



AGH UNIVERSITY OF SCIENCE  
AND TECHNOLOGY

# Selected Topics in Cryptography

## Quantum cryptanalysis

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# Quantum crypanalysis

## Agenda

1. Bra-ket notation
2. Quantum gates
3. Grover's Database Search
4. Shore's factorization algorithm
  - Fast modular exponentiation
  - Quantum Fourier Transform

# Bra-ket notation

## Origins

Bra-ket notation:  $\langle x|y \rangle$  is a standard notation for describing quantum states. It can also be used to denote abstract vectors, linear functionals and scalar product in mathematics.

The left part:  $\langle x|$ , called the bra, is a row vector.

The right part:  $|y \rangle$ , called the ket, is a column vector.

In quantum computing and specifically the quantum circuit model of computation, a quantum gate (or quantum logic gate) is a basic quantum circuit operating on a small number of qubits.

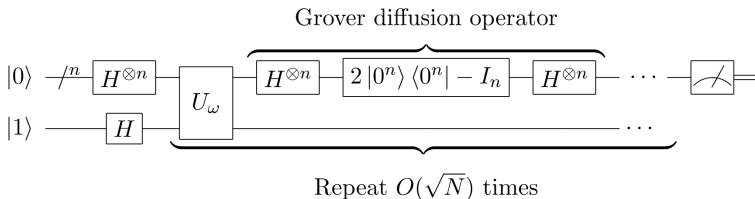
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## Fast database search

Grover's database search uses possibility to parallel process of qbit. The algorithm allows us to find selected element in unsorted set. Complexity  $\sqrt{n}$

# Advanced Encryption Standard

## Overview of AES



# Advanced Encryption Standard

## 3.MixColumns

Each column is represented as four-bytes vector.

Each column of State is replaced by a new column which is formed by multiplying that column by a certain matrix of elements of the field.

Together with ShiftRows, MixColumns provides *diffusion* in the cipher.

MixColumns step is used in every cycle **except** the last one cycle.

# Advanced Encryption Standard

## 3.MixColumns

It is also possible to see this operation as polynomial multiplication where each column is represented with polynomial  $a(x)$ :

$$a(x) = c(x).a(x) \bmod x^4 + 1 =$$

$$(03x^3 + 01x^2 + 01x + 02).(a_3x^3 + a_2x^2 + a_1x^1 + a_0) \bmod x^4 + 1$$

$$c(x) = \begin{bmatrix} 02 & 03 \\ 01 & 02 \end{bmatrix}$$



# Advanced Encryption Standard

## Key Schedule: Rcon Table

Rcon Constants			
Round	Constant(Rcon)	Round	Constant(Rcon)
1	01 00 00 00	6	20 00 00 00
2	02 00 00 00	7	40 00 00 00
3	04 00 00 00	8	80 00 00 00
4	08 00 00 00	9	1B 00 00 00
5	10 00 00 00	10	36 00 00 00

# Time for questions

### Bibliography:

- Joan Daemen, Vincent Rijmen, "The Design of Rijndael: AES – The Advanced Encryption Standard", Springer, 2002.
- Joshua Holden, "The Mathematics of Cryptography", Princeton University Press, 2017
- Federal Information Processing Standards Publication 197 : the official AES standard, United States National Institute of Standards and Technology, 2001
- Wikipedia, Advanced Encryption Standard,  
[https://en.wikipedia.org/wiki/Advanced\\_Encryption\\_Standard](https://en.wikipedia.org/wiki/Advanced_Encryption_Standard)

# Thank you for attention!