

Assignment ~ 02

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Ans. to the Q. NO-01(a)

Given,

starting point $\Rightarrow A (-5, 2)$

ending point $\Rightarrow B (25, 40)$

Now,

$$\text{Let, } P(t) = A + t(B - A), \quad t \in [0, 1]$$

the parametric equation,

$$P(t) = (x(t), y(t)) = x_0 + t(x_1 - x_0), \quad y_0 + t(y_1 - y_0)$$

\therefore

$$x(t) = -5 + t(25 - (-5)) = -5 + 30t$$

$$y(t) = 2 + t(40 - 2) = 2 + 38t$$

here,

$$x_0 = -5$$

$$x_1 = 25$$

$$y_0 = 2$$

$$y_1 = 40$$

\therefore parametric equation will be,

$$P(t) = (-5 + 30t, 2 + 38t), \quad t \in [0, 1]$$

And,

(Ans)

Coordinates at $t = 2/3$:

$$\begin{aligned} x\left(\frac{2}{3}\right) &= -5 + 30 \cdot \frac{2}{3} \\ &= 15 \end{aligned}$$

$$\begin{aligned} \text{and } y\left(\frac{2}{3}\right) &= 2 + 38 \cdot \frac{2}{3} \\ &\approx 27.33 \end{aligned}$$

[P.T.O.]

$$\therefore p\left(\frac{2}{3}\right) = \left(15, \frac{82}{3}\right) \cdot$$

$$\approx (15, 27.33)$$

(Ans)

Again,

when $t = 5$,

It is not inside the segment.

\therefore start point in range $\rightarrow 0$

end point in range $\rightarrow 1$

$\therefore t = 5$ is lying outside the line segment.

(Ans)

Ans. to the Q. NO - 01(b)

Role of parametric equation in the Cyrus-Beck algorithm :

- 1) \rightarrow Representation of line as $P(t) = P_0 + t(P_1 - P_0)$
- 2) \rightarrow The value of t : determines entry and exit points of the line with respect to the convex polygon.
- 3) \rightarrow Allows calculating intersections with edges using dot products and normal vectors.
- 4) \rightarrow Clipping is done by finding valid value of t in the range $[t_{\max}, t_{\min}]$ where the line is inside the clipping window.

(Ans)

Ans. to the Q. NO - 01 (c)

Given,

window clipping $\rightarrow x \in [-15, 60], y \in [5, 120]$

line segment $\rightarrow p_0 = (20, 30)$

$p_1 = (90, 80)$

According to parametric equation using given values:
 $p(t) = (x(t), y(t)) = (x_0 + t(x_1 - x_0), y_0 + t(y_1 - y_0))$
 $\Rightarrow p(t) = (20 + 70t, 30 + 50t), t \in [0, 1]$

Now,

4 edges of the window and their normal vectors:

here,
 $x_0 = 20$
 $x_1 = 90$
 $y_0 = 30$
 $y_1 = 80$

Edge	Point on edge	Normal Vector (n)	Direction.
Left	$x = (-15, 5)$ to $(-15, 120)$	$(-1, 0)$	Faces left to right
Right	$x = (60, 5)$ to $(60, 120)$	$(1, 0)$	Faces right-to-left
Bottom	$y = (50, 5)$ to $(-15, 5)$	$(0, -1)$	Faces bottom-top
Top	$(-15, 120)$ to $(60, 120)$	$(0, 1)$	Faces top-bottom

We know,

Cyrus - Beck Line Clipping Formula:

$$t = \frac{(n \cdot (P_e - P_o))}{n \cdot D}$$

for left edge: ($x = -15$)

$$n_L = (-1, 0)$$

$$P_e = (-15, y)$$

$$\approx [\text{let, use } (-15, 0)]$$

$$\begin{aligned} D \cdot n_L &= (70, 50) \cdot (-1, 0) \\ &= -70 \end{aligned}$$

$$\begin{aligned} -(P_o - P_e) \cdot n_L &= -((20, 30) - (-15, 0)) \cdot (-1, 0) \\ &= 35 \end{aligned}$$

$$\therefore D \cdot n = -70 < 0 \text{ (entering)}$$

$$t_L = \frac{35}{-70} = -0.5 \quad [\text{potential exit}]$$

$$t_{\text{enter}} = \max(0, -0.5) = 0$$

$$t_{\text{exit}} = 1$$

Here,

$$P_o = (20, 30)$$

$$\begin{aligned} \text{Direction vector,} \\ D &= (90-20, 80-30) \\ &= (70, 50) \end{aligned}$$

P_e = a point on the edge

n = normal vector of the edge

for right edge : ($x=60$)

$$P_e = (60, 0)$$

$$n_R = (1, 0)$$

$$D \cdot n = (70, 50) \cdot (1, 0) = 70 \text{ (exit)}$$

$$\begin{aligned} - (P_o - P_e) \cdot n_R &= - ((20, 30) - (60, 0)) \cdot (1, 0) \\ &= 40 \end{aligned}$$

$$t_R = 40/70 = 4/7 \approx 0.5714$$

$$t_{\text{enter}} = 0$$

$$t_{\text{exit}} = \min(1, 4/7) = 4/7$$

for bottom edge : ($y=5$)

$$P_e = (0, 5)$$

$$n_b = (0, -1)$$

$$D \cdot n_b = (70, 50) \cdot (0, -1) = -50 \text{ (entry)}$$

$$\begin{aligned} - (P_o - P_e) \cdot n_b &= - ((20, 30) - (0, 5)) \cdot (0, -1) \\ &= 25 \end{aligned}$$

$$t_b = 25/-50 = 0.5$$

$$t_{\text{enter}} = \max(0, -0.5) = 0$$

$$t_{\text{exit}} = 4/7$$

Forc top edge ($y = 120$):

$$P_e = (0, 120)$$

$$n_T = (0, 1)$$

$$D \cdot n_T = (70, 50) \cdot (0, 1) = 50 \text{ (exit)}$$

$$-(P_o - P_e) \cdot n_T = -((20, 30) - (0, 120)) \cdot (0, 1) = 90$$

$$t_T = \frac{90}{50} = 1.8$$

$$t_{\text{enter}} = 0.5714$$

$$t_{\text{exit}} = \min(1) = 1 \quad \left. \begin{array}{l} \\ \end{array} \right\} \therefore (t_e \notin [0, 1), > 1) \therefore \text{no update to } t_{\text{enter}}.$$

\therefore

$$0.5714 > 1$$

\therefore the line is not rejected.

The Cyrus-Beck algorithm fundamentally finds the segment of the line $(P_1 + t \cdot D)$ lies within convex polygon.

We get,

$$t_L = -0.5 \text{ (exit left - before } P_1)$$

$$t_b = -0.5 \text{ (exit bottom - before } P_1)$$

$$t_T = 1.8 \text{ (enters top - after } P_2) \quad [P, T, O]$$

the only intersection point within $[0, 1]$

where the line is exiting the window is at $t = 4/7$ [with right boundary].

\therefore the clipped segment $\Rightarrow P(0)$ to $P(4/7)$

\therefore the line segment from $(20, 30)$ to $(90, 80)$ needs to be clipped.

The clipped line's endpoints:

① first endpoint : $P(0) = (20, 30)$ $\left[\because P_1 \text{ is inside the window} \right]$

② second endpoint : $P(4/7)$

$$\Rightarrow x = 20 + 70 \cdot (4/7) = 60$$

$$\Rightarrow y = 30 + 50 \cdot (4/7) \approx 58.57$$

$$\therefore (x, y) = (60, 58.57)$$

\therefore The clipped line segment $\Rightarrow (20, 30)$ to $(60, 58.57)$

(Ans.)

Ans. to the Q. NO - 02 (a)

Scenarios where Cohen - Sutherland fails:

→ (i) Non-rectangular Clipping window:

This algorithm fails, becomes inefficient for arbitrary polygonal clip regions.

→ (ii) Inefficient for lines that require multiple clipping steps.

→ (iii) In floating point arithmetic, precision errors may cause incorrect values of endpoints.

* Drawbacks:

- (i) Only supports rectangular clipping regions.
- (ii) Repetitive calculation for partial segments, especially in complex scenarios.
- (iii) It may clip unnecessarily, even when the line is trivially accepted/rejected.

(iv) Inefficient for clipping large numbers of lines, especially in dynamic scenes/animations.

Ans. to the Q. NO-02(b)

Given,

Clip region:

$$x_{\min} = -40,$$

$$y_{\min} = -20,$$

$$x_{\max} = 20$$

$$y_{\max} = 30$$

Line segment:

$$P_1 = (-10, -50)$$

$$P_2 = (15, 25)$$

Now,

Region	Condition
Top	$y > y_{\max} (30)$
Bottom	$y < y_{\min} (-20)$
Right	$x > x_{\max} (20)$
Left	$x < x_{\min} (-40)$

for $P_1 (-10, -50)$:

here,

$x = -10$, \rightarrow within x range \rightarrow Right = 0
left = 0
 $y = -50 < -20 \rightarrow$ Bottom = 1

And Top = 0

\therefore ABRL \rightarrow 0100 \rightarrow (4-bit code) $\rightarrow P_1$

for $P_2 (15, 25)$:

$x = 15$ [within x range]

$y = 25$ [within y range]

\therefore ABRL \rightarrow 0000 [4-bit code] $\rightarrow P_2$

Now,

$P_1 \rightarrow 0100$

$P_2 \rightarrow 0000$

(AND) $\rightarrow 0000$

\rightarrow Not both outside in the same region

\rightarrow Partially inside

\rightarrow not trivially rejected

\rightarrow continue clipping.

[P.T.O.]

Now, $P_1 = (-10, -15)$ is outside the bottom.

bottom edge $\rightarrow (y = -20)$

the intersections:

We know,

$$x = x_1 + (x_2 - x_1)t$$

$$y = y_1 + (y_2 - y_1)t$$

from:

$$P_1 (-10, -15)$$

$$P_2 (15, 25)$$

① at $y = -20$:

$$y = y_1 + (y_2 - y_1)t$$

$$\Rightarrow -20 = -15 + 40t$$

$$\Rightarrow t = 0.4$$

② at $t = 0.4$, value of x :

$$x = -10 + (15 - (-10)) \cdot 0.4$$

$$= 0$$

\therefore New Clipped point $(0, -20)$ [intersection]

Now,

Replacing P_1 with $P_1' (0, -20)$ and repeating the calculations:

New line segment: $P_1' (0, -20)$ to $P_2 (15, 25)$

for $P_1' (0, -20)$:

$$x_1' = 0 \quad [\text{between } x_{\min} \& x_{\max}]$$

$$y_1' = -20 \quad [\text{on } y_{\min}]$$

$\therefore P_1'$ is inside the window.

\therefore Outcode (P_1') = 0000 (4-bit code)

for $P_2 (15, 25)$: 0000 [from previous calculation]



outcode (P_2)

Now,

Outcode (P_1') AND Outcode (P_2)

(0000) AND (0000)

= 0000

\therefore the line segment is fully accepted.

\therefore final clipped line segment (0, -20) to (15, 25)