c) Ā⊆B

F.M.: 75 P.M.: 30

	Group 'A'
1.	Which one of the following is the symbolic form of connective in the
	statement "students are hardworking and happy"?
	a) $\vee$ b) $\wedge$ c) $\Rightarrow$ d) $\Leftrightarrow$
2.	Let A, B and C are subsets of universal set U, such that A⊆B then
T. A	a) $C-B \subseteq C-A$ b) $C-A \subseteq C-B$

d) Ā⊆ B

3. If |2x-1| < 5,  $x \in \mathbb{R}$ , then the possible value of x lies in the interval

a)  $(-\infty, 3)$ b) (-2, 3)c)  $(-\infty, -2) \cup (3, \infty)$ d)  $(3, \infty)$ 

4. What is the determinant of A = [-3]?

a) 3 b) 3 c) 0 d) 1

5. One of zero's of the polynomial  $f(x) = x^2 - x - 2$  is

a) 0 b) 1 \_c) 2 d) -2

6. Which one of the following is not parallel to y = 4x-7?

a) y = 4x-7 b) 4x+y = 10 c) y-7 = 4(x-2) d)  $x = \frac{y}{4}$ 

7. The sum of slopes of the lines represented by  $x^2+2hxy-6y^2=0$  is equal to the product of slopes then h equal to

a) 4 (b) -2 c) -6 d) 8

3.	Which one of the following expression doesn't representing indetermina	ate
	form	
	a) $\frac{0}{0}$ b) $0 \times \infty$ c) $\frac{\infty}{0}$ d) $1^{\infty}$	
9.	Value of $\lim_{x\to 0} \frac{1}{x}$ is	
	a) 0 b) 1 c) -1 d) doesn't exist	
10.	$\lim_{x\to\infty} x \sin\frac{1}{x} is$	
	a) 1 b) $-1$ c) 0 d) can not be said	
11.	Given function $f(x) = \frac{ x }{x}$ , then $f(x)$ is discontinuous at $x = 0$ because	
	a) limit doesn't exist	
	b) limiting values infinity	
	c) limit exist but not equal to functional value	
	d) Functional value is infinity  Group 'B'	
12. a	Define conjunction of two statements	[1]
b	Let p and q be any two statement, prove that:	
	$\sim (p \lor q) \equiv (\sim p \land \sim q)$	[3]
Ç	Find the truth value of statement "If $2\times 3 = 6$ or $2+3 = 6$ then $5 < 0$ "	[1]
13. a	If A, B and C are subsets of universal set U then prove	that
	$A \cap (B \cup C) = (A \cap B) \cup (A \cap C).$	[2]
b	For any two real numbers x and y show that $ x+y  \le  x  +  y $	[3]
	Find the distance from the point $(-2, -3)$ to the line $2x - 3y + 5 = 0$ .	[2]
	Find the equation of the bisector of the angles between the lines 3x-2y	= 5
	and $6x+2y+15=0$ which contains the origin.	[3]

13. a) Write the conditions for angle between pair of straight line represented by  $ax^2+2hxy+by^2=0$  to be perpendicular. [1]

b) If p and p' be the length of the perpendicular from the origin upon the straight line whose equation are  $x \sec\theta + y \csc\theta = a$  and  $x \cos\theta - y\sin\theta = a \cos^2\theta$ , prove that  $4p^2 + p'^2 = a^2$ . [4]

16. a) If 
$$\alpha$$
 &  $\beta$  are the roots of  $px^2+qx+q=0$ , prove that  $\sqrt{\frac{\alpha}{\beta}}+\sqrt{\frac{\beta}{\alpha}}+\sqrt{\frac{q}{p}}=0$ . [3]

b) If the equation  $x^2 + (k+2)x + 2k = 0$  has equal roots, find value of 'k'? [2]

17. a) Define symmetric matrix. [1]

b) If 
$$A = \begin{pmatrix} 2 & 4 & 3 \\ 2 & 3 & 4 \\ 5 & 2 & 6 \end{pmatrix}$$

i) Find A<sup>T</sup>

ii) Show that the sum of given matrix and its transpose is a symmetric matrix.

[1]

matrix.

c) If  $A = \begin{pmatrix} 4 & x+2 \\ 2x-1 & 0 \end{pmatrix}$  and  $A = A^{T}$ , find the value of x. [2]

18. Find the limiting values of 
$$y \to 0$$
 
$$\lim_{y \to 0} \frac{(x+y)\sec(x+y) - x \sec x}{y}$$
 [5]

19. a) What do mean by indeterminate form. Give Example. [1]

To the function 
$$f(x) = \frac{x-1}{x+2}$$
 define for the value  $x = -2$ ?

c) Evaluate: 
$$\lim_{x\to 0} \frac{e^{2x}-1}{x \cdot 2^{x+1}}$$
 [3]

20. (a) Function f(x) is defined by

$$f(x) = \begin{cases} x^2 - 1 & \text{for } x < 2 \\ 2x & \text{for } x = 2 \\ x + 1 & \text{for } x > 2 \end{cases}$$

- i) Is the function continuous at x = 2?
- ii) If not how can you make it continuous at x = 2.

[4]

- b) Evaluate:  $\lim_{x \to 2} \frac{x \sqrt{8 x^2}}{\sqrt{x^2 + 12} 4}$
- Find the equation to the pair of straight line joining the origin to the intersection of the straight line y = mx + c and the curse  $x^2 + y^2 = a^2$ , prove that they are right angled if  $2c^2 = a^2(1+m^2)$ . [4]
  - by Solve the inequality  $|2x-1| \ge 3$  and draw its graph. [4]
- 22. a) The sum of the roots of the equation  $\frac{1}{x+a} + \frac{1}{x+b} = \frac{1}{c}$  is zero. Prove that the product of the roots is  $-\frac{1}{2}(a^2+b^2)$ .
  - b) Find the Coordinates of the points which is equidistant from the four pints
    O, A, B & C where O is origin A, B & C are the points on the x, y, z axis
    respectively at a distances a, b, & c from the origin.
    [4]