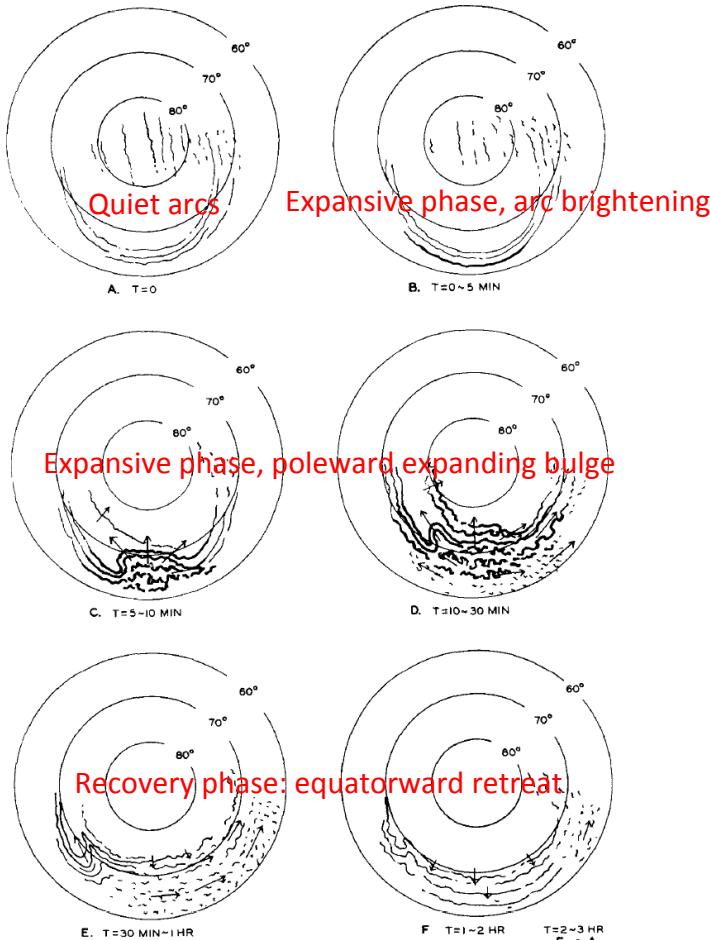
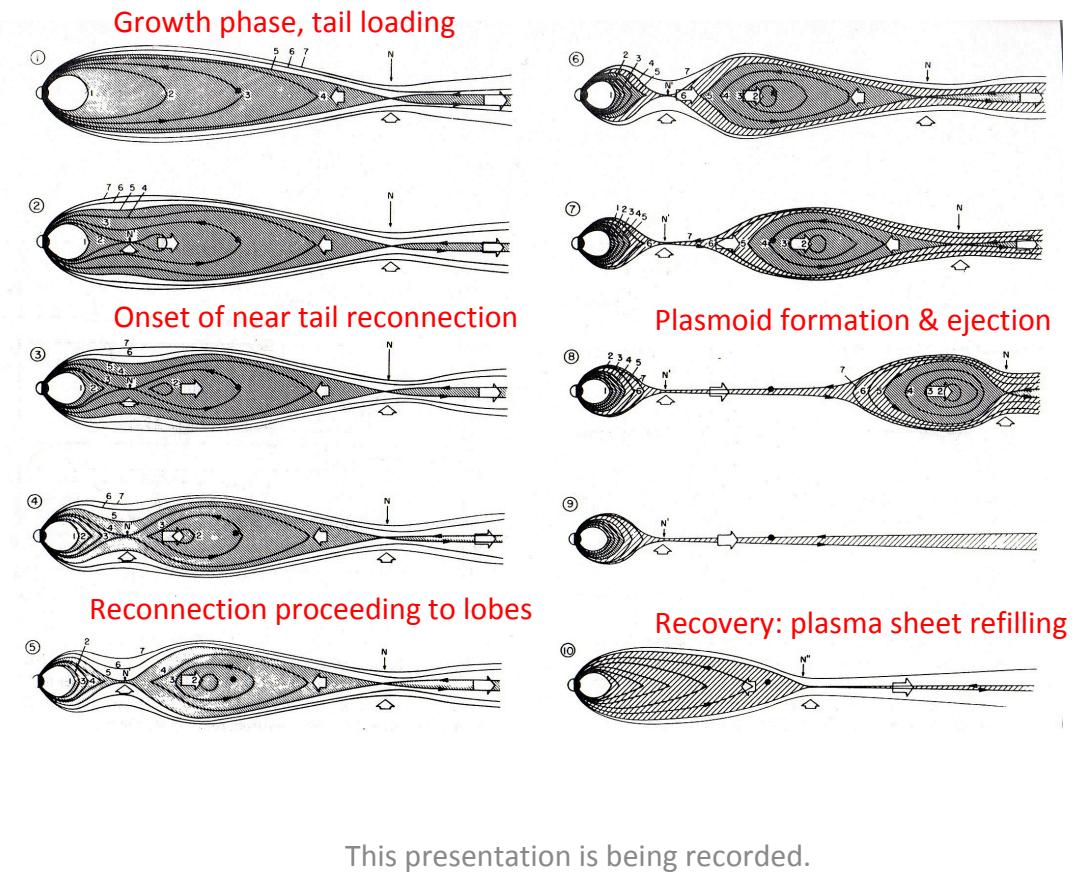


# The Dynamic Magnetotail: Substorms

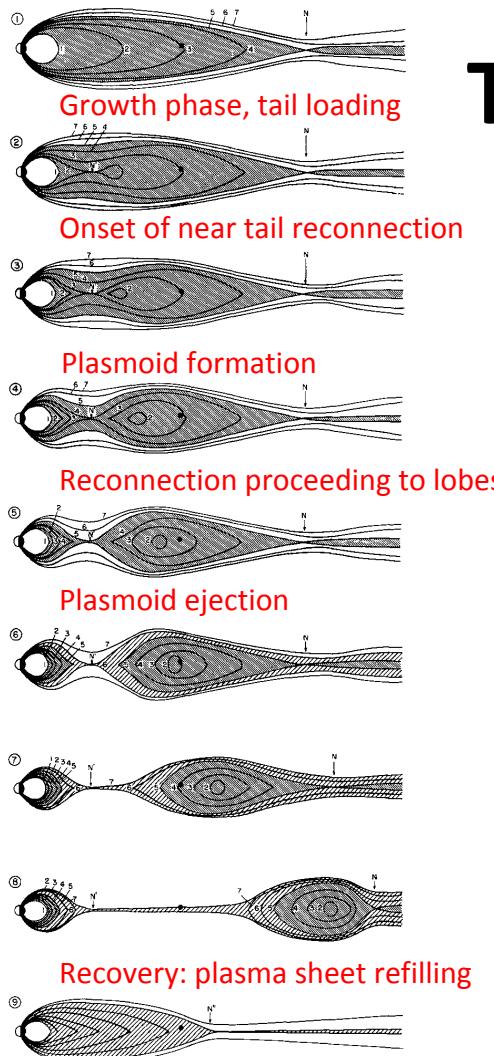
Auroral substorm (Akasofu, 1964,  
term owed to S. Chapman)



Magnetospheric substorm model  
(Hones, 1977, 1980)



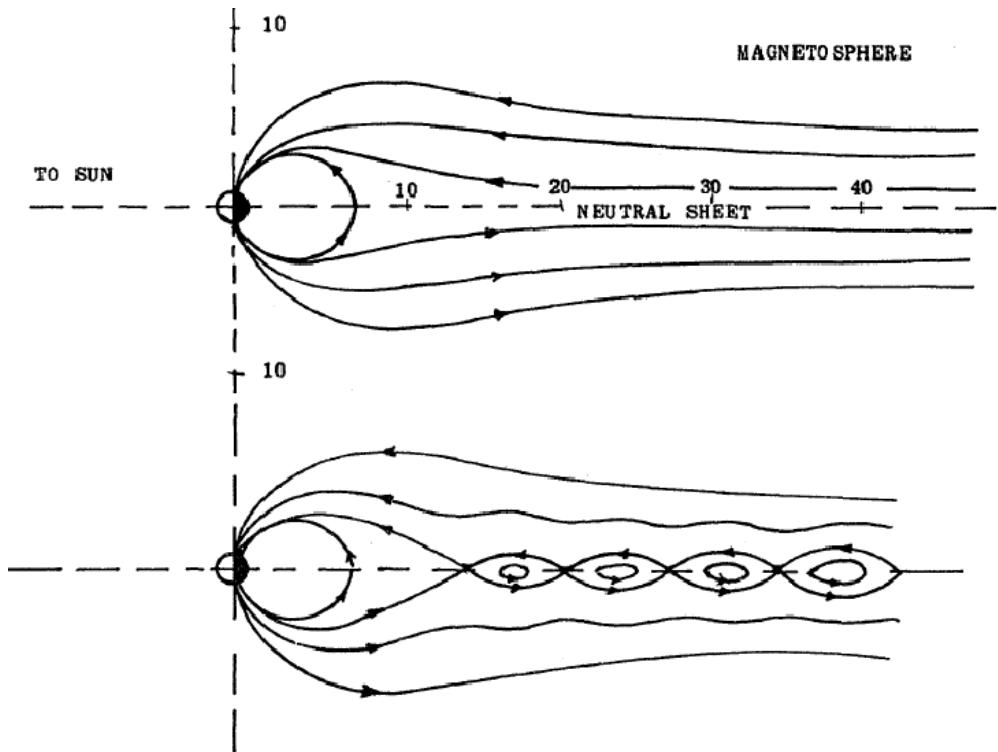
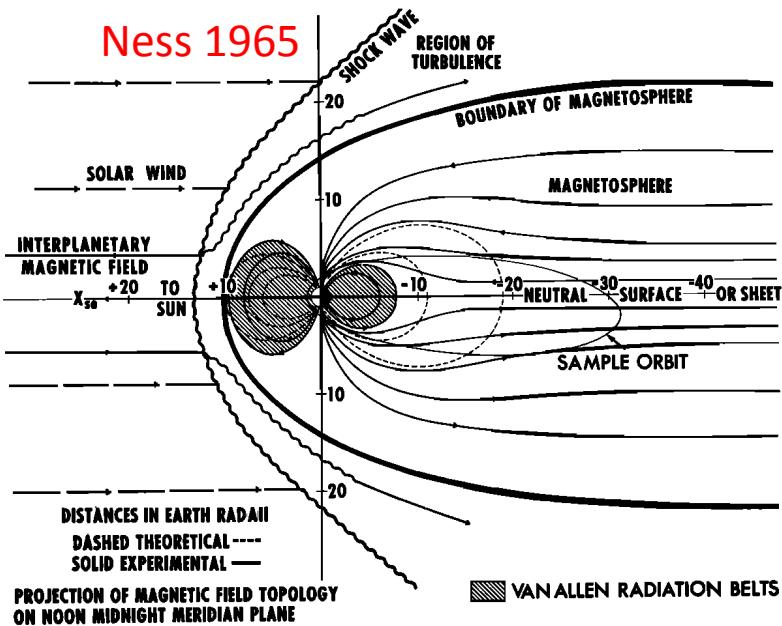
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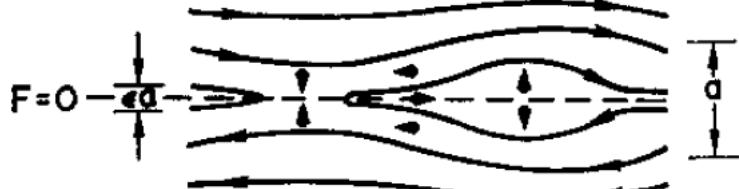
# The Dynamic Magnetotail: Outline

1. Origin of NENL-line model
2. Formation of thin current sheet (MHD)
3. Onset of reconnection (PIC simulations)
4. Substorm Expansion (MHD simulation):  
flow bursts, dipolarization,  
substorm current wedge
5. Particle acceleration (test particles)
6. Open problems

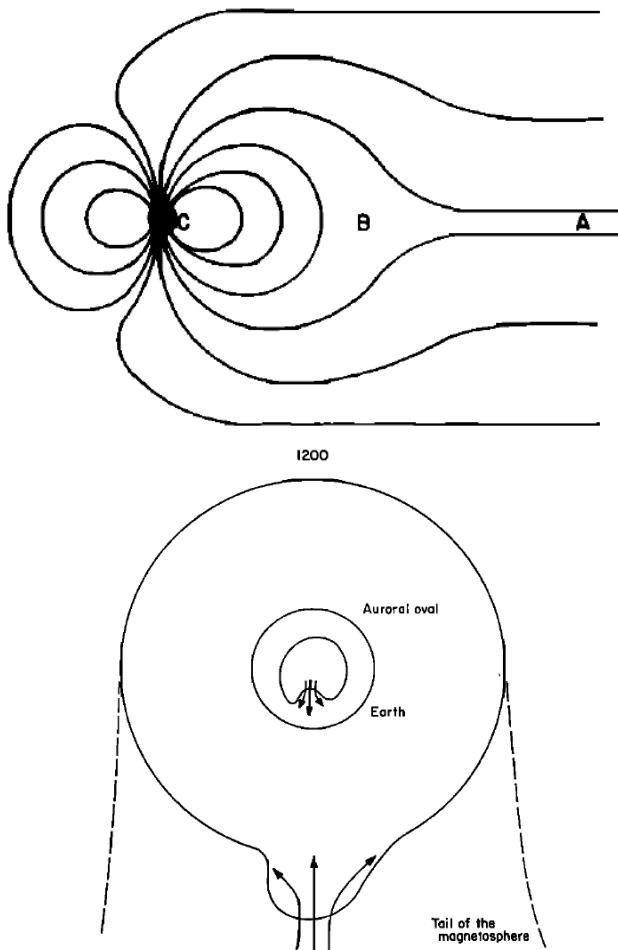
# Coppi, Laval & Pellat, 1966



Onset of (electron) tearing mode



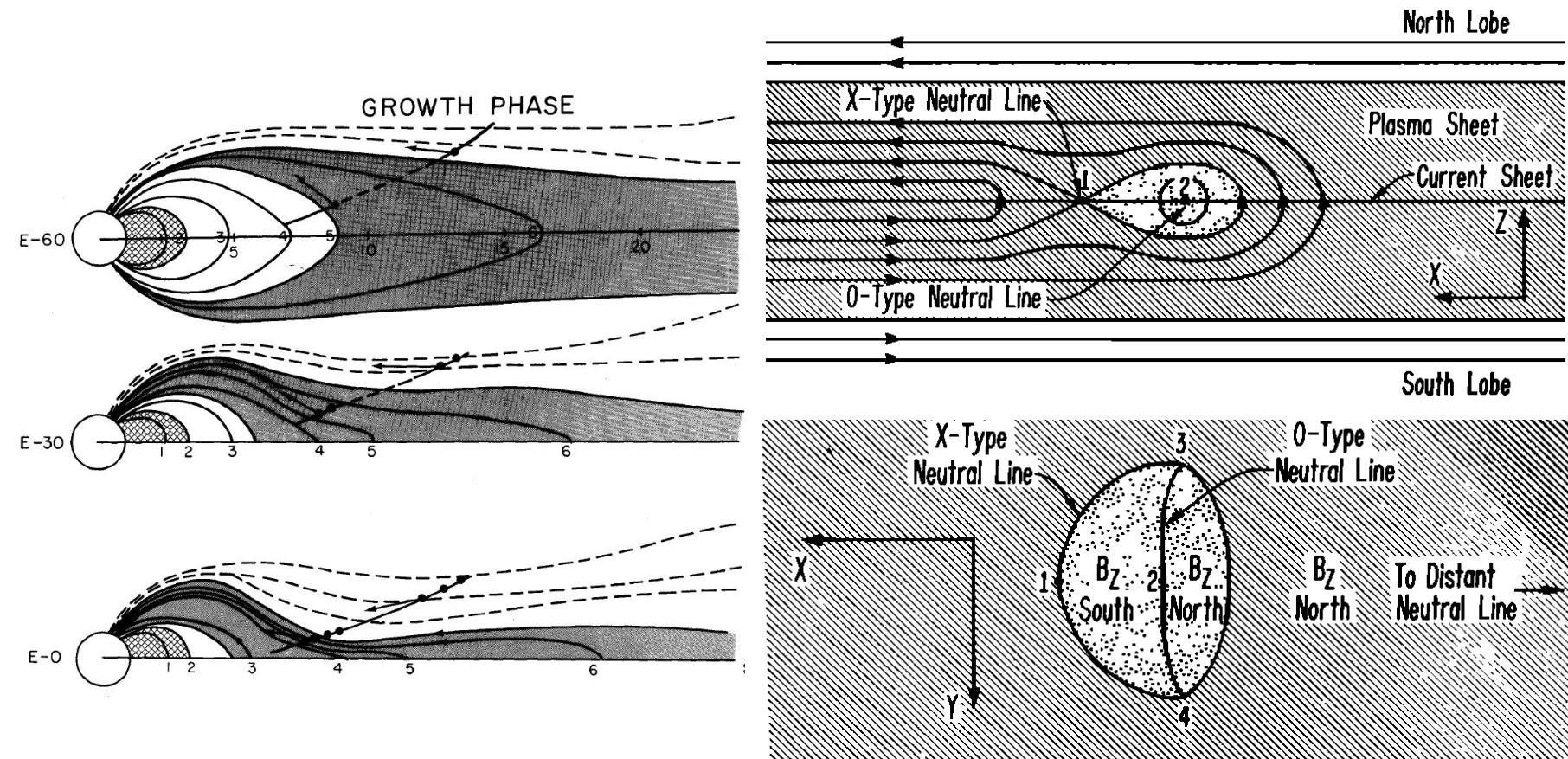
# Atkinson 1966, 1967



- a. The solar wind drags field lines from the region of closed field lines into the tail, either by viscous forces, or by the neutral-point mechanism proposed by *Dungey* [1958]. There is a resulting increase in the tail magnetic field strength and a storing of potential energy.
- b. The polar substorm begins when field lines recombine in an implosive fashion at the neutral sheet, in the manner indicated by *Petschek* [1964]. This recombination implies the release of stored potential energy.
- c. The recombined flux tubes are added to the night side of the closed region as a giant bulge, causing auroral effects.
- d. The flux tubes flow around the closed region toward the day side, causing the magnetic substorm and further auroral effects.

Credit to Axford (1965) and Dungey (1966)

# McPherron et al., 1973

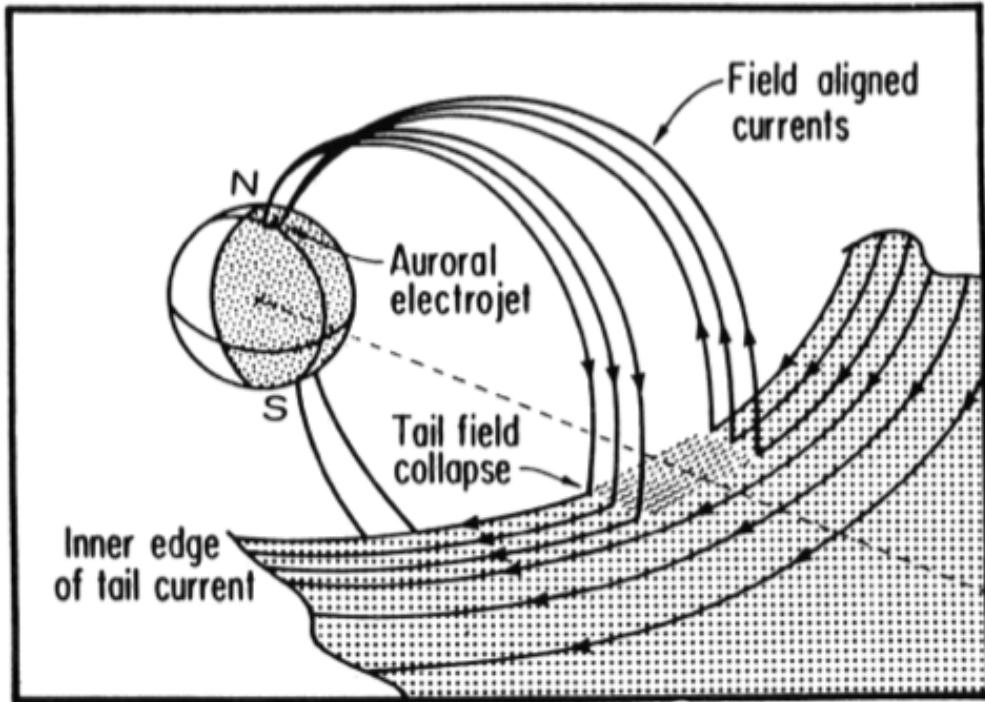
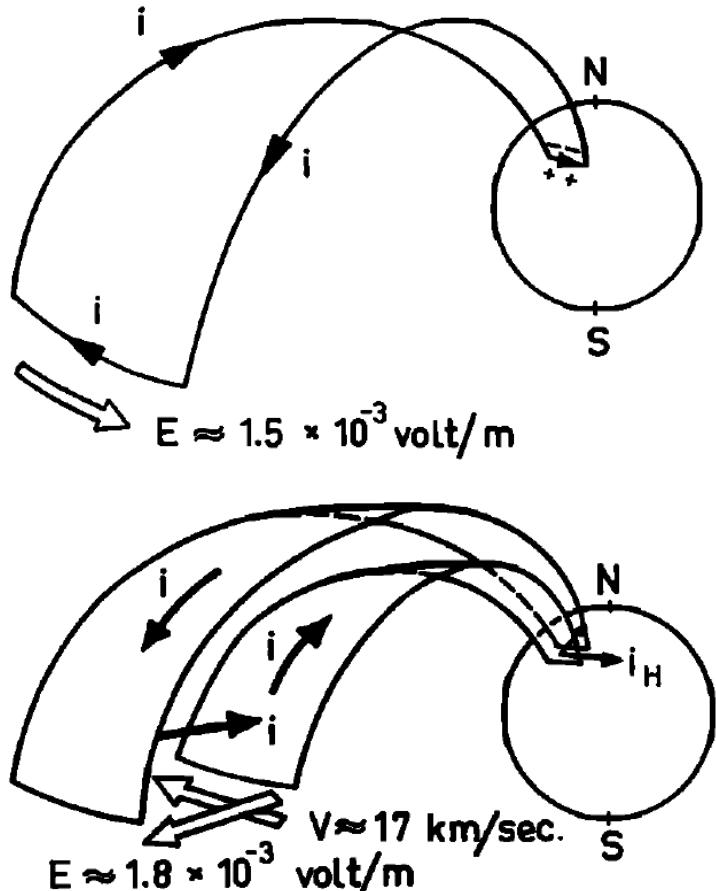


JGR, June 1973

Radio Science, Nov. 1973

This presentation is being recorded.

# Substorm current wedge



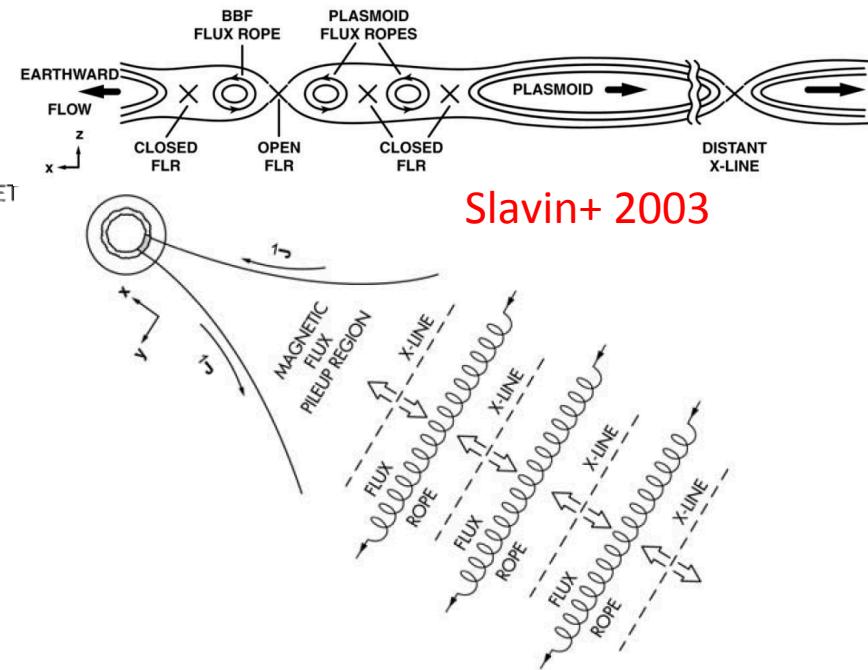
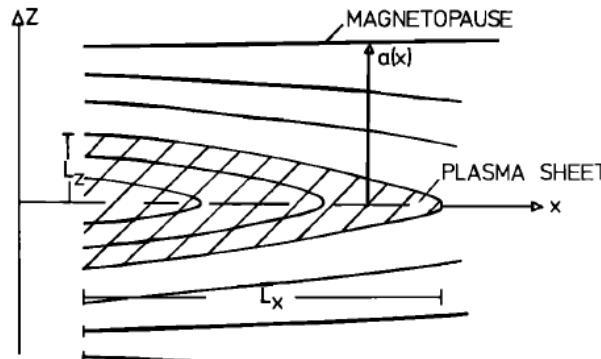
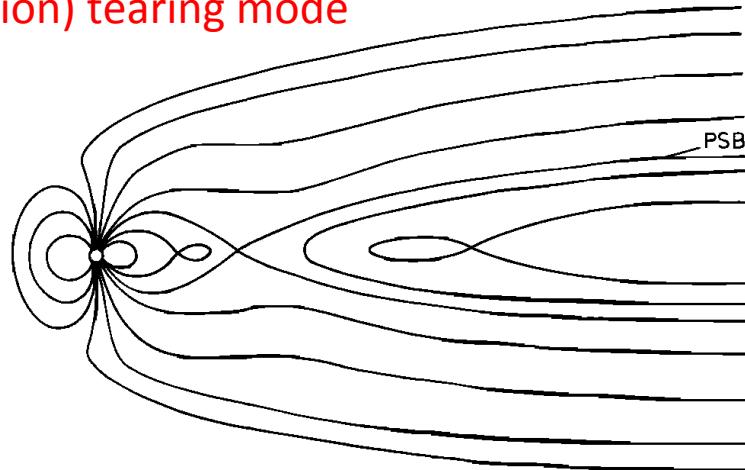
Boström, 1964

This presentation is being recorded.

McPherron+, 1973

# Theory of substorm mechanism, Schindler 1974

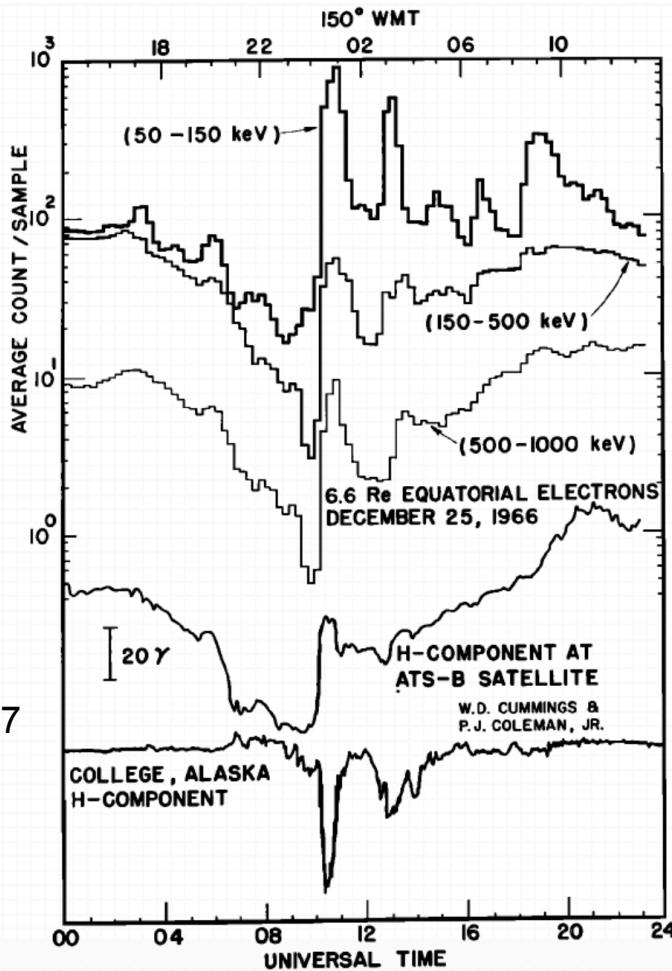
Tail configuration,  
finite  $B_z > 0$ ,  
destabilization by  
reduction of  $B_z$ ,  $L_z$   
Onset of (ion) tearing mode



Slavin+ 2003

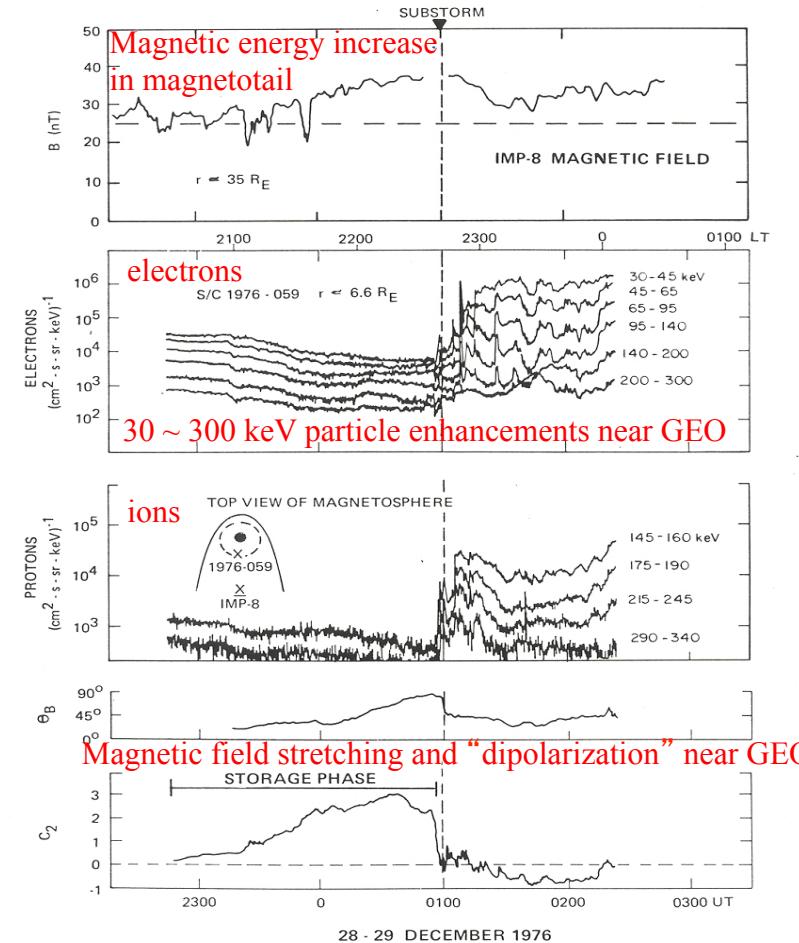
However: Ion tearing stabilized for small  $B_z$   
e.g., Pellat+ 1991, Pritchett 1994,  
Schindler 2007

# Substorm Particle “Injections”



Jelly & Brice, 1967  
 Konradi, 1967  
 Lezniak+, 1968  
 Hones+, 1968  
 Parks+, 1968

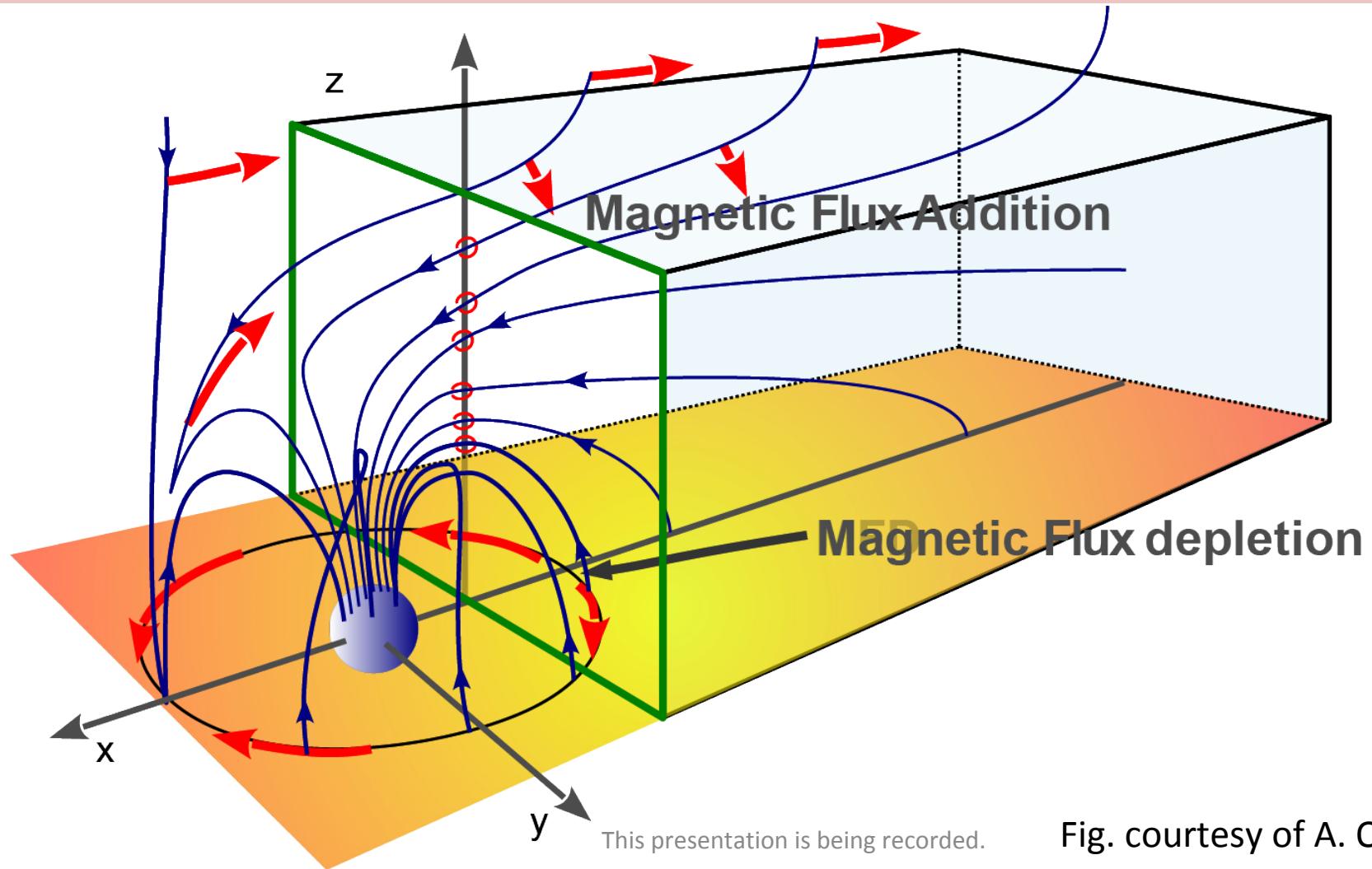
[Parks & Winckler, 1968]



This presentation is being recorded.

[Baker et al., 1981]

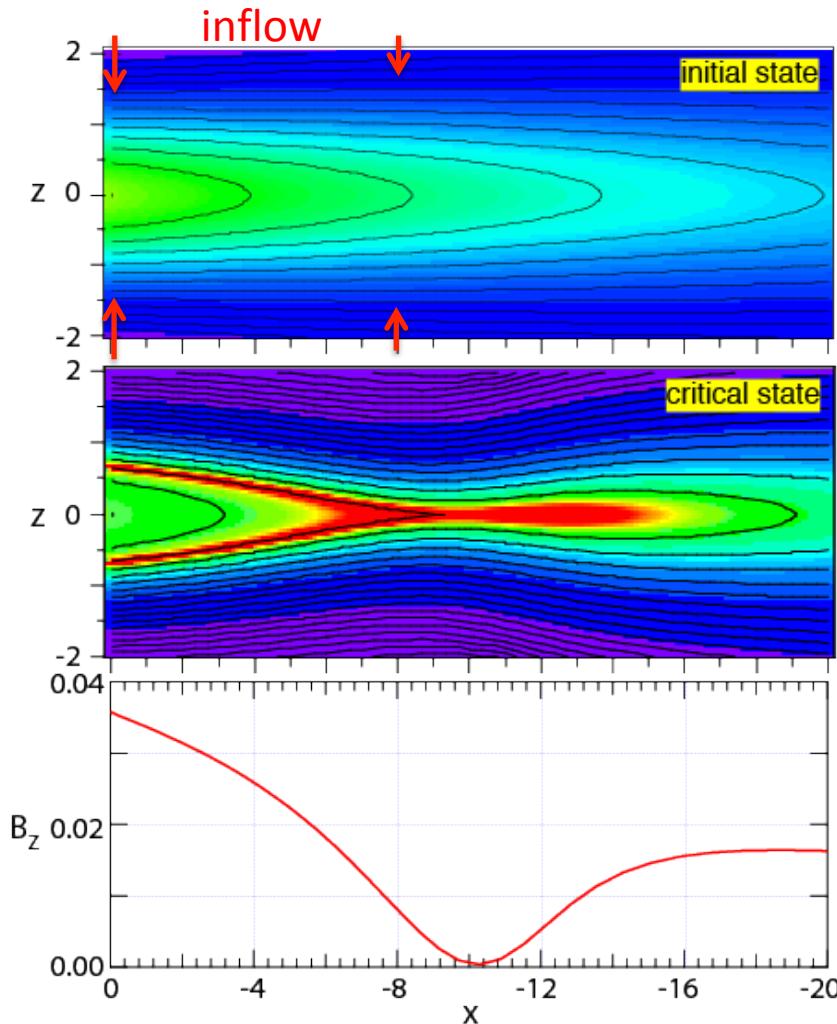
## 2. Pre-onset: Thin current sheet formation



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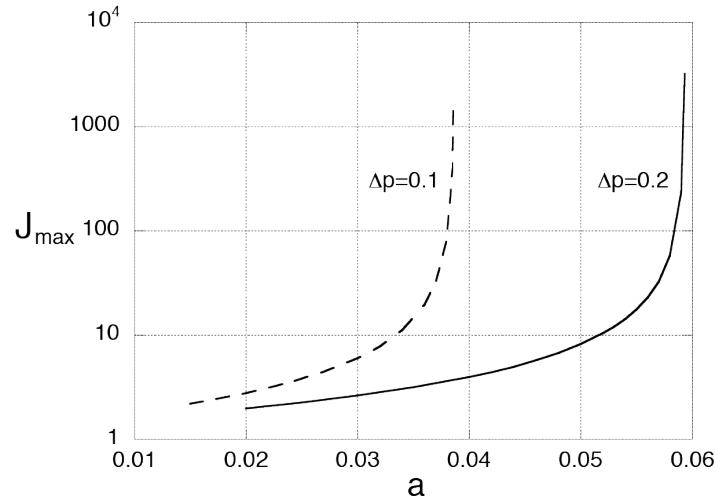
Fig. courtesy of A. Otto

# TCS formation: High latitude flux addition



2D Quasi-static theory:  
mass & entropy conservation

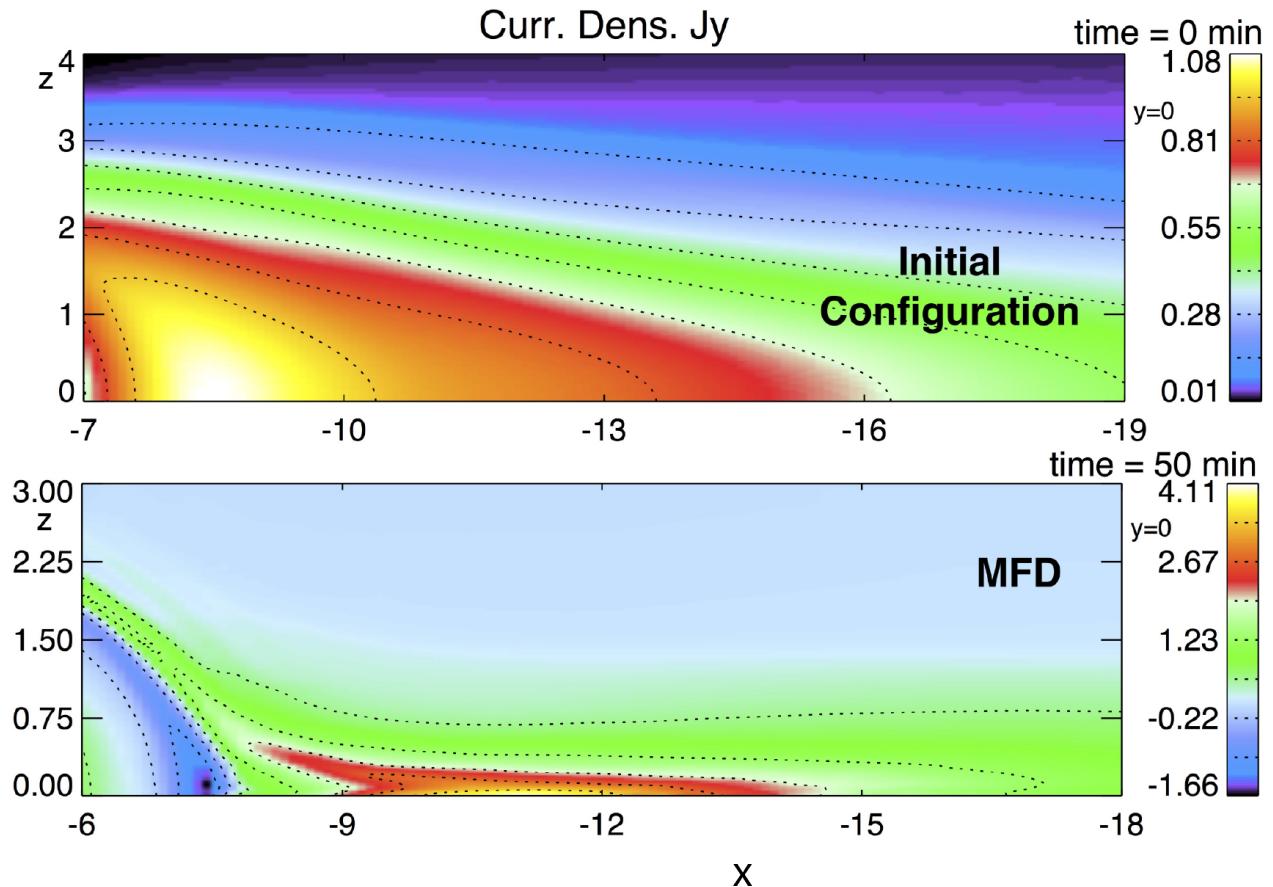
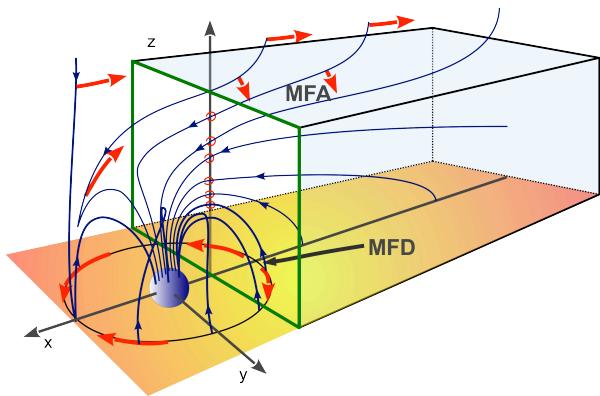
$$S = \int p^{1/\gamma} ds / B = p^{1/\gamma} V$$
$$V = \int ds / B$$



Finite deformation leads to critical point, loss of equilibrium, thin current sheet,  $B_z$  minimum

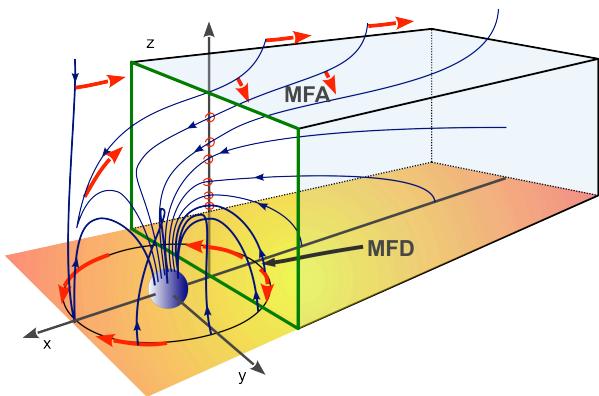
(Birn & Schindler, 2002)

# TCS formation: Low latitude flux depletion

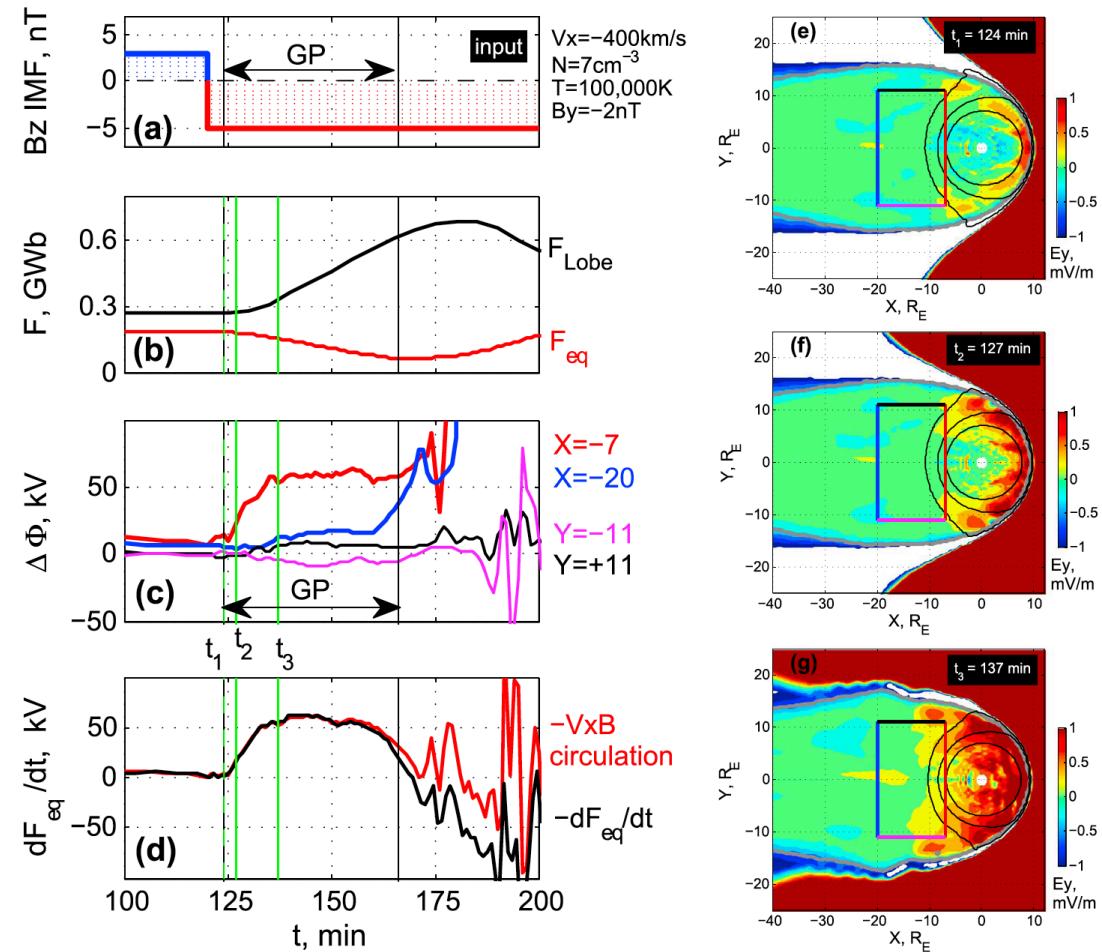


(Hsieh & Otto, 2014, 2015; Otto+, 2015)

# TCS formation: Low latitude flux depletion

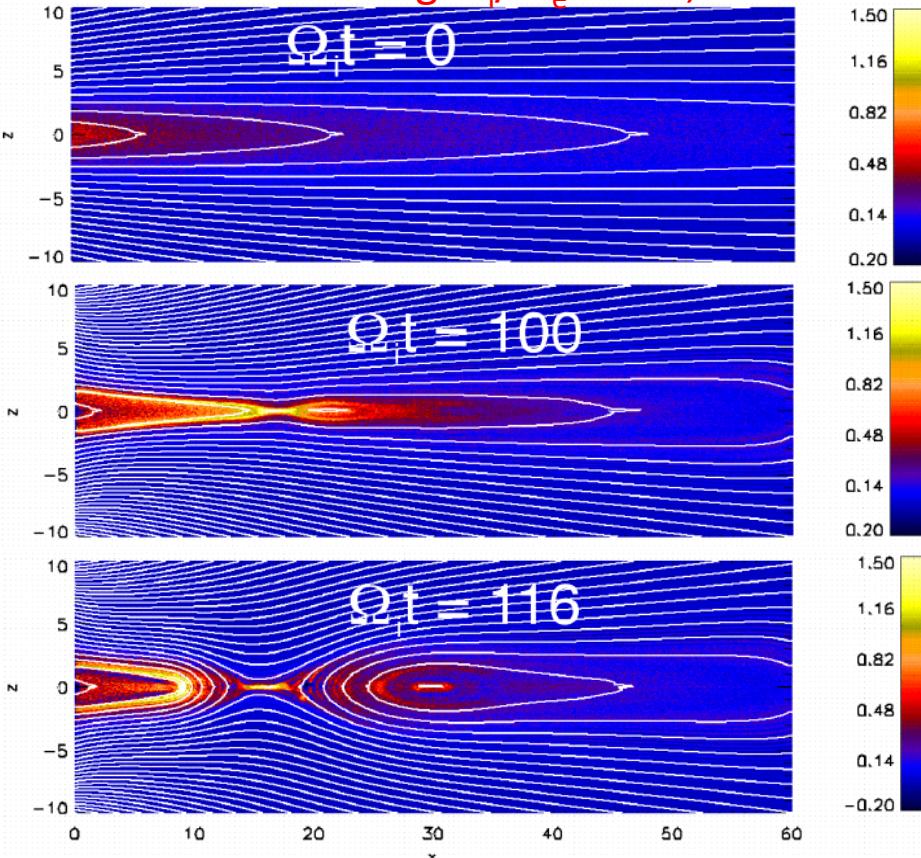


Gordeev+, 2017 (global LFM simulation):  
Removal of closed magnetic flux by  
return convection controls the major  
reconfiguration of near magnetotail  
during substorm growth phase



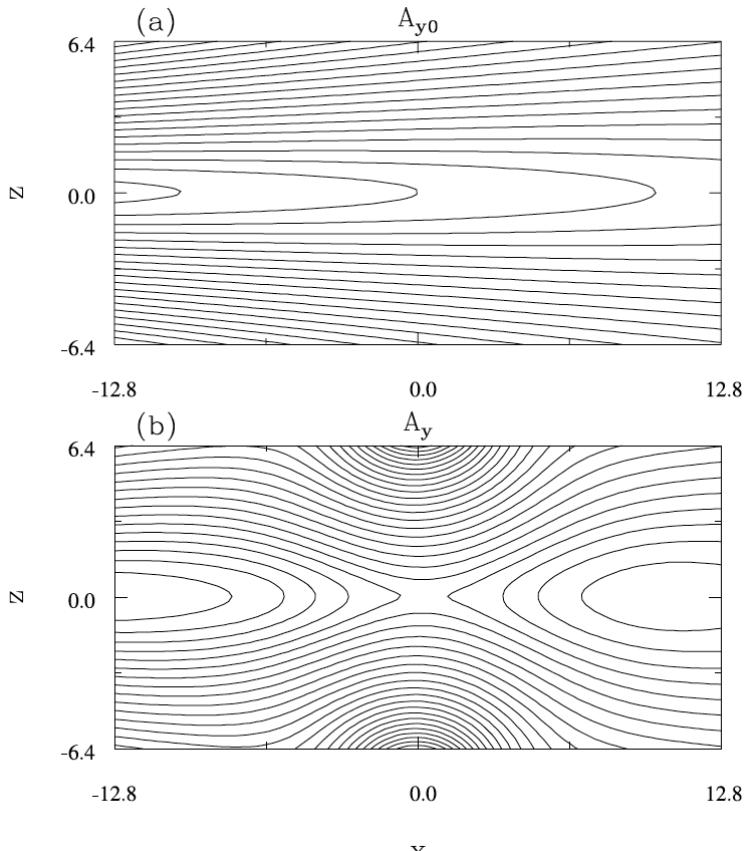
# 3. Onset of Reconnection: PIC Simulations

limited driving  $m_i/m_e = 100$ , 2D



Hesse & Schindler 2001

continued driving  $m_i/m_e = 100$ , 3D



(Pritchett&Coroniti, 1993) Pritchett 2005

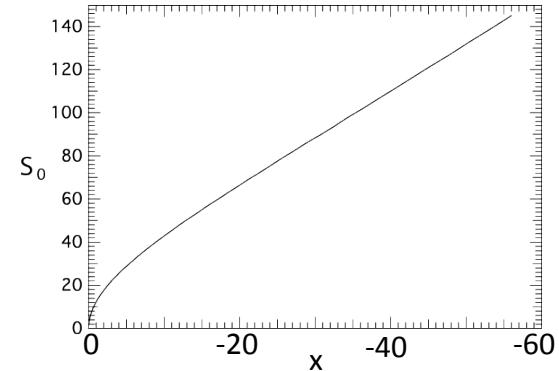
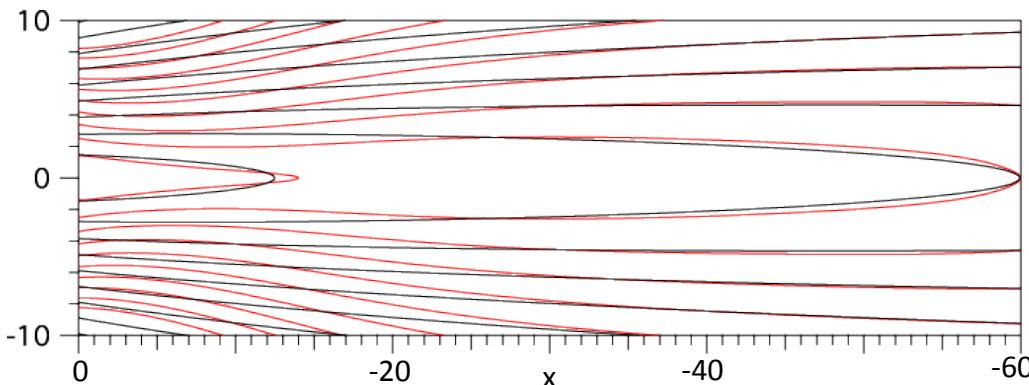
# Finite deformation of stable tail (LiuYH+ 2014)

Initial state:  $L_z = 2 d_i$ ,  $B_z = 0.05 B_0$

-> stability to tearing (e.g., Brittnacher et al., 1995; Daughton, 1999)

Monotonic entropy function,  $S = P^{1/\gamma} V$

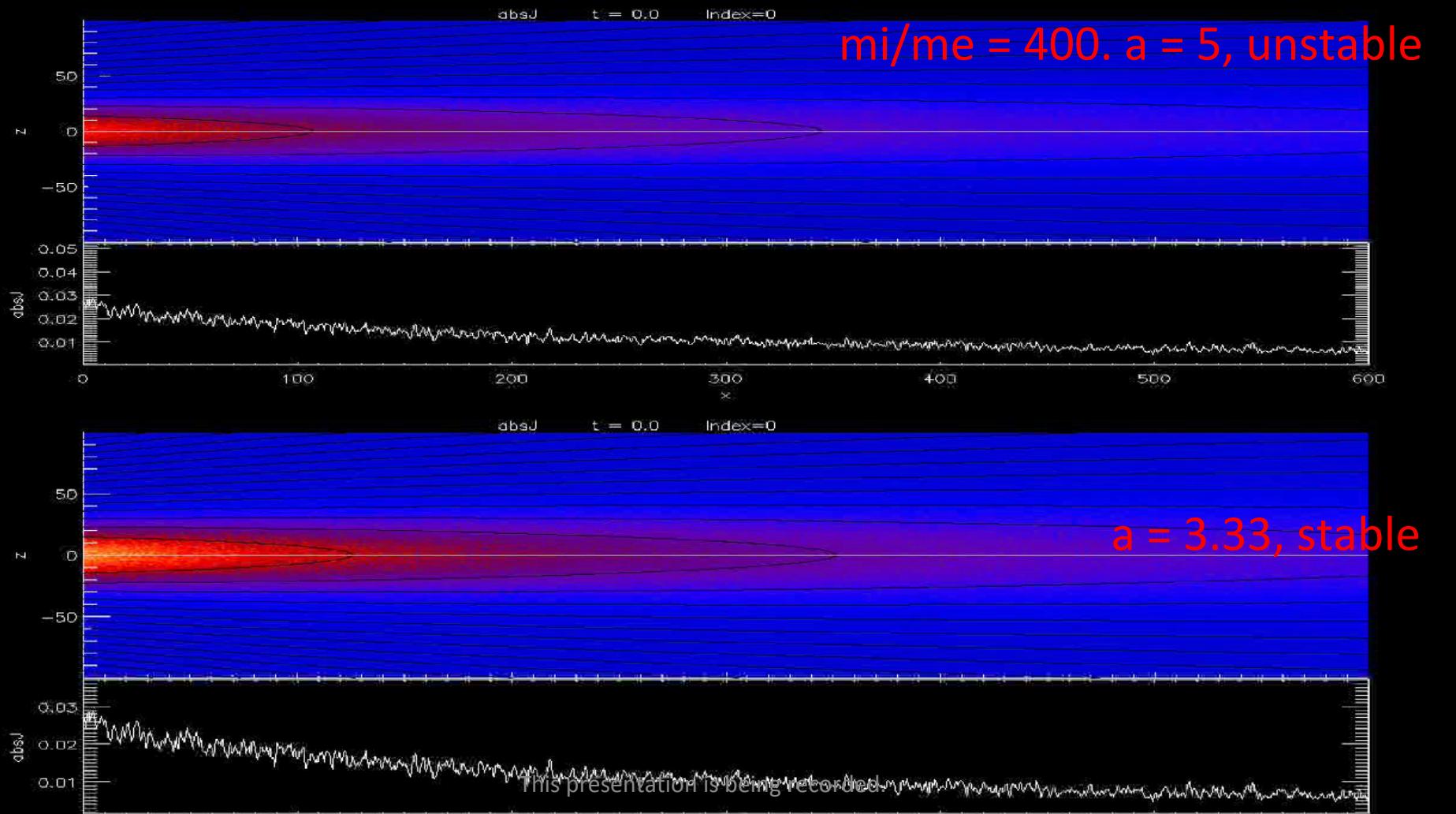
-> stability to ballooning/interchange (e.g., Schindler, 2007)



Finite deformation of tail equilibrium by temporally limited external inflow  
of magnetic flux; (vary amplitude  $a$ ,  $m_i/m_e$  up to 1836)

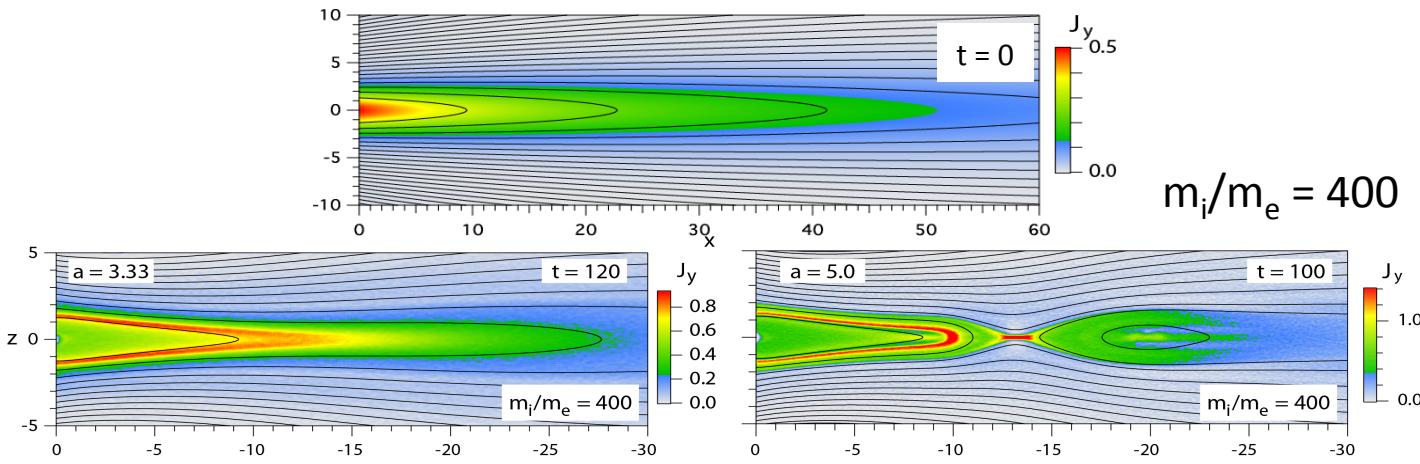
Formation of thin embedded current sheet – may or may not lead to onset,  
loss of equilibrium

# Finite deformation (Liu+ 2014)

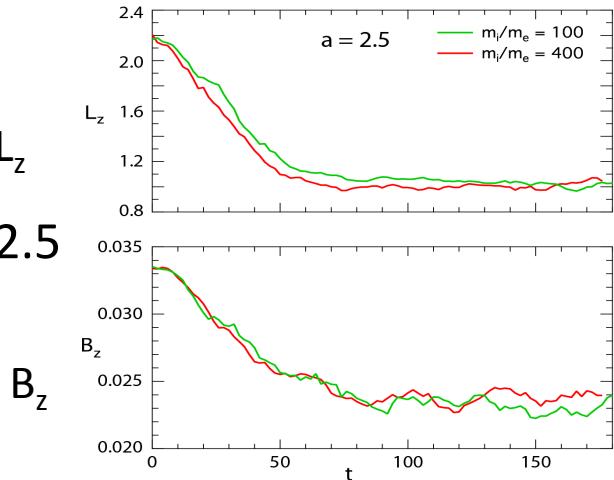


# Onset depends on deformation amplitude $a$

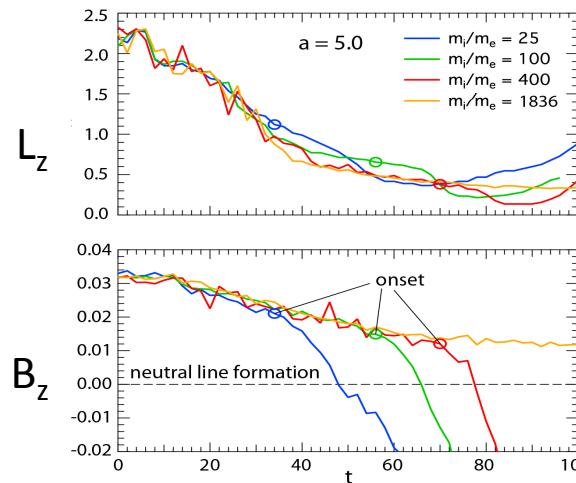
$a = 3.3$   
stable



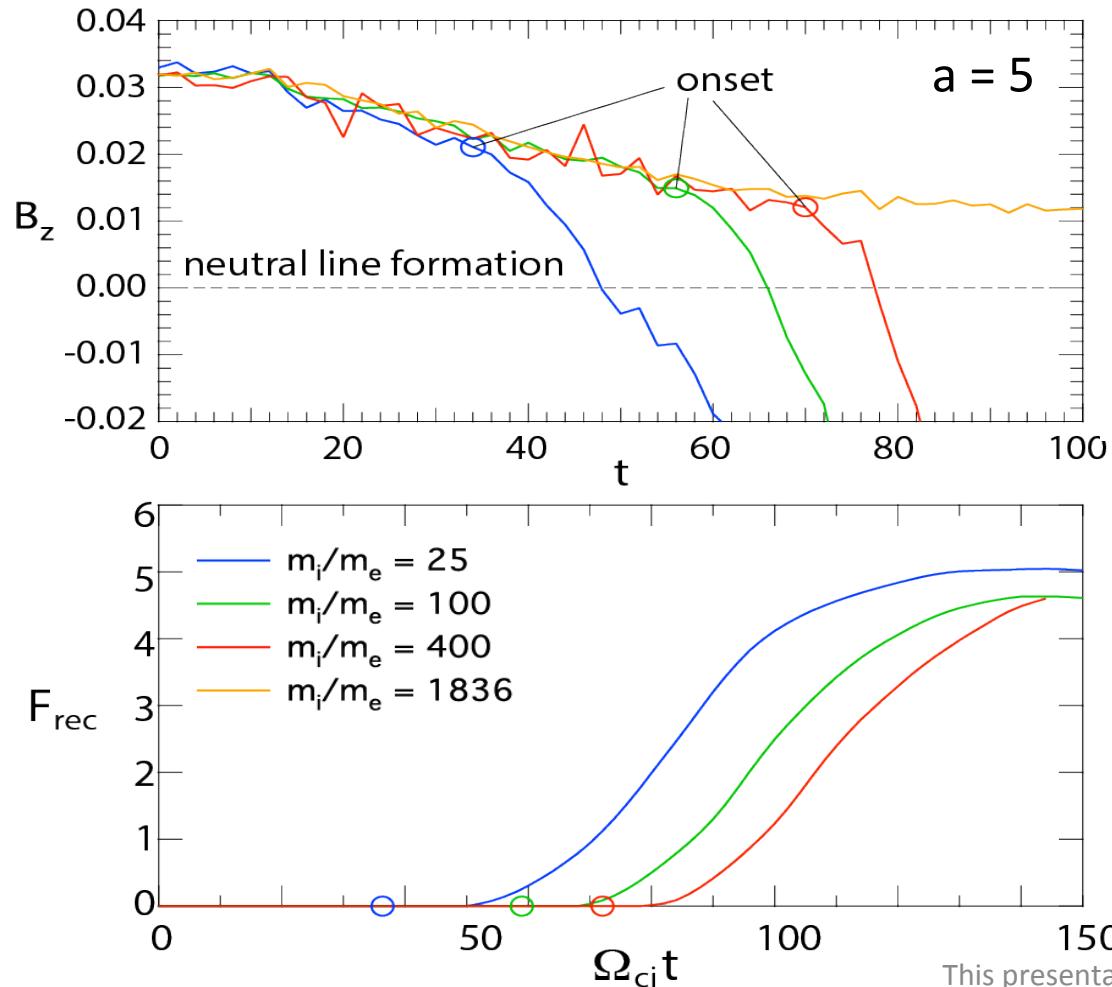
$a = 2.5$



$a = 5$



# Onset & Evolution: Dependence on Mass Ratio



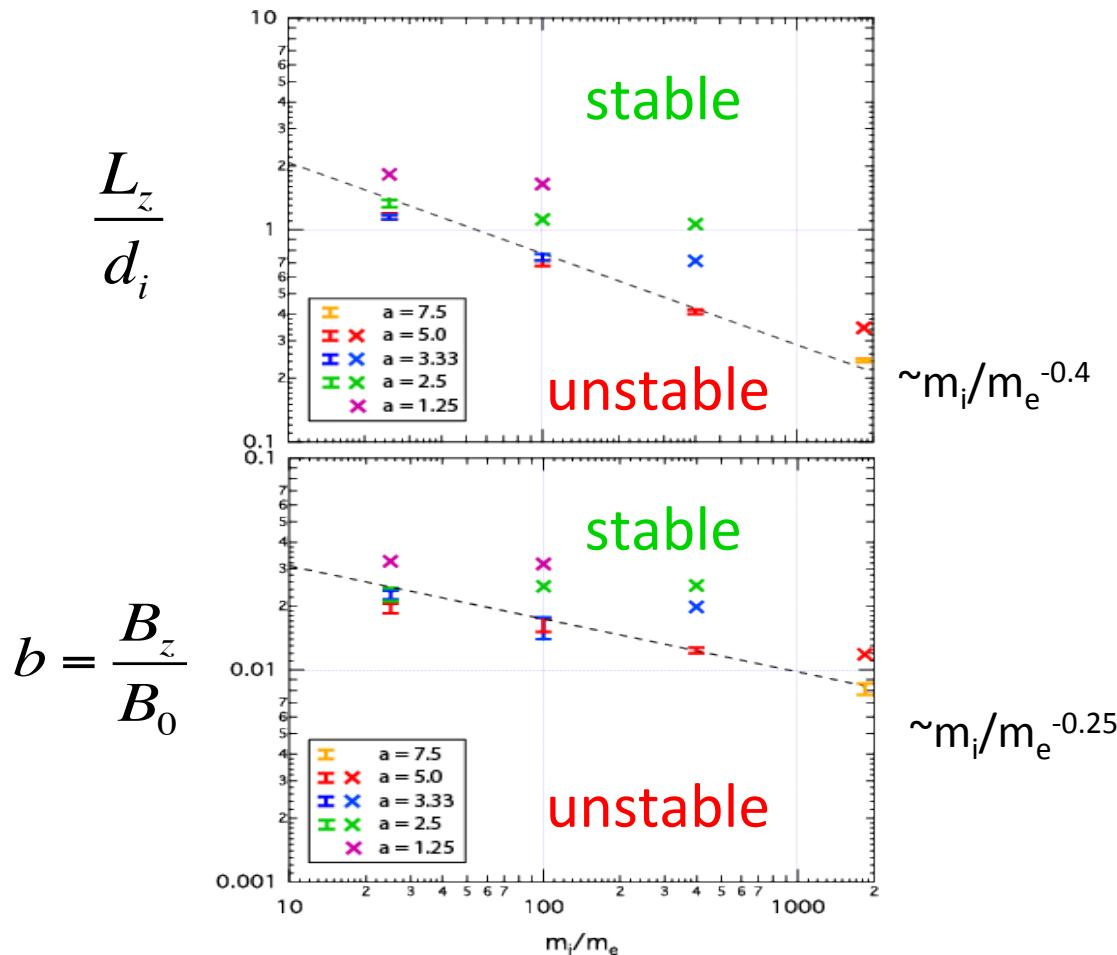
Early evolution independent of  $m_i/m_e$ , consistent with MHD

Onset depends on mass ratio

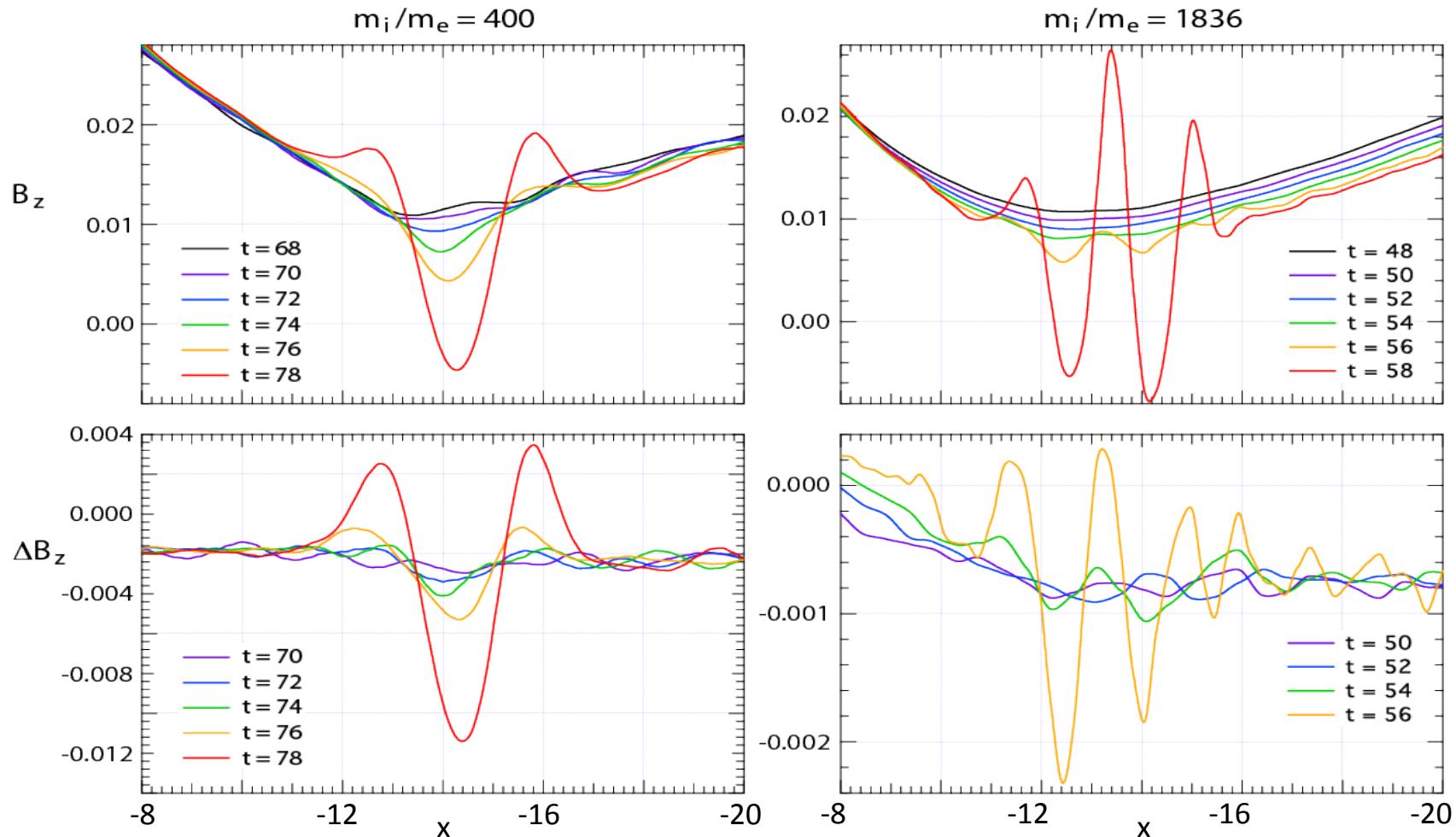
True mass ratio onset requires stronger deformation

Evolution after x-line formation does not depend on mass ratio (consistent with GEM studies)

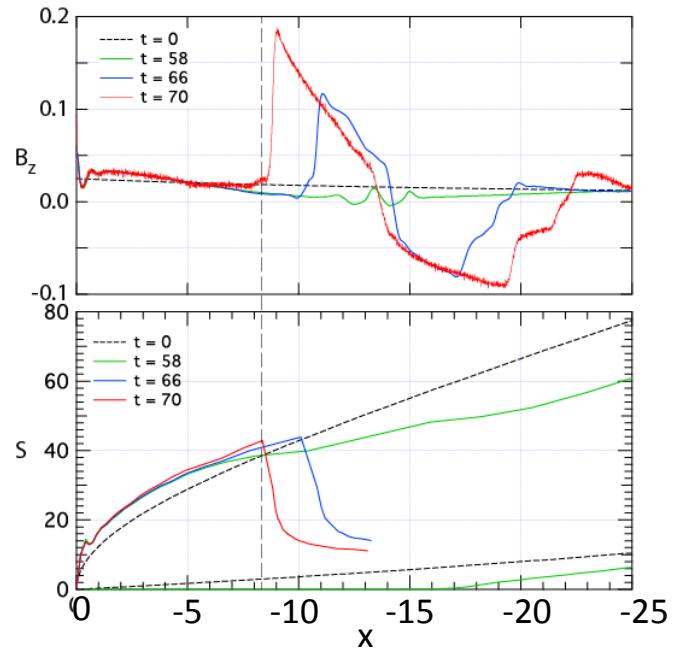
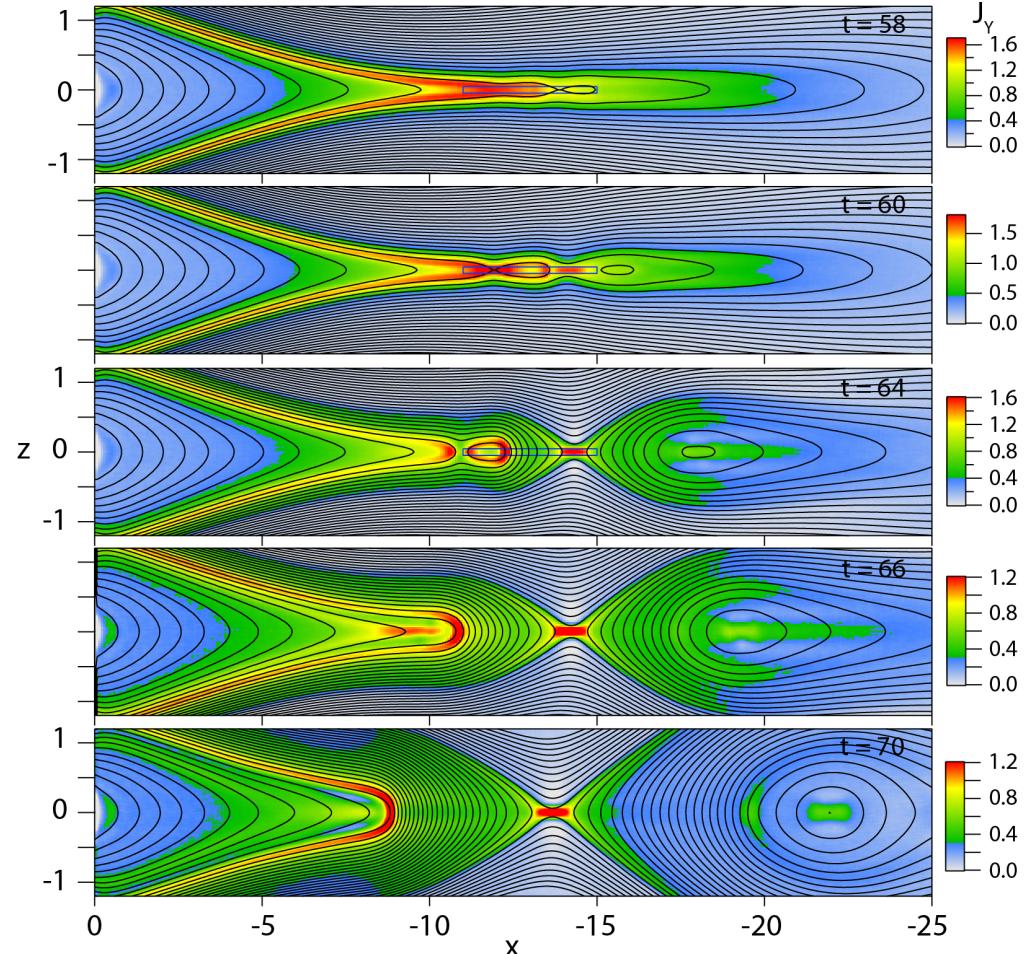
# Onset dependence on mass ratio $m_i/m_e$ , $L_z$ , $B_z$



# Unstable mode: electron tearing



# Evolution of tail reconnection at $m_i/m_e=1836$



Temporary secondary islands  
Steep dipolarization front  
Enhanced  $B_z$  – reduced entropy,  
not pile up of external flux

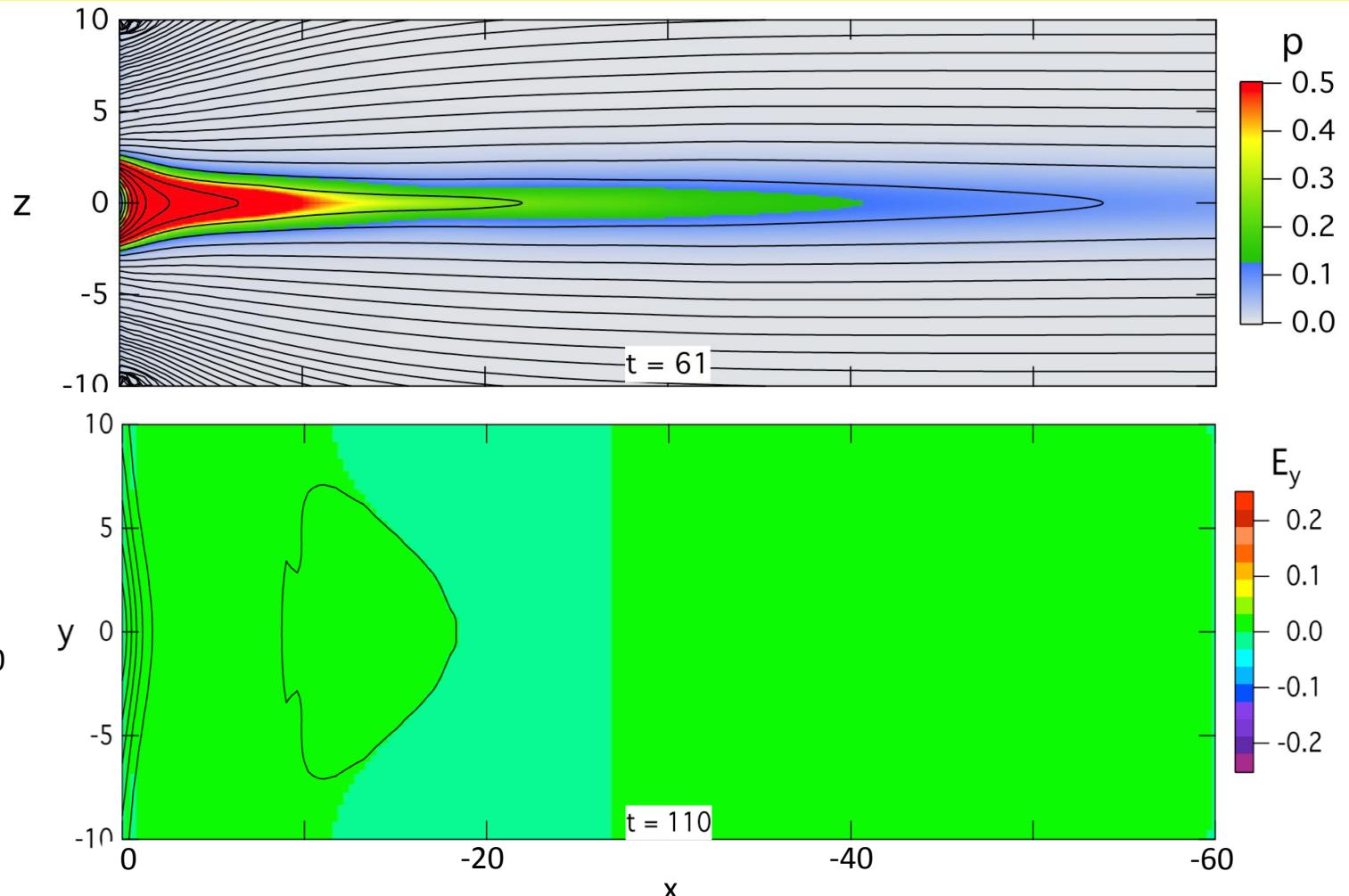
# Summary: Onset & Early Evolution

- CS thinning, onset of tearing instability depend on the amount of deformation, localization (continuous driving not necessary)
- Onset requires both (**local**) thinning and reduction of  $B_z$  (go together under external deformation)
- Early, stable evolution independent of mass ratio, consistent with MHD
- Onset of instability depends on mass ratio (electron tearing)
- Unstable tearing mode rises even before  $B_z$  changes sign (brief period)
- Fast evolution after x-line formation independent of mass ratio
- PIC (2D) evolution conserves entropy integral prior to onset:  
ballooning stability before onset of tearing, but plasmoid loss changes entropy integral, may enable ballooning instability

# 4. Dynamic Evolution: 3D MHD Simulation

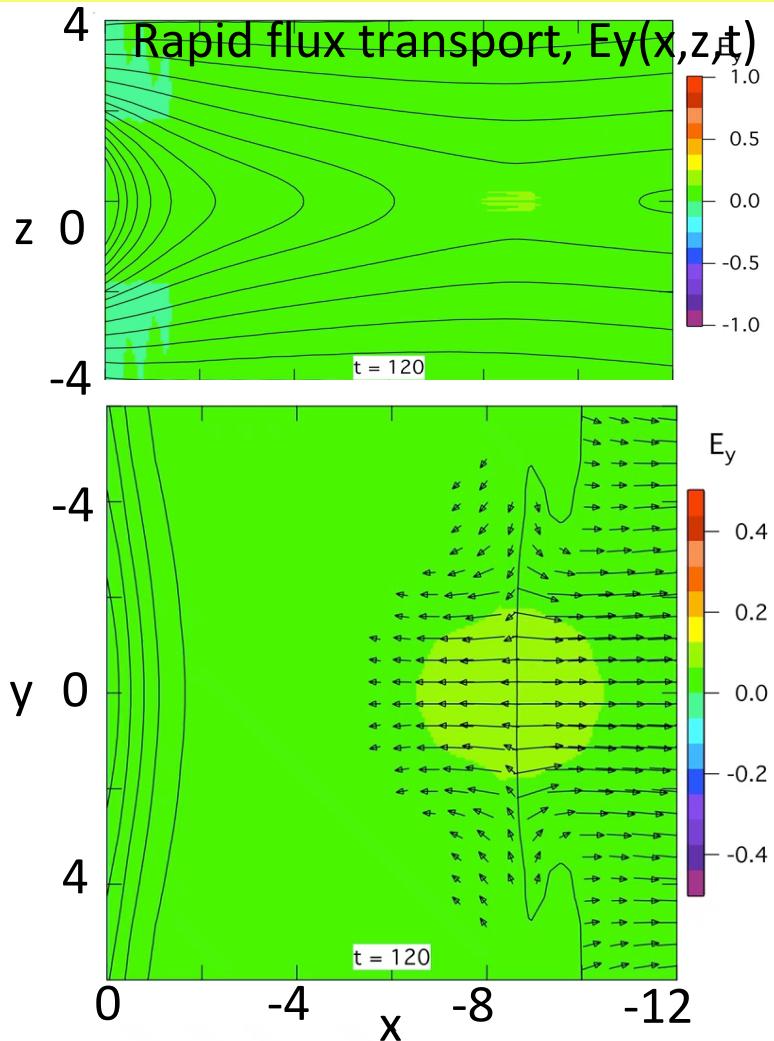
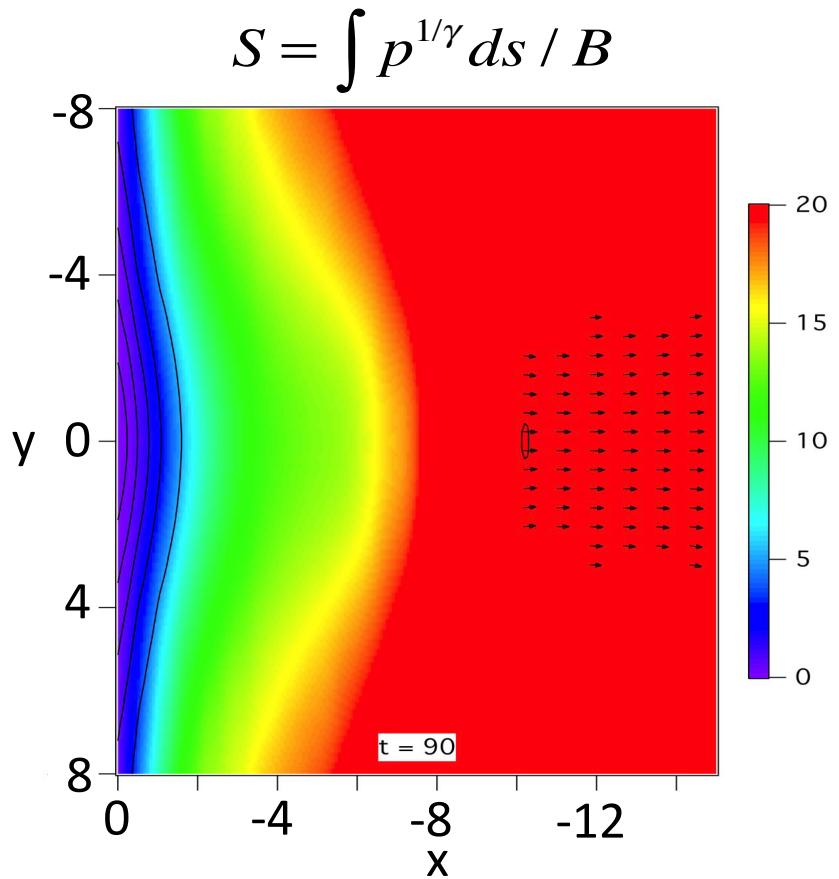
2D:  
(Leboeuf+, 1978)  
Birn, 1980  
Scholer&Otto, 1980  
Lyon+, 1981

3D:  
(Leboeuf+, 1981)  
Birn&Hones, 1981  
Brecht+, 1982  
Ogino+, 1986  
Fedder&Lyon, 1987  
Walker+, 1988  
Ogino+, 1994  
Watanabe&Sato, 1990  
Fedder+, 1995  
Tanaka+, 1995  
Lyon+, 1998  
Wiltberger+, 2000



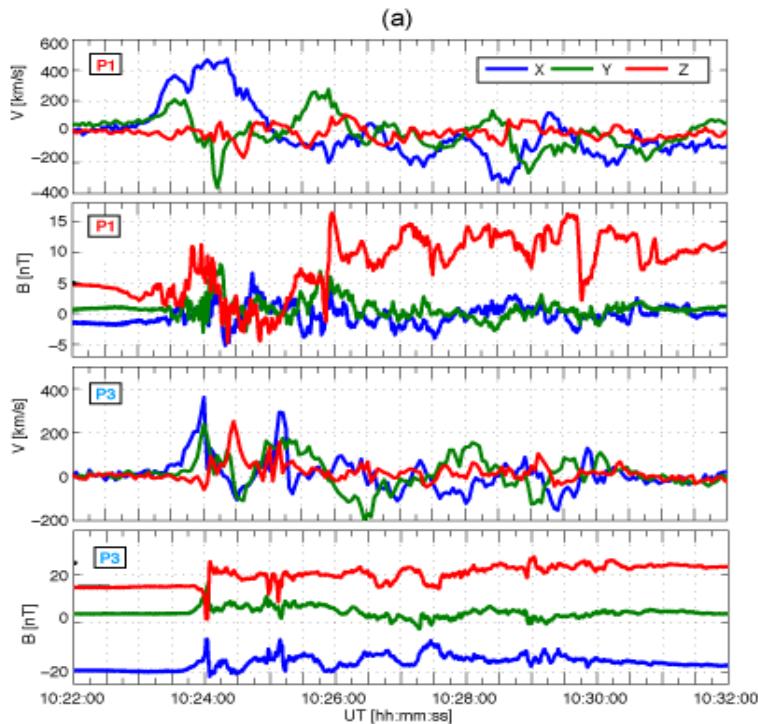
(Birn+ 2011)

# Entropy and Flow in 3D MHD Simulation

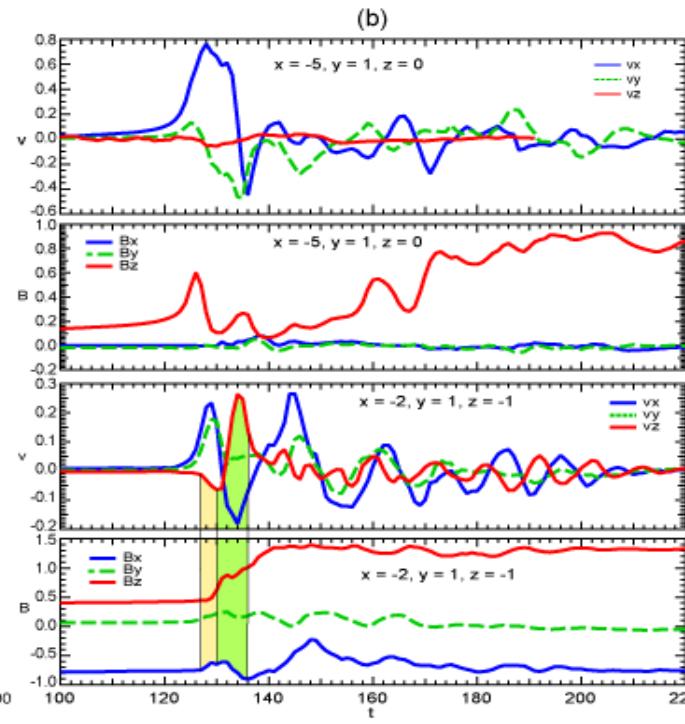


# 3D MHD Simulations & Observations

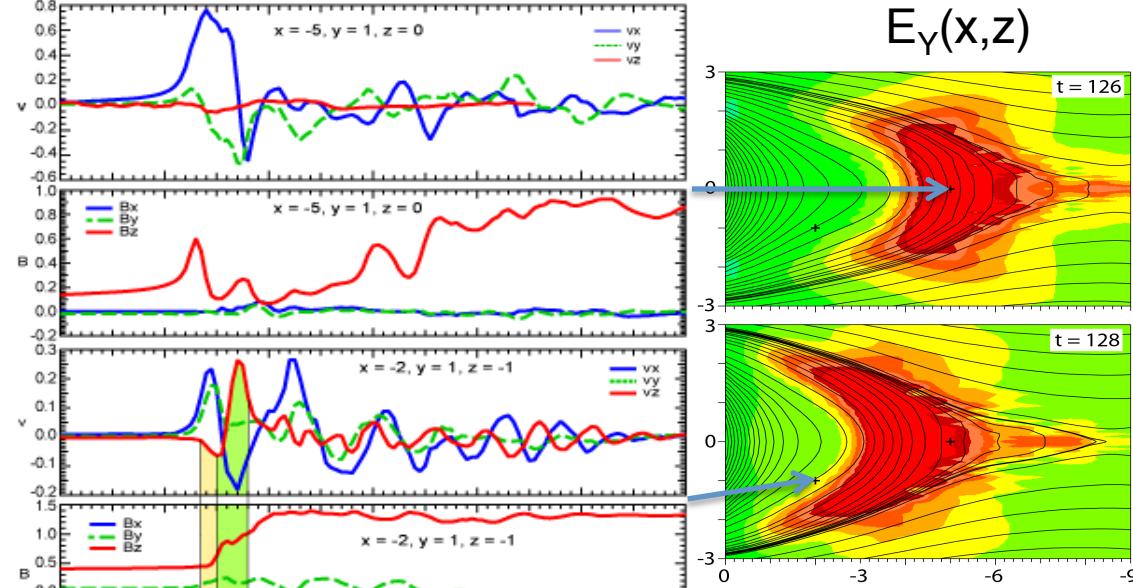
THEMIS observations  
(Panov et al., 2010)



MHD simulations  
(Birn et al., 2011)

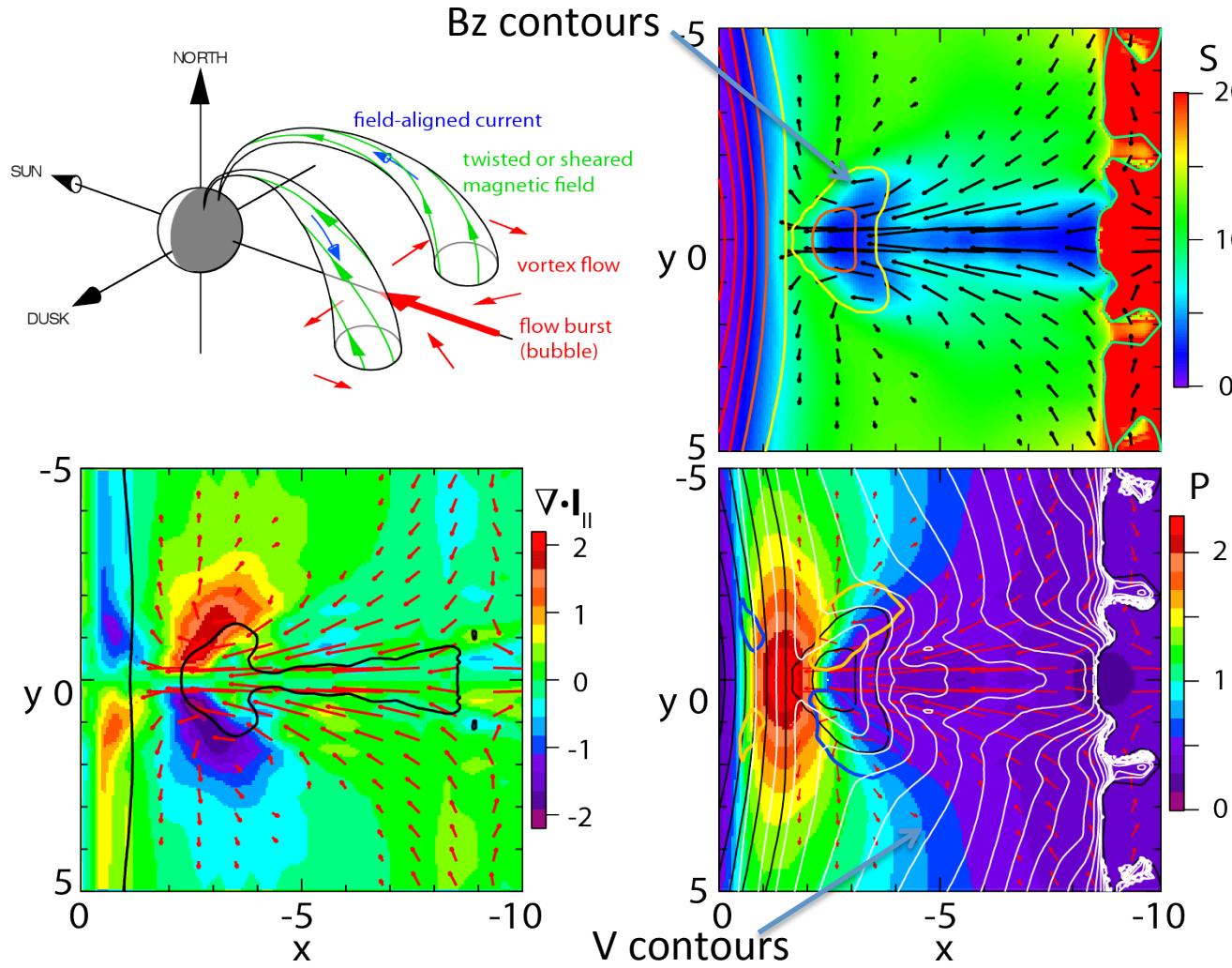


$E_Y(x, z)$



Bouncing, pulsating, dipolarization sequences

# Buildup of substorm current wedge in MHD



$$\mathbf{j} \times \mathbf{B} \approx \nabla p$$

$$\mathbf{j}_{\perp} = \frac{\mathbf{B} \times \nabla p}{B^2}$$

$$\nabla \cdot \mathbf{j}_{\parallel} = \mathbf{B} \cdot \nabla \frac{j_{\parallel}}{B} = -\nabla \cdot \mathbf{j}_{\perp}$$

$$j_{\parallel} \approx \frac{\mathbf{B}}{B} \cdot \nabla V \times \nabla p$$

$$V = \int ds / B$$

Vasyliunas' formula

# Summary, MHD Results

- Onset of reconnection in near tail leads to fast flow, plasmoid ejection, dipolarization sequence, bouncing, pulsating consistent with observations
- Flow bursts associated with low entropy bubbles, dipolarization
- Individual bursts cause SCW type field-aligned currents
- Multiple bursts can contribute to growth of SCW

# 5. Particle acceleration in dipolarization events

Birn+, 1994, 97, 89, 2004..; LiX+, 1998; Zaharia+, 2000, 2004; Sarris+, 2002; Ashour-Abdalla+, 2009, 2011; LiuWL+, 2009; Shibahara+, 2010; Gabrielse+, 2012, 2016, 2017; Pan+, 2012, 2014; Zhou+, 2010, 2012; Perri+, 2011; Ukhorskiy+, 2013, 2017; Greco+ 2014, 2015; Liang+, 2014; Artemyev+, 2015; LiuCM+, 2017; review by Fu+, 2020)

- MHD simulation of reconnection,  
dipolarization
- E,B interpolated in space and time
- Test particle orbit integration

# Test particle tracing in MHD fields

Using time-dependent MHD fields, interpolated in space and time  
(cubic spline in space; monotonicity conserving algorithm; avoid spurious  $E_{||}$ )  
Backward tracing from final destination to origin at boundary or initial state  
Impose  $f$  at origin =  $f$  at final location (Liouville mapping)  
Reflection at near-Earth boundary accounts for delay from mirroring closer to Earth, based on estimates from orbits in Tsyganenko field model.

Full equation of motion in strongly varying or weak fields (always for ions)

$$\frac{d\mathbf{m}\mathbf{u}}{dt} = q(\mathbf{E} + \mathbf{u} \times \mathbf{B})$$

Gyrocenter drift in weakly varying fields ( $\mu_{\text{rel}}$  conserved)

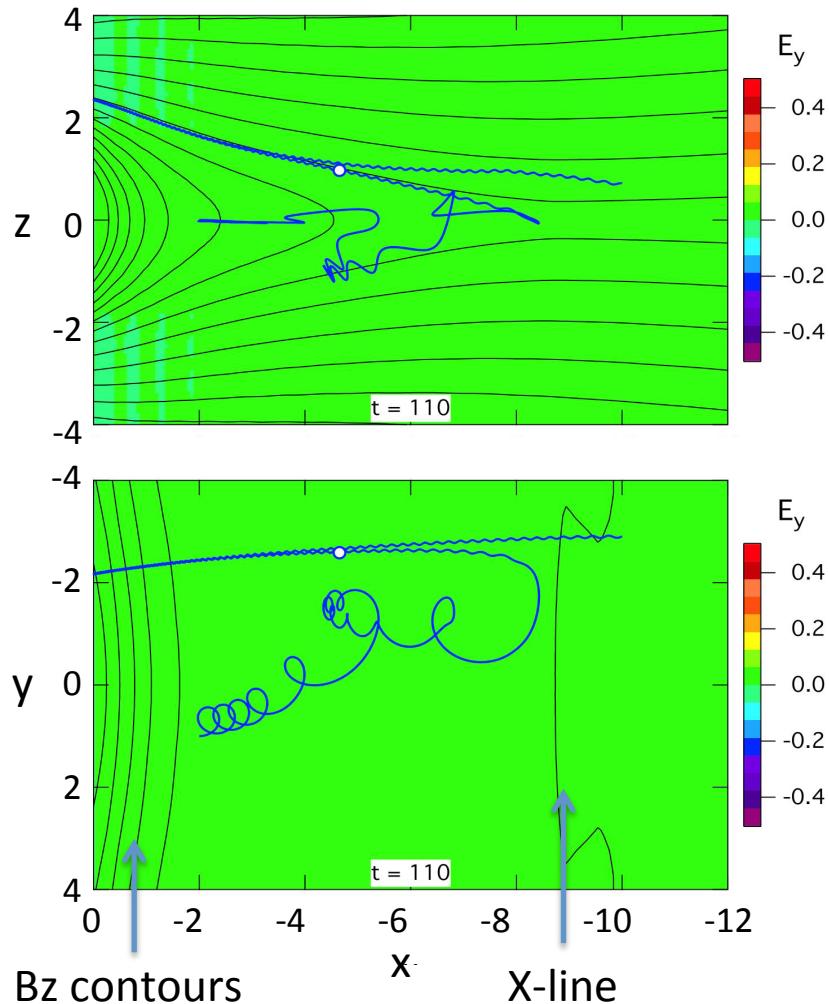
$$\mathbf{v}_{\perp} = \mathbf{v}_E + \mathbf{v}_{\nabla B} + \mathbf{v}_C = \frac{\mathbf{E} \times \mathbf{B}}{B^2} + \frac{\mu}{q} \frac{\mathbf{B} \times \nabla B}{B^2} + \frac{mv_{||}^2}{q} \frac{\mathbf{B}}{B^2} \times (\mathbf{b} \cdot \nabla \mathbf{b})$$

$$\frac{dmv_{||}}{dt} = qE_{||} - \mu \mathbf{b} \cdot \nabla B + mv_{||}(\mathbf{v}_E + \mathbf{v}_{\nabla B}) \cdot (\mathbf{b} \cdot \nabla \mathbf{b}) \quad \mathbf{b} = \frac{\mathbf{B}}{B}$$

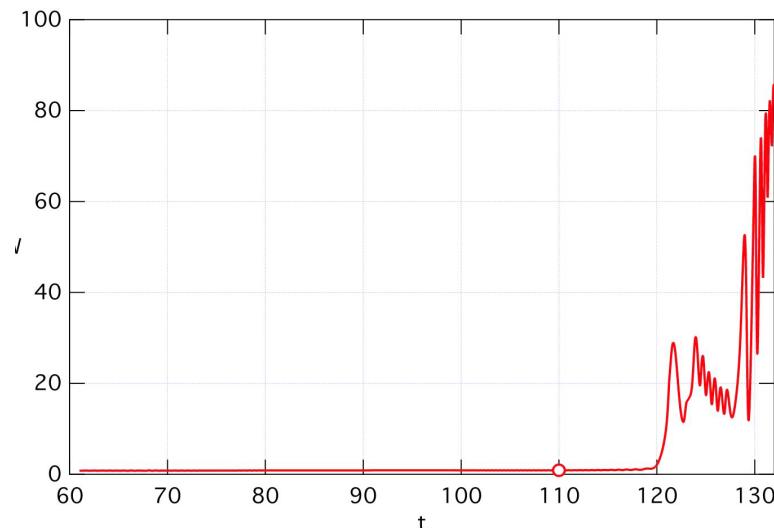
$$m = \gamma m_0 \quad \mu = \frac{\mu_{\text{rel}}}{\gamma} \quad \mu_{\text{rel}} = \frac{p_{\perp}^2}{2m_0 B} \quad \gamma = \frac{1}{\sqrt{1 - (v/c)^2}}$$

Transition based on adiabaticity parameter ( $\kappa^2 = r_{\text{curv}}/a_{\text{gyr}}$ )

# Ion acceleration, central plasma sheet

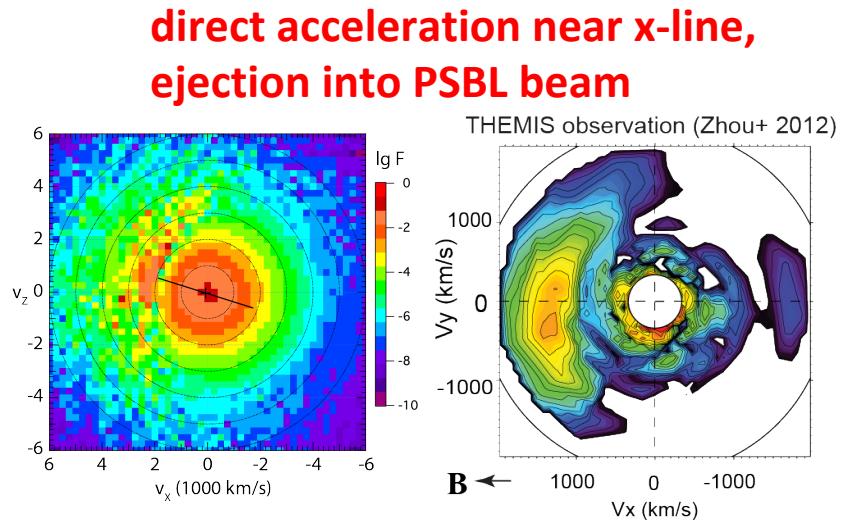
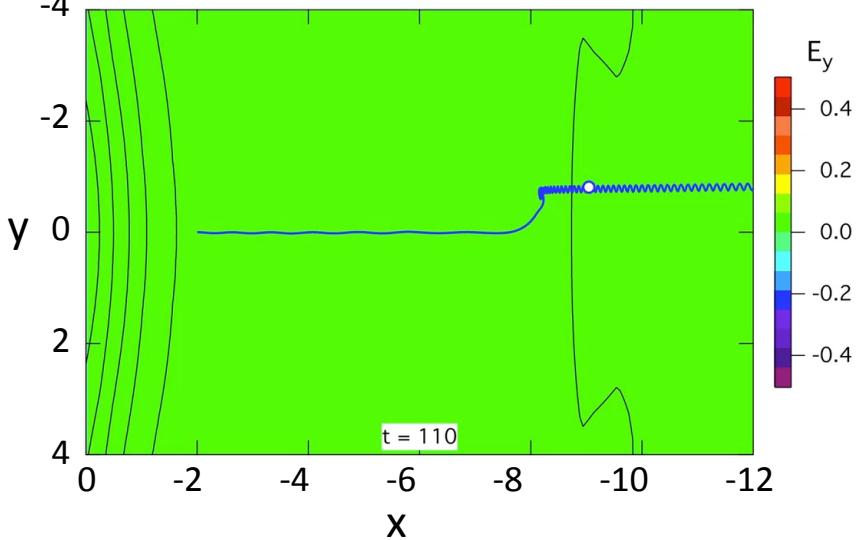
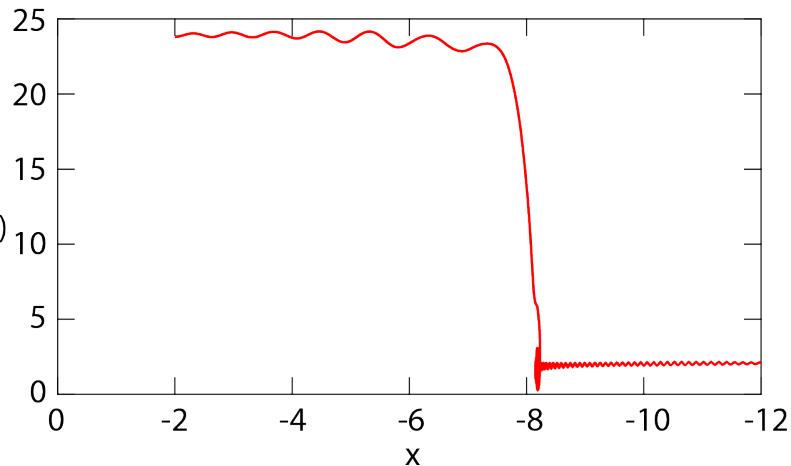
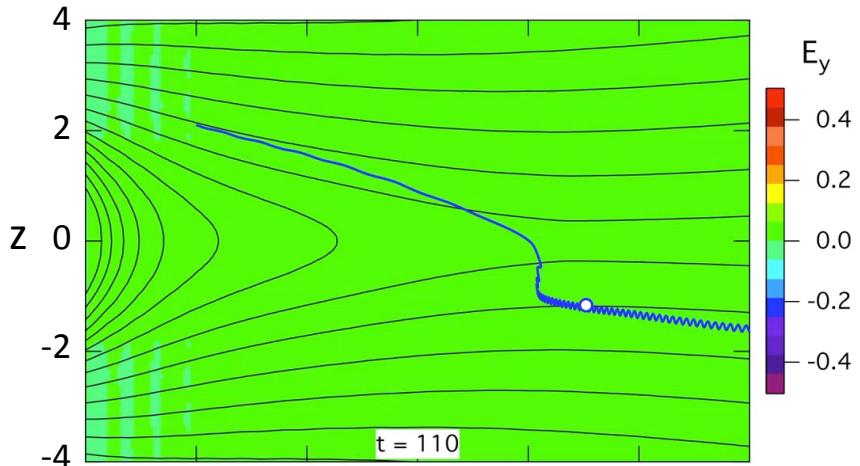


Proton, final energy  $\approx 86$  keV

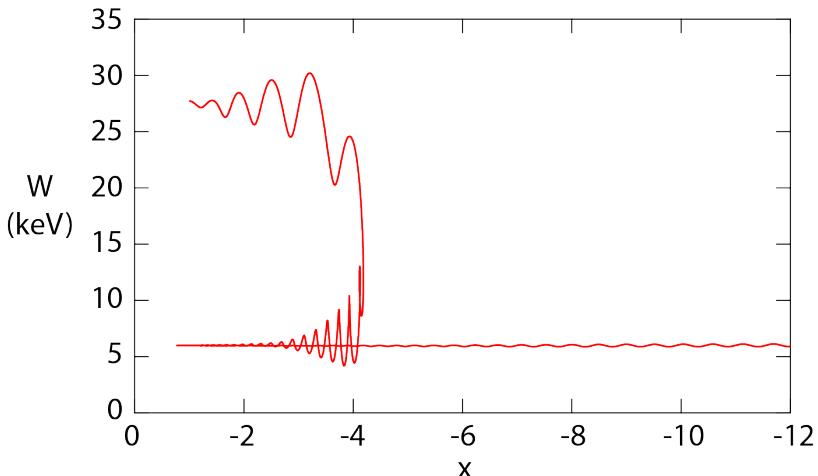
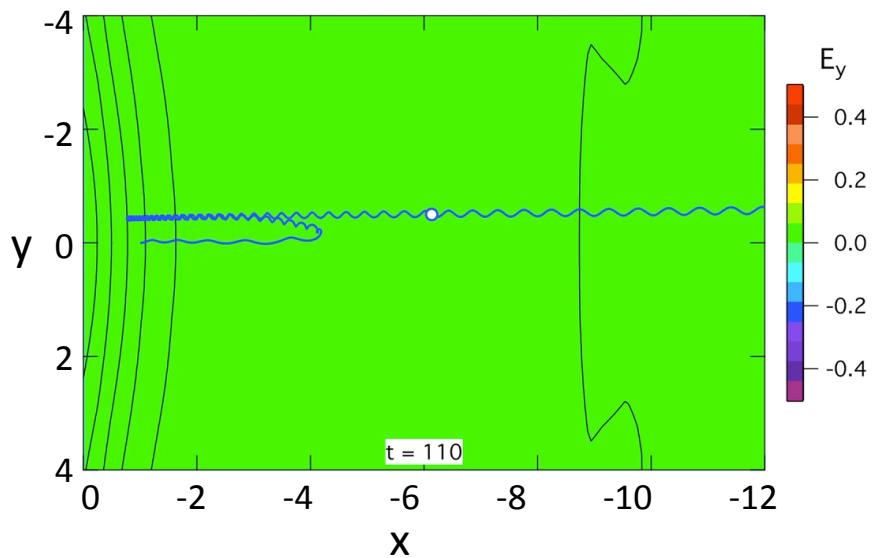
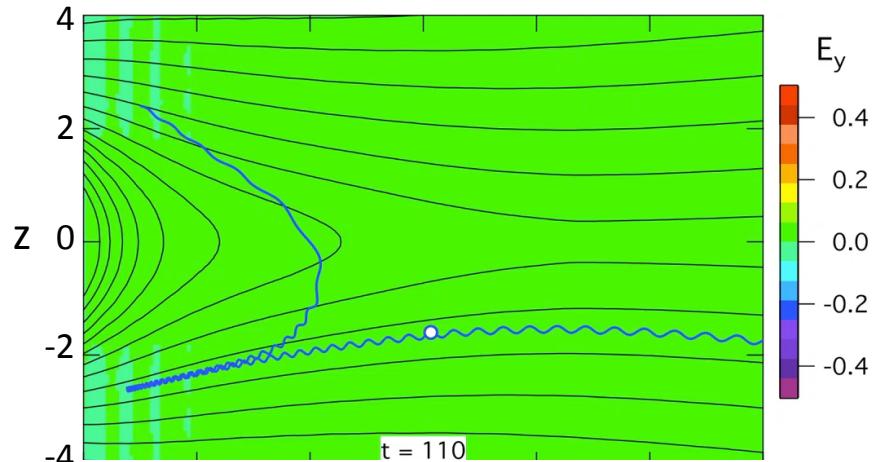


**Entry via reconnection,  
direct acceleration +  
betatron like acceleration**

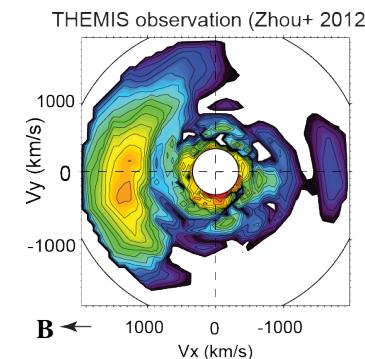
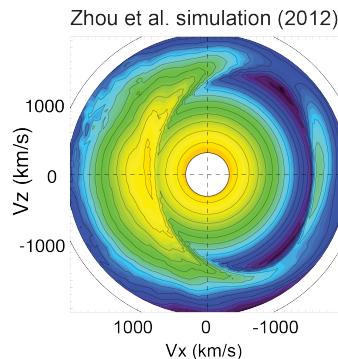
# Ion acceleration, plasma sheet boundary



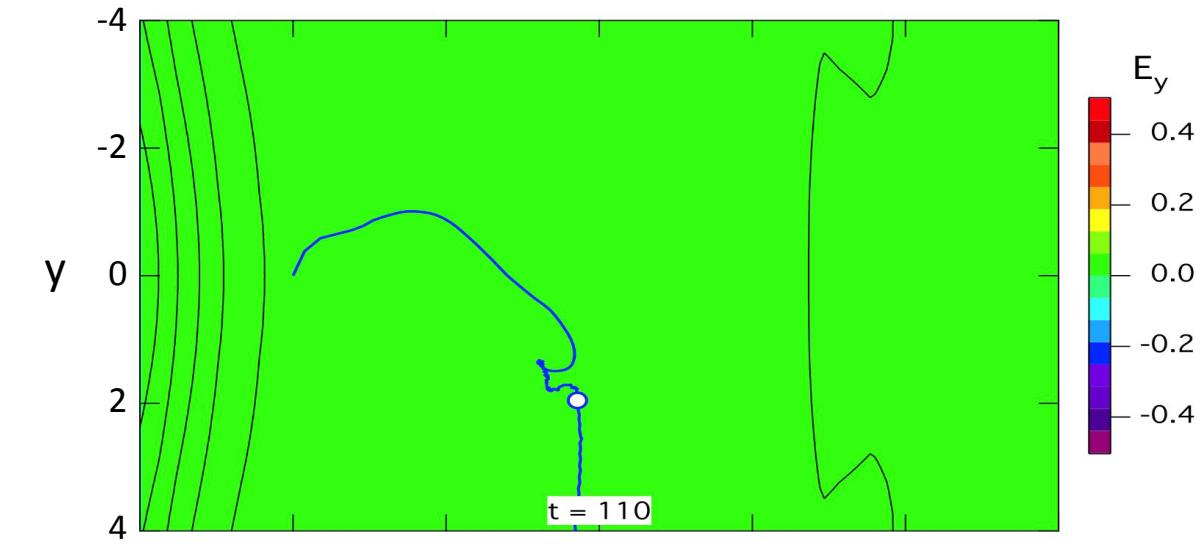
# Ion acceleration, PSBL beam



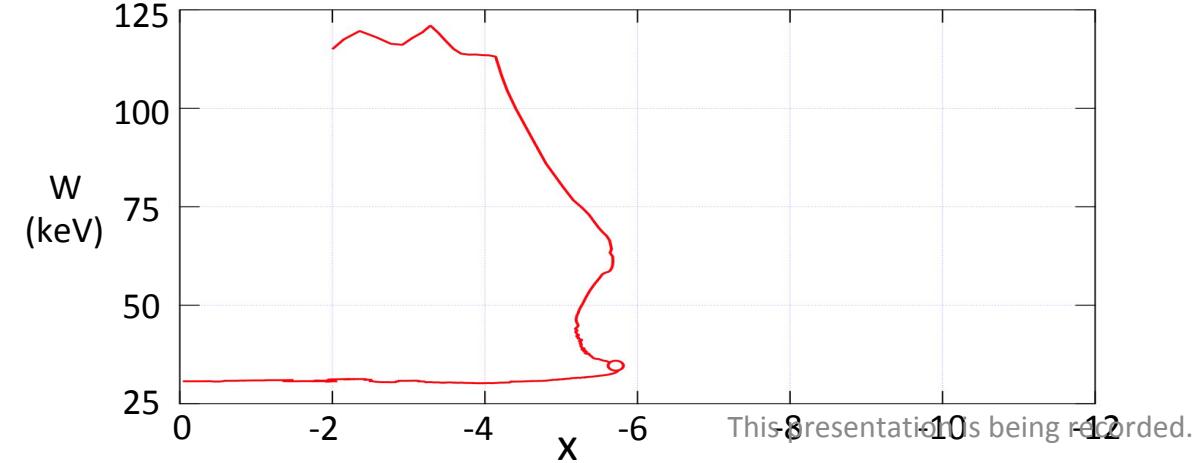
current sheet acceleration (Lyons&Speiser, 1982)  
convection surge mechanism  
(Quinn&Southwood, 1982; Mauk, 1986)



# Sample electron acceleration, 90° pitch angle

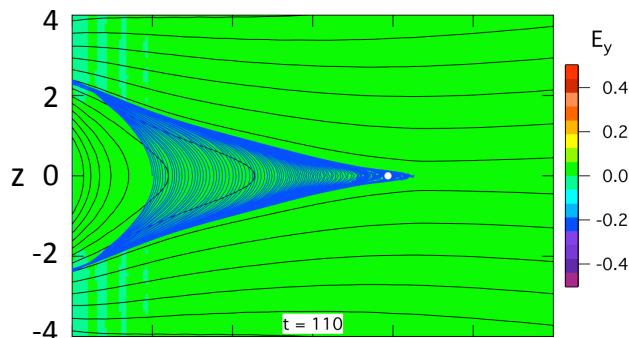


Entry via cross-tail VB drift,  
betatron acceleration

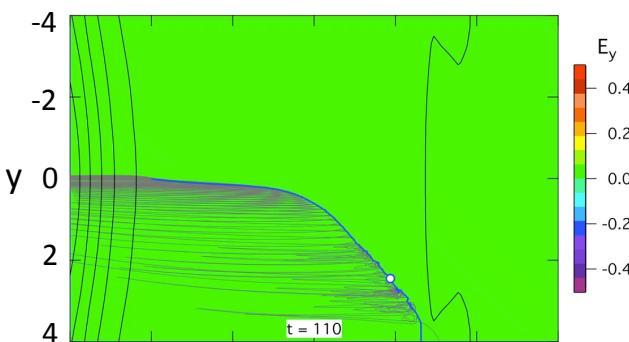


# Electron Fermi acceleration (small pitch angle)

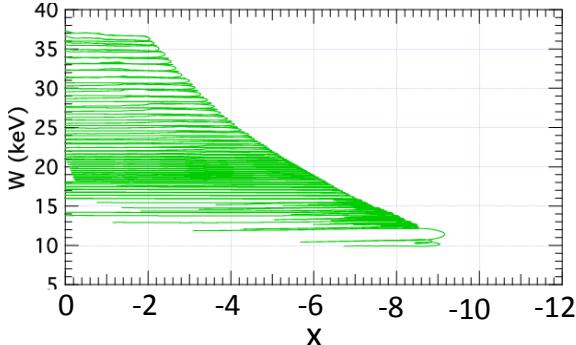
North



South



East



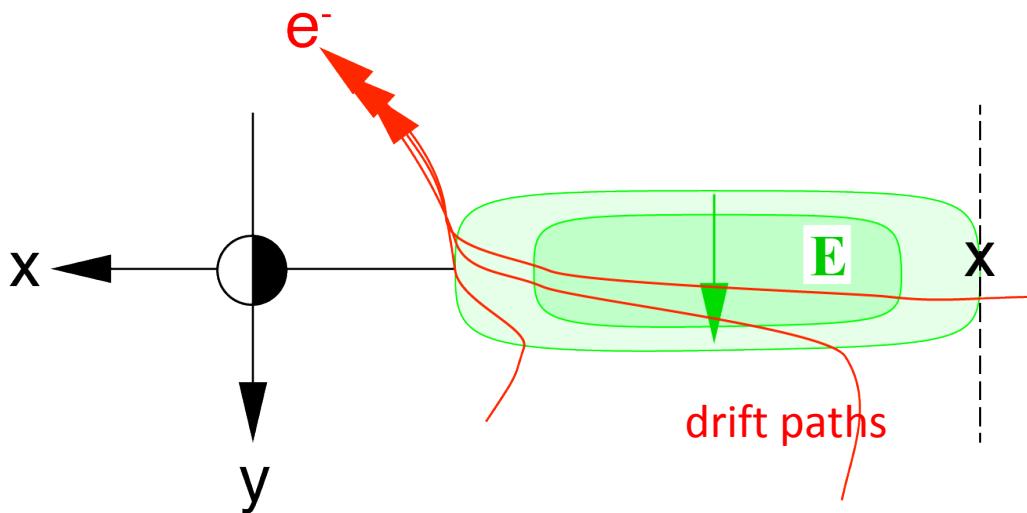
West

Entry by reconnection or cross-tail drift,  
earthward  $E \times B$  drift +  
cross-tail curvature drift

Repeated energy gain at equatorial  
crossings between mirroring  
( 1<sup>st</sup> order Fermi, type B; Northrop 1963;  
contracting field line, type A)

current sheet acceleration (Lyons&Speiser, 1982)  
convection surge mechanism  
(Quinn&Southwood, 1982; Mauk, 1986)

# Electron acceleration



High energy: cross-tail drift > ExB drift

inner plasma sheet source, drift entry

Low energy: ExB drift > cross-tail drift

entry through reconnection from outer plasma sheet

Betatron acceleration:  $\mathbf{E} \times \mathbf{B}$  drift toward  $\nabla B \equiv \nabla B$  drift toward  $-\mathbf{E}$

Fermi acceleration:  $\mathbf{E} \times \mathbf{B}$  drift toward curvature vector  $\equiv$  curvature drift toward  $-\mathbf{E}$

# Summary: Particle Acceleration

Acceleration mainly from field collapse, governed by  $E_y = -v_x \times B_z$

- Importance of localization in  $y$
- Betatron acceleration (similar if nonadiabatic)
- 1<sup>st</sup> order Fermi, type B (or A; current sheet acceleration)

Direct acceleration near x-line or DF generates ion beams near PSBL

Two source regions (comparable importance in magnetotail):

- |                           |                      |                        |
|---------------------------|----------------------|------------------------|
| - flanks, inner tail      | - drift entry        | - early, higher energy |
| - outer plasma sheet/PSBL | - reconnection entry | - later, lower energy  |

Explains drop at lower energies, increase at higher energies

Acceleration limited by  $\int E_y dy$  (few 100 keV)

# Summary: Answers & Open Questions

**Growth phase, thin current sheet formation:** Local, from lobe flux addition or CPS depletion

What is the relative importance of flux addition vs. depletion?

What determines where TCSs form?

**Onset:** Localized current sheet thinning enables onset of tearing, fast reconnection

What are the actual conditions? In 3D, and with guide field?

Does turbulence play a role?

Is there a preceding instability?

External or internal trigger?

**Expansion phase:** Shear flows generate FACs, localized  $E_y$  is an effective accelerator

What is the relative role of multiple flow bursts at same location or different locations?

What is the role of waves? Anisotropy?

What is the relevance of injections for the ring current?

**Recovery phase:**

What stops reconnection?

How does a neutral line retreat?

How does the plasma sheet refill?

**How do tail features connect to auroral features?**