

PHYS12 CH:6 The Art of Falling Forever

Circular Motion and Rotation

Mr. Gullo

December 2025

Outline

- 1 Introduction
- 2 Angle of Rotation and Angular Velocity
- 3 Uniform Circular Motion
- 4 Rotational Motion
- 5 Summary

The Mystery

How do you move forward
while constantly turning?

The Mystery

How do you move forward
while constantly turning?

From Formula 1 cars screaming around curves to the Moon circling Earth...

The Mystery

How do you move forward
while constantly turning?

From Formula 1 cars screaming around curves to the Moon circling Earth...

All require a force toward the center.

Falling Forever



Figure: Formula 1 car in circular motion

Falling Forever



Figure: Formula 1 car in circular motion

The Mental Model

A satellite in orbit is falling toward Earth but moving fast enough sideways to keep missing it.

Learning Objectives

By the end of this section, you will be able to:

- **6.1:** Describe the angle of rotation and relate it to its linear counterpart

Learning Objectives

By the end of this section, you will be able to:

- **6.1:** Describe the angle of rotation and relate it to its linear counterpart
- **6.1:** Describe angular velocity and relate it to its linear counterpart

Learning Objectives

By the end of this section, you will be able to:

- **6.1:** Describe the angle of rotation and relate it to its linear counterpart
- **6.1:** Describe angular velocity and relate it to its linear counterpart
- **6.1:** Solve problems involving angle of rotation and angular velocity

6.1 Two Kinds of Rotation

Circular motion: Object moves in a circular path (race car on track)

6.1 Two Kinds of Rotation

Circular motion: Object moves in a circular path (race car on track)

Spin: Object rotates about its own axis (Earth spinning)

6.1 Two Kinds of Rotation

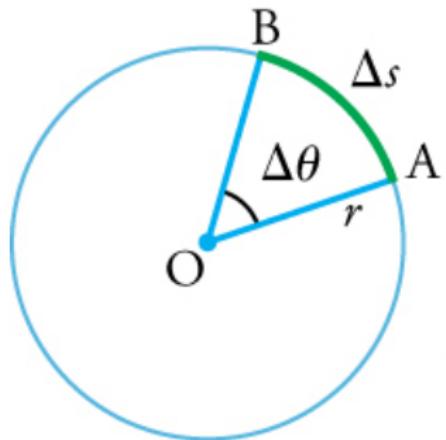
Circular motion: Object moves in a circular path (race car on track)

Spin: Object rotates about its own axis (Earth spinning)

Real-World Examples

- Earth spins on its axis (spin) AND orbits the Sun (circular motion)
- Your car tire spins (spin) while the car follows a curve (circular motion)

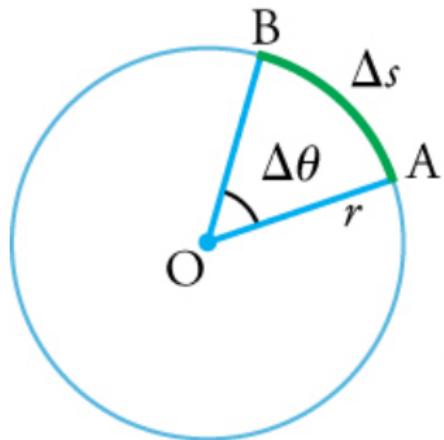
6.1 Angle of Rotation



$$\Delta\theta = \frac{\Delta s}{r}$$

Figure: Arc length and radius

6.1 Angle of Rotation



$$\Delta\theta = \frac{\Delta s}{r}$$

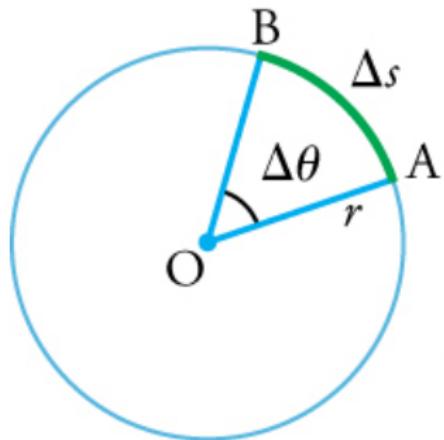
Universal Law: Angle of Rotation

$$\Delta\angle\theta = \frac{\Delta s}{r}$$

Angle equals arc length divided by radius

Figure: Arc length and radius

6.1 Angle of Rotation



$$\Delta\theta = \frac{\Delta s}{r}$$

Measured in **radians** (rad)

Figure: Arc length and radius

Universal Law: Angle of Rotation

$$\Delta\theta = \frac{\Delta s}{r}$$

Angle equals arc length divided by radius

6.1 Radians vs Degrees

The Conversion

$$1 \text{ revolution} = 2\pi \text{ rad} = 360^\circ$$

6.1 Radians vs Degrees

The Conversion

$$1 \text{ revolution} = 2\pi \text{ rad} = 360^\circ$$

Common conversions:

- $\frac{\pi}{2}$ rad = 90°

6.1 Radians vs Degrees

The Conversion

$$1 \text{ revolution} = 2\pi \text{ rad} = 360^\circ$$

Common conversions:

- $\frac{\pi}{2}$ rad = 90°
- π rad = 180°

6.1 Radians vs Degrees

The Conversion

$$1 \text{ revolution} = 2\pi \text{ rad} = 360^\circ$$

Common conversions:

- $\frac{\pi}{2}$ rad = 90°
- π rad = 180°
- 1 rad $\approx 57.3^\circ$

6.1 Radians vs Degrees

The Conversion

$$1 \text{ revolution} = 2\pi \text{ rad} = 360^\circ$$

Common conversions:

- $\frac{\pi}{2}$ rad = 90°
- π rad = 180°
- $1 \text{ rad} \approx 57.3^\circ$

Why Radians?

Radians simplify equations in physics. Degrees are arbitrary - radians are natural.

6.1 Angular Velocity

Universal Law: **Angular Velocity**

$$\omega = \frac{\Delta\angle\theta}{\Delta t}$$

Angular velocity equals change in \angle angle divided by change in time

6.1 Angular Velocity

Universal Law: **Angular Velocity**

$$\omega = \frac{\Delta\angle\theta}{\Delta t}$$

Angular velocity equals change in \angle angle divided by change in time

Units: radians per second (rad/s)

6.1 Angular Velocity

Universal Law: **Angular Velocity**

$$\omega = \frac{\Delta\angle\theta}{\Delta t}$$

Angular velocity equals change in \angle angle divided by change in time

Units: radians per second (rad/s)

Direction:

- Counterclockwise: positive (out of page toward you)
- Clockwise: negative (into page away from you)

6.1 Connecting Spinning to Moving

The Bridge Equation

$$v = r\omega$$

Tangential velocity equals radius times angular velocity

6.1 Connecting Spinning to Moving

The Bridge Equation

$$v = r\omega$$

Tangential velocity equals radius times angular velocity

The Mental Model

Points farther from the center move faster linearly, but all points have the same angular velocity.

6.1 Connecting Spinning to Moving

The Bridge Equation

$$v = r\omega$$

Tangential velocity equals radius times angular velocity

The Mental Model

Points farther from the center move faster linearly, but all points have the same angular velocity.

Example: CD spinning - outer edge moves faster than inner part, but both complete one revolution in same time.

6.1 Why Car Tires Matter

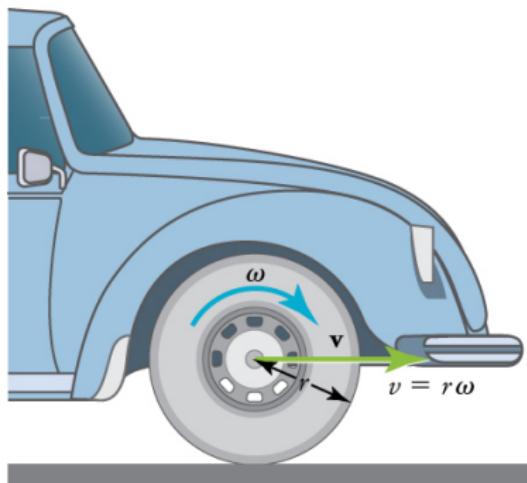


Figure: Car tire rolling

6.1 Why Car Tires Matter

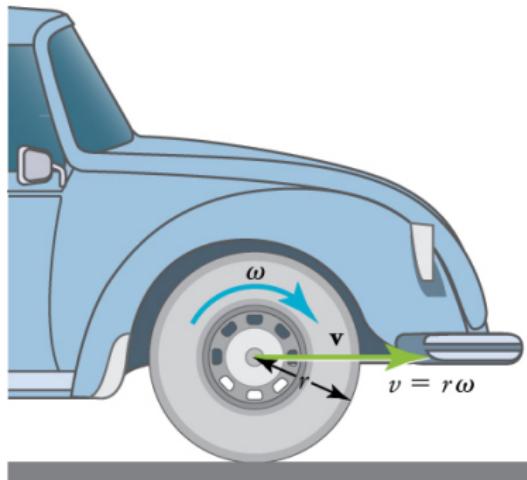


Figure: Car tire rolling

Large ω means large v because $v = r\omega$

6.1 Why Car Tires Matter

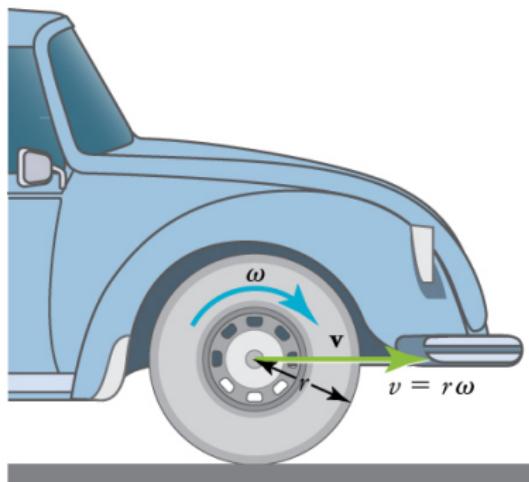


Figure: Car tire rolling

Large ω means large v because $v = r\omega$

Larger **radius** tire at same ω produces greater v

Attempt: Clock Tower Angle

The Challenge (3 min, silent)

A clock tower has a radius of 1.0 m. The hour hand moves from 12 p.m. to 3 p.m.

Given:

- Radius $r = 1.0$ m
- Time: 12 to 3 (quarter rotation)

Find:

- ① \angle Angle of rotation in radians
- ② Arc length along outer edge

Can you decode this rotation? Work silently.

Compare: Clock Tower

Turn and talk (2 min):

- ① What fraction of a full rotation does the hour hand make from 12 to 3?
- ② How many radians in a full circle?
- ③ What equation connects arc length to angle?

Compare: Clock Tower

Turn and talk (2 min):

- ① What fraction of a full rotation does the hour hand make from 12 to 3?
- ② How many radians in a full circle?
- ③ What equation connects arc length to angle?

Name wheel: One pair share your approach (not your answer).

Reveal: The Geometry of Time

Self-correct in a different color:

Part (a): From 12 to 3 is $\frac{1}{4}$ of full rotation

Reveal: The Geometry of Time

Self-correct in a different color:

Part (a): From 12 to 3 is $\frac{1}{4}$ of full rotation

Full rotation = 2π rad, so $\angle \text{angle} = 1$ —————

$$4 \times 2\pi = \boxed{\frac{\pi}{2} \text{ rad}}$$

Reveal: The Geometry of Time

Self-correct in a different color:

Part (a): From 12 to 3 is $\frac{1}{4}$ of full rotation

Full rotation = 2π rad, so $\angle \text{angle} = 1$ —————

$$4 \times 2\pi = \boxed{\frac{\pi}{2} \text{ rad}}$$

Part (b): Use $\Delta s = r\Delta\theta$

Reveal: The Geometry of Time

Self-correct in a different color:

Part (a): From 12 to 3 is $\frac{1}{4}$ of full rotation

Full rotation = 2π rad, so $\angle \text{angle} = 1$ —————

$$4 \times 2\pi = \boxed{\frac{\pi}{2} \text{ rad}}$$

Part (b): Use $\Delta s = r\Delta\theta$

$$\Delta s = (1.0 \text{ m}) \left(\frac{\pi}{2} \text{ rad} \right) = \boxed{1.6 \text{ m}}$$

Reveal: The Geometry of Time

Self-correct in a different color:

Part (a): From 12 to 3 is $\frac{1}{4}$ of full rotation

Full rotation = 2π rad, so $\angle \text{angle} = 1$ —————

$$4 \times 2\pi = \boxed{\frac{\pi}{2} \text{ rad}}$$

Part (b): Use $\Delta s = r\Delta\theta$

$$\Delta s = (1.0 \text{ m}) \left(\frac{\pi}{2} \text{ rad} \right) = \boxed{1.6 \text{ m}}$$

Check: Arc length is less than circumference ($2\pi r \approx 6.3 \text{ m}$). Reasonable!

Attempt: Spinning Car Tire

The Challenge (3 min, silent)

A car tire has radius 0.300 m and the car travels at 15.0 m/s (about 54 km/h).

Given:

- Radius $r = 0.300 \text{ m}$
- Tangential velocity $v = 15.0 \text{ m/s}$

Find: Angular velocity ω of the tire in rad/s

How fast is the tire spinning?

Compare: Tire Speed

Turn and talk (2 min):

- ① What equation connects linear and angular velocity?
- ② How did you rearrange it to solve for ω ?
- ③ What are the units of your answer?

Compare: Tire Speed

Turn and talk (2 min):

- ① What equation connects linear and angular velocity?
- ② How did you rearrange it to solve for ω ?
- ③ What are the units of your answer?

Name wheel: One pair share your rearrangement strategy.

Reveal: The Spinning Wheel

Self-correct in a different color:

Equation: $v = rw$, so $\omega = \frac{v}{r}$

Reveal: The Spinning Wheel

Self-correct in a different color:

Equation: $v = r\omega$, so $\omega = \frac{v}{r}$

Substitute:

$$\omega = \frac{15.0 \text{ m/s}}{0.300 \text{ m}}$$

Reveal: The Spinning Wheel

Self-correct in a different color:

Equation: $v = rw$, so $\omega = \frac{v}{r}$

Substitute:

$$\omega = \frac{15.0 \text{ m/s}}{0.300 \text{ m}}$$

$$\omega = 50.0 \text{ rad/s}$$

Reveal: The Spinning Wheel

Self-correct in a different color:

Equation: $v = rw$, so $\omega = \frac{v}{r}$

Substitute:

$$\omega = \frac{15.0 \text{ m/s}}{0.300 \text{ m}}$$

$$\omega = 50.0 \text{ rad/s}$$

Check: About 8 revolutions per second (since $2\pi \text{ rad} = 1 \text{ rev}$). Fast but reasonable for highway speed!

Learning Objectives

By the end of this section, you will be able to:

- **6.2:** Describe centripetal acceleration and relate it to linear acceleration

Learning Objectives

By the end of this section, you will be able to:

- **6.2:** Describe centripetal acceleration and relate it to linear acceleration
- **6.2:** Describe centripetal force and relate it to linear force

Learning Objectives

By the end of this section, you will be able to:

- **6.2:** Describe centripetal acceleration and relate it to linear acceleration
- **6.2:** Describe centripetal force and relate it to linear force
- **6.2:** Solve problems involving centripetal acceleration and centripetal force

6.2 The Paradox of Constant Speed

Uniform circular motion: Object travels circular path at constant speed

6.2 The Paradox of Constant Speed

Uniform circular motion: Object travels circular path at constant speed

Civilian View vs. Reality

Civilian: "Constant speed means no acceleration."

Physicist: "Velocity is changing direction, so there IS acceleration."

6.2 The Paradox of Constant Speed

Uniform circular motion: Object travels circular path at constant speed

Civilian View vs. Reality

Civilian: "Constant speed means no acceleration."

Physicist: "Velocity is changing direction, so there IS acceleration."

Acceleration is a change in velocity - magnitude OR direction!

6.2 The Illusion of Being Flung

The Mental Model

When you turn in a car, you feel pushed outward. But no **force** pushes you out - your body wants to go straight (Newton's first law) while the car turns.

6.2 The Illusion of Being Flung

The Mental Model

When you turn in a car, you feel pushed outward. But no **force** pushes you out - your body wants to go straight (Newton's first law) while the car turns.

The Fictional Force

Centrifugal force is not real - it's the illusion created by your inertia resisting the turn.

6.2 The Illusion of Being Flung

The Mental Model

When you turn in a car, you feel pushed outward. But no **force** pushes you out - your body wants to go straight (Newton's first law) while the car turns.

The Fictional Force

Centrifugal force is not real - it's the illusion created by your inertia resisting the turn.

The real **force** is **centripetal** - pulling you inward toward the center!

6.2 Centripetal Acceleration

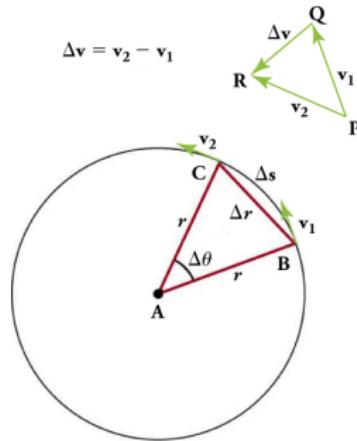


Figure: Velocity changes direction, acceleration points toward center

6.2 Centripetal Acceleration

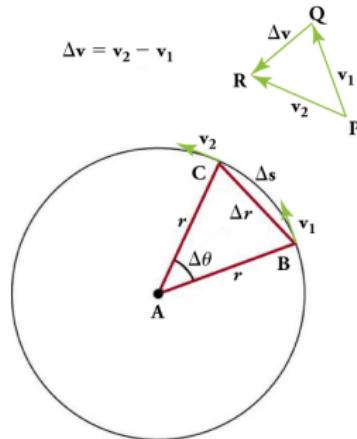


Figure: Velocity changes direction, acceleration points toward center

Universal Law: Centripetal Acceleration

$$a_c = \frac{v^2}{r} \quad \text{or} \quad a_c = r\omega^2$$

6.2 Why Speed Squared Matters

$$a_c = \frac{v^2}{r}$$

6.2 Why Speed Squared Matters

$$a_c = \frac{v^2}{r}$$

Proportional to v^2 : Doubling speed means 4 times the acceleration!

6.2 Why Speed Squared Matters

$$a_c = \frac{v^2}{r}$$

Proportional to v^2 : Doubling speed means 4 times the acceleration!

Example:

- Curve at 50 km/h: moderate acceleration
- Same curve at 100 km/h: 4 times the acceleration

6.2 Why Speed Squared Matters

$$a_c = \frac{v^2}{r}$$

Proportional to v^2 : Doubling speed means 4 times the acceleration!

Example:

- Curve at 50 km/h: moderate acceleration
- Same curve at 100 km/h: 4 times the acceleration

The Warning

This is why speed limits are lower on curves - small speed increase creates huge acceleration increase.

6.2 Centripetal Force

Newton's second law: $F_{\text{net}} = ma$

6.2 Centripetal Force

Newton's second law: $F_{\text{net}} = ma$

For circular motion: $F_{\text{net}} = ma_c$

6.2 Centripetal Force

Newton's second law: $F_{\text{net}} = ma$

For circular motion: $F_{\text{net}} = ma_c$

Universal Law: Centripetal Force

$$F_c = m \frac{v^2}{r}$$

or

$$F_c = mr\omega^2$$

6.2 Centripetal Force

Newton's second law: $F_{\text{net}} = ma$

For circular motion: $F_{\text{net}} = ma_c$

Universal Law: Centripetal Force

$$F_c = m \frac{v^2}{r}$$

or

$$F_c = mr\omega^2$$

Direction: Always toward the center of rotation

6.2 Sources of Centripetal Force

Centripetal force can be provided by:

- **Friction:** Car tires on road

6.2 Sources of Centripetal Force

Centripetal force can be provided by:

- **Friction:** Car tires on road
- **Tension:** String on tetherball

6.2 Sources of Centripetal Force

Centripetal force can be provided by:

- **Friction:** Car tires on road
 - **Tension:** String on tetherball
 - **Gravity:** Moon orbiting Earth

6.2 Sources of Centripetal Force

Centripetal **force** can be provided by:

- **Friction:** Car tires on road
- **Tension:** String on tetherball
- **Gravity:** Moon orbiting Earth
- **Normal force:** Roller coaster on loop

6.2 Sources of Centripetal Force

Centripetal **force** can be provided by:

- **Friction:** Car tires on road
- **Tension:** String on tetherball
- **Gravity:** Moon orbiting Earth
- **Normal force:** Roller coaster on loop

The Mental Model

Centripetal **force** isn't a new kind of **force** - it's whatever **force** points toward the center and causes circular motion.

Attempt: Car on Curve

The Challenge (3 min, silent)

A 900 kg car rounds a curve with radius 600 m at speed 25.0 m/s.

Given:

- Mass $m = 900 \text{ kg}$
- Radius $r = 600 \text{ m}$
- Speed $v = 25.0 \text{ m/s}$

Find: Centripetal force required to keep car on curve

How much force do the tires provide?

Compare: Car Force

Turn and talk (2 min):

- ① What equation did you use for centripetal **force**?
- ② Did you remember to square the **velocity**?
- ③ What **force** provides the centripetal **force** for a car?

Compare: Car Force

Turn and talk (2 min):

- ① What equation did you use for centripetal **force**?
- ② Did you remember to square the **velocity**?
- ③ What **force** provides the centripetal **force** for a car?

Name wheel: One pair share your equation and reasoning.

Reveal: The Force That Turns

Self-correct in a different color:

Equation: $F_c = m \frac{v^2}{r}$

Reveal: The Force That Turns

Self-correct in a different color:

Equation: $F_c = m \frac{v^2}{r}$

Substitute:

$$F_c = \frac{(900 \text{ kg})(25.0 \text{ m/s})^2}{600 \text{ m}}$$

Reveal: The Force That Turns

Self-correct in a different color:

Equation: $F_c = m \frac{v^2}{r}$

Substitute:

$$F_c = \frac{(900 \text{ kg})(25.0 \text{ m/s})^2}{600 \text{ m}}$$

$$F_c = \frac{(900)(625)}{600} = \boxed{938 \text{ N}}$$

Reveal: The Force That Turns

Self-correct in a different color:

Equation: $F_c = m \frac{v^2}{r}$

Substitute:

$$F_c = \frac{(900 \text{ kg})(25.0 \text{ m/s})^2}{600 \text{ m}}$$

$$F_c = \frac{(900)(625)}{600} = \boxed{938 \text{ N}}$$

Check: About 940 N - this is the friction **force** between tires and road.
Without it, car slides straight!

Attempt: Acceleration Comparison

The Challenge (3 min, silent)

A car follows a curve of radius 500 m at speed 25.0 m/s.

Given:

- Radius $r = 500 \text{ m}$
- Speed $v = 25.0 \text{ m/s}$
- $g = 9.80 \text{ m/s}^2$

Find:

- ① Centripetal acceleration
- ② Express as fraction of g

How does turning compare to falling?

Compare: Acceleration Scale

Turn and talk (2 min):

- ① What equation did you use for centripetal **acceleration**?
- ② How did you express it as a fraction of g ?
- ③ Is the **acceleration** large or small compared to gravity?

Compare: Acceleration Scale

Turn and talk (2 min):

- ① What equation did you use for centripetal **acceleration**?
- ② How did you express it as a fraction of g ?
- ③ Is the **acceleration** large or small compared to gravity?

Name wheel: One pair share your comparison method.

Reveal: Comparing to Gravity

Self-correct in a different color:

Calculate a_c :

$$a_c = \frac{v^2}{r} = \frac{(25.0 \text{ m/s})^2}{500 \text{ m}}$$

Reveal: Comparing to Gravity

Self-correct in a different color:

Calculate a_c :

$$a_c = \frac{v^2}{r} = \frac{(25.0 \text{ m/s})^2}{500 \text{ m}}$$

$$a_c = \frac{625}{500} = \boxed{1.25 \text{ m/s}^2}$$

Reveal: Comparing to Gravity

Self-correct in a different color:

Calculate a_c :

$$a_c = \frac{v^2}{r} = \frac{(25.0 \text{ m/s})^2}{500 \text{ m}}$$

$$a_c = \frac{625}{500} = \boxed{1.25 \text{ m/s}^2}$$

Compare to g :

$$\frac{a_c}{g} = \frac{1.25}{9.80} = 0.128 \quad \Rightarrow \quad \boxed{a_c = 0.13g}$$

Reveal: Comparing to Gravity

Self-correct in a different color:

Calculate a_c :

$$a_c = \frac{v^2}{r} = \frac{(25.0 \text{ m/s})^2}{500 \text{ m}}$$

$$a_c = \frac{625}{500} = \boxed{1.25 \text{ m/s}^2}$$

Compare to g :

$$\frac{a_c}{g} = \frac{1.25}{9.80} = 0.128 \quad \Rightarrow \quad \boxed{a_c = 0.13g}$$

Revelation: Gentle highway curve at moderate **speed** produces about 1/10th the **acceleration** of gravity!

Learning Objectives

By the end of this section, you will be able to:

- **6.3:** Describe rotational kinematic variables and relate them to linear counterparts

Learning Objectives

By the end of this section, you will be able to:

- **6.3:** Describe rotational kinematic variables and relate them to linear counterparts
- **6.3:** Describe torque and lever arm

Learning Objectives

By the end of this section, you will be able to:

- **6.3:** Describe rotational kinematic variables and relate them to linear counterparts
- **6.3:** Describe torque and lever arm
- **6.3:** Solve problems involving torque and rotational kinematics

6.3 When Spin Changes

So far: constant angular velocity

6.3 When Spin Changes

So far: constant angular velocity

But what if spin changes?

- Figure skater pulls arms in - spins faster

6.3 When Spin Changes

So far: constant angular velocity

But what if spin changes?

- Figure skater pulls arms in - spins faster
- Child pushes merry-go-round - starts rotating

6.3 When Spin Changes

So far: constant angular velocity

But what if spin changes?

- Figure skater pulls arms in - spins faster
- Child pushes merry-go-round - starts rotating
- CD player stops - disc slows to halt

6.3 When Spin Changes

So far: constant angular velocity

But what if spin changes?

- Figure skater pulls arms in - spins faster
- Child pushes merry-go-round - starts rotating
- CD player stops - disc slows to halt

Universal Law: **Angular Acceleration**

$$\alpha = \frac{\Delta\omega}{\Delta t}$$

Rate of change of **angular velocity**

6.3 Connecting Linear and Angular Acceleration

The Bridge

$$a = r\alpha \quad \text{or} \quad \alpha = \frac{a}{r}$$

6.3 Connecting Linear and Angular Acceleration

The Bridge

$$a = r\alpha \quad \text{or} \quad \alpha = \frac{a}{r}$$

Tangential acceleration: Linear acceleration along the circle's edge

6.3 Connecting Linear and Angular Acceleration

The Bridge

$$a = r\alpha \quad \text{or} \quad \alpha = \frac{a}{r}$$

Tangential acceleration: Linear acceleration along the circle's edge

The Mental Model

Greater angular acceleration means greater tangential acceleration. Points farther from center have larger tangential acceleration for same α .

6.3 Rotational Kinematics Equations

Linear

$$v = v_0 + at$$

$$x = x_0 + v_0 t + \frac{1}{2}at^2$$

$$v^2 = v_0^2 + 2a\Delta x$$

Rotational

$$\omega = \omega_0 + \alpha t$$

$$\angle\theta = \angle\theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$$

$$\omega^2 = \omega_0^2 + 2\alpha\Delta\angle\theta$$

6.3 Rotational Kinematics Equations

Linear

$$v = v_0 + at$$

$$x = x_0 + v_0 t + \frac{1}{2}at^2$$

$$v^2 = v_0^2 + 2a\Delta x$$

Rotational

$$\omega = \omega_0 + \alpha t$$

$$\angle\theta = \angle\theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$$

$$\omega^2 = \omega_0^2 + 2\alpha\Delta\angle\theta$$

The Pattern

Every linear kinematics equation has a rotational analog. Just swap

$x \rightarrow \angle\theta$, $v \rightarrow \omega$, $a \rightarrow \alpha$!

6.3 The Rotational Version of Force

Force causes linear acceleration

What causes angular acceleration?

6.3 The Rotational Version of Force

Force causes linear acceleration

What causes angular acceleration?

Universal Law: Torque

$$\tau = rF \sin \angle\theta$$

Torque equals lever arm times force times sine of \angle angle

6.3 The Rotational Version of Force

Force causes linear acceleration

What causes angular acceleration?

Universal Law: Torque

$$\tau = rF \sin \angle\theta$$

Torque equals lever arm times force times sine of \angle angle

Units: N·m (Newton-meters)

Direction: Same as the angular acceleration it produces

6.3 Maximizing Torque

$$\tau = rF \sin \angle\theta$$

6.3 Maximizing Torque

$$\tau = rF \sin \angle\theta$$

To maximize torque:

- Apply force far from pivot (large r)

6.3 Maximizing Torque

$$\tau = rF \sin \angle\theta$$

To maximize torque:

- Apply force far from pivot (large r)
- Apply force perpendicular to lever arm ($\angle\theta = 90^\circ$, so $\sin \angle\theta = 1$)

6.3 Maximizing Torque

$$\tau = rF \sin \angle\theta$$

To maximize torque:

- Apply force far from pivot (large r)
- Apply force perpendicular to lever arm ($\angle\theta = 90^\circ$, so $\sin \angle\theta = 1$)
- Apply larger force (large F)

6.3 Maximizing Torque

$$\tau = rF \sin \angle\theta$$

To maximize torque:

- Apply force far from pivot (large r)
- Apply force perpendicular to lever arm ($\angle\theta = 90^\circ$, so $\sin \angle\theta = 1$)
- Apply larger force (large F)

Real-World Applications

- Door handle placed far from hinges
- Wrench with long handle
- Teeter-totter balanced by distance and weight

Attempt: Fishing Reel

The Challenge (3 min, silent)

A fishing reel spins at $\omega_0 = 220 \text{ rad/s}$. Fisherman applies brake creating angular acceleration $\alpha = -300 \text{ rad/s}^2$.

Given:

- Initial $\omega_0 = 220 \text{ rad/s}$
- Final $\omega = 0$ (stops)
- $\alpha = -300 \text{ rad/s}^2$

Find: Time t for reel to stop

How long does it take?

Compare: Fishing Reel

Turn and talk (2 min):

- ① Which rotational kinematics equation did you choose?
- ② How did you solve for time t ?
- ③ Why is α negative?

Compare: Fishing Reel

Turn and talk (2 min):

- ① Which rotational kinematics equation did you choose?
- ② How did you solve for time t ?
- ③ Why is α negative?

Name wheel: One pair share your equation choice and reasoning.

Reveal: Stopping the Spin

Self-correct in a different color:

Equation: $\omega = \omega_0 + \alpha t$

Reveal: Stopping the Spin

Self-correct in a different color:

Equation: $\omega = \omega_0 + \alpha t$

Solve for t :

$$t = \frac{\omega - \omega_0}{\alpha}$$

Reveal: Stopping the Spin

Self-correct in a different color:

Equation: $\omega = \omega_0 + \alpha t$

Solve for t :

$$t = \frac{\omega - \omega_0}{\alpha}$$

Substitute:

$$t = \frac{0 - 220 \text{ rad/s}}{-300 \text{ rad/s}^2} = \frac{-220}{-300}$$

Reveal: Stopping the Spin

Self-correct in a different color:

Equation: $\omega = \omega_0 + \alpha t$

Solve for t :

$$t = \frac{\omega - \omega_0}{\alpha}$$

Substitute:

$$t = \frac{0 - 220 \text{ rad/s}}{-300 \text{ rad/s}^2} = \frac{-220}{-300}$$

$$t = 0.733 \text{ s}$$

Reveal: Stopping the Spin

Self-correct in a different color:

Equation: $\omega = \omega_0 + \alpha t$

Solve for t :

$$t = \frac{\omega - \omega_0}{\alpha}$$

Substitute:

$$t = \frac{0 - 220 \text{ rad/s}}{-300 \text{ rad/s}^2} = \frac{-220}{-300}$$

$$t = 0.733 \text{ s}$$

Insight: Less than one second because the angular acceleration is quite large!

Attempt: Merry-Go-Round Torque

The Challenge (3 min, silent)

A man pushes a merry-go-round with force 250 N at the edge, perpendicular to the radius of 1.50 m.

Given:

- Force $F = 250 \text{ N}$
- Lever arm $r = 1.50 \text{ m}$
- $\angle \text{Angle} \theta = 90^\circ$ (perpendicular)

Find: Torque τ produced

How effective is his push?

Compare: Torque Calculation

Turn and talk (2 min):

- ① What is the value of $\sin 90^\circ$?
- ② How does this simplify the torque equation?
- ③ Why did the man push at the edge and perpendicular?

Compare: Torque Calculation

Turn and talk (2 min):

- ① What is the value of $\sin 90^\circ$?
- ② How does this simplify the torque equation?
- ③ Why did the man push at the edge and perpendicular?

Name wheel: One pair explain why perpendicular force maximizes torque.

Reveal: The Power of Position

Self-correct in a different color:

Equation: $\tau = rF \sin \angle\theta$

Reveal: The Power of Position

Self-correct in a different color:

Equation: $\tau = rF \sin \angle\theta$

Substitute: $\angle\theta = 90^\circ$, so $\sin 90^\circ = 1$

Reveal: The Power of Position

Self-correct in a different color:

Equation: $\tau = rF \sin \angle\theta$

Substitute: $\angle\theta = 90^\circ$, so $\sin 90^\circ = 1$

$$\tau = (1.50 \text{ m})(250 \text{ N})(1)$$

Reveal: The Power of Position

Self-correct in a different color:

Equation: $\tau = rF \sin \angle\theta$

Substitute: $\angle\theta = 90^\circ$, so $\sin 90^\circ = 1$

$$\tau = (1.50 \text{ m})(250 \text{ N})(1)$$

$$\boxed{\tau = 375 \text{ N} \cdot \text{m}}$$

Reveal: The Power of Position

Self-correct in a different color:

Equation: $\tau = rF \sin \angle\theta$

Substitute: $\angle\theta = 90^\circ$, so $\sin 90^\circ = 1$

$$\tau = (1.50 \text{ m})(250 \text{ N})(1)$$

$$\boxed{\tau = 375 \text{ N} \cdot \text{m}}$$

Strategy: Man maximized **torque** by pushing perpendicular at the outer edge!

What You Now Know

The Revelations

- ① Radians are natural units - \angle angles from circle geometry

What You Now Know

The Revelations

- ① Radians are natural units - \angle angles from circle geometry
- ① $v = r\omega$ connects spinning to moving

What You Now Know

The Revelations

- ① Radians are natural units - \angle angles from circle geometry
- ① $v = rw$ connects spinning to moving
- ② Circular motion requires acceleration toward center

What You Now Know

The Revelations

- ① Radians are natural units - \angle angles from circle geometry
- ② $v = rw$ connects spinning to moving
- ③ Circular motion requires acceleration toward center
- ④ Centripetal force $F_c = \frac{mv^2}{r}$ keeps objects turning

What You Now Know

The Revelations

- ① Radians are natural units - \angle angles from circle geometry
- ② $v = r\omega$ connects spinning to moving
- ③ Circular motion requires acceleration toward center
- ④ Centripetal force $F_c = \frac{mv^2}{r}$ keeps objects turning
- ⑤ Rotational kinematics mirrors linear kinematics

What You Now Know

The Revelations

- ① Radians are natural units - \angle angles from circle geometry
- ② $v = rw$ connects spinning to moving
- ③ Circular motion requires acceleration toward center
- ④ Centripetal force $F_c = \frac{mv^2}{r}$ keeps objects turning
- ⑤ Rotational kinematics mirrors linear kinematics
- ⑥ Torque $\tau = rF \sin \angle\theta$ is the rotational force

Key Equations

$$\Delta\theta = \frac{\Delta s}{r} \quad (\text{angle of rotation}) \quad (1)$$

$$\omega = \frac{\Delta\theta}{\Delta t} \quad (\text{angular velocity}) \quad (2)$$

$$v = r\omega \quad (\text{tangential velocity}) \quad (3)$$

$$a_c = \frac{v^2}{r} = r\omega^2 \quad (\text{centripetal acceleration}) \quad (4)$$

$$F_c = m\frac{v^2}{r} = mr\omega^2 \quad (\text{centripetal force}) \quad (5)$$

$$\alpha = \frac{\Delta\omega}{\Delta t} \quad (\text{angular acceleration}) \quad (6)$$

$$a = r\alpha \quad (\text{tangential acceleration}) \quad (7)$$

$$\tau = rF \sin \theta \quad (\text{torque}) \quad (8)$$

Homework

Complete the assigned problems
posted on the LMS