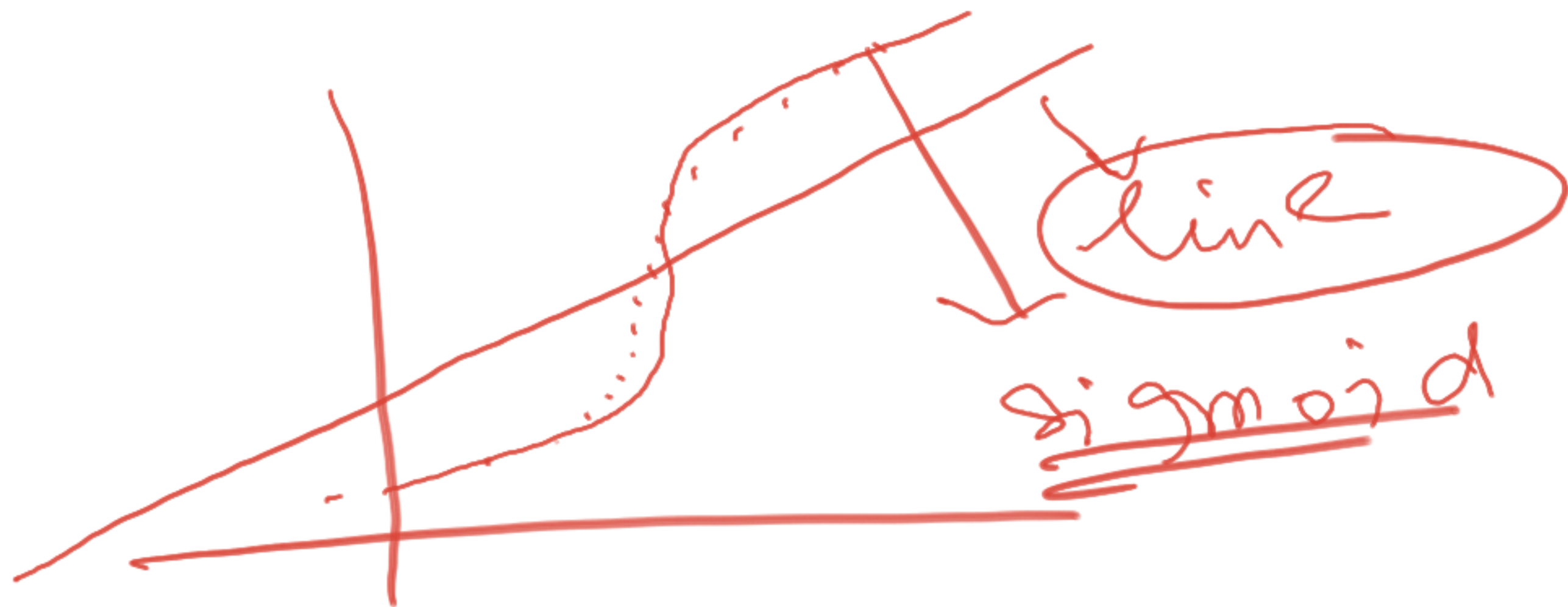


outliers
calith
topper,

minimize error

UR -> gone
outlier

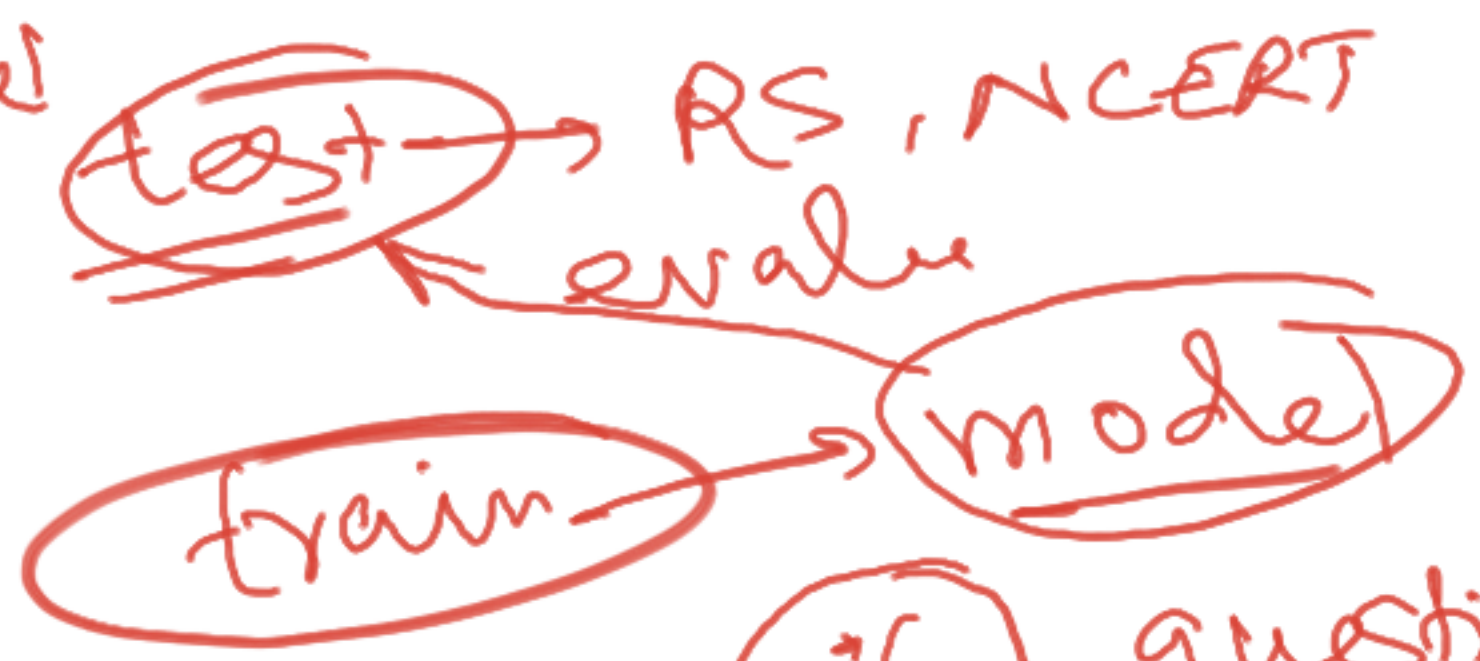
underfitting, small \rightarrow adapt



residual \rightarrow normally data



Evaluation Metric model

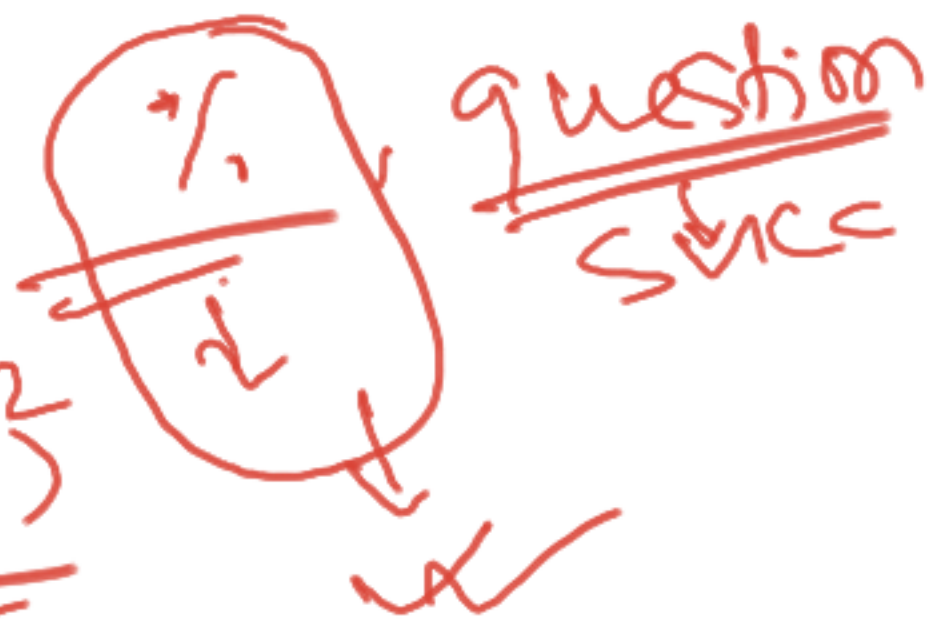


→ MSE, MAPE

RMS R^2

MAE

adj R^2



1

—
—
—
—
—

$$\frac{(y - \hat{y})^2}{n}$$

mean

$$\frac{1}{n} \sum (y - \hat{y})^2$$

R^2

$$\frac{MSE(\text{model})}{MSE(\text{no-brain})}$$

mod



y_1

y_2

y_3

y_4

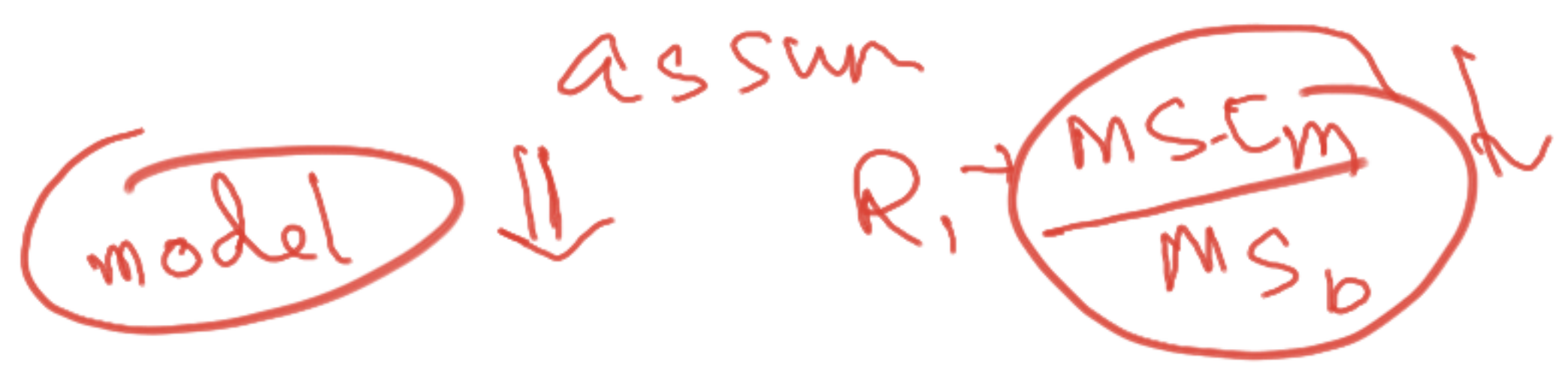
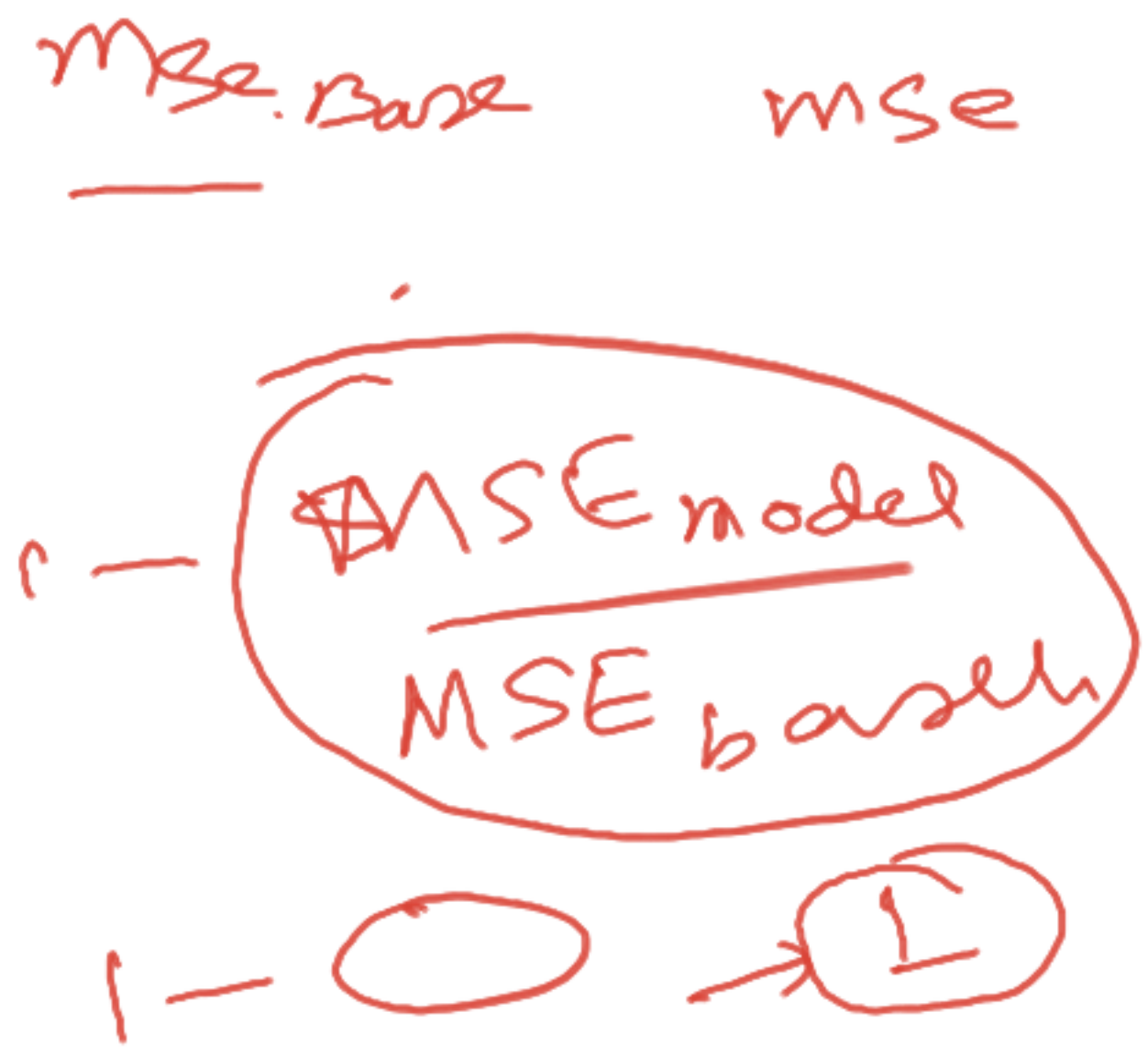
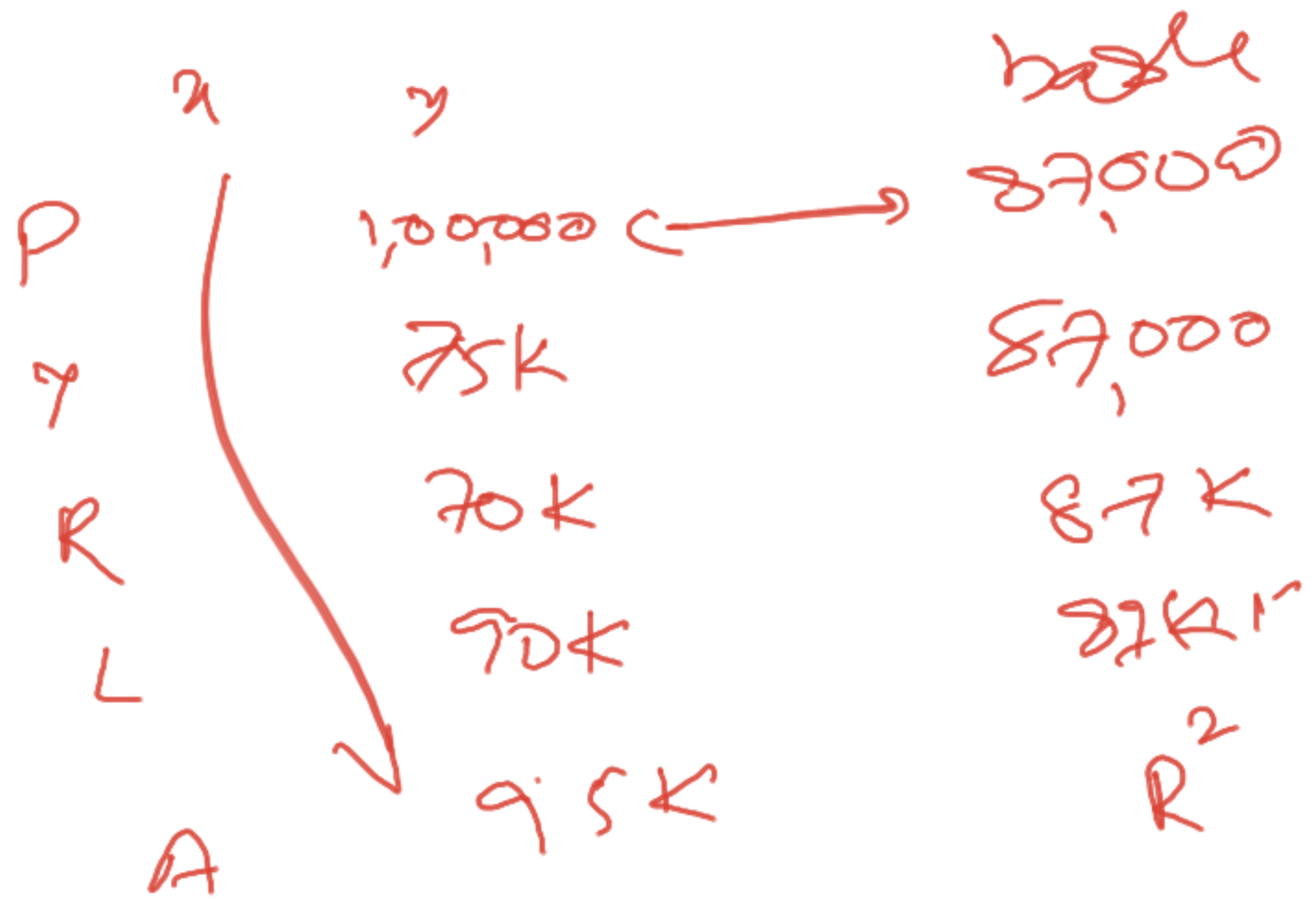
y_{mean}
 y_{mean}
 y_{mean}
 y_{mean}
 y_{mean}

MSE model

MSE_{nb}

better

MSE_m



10	8	2
9	8	1
8	8	0
7	8	-1
6	8	-2

Adj

$$\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \underbrace{\beta_3 x_3 + \beta_4 x_4}_{2 \text{ vars}}$$

$$\frac{\text{MSE}}{y - \hat{y}} \quad 1 - \frac{\text{MSE}_{\text{model}}}{\text{MSE}_{\text{base}}}$$

0.9

$$B_e = y - \hat{y}'$$
$$B = (y - \hat{y}) + (\hat{y} - \hat{y}')$$
$$\frac{\text{MSE}}{\text{MSE} - \text{MSE}'} \downarrow$$

10000 \rightarrow 10

0.92 \rightarrow 0.9

0.92 $R^2 \uparrow$

lot of info

MSE

RMSE

unit MSE $\rightarrow R^2$

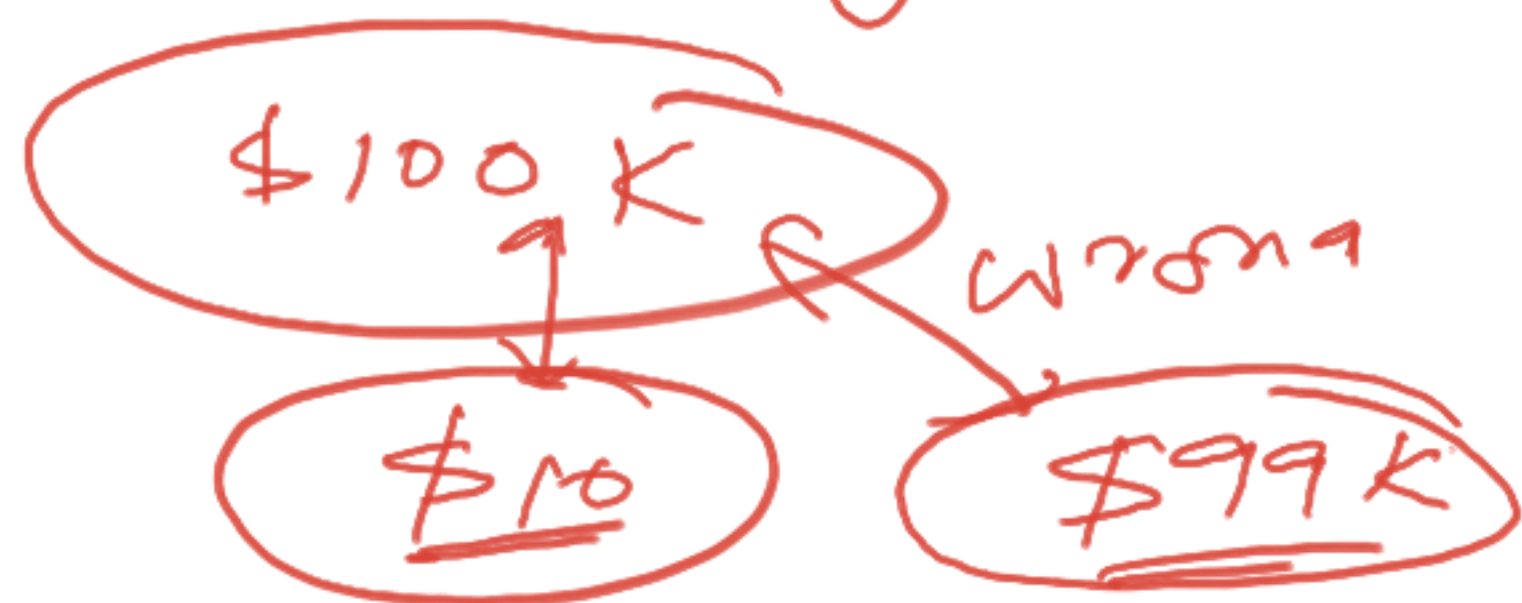
RMSE = RS

avg salary

$(5-2)^2$ - 9 more

$(5-1)^2$ - 16 error

penalize deviation



MAE MAPE

penalize → dev

↑↓

SEM

$$\text{Diff} \sqrt{\sum (y - \hat{y})^2}$$

avg

R^2 → goodness of fit

$$\frac{\text{AISE}_m}{\text{MSE}_b}$$

adj → model
complex