

# Assignment - 04

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# Block Coding

Ans. to the Q. NO-01

Haming distance,

$$(00, 01) = 7$$

$$(00, 10) = 3$$

$$(00, 11) = 6$$

$$(01, 10) = 6$$

$$(01, 11) = 3$$

$$(10, 11) = 7$$

$$\therefore d_{\min} = 3$$

$$\therefore \text{detection} = d_{\min} = 5 + 1$$

$$\Rightarrow 3 = 5 + 1$$

$$\Rightarrow 5 = 3 - 1 = 2$$

$$\therefore \text{error detection} = 2 \quad (\text{Ans})$$

$$d_{\min} = 2t + 1 \Rightarrow (\text{connection})$$

$$\Rightarrow 3 = 2t + 1$$

$$2t = 2$$

$$t = 1$$

$$\therefore \text{error correction} = 1$$

(Ans)

$$\begin{array}{r} 11100000 \\ \oplus 00011101 \\ \hline 11111101 \\ (00, 10) \end{array}$$

$$\begin{array}{r} 11100000 \\ \oplus 10101010 \\ \hline 01001010 \\ (00, 10) \end{array}$$

$$\begin{array}{r} 11100000 \\ \oplus 01010111 \\ \hline 10110111 \\ (00, 11) \end{array}$$

$$\begin{array}{r} 00011101 \\ \oplus 10101010 \\ \hline 10110111 \\ (01, 10) \end{array}$$

$$\begin{array}{r} 00011101 \\ \oplus 01010111 \\ \hline 01001010 \\ (01, 11) \end{array}$$

$$\begin{array}{r} 10101010 \\ \oplus 01010111 \\ \hline 11111101 \\ (10, 11) \end{array}$$

Ans. to the Q. No-02

Haming distance here,

$$(00, 01) = 7$$

$$(00, 10) = 3$$

$$(00, 11) = 4$$

$$(01, 10) = 6$$

$$(01, 11) = 5$$

$$(10, 11) = 5$$

here,

$$d_{\min} = 3$$

$$\therefore \text{detection} = d_{\min} = 5 + 1$$

$$\Rightarrow 3 = 5 + 1$$

$$\therefore 5 = 3 - 1 = 2$$

$$\therefore \text{error detection} = 2$$

(Ans.)

again,

$$\text{correction} = d_{\min} = 2t + 1$$

$$\Rightarrow 3 = 2t + 1$$

$$\Rightarrow 2t = 2$$

$$\Rightarrow t = 1$$

$$\therefore \text{error correction} = 1$$

$$\begin{array}{r} 1110000 \\ \oplus 00001101 \\ \hline 11111101 \end{array} \quad (00, 01)$$

$$\begin{array}{r} 11110000 \\ 10111010 \\ \oplus \\ \hline 01001010 \end{array} \quad (00, 10)$$

$$\begin{array}{r} 11110000 \\ 01110111 \\ \oplus \\ \hline 10001111 \end{array} \quad (00, 11)$$

$$\begin{array}{r} 00001101 \\ 10111010 \\ \oplus \\ \hline 10110111 \end{array} \quad (01, 10)$$

$$\begin{array}{r} 00001101 \\ 01110111 \\ \oplus \\ \hline 01111010 \end{array} \quad (01, 11)$$

$$\begin{array}{r} 10111010 \\ 01110111 \\ \oplus \\ \hline 11001101 \end{array} \quad (10, 11)$$

[P.T.O.]

Now,

given codeword = 10101010

for dataword '10': codeword = 10111010

$$\begin{array}{r} \therefore \text{hamming distance} = \begin{array}{r} 10101010 \\ 1011010 \\ \hline 00010000 \end{array} \end{array}$$

$\therefore$  here, error detection = 1

$\therefore$  we can correct this error here.

$\therefore$  for given code word,  
the dataword will be 10.

(Ans)

## CRC

Ans. to the Q. NO-01

Given message,

1011101000

CRC generator polynomial = 1011

Now,

adding 0's = 10111010000000

[ $\because$  divisor = 5 bit  
 $\therefore$  0's to add =  $5-1$   
= 4 bit]

Here,

$$\begin{array}{r|l} 11011 & 10111010000000 \\ & 11011 \downarrow \\ \hline & 011000 \\ & 11011 \downarrow \\ \hline & 00011100 \\ & 11011 \downarrow \\ \hline & 0011100 \\ & 11011 \downarrow \\ \hline & 0011100 \\ & 11011 \downarrow \\ \hline & 001110 \end{array}$$

$\therefore$  remainder = 1110.

transmitted message = 10111010000000

corrupted message = 10111010101110

P.T.O.]



Now,

~~1101~~ | ~~10111010101110~~ |

corrupting 6 bit = 10 111 010 10 111 0

∴

11011	101110	1010	1110
	11011		
	011000		
	11011		
	00011101		
	11011		
	0011001		
	11011		
	000010110		
	11011		
	01101		

∴ remainder is not 0.

∴ error occurs here.

(Ans)

## Answer to the Q. NO-02

Given,

$$\text{message} = x^8 + x^7 + x^5 + x^4 + x + 1$$

$$\text{divisor} = x^4 + 1$$

Here,

multiplying the given message with  $x^4$ ,

$$= x^{12} + x^{11} + x^9 + x^8 + x^5 + x^4$$

$$\begin{array}{r} \therefore x^4 + 1 \overline{) x^{12} + x^{11} + x^9 + x^8 + x^5 + x^4} \quad x^8 + x^7 + x^5 + x^3 + 1 \\ \underline{x^{12} + x^8} \phantom{+ x^5 + x^4} \\ x^{11} + x^9 + x^5 + x^4 \\ \underline{x^{11} + x^7} \phantom{+ x^5 + x^4} \\ x^9 + x^7 + x^5 + x^4 \\ \underline{x^9 + x^5} \phantom{+ x^4} \\ x^7 + x^4 \\ \underline{x^7 + x^3} \phantom{+ x^4} \\ x^4 + x^3 \\ \underline{x^4 + 1} \phantom{+ x^3} \\ x^3 + 1 \end{array}$$

$$\therefore \text{remainder} = x^3 + 1$$

$$\text{transmitted message} = x^{12} + x^{11} + x^9 + x^8 + x^5 + x^4 + x^3 + 1$$

Now,

corrupting right most 5th bit

$$= x^{12} + x^{11} + x^9 + x^8 + x^5 + x^3 + 1$$

[P.T.O.]

Now,

$$\begin{array}{r}
 x^4 + 1 \mid x^{12} + x^{11} + x^9 + x^8 + x^5 + x^3 + 1 \mid \begin{matrix} x^8 + x^7 + x^5 \\ x^3 \end{matrix} \\
 \underline{x^{12} + x^8} \\
 x^{11} + x^9 + x^5 + x^3 + 1 \\
 \underline{x^{11} + x^7} \\
 x^9 + x^7 + x^5 + x^3 + 1 \\
 \underline{x^9 + x^5} \\
 x^7 + x^3 + 1 \\
 \underline{x^7 + x^3} \\
 1
 \end{array}$$

$\therefore$  remainder is not 0.

$\therefore$  error occurs here.

(Ans)



## Ans. to the Q. NO-03

Given,

$$\text{dataword} = 100110$$

$$\text{Remainder} = 100$$

$$\text{transmitted message} = 100110100$$

$$\therefore \text{Remainder} = 3 \text{ bit}$$

$\therefore$  To add 0's,

$$\text{divisor} = 3+1=4 \quad \left[ \because \text{Where first 2 bits are 1, rest are 0} \right]$$

$$\therefore \text{divisor} = 1100$$

Now,

$$\begin{array}{r|l} 1100 & 100110100 \\ & \underline{1100} \\ & 01011 \\ & \underline{1100} \\ & 01110 \\ & \underline{1100} \\ & 001010 \\ & \underline{1100} \\ & 01100 \\ & \underline{1100} \\ & 0000 \end{array}$$

Here,

$$\therefore \text{remainder} = 0$$

$\therefore$  This given codeword has no errors.

(Ans)