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Auditing a Poly1305 MAC implementation in Jasmin for x86

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Abstract

Poly1305 is a one time authenticator that generates a message authentication code for a given input and secret key using, for that purpose, a similar mechanism to universal hashing. Jasmin is a framework for developing high performance and high assurance cryptographic software. The present work aims to audit an implementation of the Poly1305 MAC using the Jasmin framework. I'll begin by describing the Poly1305 MAC at a high(abstraction) level, followed by an in-depth analysis of the Jasmin implementation of the algorithm. The work concludes with an auditing/verification of the premisses/assumptions that were made in the implementation.

1 Introduction

Message authentication codes play a major role in guaranteeing the authenticity and integrity of data being sent across an untrusted channel. There are many cryptoprimitives that implement MAC's and, for a long time, HMACs(Hash-MACs) were preferred over others due to their performance, with other primitives such as the ones based on universal hashing being discarded. This preference was further reinforced by the introduction of assembly instructions to perform hash functions directly in hardware [2], such as Intel's instruction for SHA-256: `sha256rnds2`. The development of cryptoprimitives such as Poly1305 MAC using Jasmin, a framework for developing high performance and high assurance cryptographic software [1], allowed this tendency to be reversed by obtaining highly performant implementations with relative ease.

2 Poly1305 explained

Poly1305 is a message authentication code(MAC) that guarantees integrity and authenticity of messages. It achieves so similarly to a universal hash function, using a polynomial over a prime field to calculate a MAC for a given message,key pair. As stated Poly1305 evaluates a polynomial over a prime field, the prime, $2^{130} - 5$, being where the name (Poly**1305**) stems from. Thus, Poly1305 can be expressed by the following expression:

$$mac = (m_1 * r^4 + m_2 * r^3 + m_3 * r^2 + m_4 * r + k) \mod p$$

where m_i is the i -th block of the message. Being an authenticator, Poly1305 also takes in a 256 bit secret, derived via a Password-Based Key Derivation Function(PBKDF), that is then split up into two blocks of 128 bits each, the first block being used for the parameter k , and the second for the parameter r . Poly1305 works by breaking the input in 16 byte blocks, appending each block with a 1 byte(00000001) to prevent forgery. It then proceeds to apply the following algorithm/formula:

```
h = 0
for block in blocks:
    h += block
    h *= r
mac = (h + k) mod 2^130-5
```

where:

- h is a (temporary) accumulator for the successive multiplications/additions
- $block$ is a 16 byte message block plus a 1 byte
- r and k are the 128 bit values derived from the 256 bit secret

One of the consequences of the presented algorithm is the fact that, after a certain number of blocks, the variable h will overflow due to the successive multiplications. Therefore, it is necessary to perform the calculation via modular arithmetic. To do this in an efficient manner the prime $2^{130} - 5$ was chosen to perform schoolbook multiplication furthermore, carry propagation is delayed to allow for fast(er) modular reduction.

2.1 (Schoolbook) Multiplication

After adding the message block mi to the current h value, h is multiplied with r using schoolbook multiplication. Note that, to perform this multiplication, r and h are divided in five 4 byte(32 bit) blocks, called limbs, and multiplied with each other as follows:

*	h5 r5	h4 r4	h3 r3	h2 r2	h1 r1
	$h5*r1$	$h4*r1$	$h3*r1$	$h2*r1$	$h1*r1$
+	$h4*r2$	$h3*r2$	$h2*r2$	$h1*r2$	$5*h5*r2$
+	$h3*r3$	$h2*r3$	$h1*r3$	$5*h5*r3$	$5*h4*r3$
+	$h2*r4$	$h1*r4$	$5*h5*r4$	$5*h4*r4$	$5*h3*r4$
+	$h1*r5$	$5*h5*r5$	$5*h4*r5$	$5*h3*r5$	$5*h2*r5$

The expressions in bold are the modular reductions of the values overflowing 128 bits. Since the modular reduction is over $2^{130} - 5$, requiring 130 bits, and the limbs are 32 bits, the closest multiple is 128, thus a shift of 2 bits to the right is required. The modular reduction is possible due to the fact that 2^{130} is congruent with 5:

$$2^{130} \equiv 5 \pmod{2^{130} - 5}$$

hence why choosing a prime that is of the form $2^n - q$, with q being a small number (such as $2^{130} - 5$), is important because it allows modular reduction to be performed by multiplying by 5 (**n.b.** this isn't a full modular reduction by $2^{130} - 5$, this one can be delayed until the very end of the MAC calculation).

2.2 Limb size

As explained before (2.1), h and r are divided in 32 bit blocks called limbs and subsequently multiplied via schoolbook multiplication. There is a caviat in this process, if a h limb spans 32 bits, a multiplication will cause an overflow of a 64 bit register thus, it will make it imperative to perform carry propagation in each multiplication, hindering performance significantly. To prevent this from happening, Poly1305 clears 22 bits from r in the following manner:

```
r[0] = r[0] & 0x0fffffff
r[2] = r[2] & 0x0ffffffc
r[3] = r[3] & 0x0ffffffc
r[4] = r[4] & 0x0ffffffc
```

Thus each r limb will have, at most, 28 bits set (32-4). As a consequence, even if h limbs span 32 bits, a multiplication will only take up 60 bits (28+32).

After processing the entire message (i.e all it's blocks) the value k is added and a final full modular reduction is performed:

$$mac = (h + k) \pmod{2^{130} - 5}$$

and the result is the MAC of the message.

The full modular reduction is just a matter of checking whether $h + k$ exceeds $2^{130} - 5$, and subtracting $2^{130} - 5$ if it is.

3 Jasmin Poly1305 Implementation

Let's now examine an implementation of the Poly1305 using Jasmin. Jasmin is a framework for developing cryptographic software inspired by qhasm, however Jasmin uses Coq proof assistant to formally verify the (assembly) code generated by the (Jasmin) compiler, providing high *assurance* high performance cryptographic code [1]. The function that represents the entry point for the implementation has the following signature:

```
poly1305_ref3(reg u64 out, reg u64 in, reg u64 inlen, re
```

This function takes in as parameters `out`, `in`, `k` which are (64 bit) pointers to the output, input and 256 bit secret location in memory respectively. The `inlen` parameter is self-explanatory, holding the length of the input.

3.1 Setup

The parameters used in Poly1305 are loaded and initialized by calling

```
fn poly1305_ref3_setup(reg u64 k) -> reg u64[3], reg u64
```

which returns h initialized as 0, r , $r54$ and the pointer to the value of k . Using the parameter `k`, the value of r is loaded and the limb reduction $((r >> 2) * 5)$ is precalculated and stored in `r54`:

```
r = load(k);
r[0] &= 0xffffffffc0ffffff;
r[1] &= 0xffffffffc0ffffff;
r54 = r[1];
r54 >>= 2;
r54 += r[1];
return r, r54; // r54 = r[1] * 5/4;
```

3.2 MAC Calculation

4 Conclusion

References

- [1] José Bacelar Almeida et al. “Jasmin: High-Assurance and High-Speed Cryptography”. In: Oct. 2017, pp. 1807–1823. DOI: 10.1145/3133956.3134078.
- [2] Sean Gulley et al. *Intel ® SHA Extensions New Instructions Supporting the Secure Hash Algorithm on Intel ® Architecture Processors*. URL: <https://software.intel.com/sites/default/files/article/402097/intel-sha-extensions-white-paper.pdf>. 2013.