

Latihan Aljabar Boolean

1. Nyatakan $f(a, b, c) = ((ab)'c)'((a'+c)(b'+d'))'$ dalam bentuk kanonik SOP

2. Cari komplemen dari fungsi $f(w, x, y, z) = x'z + w'xy' + wyz + w'xy$ dengan cara:

a. deMorgan

b. Dualitas

3. Sederhanakan fungsi Boolean berikut secara aljabar

a. $xy + x'z + yz$

b. $(x+y)(x'+z)(y+z)$

4. Minimisasi fungsi-fungsi Boolean berikut dengan metode Peta Karnaugh, dalam bentuk baku SOP dan bentuk baku POS

a. $f(x, y, z) = \sum (2, 5, 6, 7)$

b. $f(x, y, z) = xy + x'y'z + x'yz'$

c. Diberikan table kebenaran:

x	y	z	$f(x, y, z)$
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

$$\begin{aligned} 1 \quad ab &= ab(c + c') \quad \text{jawab} \\ &= abc + abc' \end{aligned}$$

$$\begin{aligned} c &= c(a + a') \\ &= ca + ca' \\ &= c(ab + ab') + ca'(b + b') \\ &= abc + ab'c + a'bc + a'b'c \end{aligned}$$

$$\begin{aligned} a' &= a'(b + b') \\ &= a'b + a'b' \\ &= a'b(c + c') + a'b'(c + c') \\ &= a'bc + a'b'c + a'b'c + a'b'c' \end{aligned}$$

$$\begin{aligned} b' &= b'(a + a') \\ &= ab' + a'b' \\ &= ab'(c + c') + a'b'(c + c') \\ &= ab'c + ab'c' + a'b'c + a'b'c' \end{aligned}$$

$$\begin{aligned} c' &= c'(a + a') \\ &= ac' + a'c' \\ &= ac'(b + b') + a'c'(b + b') \\ &= abc' + ab'c' + a'c'b + a'b'c' \end{aligned}$$

$$\begin{aligned}
 f(a,b,c) &= (cabc + abc')' abc + abc + abc + abc' (-ab'c + ab'c' + ab'c' + ab'c' + ab'c' + ab'c' + ab'c') \\
 &= (cabc + abc')' abc + abc + abc + abc' (ab'c + ab'c' + ab'c' + ab'c' + ab'c' + ab'c' + ab'c') \\
 &= (ab'c' + ab'c' + ab'c' + ab'c' + ab'c' + ab'c' + ab'c')' (ab'c + ab'c' + ab'c' + ab'c' + ab'c' + ab'c' + ab'c') \\
 &= ab'c + ab'c' + ab'c + ab'c + ab'c + ab'c + ab'c \\
 &= ab'c + ab'c' + ab'c + ab'c + ab'c + ab'c + ab'c
 \end{aligned}$$

$$\begin{aligned}
 f(a,b,c) &= m_7 + m_6 + m_5 + m_3 + m_1 + m_2 \\
 &= \sum(1, 2, 3, 5, 6, 7)
 \end{aligned}$$

$$2. f(w, x, y, z) = x'z + w'xy' + wyz + w'xy$$

2. de Morgan

$$f(w, x, y, z) = (x + z') (w + x' + y) (w' + y' + z) (w + x')$$

b. dualize

$$\begin{aligned}
 f(w, x, y, z) &= (x' + z) (w' + x + y') (w + y + z) (w' + x + y) \\
 &= (x + z') (w + x' + y) (w' + y' + z) (w + x' + y) = f
 \end{aligned}$$

$$\begin{aligned}
 3.2. f(x, y, z) &= xy + x'z + yz \\
 &= xy + x'z + yz(x + x') \\
 &= xy + x'z + xyz + x'yz \\
 &= xy + xyz + x'z = x'yz \\
 &= xy(1+z) + x'z(1+y)
 \end{aligned}$$

$$\begin{aligned}
 b. f(x, y, z) &= (x+y)(x'+z)(y+z) \\
 &= x' + (yz) + (y+z)
 \end{aligned}$$

$$4.2. f(x, y, z) = \sum(2, 3, 6, 7)$$

• Petz Kernewh

		$z=0$	$z=1$		
		$m_2 + m_3 + m_6 + m_7$	$m_1 + m_5$		
x	0	$x'y'z'$	$x'y'z$	$x'y'z$	$x'y'z'$
	1	$xy'z'$	$xy'z$	xyz	xyz'
				m_3	m_2
				m_7	m_6
		m_4	m_5	m_3	m_2
		m_4	m_5	m_7	m_6

$$= x'y'z' + x'y'z + xyz' + xyz$$

$$\begin{aligned}
 \bullet \text{ SOP} &= m_2 + m_3 + m_6 + m_7 \\
 &= x'y'z' + x'y'z + xyz' + xyz
 \end{aligned}$$

$$\begin{aligned}
 \bullet \text{ POS} &= M_4 + M_5 + M_1 + M_3 \\
 &= (x+y'+z) \cdot (x+y'+z') \cdot (x'+y+z) \cdot (x'+y+z')
 \end{aligned}$$

b. $f(x, y, z) = xy + x'y'z + x'y z'$

(bentuk belum sempurna maka tinggal dalam kanonik SOP)

• SOP :

$$xy = xy(z + z')$$

$$= xy z + xy z'$$

$$= xy z + xy z' + x'y'z + x'y z'$$

$$= m_7 + m_6 + m_1 + m_2 = \Sigma(1, 2, 6, 7)$$

• Peta Karnaugh

m_0	m_1	m_3	m_2
m_4	m_5	m_7	m_6

$x \backslash yz$	00	01	11	10
0	$x'y'z'$	$x'y'z$	$x'y z$	$x'y z'$
1	$xy'z'$	$xy'z$	$xy z$	$xy z'$

Diagram Karnaugh map with groupings: m_1 (top row, columns 01 and 11), m_2 (top row, column 10), m_7 (bottom row, column 11), m_6 (bottom row, column 10).

$$= m_7 + m_6 + m_1 + m_2$$

$$= xy z + xy z' + x'y'z + x'y z'$$

• POS: $M_2 + M_7 + M_6 + M_1$

$$= (x+y'+z) \cdot (x+y'z) \cdot (x+y'z') \cdot (x+y'z)$$

c. $x \quad y \quad z \quad f(x, y, z)$

0 0 0 0

0 0 1 1

$$\rightarrow m_1 = M_1$$

0 1 0 1

$$\rightarrow m_2 = M_2$$

0 1 1 0

1 0 0 1

$$\rightarrow m_4 = M_4$$

1 0 1 0

1 1 0 0

1 1 1 1

$$\rightarrow m_7 = M_7$$

• Pete Kernigh

m_0	m_1	m_3	m_2
m_4	m_5	m_7	m_6

	y_2	00	01	11	10
0	$x y_2$	$x y_2$	$x y_2$	$x y_2$	$x y_2$
1	$x y_2'$	$x y_2$	$x y_2$	$x y_2$	$x y_2'$
		m_4		m_7	

$$= m_1 + m_2 + m_4 + m_7$$

$$= x' y' z + x' y z' + x y z' + x y z$$

• SOP = $m_1 + m_2 + m_4 + m_7$

$$= x' y' z + x' y z' + x y z' + x y z$$

• POS = $M_0 + M_3 + M_5 + M_6$

$$= (x + y + z') \cdot (x + y' + z) \cdot (x' + y + z) \cdot (x' + y' + z)$$

Latihan ini dikerjakan oleh Hanif Ahmad Syarif (16121161)

jeff