Feature Transformations - Assignment 11

Data and Package Import

```
In [1]: %matplotlib inline import numpy as np import pandas as pd import matplotlib.pyplot as plt

In [2]: perov = pd.read_csv('data/perovskite_data.csv')
```

1. One-hot Encoding

Creat a matrix of one-hot encoded features.

Use the X column of the perovskite dataset (corresponding to the identity of the X ion in the ABX₃ coumpound).

```
In [3]: X_onehot = pd.get_dummies(perov['X'])

In [4]: X_onehot.head(5)
```

Out[4]:

	Br	CI	F	I	0
0	0	0	0	0	1
1	0	0	0	0	1
2	0	1	0	0	0
3	1	0	0	0	0
4	0	0	Ο	0	1

Print the dimensions of the matrix.

```
In [5]: print(X_onehot.shape)
(576, 5)
```

Print the sum across all rows for each feature.

In [6]: print(X_onehot.sum(axis = 0))

Br 27

CI 71

F 66

I 43

0 369

dtype: int64

One-hot encoding for a categorical variable

Consider a dataset consisting of a single categorical variable with a total of N datapoints and corresponding outputs, y. Assume that each datapoint has a unique category label such that there are N distinct categories. You apply one-hot encoding to create a new feature matrix, \bar{X} and decide to fit a linear regression model:

$$\vec{v} = \bar{\bar{X}}\vec{w}$$

What will the optimal values of \vec{w} be and the R^2 be? You can use code, math, or a conceptual explanation to answer this question.

N datapoints with N distinct categories will result in an N x N feature matrix $\bar{\bar{X}}$ where all diagonal elements are 1 and others are 0. This is simply an identity matrix in which case \vec{w} will be exactly identical to \vec{y} . Therefore, the optimal \vec{w} will be \vec{y} and the corresponding r^2 will be 1.0.

Is this a reliable model? Briefly explain.

This is not a reliable model. It just memorizes the \vec{y} such that it will break when a new kind of data is introduced.

2. PCA vs. LDA

Load the MNIST dataset.

In [7]: from sklearn.datasets import load_digits

digits = load_digits()

X_mnist = np.array(digits.data)

y_mnist = np.array(digits.target)

Use PCA on the MNIST dataset.

Set n_components to 9.

```
In [8]: from sklearn.decomposition import PCA

pca = PCA(n_components = 9)
X_pca = pca.fit_transform(X_mnist)
```

Apply k-means clustering to the PCA transformed data.

Set n_clusters to 10.

```
In [9]: from sklearn.cluster import KMeans

kmeans = KMeans(n_clusters = 10)

y_pca = kmeans.fit_predict(X_pca)
```

Assign a label to each cluster by using the most common label from the cluster.

This step converts the clustering to a classification prediction. If the label 9 is most common in the cluster 1, all points belonging to that cluster should be labeled as 9. However, be aware that these labels may change if you re-run the clustering, so you probably want to assign them programatically rather than manually.

Hint: np.bincount() function may be helpful.

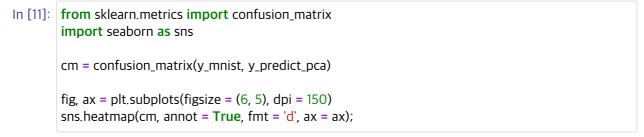
```
In [10]: y_predict_pca = np.zeros(y_mnist.shape)

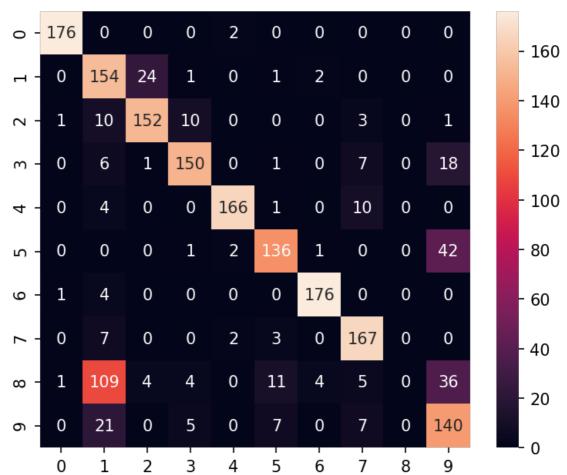
for i in range(10):
    collect_label = y_mnist[y_pca == i]
    count_label = np.bincount(collect_label)
    common_label = np.argmax(count_label)

y_predict_pca[y_pca == i] = common_label
```

Create a confusion matrix based on the clustering result.

Plot the confusion matrix.





Follow the same steps using LDA instead of PCA.

- Use LDA on the MNIST dataset.
- · Apply k-means clustering.
- · Assign labels.
- Plot the resulting matrix.

```
In [12]: from sklearn.discriminant_analysis import LinearDiscriminantAnalysis

Ida = LinearDiscriminantAnalysis()
Ida.fit(X_mnist, y_mnist)
X_Ida = Ida.transform(X_mnist)

kmeans = KMeans(n_clusters = 10)
y_Ida = kmeans.fit_predict(X_Ida)

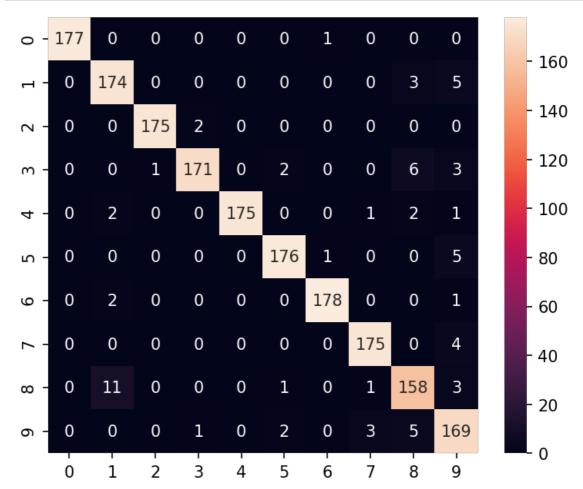
y_predict_Ida = np.zeros(y_mnist.shape)

for i in range(10):
    collect_label = y_mnist[y_Ida == i]
```

```
count_label = np.bincount(collect_label)
common_label = np.argmax(count_label)

y_predict_lda[y_lda == i] = common_label

fig, ax = plt.subplots(figsize = (6, 5), dpi = 150)
cm = confusion_matrix(y_mnist, y_predict_lda)
sns.heatmap(cm, annot = True, fmt = 'd', ax = ax);
```



Briefly discuss the results.

Clustering performs much better for the LDA-projected data compared to the PCA-projected data. While the PCA-projected data struggles identifying 1 and 9, there are much less mispredictions for the LDAprojected data.

3. Symbolic Classification

Drop ABX3, t and tau features of the perovskite dataset.

```
In [13]: dropped_perov = perov.drop(['ABX3', 't', 'tau', 'exp_label'], axis = 1)
    y = perov['exp_label']
```

Apply one-hot encoding to dropped_perov.

In [14]: one_hot_perov = pd.get_dummies(dropped_perov)

Do a train/test split with test_size =0.3.

In [15]: from sklearn,model_selection import train_test_split

X_train, X_test, y_train, y_test = train_test_split(one_hot_perov, y, test_size = 0.3)

Train a autofeat classifier.

Use transforms below for the non-linear transformations.

In [16]: from autofeat import AutoFeatClassifier

In [17]: transforms = ['1/', 'exp', '^2', '^3']

autoClass = AutoFeatClassifier(verbose = 1, feateng_steps = 2, featsel_runs = 1, transformations = to autoClass.fit(X_train, y_train)

[AutoFeat] Warning: This just calls fit_transform() but does not return the transformed datafram e

[AutoFeat] It is much more efficient to call fit_transform() instead of fit() and transform()!

[AutoFeat] The 2 step feature engineering process could generate up to 129286 features.

[AutoFeat] With 403 data points this new feature matrix would use about 0.21 gb of space.

[feateng] Step 1: transformation of original features

[feateng] Generated 20 transformed features from 127 original features - done.

[feateng] Step 2: first combination of features

[feateng] Generated 2720 feature combinations from 10731 original feature tuples - done.

[feateng] Generated altogether 10735 new features in 2 steps

[feateng] Removing correlated features, as well as additions at the highest level

/Users/SihoonChoi/opt/anaconda3/lib/python3.7/site-packages/sympy/_init_.py:676: SymPyDe precationWarning:

importing sympy.core.add with 'from sympy import *' has been deprecated since SymPy 1.6. Use import sympy.core.add instead. See https://github.com/sympy/sympy/issues/18245 (https://github.com/sympy/sympy/issues/18245) for more info.

deprecated_since_version="1.6").warn()

[feateng] Generated a total of 1189 additional features [featcal] Scaling data done

Out[17]: AutoFeatClassifier(featsel_runs=1, transformations=['1/', 'exp', '^2', '^3'], verbose=1)

Print the 5 most important features.

In [18]: # Resulting new features and good_cols_ heavily depend on randomness of train_test_split # Please don't deduct points just because the features are different from yours or mine

print('5 most important features: \n') for feat in autoClass.good_cols_[:5]: print(feat)

5 most important features:

rXAng/rAAng 1/(nB*rBAng)

Print the accuracy on the test set.

In [19]: autoClass.score(X_test, y_test)

[AutoFeat] Computing 2 new features. [AutoFeat] 2/ 2 new features ...done.

Out[19]: 0.7283236994219653