

## Threaded - Connections

Mechanical connection: machine elements responsible for connecting mechanical components

First classification:

↳ Detachable Connection

↳ screws, bolt, pins, keys, splined profiles

↳ Fixed Connections (cannot be disassembled without damage)

↳ Welding

↳ Pressfits

Threaded (screw) connections

↳ Male screw

↳ Head screw/nut screw/Female screw

What under the connection is the friction and the geometry.

Specific characteristics of screw connections:

↳ Components can be made of different materials

↳ no special tools

↳ most standardised machine elements

↳ typically more expensive and heavy relative to other connections.

## Basic types of screws pg. 4

- ↳ Most important
  - ↳ Through bolt
  - ↳ Tap bolt
- ↳ Stud

There are also set screws, to help define a position.

There are many different kinds of screw heads.

## Basic types of nuts: pg. 5

There are solutions to prevent unscrewing.

$$\text{Screw} + \text{Nut} (+\text{washer}) = \text{Bolt}$$

## Screw Thread Types (all standardized)

- ↳ Most common for us is the metric thread.
- ↳ Next most common is Whitworth

Saw tooth and trapezoidal are used for power transmission or for very high loads.

Ecklon Thread, just for light bolts.

Metric  $\rightarrow M$

Whitworth  $\rightarrow W$

Trapezoid  $\rightarrow$  Tr

Sawtooth  $\rightarrow$  S

ISO grades (strength classes)

(10.9)  $\sim$  90% of Yield Stress  $\Rightarrow 10,9 = 900 \text{ MPa}$

$\hookrightarrow 1000 \text{ MPa} = \text{Yield Stress}$

$\hookrightarrow \frac{\text{UTS}}{100}$   $\rightarrow$  Ultimate Tensile Strength / Stress  
at which one

$$6,8 = 600 \cdot .8 = 480 \text{ MPa}$$

The strength class is just a different way to call materials by their strength.

Knowing the class we know the mechanical properties.

Each class corresponds a material.

Never use a nut of a lower grade than a screw, since the system will fail due to the nut.

$\hookrightarrow$  We design based on the screw, so if the nut is better it doesn't matter.

Metric threaded shapes : pg. 8

$\hookrightarrow$  We use tables to browse standard nuts.

$$\text{Stress area : } A_{\text{res}} = \frac{\pi}{4} \left( \frac{d_2 + d_3}{2} \right)^2$$

Like gear with modules, we have columns to define how desirable it is to choose that screw, with the third column being the least desirable.

Minor diameter  $\rightarrow$  base diameter.

Nominal diameter is what we design based on.

Screws are defined by coarse or fine pitch.

The previous table on repeated the coarse which is singular to the diameter.

Each diameter has 3 fine pitches.

Coarse Pitch:

- ↳ Faster screws
- ↳ Less chance of thread damage
- ↳ High strength

Fine pitch

- ↳ finer position adjustable
- ↳ less tendency to unscrew
- ↳ higher strength of core
- ↳ higher thread increase.

Coarse or fine or coarse or a few fine pitches.

or pg. 10

Screws cannot be used for centring, because the position does not require the whole to be within tolerances.

Usually, the holes are:

$$\text{Up to M24} = D + 1.5 \text{ mm}$$

$$\text{Above M24} = D + 2 \text{ mm}$$

Nomenclature

Standard +

Type of geometry +

Nominal Diameter

Pitch + → for coarse it can be slipped

Length +

Material grade

Informally we can define just the geometry, diameter and pitch

And for non-standards, we say the diameter, pitch and geometry.

## Design (how to choose)

Failure modes

↳ static case

↳ yielding and then fracture → occurs at the first thread in contact

↳ Fatigue (cracking)

↳ under the head (since notch)

↳ beginning of the reloaded region

↳ first thread in connection between thread and lead thread ↳ this is because of the uneven

distribution of load, the first thread takes 50% of the

same reason

load.

Strength of screws

↳ Cases:

- ↳ Not tightened screws (loose)
- ↳ Tightened screw (preloaded)

→ freedom of rotation, and unloaded until loaded  
→ we can put a preload, so it is loaded even though the machine is not loaded.

↳ The design for the two is different

For designing we will be using nominal stresses, since things like notch effect are not easy to consider.

→ We will be using fatigue limits for screws that have already been tested.

→ The notch effect is around 4-10, so we usually try to not use threaded connections for fatigues.

Algorithm for sizing and checking: pg. 14

Generally pre-sizing (pre-checking) and checking.

With symmetry we can use the symmetry to find force.

If the are not symmetric, the structure is hyperstatic and there are some tricks we can use to solve.

Loose Screws.

→ The stress is uniaxial, directed along the axis.

For the static case:  $\sigma_a = \frac{P}{A}$

$$\sigma_{max} = \frac{F_{A,max}}{A_3} \quad \begin{matrix} \curvearrowright \\ \text{minor area (to be on safe side)} \end{matrix}$$

or we can use  $d_2$  (weighted average  
area of diameter)

For the fatigue case:

$$\left\{ \begin{array}{l} \sigma_a = \frac{\Delta \sigma}{2} = \frac{F_{A,max} - F_{A,min}}{2A_3} \\ \sigma_{med} = \frac{F_{A,max} + F_{A,min}}{2A_3} \end{array} \right.$$

mean stress  
alternating stress

$A_3$  is mandatory  
in this case

Static Check (as always)

$$\sigma_{max} \leq \frac{R_{SN}}{\eta} = \sigma_{allow}$$

we use  $\eta$  to select and find  $R_{SN}$

Fatigue

again

$$\sigma_a \leq \frac{\sigma_{lim}}{\eta} = \sigma_{allow}$$

$\sigma_{lim}$  is given by the standard in this case, based on screw

material.

The standard does not consider the effect of  $T_{\text{med}}$ , if it is present then we have to use the Haig diagram.

Preloaded Screw:

↳ Preloads are used to compress parts together.

The preload is a design parameter, how do we choose this.

How is the pre-load chosen?

↳ We cannot preload as much as we can since that will cause damage.

↳ We use special tools to set preloads, we use torque wrenches to assign a given torque.

↳ We use torque since it's the only way to load a screw.

Relationship between torque and axial load?

Torque has to combat  $T_{\text{GA}}$  and  $T_{\text{fr}}$

↓  
friction between threads.

$$T_{\text{A}} = T_{\text{GA}} + T_{\text{fr}}$$

↳ Total torque

$T_{\text{GA}}$  is what causes the preload, but we cannot ignore  $T_{\text{fr}}$ .

$$T_u = \mu_k \cdot F_s \cdot \frac{d_{\text{int}}}{2} \quad \begin{matrix} \text{mean diameter of int} \approx 1,5 D \\ \text{of screw.} \end{matrix}$$

The preload is  $\int dF_s = F_s$

$\int dF_u = 0$  since the direction changes around the axis.

$$dF_u = dF_s \cdot \tan \varphi$$

$$T_a = \int dF_u \cdot \frac{dz}{2} = \int dF_s \cdot \tan \varphi \cdot \frac{dz}{2} = F_s \tan \varphi \cdot \frac{dz}{2}$$

The component of the friction changes the force triangle.

The only thing that changes though is that:

$$dF_u = dF_s \tan(\varphi + \rho) \Rightarrow T_{a1} = F_s \tan(\varphi + \rho) \frac{dz}{2}$$

Geometric contribution

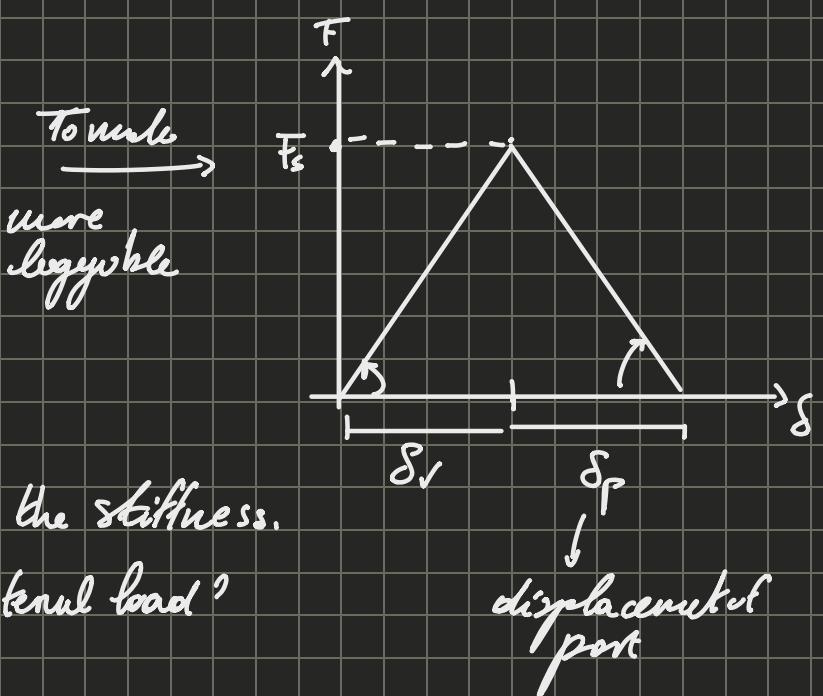
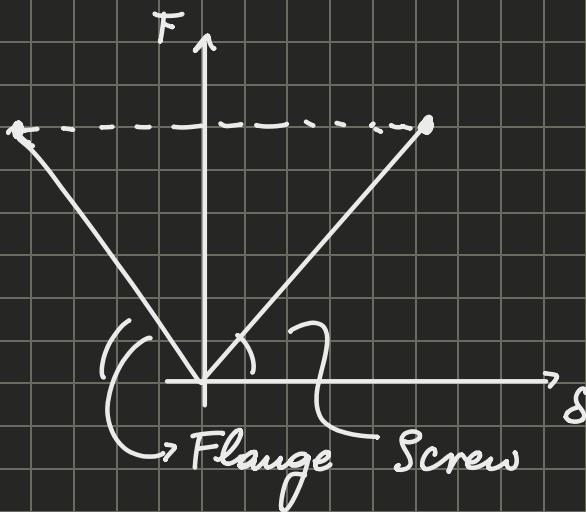
Friction contribution.

Since before we considered square threads, but we are using triangular threads, we consider an approach friction angle (that considers this geometry) and we get:

$$T_s = T_u + T_{a1} = F_s \left[ \mu_k \frac{d_{\text{int}}}{2} + \tan(\varphi + \rho') \cdot \frac{dz}{2} \right]$$

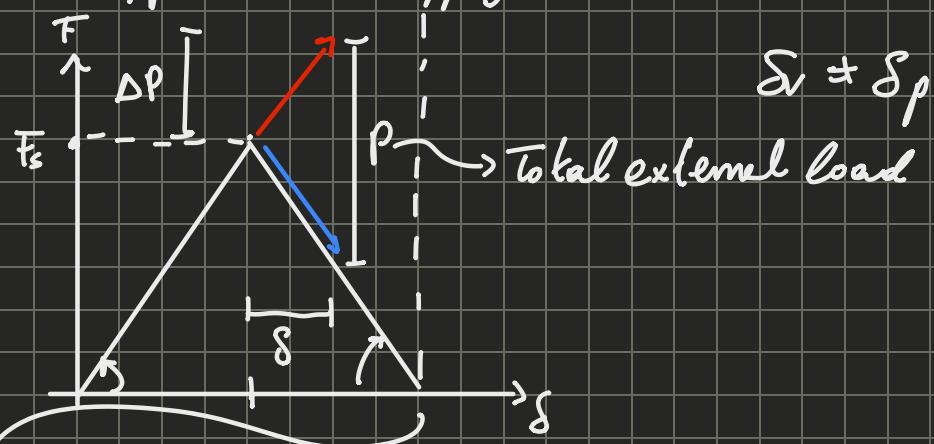
### Elastic Analysis of loaded connection

Because of the "gasket effect", we cannot pre-load belts one after another, crossed to cross.



The slope is defined by the stiffness.

What happens when we apply external load?



$$\delta_r = \delta_p$$

$\delta_r$  is the displacement of the part.

$\delta$  is the same for the bolt and part.

limit for joint, once we get here the joint fails.

We need to find the force that causes the bolt to fail.

$$k_r = \frac{\Delta P}{\Delta S}$$

$$k_p = \frac{P - \Delta P}{\Delta S} \Rightarrow \Delta P = P \cdot \left( \frac{k_r}{k_r + k_p} \right) \Rightarrow P_r = F_s \Rightarrow \Delta P$$

we use  $F_s + P_r$  to check the bolt and  $P_{max}$  to check if the system as a whole is ok.

Stress or fatigue calculations  $\rightarrow$  pg. 28+29