

$$\Delta < 0 \implies \lambda_{1,2} = \alpha \pm i\beta \ \& \ y_1 = e^{\alpha x} \cos(\beta x), y_2 = e^{\alpha x} \sin(\beta x)$$

$$f(t) = Ae^{\alpha t} \implies y_p(t) = ce^{\alpha t}$$

$$f(t) = \text{polinomio} \implies y_p(t) = At^2 + Bt + C$$

$$f(t) = \text{trigonometrico} \implies y_p(t) = A\cos(vt) + B\sin(vt)$$

$$L(x, y, \lambda) = f(x, y) - \lambda \cdot g(x, y)$$

$$H_f = \begin{bmatrix} f_{xx} & f_{xy} \\ f_{yx} & f_{yy} \end{bmatrix}$$

$$\text{se } \det(H_f) > 0 \text{ e } f_{xx} > 0 : \text{Minimo locale}$$

$$\text{se } \det(H_f) > 0 \text{ e } f_{xx} < 0 : \text{Massimo locale}$$

$$\text{se } \det(H_f) < 0 : \text{Punto di sella}$$

$$JT = \begin{bmatrix} g_u & g_v \\ h_u & h_v \end{bmatrix}$$

$$\text{Cambio di variabile: } \iint_D f(x, y) dx dy = \iint_S f(g(u, v), h(u, v)) |\det(JT)| du dv$$

$$\text{rot} \underline{F} = \begin{bmatrix} \underline{i} & \underline{j} & \underline{k} \\ \partial x & \partial y & \partial z \\ F_1 & F_2 & F_3 \end{bmatrix}$$

$$L = \int_{\gamma} \underline{F} \cdot d\underline{r} = \int_a^b \underline{F}(\underline{r}(t)) \cdot \underline{r}'(t) dt$$

$$\int_{\partial A^+} \underline{F} \cdot d\underline{r} = \iint_A \text{rot}(\underline{F}) dx dy$$

$$\underline{n} = \frac{\underline{r}_u \times \underline{r}_v}{|\underline{r}_u \times \underline{r}_v|}$$

$$\nabla f = \begin{bmatrix} \pm f_x \\ \pm f_y \\ \mp 1 \end{bmatrix}$$

$$dS = \sqrt{1 + \|\nabla f\|^2} dx dy$$

$$\underline{n} \cdot dS = \nabla f dx dy$$

$$\phi(\underline{F}, S) = \iint_S \underline{F} \cdot \underline{n} dS$$

$$\text{div} \underline{F} = \frac{\partial F_1}{\partial x} \underline{i} + \frac{\partial F_2}{\partial y} \underline{j} + \frac{\partial F_3}{\partial z} \underline{k}$$

$$\iint_{\partial D^+} \underline{F} \cdot \underline{n} dS = \iiint_D \text{div} \underline{F} dx dy dz$$

$$A(D) = \frac{1}{2} \int_{\partial^+ D} x dy - y dx = \frac{1}{2} \int_{\partial^+ D} \underline{F} \cdot d\underline{r}$$

$$U(x, y) = \int_{y_o}^y F_2(x_o, t) dt + \int_{x_o}^x F_1(t, y) dt$$