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Machine Learning

CS 686-02

Spring 2018





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Section 1

About this Class



The Warden





Who Am I?

- Ph.D. Operations Management (McGill University)
 - Research focused on service operations
 - Model and solve optimization problems (e.g., MIPs)
- B.Sc., M.Sc. Industrial Engineering (Purdue University)
- B. Commerce (McGill University)
- Assistant Prof @ USF as of August 2014
- I teach or have taught
 - MSAN 593 - Exploratory Data Analysis with R
 - MSAN 601 - Linear Regression Analysis with R
 - MSAN 605/625/627/632 - Practicum
- MS Analytics Practicum Director [2014 - 2017]
- Founding Associate Director of Data Institute [2016 - 2017]



What I Do

$$\min_{y, x^+, x^-} \sum_{j \in \mathbb{J}} \sum_{\nu \in \mathbb{V}} \sum_{t \in \mathbb{T}} r^{(t-1)} \left[\sum_{\omega \in \Omega} \left[f_{j\nu\omega}^+ z_{j\nu\omega}^+ - f_{j\nu\omega}^- z_{j\nu\omega}^- \right] + \gamma_\nu \left(\kappa_{j\nu t} - \rho_{j\nu t} + \sum_{i \in \mathbb{I}} y_{ij\nu t} \right) \right] \quad (4.1)$$

subject to

$$\kappa_{j\nu t} = \kappa_{j\nu(t-1)} + \sum_{\omega \in \Omega} C_{\nu\omega} \left(z_{j\nu\omega}^+ - z_{j\nu\omega}^- \right) \quad \forall j \in \mathbb{J}, \nu \in \mathbb{V}, t \in \mathbb{T} \quad (4.2)$$

$$\rho_{j\nu t} = \rho_{j\nu(t-1)} + \sum_{\omega \in \Omega} C_{\nu\omega} \left(z_{j\nu\omega}^+ - z_{j\nu\omega}^- \right) - \sum_{i \in \mathbb{I}} y_{ij\nu(t-1)} + \alpha_{j\nu(t-1)} - \psi_{j(t-1)}^{(\nu+1 \rightarrow \nu)} + \psi_{j(t-1)}^{(\nu \rightarrow \nu-1)} \quad \forall j \in \mathbb{J}, \nu \in \mathbb{V}, t \in \mathbb{T} \quad (4.3)$$

$$\alpha_{j\nu t} = \mu_{\nu t} \left(\kappa_{j\nu t} - \rho_{j\nu t} + \sum_{i \in \mathbb{I}} y_{ij\nu t} \right) \quad \forall j \in \mathbb{J}, \nu \in \mathbb{V}, t \in \mathbb{T} \setminus \{1\} \quad (4.4)$$

$$\psi_{jt}^{(\nu \rightarrow \nu-1)} = \tau_t^{(\nu \rightarrow \nu-1)} \left(\kappa_{j\nu t} - \rho_{j\nu t} + \sum_{i \in \mathbb{I}} y_{ij\nu t} - \alpha_{j\nu t} \right) \quad \forall j \in \mathbb{J}, \nu \in \mathbb{V} \setminus \{1\}, t \in \mathbb{T} \setminus \{1\} \quad (4.5)$$

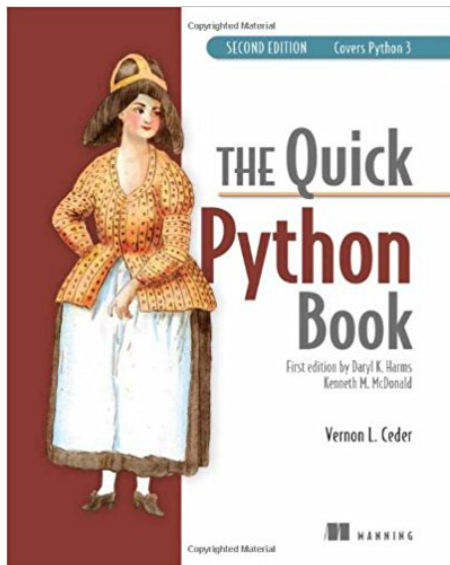
$$\eta_{it} \lambda_{it} + \psi_{i(t-1)}^{(\nu+1 \rightarrow \nu)} = \sum_{j \in \mathbb{J}} y_{ij\nu t} \quad \forall i \in \mathbb{I}, \nu \in \mathbb{V}, t \in \mathbb{T} \quad (4.6)$$

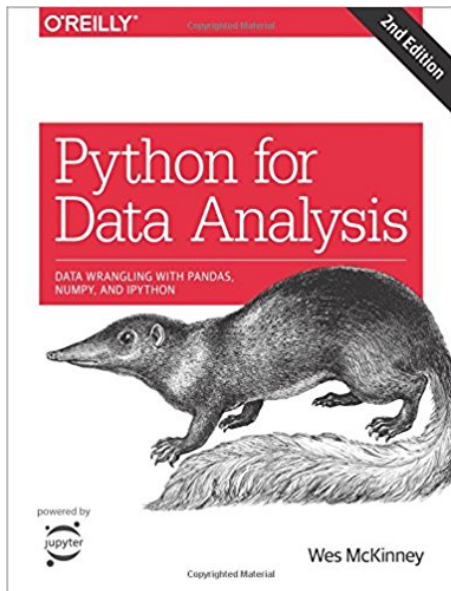
$$\eta_{it} \lambda_{it} \pi_{it} + \psi_{i(t-1)}^{(\nu+1 \rightarrow \nu)} \leq y_{ij\nu t} \quad \forall i = j \in \mathbb{J}, \nu \in \mathbb{V}, t \in \mathbb{T} \quad (4.7)$$

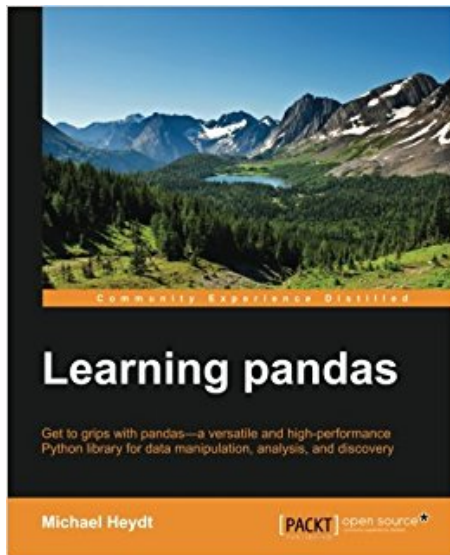


Subsection 3

Reference Textbooks



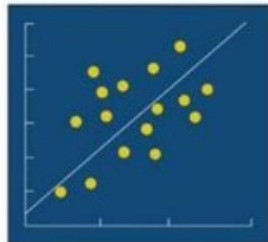






APPLIED LINEAR REGRESSION MODELS

FOURTH EDITION



Kutner

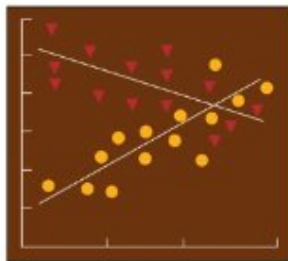
Nachtsheim

Neter

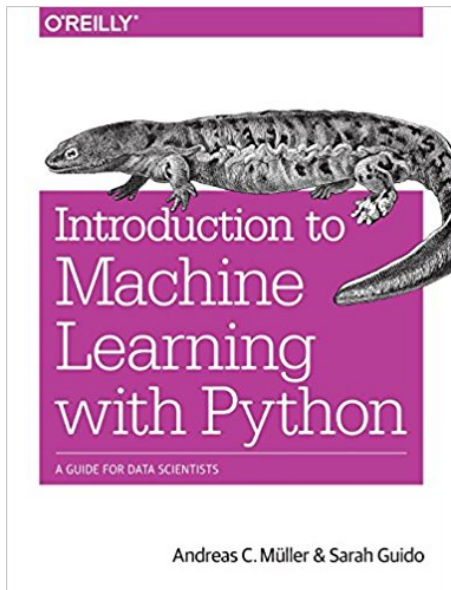


APPLIED LINEAR STATISTICAL MODELS

FIFTH EDITION



Kutner
Nachtsheim
Neter





Section 2

A Brief Introduction to Python



Python 3

- Python 2 will be not longer be supported as of 2020
- We will **exclusively** use Python 3 for this course
- Installing Python
 - <https://www.python.org/>
 - <https://anaconda.org/>
- <https://www.python.org/> Python 3 distributions include the **pip3** package manager
- <https://anaconda.org/> Anaconda 3 distributions include the **conda** package manager
- n.b.** This class will **exclusively** support **pip3**
- n.b.** Don't conflate **pip3** with **pip**; the latter installs packages to Python 2



Jupyter Notebooks

- Once you have Python 3 installed, open a terminal window and run the following command to install Jupyter Notebooks

```
Pauls-iMac:~ paul$ pip3 install jupyter
```

- Opening an instance of Jupyter Notebook is achieved by running the following command in a terminal window

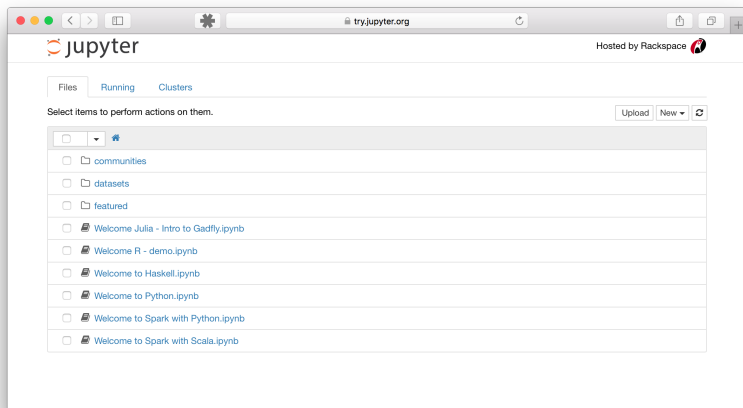
```
Pauls-iMac:~ paul$ jupyter notebook
```

- Jupyter, an interactive programming environment, will open in your browser to the Jupyter Notebook Dashboard



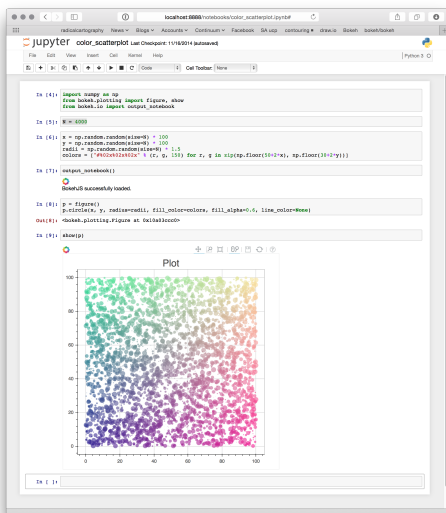
Jupyter Notebook Dashboard

In the top right of the Dashboard, click on the button labeled **New** to run a new Python 3 kernel and open a Notebook





Jupyter Notebook using a Python 3 Kernel





Why use Jupyter Notebooks?

- Interactive environment works well with interpreted languages such as Python
- Run code snippets and observe output immediately, line by line
- Facilitates the exploration of data
- Great for interactive data visualization
- Can include Markdown and \LaTeX
- Can be used with various kernels (not only Python)
 - The name *Jupyter* is an imperfect aggregation of the languages that inspired its creation: **Julia**, **Python** and **R**

n.b. This class will **exclusively** use Jupyter Notebooks for examples, in-class labs, and all deliverables



Jupyter Notebook Cheat Sheet

Python For Data Science Cheat Sheet

Jupyter Notebook

Learn More Python for Data Science Interactively at www.DataCamp.com



Saving/Loading Notebooks

Diagram illustrating Jupyter Notebook actions:

- Create new notebook
- Make a copy of the current notebook
- Save current notebook and record checkpoint
- Preview of the printed notebook
- Close notebook & stop running any scripts
- Open an existing notebook
- Rename notebook
- Revert notebook to a previous checkpoint
- Download notebook as:
 - Python notebook
 - Python
 - HTML
 - Markdown
 - TeX
 - LaTeX
 - PDF

Writing Code And Text

Code and text are encapsulated by 3 basic cell types: markdown cells, code cells, and raw NBConvert cells.

Edit Cells

Diagram illustrating Jupyter Notebook actions:

- Cut currently selected cells to clipboard
- Paste cells from clipboard above current cell
- Paste cells from clipboard on top of current cell
- Revert "Delete Cells" invocation
- Merge current cell with the one above
- Move current cell up
- Adjust metadata underlying the current notebook
- Remove cell attachments
- Paste attachments of current cell
- Copy cells from clipboard to current cursor position
- Paste cells from clipboard below current cell
- Delete current cells
- Split up a cell from current cursor position
- Merge current cell with the one below
- Move current cell down
- Find and replace in selected cells
- Copy attachments of current cell
- Insert image in selected cells

Insert Cells

Diagram illustrating Jupyter Notebook actions:

- Add new cell above the current one
- Add new cell below the current one

Working with Different Programming Languages

Kernels provide computation and communication with front-end interfaces like the notebooks. There are three main kernels:

IPython
Python

R

Julia

Installing Jupyter Notebook will automatically install the IPython kernel.

Diagram illustrating Jupyter Notebook actions:

- Restart kernel
- Restart kernel & run all cells
- Restart kernel & run all cells
- Interrupt kernel
- Interrupt kernel & clear all output
- Connect back to a remote notebook
- Run other installed kernels

Command Mode

Diagram illustrating Jupyter Notebook interface:

- File Edit View Insert Cell Kernel Widgets Help
- Run selected cells (1-12)
- Run current cells down and create a new one below
- Run all cells
- Run all cells below the current cell
- toggle, toggle scrolling and clear current outputs

Edit Mode

Diagram illustrating Jupyter Notebook interface:

- Run selected cells (1-12)
- Run current cells down and create a new one below
- Run all cells
- Run all cells below the current cell
- toggle, toggle scrolling and clear current outputs

Executing Cells

Diagram illustrating Jupyter Notebook actions:

- Run selected cells (1-12)
- Run current cells down and create a new one below
- Run all cells
- Run all cells below the current cell
- toggle, toggle scrolling and clear current outputs

View Cells

Diagram illustrating Jupyter Notebook actions:

- Toggle display of Jupyter logo and filename
- Toggle display of toolbar
- Toggle display of cell action icons:
 - None
 - Edit metadata
 - Raw cell format
 - SlideShow
 - Attachments
 - Tags
- Toggle line numbers in cells

Widgets

Notebook widgets provide the ability to visualize and control changes in your data, often as a control like a slider, textbox, etc.

You can use them to build interactive GUIs for your notebooks or to synchronize stateful and stateless information between Python and JavaScript.

Diagram illustrating Jupyter Notebook actions:

- Download serialized state of all widget models in use
- Save notebook with interactive widgets
- Embed current widgets

Asking For Help

Diagram illustrating Jupyter Notebook actions:

- Walk through a UI tour
- Edit the built-in keyboard shortcuts
- Description of markdown available in notebook
- Python help topics
- NumPy help topics
- Matplotlib help topics
- Pandas help topics
- List of built-in keyboard shortcuts
- Notebook help topics
- Information on unofficial Jupyter Notebook extensions
- IPython help topics
- SciPy help topics
- SymPy help topics
- About Jupyter Notebook

DataCamp
Learn Python for Data Science Interactively





Useful Keyboard Shortcuts in Jupyter

Action	Shortcut
Run cell	ctrl-Enter
Run cell, select below	shift-Enter
Convert cell to code	Y
Convert cell to Markdown	M
Insert cell above	A
Insert cell below	B
Cut selected cell	X
Delete selected cell	D,D
Merge with cell below	shift-M



Markdown Cheat Sheet

HEADERS

```
# This is an <h1> tag
## This is an <h2> tag
##### This is an <h6> tag
```

EMPHASIS

```
*This text will be italic*
_This will also be italic_

**This text will be bold**
__This will also be bold__

*You **can** combine them*
```

BLOCKQUOTES

As Grace Hopper said:

```
> I've always been more interested
> in the future than in the past.
```

As Grace Hopper said:

```
| I've always been more interested
| in the future than in the past.
```

LISTS

Unordered

- * Item 1
- * Item 2
- * Item 2a
- * Item 2b

Ordered

1. Item 1
2. Item 2
3. Item 3
- * Item 3a
- * Item 3b

IMAGES

```
![GitHub Logo](/images/Logo.png)
```

Format: ![Alt Text](url)

LINKS

```
http://github.com - automatic!
```

```
[GitHub](http://github.com)
```

BACKSLASH ESCAPES

Markdown allows you to use backslash escapes to generate literal characters which would otherwise have special meaning in Markdown's formatting syntax.

```
\*literal asterisks\*
```

```
*literal asterisks*
```

Markdown provides backslash escapes for the following characters:

\ backslash	() parentheses
` backtick	# hash mark
* asterisk	+ plus sign
_ underscore	- minus sign (hyphen)
{ curly braces	. dot
[] square brackets	! exclamation mark



Useful L^AT_EX Commands

- Inline commands

Code	Result
<code>$\frac{a}{b}$</code>	$\frac{a}{b}$
<code>$\S 1.3$</code>	Section §1.3
<code>$\Phi^{\phi+1} = \pi$</code>	$\Phi^{\phi+1} = \pi$
<code>$\sum_{i=1}^n x_i / n = \bar{x}$</code>	$\sum_{i=1}^n x_i / n = \bar{x}$

- Mathematical equations

```
\begin{equation}
e^{i \pi} + 1 = 0
\end{equation}
```

$$e^{i\pi} + 1 = 0 \tag{1}$$



L^AT_EX, Markdown, Jupyter Lab

jupyterNotebook_Markdown_LAB.ipynb

here.'."/>

jupyter jupyterNotebook_Markdown_LAB (autosaved) Logout

File Edit View Insert Cell Kernel Widgets Help Trusted Python 3 O

My first iPython Markdown notebook

Jupyter notebook has a tool to create markdown files. Here we will cover some basics of working with iPython Markdown (press on the link to jump to the section)

- [§ 1. What is Markdown?](#)
- [§ 2. How to make a list](#)
- [§ 3. How to create a table](#)
- [§ 4. Formulas](#)
- [§ 5. Colored text boxes](#)
- [§ 6. Bonus tasks](#)

§ 1. What is Markdown?

As defined by John Gruber [here](#).



Lists

- Lists are like arrays, do not need to be declared (type or size), and can contain a mixture of other types as its elements, including
 - strings
 - tuples
 - other lists
 - dictionaries
 - etc.
- A list can be indexed from the front or the back

```
>>> x = ["1st", "2nd", "3rd", "4th"]  
  
>>> x[0]  
'1st'  
  
>>> x[2]  
'3rd'  
  
>>> x[-1]  
'4th'
```



Lists [CONT'D]

- Lists can be sliced to generate a subset
 - Slice an array using the `:` operator
 - Subset a list from the *beginning*, starting with 0
 - Subset a list from the *end*, starting with -1
 - When slicing an array from index *a* to *b*, the left most index is *included* in the slice, but the rightmost index is *excluded*, i.e., `[a, b)`

<code>x = [</code>		<code>"1st",</code>		<code>"2nd",</code>		<code>"3rd",</code>		<code>"4th"</code>	<code>]</code>
Positive Indices	0		1		2		3		
Negative Indices	-4		-3		-2		-1		



YOU TRY IT

```
>>> x = ["1st", "2nd", "3rd", "4th"]  
  
>>> x[1:-1]  
  
>>> x[0:3]  
  
>>> x[-2:-1]  
  
>>> x[:3]  
  
>>> x[-2:]
```



SOLUTION

```
>>> x = ["1st", "2nd", "3rd", "4th"]

>>> x[1:-1]
['2nd', '3rd']

>>> x[0:3]
['1st', '2nd', '3rd']

>>> x[-2:-1]
['3rd']

>>> x[:3]
['1st', '2nd', '3rd']

>>> x[-2:]
['3rd', '4th']
```



Slicing Lists and Data Type-Matching

```
>>> myList = list(range(1, 9))    # create a list
>>> print(myList)
[1, 2, 3, 4, 5, 6, 7, 8]

>>> type(myList[3])
int

>>> myList[3] = -99                # replace scalar with scalar
>>> print(myList)
[1, 2, 3, -99, 5, 6, 7, 8]

>>> type(myList[:4])
list

>>> myList[:4] = 555               # can't replace a list with a scalar...
<...error code truncated...>
TypeError: can only assign an iterable

>>> myList[:4] = [555]            # ...but can replace list with another list,
                                   # even if list is of different length

>>> print(myList)
[555, 5, 6, 7, 8]

>>> myList[0:1] = list(range(101, 103)) # scalar can also be replaced with...
>>> print(myList)                       # ... a list so long as you select the...
[101, 102, 6, 7, 8]                     # ... scalar as a list before assignment
```



Common List Operators & Operations

List operation	Explanation	Example
<code>[]</code>	Creates an empty list	<code>x = []</code>
<code>len</code>	Returns the length of a list	<code>len(x)</code>
<code>append</code>	Adds a single element to the end of a list	<code>x.append('y')</code>
<code>insert</code>	Inserts a new element at a given position in the list	<code>x.insert(0, 'y')</code>
<code>del</code>	Removes a list element or slice	<code>del(x[0])</code>
<code>remove</code>	Searches for and removes a given value from a list	<code>x.remove('y')</code>
<code>reverse</code>	Reverses a list in place	<code>x.reverse()</code>

- `.extend()`



Common List Operators & Operations [CONT'D]

List operation	Explanation	Example
<code>sort</code>	Sorts a list in place	<code>x.sort()</code>
<code>+</code>	Adds two lists together	<code>x1 + x2</code>
<code>*</code>	Replicates a list	<code>x = ['y'] * 3</code>
<code>min</code>	Returns the smallest element in a list	<code>min(x)</code>
<code>max</code>	Returns the largest element in a list	<code>max(x)</code>
<code>index</code>	Returns the position of a value in a list	<code>x.index('y')</code>
<code>count</code>	Counts the number of times a value occurs in a list	<code>x.count('y')</code>
<code>in</code>	Returns whether an item is in a list	<code>'y' in x</code>



Tuples

Very similar to lists save for one **BIG** difference

- Lists are **MUTABLE**
- Tuples are **IMMUTABLE**

```
>>> myList = [1, 2, 3, "four"]           # create a list

>>> myList[2] = "three"                 # change third entry of list
>>> print("myList = " + str(myList))

myList = [1, 2, 'three', 'four']

>>> myTuple = (1, 2, 3, "four")          # create a tuple, note round braces

myTuple = (1, 2, 3, 'four')

>>> myTuple[2] = "three"                 # try to change third entry of list

Traceback (most recent call last):
  File "/Users/paul/Desktop/myFile.py", line 13, in <module>
    myTuple[2] = "three" # try to change third entry of list
TypeError: 'tuple' object does not support item assignment
```




Dictionaries

A dictionary may feel like an associative array or hash table

- In a list
 - values are accessed by means of an integer index
 - values are implicitly ordered by their position in the list
- In a dictionary
 - values are accessed by means of a *key*, which can be integers, strings, or other Python objects
 - values are not implicitly ordered

A dictionary is a way of mapping from one set of arbitrary objects to an associated but equally arbitrary set of objects



Dictionaries [CONT'D]

Let's make an actual translational dictionary using Python's dictionary data structure

```
>>> eng_to_french = {}                                # initialize empty dictionary
                                                    # note curly braces for dictionaries

>>> eng_to_french['blue'] = 'bleu'                    # create a single key-value pair

>>> eng_to_french['red'] = 'rouge'                     # create a single key-value pair

>>> eng_to_french['yellow'] = 'jaune'                 # create a single key-value pair

>>> print("In French, the colour yellow is", eng_to_french['yellow'])

In French, the colour yellow is jaune

# one may alternatively build a dictionary in a single line of code

>>> eng_to_french = {'blue':'bleu', 'red':'rouge', 'yellow':'jaune'}
```



Common Dictionary Operators & Operations

Dictionary operation	Explanation	Example
<code>{}</code>	Creates an empty dictionary	<code>x = {}</code>
<code>len</code>	Returns the number of entries in a dictionary	<code>len(x)</code>
<code>keys</code>	Returns a view of all keys in a dictionary	<code>x.keys()</code>

Dictionary operation	Explanation	Example
<code>values</code>	Returns a view of all values in a dictionary	<code>x.values()</code>
<code>items</code>	Returns a view of all items in a dictionary	<code>x.items()</code>
<code>del</code>	Removes an entry from a dictionary	<code>del(x[key])</code>
<code>in</code>	Tests whether a key exists in a dictionary	<code>'y' in x</code>
<code>get</code>	Returns the value of a key or a configurable default	<code>x.get('y', None)</code>
<code>setdefault</code>	Returns the value if the key is in the dictionary; otherwise, sets the value for the key to the default and returns the value	<code>x.setdefault('y', None)</code>
<code>copy</code>	Makes a copy of a dictionary	<code>y = x.copy()</code>
<code>update</code>	Combines the entries of two dictionaries	<code>x.update(z)</code>



Python Basics Cheat Sheet

Python For Data Science Cheat Sheet

Python Basics

Learn More Python for Data Science [interactively at: www.datacamp.com](https://www.datacamp.com)

Variables and Data Types

Variable Assignment

```
>>> x=5
>>> x
5
```

Calculations With Variables

>>> x+2	Sum of two variables
>>> x-2	Subtraction of two variables
>>> x*2	Multiplication of two variables
>>> x**2	Exponentiation of a variable
>>> x%2	Remainder of a variable
>>> x/float(2)	Division of a variable

Types and Type Conversion

str()	'5', '3.45', 'True'	Variables to strings
int()	5, 3, 1	Variables to integers
float()	5.0, 1.0	Variables to floats
bool()	True, True, True	Variables to booleans

Asking For Help

```
>>> help(str)
```

Strings

```
>>> my_string = 'thisStringIsAwesome'
>>> my_string
'thisStringIsAwesome'
```

String Operations

```
>>> my_string * 2
'thisStringIsAwesomethisStringIsAwesome'
>>> my_string + 'Init'
'thisStringIsAwesomeInit'
>>> 'm' in my_string
True
```

String Methods

>>> my_string.upper()	String to uppercase
>>> my_string.lower()	String to lowercase
>>> my_string.count('u')	Count String elements
>>> my_string.replace('e', 'i')	Replace String elements
>>> my_string.strip()	Strip whitespaces

Lists

Also see Numpy Arrays

```
>>> a = 'is'
>>> b = 'nice'
>>> my_list = ['my', 'list', a, b]
>>> my_list2 = [[4,5,6,7], [3,4,5,6]]
```

Selecting List Elements

Index starts at 0

Subset <pre>>>> my_list[1] >>> my_list[-3]</pre>	Select item at index 1 Select 3rd last item
Slice <pre>>>> my_list[1:3] >>> my_list[1:] >>> my_list[:3] >>> my_list[:]</pre>	Select items at index 1 and 2 Select items after index 0 Select items before index 3 Copy my_list
Subset Lists of Lists <pre>>>> my_list2[1][0] >>> my_list2[1][1:2]</pre>	my_list[itemOffset]

List Operations

```
>>> my_list + my_list2
['my', 'list', 'is', 'nice', 'my', 'list', 'is', 'nice']
>>> my_list * 2
['my', 'list', 'is', 'nice', 'my', 'list', 'is', 'nice']
>>> my_list2 > 4
True
```

List Methods

<pre>>>> my_list.index(a) >>> my_list.count(a) >>> my_list.append('!') >>> my_list.remove('!') >>> del(my_list[0:1]) >>> my_list.reverse() >>> my_list.extend('!!') >>> my_list.pop(-1) >>> my_list.insert(0, '!!') >>> my_list.sort()</pre>	Get the index of an item Count an item Append an item at a time Remove an item Remove an item Reverse the list Append an item Remove an item Insert an item Sort the list
--	--

Libraries

Import libraries

```
>>> import numpy
>>> import numpy as np
>>> from math import pi
```

Data analysis
 Scientific computing
 xD plotting
 Machine learning
 Kaggle

Install Python

ANACONDA
 Leading open data science platform powered by Python
 spyder
 Free IDE that is included with Anaconda
 jupyter
 Create and share documents with live code, visualizations, text, ...

Numpy Arrays

Also see Lists

```
>>> my_list = [1, 2, 3, 4]
>>> my_array = np.array(my_list)
>>> my_2darray = np.array([[1,2,3],[4,5,6]])
```

Selecting Numpy Array Elements

Index starts at 0

Subset <pre>>>> my_array[1] >>> my_array[0:2]</pre>	Select item at index 1 Select items at index 0 and 1
Slice <pre>>>> my_array[0:2] array([1, 2])</pre>	Subset 2D Numpy arrays <pre>>>> my_2darray[1,0] array([2, 4])</pre> my_2darray[rows, columns]

Numpy Array Operations

```
>>> my_array > 3
array([False,  False,  False,  True], dtype=bool)
>>> my_array * 2
array([2,  4,  6,  8])
>>> my_array + np.array([5, 6, 7, 8])
array([6,  8, 10, 12])
```

Numpy Array Functions

<pre>>>> my_array.shape >>> np.append(other_array) >>> np.insert(my_array, 1, 5) >>> np.delete(my_array, [1]) >>> np.mean(my_array) >>> np.median(my_array) >>> my_array.corrcoef() >>> np.std(my_array)</pre>	Get the dimensions of the array Append items to an array Insert items in an array Delete items in an array Mean of the array Median of the array Correlation coefficient Standard deviation
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DataCamp

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An Introduction to NumPy

- The Numerical Python (NumPy) package is designed for high-performance scientific computing and analysis of data
- NumPy is foundational, and it serves as a basis on which many other scientific and analytic tools are built
- Notably, NumPy incorporates very fast vectorized array operations



np.array

- Just as it is possible to create n -dimensional lists, the ndarray object creates an n -dimensional array
- Unlike lists, an ndarray objects contain only *homogeneous* data
- ndarrays have, amongst others,
 - shapes, dimensions of the ndarray
 - dtypes, the data type of the ndarray

```
>>> import numpy as np
>>> x = np.array([[1, 2, 3], [-99, -98, -97]])
>>> print(x)

[[ 1  2  3]
 [-99 -98 -97]]

>>> print(x.shape)

(2, 3)

>>> print(x.dtype)

int64
```



Vectorization of `np.array`s

- As `ndarray` objects contain homogeneous data, fast, vectorized mathematical operations are possible, and differ significantly from how lists behave

```
>>> x = np.array([[1, 2, 3], [-99, -98, -97]]) # create array
>>> y = x.tolist() # convert array to list

>>> print(x + x) # array operation

[[ 2  4  6]
 [-198 -196 -194]]

>>> print(y + y) # list operation

[[1, 2, 3], [-99, -98, -97], [1, 2, 3], [-99, -98, -97]]
```

n.b. `np.zeros` creates an n -dimensional array of zeros, but `np.empty` creates an n -dimensional array filled with a random mix of zeros, very small or very large numbers



Mixing Vectors and Scalars with `np.array`s

- `NumPy` will automatically vectorize operations between scalars and arrays
- The `'.'` after an integer implies that is it of type `float`; can also be used for array initialization

```
>>> y = np.array([1, 2, 3])      # create an array
>>> y.dtype                     # numpy creates an int64 type array
dtype('int64')

>>> z = 1/y
>>> print(z)
[ 1.          0.5          0.33333333]

>>> z.dtype                     # numpy automatically converts to float type array
dtype('float64')
```




Slicing np.arrays

- NumPy has its own range function, `np.arange` (note the single 'r'), which operates similarly to the `range` function
- NumPy likes to vectorize, so array manipulation is different from list manipulation

```
>>> y = np.arange(5)      # create an array
>>> print(y)

[0 1 2 3 4]

>>> y[1:3] = 99           # numpy automatically vectorizes the scalar to the length
>>> print(y)              # of what is being replaced

[ 0 99 99  3  4]
```



Memory Allocation with NumPy

- As NumPy is designed to deal with large amounts of data, it seeks to be as efficient with memory as possible
- One of the results of this design approach is that array slices of an ndarray object are *views* of the original array
- An implication of the behaviour: modifying data in a view changes the value(s) in the parent (original) array
- Copies of slices can be made by appending `.copy()` to a slice

```
>>> y = np.arange(5)
>>> myNumPySlice = y[1:3]
>>> myNumPySlice[:] = 789
>>> print(myNumPySlice)

array([789, 789])

>>> print(y)

array([ 0, 789, 789,  3,  4])
```



Logical Operations on `np.array`s

- Use the logical operators `>`, `>=`, `==`, `=<`, `<`, `|` (OR) and `&` (AND) to test conditions in a vectorized fashion
- The result is a boolean vector of `True` and `False` values
- `True` and `False` values are treated as 0's and 1's, upon which mathematical calculations can be completed
- Vectors can also be compared against other vectors



Logical Operations on np.arrays [CONT'D]

EXAMPLES

```
>>> x = np.arange(5)
>>> x > 2
array([False, False, False,  True,  True], dtype=bool)

>>> (x > 2) | (x < 1)
array([ True, False, False,  True,  True], dtype=bool)

>>> y = (x > 2) | (x < 1)                # n.b. fails without brackets
>>> y.sum()                             # arithmetic operations on booleans
3

>>> y.mean()
0.59999999999999998

>>> y.astype(int)                       # convert boolean to numeric type
array([0, 0, 1, 0, 0])

>>> np.random.seed(1)
# 5 random normal vars, mu = 1, sig^2 = 36
>>> z = np.random.normal(1, 6, 5)
array([ 10.74607218, -2.67053848, -2.16903051, -5.43781173,  6.19244578])

>>> x > z                               # comparing two arrays
array([False,  True,  True,  True, False], dtype=bool)
```



NumPy Cheat Sheet

Python For Data Science Cheat Sheet

NumPy Basics

Learn Python for Data Science [interactively at www.datacamp.com](https://www.datacamp.com)



NumPy

The NumPy library is the core library for scientific computing in Python. It provides a high-performance multidimensional array object, and tools for working with these arrays.

Use the following import convention:

```
>>> import numpy as np
```



NumPy Arrays

1D array



2D array



3D array



Creating Arrays

```
>>> a = np.array([1,2,3])
>>> b = np.array([1,5,2,3], (4,5,6), dtype = float)
>>> c = np.array([1,1,5,2,3], (4,5,6), [(3,2,1), (4,5,6)],
dtype = float)
```

Initial Placeholders

```
>>> np.zeros((2,4))
>>> np.ones((2,3,4), dtype=np.int16)
>>> d = np.arange(10,25,5)
>>> np.linspace(0,2,8)
>>> e = np.full((2,2),7)
>>> f = np.eye(2)
>>> np.random.random((2,2))
>>> np.empty((3,2))
```

Create an array of zeros
Create an array of ones
Create an array of evenly spaced values (step value)
Create an array of evenly spaced values (number of samples)
Create a constant array
Create a 2D identity matrix
Create an array with random values
Create an empty array

I/O

Saving & Loading On Disk

```
>>> np.save("my_array", a)
>>> np.savez("array.npz", a, b)
>>> np.load("my_array.npy")
```

Saving & Loading Text Files

```
>>> np.savetxt("myfile.txt")
>>> np.genfromtxt("my_file.csv", delimiter=',')
>>> np.savetxt("myarray.txt", a, delimiter=',')
```

Data Types

```
>>> np.int64 Signed 64-bit integer types
>>> np.float32 Standard double-precision floating point
>>> np.complex Complex numbers represented by 128 floats
>>> np.bool Boolean type storing TRUE and FALSE values
>>> np.object Python object type
>>> np.string Fixed-length string type
>>> np.unicode Fixed-length unicode type
```

Inspecting Your Array

```
>>> a.shape Array dimensions
>>> len(a) Length of array
>>> b.ndim Number of array dimensions
>>> a.size Number of array elements
>>> b.dtype Data type of array elements
>>> b.dtype.name Name of data type
>>> b.astype(int) Convert an array to a different type
```

Asking For Help

```
>>> np.info(np.ndarray.dtype)
```

Array Mathematics

Arithmetic Operations

```
>>> g = a - b Subtraction
>>> h = a * b Multiplication
>>> np.subtract(a,b) Subtraction
>>> b + a Addition
>>> np.add(b,a) Addition
>>> np.divide(a,b) Division
>>> a / b Division
>>> np.multiply(a,b) Multiplication
>>> a * b Multiplication
>>> np.exp(b) Exponentiation
>>> np.sqrt(b) Square root
>>> np.sin(a) Print lines of an array
>>> np.cos(b) Element-wise cosine
>>> np.log(a) Element-wise natural logarithm
>>> a.dot(f) Dot product
>>> np.linalg.pinv(a) Pseudoinverse
```

Comparison

```
>>> a < b Element-wise comparison
>>> a <= b Element-wise comparison
>>> a > b Element-wise comparison
>>> a >= b Element-wise comparison
>>> np.array_equal(a, b) Array-wise comparison
```

Aggregate Functions

```
>>> a.sum() Array-wise sum
>>> a.min() Array-wise minimum value
>>> a.max() Maximum value of an array row
>>> b.cumsum(axis=1) Cumulative sum of the elements
>>> a.mean() Mean
>>> b.median() Median
>>> a.correlcoef() Correlation coefficient
>>> np.std(b) Standard deviation
```

Copying Arrays

```
>>> b = a.view() Create a view of the array with the same data
>>> np.copy(a) Create a copy of the array
>>> b = a.copy() Create a deep copy of the array
```

Sorting Arrays

```
>>> a.sort() Sort an array
>>> a.sort(axis=0) Sort the elements of an array's axis
```

Subsetting, Slicing, Indexing

Also see Lists

Subsetting

```
>>> a[2]
```



Select the element at the 2nd index

```
>>> b[1,2]
```



Select the element at row 0 column 2 (equivalent to `a[0][2]`)

Slicing

```
>>> a[0:2]
```



Select items at index 0 and 1

```
>>> a[0:2,1]
```



Select items at rows 0 and 1 in column 1

```
>>> a[0:2,:]
```



Select all items at row 0 (equivalent to `a[0,:]`)

```
>>> a[:,1:]
```



Select all items at row 0 (equivalent to `a[0,:]`)

```
>>> a[::-1]
```



Reversed array

```
>>> a[a<2]
```



Select elements from `a` less than 2

Boolean Indexing

```
>>> a[a<2]
```



Select elements from `a` less than 2

Fancy Indexing

```
>>> b[[2, 0, 1, 0]]
```



Select elements `a[[2,0,1,0]]` and `a[[0,1,2,0]]`

```
>>> b[[2, 0, 1, 0], [0, 1, 2, 0]]
```



Select a subset of the matrix's rows and columns

```
>>> b[[2, 0, 1, 0], [0, 1, 2, 0]]
```



Select a subset of the matrix's rows and columns

Array Manipulation

Transposing Array

```
>>> a = np.transpose(b)
```

Permute array dimensions

```
>>> a.T
```

Permute array dimensions

Changing Array Shape

```
>>> b.reshape(1,2)
```

Flatten the array

```
>>> b.reshape(2,6)
```

Reshape, but don't change data

```
>>> np.append(b,0)
```

Return a new array with shape (2,6)

```
>>> np.append(b,0)
```

Append items to an array

```
>>> np.insert(a, 1, 5)
```

Insert items in an array

```
>>> np.delete(a, [1])
```

Delete items from an array

Combining Arrays

```
>>> np.concatenate((a,d), axis=0)
```

Concatenate arrays

```
>>> np.vstack((a,b))
```

Stack arrays vertically (row-wise)

```
>>> np.hstack((a,b))
```

Stack arrays horizontally (column-wise)

```
>>> np.dstack((a,b))
```

Stack arrays vertically (column-wise)

```
>>> np.r_[a,b]
```

Create stacked column-wise arrays

```
>>> np.c_[a,b]
```

Create stacked column-wise arrays

Splitting Arrays

```
>>> np.hsplit(a,3)
```

Split the array horizontally at the 3rd index

```
>>> np.vsplit(a,2)
```

Split the array vertically at the 2nd index

```
>>> np.split(a, [1,2], axis=1)
```

Split the array at indices 1 and 2 along axis 1

```
>>> np.split(a, [1,2], axis=0)
```

Split the array at indices 1 and 2 along axis 0

