## Chapter 27

## Problems & Exercises

- 1
- 1/1.333 = 0.750
- 3.
- 1.49, Polystyrene
- 5.
- 0.877 glass to water
- 6.
- $0.516^{\circ}$
- 8.
- $1.22\times10^{-6}~\mathrm{m}$
- 10.
- $600~\mathrm{nm}$
- 12.
- $2.06^{\circ}$
- 14.
- 1200 nm (not visible)
- 16.
- (a) 760 nm
- (b) 1520 nm
- 18.

For small angles  $\sin \theta - \tan \theta \approx \theta$  (in radians).

For two adjacent fringes we have,

$$d\,\sin\,\theta_{\rm m}=m\lambda$$

and

$$d\,\sin\,\theta_{\mathrm{m}+1} = (m+1)\lambda$$

Subtracting these equations gives

$$egin{aligned} d(\sin heta_{ ext{m}+1} - \sin heta_{ ext{m}}) &= [(m+1) - m] \lambda \ d( heta_{ ext{m}+1} - heta_{ ext{m}}) &= \lambda \ an heta_{ ext{m}} &= rac{y_{ ext{m}}}{x} pprox heta_{ ext{m}} \Rightarrow dig(rac{y_{ ext{m}+1}}{x} - rac{y_{ ext{m}}}{x}ig) &= \lambda \ drac{\Delta y}{x} &= \lambda \Rightarrow \Delta y = rac{x\lambda}{d} \end{aligned}$$

20.

450 nm

21.

 $5.97^{\circ}$ 

23.

 $8.99\times 10^3$ 

25.

707 nm

27.

(a) 
$$11.8^{\circ}$$
,  $12.5^{\circ}$ ,  $14.1^{\circ}$ ,  $19.2^{\circ}$ 

$$_{
m (b)}\ 24.2^{
m o}\,,\ 25.7^{
m o}\,,\ 29.1^{
m o}\,,\ 41.0^{
m o}$$

(c) Decreasing the number of lines per centimeter by a factor of x means that the angle for the x-order maximum is the same as the original angle for the first-order maximum.

29.

 $589.1~\mathrm{nm}$  and  $589.6~\mathrm{nm}$ 

31.

 $28.7^{\circ}$ 

33.

43.2

35.

90.0

37.

- (a) The longest wavelength is 333.3 nm, which is not visible.
- (b) 333 nm (UV)
- (c)  $6.58\times10^3~\mathrm{cm}$

39.

 $1.13 \times 10^{-2} \text{ m}$ 

41.

- (a) 42.3 nm
- (b) Not a visible wavelength

The number of slits in this diffraction grating is too large. Etching in integrated circuits can be done to a resolution of 50 nm, so slit separations of 400 nm are at the limit of what we can do today. This line spacing is too small to produce diffraction of light.

43.

- (a) 33.4
- (b) No

45.

- (a)  $1.35 \times 10^{-6}$  m
- (b) 69.9

47.

750 nm

49.

- (a)  $9.04^{\circ}$
- (b) 12

51.

- (a)  $0.0150^{\circ}$
- (b) 0.262 mm
- (c) This distance is not easily measured by human eye, but under a microscope or magnifying glass it is quite easily measurable.

53.

- (a) 30.1
- (b) 48.7
- (c) No
- (d)  $2\theta_1=(2)(14.5^{\rm o})=29^{\rm o},\ \theta_2-\theta_1=30.05^{\rm o}-14.5=15.56^{\rm o}.$  Thus,  $29^{\rm o}\approx(2)(15.56^{\rm o})=31.1.$

55.

23.6 and 53.1

57.

(	a)	1.63	X	$10^{-4}$	rac
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(b) 326 ly

59.

 $1.46 \times 10^{-5} \text{ rad}$ 

61.

(a) 
$$3.04 \times 10^{-7}$$
 rad

(b) Diameter of 235 m

63.

 $5.15~\mathrm{cm}$ 

65.

- (a) Yes. Should easily be able to discern.
- (b) The fact that it is just barely possible to discern that these are separate bodies indicates the severity of atmospheric aberrations.

70.

532 nm (green)

72.

83.9 nm

74.

620 nm (orange)

76.

 $380~\mathrm{nm}$ 

78.

 $33.9~\mathrm{nm}$ 

80.

 $4.42 \times 10^{-5} \text{ m}$ 

82.

The oil film will appear black, since the reflected light is not in the visible part of the spectrum.

84.

45.0

86.

$$45.7~\mathrm{mW/m}^2$$

88.

90.0%

90.

 $I_0$ 

92.

48.8

94.

41.2

96.

- (a) 1.92, not diamond (Zircon)
- (b) 55.2

98.

$$B_2 = 0.707\ B_1$$

100.

(a) 
$$2.07 \times 10^{-2} \, {}^{\circ}\text{C/s}$$

(b) Yes, the polarizing filters get hot because they absorb some of the lost energy from the sunlight.

101.

(a) 
$$\sin \theta = \frac{4.00 \times 10^{-7}}{10^{-6}} = 0.400 \ \theta = 0.400 = 23.6^{\circ}$$

(b) 
$${\rm sin}\theta = \frac{(2)(4.00\times 10^{-7})}{10^{-6}}0.800~\theta = 0.800 = 53.1^\circ$$

(c) 
$$\sin\!23.9^\circ = \frac{x}{10^{-6}~\mathrm{cm}}~x = \sin\!23.9^\circ (10^{-6}) = 4.05 \times 10^{-7} = 405~\mathrm{nm}$$

(d) 
$$\sin \theta = \frac{4.00 \times 10^{-7}}{2.00 \times 10^{-6}} = 0.200 \ \theta = 0.200 = 11.5^{\circ}$$

(e) No.