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Define conjunction of a statement. Construct a truth table for the compound statement \sim (p\Lambda q)
  Define a statement. If P is true, q is true, find the truth value of (p \lor q) \land (\sim q)
Define negation of a statement. Construct a truth table for the compound statement \sim (p \lor (\sim q))
Define conditional statement. Compute the truth table of the statement (p \Rightarrow q) \Leftrightarrow (\sim q \Rightarrow \sim p)
If A,B and C be any three non-empty sets, prove that: A - (B \cup C) = (A - B) \cap (A - C)
6. Define the complement of a set. State and prove De-Morgan's laws.
7. Prove that A\Delta B = (A \cup B) - (A \cap B)
8. For any two real numbers x and y, prove that |x + y| \le |x| + |y|
    Rewrite, using absolute value sign for |3x + 2| \le 1
10. Let p,q and r be statements, show that the statements (p \land q \Rightarrow r) \Leftrightarrow [(p \Rightarrow (q \Rightarrow r)] is true.
DAY-2
11. For any two real numbers x and y
     a) |x+y| \leq |x| + |y|
       b) |x - y| \ge |x| - |y|
 12. If x \in R and a be any positive real number then |x| < a \Rightarrow a < x < a and conversely.
 13. Solve the inequality \frac{x+2}{x^2-3x} > 0
 14. Solve the inequality |2x-1| \ge 3 and draw its graph.
 15./Solve x^2 - 2x - 3 \ge 0
 16. Solve the inequality x^2 + 7x + 10 < 0
 17. Let A = \{-1,0,2,4,6\} and a function f: A \to R is defined by i) y = f(x) = \frac{x}{x+2} Find the range of f
 18. Let a function f: A \to B be defined by f(x) = \frac{x^2}{6} with A = \{-2, -1, 0, 1, 2\} and B = \{0, \frac{1}{6}, \frac{2}{3}\}. Find the range
   of f.ls the function f one to one and onto.
 17. Define symmetric and skew-symmetric matrix with example.
 18. If A = \begin{pmatrix} 2 & 4 & 3 \\ 2 & 1 & -2 \\ -2 & 2 & -1 \end{pmatrix} find A^T
       a) Show that the sum of the given matrix and its transpose is a symmetric matrix.
       b) Show that the difference of the given matrix and its transpose is a skew-symmetric matrix.
        c) Express the given matrix A as the sum of the symmetric and skew-symmetric matrix form
 19./If A = \begin{pmatrix} 0 & 2y - 3 \\ 1 - y & 0 \end{pmatrix} and A = A^T, Find the value of y.
 DAY-3
 20. Without expanding the determinant show that the value of the determinant is zero
        i) \begin{vmatrix} 1 & bc & a(b+c) \\ 1 & ca & b(c+a) \\ 1 & ab & c(a+b) \end{vmatrix} ii) \begin{vmatrix} 1 & bc & bc(b+c) \\ 1 & ca & ca(c+a) \\ 1 & ab & ab(a+b) \end{vmatrix}
 21. Without expanding the determinant, prove that
           i) \begin{vmatrix} 1 & x & x^2 \\ 1 & y & y^2 \\ 1 & z & z^2 \end{vmatrix} = \begin{vmatrix} 1 & x & yz \\ 1 & y & zx \\ 1 & z & xy \end{vmatrix} ii) \begin{vmatrix} 1 & bc & b+c \\ 1 & ca & c+a \\ 1 & ab & a+b \end{vmatrix} = \begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix}
 22. Show that
      Show that

i) \begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ bc & ca & ab \end{vmatrix} = (a-b)(b-c)(c-a)

ii) \begin{vmatrix} a & b & c \\ a^2 & b^2 & c^2 \\ b+c & c+a & a+b \end{vmatrix} = (b-c)(c-a)(a-b)(a+b+c)c

iii) \begin{vmatrix} a-b-c & 2a & 2a \\ 2b & b-c-a & 2b \\ 2c & 2c & c-a-b \end{vmatrix} = (a+b+c)^3

iv) \begin{vmatrix} 1+x & 1 & 1 \\ 1 & 1+y & 1 \\ 1 & 1 & 1+z \end{vmatrix} = xyz(1+\frac{1}{x}+\frac{1}{y}+\frac{1}{z})
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\begin{vmatrix} x^2 + 1 & xy & xz \\ xy & y^2 + 1 & yz \\ xz & yz & z^2 + 1 \end{vmatrix} = 1 + x^2 + y^2 + z^2
\begin{vmatrix} a & b & ax + by \\ b & c & bx + cy \\ ax + by & bx + cy & 0 \end{vmatrix} = (b^2 - ac)(ax^2 + 2bxy + cy^2)
23 If A = \begin{pmatrix} 7 & -3 \\ 6 & 2 \end{pmatrix}, prove that A^{-1} = \frac{1}{32} \begin{pmatrix} 2 & 3 \\ -6 & 7 \end{pmatrix}
24 Prove that the two matrices \begin{pmatrix} -3 & -2 \\ 5 & 3 \end{pmatrix} and \begin{pmatrix} 3 & 2 \\ -5 & -3 \end{pmatrix} are the inverse of each others.
25. Given a matrix \begin{pmatrix} 3 & -1 \\ 5 & -2 \end{pmatrix}, find a matrix \begin{pmatrix} p & q \\ r & s \end{pmatrix} such that they are inverse of each other 26. Determine the nature of the roots of x^2 - 6x + 5 = 0
DAY-4
27 For what values of P will the equation 5x^2 - px + 45 = 0 have equal roots?
28 If a,b,c are rational and a+b+c=0, show that the roots of (b+c-a)x^2+(c+a-b)x+
     (a+b-c)=0 are rational.
29 Find a quadratic equation whose roots are the reciprocal of the roots of: 3x^2 - 5x - 2 = 0
30. If the roots of the equation x^2 + ax + c = 0 differ by 1, prove that a^2 = 4c + 1
31 If the roots of the equation ax^2 + bx + c = 0 be in the ratio of 3:4 prove that: 12b^2 = 49ac
 32. For what value of m, the equation x = mx + m + 1 = 0 may have its roots in the ratio 2:3
 33 Af \alpha and \beta are the roots of px^2 + qx + q = 0 prove that \sqrt{\alpha/\beta} + \sqrt{\beta/\alpha} + \sqrt{q/p} = 0
 34. If the quadratic equation x^2 + px + q = 0 and x^2 + p'x + q' = 0 have a common root, show that it must be
      either, \frac{pq-p}{q} or \frac{q-q}{q}
 35. If the equation x^2 + px + q = 0 and x^2 + qx + p = 0 have a common root, prove that either p = q or p + q
   \sqrt{q+1}=0
  36. Prove that the roots of the equation x^2 + (2k-1)x + k^2 = 0 are real if k \le \frac{1}{4}
  37 Af -4 is a root of the equation x^2 + px - 4 = 0 and the equation x^2 + px + q = 0 has equal roots, find the
       value of q.
  38/If the sum of the roots of the equation ax^2 + bx + c = 0 be equal to the sum of their squares, show that
        2ac = ab + b^2
  39/1f the difference of the roots of x^2 + 2px + q = 0 be equal to the difference of the roots of x^2 + 2qx + p
        0 prove that p + q + 1 = 0
   40 Af a+b+c=0 solve the equation (b+c)x^2+(c+a)x+(a+b)=0
   41. Find the length of the perpendicular from a point on a straight line x\cos\alpha + y\sin\alpha = p
   Find the length of the perpendicular from a point (x',y') on the line whose equation is Ax + By + C = 0
   43. Find the acute angle between the lines x - 3y - 6 = 0 and y = 2x + 5
   44. Find the equation of the bisectors of the angles between the lines
        a) 3x - 4y + 2 = 0 and 5x + 12y + 5 = 0
        b) x - 2y = 0 and 2y = 11x = 6
    45. The length of the perpendicular drawn from the point (a, 3) on the line: 3x + 4y + 5 = 0 is 4. Find the value of a.
    46. What are the points on the axis of x whose perpendicular distance from the straight line \frac{x}{a} + \frac{y}{b} = 1 is a
    47. Find the equation of the two straight lines each of which is parallel to and at a distance of \sqrt{5} from the line
    48. Find the equation of the two straight lines drawn through the point (0, a) on which the perpendicular drawn
         from the point (2a, 2a) are each of length a.
    49. Find the equation of the line which is at right angles to 3x + 4y = 12, such that its perpendicular distance
         from the origin is equal to the length of the perpendicular from (3,2). On the given line.
    50. The equation of the diagonal of a parallelogram is 3y = 5x + k. The two opposite vertices of a
         parallelogram are the points (1, -2) and (-2, 1). Find the value of K.
    51. Write the conditions of perpendicular Tyand parallelism of the lines represented by lx^2 + 2hxy + ny^2 = 0
    52. Find the bisectors of the angles between the pair of lines represent by ax^2 + 2hxy + by^2 = 0
    53. Find the angle between the line pair represented by ax^2 + 2hxy + by^2 = 0
    54. Find the angle between the pair of lines x^2 - 2xy\cot\theta - y^2 = 0
    Find the angle between the pair of lines x^2 + 6xy + 9y^2 + 4x + 12y - 5 = 0
  156. Find the value of k so that x^2 + kxy + 2y^2 + 3x + 5y + 2 = 0 may represent a pair of lines.
     57. Find the equation of the straight lines through the origin and at right angles to the lines x^2 - 5xy + 4y^2 = 0
     58. Find the equation to the straight lines passing through (1.1) and parallel to the lines represented by
      \sqrt{x^2 - 5xy + 4y^2 + x + 2y - 2} = 0
     59 Show that the points (1,2,3), (-1,-2,-3), (2,3,2) and (4,7,6) are the vertices of a parallelogram.
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60. Show that the points (1,1,1), (-2,4,1). (-1,5,5) and (2,2,5) are the vertices of a square.

61. Find the point where the line through the points (1,2,3) and (4,-4,9) meets the zx-plane.

62. Find the point where the line joining the points (1,2,3) and (4,-4,3) meets the $2x^2$ plane.

DAY-7

63. Compute the following limits

a)
$$\lim_{x \to 4} \frac{x^3 - 64}{x^2 - 16}$$
b) $\lim_{x \to a} \frac{\sqrt{3x} - \sqrt{2x + a}}{2(x - a)}$
c) $\lim_{x \to \infty} (\sqrt{x} - \sqrt{x - 3})$
c) $\lim_{x \to 0} \frac{1 - \cos 6x}{x^2}$
c) Discuss the continuity of $\int_{x \to \infty}^{1} \frac{\sin \sqrt{3x} - \sqrt{2x + a}}{2(x - a)}$
c) $\lim_{x \to \infty} \frac{1 - \cos 6x}{x^2}$
c) Discuss the continuity of $\int_{x \to \infty}^{1} \frac{\tan x - \tan y}{x - y}$

$$\lim_{\substack{x \to \infty \\ \text{lim} \\ x \to y}} (\sqrt{x-a} - \sqrt{bx})$$

$$\lim_{\substack{x \to \infty \\ \text{lim} \\ x \to y}} \frac{\sin(x-a)}{x^2 - a^2}$$

$$\lim_{\substack{x \to \infty \\ \text{lim} \\ \cos x - \cos y \\ x \to y}} \frac{\cos(x-a)}{x^2 - a^2}$$

 $\lim \sqrt[4]{x-2}$

 $\lim \sqrt{x} - \sqrt{c}$ $iv_x \to c \frac{1}{\sin x - \sin c}$

 $2x \rightarrow 64\sqrt[3]{x-4}$

64. Discuss the continuity of function at the given point

i)
$$f(x) = 2 - x^2$$
 for $x \le 2$
 $x - 4$ for $x > 2$ at $x = 2$
 $2x + 1$ for $x < 1$
ii) $f(x) = 2$ for $x = 1$ at $x = 1$
 $3x$ for $x > 1$

65. A function
$$f(x)$$
 is defined as follows $f(x) = \frac{2x^2 - 18}{x - 3}$ for $x \neq 3$
Find the value of k so that $f(x)$ is $f(x) = \frac{2x^2 - 18}{x - 3}$ for $f(x) = \frac{2x^2 - 18}{x - 3}$

Find the value of k so that f(x) is continuous at x=3

66. Find from definition the derivative of

i)
$$x^2 - 2$$
 ii) $\frac{1}{x}$ iii) $\frac{1}{x-1}$ iv) $\sqrt{1+x}$ v) $\frac{1}{\sqrt{3x+4}}$ 67. Find the derivative of

i)
$$(a + \sqrt{x}) (a - \sqrt{x})$$
 ii) $\frac{x^2 - a^2}{x^2 + a^2}$ iii) $\frac{1}{\sqrt{a^n - x^n}}$

i)
$$(a + \sqrt{x})$$
 $(a-\sqrt{x})$ ii) $\frac{x^2 - a^2}{x^2 + a^2}$ i
68 Use the chain rule find $\frac{dy}{dx}$ of
i) $y = 2u^2 - 3u + 1$ and $u = 2x^2$
ii) $y = \frac{t}{t^2 - 1}$ and $t = 3x^2 + 1$

69. Find from the first principles, the derivative of i) sin4x ii) $\cos^2 x$

70. Find the angle between the two lines whose direction cosines are proportional to 1,2,3 and 3,4,5 71. Find the angle between the lines whose direction ratio are 1,2,4 and -2,1,5