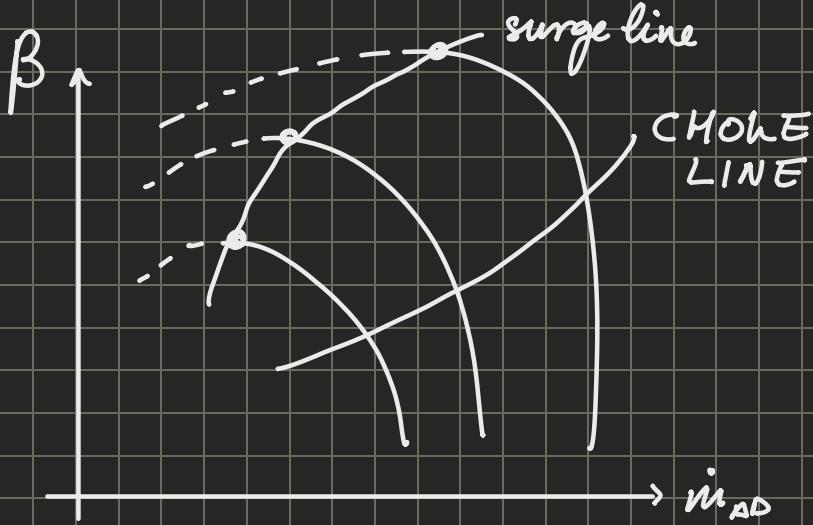


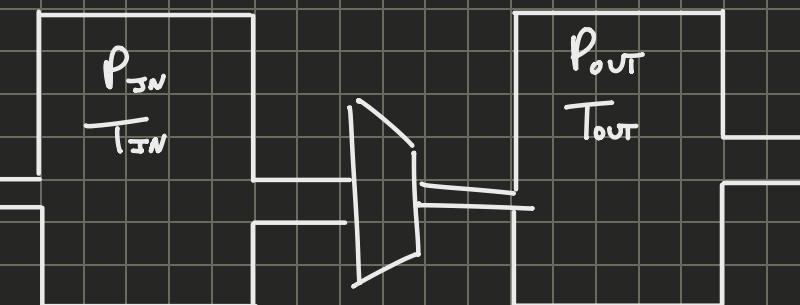
Lezione 25 - Axial Turbines

Surge Instability in Axial Compressors

If a compressor is tested alone, we can reconstruct the machine behaviour and reconstruct the curve.



The curve to the right can be measured.
on the left it cannot be measured due to large noise.



8:38

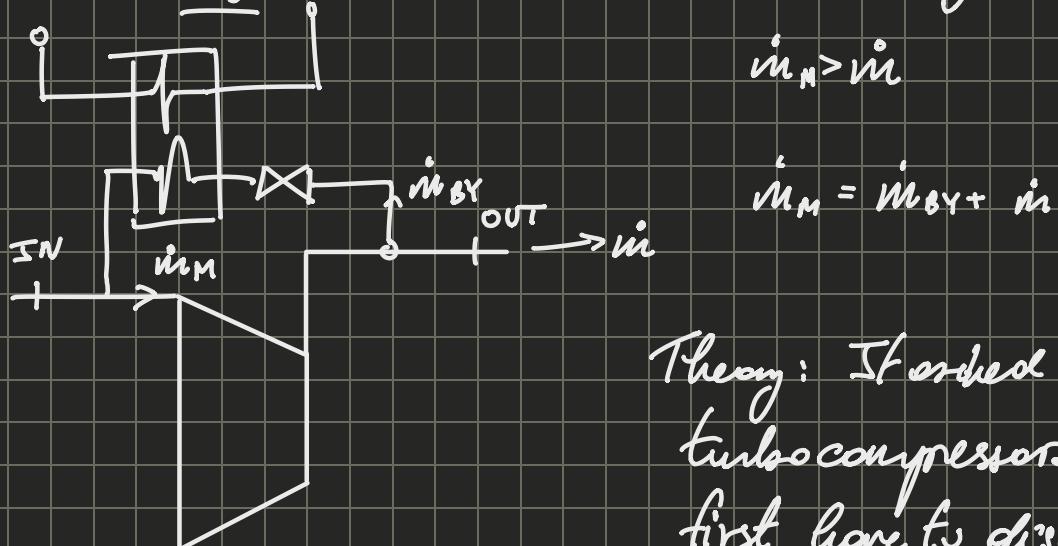
The compressor keeps the β . One moves to the left due to instability, there is ~~unbal~~ —, this is a perturbation. As this increases the flow rate goes back, causing the fluid to go back.

The velocity triangles are completely changed and so are the forces, slowly destroying the machine.

This backflow increases P_{in} and decreases P_{out} , at some point $P_{in} > P_{out}$, because it's an elastic system, the fluid the when P_{in} is even bigger than P_{out} initial the flow will go back, and the flow continues to go back

and forth, and at some point the machine explodes.

- Bypass System → One method of avoiding surge



Theory: It is about
turbo compressors, we
first have to discuss
about dimensionless quantities,
then talk about curves,
then talk about surge.

Uses for Axial-Flow Turbines → used mainly in every generation.

There are many typical applications:

- Rankine Cycle → constructed around the water state diagram

- ↳ $m = 500 \text{ kg/s}$
- ↳ L can be up to 1 GW.

This cycle has a crucial role for superheater/turbine technologies on cycle optimization.

Any amount of efficiency we can extract is huge.

$$Q_{out} / Q_{in} \sim 100$$

→ the cross section has to change by two orders of magnitude to disperse the same mass flow rate

at inlet and outlet of the turbine (constant V_m).

Limitations are in the maximum pressure ratio achievable with a single stage, and in the maximum flow rate passing through a feasible annular cascade.

[9:00]

A multi-stage axial configuration allows to combine the extreme flow rate with high pressure ratios.

There are different possible configurations

The machine has to operate at $n = 3000 \text{ rpm}$, because no gearbox that works in those conditions do not exist, so since we need to produce electricity we need to spin at that specific speed.

The steam-cycle is not studied here.

Second Application:

↳ Turboror cycle

↳ Realization of the Joule-Brayton cycle with two nearly isentropic and one ^{almost} isobaric transformations.

$m \sim 200 \text{ kg/s}$

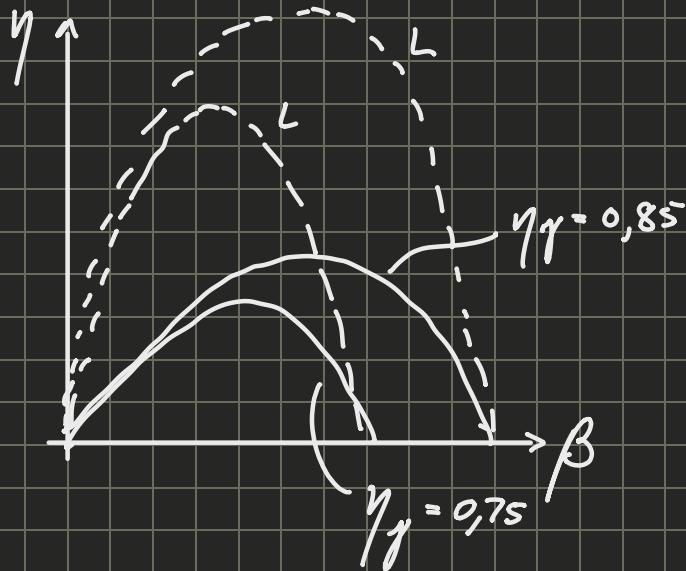
$\beta \approx 15-15$

L can exceed easily 100 MW .

Turboror performance and technology are crucial

for optimisation.

We need T_3 to be very high, $\sim 2000\text{ K}$, which exceed material sustainability, but we can actively cool the blades.

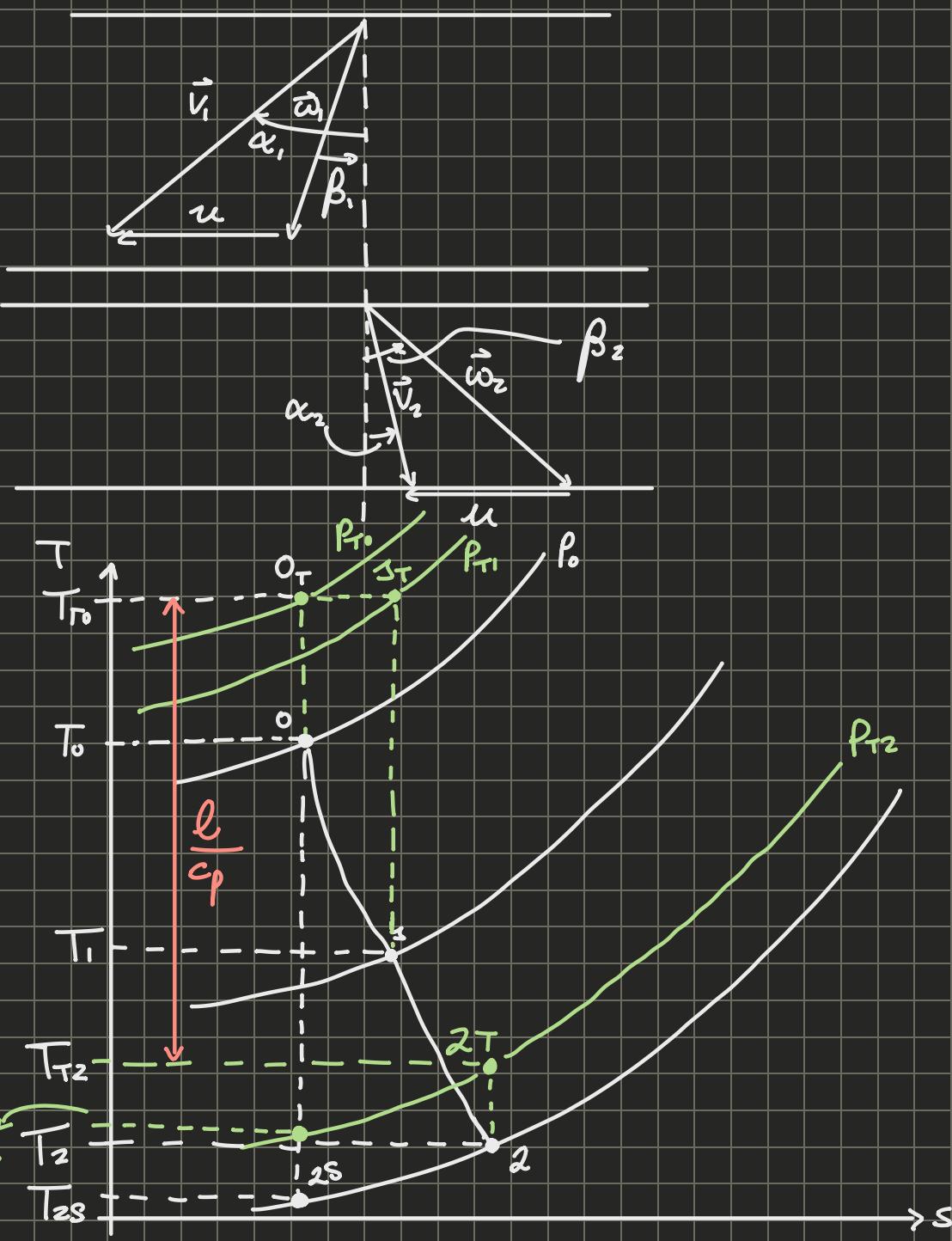
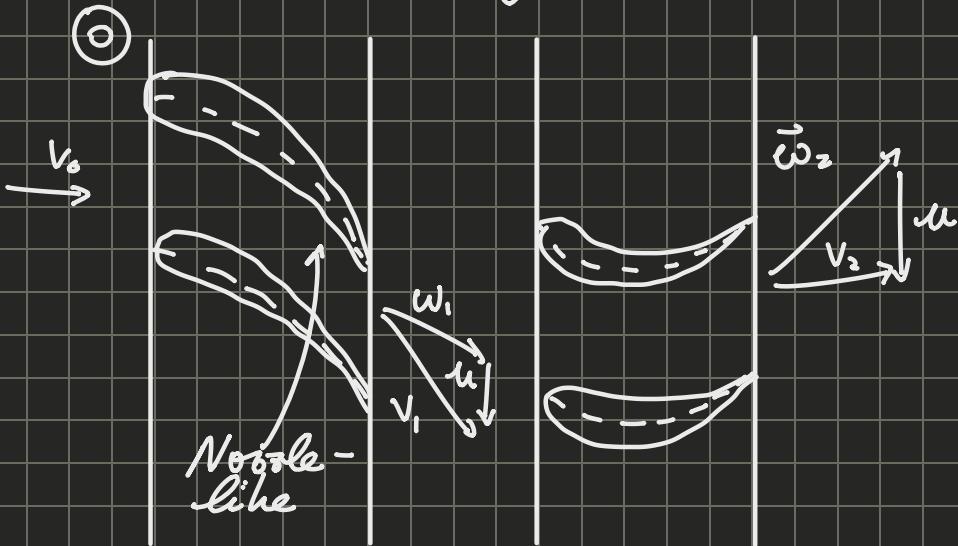


We use multi-stage compressors and turbines.
The machine can operate on different shafts at different speeds.

We use 2 compressors and 2 turbines, each operating at different pressures.

Turbine - stage

Thermofluid dynamic diagram



$$l+g = \Delta h_T$$

STATOR: $l=0, g=0 \Rightarrow \Delta h_T = 0 \Rightarrow h_{T1} = h_{T0} \Rightarrow T_{T1} = T_{T0}$
 ROTOR: $l \neq 0, g=0 \Rightarrow \Delta h_T = l \Rightarrow l = c_p (T_{T2} - T_{T1}) = c_p (T_{T2} - T_0)$

$$\eta_{TS} = \frac{|l|}{h_{T0} - h_{2s}}$$

↓
Total to static
efficiency

$$\eta_{TT} = \frac{|l|}{h_{T0} - (h_{2s} + \frac{V_2^2}{2})}$$

$\underbrace{h_{T2s}}$

Should be V_{2s}

↳ the calculate
velocity if the transformation
had been isentropic.

$$\eta_{TT} > \eta_{TS}$$

↳ Because η_{TS} consider also the loss
due to disengaged flow.

$$\chi = \frac{\Delta h_R}{l} = \frac{\omega_2^2 - \omega_1^2}{V_1^2 - V_2^2 + \omega_2^2 - \omega_1^2}$$

↳ same definition, can have
sign, as compressor

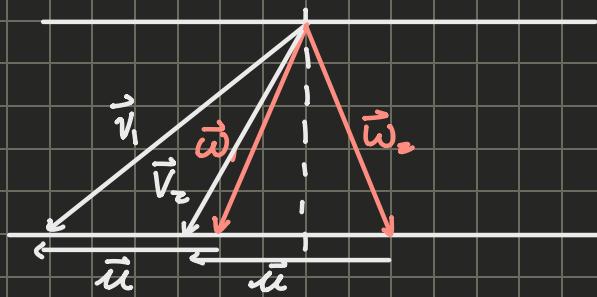
Stage-styles in axial turbines

↳ In turbines we have more creative liberty for designs.

Impulse Stage $v_m = \text{const}$

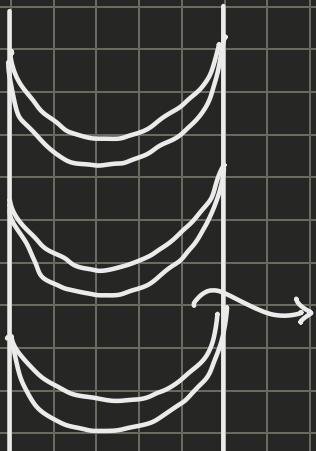
$$\chi = 0 \Rightarrow D h_R = 0 \Rightarrow |\vec{\omega}_z| = |\vec{\omega}_r|$$

↳ like Pelton.

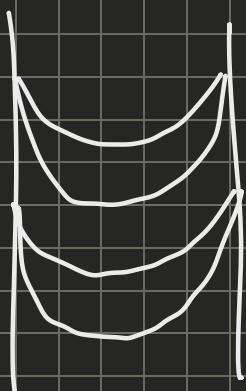


$$|\beta_r| = |\beta_e|$$

↳ Draw different to separate v_e , but it's the same



This is a divergent, then convergent which will create adverse pressure gradients.

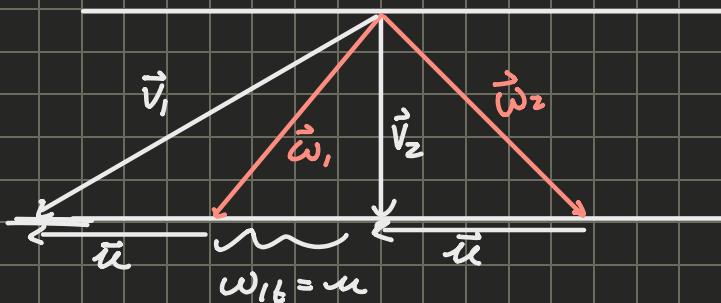


So we design around the channel instead of the blade (creative liberty) or to keep the channel in constant dimension.

9:56 \rightarrow internet keeps disconnecting.

Stage optimized if $V_{2B} = 0$!

To design we can start from the bottom instead of the top:



$$V_{1t} = V_1 \sin \alpha_1 = 2u$$

$$k_p = \frac{u}{\sqrt{V_1}} \Rightarrow k_{p, \text{opt}} = \frac{\sin \alpha_1}{2}$$

$$\ell_{\text{opt}} = u(V_{2t} - V_{1t}) = -\alpha_2 u^2$$

In first approximation

$\rho = \text{const}$, $D_m = \text{const}$, $V_m = \text{const} \Rightarrow b = \text{const}$

↳ Across the rotor, the b will change for the stator.