

Problem n.3

A newly designed airfoil is tested with a series of aerodynamic and acoustic tests in an anechoic wind tunnel. The file `airfoil.txt` reports the sound level (in decibel) measured under different experimental conditions characterized by different air stream frequencies (in hertz) and velocities (labelled H and L for high velocity and low velocity respectively). Consider the following linear model for the sound level (Y), which accounts for the air stream frequency x and for the air stream velocity:

$$Y = \beta_{0,g} + \beta_{1,g} \cdot x + \epsilon,$$

with $\epsilon \sim N(0, \sigma^2)$ and g the grouping structure induced by the velocity of the air stream.

- a) Provide the pointwise estimates of the parameters of the model and verify the model assumptions.
- b) Perform three statistical tests to verify if
 - there is a significant dependence of the mean sound level on the air stream frequency,
 - there is a significant dependence of the mean sound level on the air stream velocity,
 - the increase in the mean sound level induced by a unitary increase in the frequency is significantly different for high and low air stream velocities.
- c) Based on the results of the previous point, reduce the model and update the parameters.
- d) Using the model at point c), provide a confidence interval for the mean of the sound level of a new test performed with air stream frequency of 15 000 Hz and high air stream velocity.