



$$\vec{E} = \frac{q(t)}{\epsilon A}, \quad \vec{E} = \frac{V_c(t)}{d}$$

$$\rightarrow \frac{V_c(t)}{d} = \frac{q(t)}{\epsilon A} \rightarrow q(t) = \underbrace{\frac{\epsilon A}{d}}_{\rightarrow \frac{\epsilon A}{d} = C} V_c(t)$$

$$\Rightarrow q(t) = C V_c(t)$$

I-V relationship of a capacitor

$$\begin{aligned}\frac{dq(t)}{dt} &= C \frac{d}{dt} V_C(t) \\ &= i_C(t) \quad \frac{\text{Coulombs}}{\text{seconds}}\end{aligned}$$

$$\int \frac{1}{C} i_C(t) dt = \int \frac{d}{dt} V_C(t)$$

$$\frac{1}{C} \int i_C(t) dt = V_C(t) - V_C(t_0)$$

~~$$V_C(t) = V_C(t_0)$$~~

$$V_C(t) = V_C(t_0) + \frac{1}{C} \int_{t_0}^t i_C(x) dx$$