

$\lambda := \lambda;$
 $\epsilon := \epsilon;$
 $y := y;$
 $R := R;$
 $M := M;$

$\lambda := \lambda$

$\epsilon := \epsilon$

$y := y$

$R := R$

$M := M$

(1)

$$\begin{aligned}
 & H := \frac{15}{8} \cdot \frac{1}{M^3} \cdot \lambda \cdot \epsilon \cdot \left(\frac{r}{M} \right)^2 \cdot \left(1 - \frac{2 \cdot M}{r} \right) \cdot \left(- \frac{M \cdot (M-r) \cdot (2 \cdot M^2 + 6 \cdot M \cdot r - 3 \cdot r^2)}{r^2 \cdot (2 \cdot M - r)^2} + \frac{3}{2} \cdot \right. \\
 & \quad \left. \ln \left(\frac{r}{r - 2 \cdot M} \right) \right) + M^2 \cdot \epsilon \cdot \left(\frac{r}{M} \right)^2 \cdot \left(1 - \frac{2 \cdot M}{r} \right);
 \end{aligned}$$

$$\begin{aligned}
 H := & \frac{15}{8} \frac{\lambda \epsilon r^2 \left(1 - \frac{2 M}{r} \right) \left(- \frac{M (M-r) (2 M^2 + 6 M r - 3 r^2)}{r^2 (2 M-r)^2} + \frac{3}{2} \ln \left(\frac{r}{r-2 M} \right) \right)}{M^5} \\
 & + \epsilon r^2 \left(1 - \frac{2 M}{r} \right)
 \end{aligned}
 \tag{2}$$

$dH_dr := \text{diff}(H, r);$

$$\begin{aligned}
 dH_dr := & \frac{15}{4} \frac{\lambda \epsilon r \left(1 - \frac{2 M}{r} \right) \left(- \frac{M (M-r) (2 M^2 + 6 M r - 3 r^2)}{r^2 (2 M-r)^2} + \frac{3}{2} \ln \left(\frac{r}{r-2 M} \right) \right)}{M^5} \\
 & + \frac{15}{4} \frac{\lambda \epsilon \left(- \frac{M (M-r) (2 M^2 + 6 M r - 3 r^2)}{r^2 (2 M-r)^2} + \frac{3}{2} \ln \left(\frac{r}{r-2 M} \right) \right)}{M^4} \\
 & + \frac{15}{8} \frac{1}{M^5} \left(\lambda \epsilon r^2 \left(1 - \frac{2 M}{r} \right) \left(\frac{M (2 M^2 + 6 M r - 3 r^2)}{r^2 (2 M-r)^2} - \frac{M (M-r) (6 M - 6 r)}{r^2 (2 M-r)^2} \right. \right. \\
 & + \frac{2 M (M-r) (2 M^2 + 6 M r - 3 r^2)}{r^3 (2 M-r)^2} - \frac{2 M (M-r) (2 M^2 + 6 M r - 3 r^2)}{r^2 (2 M-r)^3} \\
 & \left. \left. + \frac{3}{2} \frac{\left(\frac{1}{r-2 M} - \frac{r}{(r-2 M)^2} \right) (r-2 M)}{r} \right) \right) + 2 \epsilon r \left(1 - \frac{2 M}{r} \right) + 2 \epsilon M
 \end{aligned}
 \tag{3}$$

$H_R := \text{subs}(r=R, H);$

$H_R :=$

(4)

$$\frac{15}{8} \frac{\lambda \epsilon R^2 \left(1 - \frac{2 M}{R} \right) \left(- \frac{M (M-R) (2 M^2 + 6 M R - 3 R^2)}{R^2 (2 M-R)^2} + \frac{3}{2} \ln \left(\frac{R}{R-2 M} \right) \right)}{M^5}$$

$$+ \epsilon R^2 \left(1 - \frac{2M}{R} \right)$$

$$\begin{aligned} &> dH_{\bar{d}R} := \text{subs}(r=R, dH_{\bar{d}r}); \\ dH_{\bar{d}R} := \end{aligned}$$

(5)

$$\begin{aligned} & \frac{15}{4} \frac{\lambda \in R \left(1 - \frac{2M}{R} \right) \left(-\frac{M(M-R)(2M^2+6MR-3R^2)}{R^2(2M-R)^2} + \frac{3}{2} \ln\left(\frac{R}{R-2M}\right) \right)}{M^5} \\ & + \frac{15}{4} \frac{\lambda \in \left(-\frac{M(M-R)(2M^2+6MR-3R^2)}{R^2(2M-R)^2} + \frac{3}{2} \ln\left(\frac{R}{R-2M}\right) \right)}{M^4} \\ & + \frac{15}{8} \frac{1}{M^5} \left(\lambda \in R^2 \left(1 - \frac{2M}{R} \right) \left(\frac{M(2M^2+6MR-3R^2)}{R^2(2M-R)^2} \right. \right. \\ & \left. \left. - \frac{M(M-R)(6M-6R)}{R^2(2M-R)^2} + \frac{2M(M-R)(2M^2+6MR-3R^2)}{R^3(2M-R)^2} \right. \right. \\ & \left. \left. - \frac{2M(M-R)(2M^2+6MR-3R^2)}{R^2(2M-R)^3} \right. \right. \\ & \left. \left. + \frac{3}{2} \left(\frac{1}{R-2M} - \frac{R}{(R-2M)^2} \right) (R-2M) \right) \right) + 2 \epsilon R \left(1 - \frac{2M}{R} \right) + 2 \epsilon M \end{aligned}$$

$$\begin{aligned} &> eq := \frac{R \cdot dH_{\bar{d}R}}{H_{\bar{d}R}} = y; \\ eq := \end{aligned}$$

(6)

$$\begin{aligned} & \left(R \left(\frac{15}{4} \frac{1}{M^5} \left(\lambda \in R \left(1 - \frac{2M}{R} \right) \left(-\frac{M(M-R)(2M^2+6MR-3R^2)}{R^2(2M-R)^2} \right. \right. \right. \right. \right. \\ & \left. \left. \left. + \frac{3}{2} \ln\left(\frac{R}{R-2M}\right) \right) \right) \right) \\ & + \frac{15}{4} \frac{\lambda \in \left(-\frac{M(M-R)(2M^2+6MR-3R^2)}{R^2(2M-R)^2} + \frac{3}{2} \ln\left(\frac{R}{R-2M}\right) \right)}{M^4} \\ & + \frac{15}{8} \frac{1}{M^5} \left(\lambda \in R^2 \left(1 - \frac{2M}{R} \right) \left(\frac{M(2M^2+6MR-3R^2)}{R^2(2M-R)^2} \right. \right. \end{aligned}$$

$$\begin{aligned}
& - \frac{M(M-R)(6M-6R)}{R^2(2M-R)^2} + \frac{2M(M-R)(2M^2+6MR-3R^2)}{R^3(2M-R)^2} \\
& - \frac{2M(M-R)(2M^2+6MR-3R^2)}{R^2(2M-R)^3} \\
& + \frac{3}{2} \left(\frac{\left(\frac{1}{R-2M} - \frac{R}{(R-2M)^2} \right) (R-2M)}{R} \right) \left(+ 2 \epsilon R \left(1 - \frac{2M}{R} \right) + 2 \epsilon M \right) \right) \\
& \left(\frac{15}{8} \frac{\lambda \epsilon R^2 \left(1 - \frac{2M}{R} \right) \left(- \frac{M(M-R)(2M^2+6MR-3R^2)}{R^2(2M-R)^2} + \frac{3}{2} \ln \left(\frac{R}{R-2M} \right) \right)}{M^5} \right. \\
& \left. + \epsilon R^2 \left(1 - \frac{2M}{R} \right) \right) = y
\end{aligned}$$

> solve((6), lambda);

$$\begin{aligned}
& \frac{16}{15} \left(R^2 M^5 (8 M^3 y - 12 M^2 R y + 6 M R^2 y - R^3 y - 8 M^3 + 16 M^2 R - 10 M R^2 + 2 R^3) \right) / \\
& \left(-24 M^3 \ln \left(-\frac{R}{2M-R} \right) R^2 y + 36 M^2 \ln \left(-\frac{R}{2M-R} \right) R^3 y - 18 M \ln \left(-\frac{R}{2M-R} \right) R^4 y \right. \\
& + 3 \ln \left(-\frac{R}{2M-R} \right) R^5 y + 8 M^5 y + 12 M^4 R y + 24 M^3 \ln \left(-\frac{R}{2M-R} \right) R^2 - 44 M^3 R^2 y \\
& - 48 M^2 \ln \left(-\frac{R}{2M-R} \right) R^3 + 30 M^2 R^3 y + 30 M \ln \left(-\frac{R}{2M-R} \right) R^4 - 6 M R^4 y - 6 \ln \left(-\frac{R}{2M-R} \right) R^5 \\
& \left. + 8 M^5 - 8 M^4 R + 52 M^3 R^2 - 48 M^2 R^3 + 12 M R^4 \right) \quad (7)
\end{aligned}$$

> simplify((7), 'size');

$$\begin{aligned}
& (16 R^2 M^5 (2M-R)^2 (2My - Ry - 2M + 2R)) / \left(-360 \left(M - \frac{1}{2} R \right)^2 \left((y-1) M \right. \right. \\
& \left. \left. - \frac{1}{2} R (y-2) \right) R^2 \ln \left(-\frac{R}{2M-R} \right) + 120 M \left((y+1) M^4 + R \left(\frac{3}{2} y - 1 \right) M^3 \right. \right. \\
& \left. \left. - \frac{11}{2} \left(y - \frac{13}{11} \right) R^2 M^2 + \frac{15}{4} R^3 \left(y - \frac{8}{5} \right) M - \frac{3}{4} R^4 (y-2) \right) \right) \quad (8)
\end{aligned}$$

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