## **PadhAl: The Convolution Operation**

## One Fourth Labs

## The 1D convolution operation

What does the convolution operation do?

- 1. Let's approach this with a real world example
- 2. Consider a flight from Chennai to Delhi
  - a. We measure the distance of the flight from Chennai at regular intervals,
    - i.  $x_0$  at  $t_0$
  - ii.  $x_1$  at  $t_1$
  - iii.  $x_2$  at  $t_2$
  - b. In general, to calculate the overall speed, we would take the average speed at these measured points i.e  $\frac{1}{3}(x_0 + x_1 + x_2)$ .
  - c. However, let us try giving the most importance to the current reading, and a progressively decreasing level of importance to every reading preceding the current one.
  - d. Let's assign different weights to each of these reading points
    - i.  $x_0 \longrightarrow w_0$  (0 indicates current reference point)
    - ii.  $x_1 \longrightarrow w_{-1}$  (1 reading before reference point)
  - iii.  $x_2 \longrightarrow w_{-2}$  (1 readings before reference point)
  - e. So the new overall speed would be calculated by  $w_{-2}x_0 + w_{-1}x_1 + w_0x_2$  where the weights are decreasing from  $w_0$
- 3. The formula could be written as follows

a. 
$$s_t = \sum_{a=0}^{\infty} w_{-a} x_{t-a} = (x * w)_t$$

- b. Where t refers to reference point
- c. a is the index of the weight, ranging from 0 for reference point to  $\infty$
- 4. In practice, we wouldn't want to take the reading up till  $-\infty$ , thus we can simply say that those unwanted weights are all 0.
- 5. Consider the following table

	W <sub>-6</sub>	W <sub>-5</sub>	W <sub>-4</sub>	W <sub>-3</sub>	W <sub>-2</sub>	W <sub>-1</sub>	$W_0$					
W	0.01	0.01	0.02	0.02	0.04	0.04	0.05					
×	1.00	1.10	1.20	1.40	1.70	1.80	1.90	2.10	2.20	2.40	2.50	2.70
S							1.80					

- 6. In the above table,  $w_{27}$  to  $w_{27}$  are all consider to be 0
- 7. Here,  $s_6 = x_6 w_0 + x_5 w_{-1} + x_4 w_{-2} + x_3 w_{-3} + x_2 w_{-4} + x_1 w_{-5} + x_0 w_{-6}$