

# Problem G

## The Number of 2's

Time limit: 1 second

How many factors of 2 can you extract from factorial of  $n$ ? For example, you know  $10! = 1 \times 2 \times \cdots \times 10 = 3628800$ . By successively extracting factor 2 from  $10!$ , you get the following sequence

3628800, 1814400, 907200, 453600, 226800, 113400, 56700, 28350, 14175 .

The sequence finally stops at 14175 because it is not a multiple of 2. Since there are 9 numbers in this sequence, you can get totally 8 factor 2's from  $10!$ . We use  $\epsilon_2(n!)$  to denote this number. In this example, it tells you that  $\epsilon_2(10!) = 8$ .

The first approach to find  $\epsilon_2(n)$  is to write a computer program that computes  $n!$  and then extracts 2 successively from it. However, this approach is not practical because  $n!$  is easy to be very large. Thus, a more elegant way is to derive a *formula* that can compute this. Fortunately, in many textbooks about number theory, you can find such an amazing formula

$$\epsilon_2(n!) = \left\lfloor \frac{n}{2} \right\rfloor + \left\lfloor \frac{n}{4} \right\rfloor + \left\lfloor \frac{n}{8} \right\rfloor + \cdots = \sum_{k \geq 1} \left\lfloor \frac{n}{2^k} \right\rfloor ,$$

where  $\lfloor x \rfloor$  returns the largest integer that does not exceed  $x$ . In our example,  $\epsilon_2(10!) = \lfloor 5 \rfloor + \lfloor 2.5 \rfloor + \lfloor 1.25 \rfloor = 5 + 2 + 1 = 8$  by using this formula.

The third way, possibly the most efficient one, is based on the function  $v_2(n)$  that computes the number of 1's in the binary representation of  $n$ . For example, 10 is  $1010_2$  in binary, and there are two 1's in its binary representation. Thus,  $v_2(10) = 2$ . A surprising fact is  $\epsilon_2(n!) = n - v_2(n)$ . Based on it, you can easily calculate  $\epsilon_2(10!) = 10 - v_2(10) = 10 - 2 = 8$ . The computation of  $v_2(n)$  can be done without using any division. Several acceleration techniques can be applied to speed up the computation of  $v_2(n)$ . Therefore, the third approach is possibly the most efficient way to computer  $\epsilon_2(n!)$ . On input  $n$ , your task is to output the value of  $\epsilon_2(n!)$ . Notice that either the second or third method can lead to a correct implementation that passes this task.

## Input File Format

The first line gives you the total number of test cases, which is a positive integer that does not exceed 1000. Each test case occupies a single line, which contains only one positive integer  $n$ , where  $1 \leq n < 2^{31}$ . Test cases are listed consecutively, so there is no empty line between two adjacent cases.

## Output Format

For each test case, output the value of  $\epsilon_2(n!)$  in one line.

## Sample Input

4  
1  
5  
10  
16

## Output for the Sample Input

0  
3  
8  
15