**CHAPTER** 

SIX

# **API REFERENCE**

This is the class and function reference of scikit-learn. Please refer to the *full user guide* for further details, as the class and function raw specifications may not be enough to give full guidelines on their uses. For reference on concepts repeated across the API, see *Glossary of Common Terms and API Elements*.

# 6.1 sklearn.base: Base classes and utility functions

Base classes for all estimators.

# 6.1.1 Base classes

base.BaseEstimator	Base class for all estimators in scikit-learn
base.BiclusterMixin	Mixin class for all bicluster estimators in scikit-learn
base.ClassifierMixin	Mixin class for all classifiers in scikit-learn.
base.ClusterMixin	Mixin class for all cluster estimators in scikit-learn.
base.DensityMixin	Mixin class for all density estimators in scikit-learn.
base.RegressorMixin	Mixin class for all regression estimators in scikit-learn.
base.TransformerMixin	Mixin class for all transformers in scikit-learn.

# sklearn.base.BaseEstimator

class sklearn.base.BaseEstimator

Base class for all estimators in scikit-learn

# **Notes**

All estimators should specify all the parameters that can be set at the class level in their \_\_init\_\_ as explicit keyword arguments (no \*args or \*\*kwargs).

# **Methods**

<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
___init___ (self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

# get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.base.BaseEstimator

- Inductive Clustering
- Column Transformer with Heterogeneous Data Sources

# sklearn.base.BiclusterMixin

# class sklearn.base.BiclusterMixin

Mixin class for all bicluster estimators in scikit-learn

# Attributes

biclusters\_ Convenient way to get row and column indicators together.

# **Methods**

get_indices(self, i)	Row and column indices of the i'th bicluster.
get_shape(self, i)	Shape of the i'th bicluster.
<pre>get_submatrix(self, i, data)</pre>	Returns the submatrix corresponding to bicluster i.

```
___init___(self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

# biclusters\_

Convenient way to get row and column indicators together.

Returns the rows\_and columns\_members.

# get\_indices (self, i)

Row and column indices of the i'th bicluster.

Only works if rows\_ and columns\_ attributes exist.

#### **Parameters**

i [int] The index of the cluster.

# Returns

row\_ind [np.array, dtype=np.intp] Indices of rows in the dataset that belong to the bicluster.

col\_ind [np.array, dtype=np.intp] Indices of columns in the dataset that belong to the bicluster

# get\_shape (self, i)

Shape of the i'th bicluster.

#### **Parameters**

i [int] The index of the cluster.

### **Returns**

**shape** [(int, int)] Number of rows and columns (resp.) in the bicluster.

# get\_submatrix(self, i, data)

Returns the submatrix corresponding to bicluster i.

#### **Parameters**

i [int] The index of the cluster.

data [array] The data.

#### Returns

submatrix [array] The submatrix corresponding to bicluster i.

# **Notes**

Works with sparse matrices. Only works if rows\_and columns\_attributes exist.

### sklearn.base.ClassifierMixin

### class sklearn.base.ClassifierMixin

Mixin class for all classifiers in scikit-learn.

# **Methods**

score(self, X, y[, sample\_weight])

Returns the mean accuracy on the given test data and labels.

```
__init__ (self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

X [array-like, shape = (n\_samples, n\_features)] Test samples.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

### sklearn.base.ClusterMixin

### class sklearn.base.ClusterMixin

Mixin class for all cluster estimators in scikit-learn.

### **Methods**

# fit\_predict(self, X[, y])

Performs clustering on X and returns cluster labels.

```
___init__(self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

# fit\_predict (self, X, y=None)

Performs clustering on X and returns cluster labels.

#### **Parameters**

**X** [ndarray, shape (n\_samples, n\_features)] Input data.

y [Ignored] not used, present for API consistency by convention.

### **Returns**

labels [ndarray, shape (n\_samples,)] cluster labels

# sklearn.base.DensityMixin

# class sklearn.base.DensityMixin

Mixin class for all density estimators in scikit-learn.

# **Methods**

# score(self, X[, y])

Returns the score of the model on the data X

```
__init__(self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

```
score(self, X, y=None)
```

Returns the score of the model on the data X

# **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)]

### Returns

score [float]

# sklearn.base.RegressorMixin

# class sklearn.base.RegressorMixin

Mixin class for all regression estimators in scikit-learn.

#### **Methods**

score(self, X, y[, sample_weight])	Returns the coefficient of determination R <sup>2</sup> of the pre-
	diction.

```
___init__(self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

### **Parameters**

- X [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

# **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

# sklearn.base.TransformerMixin

### class sklearn.base.TransformerMixin

Mixin class for all transformers in scikit-learn.

# **Methods**

```
___init___(self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# Examples using sklearn.base.TransformerMixin

• Column Transformer with Heterogeneous Data Sources

# 6.1.2 Functions

base.clone(estimator[, safe])	Constructs a new estimator with the same parameters.
base.is_classifier(estimator)	Returns True if the given estimator is (probably) a classi-
	fier.
base.is_regressor(estimator)	Returns True if the given estimator is (probably) a regres-
	sor.
<pre>config_context(\*\*new_config)</pre>	Context manager for global scikit-learn configuration
<pre>get_config()</pre>	Retrieve current values for configuration set by
	set_config
<pre>set_config([assume_finite, working_memory,])</pre>	Set global scikit-learn configuration
show_versions()	Print useful debugging information

### sklearn.base.clone

sklearn.base.clone (estimator, safe=True)

Constructs a new estimator with the same parameters.

Clone does a deep copy of the model in an estimator without actually copying attached data. It yields a new estimator with the same parameters that has not been fit on any data.

#### **Parameters**

**estimator** [estimator object, or list, tuple or set of objects] The estimator or group of estimators to be cloned

**safe** [boolean, optional] If safe is false, clone will fall back to a deep copy on objects that are not estimators.

# sklearn.base.is classifier

```
sklearn.base.is_classifier(estimator)
```

Returns True if the given estimator is (probably) a classifier.

### **Parameters**

estimator [object] Estimator object to test.

#### Returns

out [bool] True if estimator is a classifier and False otherwise.

# sklearn.base.is\_regressor

```
sklearn.base.is_regressor(estimator)
```

Returns True if the given estimator is (probably) a regressor.

### **Parameters**

estimator [object] Estimator object to test.

### Returns

out [bool] True if estimator is a regressor and False otherwise.

# sklearn.config\_context

```
sklearn.config_context(**new_config)
```

Context manager for global scikit-learn configuration

### **Parameters**

**assume\_finite** [bool, optional] If True, validation for finiteness will be skipped, saving time, but leading to potential crashes. If False, validation for finiteness will be performed, avoiding error. Global default: False.

working\_memory [int, optional] If set, scikit-learn will attempt to limit the size of temporary arrays to this number of MiB (per job when parallelised), often saving both computation time and memory on expensive operations that can be performed in chunks. Global default: 1024.

### See also:

```
set_config Set global scikit-learn configuration
```

get\_config Retrieve current values of the global configuration

# **Notes**

All settings, not just those presently modified, will be returned to their previous values when the context manager is exited. This is not thread-safe.

# **Examples**

```
>>> import sklearn
>>> from sklearn.utils.validation import assert_all_finite
>>> with sklearn.config_context(assume_finite=True):
... assert_all_finite([float('nan')])
>>> with sklearn.config_context(assume_finite=True):
... with sklearn.config_context(assume_finite=False):
... assert_all_finite([float('nan')])
...
Traceback (most recent call last):
...
ValueError: Input contains NaN, ...
```

# sklearn.get\_config

```
sklearn.get_config()
```

Retrieve current values for configuration set by set\_config

# Returns

**config** [dict] Keys are parameter names that can be passed to set\_config.

### See also:

config\_context Context manager for global scikit-learn configuration
set\_config Set global scikit-learn configuration

# sklearn.set config

sklearn.**set\_config** (assume\_finite=None, working\_memory=None, print\_changed\_only=None)
Set global scikit-learn configuration

New in version 0.19.

#### **Parameters**

**assume\_finite** [bool, optional] If True, validation for finiteness will be skipped, saving time, but leading to potential crashes. If False, validation for finiteness will be performed, avoiding error. Global default: False.

New in version 0.19.

working\_memory [int, optional] If set, scikit-learn will attempt to limit the size of temporary arrays to this number of MiB (per job when parallelised), often saving both computation time and memory on expensive operations that can be performed in chunks. Global default: 1024.

New in version 0.20.

print\_changed\_only [bool, optional] If True, only the parameters that were set to non-default
values will be printed when printing an estimator. For example, print (SVC()) while
True will only print 'SVC()' while the default behaviour would be to print 'SVC(C=1.0,
cache\_size=200,...)' with all the non-changed parameters.

New in version 0.21.

# See also:

config\_context Context manager for global scikit-learn configuration

get\_config Retrieve current values of the global configuration

# Examples using sklearn.set\_config

• Compact estimator representations

# sklearn.show versions

```
sklearn.show versions()
```

Print useful debugging information

# 6.2 sklearn.calibration: Probability Calibration

Calibration of predicted probabilities.

**User guide:** See the *Probability calibration* section for further details.

 $calibration. \textit{CalibratedClassifierCV}([\dots]) \qquad \textbf{Probability calibration with isotonic regression or sigmoid.}$ 

# 6.2.1 sklearn.calibration.CalibratedClassifierCV

Probability calibration with isotonic regression or sigmoid.

See glossary entry for cross-validation estimator.

With this class, the base\_estimator is fit on the train set of the cross-validation generator and the test set is used for calibration. The probabilities for each of the folds are then averaged for prediction. In case that cv="prefit" is passed to \_\_init\_\_, it is assumed that base\_estimator has been fitted already and all data is used for calibration. Note that data for fitting the classifier and for calibrating it must be disjoint.

Read more in the User Guide.

### **Parameters**

**base\_estimator** [instance BaseEstimator] The classifier whose output decision function needs to be calibrated to offer more accurate predict\_proba outputs. If cv=prefit, the classifier must have been fit already on data.

**method** ['sigmoid' or 'isotonic'] The method to use for calibration. Can be 'sigmoid' which corresponds to Platt's method or 'isotonic' which is a non-parametric approach. It is not advised to use isotonic calibration with too few calibration samples (<<1000) since it tends to overfit. Use sigmoids (Platt's calibration) in this case.

- **cv** [integer, cross-validation generator, iterable or "prefit", optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross-validation,
  - integer, to specify the number of folds.
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if y is binary or multiclass,  $sklearn.model\_selection$ . StratifiedKFold is used. If y is neither binary nor multiclass,  $sklearn.model\_selection$ . KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

If "prefit" is passed, it is assumed that base\_estimator has been fitted already and all data is used for calibration.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

### **Attributes**

**classes**\_ [array, shape (n\_classes)] The class labels.

**calibrated\_classifiers\_** [list (len() equal to cv or 1 if cv == "prefit")] The list of calibrated classifiers, one for each crossvalidation fold, which has been fitted on all but the validation fold and calibrated on the validation fold.

### References

[R57cf438d7060-1], [R57cf438d7060-2], [R57cf438d7060-3], [R57cf438d7060-4]

### **Methods**

fit(self, X, y[, sample_weight])	Fit the calibrated model
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict the target of new samples.
predict_proba(self, X)	Posterior probabilities of classification
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_\_init\_\_ (self, base\_estimator=None, method='sigmoid', cv='warn')

fit (self, X, y, sample\_weight=None)

Fit the calibrated model

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data.

y [array-like, shape (n\_samples,)] Target values.

**sample\_weight** [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted.

# Returns

self [object] Returns an instance of self.

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

# predict (self, X)

Predict the target of new samples. Can be different from the prediction of the uncalibrated classifier.

# **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The samples.

### Returns

C [array, shape (n\_samples,)] The predicted class.

### predict\_proba (self, X)

Posterior probabilities of classification

This function returns posterior probabilities of classification according to each class on an array of test vectors X.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The samples.

#### Returns

C [array, shape (n\_samples, n\_classes)] The predicted probas.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

# **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape =  $(n_samples)$  or  $(n_samples, n_outputs)$ ] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# Examples using sklearn.calibration.CalibratedClassifierCV

- Probability Calibration curves
- Probability calibration of classifiers
- Probability Calibration for 3-class classification

calibration.calibration_curve(y_true,	Compute true and predicted probabilities for a calibration
y_prob)	curve.

# 6.2.2 sklearn.calibration.calibration\_curve

sklearn.calibration.calibration\_curve(y\_true, y\_prob, normalize=False, n\_bins=5, strategy='uniform')

Compute true and predicted probabilities for a calibration curve.

The method assumes the inputs come from a binary classifier.

Calibration curves may also be referred to as reliability diagrams.

Read more in the *User Guide*.

#### **Parameters**

y\_true [array, shape (n\_samples,)] True targets.

**y\_prob** [array, shape (n\_samples,)] Probabilities of the positive class.

**normalize** [bool, optional, default=False] Whether y\_prob needs to be normalized into the bin [0, 1], i.e. is not a proper probability. If True, the smallest value in y\_prob is mapped onto 0 and the largest one onto 1.

**n\_bins** [int] Number of bins. A bigger number requires more data. Bins with no data points (i.e. without corresponding values in y\_prob) will not be returned, thus there may be fewer than n\_bins in the return value.

**strategy** [{'uniform', 'quantile'}, (default='uniform')] Strategy used to define the widths of the bins.

uniform All bins have identical widths.

quantile All bins have the same number of points.

### Returns

**prob\_true** [array, shape (n\_bins,) or smaller] The true probability in each bin (fraction of positives).

**prob\_pred** [array, shape (n\_bins,) or smaller] The mean predicted probability in each bin.

# References

Alexandru Niculescu-Mizil and Rich Caruana (2005) Predicting Good Probabilities With Supervised Learning, in Proceedings of the 22nd International Conference on Machine Learning (ICML). See section 4 (Qualitative Analysis of Predictions).

# Examples using sklearn.calibration.calibration\_curve

- Comparison of Calibration of Classifiers
- Probability Calibration curves

# 6.3 sklearn.cluster: Clustering

The sklearn.cluster module gathers popular unsupervised clustering algorithms.

**User guide:** See the *Clustering* section for further details.

# 6.3.1 Classes

cluster.AffinityPropagation([damping,])	Perform Affinity Propagation Clustering of data.
cluster.AgglomerativeClustering([])	Agglomerative Clustering
<pre>cluster.Birch([threshold, branching_factor,])</pre>	Implements the Birch clustering algorithm.
cluster.DBSCAN([eps, min_samples, metric,])	Perform DBSCAN clustering from vector array or distance
	matrix.
<pre>cluster.OPTICS([min_samples, max_eps,])</pre>	Estimate clustering structure from vector array
cluster.FeatureAgglomeration([n_clusters,	Agglomerate features.
])	
<pre>cluster.KMeans([n_clusters, init, n_init,])</pre>	K-Means clustering
<pre>cluster.MiniBatchKMeans([n_clusters, init,])</pre>	Mini-Batch K-Means clustering
<pre>cluster.MeanShift([bandwidth, seeds,])</pre>	Mean shift clustering using a flat kernel.
cluster.SpectralClustering([n_clusters,])	Apply clustering to a projection of the normalized Lapla-
	cian.

# sklearn.cluster.AffinityPropagation

Perform Affinity Propagation Clustering of data.

Read more in the *User Guide*.

### **Parameters**

**damping** [float, optional, default: 0.5] Damping factor (between 0.5 and 1) is the extent to which the current value is maintained relative to incoming values (weighted 1 - damping). This in order to avoid numerical oscillations when updating these values (messages).

max iter [int, optional, default: 200] Maximum number of iterations.

**convergence\_iter** [int, optional, default: 15] Number of iterations with no change in the number of estimated clusters that stops the convergence.

copy [boolean, optional, default: True] Make a copy of input data.

**preference** [array-like, shape (n\_samples,) or float, optional] Preferences for each point - points with larger values of preferences are more likely to be chosen as exemplars. The number of exemplars, ie of clusters, is influenced by the input preferences value. If the preferences are not passed as arguments, they will be set to the median of the input similarities.

**affinity** [string, optional, default="euclidean"] Which affinity to use. At the moment precomputed and euclidean are supported. euclidean uses the negative squared euclidean distance between points.

verbose [boolean, optional, default: False] Whether to be verbose.

### Attributes

```
cluster_centers_indices_ [array, shape (n_clusters,)] Indices of cluster centers
cluster_centers_ [array, shape (n_clusters, n_features)] Cluster centers (if affinity !=
    precomputed).
labels_ [array, shape (n_samples,)] Labels of each point
affinity_matrix_ [array, shape (n_samples, n_samples)] Stores the affinity matrix used in fit.
n_iter_ [int] Number of iterations taken to converge.
```

# **Notes**

For an example, see examples/cluster/plot\_affinity\_propagation.py.

The algorithmic complexity of affinity propagation is quadratic in the number of points.

When fit does not converge, cluster\_centers\_becomes an empty array and all training samples will be labelled as -1. In addition, predict will then label every sample as -1.

When all training samples have equal similarities and equal preferences, the assignment of cluster centers and labels depends on the preference. If the preference is smaller than the similarities, fit will result in a single cluster center and label 0 for every sample. Otherwise, every training sample becomes its own cluster center and is assigned a unique label.

### References

Brendan J. Frey and Delbert Dueck, "Clustering by Passing Messages Between Data Points", Science Feb. 2007

### **Examples**

# **Methods**

fit(self, X[, y])	Create affinity matrix from negative euclidean dis-
	tances, then apply affinity propagation clustering.
<pre>fit_predict(self, X[, y])</pre>	Performs clustering on X and returns cluster labels.
	Continued on next page

Table 6.14 – continued from previous page

<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict the closest cluster each sample in X belongs to.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, damping=0.5, max\_iter=200, convergence\_iter=15, copy=True, preference=None, affinity='euclidean', verbose=False)

# fit (self, X, y=None)

Create affinity matrix from negative euclidean distances, then apply affinity propagation clustering.

### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features) or (n\_samples, n\_samples)] Data matrix or, if affinity is precomputed, matrix of similarities / affinities.
- y [Ignored]

# fit\_predict (self, X, y=None)

Performs clustering on X and returns cluster labels.

#### **Parameters**

- **X** [ndarray, shape (n\_samples, n\_features)] Input data.
- y [Ignored] not used, present for API consistency by convention.

#### Returns

**labels** [ndarray, shape (n\_samples,)] cluster labels

# get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

#### predict (self, X)

Predict the closest cluster each sample in X belongs to.

# **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] New data to predict.

### Returns

labels [array, shape (n\_samples,)] Index of the cluster each sample belongs to.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### Examples using sklearn.cluster.AffinityPropagation

- Demo of affinity propagation clustering algorithm
- Comparing different clustering algorithms on toy datasets

# sklearn.cluster.AgglomerativeClustering

**Agglomerative Clustering** 

Recursively merges the pair of clusters that minimally increases a given linkage distance.

Read more in the *User Guide*.

### **Parameters**

- **n\_clusters** [int or None, optional (default=2)] The number of clusters to find. It must be None if distance\_threshold is not None.
- **affinity** [string or callable, default: "euclidean"] Metric used to compute the linkage. Can be "euclidean", "11", "12", "manhattan", "cosine", or "precomputed". If linkage is "ward", only "euclidean" is accepted. If "precomputed", a distance matrix (instead of a similarity matrix) is needed as input for the fit method.
- **memory** [None, str or object with the joblib.Memory interface, optional] Used to cache the output of the computation of the tree. By default, no caching is done. If a string is given, it is the path to the caching directory.
- connectivity [array-like or callable, optional] Connectivity matrix. Defines for each sample the neighboring samples following a given structure of the data. This can be a connectivity matrix itself or a callable that transforms the data into a connectivity matrix, such as derived from kneighbors\_graph. Default is None, i.e, the hierarchical clustering algorithm is unstructured.
- compute\_full\_tree [bool or 'auto' (optional)] Stop early the construction of the tree at n\_clusters. This is useful to decrease computation time if the number of clusters is not small compared to the number of samples. This option is useful only when specifying a connectivity matrix. Note also that when varying the number of clusters and using caching, it may be advantageous to compute the full tree. It must be True if distance\_threshold is not None.
- **linkage** [{"ward", "complete", "average", "single"}, optional (default="ward")] Which linkage criterion to use. The linkage criterion determines which distance to use between sets of observation. The algorithm will merge the pairs of cluster that minimize this criterion.
  - ward minimizes the variance of the clusters being merged.
  - average uses the average of the distances of each observation of the two sets.
  - complete or maximum linkage uses the maximum distances between all observations of the two sets.
  - single uses the minimum of the distances between all observations of the two sets.

pooling\_func [callable, default='deprecated'] Ignored.

Deprecated since version 0.20: pooling\_func has been deprecated in 0.20 and will be removed in 0.22.

**distance\_threshold** [float, optional (default=None)] The linkage distance threshold above which, clusters will not be merged. If not None, n\_clusters must be None and compute\_full\_tree must be True.

New in version 0.21.

### **Attributes**

**n\_clusters** [int] The number of clusters found by the algorithm. If distance\_threshold=None, it will be equal to the given n\_clusters.

labels\_ [array [n\_samples]] cluster labels for each point

n\_leaves\_ [int] Number of leaves in the hierarchical tree.

**n\_connected\_components**\_ [int] The estimated number of connected components in the graph.

# **Examples**

# **Methods**

fit(self, X[, y])	Fit the hierarchical clustering on the data
<pre>fit_predict(self, X[, y])</pre>	Performs clustering on X and returns cluster labels.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__(self, n_clusters=2, affinity='euclidean', memory=None, connectivity=None, compute_full_tree='auto', linkage='ward', pooling_func='deprecated', distance_threshold=None)
```

fit (self, X, y=None)

Fit the hierarchical clustering on the data

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Training data. Shape [n\_samples, n\_features], or [n\_samples, n\_samples] if affinity=='precomputed'.

y [Ignored]

# Returns

self

# fit\_predict (self, X, y=None)

Performs clustering on X and returns cluster labels.

# **Parameters**

- **X** [ndarray, shape (n\_samples, n\_features)] Input data.
- y [Ignored] not used, present for API consistency by convention.

### **Returns**

labels [ndarray, shape (n\_samples,)] cluster labels

### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# Examples using sklearn.cluster.AgglomerativeClustering

- Agglomerative clustering with and without structure
- Various Agglomerative Clustering on a 2D embedding of digits
- A demo of structured Ward hierarchical clustering on an image of coins
- Hierarchical clustering: structured vs unstructured ward
- Agglomerative clustering with different metrics
- Inductive Clustering
- Comparing different hierarchical linkage methods on toy datasets
- Comparing different clustering algorithms on toy datasets

#### sklearn.cluster.Birch

class sklearn.cluster.Birch (threshold=0.5, branching\_factor=50, n\_clusters=3, compute\_labels=True, copy=True)

Implements the Birch clustering algorithm.

It is a memory-efficient, online-learning algorithm provided as an alternative to <code>MiniBatchKMeans</code>. It constructs a tree data structure with the cluster centroids being read off the leaf. These can be either the final cluster centroids or can be provided as input to another clustering algorithm such as <code>AgglomerativeClustering</code>.

Read more in the *User Guide*.

#### **Parameters**

**threshold** [float, default 0.5] The radius of the subcluster obtained by merging a new sample and the closest subcluster should be lesser than the threshold. Otherwise a new subcluster is started. Setting this value to be very low promotes splitting and vice-versa.

**branching\_factor** [int, default 50] Maximum number of CF subclusters in each node. If a new samples enters such that the number of subclusters exceed the branching\_factor then that node is split into two nodes with the subclusters redistributed in each. The parent subcluster of that node is removed and two new subclusters are added as parents of the 2 split nodes.

**n\_clusters** [int, instance of sklearn.cluster model, default 3] Number of clusters after the final clustering step, which treats the subclusters from the leaves as new samples.

- None: the final clustering step is not performed and the subclusters are returned as they
  are.
- sklearn.cluster Estimator: If a model is provided, the model is fit treating the subclusters as new samples and the initial data is mapped to the label of the closest subcluster.
- int : the model fit is AgglomerativeClustering with n\_clusters set to be equal to the int.

**compute\_labels** [bool, default True] Whether or not to compute labels for each fit.

**copy** [bool, default True] Whether or not to make a copy of the given data. If set to False, the initial data will be overwritten.

#### **Attributes**

**root** [ CFNode] Root of the CFTree.

dummy\_leaf\_ [\_CFNode] Start pointer to all the leaves.

subcluster\_centers\_ [ndarray,] Centroids of all subclusters read directly from the leaves.

**subcluster\_labels**\_ [ndarray,] Labels assigned to the centroids of the subclusters after they are clustered globally.

**labels**\_ [ndarray, shape (n\_samples,)] Array of labels assigned to the input data. if partial\_fit is used instead of fit, they are assigned to the last batch of data.

# **Notes**

The tree data structure consists of nodes with each node consisting of a number of subclusters. The maximum number of subclusters in a node is determined by the branching factor. Each subcluster maintains a linear sum, squared sum and the number of samples in that subcluster. In addition, each subcluster can also have a node as its child, if the subcluster is not a member of a leaf node.

For a new point entering the root, it is merged with the subcluster closest to it and the linear sum, squared sum and the number of samples of that subcluster are updated. This is done recursively till the properties of the leaf node are updated.

### References

- Tian Zhang, Raghu Ramakrishnan, Maron Livny BIRCH: An efficient data clustering method for large databases. https://www.cs.sfu.ca/CourseCentral/459/han/papers/zhang96.pdf
- Roberto Perdisci JBirch Java implementation of BIRCH clustering algorithm https://code.google.com/ archive/p/jbirch

# **Examples**

### **Methods**

fit(self, X[, y])	Build a CF Tree for the input data.
<pre>fit_predict(self, X[, y])</pre>	Performs clustering on X and returns cluster labels.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self[, X, y])</pre>	Online learning.
predict(self, X)	Predict data using the centroids_of subclusters.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform X into subcluster centroids dimension.

```
__init__(self, threshold=0.5, branching_factor=50, n_clusters=3, compute_labels=True, copy=True)
```

fit (self, X, y=None)

Build a CF Tree for the input data.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Input data.

y [Ignored]

fit\_predict (self, X, y=None)

Performs clustering on X and returns cluster labels.

#### **Parameters**

**X** [ndarray, shape (n\_samples, n\_features)] Input data.

y [Ignored] not used, present for API consistency by convention.

### **Returns**

labels [ndarray, shape (n\_samples,)] cluster labels

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- **y** [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

# partial\_fit (self, X=None, y=None)

Online learning. Prevents rebuilding of CFTree from scratch.

# **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features), None] Input data. If X is not provided, only the global clustering step is done.
- y [Ignored]

# predict (self, X)

Predict data using the centroids\_ of subclusters.

Avoid computation of the row norms of X.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Input data.

### **Returns**

labels [ndarray, shape(n\_samples)] Labelled data.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

#### transform(self, X)

Transform X into subcluster centroids dimension.

Each dimension represents the distance from the sample point to each cluster centroid.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Input data.

#### Returns

**X\_trans** [{array-like, sparse matrix}, shape (n\_samples, n\_clusters)] Transformed data.

# Examples using sklearn.cluster.Birch

- Compare BIRCH and MiniBatchKMeans
- Comparing different clustering algorithms on toy datasets

### sklearn.cluster.DBSCAN

class sklearn.cluster.DBSCAN(eps=0.5, min\_samples=5, metric='euclidean', metric\_params=None, algorithm='auto', leaf\_size=30, p=None, n\_jobs=None)

Perform DBSCAN clustering from vector array or distance matrix.

DBSCAN - Density-Based Spatial Clustering of Applications with Noise. Finds core samples of high density and expands clusters from them. Good for data which contains clusters of similar density.

Read more in the *User Guide*.

# **Parameters**

- **eps** [float, optional] The maximum distance between two samples for one to be considered as in the neighborhood of the other. This is not a maximum bound on the distances of points within a cluster. This is the most important DBSCAN parameter to choose appropriately for your data set and distance function.
- **min\_samples** [int, optional] The number of samples (or total weight) in a neighborhood for a point to be considered as a core point. This includes the point itself.
- **metric** [string, or callable] The metric to use when calculating distance between instances in a feature array. If metric is a string or callable, it must be one of the options allowed by <code>sklearn.metrics.pairwise\_distances</code> for its metric parameter. If metric is "precomputed", X is assumed to be a distance matrix and must be square. X may be a sparse matrix, in which case only "nonzero" elements may be considered neighbors for DBSCAN.

New in version 0.17: metric *precomputed* to accept precomputed sparse matrix.

metric\_params [dict, optional] Additional keyword arguments for the metric function.

New in version 0.19.

- **algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] The algorithm to be used by the NearestNeighbors module to compute pointwise distances and find nearest neighbors. See NearestNeighbors module documentation for details.
- **leaf\_size** [int, optional (default = 30)] Leaf size passed to BallTree or cKDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

- **p** [float, optional] The power of the Minkowski metric to be used to calculate distance between points.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### **Attributes**

**core\_sample\_indices**\_ [array, shape = [n\_core\_samples]] Indices of core samples.

**components**\_ [array, shape = [n\_core\_samples, n\_features]] Copy of each core sample found by training.

**labels**\_ [array, shape = [n\_samples]] Cluster labels for each point in the dataset given to fit(). Noisy samples are given the label -1.

#### See also:

**OPTICS** A similar clustering at multiple values of eps. Our implementation is optimized for memory usage.

#### **Notes**

For an example, see examples/cluster/plot\_dbscan.py.

This implementation bulk-computes all neighborhood queries, which increases the memory complexity to O(n.d) where d is the average number of neighbors, while original DBSCAN had memory complexity O(n). It may attract a higher memory complexity when querying these nearest neighborhoods, depending on the algorithm.

One way to avoid the query complexity is to pre-compute sparse neighborhoods in chunks using <code>NearestNeighbors.radius\_neighbors\_graph</code> with <code>mode='distance'</code>, then using <code>metric='precomputed'</code> here.

Another way to reduce memory and computation time is to remove (near-)duplicate points and use sample\_weight instead.

cluster.OPTICS provides a similar clustering with lower memory usage.

### References

Ester, M., H. P. Kriegel, J. Sander, and X. Xu, "A Density-Based Algorithm for Discovering Clusters in Large Spatial Databases with Noise". In: Proceedings of the 2nd International Conference on Knowledge Discovery and Data Mining, Portland, OR, AAAI Press, pp. 226-231. 1996

Schubert, E., Sander, J., Ester, M., Kriegel, H. P., & Xu, X. (2017). DBSCAN revisited, revisited: why and how you should (still) use DBSCAN. ACM Transactions on Database Systems (TODS), 42(3), 19.

# **Examples**

```
array([ 0,  0,  0,  1,  1, -1])
>>> clustering
DBSCAN(algorithm='auto', eps=3, leaf_size=30, metric='euclidean',
    metric_params=None, min_samples=2, n_jobs=None, p=None)
```

### **Methods**

<pre>fit(self, X[, y, sample_weight])</pre>	Perform DBSCAN clustering from features or distance
	matrix.
<pre>fit_predict(self, X[, y, sample_weight])</pre>	Performs clustering on X and returns cluster labels.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__(self, eps=0.5, min_samples=5, metric='euclidean', metric_params=None, algorithm='auto', leaf_size=30, p=None, n_jobs=None)
```

fit (self, X, y=None, sample\_weight=None)

Perform DBSCAN clustering from features or distance matrix.

#### **Parameters**

X [array or sparse (CSR) matrix of shape (n\_samples, n\_features), or array of shape (n\_samples, n\_samples)] A feature array, or array of distances between samples if metric='precomputed'.

**sample\_weight** [array, shape (n\_samples,), optional] Weight of each sample, such that a sample with a weight of at least min\_samples is by itself a core sample; a sample with negative weight may inhibit its eps-neighbor from being core. Note that weights are absolute, and default to 1.

y [Ignored]

fit\_predict (self, X, y=None, sample\_weight=None)

Performs clustering on X and returns cluster labels.

# **Parameters**

X [array or sparse (CSR) matrix of shape (n\_samples, n\_features), or array of shape (n\_samples, n\_samples)] A feature array, or array of distances between samples if metric='precomputed'.

**sample\_weight** [array, shape (n\_samples,), optional] Weight of each sample, such that a sample with a weight of at least min\_samples is by itself a core sample; a sample with negative weight may inhibit its eps-neighbor from being core. Note that weights are absolute, and default to 1.

y [Ignored]

# Returns

y [ndarray, shape (n\_samples,)] cluster labels

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# Examples using sklearn.cluster.DBSCAN

- Demo of DBSCAN clustering algorithm
- Comparing different clustering algorithms on toy datasets

### sklearn.cluster.OPTICS

Estimate clustering structure from vector array

OPTICS (Ordering Points To Identify the Clustering Structure), closely related to DBSCAN, finds core sample of high density and expands clusters from them [R2c55e37003fe-1]. Unlike DBSCAN, keeps cluster hierarchy for a variable neighborhood radius. Better suited for usage on large datasets than the current sklearn implementation of DBSCAN.

Clusters are then extracted using a DBSCAN-like method (cluster\_method = 'dbscan') or an automatic technique proposed in [R2c55e37003fe-1] (cluster\_method = 'xi').

This implementation deviates from the original OPTICS by first performing k-nearest-neighborhood searches on all points to identify core sizes, then computing only the distances to unprocessed points when constructing the cluster order. Note that we do not employ a heap to manage the expansion candidates, so the time complexity will be  $O(n^2)$ .

Read more in the User Guide.

### **Parameters**

min\_samples [int > 1 or float between 0 and 1 (default=5)] The number of samples in a neighborhood for a point to be considered as a core point. Also, up and down steep regions can't have more then min\_samples consecutive non-steep points. Expressed as an absolute number or a fraction of the number of samples (rounded to be at least 2).

max\_eps [float, optional (default=np.inf)] The maximum distance between two samples for one to be considered as in the neighborhood of the other. Default value of np.inf will identify clusters across all scales; reducing max\_eps will result in shorter run times.

**metric** [string or callable, optional (default='minkowski')] Metric to use for distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.

If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating

the distance between them. This works for Scipy's metrics, but is less efficient than passing the metric name as a string. If metric is "precomputed", X is assumed to be a distance matrix and must be square.

Valid values for metric are:

- from scikit-learn: ['cityblock', 'cosine', 'euclidean', '11', '12', 'manhattan']
- from scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule']

See the documentation for scipy.spatial.distance for details on these metrics.

- **p** [integer, optional (default=2)] Parameter for the Minkowski metric from *sklearn*. *metrics.pairwise\_distances*. When p = 1, this is equivalent to using manhattan\_distance (11), and euclidean\_distance (12) for p = 2. For arbitrary p, minkowski\_distance (1\_p) is used.
- **metric\_params** [dict, optional (default=None)] Additional keyword arguments for the metric function.
- **cluster\_method** [string, optional (default='xi')] The extraction method used to extract clusters using the calculated reachability and ordering. Possible values are "xi" and "dbscan".
- eps [float, optional (default=None)] The maximum distance between two samples for one to be considered as in the neighborhood of the other. By default it assumes the same value as max\_eps. Used only when cluster\_method='dbscan'.
- xi [float, between 0 and 1, optional (default=0.05)] Determines the minimum steepness on the reachability plot that constitutes a cluster boundary. For example, an upwards point in the reachability plot is defined by the ratio from one point to its successor being at most 1-xi. Used only when cluster\_method='xi'.
- **predecessor\_correction** [bool, optional (default=True)] Correct clusters according to the predecessors calculated by OPTICS [R2c55e37003fe-2]. This parameter has minimal effect on most datasets. Used only when cluster\_method='xi'.
- min\_cluster\_size [int > 1 or float between 0 and 1 (default=None)] Minimum number of samples in an OPTICS cluster, expressed as an absolute number or a fraction of the number of samples (rounded to be at least 2). If None, the value of min\_samples is used instead. Used only when cluster\_method='xi'.
- **algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] Algorithm used to compute the nearest neighbors:
  - 'ball tree' will use BallTree
  - 'kd\_tree' will use KDTree
  - 'brute' will use a brute-force search.
  - 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method. (default)

Note: fitting on sparse input will override the setting of this parameter, using brute force.

**leaf\_size** [int, optional (default=30)] Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

**n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

### **Attributes**

- labels\_ [array, shape (n\_samples,)] Cluster labels for each point in the dataset given to fit(). Noisy samples and points which are not included in a leaf cluster of cluster\_hierarchy\_ are labeled as -1.
- **reachability** [array, shape (n\_samples,)] Reachability distances per sample, indexed by object order. Use clust.reachability\_[clust.ordering\_] to access in cluster order.
- **ordering**\_ [array, shape (n\_samples,)] The cluster ordered list of sample indices.
- core\_distances\_ [array, shape (n\_samples,)] Distance at which each sample becomes a core
  point, indexed by object order. Points which will never be core have a distance of inf. Use
  clust.core\_distances\_[clust.ordering\_] to access in cluster order.
- **predecessor**\_ [array, shape (n\_samples,)] Point that a sample was reached from, indexed by object order. Seed points have a predecessor of -1.
- cluster\_hierarchy\_ [array, shape (n\_clusters, 2)] The list of clusters in the form of [start,
   end] in each row, with all indices inclusive. The clusters are ordered according
   to (end, -start) (ascending) so that larger clusters encompassing smaller clusters
   come after those smaller ones. Since labels\_ does not reflect the hierarchy, usually
   len(cluster\_hierarchy\_) > np.unique(optics.labels\_). Please also
   note that these indices are of the ordering\_, i.e. X[ordering\_][start:end +
   1] form a cluster. Only available when cluster\_method='xi'.

# See also:

**DBSCAN** A similar clustering for a specified neighborhood radius (eps). Our implementation is optimized for runtime.

# References

[R2c55e37003fe-1], [R2c55e37003fe-2]

# **Methods**

fit(self, X[, y])	Perform OPTICS clustering
$fit\_predict(self, X[, y])$	Performs clustering on X and returns cluster labels.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_ (self, min\_samples=5, max\_eps=inf, metric='minkowski', p=2, metric\_params=None, cluster\_method='xi', eps=None, xi=0.05, predecessor\_correction=True, min cluster size=None, algorithm='auto', leaf size=30, n jobs=None)

**fit** (self, X, y=None)

Perform OPTICS clustering

Extracts an ordered list of points and reachability distances, and performs initial clustering using max\_eps distance specified at OPTICS object instantiation.

#### **Parameters**

- **X** [array, shape (n\_samples, n\_features), or (n\_samples, n\_samples) if metric='precomputed'.] A feature array, or array of distances between samples if metric='precomputed'.
- y [ignored]

# Returns

**self** [instance of OPTICS] The instance.

# fit\_predict (self, X, y=None)

Performs clustering on X and returns cluster labels.

### **Parameters**

- **X** [ndarray, shape (n\_samples, n\_features)] Input data.
- y [Ignored] not used, present for API consistency by convention.

### **Returns**

labels [ndarray, shape (n\_samples,)] cluster labels

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# Examples using sklearn.cluster.OPTICS

- Demo of OPTICS clustering algorithm
- Comparing different clustering algorithms on toy datasets

# sklearn.cluster.FeatureAgglomeration

```
 \begin{array}{c} \textbf{class} \; \textbf{sklearn.cluster.FeatureAgglomeration} \; (\textit{n\_clusters} = 2, & \textit{affinity} = '\textit{euclidean'}, & \textit{mem-ory} = \textit{None}, & \textit{connectivity} = \textit{None}, & \textit{com-pute\_full\_tree} = '\textit{auto'}, & \textit{linkage} = '\textit{ward'}, \\ \textit{pooling\_func} = < \textit{function} & \textit{mean} >, & \textit{distance\_threshold} = \textit{None}) \\ \end{array}
```

Agglomerate features.

Similar to AgglomerativeClustering, but recursively merges features instead of samples.

Read more in the *User Guide*.

#### **Parameters**

- **n\_clusters** [int or None, optional (default=2)] The number of clusters to find. It must be None if distance\_threshold is not None.
- **affinity** [string or callable, default "euclidean"] Metric used to compute the linkage. Can be "euclidean", "11", "12", "manhattan", "cosine", or 'precomputed'. If linkage is "ward", only "euclidean" is accepted.
- **memory** [None, str or object with the joblib.Memory interface, optional] Used to cache the output of the computation of the tree. By default, no caching is done. If a string is given, it is the path to the caching directory.
- connectivity [array-like or callable, optional] Connectivity matrix. Defines for each feature the neighboring features following a given structure of the data. This can be a connectivity matrix itself or a callable that transforms the data into a connectivity matrix, such as derived from kneighbors\_graph. Default is None, i.e, the hierarchical clustering algorithm is unstructured.
- compute\_full\_tree [bool or 'auto', optional, default "auto"] Stop early the construction of the tree at n\_clusters. This is useful to decrease computation time if the number of clusters is not small compared to the number of features. This option is useful only when specifying a connectivity matrix. Note also that when varying the number of clusters and using caching, it may be advantageous to compute the full tree. It must be True if distance threshold is not None.
- **linkage** [{"ward", "complete", "average", "single"}, optional (default="ward")] Which linkage criterion to use. The linkage criterion determines which distance to use between sets of features. The algorithm will merge the pairs of cluster that minimize this criterion.
  - ward minimizes the variance of the clusters being merged.
  - average uses the average of the distances of each feature of the two sets.
  - complete or maximum linkage uses the maximum distances between all features of the two sets.
  - single uses the minimum of the distances between all observations of the two sets.
- **pooling\_func** [callable, default np.mean] This combines the values of agglomerated features into a single value, and should accept an array of shape [M, N] and the keyword argument axis=1, and reduce it to an array of size [M].
- **distance\_threshold** [float, optional (default=None)] The linkage distance threshold above which, clusters will not be merged. If not None, n\_clusters must be None and compute full tree must be True.

New in version 0.21.

# Attributes

- **n\_clusters\_** [int] The number of clusters found by the algorithm. If distance\_threshold=None, it will be equal to the given n\_clusters.
- **labels**\_ [array-like, (n\_features,)] cluster labels for each feature.
- **n\_leaves**\_ [int] Number of leaves in the hierarchical tree.
- **n\_connected\_components\_** [int] The estimated number of connected components in the graph.
- **children**\_ [array-like, shape (n\_nodes-1, 2)] The children of each non-leaf node. Values less than  $n_{features}$  correspond to leaves of the tree which are the original samples. A node

i greater than or equal to  $n\_features$  is a non-leaf node and has children <code>children\_[i] - n\_features]</code>. Alternatively at the i-th iteration, children[i][0] and children[i][1] are merged to form node <code>n\_features + i</code>

# **Examples**

### **Methods**

fit(self, X[, y])	Fit the hierarchical clustering on the data
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, Xred)	Inverse the transformation.
pooling_func(a[, axis, dtype, out, keepdims])	Compute the arithmetic mean along the specified axis.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform a new matrix using the built clustering

```
__init__ (self, n_clusters=2, affinity='euclidean', memory=None, connectivity=None, compute_full_tree='auto', linkage='ward', pooling_func=<function mean at 0x7f3c23df3400>, distance_threshold=None)
```

fit (self, X, y=None, \*\*params)

Fit the hierarchical clustering on the data

# **Parameters**

```
\mathbf{X} [array-like, shape = [n_samples, n_features]] The data
```

y [Ignored]

#### Returns

self

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit params and returns a transformed version of X.

#### **Parameters**

**X** [numpy array of shape [n\_samples, n\_features]] Training set.

y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

# inverse\_transform(self, Xred)

Inverse the transformation. Return a vector of size nb\_features with the values of Xred assigned to each group of features

#### **Parameters**

**Xred** [array-like, shape=[n\_samples, n\_clusters] or [n\_clusters,]] The values to be assigned to each cluster of samples

#### Returns

**X** [array, shape=[n\_samples, n\_features] or [n\_features]] A vector of size n\_samples with the values of Xred assigned to each of the cluster of samples.

pooling\_func (a, axis=None, dtype=None, out=None, keepdims=<no value>)

Compute the arithmetic mean along the specified axis.

Returns the average of the array elements. The average is taken over the flattened array by default, otherwise over the specified axis. float64 intermediate and return values are used for integer inputs.

#### **Parameters**

- **a** [array\_like] Array containing numbers whose mean is desired. If a is not an array, a conversion is attempted.
- **axis** [None or int or tuple of ints, optional] Axis or axes along which the means are computed. The default is to compute the mean of the flattened array.

New in version 1.7.0.

If this is a tuple of ints, a mean is performed over multiple axes, instead of a single axis or all the axes as before.

- **dtype** [data-type, optional] Type to use in computing the mean. For integer inputs, the default is float 64; for floating point inputs, it is the same as the input dtype.
- out [ndarray, optional] Alternate output array in which to place the result. The default is None; if provided, it must have the same shape as the expected output, but the type will be cast if necessary. See doc.ufuncs for details.
- **keepdims** [bool, optional] If this is set to True, the axes which are reduced are left in the result as dimensions with size one. With this option, the result will broadcast correctly against the input array.

If the default value is passed, then keepdims will not be passed through to the mean method of sub-classes of ndarray, however any non-default value will be. If the sub-class' method does not implement keepdims any exceptions will be raised.

#### Returns

**m** [ndarray, see dtype parameter above] If out=None, returns a new array containing the mean values, otherwise a reference to the output array is returned.

See also:

```
average Weighted average
std, var, nanmean, nanstd, nanvar
```

### **Notes**

The arithmetic mean is the sum of the elements along the axis divided by the number of elements.

Note that for floating-point input, the mean is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-precision accumulator using the *dtype* keyword can alleviate this issue.

By default, float16 results are computed using float32 intermediates for extra precision.

# **Examples**

```
>>> a = np.array([[1, 2], [3, 4]])
>>> np.mean(a)
2.5
>>> np.mean(a, axis=0)
array([ 2.,  3.])
>>> np.mean(a, axis=1)
array([ 1.5,  3.5])
```

In single precision, mean can be inaccurate:

```
>>> a = np.zeros((2, 512*512), dtype=np.float32)
>>> a[0, :] = 1.0
>>> a[1, :] = 0.1
>>> np.mean(a)
0.54999924
```

Computing the mean in float64 is more accurate:

```
>>> np.mean(a, dtype=np.float64)
0.55000000074505806
```

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### **Returns**

self

# transform(self, X)

Transform a new matrix using the built clustering

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features] or [n\_features]] A M by N array of M observations in N dimensions or a length M array of M one-dimensional observations.

#### Returns

Y [array, shape = [n\_samples, n\_clusters] or [n\_clusters]] The pooled values for each feature cluster

# Examples using sklearn.cluster.FeatureAgglomeration

- Feature agglomeration
- Feature agglomeration vs. univariate selection

#### sklearn.cluster.KMeans

```
class sklearn.cluster.KMeans (n_clusters=8, init='k-means++', n_init=10, max_iter=300, tol=0.0001, precompute_distances='auto', verbose=0, random_state=None, copy_x=True, n_iobs=None, algorithm='auto')
```

K-Means clustering

Read more in the User Guide.

#### **Parameters**

- **n\_clusters** [int, optional, default: 8] The number of clusters to form as well as the number of centroids to generate.
- init [{'k-means++', 'random' or an ndarray}] Method for initialization, defaults to 'kmeans++':

'k-means++': selects initial cluster centers for k-mean clustering in a smart way to speed up convergence. See section Notes in k\_init for more details.

'random': choose k observations (rows) at random from data for the initial centroids.

If an ndarray is passed, it should be of shape (n\_clusters, n\_features) and gives the initial centers.

- n\_init [int, default: 10] Number of time the k-means algorithm will be run with different centroid seeds. The final results will be the best output of n\_init consecutive runs in terms of inertia.
- **max\_iter** [int, default: 300] Maximum number of iterations of the k-means algorithm for a single run.
- tol [float, default: 1e-4] Relative tolerance with regards to inertia to declare convergence
- precompute\_distances [{'auto', True, False}] Precompute distances (faster but takes more memory).

'auto': do not precompute distances if n\_samples \* n\_clusters > 12 million. This corresponds to about 100MB overhead per job using double precision.

True: always precompute distances

False: never precompute distances

verbose [int, default 0] Verbosity mode.

- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for centroid initialization. Use an int to make the randomness deterministic. See *Glossary*.
- copy\_x [boolean, optional] When pre-computing distances it is more numerically accurate to center the data first. If copy\_x is True (default), then the original data is not modified, ensuring X is C-contiguous. If False, the original data is modified, and put back before the function returns, but small numerical differences may be introduced by subtracting and then adding the data mean, in this case it will also not ensure that data is C-contiguous which may cause a significant slowdown.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. This works by computing each of the n\_init runs in parallel.

None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

algorithm ["auto", "full" or "elkan", default="auto"] K-means algorithm to use. The classical EM-style algorithm is "full". The "elkan" variation is more efficient by using the triangle inequality, but currently doesn't support sparse data. "auto" chooses "elkan" for dense data and "full" for sparse data.

#### **Attributes**

cluster\_centers\_ [array, [n\_clusters, n\_features]] Coordinates of cluster centers. If the algorithm stops before fully converging (see tol and max\_iter), these will not be consistent
with labels\_.

labels: Labels of each point

inertia\_ [float] Sum of squared distances of samples to their closest cluster center.

**n\_iter\_** [int] Number of iterations run.

# See also:

**MiniBatchKMeans** Alternative online implementation that does incremental updates of the centers positions using mini-batches. For large scale learning (say n\_samples > 10k) MiniBatchKMeans is probably much faster than the default batch implementation.

### **Notes**

The k-means problem is solved using either Lloyd's or Elkan's algorithm.

The average complexity is given by O(k n T), were n is the number of samples and T is the number of iteration.

The worst case complexity is given by  $O(n^{(k+2/p)})$  with n = n\_samples, p = n\_features. (D. Arthur and S. Vassilvitskii, 'How slow is the k-means method?' SoCG2006)

In practice, the k-means algorithm is very fast (one of the fastest clustering algorithms available), but it falls in local minima. That's why it can be useful to restart it several times.

If the algorithm stops before fully converging (because of tol or max\_iter), labels\_ and cluster\_centers\_ will not be consistent, i.e. the cluster\_centers\_ will not be the means of the points in each cluster. Also, the estimator will reassign labels\_ after the last iteration to make labels\_ consistent with predict on the training set.

# **Examples**

#### **Methods**

fit(self, X[, y, sample_weight])	Compute k-means clustering.
<pre>fit_predict(self, X[, y, sample_weight])</pre>	Compute cluster centers and predict cluster index for
	each sample.
<pre>fit_transform(self, X[, y, sample_weight])</pre>	Compute clustering and transform X to cluster-distance
	space.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, sample_weight])</pre>	Predict the closest cluster each sample in X belongs to.
score(self, X[, y, sample_weight])	Opposite of the value of X on the K-means objective.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Transform X to a cluster-distance space.

```
__init__ (self, n_clusters=8, init='k-means++', n_init=10, max_iter=300, tol=0.0001, precompute_distances='auto', verbose=0, random_state=None, copy_x=True, n_jobs=None, algorithm='auto')
```

# fit (self, X, y=None, sample\_weight=None)

Compute k-means clustering.

# **Parameters**

- **X** [array-like or sparse matrix, shape=(n\_samples, n\_features)] Training instances to cluster. It must be noted that the data will be converted to C ordering, which will cause a memory copy if the given data is not C-contiguous.
- y [Ignored] not used, present here for API consistency by convention.
- **sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)
- fit\_predict (self, X, y=None, sample\_weight=None)

Compute cluster centers and predict cluster index for each sample.

Convenience method; equivalent to calling fit(X) followed by predict(X).

# **Parameters**

- $X = \{\text{array-like, sparse matrix}\}, \text{ shape} = [\text{n\_samples, n\_features}]\}$  New data to transform.
- y [Ignored] not used, present here for API consistency by convention.

**sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)

#### Returns

labels [array, shape [n\_samples,]] Index of the cluster each sample belongs to.

**fit\_transform** (*self*, *X*, *y=None*, *sample\_weight=None*)

Compute clustering and transform X to cluster-distance space.

Equivalent to fit(X).transform(X), but more efficiently implemented.

#### **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] New data to transform.
- **y** [Ignored] not used, present here for API consistency by convention.

**sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)

### **Returns**

**X\_new** [array, shape [n\_samples, k]] X transformed in the new space.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

# predict (self, X, sample\_weight=None)

Predict the closest cluster each sample in X belongs to.

In the vector quantization literature, cluster\_centers\_ is called the code book and each value returned by predict is the index of the closest code in the code book.

### **Parameters**

 $\mathbf{X}$  [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] New data to predict.

**sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)

### Returns

labels [array, shape [n\_samples,]] Index of the cluster each sample belongs to.

score (self, X, y=None, sample\_weight=None)

Opposite of the value of X on the K-means objective.

# **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] New data.
- y [Ignored] not used, present here for API consistency by convention.

**sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)

#### Returns

**score** [float] Opposite of the value of X on the K-means objective.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## transform(self, X)

Transform X to a cluster-distance space.

In the new space, each dimension is the distance to the cluster centers. Note that even if X is sparse, the array returned by *transform* will typically be dense.

## **Parameters**

**X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] New data to transform.

#### Returns

**X\_new** [array, shape [n\_samples, k]] X transformed in the new space.

# Examples using sklearn.cluster.KMeans

- Demonstration of k-means assumptions
- Vector Quantization Example
- K-means Clustering
- Color Quantization using K-Means
- Empirical evaluation of the impact of k-means initialization
- Comparison of the K-Means and MiniBatchKMeans clustering algorithms
- A demo of K-Means clustering on the handwritten digits data
- Selecting the number of clusters with silhouette analysis on KMeans clustering
- Clustering text documents using k-means

## sklearn.cluster.MiniBatchKMeans

 $\begin{array}{lll} \textbf{class} \; \textbf{sklearn.cluster.MiniBatchKMeans} \; (n\_clusters=8, & init='k-means++', & max\_iter=100, \\ & batch\_size=100, & verbose=0, & compute\_labels=True, \\ & random\_state=None, \; tol=0.0, \; max\_no\_improvement=10, \\ & init\_size=None, \; n\_init=3, \; reassignment\_ratio=0.01) \end{array}$ 

Mini-Batch K-Means clustering

Read more in the *User Guide*.

# **Parameters**

**n\_clusters** [int, optional, default: 8] The number of clusters to form as well as the number of centroids to generate.

init [{'k-means++', 'random' or an ndarray}, default: 'k-means++'] Method for initialization,
 defaults to 'k-means++':

'k-means++': selects initial cluster centers for k-mean clustering in a smart way to speed up convergence. See section Notes in k\_init for more details.

'random': choose k observations (rows) at random from data for the initial centroids.

If an ndarray is passed, it should be of shape (n\_clusters, n\_features) and gives the initial centers

**max\_iter** [int, optional] Maximum number of iterations over the complete dataset before stopping independently of any early stopping criterion heuristics.

batch\_size [int, optional, default: 100] Size of the mini batches.

verbose [boolean, optional] Verbosity mode.

**compute\_labels** [boolean, default=True] Compute label assignment and inertia for the complete dataset once the minibatch optimization has converged in fit.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for centroid initialization and random reassignment. Use an int to make the randomness deterministic. See *Glossary*.

tol [float, default: 0.0] Control early stopping based on the relative center changes as measured by a smoothed, variance-normalized of the mean center squared position changes. This early stopping heuristics is closer to the one used for the batch variant of the algorithms but induces a slight computational and memory overhead over the inertia heuristic.

To disable convergence detection based on normalized center change, set tol to 0.0 (default).

**max\_no\_improvement** [int, default: 10] Control early stopping based on the consecutive number of mini batches that does not yield an improvement on the smoothed inertia.

To disable convergence detection based on inertia, set max\_no\_improvement to None.

- init\_size [int, optional, default: 3 \* batch\_size] Number of samples to randomly sample for speeding up the initialization (sometimes at the expense of accuracy): the only algorithm is initialized by running a batch KMeans on a random subset of the data. This needs to be larger than n\_clusters.
- **n\_init** [int, default=3] Number of random initializations that are tried. In contrast to KMeans, the algorithm is only run once, using the best of the n\_init initializations as measured by inertia.
- **reassignment\_ratio** [float, default: 0.01] Control the fraction of the maximum number of counts for a center to be reassigned. A higher value means that low count centers are more easily reassigned, which means that the model will take longer to converge, but should converge in a better clustering.

## **Attributes**

cluster\_centers\_ [array, [n\_clusters, n\_features]] Coordinates of cluster centers

**labels\_:** Labels of each point (if compute\_labels is set to True).

inertia\_ [float] The value of the inertia criterion associated with the chosen partition (if compute\_labels is set to True). The inertia is defined as the sum of square distances of samples to their nearest neighbor.

See also:

**KMeans** The classic implementation of the clustering method based on the Lloyd's algorithm. It consumes the whole set of input data at each iteration.

## **Notes**

See https://www.eecs.tufts.edu/~dsculley/papers/fastkmeans.pdf

# **Examples**

```
>>> from sklearn.cluster import MiniBatchKMeans
>>> import numpy as np
>>> X = np.array([[1, 2], [1, 4], [1, 0],
                  [4, 2], [4, 0], [4, 4],
                  [4, 5], [0, 1], [2, 2],
. . .
                  [3, 2], [5, 5], [1, -1]])
>>> # manually fit on batches
>>> kmeans = MiniBatchKMeans(n_clusters=2,
                              random_state=0,
. . .
                             batch_size=6)
. . .
>>> kmeans = kmeans.partial_fit(X[0:6,:])
>>> kmeans = kmeans.partial_fit(X[6:12,:])
>>> kmeans.cluster_centers_
array([[1, 1],
       [3, 4]])
>>> kmeans.predict([[0, 0], [4, 4]])
array([0, 1], dtype=int32)
>>> # fit on the whole data
>>> kmeans = MiniBatchKMeans(n_clusters=2,
                             random_state=0,
                             batch_size=6,
. . .
                             max_iter=10).fit(X)
>>> kmeans.cluster_centers_
array([[3.95918367, 2.40816327],
       [1.12195122, 1.3902439 ]])
>>> kmeans.predict([[0, 0], [4, 4]])
array([1, 0], dtype=int32)
```

## **Methods**

fit(self, X[, y, sample_weight])	Compute the centroids on X by chunking it into mini-
	batches.
<pre>fit_predict(self, X[, y, sample_weight])</pre>	Compute cluster centers and predict cluster index for
	each sample.
<pre>fit_transform(self, X[, y, sample_weight])</pre>	Compute clustering and transform X to cluster-distance
	space.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X[, y, sample_weight])</pre>	Update k means estimate on a single mini-batch X.
<pre>predict(self, X[, sample_weight])</pre>	Predict the closest cluster each sample in X belongs to.
score(self, X[, y, sample_weight])	Opposite of the value of X on the K-means objective.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Transform X to a cluster-distance space.

- \_\_init\_\_ (self, n\_clusters=8, init='k-means++', max\_iter=100, batch\_size=100, verbose=0, compute\_labels=True, random\_state=None, tol=0.0, max\_no\_improvement=10, init\_size=None, n\_init=3, reassignment\_ratio=0.01)
- **fit** (self, X, y=None, sample weight=None)

Compute the centroids on X by chunking it into mini-batches.

#### **Parameters**

- **X** [array-like or sparse matrix, shape=(n\_samples, n\_features)] Training instances to cluster. It must be noted that the data will be converted to C ordering, which will cause a memory copy if the given data is not C-contiguous.
- y [Ignored] not used, present here for API consistency by convention.
- **sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)
- fit\_predict (self, X, y=None, sample\_weight=None)

Compute cluster centers and predict cluster index for each sample.

Convenience method; equivalent to calling fit(X) followed by predict(X).

## **Parameters**

- X [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] New data to transform.
- y [Ignored] not used, present here for API consistency by convention.

**sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)

#### Returns

labels [array, shape [n\_samples,]] Index of the cluster each sample belongs to.

fit\_transform(self, X, y=None, sample\_weight=None)

Compute clustering and transform X to cluster-distance space.

Equivalent to fit(X).transform(X), but more efficiently implemented.

## **Parameters**

- X [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] New data to transform.
- y [Ignored] not used, present here for API consistency by convention.

**sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)

## **Returns**

**X\_new** [array, shape [n\_samples, k]] X transformed in the new space.

#### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

partial\_fit (self, X, y=None, sample\_weight=None)

Update k means estimate on a single mini-batch X.

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Coordinates of the data points to cluster. It must be noted that X will be copied if it is not C-contiguous.
- y [Ignored] not used, present here for API consistency by convention.

**sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)

## predict (self, X, sample\_weight=None)

Predict the closest cluster each sample in X belongs to.

In the vector quantization literature, cluster\_centers\_ is called the code book and each value returned by predict is the index of the closest code in the code book.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] New data to predict.

**sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)

#### Returns

labels [array, shape [n\_samples,]] Index of the cluster each sample belongs to.

score (self, X, y=None, sample\_weight=None)

Opposite of the value of X on the K-means objective.

#### **Parameters**

- X [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] New data.
- y [Ignored] not used, present here for API consistency by convention.

**sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)

#### Returns

**score** [float] Opposite of the value of X on the K-means objective.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# transform(self, X)

Transform X to a cluster-distance space.

In the new space, each dimension is the distance to the cluster centers. Note that even if X is sparse, the array returned by transform will typically be dense.

# **Parameters**

**X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] New data to transform.

## Returns

**X\_new** [array, shape [n\_samples, k]] X transformed in the new space.

## Examples using sklearn.cluster.MiniBatchKMeans

- Biclustering documents with the Spectral Co-clustering algorithm
- Online learning of a dictionary of parts of faces
- · Compare BIRCH and MiniBatchKMeans
- Empirical evaluation of the impact of k-means initialization
- Comparison of the K-Means and MiniBatchKMeans clustering algorithms
- · Comparing different clustering algorithms on toy datasets
- Faces dataset decompositions
- Clustering text documents using k-means

## sklearn.cluster.MeanShift

 $\begin{array}{c} \textbf{class} \text{ sklearn.cluster.} \textbf{MeanShift} \ (bandwidth=None, & seeds=None, & bin\_seeding=False, \\ & min\_bin\_freq=1, \ cluster\_all=True, \ n\_jobs=None) \\ \\ \textbf{Mean shift clustering using a flat kernel.} \end{array}$ 

Mean shift clustering aims to discover "blobs" in a smooth density of samples. It is a centroid-based algorithm, which works by updating candidates for centroids to be the mean of the points within a given region. These candidates are then filtered in a post-processing stage to eliminate near-duplicates to form the final set of centroids.

Seeding is performed using a binning technique for scalability.

Read more in the User Guide.

## **Parameters**

bandwidth [float, optional] Bandwidth used in the RBF kernel.

If not given, the bandwidth is estimated using sklearn.cluster.estimate\_bandwidth; see the documentation for that function for hints on scalability (see also the Notes, below).

- **seeds** [array, shape=[n\_samples, n\_features], optional] Seeds used to initialize kernels. If not set, the seeds are calculated by clustering.get\_bin\_seeds with bandwidth as the grid size and default values for other parameters.
- **bin\_seeding** [boolean, optional] If true, initial kernel locations are not locations of all points, but rather the location of the discretized version of points, where points are binned onto a grid whose coarseness corresponds to the bandwidth. Setting this option to True will speed up the algorithm because fewer seeds will be initialized. default value: False Ignored if seeds argument is not None.
- min\_bin\_freq [int, optional] To speed up the algorithm, accept only those bins with at least min\_bin\_freq points as seeds. If not defined, set to 1.
- **cluster\_all** [boolean, default True] If true, then all points are clustered, even those orphans that are not within any kernel. Orphans are assigned to the nearest kernel. If false, then orphans are given cluster label -1.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. This works by computing each of the n\_init runs in parallel.

None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

## **Attributes**

cluster\_centers\_ [array, [n\_clusters, n\_features]] Coordinates of cluster centers.labels\_: Labels of each point.

# Notes

# Scalability:

Because this implementation uses a flat kernel and a Ball Tree to look up members of each kernel, the complexity will tend towards  $O(T^*n^*log(n))$  in lower dimensions, with n the number of samples and T the number of points. In higher dimensions the complexity will tend towards  $O(T^*n^2)$ .

Scalability can be boosted by using fewer seeds, for example by using a higher value of min\_bin\_freq in the get\_bin\_seeds function.

Note that the estimate\_bandwidth function is much less scalable than the mean shift algorithm and will be the bottleneck if it is used.

## References

Dorin Comaniciu and Peter Meer, "Mean Shift: A robust approach toward feature space analysis". IEEE Transactions on Pattern Analysis and Machine Intelligence. 2002. pp. 603-619.

# **Examples**

## **Methods**

fit(self, X[, y])	Perform clustering.
$fit\_predict(self, X[, y])$	Performs clustering on X and returns cluster labels.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict the closest cluster each sample in X belongs to.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, bandwidth=None, seeds=None, bin_seeding=False, min_bin_freq=1, cluster_all=True, n_jobs=None)

fit (self, X, y=None)
```

Perform clustering.

## **Parameters**

- **X** [array-like, shape=[n\_samples, n\_features]] Samples to cluster.
- y [Ignored]

## fit predict (self, X, y=None)

Performs clustering on X and returns cluster labels.

## **Parameters**

- **X** [ndarray, shape (n\_samples, n\_features)] Input data.
- y [Ignored] not used, present for API consistency by convention.

#### Returns

labels [ndarray, shape (n\_samples,)] cluster labels

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## **Returns**

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict the closest cluster each sample in X belongs to.

# **Parameters**

**X** [{array-like, sparse matrix}, shape=[n\_samples, n\_features]] New data to predict.

#### Returns

labels [array, shape [n\_samples,]] Index of the cluster each sample belongs to.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# Examples using sklearn.cluster.MeanShift

- $\bullet \ \ A \ demo \ of \ the \ mean-shift \ clustering \ algorithm$
- Comparing different clustering algorithms on toy datasets

## sklearn.cluster.SpectralClustering

```
class sklearn.cluster.SpectralClustering (n\_clusters=8, eigen\_solver=None, random\_state=None, n\_init=10, gamma=1.0, affinity='rbf', n\_neighbors=10, eigen\_tol=0.0, assign\_labels='kmeans', degree=3, coef0=1, kernel\_params=None, n\_jobs=None)
```

Apply clustering to a projection of the normalized Laplacian.

In practice Spectral Clustering is very useful when the structure of the individual clusters is highly non-convex or more generally when a measure of the center and spread of the cluster is not a suitable description of the complete cluster. For instance when clusters are nested circles on the 2D plane.

If affinity is the adjacency matrix of a graph, this method can be used to find normalized graph cuts.

When calling fit, an affinity matrix is constructed using either kernel function such the Gaussian (aka RBF) kernel of the euclidean distanced d(X, X):

```
np.exp(-gamma * d(X,X) ** 2)
```

or a k-nearest neighbors connectivity matrix.

Alternatively, using precomputed, a user-provided affinity matrix can be used.

Read more in the User Guide.

#### **Parameters**

- **n\_clusters** [integer, optional] The dimension of the projection subspace.
- **eigen\_solver** [{None, 'arpack', 'lobpcg', or 'amg'}] The eigenvalue decomposition strategy to use. AMG requires pyamg to be installed. It can be faster on very large, sparse problems, but may also lead to instabilities.
- **random\_state** [int, RandomState instance or None (default)] A pseudo random number generator used for the initialization of the lobpcg eigen vectors decomposition when eigen\_solver='amg' and by the K-Means initialization. Use an int to make the randomness deterministic. See *Glossary*.
- **n\_init** [int, optional, default: 10] Number of time the k-means algorithm will be run with different centroid seeds. The final results will be the best output of n\_init consecutive runs in terms of inertia.
- **gamma** [float, default=1.0] Kernel coefficient for rbf, poly, sigmoid, laplacian and chi2 kernels. Ignored for affinity='nearest\_neighbors'.
- **affinity** [string, array-like or callable, default 'rbf'] If a string, this may be one of 'nearest\_neighbors', 'precomputed', 'rbf' or one of the kernels supported by sklearn. metrics.pairwise\_kernels.
  - Only kernels that produce similarity scores (non-negative values that increase with similarity) should be used. This property is not checked by the clustering algorithm.
- **n\_neighbors** [integer] Number of neighbors to use when constructing the affinity matrix using the nearest neighbors method. Ignored for affinity='rbf'.
- **eigen\_tol** [float, optional, default: 0.0] Stopping criterion for eigendecomposition of the Laplacian matrix when eigen\_solver='arpack'.
- **assign\_labels** [{'kmeans', 'discretize'}, default: 'kmeans'] The strategy to use to assign labels in the embedding space. There are two ways to assign labels after the laplacian embedding.

k-means can be applied and is a popular choice. But it can also be sensitive to initialization. Discretization is another approach which is less sensitive to random initialization.

**degree** [float, default=3] Degree of the polynomial kernel. Ignored by other kernels.

coef0 [float, default=1] Zero coefficient for polynomial and sigmoid kernels. Ignored by other kernels.

**kernel\_params** [dictionary of string to any, optional] Parameters (keyword arguments) and values for kernel passed as callable object. Ignored by other kernels.

**n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### Attributes

**affinity\_matrix** [array-like, shape (n\_samples, n\_samples)] Affinity matrix used for clustering. Available only if after calling fit.

labels\_: Labels of each point

## **Notes**

If you have an affinity matrix, such as a distance matrix, for which 0 means identical elements, and high values means very dissimilar elements, it can be transformed in a similarity matrix that is well suited for the algorithm by applying the Gaussian (RBF, heat) kernel:

```
np.exp(- dist_matrix ** 2 / (2. * delta ** 2))
```

Where delta is a free parameter representing the width of the Gaussian kernel.

Another alternative is to take a symmetric version of the k nearest neighbors connectivity matrix of the points.

If the pyamg package is installed, it is used: this greatly speeds up computation.

## References

- Normalized cuts and image segmentation, 2000 Jianbo Shi, Jitendra Malik http://citeseer.ist.psu.edu/viewdoc/summary?doi=10.1.1.160.2324
- A Tutorial on Spectral Clustering, 2007 Ulrike von Luxburg http://citeseerx.ist.psu.edu/viewdoc/ summary?doi=10.1.1.165.9323
- Multiclass spectral clustering, 2003 Stella X. Yu, Jianbo Shi https://www1.icsi.berkeley.edu/~stellayu/publication/doc/2003kwayICCV.pdf

## **Examples**

## **Methods**

fit(self, X[, y])	Creates an affinity matrix for X using the selected affinity, then applies spectral clustering to this affinity matrix.
<pre>fit_predict(self, X[, y])</pre>	Performs clustering on X and returns cluster labels.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, n\_clusters=8, eigen\_solver=None, random\_state=None, n\_init=10, gamma=1.0, affinity='rbf', n\_neighbors=10, eigen\_tol=0.0, assign\_labels='kmeans', degree=3, coef0=1, kernel\_params=None, n\_jobs=None)

## **fit** (self, X, y=None)

Creates an affinity matrix for X using the selected affinity, then applies spectral clustering to this affinity matrix.

## **Parameters**

- **X** [array-like or sparse matrix, shape (n\_samples, n\_features)] OR, if affinity=='precomputed', a precomputed affinity matrix of shape (n\_samples, n\_samples)
- y [Ignored]

# fit\_predict (self, X, y=None)

Performs clustering on X and returns cluster labels.

#### **Parameters**

- **X** [ndarray, shape (n\_samples, n\_features)] Input data.
- **y** [Ignored] not used, present for API consistency by convention.

## Returns

labels [ndarray, shape (n\_samples,)] cluster labels

## get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

**params** [mapping of string to any] Parameter names mapped to their values.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# Examples using sklearn.cluster.SpectralClustering

• Comparing different clustering algorithms on toy datasets

# 6.3.2 Functions

cluster.affinity_propagation( $S[,]$ )	Perform Affinity Propagation Clustering of data
cluster.cluster_optics_dbscan(reachability,	Performs DBSCAN extraction for an arbitrary epsilon.
)	
cluster.cluster_optics_xi(reachability,)	Automatically extract clusters according to the Xi-steep
	method.
cluster.compute_optics_graph(X,	Computes the OPTICS reachability graph.
min_samples,)	
$cluster.dbscan(X[, eps, min_samples,])$	Perform DBSCAN clustering from vector array or distance
	matrix.
cluster.estimate_bandwidth( $X[$ , quantile,])	Estimate the bandwidth to use with the mean-shift algo-
	rithm.
cluster.k_means(X, n_clusters[,])	K-means clustering algorithm.
$cluster.mean\_shift(X[, bandwidth, seeds,])$	Perform mean shift clustering of data using a flat kernel.
$cluster.spectral\_clustering(affinity[,])$	Apply clustering to a projection of the normalized Lapla-
	cian.
$cluster.ward\_tree(X[,connectivity,])$	Ward clustering based on a Feature matrix.

## sklearn.cluster.affinity\_propagation

```
sklearn.cluster.affinity_propagation(S, preference=None, convergence_iter=15, max_iter=200, damping=0.5, copy=True, verbose=False, return_n_iter=False)
```

Perform Affinity Propagation Clustering of data

Read more in the User Guide.

## **Parameters**

S [array-like, shape (n\_samples, n\_samples)] Matrix of similarities between points

**preference** [array-like, shape (n\_samples,) or float, optional] Preferences for each point - points with larger values of preferences are more likely to be chosen as exemplars. The number of exemplars, i.e. of clusters, is influenced by the input preferences value. If the preferences are not passed as arguments, they will be set to the median of the input similarities (resulting in a moderate number of clusters). For a smaller amount of clusters, this can be set to the minimum value of the similarities.

**convergence\_iter** [int, optional, default: 15] Number of iterations with no change in the number of estimated clusters that stops the convergence.

max\_iter [int, optional, default: 200] Maximum number of iterations

```
damping [float, optional, default: 0.5] Damping factor between 0.5 and 1.
```

**copy** [boolean, optional, default: True] If copy is False, the affinity matrix is modified inplace by the algorithm, for memory efficiency

verbose [boolean, optional, default: False] The verbosity level

**return\_n\_iter** [bool, default False] Whether or not to return the number of iterations.

#### Returns

```
cluster_centers_indices [array, shape (n_clusters,)] index of clusters centers
labels [array, shape (n_samples,)] cluster labels for each point
n_iter [int] number of iterations run. Returned only if return_n_iter is set to True.
```

## **Notes**

For an example, see examples/cluster/plot\_affinity\_propagation.py.

When the algorithm does not converge, it returns an empty array as cluster\_center\_indices and -1 as label for each training sample.

When all training samples have equal similarities and equal preferences, the assignment of cluster centers and labels depends on the preference. If the preference is smaller than the similarities, a single cluster center and label 0 for every sample will be returned. Otherwise, every training sample becomes its own cluster center and is assigned a unique label.

#### References

Brendan J. Frey and Delbert Dueck, "Clustering by Passing Messages Between Data Points", Science Feb. 2007

## Examples using sklearn.cluster.affinity\_propagation

• Visualizing the stock market structure

# sklearn.cluster.cluster\_optics\_dbscan

```
sklearn.cluster.cluster_optics_dbscan (reachability, core_distances, ordering, eps)
Performs DBSCAN extraction for an arbitrary epsilon.
```

Extracting the clusters runs in linear time. Note that this results in labels\_which are close to a *DBSCAN* with similar settings and eps, only if eps is close to max\_eps.

#### **Parameters**

```
core_distances [array, shape (n_samples,)] Distances at which points become core
  (core_distances_)
```

```
ordering [array, shape (n_samples,)] OPTICS ordered point indices (ordering_)
```

eps [float] DBSCAN eps parameter. Must be set to < max\_eps. Results will be close to DBSCAN algorithm if eps and max\_eps are close to one another.

## Returns

labels\_ [array, shape (n\_samples,)] The estimated labels.

# Examples using sklearn.cluster.cluster\_optics\_dbscan

• Demo of OPTICS clustering algorithm

# sklearn.cluster.cluster\_optics\_xi

Automatically extract clusters according to the  $\overline{X}i$ -steep method.

## **Parameters**

reachability [array, shape (n\_samples,)] Reachability distances calculated by OPTICS
 (reachability\_)

**predecessor** [array, shape (n\_samples,)] Predecessors calculated by OPTICS.

ordering [array, shape (n\_samples,)] OPTICS ordered point indices (ordering\_)

- min\_samples [int > 1 or float between 0 and 1] The same as the min\_samples given to OPTICS. Up and down steep regions can't have more then min\_samples consecutive non-steep points. Expressed as an absolute number or a fraction of the number of samples (rounded to be at least 2).
- min\_cluster\_size [int > 1 or float between 0 and 1 (default=None)] Minimum number of samples in an OPTICS cluster, expressed as an absolute number or a fraction of the number of samples (rounded to be at least 2). If None, the value of min\_samples is used instead.
- xi [float, between 0 and 1, optional (default=0.05)] Determines the minimum steepness on the reachability plot that constitutes a cluster boundary. For example, an upwards point in the reachability plot is defined by the ratio from one point to its successor being at most 1-xi.
- **predecessor\_correction** [bool, optional (default=True)] Correct clusters based on the calculated predecessors.

#### Returns

**labels** [array, shape (n\_samples)] The labels assigned to samples. Points which are not included in any cluster are labeled as -1.

clusters [array, shape (n\_clusters, 2)] The list of clusters in the form of [start, end]
 in each row, with all indices inclusive. The clusters are ordered according to (end,
 -start) (ascending) so that larger clusters encompassing smaller clusters come after such nested smaller clusters. Since labels does not reflect the hierarchy, usually
 len(clusters) > np.unique(labels).

# sklearn.cluster.compute\_optics\_graph

sklearn.cluster.compute\_optics\_graph(X, min\_samples, max\_eps, metric, p, metric\_params, algorithm, leaf size, n jobs)

Computes the OPTICS reachability graph.

Read more in the *User Guide*.

#### **Parameters**

- **X** [array, shape (n\_samples, n\_features), or (n\_samples, n\_samples) if metric='precomputed'.] A feature array, or array of distances between samples if metric='precomputed'
- min\_samples [int > 1 or float between 0 and 1] The number of samples in a neighborhood for a point to be considered as a core point. Expressed as an absolute number or a fraction of the number of samples (rounded to be at least 2).
- max\_eps [float, optional (default=np.inf)] The maximum distance between two samples for one to be considered as in the neighborhood of the other. Default value of np.inf will identify clusters across all scales; reducing max\_eps will result in shorter run times.
- **metric** [string or callable, optional (default='minkowski')] Metric to use for distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.

If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating the distance between them. This works for Scipy's metrics, but is less efficient than passing the metric name as a string. If metric is "precomputed", X is assumed to be a distance matrix and must be square.

Valid values for metric are:

- from scikit-learn: ['cityblock', 'cosine', 'euclidean', '11', '12', 'manhattan']
- from scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule']

See the documentation for scipy.spatial.distance for details on these metrics.

- **p** [integer, optional (default=2)] Parameter for the Minkowski metric from *sklearn*. *metrics.pairwise\_distances*. When p = 1, this is equivalent to using manhattan\_distance (11), and euclidean\_distance (12) for p = 2. For arbitrary p, minkowski\_distance (1\_p) is used.
- **metric\_params** [dict, optional (default=None)] Additional keyword arguments for the metric function.
- **algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] Algorithm used to compute the nearest neighbors:
  - 'ball\_tree' will use BallTree
  - 'kd tree' will use KDTree
  - 'brute' will use a brute-force search.
  - 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method. (default)

Note: fitting on sparse input will override the setting of this parameter, using brute force.

- **leaf\_size** [int, optional (default=30)] Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### Returns

- **ordering** [array, shape (n\_samples,)] The cluster ordered list of sample indices.
- **core\_distances**\_ [array, shape (n\_samples,)] Distance at which each sample becomes a core point, indexed by object order. Points which will never be core have a distance of inf. Use clust.core\_distances\_[clust.ordering\_] to access in cluster order.
- **reachability**\_ [array, shape (n\_samples,)] Reachability distances per sample, indexed by object order. Use clust.reachability\_[clust.ordering\_] to access in cluster order.
- **predecessor**\_ [array, shape (n\_samples,)] Point that a sample was reached from, indexed by object order. Seed points have a predecessor of -1.

#### References

[1]

#### sklearn.cluster.dbscan

sklearn.cluster.dbscan (X, eps=0.5,  $min_samples=5$ , metric='minkowski',  $metric\_params=None$ , algorithm='auto',  $leaf\_size=30$ , p=2,  $sample\_weight=None$ ,  $n\_jobs=None$ ) Perform DBSCAN clustering from vector array or distance matrix.

Read more in the *User Guide*.

#### **Parameters**

- X [array or sparse (CSR) matrix of shape (n\_samples, n\_features), or array of shape (n\_samples, n\_samples)] A feature array, or array of distances between samples if metric='precomputed'.
- **eps** [float, optional] The maximum distance between two samples for one to be considered as in the neighborhood of the other. This is not a maximum bound on the distances of points within a cluster. This is the most important DBSCAN parameter to choose appropriately for your data set and distance function.
- **min\_samples** [int, optional] The number of samples (or total weight) in a neighborhood for a point to be considered as a core point. This includes the point itself.
- **metric** [string, or callable] The metric to use when calculating distance between instances in a feature array. If metric is a string or callable, it must be one of the options allowed by <code>sklearn.metrics.pairwise\_distances</code> for its metric parameter. If metric is "precomputed", X is assumed to be a distance matrix and must be square. X may be a sparse matrix, in which case only "nonzero" elements may be considered neighbors for DBSCAN.
- **metric\_params** [dict, optional] Additional keyword arguments for the metric function.

New in version 0.19.

- **algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] The algorithm to be used by the NearestNeighbors module to compute pointwise distances and find nearest neighbors. See NearestNeighbors module documentation for details.
- **leaf\_size** [int, optional (default = 30)] Leaf size passed to BallTree or cKDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.
- **p** [float, optional] The power of the Minkowski metric to be used to calculate distance between points.

- **sample\_weight** [array, shape (n\_samples,), optional] Weight of each sample, such that a sample with a weight of at least min\_samples is by itself a core sample; a sample with negative weight may inhibit its eps-neighbor from being core. Note that weights are absolute, and default to 1.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### Returns

**core\_samples** [array [n\_core\_samples]] Indices of core samples.

labels [array [n\_samples]] Cluster labels for each point. Noisy samples are given the label -1.

#### See also:

**DBSCAN** An estimator interface for this clustering algorithm.

**OPTICS** A similar estimator interface clustering at multiple values of eps. Our implementation is optimized for memory usage.

## **Notes**

For an example, see examples/cluster/plot\_dbscan.py.

This implementation bulk-computes all neighborhood queries, which increases the memory complexity to O(n.d) where d is the average number of neighbors, while original DBSCAN had memory complexity O(n). It may attract a higher memory complexity when querying these nearest neighborhoods, depending on the algorithm.

One way to avoid the query complexity is to pre-compute sparse neighborhoods in chunks using <code>NearestNeighbors.radius\_neighbors\_graph</code> with <code>mode='distance'</code>, then using <code>metric='precomputed'</code> here.

Another way to reduce memory and computation time is to remove (near-)duplicate points and use sample\_weight instead.

cluster.optics provides a similar clustering with lower memory usage.

## References

Ester, M., H. P. Kriegel, J. Sander, and X. Xu, "A Density-Based Algorithm for Discovering Clusters in Large Spatial Databases with Noise". In: Proceedings of the 2nd International Conference on Knowledge Discovery and Data Mining, Portland, OR, AAAI Press, pp. 226-231. 1996

Schubert, E., Sander, J., Ester, M., Kriegel, H. P., & Xu, X. (2017). DBSCAN revisited: why and how you should (still) use DBSCAN. ACM Transactions on Database Systems (TODS), 42(3), 19.

## sklearn.cluster.estimate\_bandwidth

Estimate the bandwidth to use with the mean-shift algorithm.

That this function takes time at least quadratic in n\_samples. For large datasets, it's wise to set that parameter to a small value.

## **Parameters**

- **X** [array-like, shape=[n\_samples, n\_features]] Input points.
- **quantile** [float, default 0.3] should be between [0, 1] 0.5 means that the median of all pairwise distances is used.
- **n\_samples** [int, optional] The number of samples to use. If not given, all samples are used.
- **random\_state** [int, RandomState instance or None (default)] The generator used to randomly select the samples from input points for bandwidth estimation. Use an int to make the randomness deterministic. See *Glossary*.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

## Returns

**bandwidth** [float] The bandwidth parameter.

## Examples using sklearn.cluster.estimate bandwidth

- A demo of the mean-shift clustering algorithm
- Comparing different clustering algorithms on toy datasets

## sklearn.cluster.k means

sklearn.cluster.k\_means (X,  $n_c$ lusters, sample\_weight=None, init='k-means++', precompute\_distances='auto',  $n_c$ init=10, max\_iter=300, verbose=False, tol=0.0001, random\_state=None, copy\_x=True,  $n_c$ jobs=None, algorithm='auto', return\_ $n_c$ iter=False)

K-means clustering algorithm.

Read more in the *User Guide*.

# Parameters

- **X** [array-like or sparse matrix, shape (n\_samples, n\_features)] The observations to cluster. It must be noted that the data will be converted to C ordering, which will cause a memory copy if the given data is not C-contiguous.
- **n\_clusters** [int] The number of clusters to form as well as the number of centroids to generate.
- **sample\_weight** [array-like, shape (n\_samples,), optional] The weights for each observation in X. If None, all observations are assigned equal weight (default: None)
- init [{'k-means++', 'random', or ndarray, or a callable}, optional] Method for initialization,
   default to 'k-means++':

'k-means++': selects initial cluster centers for k-mean clustering in a smart way to speed up convergence. See section Notes in k\_init for more details.

'random': choose k observations (rows) at random from data for the initial centroids.

If an ndarray is passed, it should be of shape (n\_clusters, n\_features) and gives the initial centers.

If a callable is passed, it should take arguments X, k and and a random state and return an initialization.

**precompute\_distances** [{'auto', True, False}] Precompute distances (faster but takes more memory).

'auto': do not precompute distances if n\_samples \* n\_clusters > 12 million. This corresponds to about 100MB overhead per job using double precision.

True: always precompute distances

False: never precompute distances

**n\_init** [int, optional, default: 10] Number of time the k-means algorithm will be run with different centroid seeds. The final results will be the best output of n\_init consecutive runs in terms of inertia.

max\_iter [int, optional, default 300] Maximum number of iterations of the k-means algorithm to run.

verbose [boolean, optional] Verbosity mode.

tol [float, optional] The relative increment in the results before declaring convergence.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for centroid initialization. Use an int to make the randomness deterministic. See *Glossary*.

- copy\_x [boolean, optional] When pre-computing distances it is more numerically accurate to center the data first. If copy\_x is True (default), then the original data is not modified, ensuring X is C-contiguous. If False, the original data is modified, and put back before the function returns, but small numerical differences may be introduced by subtracting and then adding the data mean, in this case it will also not ensure that data is C-contiguous which may cause a significant slowdown.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. This works by computing each of the n\_init runs in parallel.

None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

algorithm ["auto", "full" or "elkan", default="auto"] K-means algorithm to use. The classical EM-style algorithm is "full". The "elkan" variation is more efficient by using the triangle inequality, but currently doesn't support sparse data. "auto" chooses "elkan" for dense data and "full" for sparse data.

**return\_n\_iter** [bool, optional] Whether or not to return the number of iterations.

#### Returns

**centroid** [float ndarray with shape (k, n\_features)] Centroids found at the last iteration of k-means.

**label** [integer ndarray with shape (n\_samples,)] label[i] is the code or index of the centroid the i'th observation is closest to.

**inertia** [float] The final value of the inertia criterion (sum of squared distances to the closest centroid for all observations in the training set).

**best\_n\_iter** [int] Number of iterations corresponding to the best results. Returned only if return\_n\_iter is set to True.

## sklearn.cluster.mean shift

 $sklearn.cluster.\textbf{mean\_shift} (X, bandwidth=None, seeds=None, bin\_seeding=False, \\ min\_bin\_freq=1, cluster\_all=True, max\_iter=300, n\_jobs=None) \\ Perform mean shift clustering of data using a flat kernel.$ 

Read more in the User Guide.

#### **Parameters**

**X** [array-like, shape=[n\_samples, n\_features]] Input data.

bandwidth [float, optional] Kernel bandwidth.

If bandwidth is not given, it is determined using a heuristic based on the median of all pairwise distances. This will take quadratic time in the number of samples. The sklearn.cluster.estimate\_bandwidth function can be used to do this more efficiently.

- **seeds** [array-like, shape=[n\_seeds, n\_features] or None] Point used as initial kernel locations. If None and bin\_seeding=False, each data point is used as a seed. If None and bin\_seeding=True, see bin\_seeding.
- **bin\_seeding** [boolean, default=False] If true, initial kernel locations are not locations of all points, but rather the location of the discretized version of points, where points are binned onto a grid whose coarseness corresponds to the bandwidth. Setting this option to True will speed up the algorithm because fewer seeds will be initialized. Ignored if seeds argument is not None.
- **min\_bin\_freq** [int, default=1] To speed up the algorithm, accept only those bins with at least min\_bin\_freq points as seeds.
- **cluster\_all** [boolean, default True] If true, then all points are clustered, even those orphans that are not within any kernel. Orphans are assigned to the nearest kernel. If false, then orphans are given cluster label -1.
- **max\_iter** [int, default 300] Maximum number of iterations, per seed point before the clustering operation terminates (for that seed point), if has not converged yet.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. This works by computing each of the n\_init runs in parallel.

None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

New in version 0.17: Parallel Execution using  $n_{jobs}$ .

## Returns

**cluster\_centers** [array, shape=[n\_clusters, n\_features]] Coordinates of cluster centers.

**labels** [array, shape=[n\_samples]] Cluster labels for each point.

# **Notes**

For an example, see examples/cluster/plot\_mean\_shift.py.

## sklearn.cluster.spectral clustering

```
sklearn.cluster.spectral_clustering (affinity, n\_clusters=8, n\_components=None, eigen\_solver=None, random\_state=None, n\_init=10, eigen\_tol=0.0, assign\_labels='kmeans')
```

Apply clustering to a projection of the normalized Laplacian.

In practice Spectral Clustering is very useful when the structure of the individual clusters is highly non-convex or more generally when a measure of the center and spread of the cluster is not a suitable description of the complete cluster. For instance, when clusters are nested circles on the 2D plane.

If affinity is the adjacency matrix of a graph, this method can be used to find normalized graph cuts.

Read more in the User Guide.

#### **Parameters**

**affinity** [array-like or sparse matrix, shape: (n\_samples, n\_samples)] The affinity matrix describing the relationship of the samples to embed. **Must be symmetric**.

# Possible examples:

- · adjacency matrix of a graph,
- heat kernel of the pairwise distance matrix of the samples,
- symmetric k-nearest neighbours connectivity matrix of the samples.
- **n\_clusters** [integer, optional] Number of clusters to extract.
- **n\_components** [integer, optional, default is n\_clusters] Number of eigen vectors to use for the spectral embedding
- eigen\_solver [{None, 'arpack', 'lobpcg', or 'amg'}] The eigenvalue decomposition strategy to use. AMG requires pyamg to be installed. It can be faster on very large, sparse problems, but may also lead to instabilities
- random\_state [int, RandomState instance or None (default)] A pseudo random number generator used for the initialization of the lobpcg eigen vectors decomposition when eigen\_solver == 'amg' and by the K-Means initialization. Use an int to make the randomness deterministic. See *Glossary*.
- **n\_init** [int, optional, default: 10] Number of time the k-means algorithm will be run with different centroid seeds. The final results will be the best output of n\_init consecutive runs in terms of inertia.
- **eigen\_tol** [float, optional, default: 0.0] Stopping criterion for eigendecomposition of the Laplacian matrix when using arpack eigen\_solver.
- assign\_labels [{'kmeans', 'discretize'}, default: 'kmeans'] The strategy to use to assign labels in the embedding space. There are two ways to assign labels after the laplacian embedding. k-means can be applied and is a popular choice. But it can also be sensitive to initialization. Discretization is another approach which is less sensitive to random initialization. See the 'Multiclass spectral clustering' paper referenced below for more details on the discretization approach.

#### Returns

**labels** [array of integers, shape: n samples] The labels of the clusters.

## **Notes**

The graph should contain only one connect component, elsewhere the results make little sense.

This algorithm solves the normalized cut for k=2: it is a normalized spectral clustering.

## References

- Normalized cuts and image segmentation, 2000 Jianbo Shi, Jitendra Malik http://citeseer.ist.psu.edu/ viewdoc/summary?doi=10.1.1.160.2324
- A Tutorial on Spectral Clustering, 2007 Ulrike von Luxburg http://citeseerx.ist.psu.edu/viewdoc/ summary?doi=10.1.1.165.9323
- Multiclass spectral clustering, 2003 Stella X. Yu, Jianbo Shi https://www1.icsi.berkeley.edu/~stellayu/publication/doc/2003kwayICCV.pdf

## Examples using sklearn.cluster.spectral\_clustering

- Segmenting the picture of greek coins in regions
- Spectral clustering for image segmentation

## sklearn.cluster.ward tree

sklearn.cluster.ward\_tree(X, connectivity=None, n\_clusters=None, return\_distance=False) Ward clustering based on a Feature matrix.

Recursively merges the pair of clusters that minimally increases within-cluster variance.

The inertia matrix uses a Heapq-based representation.

This is the structured version, that takes into account some topological structure between samples.

Read more in the *User Guide*.

## **Parameters**

- X [array, shape (n\_samples, n\_features)] feature matrix representing n\_samples samples to be clustered
- **connectivity** [sparse matrix (optional).] connectivity matrix. Defines for each sample the neighboring samples following a given structure of the data. The matrix is assumed to be symmetric and only the upper triangular half is used. Default is None, i.e, the Ward algorithm is unstructured.
- n\_clusters [int (optional)] Stop early the construction of the tree at n\_clusters. This is useful to decrease computation time if the number of clusters is not small compared to the number of samples. In this case, the complete tree is not computed, thus the 'children' output is of limited use, and the 'parents' output should rather be used. This option is valid only when specifying a connectivity matrix.

**return\_distance** [bool (optional)] If True, return the distance between the clusters.

# Returns

**children** [2D array, shape (n\_nodes-1, 2)] The children of each non-leaf node. Values less than *n\_samples* correspond to leaves of the tree which are the original samples. A node i greater than or equal to *n\_samples* is a non-leaf node and has children children\_[i - n\_samples]. Alternatively at the i-th iteration, children[i][0] and children[i][1] are merged to form node n\_samples + i

**n\_connected\_components** [int] The number of connected components in the graph.

**n leaves** [int] The number of leaves in the tree

**parents** [1D array, shape (n\_nodes, ) or None] The parent of each node. Only returned when a connectivity matrix is specified, elsewhere 'None' is returned.

distances [1D array, shape (n\_nodes-1, )] Only returned if return\_distance is set to True (for compatibility). The distances between the centers of the nodes. distances[i] corresponds to a weighted euclidean distance between the nodes children[i, 1] and children[i, 2]. If the nodes refer to leaves of the tree, then distances[i] is their unweighted euclidean distance. Distances are updated in the following way (from scipy.hierarchy.linkage):

The new entry d(u, v) is computed as follows,

$$d(u,v) = \sqrt{\frac{|v| + |s|}{T}d(v,s)^2 + \frac{|v| + |t|}{T}d(v,t)^2 - \frac{|v|}{T}d(s,t)^2}$$

where u is the newly joined cluster consisting of clusters s and t, v is an unused cluster in the forest, T = |v| + |s| + |t|, and |\*| is the cardinality of its argument. This is also known as the incremental algorithm.

# 6.4 sklearn.cluster.bicluster: Biclustering

Spectral biclustering algorithms.

Authors: Kemal Eren License: BSD 3 clause

**User guide:** See the *Biclustering* section for further details.

# 6.4.1 Classes

SpectralBiclustering([n_clusters, method,])	Spectral biclustering (Kluger, 2003).
SpectralCoclustering([n_clusters,])	Spectral Co-Clustering algorithm (Dhillon, 2001).

## sklearn.cluster.bicluster.SpectralBiclustering

```
 \begin{array}{lll} \textbf{class} & \textbf{sklearn.cluster.bicluster.SpectralBiclustering} \ (\textit{n\_clusters=3}, \\ & \textit{method='bistochastic'}, \\ & \textit{n\_components=6}, & \textit{n\_best=3}, \\ & \textit{svd\_method='randomized'}, \\ & \textit{n\_svd\_vecs=None}, \\ & \textit{mini\_batch=False}, & \textit{init='k-means++'}, & \textit{n\_init=10}, \\ & \textit{n\_jobs=None}, & \textit{random_state=None}) \end{array}
```

Spectral biclustering (Kluger, 2003).

Partitions rows and columns under the assumption that the data has an underlying checkerboard structure. For instance, if there are two row partitions and three column partitions, each row will belong to three biclusters, and each column will belong to two biclusters. The outer product of the corresponding row and column label vectors gives this checkerboard structure.

Read more in the *User Guide*.

#### **Parameters**

- n\_clusters [integer or tuple (n\_row\_clusters, n\_column\_clusters)] The number of row and column clusters in the checkerboard structure.
- method [string, optional, default: 'bistochastic'] Method of normalizing and converting singular vectors into biclusters. May be one of 'scale', 'bistochastic', or 'log'. The authors recommend using 'log'. If the data is sparse, however, log normalization will not work, which is why the default is 'bistochastic'. CAUTION: if method='log', the data must not be sparse.
- **n\_components** [integer, optional, default: 6] Number of singular vectors to check.
- **n\_best** [integer, optional, default: 3] Number of best singular vectors to which to project the data for clustering.
- svd\_method [string, optional, default: 'randomized'] Selects the algorithm for finding singular vectors. May be 'randomized' or 'arpack'. If 'randomized', uses sklearn.utils.extmath.randomized\_svd, which may be faster for large matrices. If 'arpack', uses scipy.sparse.linalg.svds, which is more accurate, but possibly slower in some cases.
- **mini\_batch** [bool, optional, default: False] Whether to use mini-batch k-means, which is faster but may get different results.
- init [{'k-means++', 'random' or an ndarray}] Method for initialization of k-means algorithm;
   defaults to 'k-means++'.
- **n\_init** [int, optional, default: 10] Number of random initializations that are tried with the k-means algorithm.
  - If mini-batch k-means is used, the best initialization is chosen and the algorithm runs once. Otherwise, the algorithm is run for each initialization and the best solution chosen.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. This works by breaking down the pairwise matrix into n\_jobs even slices and computing them in parallel.
  - None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- **random\_state** [int, RandomState instance or None (default)] Used for randomizing the singular value decomposition and the k-means initialization. Use an int to make the randomness deterministic. See *Glossary*.

# Attributes

- rows\_ [array-like, shape (n\_row\_clusters, n\_rows)] Results of the clustering. rows[i, r] is True if cluster i contains row r. Available only after calling fit.
- **columns**\_ [array-like, shape (n\_column\_clusters, n\_columns)] Results of the clustering, like rows.

```
row_labels_ [array-like, shape (n_rows,)] Row partition labels.column_labels_ [array-like, shape (n_cols,)] Column partition labels.
```

## References

• Kluger, Yuval, et. al., 2003. Spectral biclustering of microarray data: coclustering genes and conditions.

# **Examples**

## **Methods**

fit(self, X[, y])	Creates a biclustering for X.
get_indices(self, i)	Row and column indices of the i'th bicluster.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_shape(self, i)	Shape of the i'th bicluster.
<pre>get_submatrix(self, i, data)</pre>	Returns the submatrix corresponding to bicluster i.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__(self, n_clusters=3, method='bistochastic', n_components=6, n_best=3, svd_method='randomized', n_svd_vecs=None, mini_batch=False, init='k-means++', n_init=10, n_jobs=None, random_state=None)
```

# biclusters\_

Convenient way to get row and column indicators together.

Returns the rows\_and columns\_members.

## **fit** (*self*, *X*, *y*=*None*)

Creates a biclustering for X.

# **Parameters**

```
\mathbf{X} [array-like, shape (n_samples, n_features)]
```

y [Ignored]

#### get indices (self, i)

Row and column indices of the i'th bicluster.

Only works if rows\_ and columns\_ attributes exist.

#### **Parameters**

i [int] The index of the cluster.

## Returns

row\_ind [np.array, dtype=np.intp] Indices of rows in the dataset that belong to the bicluster.

col\_ind [np.array, dtype=np.intp] Indices of columns in the dataset that belong to the bicluster.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# get\_shape (self, i)

Shape of the i'th bicluster.

#### **Parameters**

i [int] The index of the cluster.

#### Returns

**shape** [(int, int)] Number of rows and columns (resp.) in the bicluster.

# get\_submatrix(self, i, data)

Returns the submatrix corresponding to bicluster i.

#### **Parameters**

```
i [int] The index of the cluster.
```

```
data [array] The data.
```

## Returns

submatrix [array] The submatrix corresponding to bicluster i.

## Notes

Works with sparse matrices. Only works if rows\_ and columns\_ attributes exist.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

#### sklearn.cluster.bicluster.SpectralCoclustering

```
 \begin{array}{llll} \textbf{class} & \textbf{sklearn.cluster.bicluster.SpectralCoclustering} & (n\_clusters=3, & svd\_method='randomized', & n\_svd\_vecs=None, & mini\_batch=False, & init='k-means++', & n\_init=10, & n\_jobs=None, & random\_state=None) \end{array}
```

Spectral Co-Clustering algorithm (Dhillon, 2001).

Clusters rows and columns of an array X to solve the relaxed normalized cut of the bipartite graph created from X as follows: the edge between row vertex  $\dot{\mathbf{1}}$  and column vertex  $\dot{\mathbf{1}}$  has weight  $X[\dot{\mathbf{1}}, \dot{\mathbf{1}}]$ .

The resulting bicluster structure is block-diagonal, since each row and each column belongs to exactly one bicluster.

Supports sparse matrices, as long as they are nonnegative.

Read more in the User Guide.

#### **Parameters**

- **n\_clusters** [integer, optional, default: 3] The number of biclusters to find.
- svd\_method [string, optional, default: 'randomized'] Selects the algorithm for finding singular vectors. May be 'randomized' or 'arpack'. If 'randomized', use sklearn.utils.extmath.randomized\_svd, which may be faster for large matrices. If 'arpack', use scipy.sparse.linalg.svds, which is more accurate, but possibly slower in some cases.
- **mini\_batch** [bool, optional, default: False] Whether to use mini-batch k-means, which is faster but may get different results.
- init [{'k-means++', 'random' or an ndarray}] Method for initialization of k-means algorithm;
   defaults to 'k-means++'.
- **n\_init** [int, optional, default: 10] Number of random initializations that are tried with the k-means algorithm.
  - If mini-batch k-means is used, the best initialization is chosen and the algorithm runs once. Otherwise, the algorithm is run for each initialization and the best solution chosen.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. This works by breaking down the pairwise matrix into n\_jobs even slices and computing them in parallel.
  - None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- **random\_state** [int, RandomState instance or None (default)] Used for randomizing the singular value decomposition and the k-means initialization. Use an int to make the randomness deterministic. See *Glossary*.

## **Attributes**

rows\_ [array-like, shape (n\_row\_clusters, n\_rows)] Results of the clustering. rows[i, r] is True if cluster i contains row r. Available only after calling fit.

```
columns_ [array-like, shape (n_column_clusters, n_columns)] Results of the clustering, like rows.row_labels_ [array-like, shape (n_rows,)] The bicluster label of each row.
```

**column\_labels\_** [array-like, shape (n\_cols,)] The bicluster label of each column.

## References

• Dhillon, Inderjit S, 2001. Co-clustering documents and words using bipartite spectral graph partitioning.

# **Examples**

# **Methods**

fit(self, X[, y])	Creates a biclustering for X.
<pre>get_indices(self, i)</pre>	Row and column indices of the i'th bicluster.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_shape(self, i)	Shape of the i'th bicluster.
<pre>get_submatrix(self, i, data)</pre>	Returns the submatrix corresponding to bicluster i.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__(self, n_clusters=3, svd_method='randomized', n_svd_vecs=None, mini_batch=False, init='k-means++', n_init=10, n_jobs=None, random_state=None)
```

## biclusters\_

Convenient way to get row and column indicators together.

Returns the rows\_and columns\_members.

# fit (self, X, y=None)

Creates a biclustering for X.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

y [Ignored]

# get\_indices (self, i)

Row and column indices of the i'th bicluster.

Only works if rows\_ and columns\_ attributes exist.

#### **Parameters**

i [int] The index of the cluster.

## Returns

row\_ind [np.array, dtype=np.intp] Indices of rows in the dataset that belong to the bicluster.

col\_ind [np.array, dtype=np.intp] Indices of columns in the dataset that belong to the bicluster.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

# get\_shape (self, i)

Shape of the i'th bicluster.

## **Parameters**

i [int] The index of the cluster.

#### Returns

**shape** [(int, int)] Number of rows and columns (resp.) in the bicluster.

# get\_submatrix(self, i, data)

Returns the submatrix corresponding to bicluster i.

#### **Parameters**

```
i [int] The index of the cluster.
```

data [array] The data.

## Returns

submatrix [array] The submatrix corresponding to bicluster i.

## Notes

Works with sparse matrices. Only works if rows\_ and columns\_ attributes exist.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# 6.5 sklearn.compose: Composite Estimators

Meta-estimators for building composite models with transformers

In addition to its current contents, this module will eventually be home to refurbished versions of Pipeline and FeatureUnion.

**User guide:** See the *Pipelines and composite estimators* section for further details.

compose.ColumnTransformer(transformers[,])	Applies transformers to columns of an array or pandas DataFrame.
${\it compose.TransformedTargetRegressor}([\dots])$	Meta-estimator to regress on a transformed target.

# 6.5.1 sklearn.compose.ColumnTransformer

Applies transformers to columns of an array or pandas DataFrame.

This estimator allows different columns or column subsets of the input to be transformed separately and the features generated by each transformer will be concatenated to form a single feature space. This is useful for heterogeneous or columnar data, to combine several feature extraction mechanisms or transformations into a single transformer.

Read more in the *User Guide*.

New in version 0.20.

#### **Parameters**

**transformers** [list of tuples] List of (name, transformer, column(s)) tuples specifying the transformer objects to be applied to subsets of the data.

**name** [string] Like in Pipeline and FeatureUnion, this allows the transformer and its parameters to be set using set\_params and searched in grid search.

**transformer** [estimator or {'passthrough', 'drop'}] Estimator must support fit and transform. Special-cased strings 'drop' and 'passthrough' are accepted as well, to indicate to drop the columns or to pass them through untransformed, respectively.

**column(s)** [string or int, array-like of string or int, slice, boolean mask array or callable] Indexes the data on its second axis. Integers are interpreted as positional columns, while strings can reference DataFrame columns by name. A scalar string or int should be used where transformer expects X to be a 1d array-like (vector), otherwise a 2d array will be passed to the transformer. A callable is passed the input data X and can return any of the above.

remainder [{'drop', 'passthrough'} or estimator, default 'drop'] By default, only the specified columns in *transformers* are transformed and combined in the output, and the non-specified columns are dropped. (default of 'drop'). By specifying remainder='passthrough', all remaining columns that were not specified in *transformers* will be automatically passed through. This subset of columns is concatenated with the output of the transformers. By setting remainder to be an estimator, the remaining non-specified columns will use the remainder estimator. The estimator must support *fit* and *transform*. Note that using this feature requires that the DataFrame columns input at *fit* and *transform* have identical order.

- **sparse\_threshold** [float, default = 0.3] If the output of the different transformers contains sparse matrices, these will be stacked as a sparse matrix if the overall density is lower than this value. Use <code>sparse\_threshold=0</code> to always return dense. When the transformed output consists of all dense data, the stacked result will be dense, and this keyword will be ignored.
- **n\_jobs** [int or None, optional (default=None)] Number of jobs to run in parallel. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- **transformer\_weights** [dict, optional] Multiplicative weights for features per transformer. The output of the transformer is multiplied by these weights. Keys are transformer names, values the weights.
- **verbose** [boolean, optional(default=False)] If True, the time elapsed while fitting each transformer will be printed as it is completed.

## **Attributes**

transformers\_ [list] The collection of fitted transformers as tuples of (name, fitted\_transformer, column). fitted\_transformer can be an estimator, 'drop', or 'passthrough'. In case there were no columns selected, this will be the unfitted transformer. If there are remaining columns, the final element is a tuple of the form: ('remainder', transformer, remaining\_columns) corresponding to the remainder parameter. If there are remaining columns, then len(transformers\_) ==len(transformers)+1, otherwise len(transformers\_) ==len(transformers).

**named\_transformers\_** [Bunch object, a dictionary with attribute access] Access the fitted transformer by name.

**sparse\_output\_** [boolean] Boolean flag indicating wether the output of transform is a sparse matrix or a dense numpy array, which depends on the output of the individual transformers and the sparse\_threshold keyword.

#### See also:

**sklearn.compose.make\_column\_transformer** convenience function for combining the outputs of multiple transformer objects applied to column subsets of the original feature space.

## **Notes**

The order of the columns in the transformed feature matrix follows the order of how the columns are specified in the *transformers* list. Columns of the original feature matrix that are not specified are dropped from the resulting transformed feature matrix, unless specified in the passthrough keyword. Those columns specified with passthrough are added at the right to the output of the transformers.

## **Examples**

## **Methods**

fit(self, X[, y])	Fit all transformers using X.
<pre>fit_transform(self, X[, y])</pre>	Fit all transformers, transform the data and concatenate
	results.
get_feature_names(self)	Get feature names from all transformers.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*kwargs)</pre>	Set the parameters of this estimator.
transform(self, X)	Transform X separately by each transformer, concate-
	nate results.

```
__init__(self, transformers, remainder='drop', sparse_threshold=0.3, n_jobs=None, transformer_weights=None, verbose=False)
```

## **fit** (self, X, y=None)

Fit all transformers using X.

## **Parameters**

- **X** [array-like or DataFrame of shape [n\_samples, n\_features]] Input data, of which specified subsets are used to fit the transformers.
- y [array-like, shape (n\_samples, ...), optional] Targets for supervised learning.

# Returns

**self** [ColumnTransformer] This estimator

# fit\_transform(self, X, y=None)

Fit all transformers, transform the data and concatenate results.

## **Parameters**

- **X** [array-like or DataFrame of shape [n\_samples, n\_features]] Input data, of which specified subsets are used to fit the transformers.
- y [array-like, shape (n\_samples, ...), optional] Targets for supervised learning.

# Returns

**X\_t** [array-like or sparse matrix, shape (n\_samples, sum\_n\_components)] hstack of results of transformers. sum\_n\_components is the sum of n\_components (output dimension) over transformers. If any result is a sparse matrix, everything will be converted to sparse matrices.

# get\_feature\_names (self)

Get feature names from all transformers.

# Returns

**feature\_names** [list of strings] Names of the features produced by transform.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## named\_transformers\_

Access the fitted transformer by name.

Read-only attribute to access any transformer by given name. Keys are transformer names and values are the fitted transformer objects.

```
set_params (self, **kwargs)
```

Set the parameters of this estimator.

Valid parameter keys can be listed with get\_params().

#### Returns

self

## transform(self, X)

Transform X separately by each transformer, concatenate results.

#### **Parameters**

**X** [array-like or DataFrame of shape [n\_samples, n\_features]] The data to be transformed by subset.

# Returns

X\_t [array-like or sparse matrix, shape (n\_samples, sum\_n\_components)] hstack of results of transformers. sum\_n\_components is the sum of n\_components (output dimension) over transformers. If any result is a sparse matrix, everything will be converted to sparse matrices.

## Examples using sklearn.compose.ColumnTransformer

- Column Transformer with Mixed Types
- Column Transformer with Heterogeneous Data Sources

# 6.5.2 sklearn.compose.TransformedTargetRegressor

```
 \begin{array}{lll} \textbf{class} & \texttt{sklearn.compose.TransformedTargetRegressor} (\textit{regressor=None}, & \textit{transformer=None}, \\ & \textit{func=None}, & \textit{inverse\_func=None}, \\ & \textit{check\_inverse=True}) \end{array}
```

Meta-estimator to regress on a transformed target.

Useful for applying a non-linear transformation in regression problems. This transformation can be given as a Transformer such as the QuantileTransformer or as a function and its inverse such as log and exp.

The computation during fit is:

```
regressor.fit(X, func(y))
```

or:

```
regressor.fit(X, transformer.transform(y))
```

The computation during predict is:

```
inverse_func(regressor.predict(X))
```

or:

```
transformer.inverse_transform(regressor.predict(X))
```

Read more in the *User Guide*.

#### **Parameters**

**regressor** [object, default=LinearRegression()] Regressor object such as derived from RegressorMixin. This regressor will automatically be cloned each time prior to fitting.

transformer [object, default=None] Estimator object such as derived from TransformerMixin. Cannot be set at the same time as func and inverse\_func. If transformer is None as well as func and inverse\_func, the transformer will be an identity transformer. Note that the transformer will be cloned during fitting. Also, the transformer is restricting y to be a numpy array.

**func** [function, optional] Function to apply to y before passing to fit. Cannot be set at the same time as transformer. The function needs to return a 2-dimensional array. If func is None, the function used will be the identity function.

inverse\_func [function, optional] Function to apply to the prediction of the regressor. Cannot be set at the same time as transformer as well. The function needs to return a 2-dimensional array. The inverse function is used to return predictions to the same space of the original training labels.

check\_inverse [bool, default=True] Whether to check that transform followed by inverse\_transform or func followed by inverse\_func leads to the original tar-gets.

#### **Attributes**

**regressor**\_ [object] Fitted regressor.

transformer\_ [object] Transformer used in fit and predict.

## Notes

Internally, the target y is always converted into a 2-dimensional array to be used by scikit-learn transformers. At the time of prediction, the output will be reshaped to a have the same number of dimensions as y.

See examples/compose/plot\_transformed\_target.py.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.linear_model import LinearRegression
>>> from sklearn.compose import TransformedTargetRegressor
>>> tt = TransformedTargetRegressor(regressor=LinearRegression(),
... func=np.log, inverse_func=np.exp)
```

```
>>> X = np.arange(4).reshape(-1, 1)
>>> y = np.exp(2 * X).ravel()
>>> tt.fit(X, y)
TransformedTargetRegressor(...)
>>> tt.score(X, y)
1.0
>>> tt.regressor_.coef_
array([2.])
```

## **Methods**

<pre>fit(self, X, y[, sample_weight])</pre>	Fit the model according to the given training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the base regressor, applying inverse.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, regressor=None, transformer=None, func=None, inverse_func=None, check_inverse=True)
```

fit (self, X, y, sample\_weight=None)

Fit the model according to the given training data.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training vector, where n\_samples is the number of samples and n\_features is the number of features.

y [array-like, shape (n\_samples,)] Target values.

**sample\_weight** [array-like, shape (n\_samples,) optional] Array of weights that are assigned to individual samples. If not provided, then each sample is given unit weight.

## Returns

self [object]

 $\verb"get_params" (self, deep=True")$ 

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

# predict (self, X)

Predict using the base regressor, applying inverse.

The regressor is used to predict and the inverse\_func or inverse\_transform is applied before returning the prediction.

# **Parameters**

**X** [{array-like, sparse matrix}, shape = (n\_samples, n\_features)] Samples.

## Returns

**y\_hat** [array, shape = (n\_samples,)] Predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

## **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape =  $(n_samples)$  or  $(n_samples, n_outputs)$ ] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### **Returns**

self

# Examples using sklearn.compose.TransformedTargetRegressor

• Effect of transforming the targets in regression model

compose.make\_column\_transformer(...) Construct a ColumnTransformer from the given transformers.

# 6.5.3 sklearn.compose.make column transformer

sklearn.compose.make\_column\_transformer(\*transformers, \*\*kwargs)

Construct a ColumnTransformer from the given transformers.

This is a shorthand for the ColumnTransformer constructor; it does not require, and does not permit, naming the transformers. Instead, they will be given names automatically based on their types. It also does not allow weighting with transformer\_weights.

## **Parameters**

\*transformers [tuples of transformers and column selections]

remainder [{'drop', 'passthrough'} or estimator, default 'drop'] By default, only the specified columns in *transformers* are transformed and combined in the output, and the non-specified columns are dropped. (default of 'drop'). By specifying remainder='passthrough', all remaining columns that were not specified in *transformers* will be automatically passed through. This subset of columns is concatenated with the output of the transformers. By setting remainder to be an estimator, the remaining non-specified columns will use the remainder estimator. The estimator must support *fit* and *transform*.

sparse\_threshold [float, default = 0.3] If the transformed output consists of a mix of sparse and dense data, it will be stacked as a sparse matrix if the density is lower than this value. Use sparse\_threshold=0 to always return dense. When the transformed output consists of all sparse or all dense data, the stacked result will be sparse or dense, respectively, and this keyword will be ignored.

**n\_jobs** [int or None, optional (default=None)] Number of jobs to run in parallel. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

**verbose** [boolean, optional(default=False)] If True, the time elapsed while fitting each transformer will be printed as it is completed.

#### Returns

**ct** [ColumnTransformer]

#### See also:

**sklearn.compose.ColumnTransformer** Class that allows combining the outputs of multiple transformer objects used on column subsets of the data into a single feature space.

## **Examples**

# 6.6 sklearn.covariance: Covariance Estimators

The sklearn.covariance module includes methods and algorithms to robustly estimate the covariance of features given a set of points. The precision matrix defined as the inverse of the covariance is also estimated. Covariance estimation is closely related to the theory of Gaussian Graphical Models.

User guide: See the *Covariance estimation* section for further details.

covariance.EmpiricalCovariance([])	Maximum likelihood covariance estimator
covariance.EllipticEnvelope([])	An object for detecting outliers in a Gaussian distributed
	dataset.
covariance.GraphicalLasso([alpha, mode,])	Sparse inverse covariance estimation with an 11-penalized
	estimator.
covariance.GraphicalLassoCV([alphas,])	Sparse inverse covariance w/ cross-validated choice of the
	11 penalty.
covariance.LedoitWolf([store_precision,])	LedoitWolf Estimator
covariance.MinCovDet([store_precision,])	Minimum Covariance Determinant (MCD): robust estima-
	tor of covariance.
covariance.OAS([store_precision,])	Oracle Approximating Shrinkage Estimator
covariance.ShrunkCovariance([])	Covariance estimator with shrinkage

# 6.6.1 sklearn.covariance.EmpiricalCovariance

Maximum likelihood covariance estimator

Read more in the User Guide.

# **Parameters**

store\_precision [bool] Specifies if the estimated precision is stored.

**assume\_centered** [bool] If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False (default), data are centered before computation.

# Attributes

```
    location_ [array-like, shape (n_features,)] Estimated location, i.e. the estimated mean.
    covariance_ [2D ndarray, shape (n_features, n_features)] Estimated covariance matrix
    precision_ [2D ndarray, shape (n_features, n_features)] Estimated pseudo-inverse matrix. (stored only if store_precision is True)
```

# **Examples**

```
cov=real_cov,
size=500)

>>> cov = EmpiricalCovariance().fit(X)

>>> cov.covariance_
array([[0.7569..., 0.2818...],
        [0.2818..., 0.3928...]])

>>> cov.location_
array([[0.0622..., 0.0193...])
```

### **Methods**

error_norm(self, comp_cov[, norm, scaling,])	Computes the Mean Squared Error between two covari-
	ance estimators.
fit(self, X[, y])	Fits the Maximum Likelihood Estimator covariance
	model according to the given training data and parame-
	ters.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Getter for the precision matrix.
mahalanobis(self, X)	Computes the squared Mahalanobis distances of given
	observations.
score(self, X_test[, y])	Computes the log-likelihood of a Gaussian data set with
	self.covariance_ as an estimator of its covari-
	ance matrix.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
___init__(self, store_precision=True, assume_centered=False)
```

error\_norm(self, comp\_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

## **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

**norm** [str] The type of norm used to compute the error. Available error types: - 'frobenius' (default):  $sqrt(tr(A^t.A))$  - 'spectral':  $sqrt(max(eigenvalues(A^t.A)))$  where A is the error (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

**squared** [bool] Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

## Returns

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp\_cov covariance estimators.

# fit (self, X, y=None)

Fits the Maximum Likelihood Estimator covariance model according to the given training data and parameters.

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Training data, where n\_samples is the number of samples and n\_features is the number of features.

y not used, present for API consistence purpose.

#### Returns

self [object]

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## get\_precision(self)

Getter for the precision matrix.

#### Returns

precision\_ [array-like] The precision matrix associated to the current covariance object.

# mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

#### Returns

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

```
score (self, X_test, y=None)
```

Computes the log-likelihood of a Gaussian data set with self.covariance\_ as an estimator of its covariance matrix.

## **Parameters**

**X\_test** [array-like, shape = [n\_samples, n\_features]] Test data of which we compute the likelihood, where n\_samples is the number of samples and n\_features is the number of features. X\_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y not used, present for API consistence purpose.

## Returns

res [float] The likelihood of the data set with self.covariance\_as an estimator of its covariance matrix.

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# Examples using sklearn.covariance.EmpiricalCovariance

- Robust covariance estimation and Mahalanobis distances relevance
- Robust vs Empirical covariance estimate

# 6.6.2 sklearn.covariance.EllipticEnvelope

 $\begin{array}{ll} \textbf{class} \text{ sklearn.covariance.} \textbf{EllipticEnvelope} (\textit{store\_precision=True}, & \textit{assume\_centered=False}, \\ \textit{support\_fraction=None}, & \textit{contamination=0.1}, \\ \textit{random\_state=None}) \end{array}$ 

An object for detecting outliers in a Gaussian distributed dataset.

Read more in the User Guide.

#### **Parameters**

store\_precision [boolean, optional (default=True)] Specify if the estimated precision is stored.

- assume\_centered [boolean, optional (default=False)] If True, the support of robust location and covariance estimates is computed, and a covariance estimate is recomputed from it, without centering the data. Useful to work with data whose mean is significantly equal to zero but is not exactly zero. If False, the robust location and covariance are directly computed with the FastMCD algorithm without additional treatment.
- support\_fraction [float in (0., 1.), optional (default=None)] The proportion of points to be included in the support of the raw MCD estimate. If None, the minimum value of support\_fraction will be used within the algorithm: [n\_sample + n\_features + 1]
  / 2.
- **contamination** [float in (0., 0.5), optional (default=0.1)] The amount of contamination of the data set, i.e. the proportion of outliers in the data set.
- random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### Attributes

**location**\_ [array-like, shape (n\_features,)] Estimated robust location

**covariance** [array-like, shape (n features, n features)] Estimated robust covariance matrix

**precision**\_ [array-like, shape (n\_features, n\_features)] Estimated pseudo inverse matrix. (stored only if store\_precision is True)

- **support**\_ [array-like, shape (n\_samples,)] A mask of the observations that have been used to compute the robust estimates of location and shape.
- **offset**\_ [float] Offset used to define the decision function from the raw scores. We have the relation: decision\_function = score\_samples offset\_. The offset depends on the contamination parameter and is defined in such a way we obtain the expected number of outliers (samples with decision function < 0) in training.

See also:

### EmpiricalCovariance, MinCovDet

### **Notes**

Outlier detection from covariance estimation may break or not perform well in high-dimensional settings. In particular, one will always take care to work with  $n_{samples} > n_{features} ** 2$ .

### References

[R68ae096da0e4-1]

# **Examples**

```
>>> import numpy as np
>>> from sklearn.covariance import EllipticEnvelope
>>> true_cov = np.array([[.8, .3],
                        [.3, .4]])
>>> X = np.random.RandomState(0).multivariate_normal(mean=[0, 0],
                                                     cov=true_cov,
                                                     size=500)
>>> cov = EllipticEnvelope(random_state=0).fit(X)
>>> # predict returns 1 for an inlier and -1 for an outlier
>>> cov.predict([[0, 0],
                 [3, 3]])
array([ 1, -1])
>>> cov.covariance_
array([[0.7411..., 0.2535...],
      [0.2535..., 0.3053...]])
>>> cov.location_
array([0.0813..., 0.0427...])
```

# **Methods**

Apply a correction to raw Minimum Covariance Deter-
minant estimates.
Compute the decision function of the given observa-
tions.
Computes the Mean Squared Error between two covari-
ance estimators.
Fit the EllipticEnvelope model.
Performs fit on X and returns labels for X.
Get parameters for this estimator.
Getter for the precision matrix.
Computes the squared Mahalanobis distances of given
observations.
Predict the labels (1 inlier, -1 outlier) of X according to
the fitted model.
Re-weight raw Minimum Covariance Determinant esti-
mates.
Continued on next page

Table 6.34 - continued from previous page

score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
score_samples(self, X)	Compute the negative Mahalanobis distances.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_(self, store\_precision=True, assume\_centered=False, support\_fraction=None, contamination=0.1, random\_state=None)

# correct\_covariance (self, data)

Apply a correction to raw Minimum Covariance Determinant estimates.

Correction using the empirical correction factor suggested by Rousseeuw and Van Driessen in [RVD].

### **Parameters**

**data** [array-like, shape (n\_samples, n\_features)] The data matrix, with p features and n samples. The data set must be the one which was used to compute the raw estimates.

#### **Returns**

covariance\_corrected [array-like, shape (n\_features, n\_features)] Corrected robust covariance estimate.

#### References

[RVD]

# decision\_function(self, X, raw\_values=None)

Compute the decision function of the given observations.

# **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

raw\_values [bool, optional] Whether or not to consider raw Mahalanobis distances as the decision function. Must be False (default) for compatibility with the others outlier detection tools.

Deprecated since version 0.20: raw\_values has been deprecated in 0.20 and will be removed in 0.22.

## Returns

**decision** [array-like, shape (n\_samples, )] Decision function of the samples. It is equal to the shifted Mahalanobis distances. The threshold for being an outlier is 0, which ensures a compatibility with other outlier detection algorithms.

# error\_norm(self, comp\_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

## **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

norm [str] The type of norm used to compute the error. Available error types: - 'frobenius'
 (default): sqrt(tr(A^t.A)) - 'spectral': sqrt(max(eigenvalues(A^t.A)) where A is the error
 (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

**squared** [bool] Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

#### Returns

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp cov covariance estimators.

## **fit** (self, X, y=None)

Fit the EllipticEnvelope model.

### **Parameters**

- **X** [numpy array or sparse matrix, shape (n\_samples, n\_features).] Training data
- y [Ignored] not used, present for API consistency by convention.

# fit\_predict (self, X, y=None)

Performs fit on X and returns labels for X.

Returns -1 for outliers and 1 for inliers.

#### **Parameters**

- **X** [ndarray, shape (n\_samples, n\_features)] Input data.
- y [Ignored] not used, present for API consistency by convention.

## Returns

y [ndarray, shape (n\_samples,)] 1 for inliers, -1 for outliers.

# get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## **Returns**

**params** [mapping of string to any] Parameter names mapped to their values.

# get\_precision(self)

Getter for the precision matrix.

#### Returns

**precision**\_ [array-like] The precision matrix associated to the current covariance object.

## mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

# Returns

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

# predict (self, X)

Predict the labels (1 inlier, -1 outlier) of X according to the fitted model.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

## Returns

is\_inlier [array, shape (n\_samples,)] Returns -1 for anomalies/outliers and +1 for inliers.

### reweight covariance (self, data)

Re-weight raw Minimum Covariance Determinant estimates.

Re-weight observations using Rousseeuw's method (equivalent to deleting outlying observations from the data set before computing location and covariance estimates) described in [RVDriessen].

#### **Parameters**

**data** [array-like, shape (n\_samples, n\_features)] The data matrix, with p features and n samples. The data set must be the one which was used to compute the raw estimates.

### **Returns**

**location\_reweighted** [array-like, shape (n\_features, )] Re-weighted robust location estimate.

**covariance\_reweighted** [array-like, shape (n\_features, n\_features)] Re-weighted robust covariance estimate.

**support\_reweighted** [array-like, type boolean, shape (n\_samples,)] A mask of the observations that have been used to compute the re-weighted robust location and covariance estimates.

#### References

[RVDriessen]

# score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Test samples.

y [array-like, shape (n\_samples,) or (n\_samples, n\_outputs)] True labels for X.

**sample weight** [array-like, shape (n samples,), optional] Sample weights.

## Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

# score\_samples (self, X)

Compute the negative Mahalanobis distances.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

# Returns

**negative\_mahal\_distances** [array-like, shape (n\_samples, )] Opposite of the Mahalanobis distances.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.covariance.EllipticEnvelope

- Comparing anomaly detection algorithms for outlier detection on toy datasets
- Outlier detection on a real data set

# 6.6.3 sklearn.covariance.GraphicalLasso

```
class sklearn.covariance.GraphicalLasso (alpha=0.01, mode='cd', tol=0.0001, enet\_tol=0.0001, max\_iter=100, verbose=False, assume\_centered=False)
```

Sparse inverse covariance estimation with an 11-penalized estimator.

Read more in the User Guide.

## **Parameters**

**alpha** [positive float, default 0.01] The regularization parameter: the higher alpha, the more regularization, the sparser the inverse covariance.

**mode** [{'cd', 'lars'}, default 'cd'] The Lasso solver to use: coordinate descent or LARS. Use LARS for very sparse underlying graphs, where p > n. Elsewhere prefer cd which is more numerically stable.

**tol** [positive float, default 1e-4] The tolerance to declare convergence: if the dual gap goes below this value, iterations are stopped.

enet\_tol [positive float, optional] The tolerance for the elastic net solver used to calculate the descent direction. This parameter controls the accuracy of the search direction for a given column update, not of the overall parameter estimate. Only used for mode='cd'.

max\_iter [integer, default 100] The maximum number of iterations.

**verbose** [boolean, default False] If verbose is True, the objective function and dual gap are plotted at each iteration.

**assume\_centered** [boolean, default False] If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data are centered before computation.

# Attributes

```
    location_ [array-like, shape (n_features,)] Estimated location, i.e. the estimated mean.
    covariance_ [array-like, shape (n_features, n_features)] Estimated covariance matrix
    precision_ [array-like, shape (n_features, n_features)] Estimated pseudo inverse matrix.
    n_iter_ [int] Number of iterations run.
```

See also:

#### graphical lasso, GraphicalLassoCV

# **Examples**

```
>>> import numpy as np
>>> from sklearn.covariance import GraphicalLasso
>>> true_cov = np.array([[0.8, 0.0, 0.2, 0.0],
                          [0.0, 0.4, 0.0, 0.0],
. . .
                          [0.2, 0.0, 0.3, 0.1],
. . .
                          [0.0, 0.0, 0.1, 0.7]])
. . .
>>> np.random.seed(0)
>>> X = np.random.multivariate_normal(mean=[0, 0, 0, 0],
                                       cov=true_cov,
                                       size=200)
. . .
>>> cov = GraphicalLasso().fit(X)
>>> np.around(cov.covariance_, decimals=3)
array([[0.816, 0.049, 0.218, 0.019],
       [0.049, 0.364, 0.017, 0.034],
       [0.218, 0.017, 0.322, 0.093],
       [0.019, 0.034, 0.093, 0.69]])
>>> np.around(cov.location_, decimals=3)
array([0.073, 0.04 , 0.038, 0.143])
```

### **Methods**

<pre>error_norm(self, comp_cov[, norm, scaling,])</pre>	Computes the Mean Squared Error between two covari-
	ance estimators.
fit(self, X[, y])	Fits the GraphicalLasso model to X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Getter for the precision matrix.
mahalanobis(self, X)	Computes the squared Mahalanobis distances of given
	observations.
score(self, X_test[, y])	Computes the log-likelihood of a Gaussian data set with
	self.covariance_ as an estimator of its covari-
	ance matrix.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, alpha=0.01, mode='cd', tol=0.0001, enet_tol=0.0001, max_iter=100, verbose=False, assume centered=False)
```

error\_norm(self, comp\_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

## **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

norm [str] The type of norm used to compute the error. Available error types: - 'frobenius'
 (default): sqrt(tr(A^t.A)) - 'spectral': sqrt(max(eigenvalues(A^t.A)) where A is the error
 (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

**squared** [bool] Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

#### Returns

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp cov covariance estimators.

# **fit** (self, X, y=None)

Fits the Graphical Lasso model to X.

### **Parameters**

**X** [ndarray, shape (n\_samples, n\_features)] Data from which to compute the covariance estimate

y [(ignored)]

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

# get\_precision(self)

Getter for the precision matrix.

# Returns

**precision**\_ [array-like] The precision matrix associated to the current covariance object.

### mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

### **Returns**

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

## score(self, X test, y=None)

Computes the log-likelihood of a Gaussian data set with self.covariance\_ as an estimator of its covariance matrix.

## **Parameters**

**X\_test** [array-like, shape = [n\_samples, n\_features]] Test data of which we compute the likelihood, where n\_samples is the number of samples and n\_features is the number of features. X\_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y not used, present for API consistence purpose.

## Returns

**res** [float] The likelihood of the data set with self.covariance\_ as an estimator of its covariance matrix.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# 6.6.4 sklearn.covariance.GraphicalLassoCV

```
class sklearn.covariance.GraphicalLassoCV (alphas=4, n_refinements=4, cv='warn', tol=0.0001, enet_tol=0.0001, max_iter=100, mode='cd', n_jobs=None, verbose=False, assume_centered=False)
```

Sparse inverse covariance w/ cross-validated choice of the  $\overline{1}1$  penalty.

See glossary entry for cross-validation estimator.

Read more in the *User Guide*.

#### **Parameters**

- **alphas** [integer, or list positive float, optional] If an integer is given, it fixes the number of points on the grids of alpha to be used. If a list is given, it gives the grid to be used. See the notes in the class docstring for more details.
- **n\_refinements** [strictly positive integer] The number of times the grid is refined. Not used if explicit values of alphas are passed.
- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross-validation,
  - integer, to specify the number of folds.
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

- **tol** [positive float, optional] The tolerance to declare convergence: if the dual gap goes below this value, iterations are stopped.
- enet\_tol [positive float, optional] The tolerance for the elastic net solver used to calculate the descent direction. This parameter controls the accuracy of the search direction for a given column update, not of the overall parameter estimate. Only used for mode='cd'.

max\_iter [integer, optional] Maximum number of iterations.

- **mode** [{'cd', 'lars'}] The Lasso solver to use: coordinate descent or LARS. Use LARS for very sparse underlying graphs, where number of features is greater than number of samples. Elsewhere prefer cd which is more numerically stable.
- n\_jobs [int or None, optional (default=None)] number of jobs to run in parallel. None means 1
   unless in a joblib.parallel\_backend context. -1 means using all processors. See
   Glossary for more details.
- **verbose** [boolean, optional] If verbose is True, the objective function and duality gap are printed at each iteration.
- **assume\_centered** [boolean] If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data are centered before computation.

#### **Attributes**

**location**\_ [array-like, shape (n\_features,)] Estimated location, i.e. the estimated mean.

**covariance** [numpy.ndarray, shape (n\_features, n\_features)] Estimated covariance matrix.

**precision**\_ [numpy.ndarray, shape (n\_features, n\_features)] Estimated precision matrix (inverse covariance).

alpha\_ [float] Penalization parameter selected.

cv\_alphas\_ [list of float] All penalization parameters explored.

**grid\_scores**\_ [2D numpy.ndarray (n\_alphas, n\_folds)] Log-likelihood score on left-out data across folds.

**n\_iter\_** [int] Number of iterations run for the optimal alpha.

# See also:

```
graphical_lasso, GraphicalLasso
```

# **Notes**

The search for the optimal penalization parameter (alpha) is done on an iteratively refined grid: first the cross-validated scores on a grid are computed, then a new refined grid is centered around the maximum, and so on.

One of the challenges which is faced here is that the solvers can fail to converge to a well-conditioned estimate. The corresponding values of alpha then come out as missing values, but the optimum may be close to these missing values.

## **Examples**

### **Methods**

<pre>error_norm(self, comp_cov[, norm, scaling,])</pre>	Computes the Mean Squared Error between two covariance estimators.
fit(self, X[, y])	Fits the GraphicalLasso covariance model to X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Getter for the precision matrix.
mahalanobis(self, X)	Computes the squared Mahalanobis distances of given
	observations.
score(self, X_test[, y])	Computes the log-likelihood of a Gaussian data set with
	self.covariance_ as an estimator of its covari-
	ance matrix.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, alphas=4, n_refinements=4, cv='warn', tol=0.0001, enet_tol=0.0001, max_iter=100, mode='cd', n_jobs=None, verbose=False, assume_centered=False)
```

error\_norm(self, comp\_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

#### **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

**norm** [str] The type of norm used to compute the error. Available error types: - 'frobenius' (default):  $sqrt(tr(A^t.A))$  - 'spectral':  $sqrt(max(eigenvalues(A^t.A)))$  where A is the error (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

**squared** [bool] Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

## Returns

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp\_cov covariance estimators.

**fit** (*self*, *X*, *y*=*None*)

Fits the Graphical Lasso covariance model to X.

## Parameters

**X** [ndarray, shape (n\_samples, n\_features)] Data from which to compute the covariance estimate

y [(ignored)]

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### get\_precision(self)

Getter for the precision matrix.

#### Returns

**precision** [array-like] The precision matrix associated to the current covariance object.

# mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

#### Parameters

**X** [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

### **Returns**

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

# score (self, X\_test, y=None)

Computes the log-likelihood of a Gaussian data set with self.covariance\_ as an estimator of its covariance matrix.

## **Parameters**

**X\_test** [array-like, shape = [n\_samples, n\_features]] Test data of which we compute the likelihood, where n\_samples is the number of samples and n\_features is the number of features. X\_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y not used, present for API consistence purpose.

### Returns

res [float] The likelihood of the data set with self.covariance\_as an estimator of its covariance matrix.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

### Examples using sklearn.covariance.GraphicalLassoCV

• Visualizing the stock market structure

• Sparse inverse covariance estimation

## 6.6.5 sklearn.covariance.LedoitWolf

LedoitWolf Estimator

Ledoit-Wolf is a particular form of shrinkage, where the shrinkage coefficient is computed using O. Ledoit and M. Wolf's formula as described in "A Well-Conditioned Estimator for Large-Dimensional Covariance Matrices", Ledoit and Wolf, Journal of Multivariate Analysis, Volume 88, Issue 2, February 2004, pages 365-411.

Read more in the *User Guide*.

#### **Parameters**

**store\_precision** [bool, default=True] Specify if the estimated precision is stored.

**assume\_centered** [bool, default=False] If True, data will not be centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False (default), data will be centered before computation.

**block\_size** [int, default=1000] Size of the blocks into which the covariance matrix will be split during its Ledoit-Wolf estimation. This is purely a memory optimization and does not affect results.

#### Attributes

```
location_ [array-like, shape (n_features,)] Estimated location, i.e. the estimated mean.
```

**covariance** [array-like, shape (n\_features, n\_features)] Estimated covariance matrix

**precision**\_ [array-like, shape (n\_features, n\_features)] Estimated pseudo inverse matrix. (stored only if store\_precision is True)

**shrinkage**\_ [float, 0 <= shrinkage <= 1] Coefficient in the convex combination used for the computation of the shrunk estimate.

## **Notes**

The regularised covariance is:

```
(1 - shrinkage) * cov + shrinkage * mu * np.identity(n_features)
```

where mu = trace(cov) / n\_features and shrinkage is given by the Ledoit and Wolf formula (see References)

### References

"A Well-Conditioned Estimator for Large-Dimensional Covariance Matrices", Ledoit and Wolf, Journal of Multivariate Analysis, Volume 88, Issue 2, February 2004, pages 365-411.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.covariance import LedoitWolf
>>> real_cov = np.array([[.4, .2],
... [.2, .8]])
```

# **Methods**

error_norm(self, comp_cov[, norm, scaling,])	Computes the Mean Squared Error between two covari-
	ance estimators.
fit(self, X[, y])	Fits the Ledoit-Wolf shrunk covariance model accord-
	ing to the given training data and parameters.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Getter for the precision matrix.
mahalanobis(self, X)	Computes the squared Mahalanobis distances of given
	observations.
score(self, X_test[, y])	Computes the log-likelihood of a Gaussian data set with
	self.covariance_ as an estimator of its covari-
	ance matrix.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
___init__ (self, store_precision=True, assume_centered=False, block_size=1000)
```

error\_norm(self, comp\_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

# **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

**norm** [str] The type of norm used to compute the error. Available error types: - 'frobenius' (default):  $sqrt(tr(A^t.A))$  - 'spectral':  $sqrt(max(eigenvalues(A^t.A)))$  where A is the error (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

**squared** [bool] Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

# Returns

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp\_cov covariance estimators.

```
fit (self, X, y=None)
```

Fits the Ledoit-Wolf shrunk covariance model according to the given training data and parameters.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Training data, where n\_samples is the number of samples and n\_features is the number of features.

y not used, present for API consistence purpose.

#### Returns

self [object]

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

## get\_precision(self)

Getter for the precision matrix.

#### Returns

precision\_ [array-like] The precision matrix associated to the current covariance object.

# mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

#### Returns

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

### score (self, X\_test, y=None)

Computes the log-likelihood of a Gaussian data set with self.covariance\_ as an estimator of its covariance matrix.

## **Parameters**

**X\_test** [array-like, shape = [n\_samples, n\_features]] Test data of which we compute the likelihood, where n\_samples is the number of samples and n\_features is the number of features. X\_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y not used, present for API consistence purpose.

## Returns

**res** [float] The likelihood of the data set with self.covariance\_as an estimator of its covariance matrix.

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# Examples using sklearn.covariance.LedoitWolf

- Ledoit-Wolf vs OAS estimation
- Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood
- Model selection with Probabilistic PCA and Factor Analysis (FA)

# 6.6.6 sklearn.covariance.MinCovDet

Minimum Covariance Determinant (MCD): robust estimator of covariance.

The Minimum Covariance Determinant covariance estimator is to be applied on Gaussian-distributed data, but could still be relevant on data drawn from a unimodal, symmetric distribution. It is not meant to be used with multi-modal data (the algorithm used to fit a MinCovDet object is likely to fail in such a case). One should consider projection pursuit methods to deal with multi-modal datasets.

Read more in the User Guide.

### **Parameters**

**store\_precision** [bool] Specify if the estimated precision is stored.

- assume\_centered [bool] If True, the support of the robust location and the covariance estimates is computed, and a covariance estimate is recomputed from it, without centering the data. Useful to work with data whose mean is significantly equal to zero but is not exactly zero. If False, the robust location and covariance are directly computed with the FastMCD algorithm without additional treatment.
- **support\_fraction** [float, 0 < support\_fraction < 1] The proportion of points to be included in the support of the raw MCD estimate. Default is None, which implies that the minimum value of support\_fraction will be used within the algorithm: [n\_sample + n\_features + 1] / 2
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

## Attributes

- **raw\_location**\_ [array-like, shape (n\_features,)] The raw robust estimated location before correction and re-weighting.
- **raw\_covariance\_** [array-like, shape (n\_features, n\_features)] The raw robust estimated covariance before correction and re-weighting.
- raw\_support\_ [array-like, shape (n\_samples,)] A mask of the observations that have been used to compute the raw robust estimates of location and shape, before correction and reweighting.

**location**\_ [array-like, shape (n\_features,)] Estimated robust location

**covariance** [array-like, shape (n\_features, n\_features)] Estimated robust covariance matrix

**precision**\_ [array-like, shape (n\_features, n\_features)] Estimated pseudo inverse matrix. (stored only if store\_precision is True)

**support**\_ [array-like, shape (n\_samples,)] A mask of the observations that have been used to compute the robust estimates of location and shape.

**dist\_** [array-like, shape (n\_samples,)] Mahalanobis distances of the training set (on which fit is called) observations.

### References

[R9f63e655f7bd-Rouseeuw1984], [R9f63e655f7bd-Rouseeuw], [R9f63e655f7bd-ButlerDavies]

# **Examples**

# **Methods**

correct_covariance(self, data)	Apply a correction to raw Minimum Covariance Deter-
	minant estimates.
error_norm(self, comp_cov[, norm, scaling,])	Computes the Mean Squared Error between two covari-
	ance estimators.
fit(self, X[, y])	Fits a Minimum Covariance Determinant with the
	FastMCD algorithm.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Getter for the precision matrix.
mahalanobis(self, X)	Computes the squared Mahalanobis distances of given
	observations.
reweight_covariance(self, data)	Re-weight raw Minimum Covariance Determinant esti-
	mates.
score(self, X_test[, y])	Computes the log-likelihood of a Gaussian data set with
	self.covariance_ as an estimator of its covari-
	ance matrix.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_(self, store\_precision=True, assume\_centered=False, support\_fraction=None, ran-dom state=None)

## correct\_covariance (self, data)

Apply a correction to raw Minimum Covariance Determinant estimates.

Correction using the empirical correction factor suggested by Rousseeuw and Van Driessen in [RVD].

### **Parameters**

**data** [array-like, shape (n\_samples, n\_features)] The data matrix, with p features and n samples. The data set must be the one which was used to compute the raw estimates.

#### Returns

**covariance\_corrected** [array-like, shape (n\_features, n\_features)] Corrected robust covariance estimate.

### References

[RVD]

error\_norm(self, comp\_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

### **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

**norm** [str] The type of norm used to compute the error. Available error types: - 'frobenius' (default):  $sqrt(tr(A^t.A))$  - 'spectral':  $sqrt(max(eigenvalues(A^t.A)))$  where A is the error (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

**squared** [bool] Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

# Returns

The Mean Squared Error (in the sense of the Frobenius norm) between

self and comp\_cov covariance estimators.

**fit** (*self*, *X*, *y*=*None*)

Fits a Minimum Covariance Determinant with the FastMCD algorithm.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Training data, where n\_samples is the number of samples and n\_features is the number of features.

y not used, present for API consistence purpose.

## Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

#### get\_precision(self)

Getter for the precision matrix.

#### Returns

precision\_ [array-like] The precision matrix associated to the current covariance object.

# mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

#### Returns

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

# reweight\_covariance (self, data)

Re-weight raw Minimum Covariance Determinant estimates.

Re-weight observations using Rousseeuw's method (equivalent to deleting outlying observations from the data set before computing location and covariance estimates) described in [RVDriessen].

#### **Parameters**

**data** [array-like, shape (n\_samples, n\_features)] The data matrix, with p features and n samples. The data set must be the one which was used to compute the raw estimates.

#### **Returns**

**location\_reweighted** [array-like, shape (n\_features, )] Re-weighted robust location estimate.

**covariance\_reweighted** [array-like, shape (n\_features, n\_features)] Re-weighted robust covariance estimate.

**support\_reweighted** [array-like, type boolean, shape (n\_samples,)] A mask of the observations that have been used to compute the re-weighted robust location and covariance estimates.

# References

[RVDriessen]

## score (self, X\_test, y=None)

Computes the log-likelihood of a Gaussian data set with self.covariance\_ as an estimator of its covariance matrix.

# **Parameters**

**X\_test** [array-like, shape = [n\_samples, n\_features]] Test data of which we compute the likelihood, where n samples is the number of samples and n features is the number of

features. X\_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y not used, present for API consistence purpose.

#### Returns

res [float] The likelihood of the data set with self.covariance\_as an estimator of its covariance matrix.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# Examples using sklearn.covariance.MinCovDet

- Robust covariance estimation and Mahalanobis distances relevance
- Robust vs Empirical covariance estimate

# 6.6.7 sklearn.covariance.OAS

class sklearn.covariance.OAS (store\_precision=True, assume\_centered=False)
 Oracle Approximating Shrinkage Estimator

Read more in the *User Guide*.

OAS is a particular form of shrinkage described in "Shrinkage Algorithms for MMSE Covariance Estimation" Chen et al., IEEE Trans. on Sign. Proc., Volume 58, Issue 10, October 2010.

The formula used here does not correspond to the one given in the article. In the original article, formula (23) states that 2/p is multiplied by Trace(cov\*cov) in both the numerator and denominator, but this operation is omitted because for a large p, the value of 2/p is so small that it doesn't affect the value of the estimator.

# **Parameters**

store\_precision [bool, default=True] Specify if the estimated precision is stored.

**assume\_centered** [bool, default=False] If True, data will not be centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False (default), data will be centered before computation.

## **Attributes**

covariance\_ [array-like, shape (n\_features, n\_features)] Estimated covariance matrix.

**precision**\_ [array-like, shape (n\_features, n\_features)] Estimated pseudo inverse matrix. (stored only if store\_precision is True)

**shrinkage**\_ [float, 0 <= shrinkage <= 1] coefficient in the convex combination used for the computation of the shrunk estimate.

# **Notes**

The regularised covariance is:

(1 - shrinkage) \* cov + shrinkage \* mu \* np.identity(n\_features)

where mu = trace(cov) / n\_features and shrinkage is given by the OAS formula (see References)

#### References

"Shrinkage Algorithms for MMSE Covariance Estimation" Chen et al., IEEE Trans. on Sign. Proc., Volume 58, Issue 10, October 2010.

#### **Methods**

<pre>error_norm(self, comp_cov[, norm, scaling,])</pre>	Computes the Mean Squared Error between two covariance estimators.
fit(self, X[, y])	Fits the Oracle Approximating Shrinkage covariance
	model according to the given training data and parame-
	ters.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Getter for the precision matrix.
mahalanobis(self, X)	Computes the squared Mahalanobis distances of given
	observations.
score(self, X_test[, y])	Computes the log-likelihood of a Gaussian data set with
	self.covariance_ as an estimator of its covari-
	ance matrix.
set_params(self, \*\*params)	Set the parameters of this estimator.

**\_\_\_init\_\_** (*self*, *store\_precision=True*, *assume\_centered=False*)

error norm(self, comp cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

# **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

**norm** [str] The type of norm used to compute the error. Available error types: - 'frobenius' (default):  $sqrt(tr(A^t.A))$  - 'spectral':  $sqrt(max(eigenvalues(A^t.A)))$  where A is the error (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

**squared** [bool] Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

## Returns

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp\_cov covariance estimators.

#### **fit** (self, X, y=None)

Fits the Oracle Approximating Shrinkage covariance model according to the given training data and parameters.

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Training data, where n\_samples is the number of samples and n\_features is the number of features.

y not used, present for API consistence purpose.

### **Returns**

self [object]

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

# get\_precision(self)

Getter for the precision matrix.

#### Returns

precision\_ [array-like] The precision matrix associated to the current covariance object.

# mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

#### **Parameters**

X [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

# Returns

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

```
score (self, X_test, y=None)
```

Computes the log-likelihood of a Gaussian data set with self.covariance\_ as an estimator of its covariance matrix.

## **Parameters**

**X\_test** [array-like, shape = [n\_samples, n\_features]] Test data of which we compute the likelihood, where n\_samples is the number of samples and n\_features is the number of features. X\_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y not used, present for API consistence purpose.

# Returns

res [float] The likelihood of the data set with self.covariance\_as an estimator of its covariance matrix.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.covariance.OAS

- Ledoit-Wolf vs OAS estimation
- Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood

# 6.6.8 sklearn.covariance.ShrunkCovariance

Covariance estimator with shrinkage

Read more in the User Guide.

### **Parameters**

store\_precision [boolean, default True] Specify if the estimated precision is stored

**assume\_centered** [boolean, default False] If True, data will not be centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data will be centered before computation.

**shrinkage** [float, 0 <= shrinkage <= 1, default 0.1] Coefficient in the convex combination used for the computation of the shrunk estimate.

# **Attributes**

location\_ [array-like, shape (n\_features,)] Estimated location, i.e. the estimated mean.

**covariance** [array-like, shape (n\_features, n\_features)] Estimated covariance matrix

**precision**\_ [array-like, shape (n\_features, n\_features)] Estimated pseudo inverse matrix. (stored only if store\_precision is True)

**shrinkage** [float, 0 <= shrinkage <= 1] Coefficient in the convex combination used for the computation of the shrunk estimate.

# **Notes**

The regularized covariance is given by:

```
(1 - shrinkage) * cov + shrinkage * mu * np.identity(n_features) where mu = trace(cov) / n features
```

# **Examples**

```
>>> import numpy as np
>>> from sklearn.covariance import ShrunkCovariance
>>> from sklearn.datasets import make_gaussian_quantiles
>>> real_cov = np.array([[.8, .3],
                         [.3, .4]])
. . .
>>> rng = np.random.RandomState(0)
>>> X = rng.multivariate_normal(mean=[0, 0],
                                       cov=real_cov,
                                       size=500)
. . .
>>> cov = ShrunkCovariance().fit(X)
>>> cov.covariance_
array([[0.7387..., 0.2536...],
       [0.2536..., 0.4110...]])
>>> cov.location_
array([0.0622..., 0.0193...])
```

## **Methods**

error_norm(self, comp_cov[, norm, scaling,])	Computes the Mean Squared Error between two covari-
	ance estimators.
fit(self, X[, y])	Fits the shrunk covariance model according to the given
	training data and parameters.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Getter for the precision matrix.
mahalanobis(self, X)	Computes the squared Mahalanobis distances of given
	observations.
score(self, X_test[, y])	Computes the log-likelihood of a Gaussian data set with
	self.covariance_ as an estimator of its covari-
	ance matrix.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
___init__ (self, store_precision=True, assume_centered=False, shrinkage=0.1)
```

error\_norm(self, comp\_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

# **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

**norm** [str] The type of norm used to compute the error. Available error types: - 'frobenius' (default):  $sqrt(tr(A^t.A))$  - 'spectral':  $sqrt(max(eigenvalues(A^t.A)))$  where A is the error (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

**squared** [bool] Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

#### Returns

The Mean Squared Error (in the sense of the Frobenius norm) between

## self and comp\_cov covariance estimators.

## **fit** (self, X, y=None)

Fits the shrunk covariance model according to the given training data and parameters.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y not used, present for API consistence purpose.

### **Returns**

self [object]

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

### get\_precision(self)

Getter for the precision matrix.

#### Returns

**precision** [array-like] The precision matrix associated to the current covariance object.

# mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

## Returns

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

```
score(self, X test, y=None)
```

Computes the log-likelihood of a Gaussian data set with self.covariance\_ as an estimator of its covariance matrix.

### **Parameters**

- **X\_test** [array-like, shape = [n\_samples, n\_features]] Test data of which we compute the likelihood, where n\_samples is the number of samples and n\_features is the number of features. X\_test is assumed to be drawn from the same distribution than the data used in fit (including centering).
- y not used, present for API consistence purpose.

# Returns

res [float] The likelihood of the data set with self.covariance\_as an estimator of its covariance matrix.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.covariance.ShrunkCovariance

- Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood
- Model selection with Probabilistic PCA and Factor Analysis (FA)

$covariance.empirical\_covariance(X[,])$	Computes the Maximum likelihood covariance estimator
covariance.graphical_lasso(emp_cov, alpha[,	11-penalized covariance estimator
])	
<pre>covariance.ledoit_wolf(X[, assume_centered,</pre>	Estimates the shrunk Ledoit-Wolf covariance matrix.
])	
covariance.oas(X[, assume_centered])	Estimate covariance with the Oracle Approximating
	Shrinkage algorithm.
covariance.shrunk_covariance(emp_cov[,])	Calculates a covariance matrix shrunk on the diagonal

# 6.6.9 sklearn.covariance.empirical covariance

sklearn.covariance.empirical\_covariance (X, assume\_centered=False)
Computes the Maximum likelihood covariance estimator

#### **Parameters**

X [ndarray, shape (n\_samples, n\_features)] Data from which to compute the covariance estimate

**assume\_centered** [boolean] If True, data will not be centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data will be centered before computation.

## Returns

**covariance** [2D ndarray, shape (n\_features, n\_features)] Empirical covariance (Maximum Likelihood Estimator).

# Examples using sklearn.covariance.empirical\_covariance

• Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood

# 6.6.10 sklearn.covariance.graphical lasso

```
sklearn.covariance.graphical_lasso (emp_cov, alpha, cov_init=None, mode='cd', tol=0.0001, enet_tol=0.0001, max_iter=100, verbose=False, return_costs=False, eps=2.220446049250313e-16, return_n_iter=False)
```

Read more in the *User Guide*.

#### **Parameters**

- **emp\_cov** [2D ndarray, shape (n\_features, n\_features)] Empirical covariance from which to compute the covariance estimate.
- **alpha** [positive float] The regularization parameter: the higher alpha, the more regularization, the sparser the inverse covariance.
- cov init [2D array (n features, n features), optional] The initial guess for the covariance.
- **mode** [{'cd', 'lars'}] The Lasso solver to use: coordinate descent or LARS. Use LARS for very sparse underlying graphs, where p > n. Elsewhere prefer cd which is more numerically stable.
- **tol** [positive float, optional] The tolerance to declare convergence: if the dual gap goes below this value, iterations are stopped.
- enet\_tol [positive float, optional] The tolerance for the elastic net solver used to calculate the descent direction. This parameter controls the accuracy of the search direction for a given column update, not of the overall parameter estimate. Only used for mode='cd'.
- **max\_iter** [integer, optional] The maximum number of iterations.
- **verbose** [boolean, optional] If verbose is True, the objective function and dual gap are printed at each iteration.
- **return\_costs** [boolean, optional] If return\_costs is True, the objective function and dual gap at each iteration are returned.
- **eps** [float, optional] The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems.
- **return\_n\_iter** [bool, optional] Whether or not to return the number of iterations.

#### Returns

- **covariance** [2D ndarray, shape (n\_features, n\_features)] The estimated covariance matrix.
- **precision** [2D ndarray, shape (n\_features, n\_features)] The estimated (sparse) precision matrix.
- **costs** [list of (objective, dual\_gap) pairs] The list of values of the objective function and the dual gap at each iteration. Returned only if return\_costs is True.
- **n\_iter** [int] Number of iterations. Returned only if return\_n\_iter is set to True.

#### See also:

GraphicalLasso, GraphicalLassoCV

### **Notes**

The algorithm employed to solve this problem is the GLasso algorithm, from the Friedman 2008 Biostatistics paper. It is the same algorithm as in the R glasso package.

One possible difference with the glasso R package is that the diagonal coefficients are not penalized.

# 6.6.11 sklearn.covariance.ledoit\_wolf

sklearn.covariance.ledoit\_wolf (*X*, assume\_centered=False, block\_size=1000) Estimates the shrunk Ledoit-Wolf covariance matrix.

Read more in the *User Guide*.

#### **Parameters**

X [array-like, shape (n\_samples, n\_features)] Data from which to compute the covariance estimate

**assume\_centered** [boolean, default=False] If True, data will not be centered before computation. Useful to work with data whose mean is significantly equal to zero but is not exactly zero. If False, data will be centered before computation.

**block\_size** [int, default=1000] Size of the blocks into which the covariance matrix will be split. This is purely a memory optimization and does not affect results.

## Returns

**shrunk\_cov** [array-like, shape (n\_features, n\_features)] Shrunk covariance.

**shrinkage** [float] Coefficient in the convex combination used for the computation of the shrunk estimate.

## **Notes**

The regularized (shrunk) covariance is:
(1 - shrinkage) \* cov + shrinkage \* mu \* np.identity(n\_features)
where mu = trace(cov) / n\_features

### Examples using sklearn.covariance.ledoit\_wolf

• Sparse inverse covariance estimation

# 6.6.12 sklearn.covariance.oas

sklearn.covariance.oas(X, assume\_centered=False)

Estimate covariance with the Oracle Approximating Shrinkage algorithm.

#### **Parameters**

X [array-like, shape (n\_samples, n\_features)] Data from which to compute the covariance estimate.

**assume\_centered** [boolean] If True, data will not be centered before computation. Useful to work with data whose mean is significantly equal to zero but is not exactly zero. If False, data will be centered before computation.

#### Returns

**shrunk\_cov** [array-like, shape (n\_features, n\_features)] Shrunk covariance.

**shrinkage** [float] Coefficient in the convex combination used for the computation of the shrunk estimate.

# **Notes**

The regularised (shrunk) covariance is:

```
(1 - shrinkage) * cov + shrinkage * mu * np.identity(n_features)
```

where  $mu = trace(cov) / n_features$ 

The formula we used to implement the OAS is slightly modified compared to the one given in the article. See *OAS* for more details.

# 6.6.13 sklearn.covariance.shrunk covariance

sklearn.covariance.shrunk\_covariance(emp\_cov, shrinkage=0.1)

Calculates a covariance matrix shrunk on the diagonal

Read more in the User Guide.

#### **Parameters**

emp\_cov [array-like, shape (n\_features, n\_features)] Covariance matrix to be shrunk

**shrinkage** [float, 0 <= shrinkage <= 1] Coefficient in the convex combination used for the computation of the shrunk estimate.

#### Returns

shrunk\_cov [array-like] Shrunk covariance.

#### **Notes**

The regularized (shrunk) covariance is given by:

(1 - shrinkage) \* cov + shrinkage \* mu \* np.identity(n\_features)

where  $mu = trace(cov) / n_features$ 

# 6.7 sklearn.cross\_decomposition: Cross decomposition

**User guide:** See the *Cross decomposition* section for further details.

cross_decomposition.CCA([n_components,])	CCA Canonical Correlation Analysis.
$cross\_decomposition.PLSCanonical([])$	PLSCanonical implements the 2 blocks canonical PLS of
	the original Wold algorithm [Tenenhaus 1998] p.204, re-
	ferred as PLS-C2A in [Wegelin 2000].
$cross\_decomposition.PLSRegression([])$	PLS regression
cross_decomposition.PLSSVD([n_components,	Partial Least Square SVD
])	

# 6.7.1 sklearn.cross\_decomposition.CCA

class sklearn.cross\_decomposition.CCA ( $n\_components=2$ , scale=True,  $max\_iter=500$ , tol=1e-06, copy=True)

CCA Canonical Correlation Analysis.

CCA inherits from PLS with mode="B" and deflation\_mode="canonical".

Read more in the *User Guide*.

# **Parameters**

**n\_components** [int, (default 2).] number of components to keep.

scale [boolean, (default True)] whether to scale the data?

max\_iter [an integer, (default 500)] the maximum number of iterations of the NIPALS inner loop

tol [non-negative real, default 1e-06.] the tolerance used in the iterative algorithm

**copy** [boolean] Whether the deflation be done on a copy. Let the default value to True unless you don't care about side effects

## **Attributes**

```
x_weights [array, [p, n_components]] X block weights vectors.
```

**y\_weights**\_ [array, [q, n\_components]] Y block weights vectors.

**x\_loadings** [array, [p, n\_components]] X block loadings vectors.

y\_loadings\_ [array, [q, n\_components]] Y block loadings vectors.

**x\_scores\_** [array, [n\_samples, n\_components]] X scores.

**y\_scores**\_ [array, [n\_samples, n\_components]] Y scores.

**x\_rotations**\_ [array, [p, n\_components]] X block to latents rotations.

**y\_rotations**\_ [array, [q, n\_components]] Y block to latents rotations.

n\_iter\_ [array-like] Number of iterations of the NIPALS inner loop for each component.

## See also:

**PLSCanonical** 

PLSSVD

#### **Notes**

For each component k, find the weights u, v that maximizes max corr(Xk u, Yk v), such that |u| = |v| = 1

Note that it maximizes only the correlations between the scores.

The residual matrix of X (Xk+1) block is obtained by the deflation on the current X score: x\_score.

The residual matrix of Y (Yk+1) block is obtained by deflation on the current Y score.

# References

Jacob A. Wegelin. A survey of Partial Least Squares (PLS) methods, with emphasis on the two-block case. Technical Report 371, Department of Statistics, University of Washington, Seattle, 2000.

In french but still a reference: Tenenhaus, M. (1998). La regression PLS: theorie et pratique. Paris: Editions Technic.

# **Examples**

```
>>> from sklearn.cross_decomposition import CCA
>>> X = [[0., 0., 1.], [1.,0.,0.], [2.,2.,2.], [3.,5.,4.]]
>>> Y = [[0.1, -0.2], [0.9, 1.1], [6.2, 5.9], [11.9, 12.3]]
>>> cca = CCA(n_components=1)
>>> cca.fit(X, Y)
...
CCA(copy=True, max_iter=500, n_components=1, scale=True, tol=1e-06)
>>> X_c, Y_c = cca.transform(X, Y)
```

### **Methods**

fit(self, X, Y)	Fit model to data.
<pre>fit_transform(self, X[, y])</pre>	Learn and apply the dimension reduction on the train
	data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, copy])</pre>	Apply the dimension reduction learned on the train data.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X[, Y, copy])	Apply the dimension reduction learned on the train data.

```
__init__ (self, n_components=2, scale=True, max_iter=500, tol=1e-06, copy=True)
fit (self, X, Y)
```

Fit model to data.

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- Y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n targets is the number of response variables.

# fit\_transform(self, X, y=None)

Learn and apply the dimension reduction on the train data.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

## Returns

x\_scores if Y is not given, (x\_scores, y\_scores) otherwise.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
predict (self, X, copy=True)
```

Apply the dimension reduction learned on the train data.

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.

**copy** [boolean, default True] Whether to copy X and Y, or perform in-place normalization.

#### **Notes**

This call requires the estimation of a p x q matrix, which may be an issue in high dimensional space.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

```
transform (self, X, Y=None, copy=True)
```

Apply the dimension reduction learned on the train data.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- Y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n targets is the number of response variables.

copy [boolean, default True] Whether to copy X and Y, or perform in-place normalization.

#### **Returns**

x\_scores if Y is not given, (x\_scores, y\_scores) otherwise.

## Examples using sklearn.cross decomposition.CCA

- Multilabel classification
- Compare cross decomposition methods

# 6.7.2 sklearn.cross\_decomposition.PLSCanonical

```
class sklearn.cross_decomposition.PLSCanonical (n_components=2, scale=True, algorithm='nipals', max_iter=500, tol=1e-06, copv=True)
```

PLSCanonical implements the 2 blocks canonical PLS of the original Wold algorithm [Tenenhaus 1998] p.204, referred as PLS-C2A in [Wegelin 2000].

This class inherits from PLS with mode="A" and deflation\_mode="canonical", norm\_y\_weights=True and algorithm="nipals", but svd should provide similar results up to numerical errors.

Read more in the *User Guide*.

# **Parameters**

```
n_components [int, (default 2).] Number of components to keep
```

scale [boolean, (default True)] Option to scale data

**algorithm** [string, "nipals" or "svd"] The algorithm used to estimate the weights. It will be called n\_components times, i.e. once for each iteration of the outer loop.

**max\_iter** [an integer, (default 500)] the maximum number of iterations of the NIPALS inner loop (used only if algorithm="nipals")

tol [non-negative real, default 1e-06] the tolerance used in the iterative algorithm

**copy** [boolean, default True] Whether the deflation should be done on a copy. Let the default value to True unless you don't care about side effect

# Attributes

- **x\_weights** [array, shape = [p, n\_components]] X block weights vectors.
- **y\_weights** [array, shape = [q, n\_components]] Y block weights vectors.
- **x\_loadings** [array, shape = [p, n\_components]] X block loadings vectors.
- **y\_loadings** [array, shape = [q, n\_components]] Y block loadings vectors.
- **x\_scores\_** [array, shape = [n\_samples, n\_components]] X scores.

```
y_scores_ [array, shape = [n_samples, n_components]] Y scores.
```

- $x_{rotations}$  [array, shape = [p, n\_components]] X block to latents rotations.
- **y\_rotations**\_ [array, shape = [q, n\_components]] Y block to latents rotations.
- **n\_iter\_** [array-like] Number of iterations of the NIPALS inner loop for each component. Not useful if the algorithm provided is "svd".

#### See also:

CCA

PLSSVD

#### **Notes**

#### Matrices:

```
T: x_scores_
U: y_scores_
W: x_weights_
C: y_weights_
P: x_loadings_
Q: y_loadings_
```

#### Are computed such that:

```
X = T P.T + Err and Y = U Q.T + Err
T[:, k] = Xk W[:, k] for k in range(n_components)
U[:, k] = Yk C[:, k] for k in range(n_components)
x_rotations_ = W (P.T W)^(-1)
y_rotations_ = C (Q.T C)^(-1)
```

where Xk and Yk are residual matrices at iteration k.

Slides explaining PLS

For each component k, find weights u, v that optimize:

```
max corr(Xk u, Yk v) * std(Xk u) std(Yk u), such that ``|u| = |v| = 1``
```

Note that it maximizes both the correlations between the scores and the intra-block variances.

The residual matrix of X (Xk+1) block is obtained by the deflation on the current X score: x\_score.

The residual matrix of Y (Yk+1) block is obtained by deflation on the current Y score. This performs a canonical symmetric version of the PLS regression. But slightly different than the CCA. This is mostly used for modeling.

This implementation provides the same results that the "plspm" package provided in the R language (R-project), using the function plsca(X, Y). Results are equal or collinear with the function pls(..., mode = "canonical") of the "mixOmics" package. The difference relies in the fact that mixOmics implementation does not exactly implement the Wold algorithm since it does not normalize y\_weights to one.

# References

Jacob A. Wegelin. A survey of Partial Least Squares (PLS) methods, with emphasis on the two-block case. Technical Report 371, Department of Statistics, University of Washington, Seattle, 2000.

Tenenhaus, M. (1998). La regression PLS: theorie et pratique. Paris: Editions Technic.

# **Examples**

```
>>> from sklearn.cross_decomposition import PLSCanonical
>>> X = [[0., 0., 1.], [1.,0.,0.], [2.,2.,2.], [2.,5.,4.]]
>>> Y = [[0.1, -0.2], [0.9, 1.1], [6.2, 5.9], [11.9, 12.3]]
>>> plsca = PLSCanonical(n_components=2)
>>> plsca.fit(X, Y)
...
PLSCanonical(algorithm='nipals', copy=True, max_iter=500, n_components=2, scale=True, tol=1e-06)
>>> X_c, Y_c = plsca.transform(X, Y)
```

## **Methods**

fit(self, X, Y)	Fit model to data.
fit_transform(self, X[, y])	Learn and apply the dimension reduction on the train
	data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, copy])</pre>	Apply the dimension reduction learned on the train data.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X[, Y, copy])	Apply the dimension reduction learned on the train data.

```
__init__(self, n_components=2, scale=True, algorithm='nipals', max_iter=500, tol=1e-06, copy=True)
```

# fit (self, X, Y)

Fit model to data.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- **Y** [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

# fit\_transform(self, X, y=None)

Learn and apply the dimension reduction on the train data.

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

# Returns

x\_scores if Y is not given, (x\_scores, y\_scores) otherwise.

#### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
predict (self, X, copy=True)
```

Apply the dimension reduction learned on the train data.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.

**copy** [boolean, default True] Whether to copy X and Y, or perform in-place normalization.

#### **Notes**

This call requires the estimation of a p x q matrix, which may be an issue in high dimensional space.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample weight** [array-like, shape = [n samples], optional] Sample weights.

# Returns

**score** [float] R^2 of self.predict(X) wrt. y.

# **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

transform(self, X, Y=None, copy=True)

Apply the dimension reduction learned on the train data.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- Y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

**copy** [boolean, default True] Whether to copy X and Y, or perform in-place normalization.

#### Returns

x\_scores if Y is not given, (x\_scores, y\_scores) otherwise.

# Examples using sklearn.cross\_decomposition.PLSCanonical

• Compare cross decomposition methods

# 6.7.3 sklearn.cross\_decomposition.PLSRegression

class sklearn.cross\_decomposition.PLSRegression ( $n\_components=2$ , scale=True,  $max\_iter=500$ , tol=1e-06, copy=True)

PLS regression

PLSRegression implements the PLS 2 blocks regression known as PLS2 or PLS1 in case of one dimensional response. This class inherits from \_PLS with mode="A", deflation\_mode="regression", norm\_y\_weights=False and algorithm="nipals".

Read more in the *User Guide*.

#### **Parameters**

**n\_components** [int, (default 2)] Number of components to keep.

scale [boolean, (default True)] whether to scale the data

max\_iter [an integer, (default 500)] the maximum number of iterations of the NIPALS inner loop (used only if algorithm="nipals")

tol [non-negative real] Tolerance used in the iterative algorithm default 1e-06.

**copy** [boolean, default True] Whether the deflation should be done on a copy. Let the default value to True unless you don't care about side effect

## **Attributes**

- **x\_weights** [array, [p, n\_components]] X block weights vectors.
- **y\_weights** [array, [q, n\_components]] Y block weights vectors.
- **x\_loadings** [array, [p, n\_components]] X block loadings vectors.
- **y\_loadings** [array, [q, n\_components]] Y block loadings vectors.

```
x_scores_ [array, [n_samples, n_components]] X scores.
y_scores_ [array, [n_samples, n_components]] Y scores.
x_rotations_ [array, [p, n_components]] X block to latents rotations.
y_rotations_ [array, [q, n_components]] Y block to latents rotations.
coef_ [array, [p, q]] The coefficients of the linear model: Y = X coef_ + Err
n iter [array-like] Number of iterations of the NIPALS inner loop for each component.
```

#### **Notes**

#### Matrices:

```
T: x_scores_
U: y_scores_
W: x_weights_
C: y_weights_
P: x_loadings_
Q: y_loadings_
```

# Are computed such that:

```
X = T P.T + Err and Y = U Q.T + Err
T[:, k] = Xk W[:, k] for k in range(n_components)
U[:, k] = Yk C[:, k] for k in range(n_components)
x_rotations_ = W (P.T W)^(-1)
y_rotations_ = C (Q.T C)^(-1)
```

where Xk and Yk are residual matrices at iteration k.

#### Slides explaining PLS

```
For each component k, find weights u, v that optimizes: \max \text{corr}(Xk \text{ u}, Yk \text{ v}) * \text{std}(Xk \text{ u}) std(Yk u), such that |u| = 1
```

Note that it maximizes both the correlations between the scores and the intra-block variances.

The residual matrix of X (Xk+1) block is obtained by the deflation on the current X score: x\_score.

The residual matrix of Y (Yk+1) block is obtained by deflation on the current X score. This performs the PLS regression known as PLS2. This mode is prediction oriented.

This implementation provides the same results that 3 PLS packages provided in the R language (R-project):

- "mixOmics" with function pls(X, Y, mode = "regression")
- "plspm" with function plsreg2(X, Y)
- "pls" with function oscorespls.fit(X, Y)

# References

Jacob A. Wegelin. A survey of Partial Least Squares (PLS) methods, with emphasis on the two-block case. Technical Report 371, Department of Statistics, University of Washington, Seattle, 2000.

In french but still a reference: Tenenhaus, M. (1998). La regression PLS: theorie et pratique. Paris: Editions Technic.

# **Examples**

```
>>> from sklearn.cross_decomposition import PLSRegression
>>> X = [[0., 0., 1.], [1.,0.,0.], [2.,2.,2.], [2.,5.,4.]]
>>> Y = [[0.1, -0.2], [0.9, 1.1], [6.2, 5.9], [11.9, 12.3]]
>>> pls2 = PLSRegression(n_components=2)
>>> pls2.fit(X, Y)
...
PLSRegression(copy=True, max_iter=500, n_components=2, scale=True, tol=1e-06)
>>> Y_pred = pls2.predict(X)
```

#### **Methods**

fit(self, X, Y)	Fit model to data.
<pre>fit_transform(self, X[, y])</pre>	Learn and apply the dimension reduction on the train
	data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, copy])</pre>	Apply the dimension reduction learned on the train data.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X[, Y, copy])	Apply the dimension reduction learned on the train data.

```
__init__ (self, n_components=2, scale=True, max_iter=500, tol=1e-06, copy=True)
fit (self, X, Y)
```

Fit model to data.

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- Y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

# fit\_transform(self, X, y=None)

Learn and apply the dimension reduction on the train data.

# **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

# Returns

x\_scores if Y is not given, (x\_scores, y\_scores) otherwise.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
predict (self, X, copy=True)
```

Apply the dimension reduction learned on the train data.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.

**copy** [boolean, default True] Whether to copy X and Y, or perform in-place normalization.

#### **Notes**

This call requires the estimation of a p x q matrix, which may be an issue in high dimensional space.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape =  $(n_samples)$  or  $(n_samples, n_outputs)$ ] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

# **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

#### self

transform(self, X, Y=None, copy=True)

Apply the dimension reduction learned on the train data.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- Y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

**copy** [boolean, default True] Whether to copy X and Y, or perform in-place normalization.

#### **Returns**

x\_scores if Y is not given, (x\_scores, y\_scores) otherwise.

# Examples using sklearn.cross\_decomposition.PLSRegression

• Compare cross decomposition methods

# 6.7.4 sklearn.cross\_decomposition.PLSSVD

```
class sklearn.cross_decomposition.PLSSVD (n_components=2, scale=True, copy=True)
    Partial Least Square SVD
```

Simply perform a svd on the crosscovariance matrix: X'Y There are no iterative deflation here.

Read more in the User Guide.

# **Parameters**

```
n_components [int, default 2] Number of components to keep.
```

scale [boolean, default True] Whether to scale X and Y.

**copy** [boolean, default True] Whether to copy X and Y, or perform in-place computations.

## **Attributes**

```
x_weights [array, [p, n_components]] X block weights vectors.
```

**y\_weights** [array, [q, n\_components]] Y block weights vectors.

**x\_scores**\_ [array, [n\_samples, n\_components]] X scores.

**y\_scores\_** [array, [n\_samples, n\_components]] Y scores.

#### See also:

PLSCanonical

CCA

# **Examples**

```
>>> import numpy as np
>>> from sklearn.cross_decomposition import PLSSVD
>>> X = np.array([[0., 0., 1.],
        [1.,0.,0.],
        [2.,2.,2.],
        [2.,5.,4.]])
. . .
>>> Y = np.array([[0.1, -0.2],
       [0.9, 1.1],
        [6.2, 5.9],
. . .
       [11.9, 12.3]])
. . .
>>> plsca = PLSSVD(n_components=2)
>>> plsca.fit(X, Y)
PLSSVD(copy=True, n_components=2, scale=True)
>>> X_c, Y_c = plsca.transform(X, Y)
>>> X_c.shape, Y_c.shape
((4, 2), (4, 2))
```

#### **Methods**

fit(self, X, Y)	Fit model to data.
<pre>fit_transform(self, X[, y])</pre>	Learn and apply the dimension reduction on the train
	data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X[, Y])	Apply the dimension reduction learned on the train data.

```
__init__ (self, n_components=2, scale=True, copy=True)

fit (self, X, Y)

Fit model to data.
```

# **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- Y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

# fit\_transform(self, X, y=None)

Learn and apply the dimension reduction on the train data.

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- y [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

# Returns

x\_scores if Y is not given, (x\_scores, y\_scores) otherwise.

# get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### **Returns**

self

# transform(self, X, Y=None)

Apply the dimension reduction learned on the train data.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of predictors.
- **Y** [array-like, shape = [n\_samples, n\_targets]] Target vectors, where n\_samples is the number of samples and n\_targets is the number of response variables.

# 6.8 sklearn.datasets: Datasets

The sklearn.datasets module includes utilities to load datasets, including methods to load and fetch popular reference datasets. It also features some artificial data generators.

**User guide:** See the *Dataset loading utilities* section for further details.

# 6.8.1 Loaders

datasets.clear_data_home([data_home])	Delete all the content of the data home cache.
$datasets.dump\_svmlight\_file(X, y, f[,])$	Dump the dataset in symlight / libsym file format.
datasets.fetch_20newsgroups([data_home,	Load the filenames and data from the 20 newsgroups
])	dataset (classification).
datasets.fetch_20newsgroups_vectorized([.	. Load the 20 newsgroups dataset and vectorize it into token
	counts (classification).
datasets.fetch_california_housing([])	Load the California housing dataset (regression).
datasets.fetch_covtype([data_home,])	Load the covertype dataset (classification).
datasets.fetch_kddcup99([subset, data_home,	Load the kddcup99 dataset (classification).
])	
datasets.fetch_lfw_pairs([subset,])	Load the Labeled Faces in the Wild (LFW) pairs dataset
	(classification).
datasets.fetch_lfw_people([data_home,])	Load the Labeled Faces in the Wild (LFW) people dataset
	(classification).
datasets.fetch_olivetti_faces([data_home,	Load the Olivetti faces data-set from AT&T (classification).
])	
datasets.fetch_openml([name, version,])	Fetch dataset from openml by name or dataset id.
	Continued on next page

Continued on next page

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Table 6.47	<ul> <li>continued</li> </ul>	trom	previous page

datasets.fetch_rcv1([data_home, subset,])	Load the RCV1 multilabel dataset (classification).
datasets.fetch_species_distributions([])	Loader for species distribution dataset from Phillips et.
datasets.get_data_home([data_home])	Return the path of the scikit-learn data dir.
datasets.load_boston([return_X_y])	Load and return the boston house-prices dataset (regres-
	sion).
datasets.load_breast_cancer([return_X_y])	Load and return the breast cancer wisconsin dataset (clas-
	sification).
datasets.load_diabetes([return_X_y])	Load and return the diabetes dataset (regression).
<pre>datasets.load_digits([n_class, return_X_y])</pre>	Load and return the digits dataset (classification).
$datasets.load\_files(container\_path[,])$	Load text files with categories as subfolder names.
datasets.load_iris([return_X_y])	Load and return the iris dataset (classification).
datasets.load_linnerud([return_X_y])	Load and return the linnerud dataset (multivariate regres-
	sion).
datasets.load_sample_image(image_name)	Load the numpy array of a single sample image
datasets.load_sample_images()	Load sample images for image manipulation.
datasets.load_svmlight_file(f[, n_features,	Load datasets in the symlight / libsym format into sparse
])	CSR matrix
$datasets.load\_svmlight\_files(files[,])$	Load dataset from multiple files in SVMlight format
datasets.load_wine([return_X_y])	Load and return the wine dataset (classification).

## sklearn.datasets.clear data home

sklearn.datasets.clear\_data\_home (data\_home=None)

Delete all the content of the data home cache.

#### **Parameters**

data\_home [str | None] The path to scikit-learn data dir.

# ${\tt sklearn.datasets.} {\tt dump\_svmlight\_file}$

 $sklearn.datasets.dump\_svmlight\_file (X, y, f, zero\_based=True, comment=None, query\_id=None, multilabel=False)$ 

Dump the dataset in symlight / libsym file format.

This format is a text-based format, with one sample per line. It does not store zero valued features hence is suitable for sparse dataset.

The first element of each line can be used to store a target variable to predict.

#### **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.
- y [{array-like, sparse matrix}, shape = [n\_samples (, n\_labels)]] Target values. Class labels must be an integer or float, or array-like objects of integer or float for multilabel classifications.
- **f** [string or file-like in binary mode] If string, specifies the path that will contain the data. If file-like, data will be written to f. f should be opened in binary mode.
- **zero\_based** [boolean, optional] Whether column indices should be written zero-based (True) or one-based (False).
- **comment** [string, optional] Comment to insert at the top of the file. This should be either a Unicode string, which will be encoded as UTF-8, or an ASCII byte string. If a comment

is given, then it will be preceded by one that identifies the file as having been dumped by scikit-learn. Note that not all tools grok comments in SVMlight files.

**query\_id** [array-like, shape = [n\_samples]] Array containing pairwise preference constraints (qid in symlight format).

**multilabel** [boolean, optional] Samples may have several labels each (see https://www.csie.ntu.edu.tw/~cjlin/libsvmtools/datasets/multilabel.html)

New in version 0.17: parameter *multilabel* to support multilabel datasets.

## Examples using sklearn.datasets.dump symlight file

· Libsym GUI

# sklearn.datasets.fetch 20newsgroups

Load the filenames and data from the 20 newsgroups dataset (classification).

Download it if necessary.

Classes	20
Samples total	18846
Dimensionality	1
Features	text

Read more in the *User Guide*.

## **Parameters**

**data\_home** [optional, default: None] Specify a download and cache folder for the datasets. If None, all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders.

**subset** ['train' or 'test', 'all', optional] Select the dataset to load: 'train' for the training set, 'test' for the test set, 'all' for both, with shuffled ordering.

**categories** [None or collection of string or unicode] If None (default), load all the categories. If not None, list of category names to load (other categories ignored).

**shuffle** [bool, optional] Whether or not to shuffle the data: might be important for models that make the assumption that the samples are independent and identically distributed (i.i.d.), such as stochastic gradient descent.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset shuffling. Pass an int for reproducible output across multiple function calls. See *Glossary*.

**remove** [tuple] May contain any subset of ('headers', 'footers', 'quotes'). Each of these are kinds of text that will be detected and removed from the newsgroup posts, preventing classifiers from overfitting on metadata.

'headers' removes newsgroup headers, 'footers' removes blocks at the ends of posts that look like signatures, and 'quotes' removes lines that appear to be quoting another post.

'headers' follows an exact standard; the other filters are not always correct.

**download\_if\_missing** [optional, True by default] If False, raise an IOError if the data is not locally available instead of trying to download the data from the source site.

#### Returns

**bunch** [Bunch object with the following attribute:]

- bunch.data: list, length [n\_samples]
- bunch.target: array, shape [n\_samples]
- bunch.filenames: list, length [n\_samples]
- bunch.DESCR: a description of the dataset.
- bunch.target\_names: a list of categories of the returned data, length [n\_classes]. This depends on the categories parameter.

# Examples using sklearn.datasets.fetch\_20newsgroups

- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation
- Biclustering documents with the Spectral Co-clustering algorithm
- Column Transformer with Heterogeneous Data Sources
- Sample pipeline for text feature extraction and evaluation
- FeatureHasher and DictVectorizer Comparison
- Clustering text documents using k-means
- Classification of text documents using sparse features

#### sklearn.datasets.fetch 20newsgroups vectorized

```
sklearn.datasets.fetch_20newsgroups_vectorized(subset='train', remove=(), data\_home=None, down-load\_if\_missing=True, return\ X\ v=False)
```

Load the 20 newsgroups dataset and vectorize it into token counts (classification).

Download it if necessary.

This is a convenience function; the transformation is done using the default settings for <code>sklearn.feature\_extraction.text.CountVectorizer</code>. For more advanced usage (stopword filtering, n-gram extraction, etc.), combine fetch\_20newsgroups with a custom <code>sklearn.feature\_extraction.text.CountVectorizer</code>, <code>sklearn.feature\_extraction.text.HashingVectorizer</code>, <code>sklearn.feature\_extraction.text.TfidfTransformer</code> or <code>sklearn.feature\_extraction.text.TfidfVectorizer</code>.

Classes	20
Samples total	18846
Dimensionality	130107
Features	real

Read more in the User Guide.

#### **Parameters**

**subset** ['train' or 'test', 'all', optional] Select the dataset to load: 'train' for the training set, 'test' for the test set, 'all' for both, with shuffled ordering.

**remove** [tuple] May contain any subset of ('headers', 'footers', 'quotes'). Each of these are kinds of text that will be detected and removed from the newsgroup posts, preventing classifiers from overfitting on metadata.

'headers' removes newsgroup headers, 'footers' removes blocks at the ends of posts that look like signatures, and 'quotes' removes lines that appear to be quoting another post.

**data\_home** [optional, default: None] Specify an download and cache folder for the datasets. If None, all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders.

**download\_if\_missing** [optional, True by default] If False, raise an IOError if the data is not locally available instead of trying to download the data from the source site.

**return\_X\_y** [boolean, default=False.] If True, returns (data.data, data.target) instead of a Bunch object.

New in version 0.20.

#### Returns

**bunch** [Bunch object with the following attribute:]

- bunch.data: sparse matrix, shape [n\_samples, n\_features]
- bunch.target: array, shape [n\_samples]
- bunch.target\_names: a list of categories of the returned data, length [n\_classes].
- bunch.DESCR: a description of the dataset.

(data, target) [tuple if return\_X\_y is True] New in version 0.20.

#### Examples using sklearn.datasets.fetch 20newsgroups vectorized

- The Johnson-Lindenstrauss bound for embedding with random projections
- Model Complexity Influence
- Multiclass sparse logisitic regression on newgroups20

# sklearn.datasets.fetch\_california\_housing

sklearn.datasets.fetch\_california\_housing(data\_home=None, download\_if\_missing=True, return\_X\_y=False)

Load the California housing dataset (regression).

Samples total	20640
Dimensionality	8
Features	real
Target	real 0.15 - 5.

Read more in the *User Guide*.

#### **Parameters**

**data\_home** [optional, default: None] Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders.

**download\_if\_missing** [optional, default=True] If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

return\_X\_y [boolean, default=False.] If True, returns (data.data, data.target) instead of a Bunch object.

New in version 0.20.

#### Returns

dataset [dict-like object with the following attributes:]

dataset.data [ndarray, shape [20640, 8]] Each row corresponding to the 8 feature values in order.

**dataset.target** [numpy array of shape (20640,)] Each value corresponds to the average house value in units of 100,000.

dataset.feature\_names [array of length 8] Array of ordered feature names used in the dataset.

dataset.DESCR [string] Description of the California housing dataset.

(data, target) [tuple if return\_X\_y is True] New in version 0.20.

#### **Notes**

This dataset consists of 20,640 samples and 9 features.

# Examples using sklearn.datasets.fetch\_california\_housing

- Imputing missing values with variants of IterativeImputer
- Partial Dependence Plots
- · Compare the effect of different scalers on data with outliers

# sklearn.datasets.fetch\_covtype

sklearn.datasets.**fetch\_covtype**(data\_home=None, download\_if\_missing=True, ran-dom\_state=None, shuffle=False, return\_X\_y=False)

Load the covertype dataset (classification).

Download it if necessary.

Classes	7
Samples total	581012
Dimensionality	54
Features	int

Read more in the User Guide.

## **Parameters**

**data\_home** [string, optional] Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit learn data' subfolders.

**download\_if\_missing** [boolean, default=True] If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset shuffling. Pass an int for reproducible output across multiple function calls. See *Glossary*.

shuffle [bool, default=False] Whether to shuffle dataset.

**return\_X\_y** [boolean, default=False.] If True, returns (data.data, data.target) instead of a Bunch object.

New in version 0.20.

#### Returns

**dataset** [dict-like object with the following attributes:]

dataset.data [numpy array of shape (581012, 54)] Each row corresponds to the 54 features in the dataset.

**dataset.target** [numpy array of shape (581012,)] Each value corresponds to one of the 7 forest covertypes with values ranging between 1 to 7.

dataset.DESCR [string] Description of the forest covertype dataset.

(data, target) [tuple if return\_X\_y is True] New in version 0.20.

## sklearn.datasets.fetch kddcup99

sklearn.datasets.**fetch\_kddcup99**(subset=None, data\_home=None, shuffle=False, random\_state=None, percent10=True, down-load\_if\_missing=True, return\_X\_y=False)

Load the kddcup99 dataset (classification).

Download it if necessary.

Classes	23
Samples total	4898431
Dimensionality	41
Features	discrete (int) or continuous (float)

Read more in the User Guide.

New in version 0.18.

#### **Parameters**

**subset** [None, 'SA', 'SF', 'http', 'smtp'] To return the corresponding classical subsets of kddcup 99. If None, return the entire kddcup 99 dataset.

**data\_home** [string, optional] Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders. .. versionadded:: 0.19

**shuffle** [bool, default=False] Whether to shuffle dataset.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset shuffling and for selection of abnormal samples if subset='SA'. Pass an int for reproducible output across multiple function calls. See *Glossary*.

**percent10** [bool, default=True] Whether to load only 10 percent of the data.

**download\_if\_missing** [bool, default=True] If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

data [Bunch]

**return\_X\_y** [boolean, default=False.] If True, returns (data, target) instead of a Bunch object. See below for more information about the data and *target* object.

New in version 0.20.

#### Returns

# Dictionary-like object, the interesting attributes are:

- 'data', the data to learn.
- 'target', the regression target for each sample.
- 'DESCR', a description of the dataset.

(data, target) [tuple if return\_X\_y is True] New in version 0.20.

# sklearn.datasets.fetch\_lfw\_pairs

sklearn.datasets.fetch\_lfw\_pairs(subset='train', data\_home=None, funneled=True, resize=0.5, color=False, slice\_=(slice(70, 195, None), slice(78, 172, None)), download\_if\_missing=True)

Load the Labeled Faces in the Wild (LFW) pairs dataset (classification).

Download it if necessary.

Classes	5749
Samples total	13233
Dimensionality	5828
Features	real, between 0 and 255

In the official README.txt this task is described as the "Restricted" task. As I am not sure as to implement the "Unrestricted" variant correctly, I left it as unsupported for now.

The original images are 250 x 250 pixels, but the default slice and resize arguments reduce them to 62 x 47. Read more in the *User Guide*.

# **Parameters**

**subset** [optional, default: 'train'] Select the dataset to load: 'train' for the development training set, 'test' for the development test set, and '10\_folds' for the official evaluation set that is meant to be used with a 10-folds cross validation.

**data\_home** [optional, default: None] Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders.

**funneled** [boolean, optional, default: True] Download and use the funneled variant of the dataset.

resize [float, optional, default 0.5] Ratio used to resize the each face picture.

**color** [boolean, optional, default False] Keep the 3 RGB channels instead of averaging them to a single gray level channel. If color is True the shape of the data has one more dimension than the shape with color = False.

**slice** [optional] Provide a custom 2D slice (height, width) to extract the 'interesting' part of the jpeg files and avoid use statistical correlation from the background

**download\_if\_missing** [optional, True by default] If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

#### Returns

#### The data is returned as a Bunch object with the following attributes:

data [numpy array of shape (2200, 5828). Shape depends on subset.] Each row corresponds to 2 ravel'd face images of original size 62 x 47 pixels. Changing the slice\_, resize or subset parameters will change the shape of the output.

pairs [numpy array of shape (2200, 2, 62, 47). Shape depends on subset] Each row has 2 face images corresponding to same or different person from the dataset containing 5749 people. Changing the slice\_, resize or subset parameters will change the shape of the output.

**target** [numpy array of shape (2200,). Shape depends on subset.] Labels associated to each pair of images. The two label values being different persons or the same person.

**DESCR** [string] Description of the Labeled Faces in the Wild (LFW) dataset.

# sklearn.datasets.fetch\_lfw\_people

sklearn.datasets.fetch\_lfw\_people (data\_home=None, funneled=True, resize=0.5, min\_faces\_per\_person=0, color=False, slice\_=(slice(70, 195, None), slice(78, 172, None)), download if missing=True, return X y=False)

Load the Labeled Faces in the Wild (LFW) people dataset (classification).

Download it if necessary.

Classes	5749
Samples total	13233
Dimensionality	5828
Features	real, between 0 and 255

Read more in the User Guide.

#### **Parameters**

**data\_home** [optional, default: None] Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders.

**funneled** [boolean, optional, default: True] Download and use the funneled variant of the dataset.

**resize** [float, optional, default 0.5] Ratio used to resize the each face picture.

min\_faces\_per\_person [int, optional, default None] The extracted dataset will only retain pictures of people that have at least min faces per person different pictures.

**color** [boolean, optional, default False] Keep the 3 RGB channels instead of averaging them to a single gray level channel. If color is True the shape of the data has one more dimension than the shape with color = False.

slice\_ [optional] Provide a custom 2D slice (height, width) to extract the 'interesting' part of the jpeg files and avoid use statistical correlation from the background

**download\_if\_missing** [optional, True by default] If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

return\_X\_y [boolean, default=False.] If True, returns (dataset.data, dataset.
target) instead of a Bunch object. See below for more information about the dataset.
data and dataset.target object.

New in version 0.20.

#### Returns

dataset [dict-like object with the following attributes:]

**dataset.data** [numpy array of shape (13233, 2914)] Each row corresponds to a ravelled face image of original size 62 x 47 pixels. Changing the slice\_ or resize parameters will change the shape of the output.

**dataset.images** [numpy array of shape (13233, 62, 47)] Each row is a face image corresponding to one of the 5749 people in the dataset. Changing the slice\_ or resize parameters will change the shape of the output.

**dataset.target** [numpy array of shape (13233,)] Labels associated to each face image. Those labels range from 0-5748 and correspond to the person IDs.

dataset.DESCR [string] Description of the Labeled Faces in the Wild (LFW) dataset.

(data, target) [tuple if return\_X\_y is True] New in version 0.20.

# Examples using sklearn.datasets.fetch\_lfw\_people

• Faces recognition example using eigenfaces and SVMs

# sklearn.datasets.fetch olivetti faces

Load the Olivetti faces data-set from AT&T (classification).

Download it if necessary.

Classes	40
Samples total	400
Dimensionality	4096
Features	real, between 0 and 1

Read more in the User Guide.

#### **Parameters**

**data\_home** [optional, default: None] Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit learn data' subfolders.

**shuffle** [boolean, optional] If True the order of the dataset is shuffled to avoid having images of the same person grouped.

**random\_state** [int, RandomState instance or None (default=0)] Determines random number generation for dataset shuffling. Pass an int for reproducible output across multiple function calls. See *Glossary*.

**download\_if\_missing** [optional, True by default] If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

#### Returns

## An object with the following attributes:

**data** [numpy array of shape (400, 4096)] Each row corresponds to a ravelled face image of original size 64 x 64 pixels.

**images** [numpy array of shape (400, 64, 64)] Each row is a face image corresponding to one of the 40 subjects of the dataset.

**target** [numpy array of shape (400, )] Labels associated to each face image. Those labels are ranging from 0-39 and correspond to the Subject IDs.

**DESCR** [string] Description of the modified Olivetti Faces Dataset.

# Examples using sklearn.datasets.fetch\_olivetti\_faces

- Face completion with a multi-output estimators
- Online learning of a dictionary of parts of faces
- Faces dataset decompositions
- Pixel importances with a parallel forest of trees

## sklearn.datasets.fetch openml

sklearn.datasets.fetch\_openml (name=None, version='active', data\_id=None, data\_home=None, target\_column='default-target', cache=True, return\_X\_y=False)
Fetch dataset from openml by name or dataset id.

Datasets are uniquely identified by either an integer ID or by a combination of name and version (i.e. there might be multiple versions of the 'iris' dataset). Please give either name or data\_id (not both). In case a name is given, a version can also be provided.

Read more in the User Guide.

# **Note:** EXPERIMENTAL

The API is experimental (particularly the return value structure), and might have small backward-incompatible changes in future releases.

#### **Parameters**

**name** [str or None] String identifier of the dataset. Note that OpenML can have multiple datasets with the same name.

**version** [integer or 'active', default='active'] Version of the dataset. Can only be provided if also name is given. If 'active' the oldest version that's still active is used. Since there may be more than one active version of a dataset, and those versions may fundamentally be different from one another, setting an exact version is highly recommended.

**data\_id** [int or None] OpenML ID of the dataset. The most specific way of retrieving a dataset. If data\_id is not given, name (and potential version) are used to obtain a dataset.

**data\_home** [string or None, default None] Specify another download and cache folder for the data sets. By default all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders.

target\_column [string, list or None, default 'default-target'] Specify the column name in the data to use as target. If 'default-target', the standard target column a stored on the server is used. If None, all columns are returned as data and the target is None. If list (of strings), all columns with these names are returned as multi-target (Note: not all scikit-learn classifiers can handle all types of multi-output combinations)

**cache** [boolean, default=True] Whether to cache downloaded datasets using joblib.

**return\_X\_y** [boolean, default=False.] If True, returns (data, target) instead of a Bunch object. See below for more information about the data and *target* objects.

#### Returns

data [Bunch] Dictionary-like object, with attributes:

**data** [np.array or scipy.sparse.csr\_matrix of floats] The feature matrix. Categorical features are encoded as ordinals.

**target** [np.array] The regression target or classification labels, if applicable. Dtype is float if numeric, and object if categorical.

**DESCR** [str] The full description of the dataset

**feature\_names** [list] The names of the dataset columns

**categories** [dict] Maps each categorical feature name to a list of values, such that the value encoded as i is ith in the list.

details [dict] More metadata from OpenML

(data, target) [tuple if return\_X\_y is True]

# **Note:** EXPERIMENTAL

This interface is **experimental** and subsequent releases may change attributes without notice (although there should only be minor changes to data and target).

Missing values in the 'data' are represented as NaN's. Missing values in 'target' are represented as NaN's (numerical target) or None (categorical target)

# Examples using sklearn.datasets.fetch\_openml

- Gaussian process regression (GPR) on Mauna Loa CO2 data.
- MNIST classfification using multinomial logistic + L1
- Early stopping of Stochastic Gradient Descent
- Classifier Chain
- Visualization of MLP weights on MNIST

# sklearn.datasets.fetch\_rcv1

 $sklearn.datasets. \textbf{fetch\_rcv1} (data\_home=None, \ subset='all', \ download\_if\_missing=True, \ random\_state=None, \ shuffle=False, \ return\_X\_y=False)$ 

Load the RCV1 multilabel dataset (classification).

Download it if necessary.

Version: RCV1-v2, vectors, full sets, topics multilabels.

Classes	103
Samples total	804414
Dimensionality	47236
Features	real, between 0 and 1

Read more in the *User Guide*.

New in version 0.17.

#### **Parameters**

**data\_home** [string, optional] Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders.

subset [string, 'train', 'test', or 'all', default='all'] Select the dataset to load: 'train' for the training set (23149 samples), 'test' for the test set (781265 samples), 'all' for both, with the training samples first if shuffle is False. This follows the official LYRL2004 chronological split.

**download\_if\_missing** [boolean, default=True] If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset shuffling. Pass an int for reproducible output across multiple function calls. See *Glossary*.

**shuffle** [bool, default=False] Whether to shuffle dataset.

return\_X\_y [boolean, default=False.] If True, returns (dataset.data, dataset.
target) instead of a Bunch object. See below for more information about the dataset.
data and dataset.target object.

New in version 0.20.

# Returns

dataset [dict-like object with the following attributes:]

dataset.data [scipy csr array, dtype np.float64, shape (804414, 47236)] The array has 0.16% of non zero values.

**dataset.target** [scipy csr array, dtype np.uint8, shape (804414, 103)] Each sample has a value of 1 in its categories, and 0 in others. The array has 3.15% of non zero values.

**dataset.sample\_id** [numpy array, dtype np.uint32, shape (804414,)] Identification number of each sample, as ordered in dataset.data.

**dataset.target\_names** [numpy array, dtype object, length (103)] Names of each target (RCV1 topics), as ordered in dataset.target.

dataset.DESCR [string] Description of the RCV1 dataset.

(data, target) [tuple if return\_X\_y is True] New in version 0.20.

## sklearn.datasets.fetch species distributions

sklearn.datasets.**fetch\_species\_distributions** (data\_home=None, load\_if\_missing=True)

Loader for species distribution dataset from Phillips et. al. (2006)

Read more in the *User Guide*.

#### **Parameters**

**data\_home** [optional, default: None] Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders.

**download\_if\_missing** [optional, True by default] If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

#### Returns

# The data is returned as a Bunch object with the following attributes:

**coverages** [array, shape = [14, 1592, 1212]] These represent the 14 features measured at each point of the map grid. The latitude/longitude values for the grid are discussed below. Missing data is represented by the value -9999.

train [record array, shape = (1624,)] The training points for the data. Each point has three fields:

- train['species'] is the species name
- train['dd long'] is the longitude, in degrees
- train['dd lat'] is the latitude, in degrees

**test** [record array, shape = (620,)] The test points for the data. Same format as the training data.

Nx, Ny [integers] The number of longitudes (x) and latitudes (y) in the grid

**x\_left\_lower\_corner**, **y\_left\_lower\_corner** [floats] The (x,y) position of the lower-left corner, in degrees

grid\_size [float] The spacing between points of the grid, in degrees

## **Notes**

This dataset represents the geographic distribution of species. The dataset is provided by Phillips et. al. (2006). The two species are:

- "Bradypus variegatus", the Brown-throated Sloth.
- "Microryzomys minutus", also known as the Forest Small Rice Rat, a rodent that lives in Peru, Colombia, Ecuador, Peru, and Venezuela.
- For an example of using this dataset with scikit-learn, see *exam-ples/applications/plot\_species\_distribution\_modeling.py*.

#### References

• "Maximum entropy modeling of species geographic distributions" S. J. Phillips, R. P. Anderson, R. E. Schapire - Ecological Modelling, 190:231-259, 2006.

# Examples using sklearn.datasets.fetch\_species\_distributions

- Species distribution modeling
- Kernel Density Estimate of Species Distributions

## sklearn.datasets.get data home

sklearn.datasets.get\_data\_home(data\_home=None)

Return the path of the scikit-learn data dir.

This folder is used by some large dataset loaders to avoid downloading the data several times.

By default the data dir is set to a folder named 'scikit\_learn\_data' in the user home folder.

Alternatively, it can be set by the 'SCIKIT\_LEARN\_DATA' environment variable or programmatically by giving an explicit folder path. The '~' symbol is expanded to the user home folder.

If the folder does not already exist, it is automatically created.

#### **Parameters**

**data\_home** [str | None] The path to scikit-learn data dir.

## Examples using sklearn.datasets.get\_data\_home

• Out-of-core classification of text documents

## sklearn.datasets.load boston

sklearn.datasets.load\_boston(return\_X\_y=False)

Load and return the boston house-prices dataset (regression).

Samples total	506
Dimensionality	13
Features	real, positive
Targets	real 5 50.

Read more in the *User Guide*.

## **Parameters**

**return\_X\_y** [boolean, default=False.] If True, returns (data, target) instead of a Bunch object. See below for more information about the data and *target* object.

New in version 0.18.

# Returns

**data** [Bunch] Dictionary-like object, the interesting attributes are: 'data', the data to learn, 'target', the regression targets, 'DESCR', the full description of the dataset, and 'filename', the physical location of boston csv dataset (added in version 0.20).

(data, target) [tuple if return\_X\_y is True] New in version 0.18.

#### **Notes**

Changed in version 0.20: Fixed a wrong data point at [445, 0].

# **Examples**

```
>>> from sklearn.datasets import load_boston
>>> boston = load_boston()
>>> print(boston.data.shape)
(506, 13)
```

# Examples using sklearn.datasets.load\_boston

- Outlier detection on a real data set
- Model Complexity Influence
- Effect of transforming the targets in regression model
- Plot individual and voting regression predictions
- Gradient Boosting regression
- Feature selection using SelectFromModel and LassoCV
- Imputing missing values before building an estimator
- Plotting Cross-Validated Predictions

# sklearn.datasets.load breast cancer

```
sklearn.datasets.load_breast_cancer (return_X_y=False)
Load and return the breast cancer wisconsin dataset (classification).
```

The breast cancer dataset is a classic and very easy binary classification dataset.

Classes	2
Samples per class	212(M),357(B)
Samples total	569
Dimensionality	30
Features	real, positive

Read more in the User Guide.

## **Parameters**

**return\_X\_y** [boolean, default=False] If True, returns (data, target) instead of a Bunch object. See below for more information about the data and *target* object.

New in version 0.18.

#### **Returns**

data [Bunch] Dictionary-like object, the interesting attributes are: 'data', the data to learn, 'target', the classification labels, 'target\_names', the meaning of the labels, 'feature\_names', the meaning of the features, and 'DESCR', the full description of the dataset, 'filename', the physical location of breast cancer csv dataset (added in version 0.20).

(data, target) [tuple if return\_X\_y is True] New in version 0.18.

The copy of UCI ML Breast Cancer Wisconsin (Diagnostic) dataset is downloaded from:

# https://goo.gl/U2Uwz2

# **Examples**

Let's say you are interested in the samples 10, 50, and 85, and want to know their class name.

```
>>> from sklearn.datasets import load_breast_cancer
>>> data = load_breast_cancer()
>>> data.target[[10, 50, 85]]
array([0, 1, 0])
>>> list(data.target_names)
['malignant', 'benign']
```

# sklearn.datasets.load\_diabetes

```
sklearn.datasets.load_diabetes (return_X_y=False)
Load and return the diabetes dataset (regression).
```

Samples total	442
Dimensionality	10
Features	real, $2 < x < .2$
Targets	integer 25 - 346

Read more in the User Guide.

#### **Parameters**

**return\_X\_y** [boolean, default=False.] If True, returns (data, target) instead of a Bunch object. See below for more information about the data and *target* object.

New in version 0.18.

# Returns

**data** [Bunch] Dictionary-like object, the interesting attributes are: 'data', the data to learn, 'target', the regression target for each sample, 'data\_filename', the physical location of diabetes data csv dataset, and 'target\_filename', the physical location of diabetes targets csv dataset (added in version 0.20).

(data, target) [tuple if return\_X\_y is True] New in version 0.18.

# Examples using sklearn.datasets.load\_diabetes

- Cross-validation on diabetes Dataset Exercise
- Imputing missing values before building an estimator
- Lasso path using LARS
- Linear Regression Example
- Sparsity Example: Fitting only features 1 and 2
- Lasso and Elastic Net
- Lasso model selection: Cross-Validation / AIC / BIC

## sklearn.datasets.load digits

```
sklearn.datasets.load_digits (n\_class=10, return\_X\_y=False)
Load and return the digits dataset (classification).
```

Each datapoint is a 8x8 image of a digit.

Classes	10
Samples per class	~180
Samples total	1797
Dimensionality	64
Features	integers 0-16

Read more in the User Guide.

#### **Parameters**

**n\_class** [integer, between 0 and 10, optional (default=10)] The number of classes to return.

**return\_X\_y** [boolean, default=False.] If True, returns (data, target) instead of a Bunch object. See below for more information about the data and *target* object.

New in version 0.18.

#### Returns

data [Bunch] Dictionary-like object, the interesting attributes are: 'data', the data to learn, 'images', the images corresponding to each sample, 'target', the classification labels for each sample, 'target\_names', the meaning of the labels, and 'DESCR', the full description of the dataset.

(data, target) [tuple if return\_X\_y is True] New in version 0.18.

This is a copy of the test set of the UCI ML hand-written digits datasets

https://archive.ics.uci.edu/ml/datasets/Optical+Recognition+of+Handwritten+Digits

# **Examples**

To load the data and visualize the images:

```
>>> from sklearn.datasets import load_digits
>>> digits = load_digits()
>>> print(digits.data.shape)
(1797, 64)
>>> import matplotlib.pyplot as plt
>>> plt.gray()
>>> plt.matshow(digits.images[0])
>>> plt.show()
```

#### Examples using sklearn.datasets.load digits

- The Johnson-Lindenstrauss bound for embedding with random projections
- Explicit feature map approximation for RBF kernels
- · Recognizing hand-written digits

- Feature agglomeration
- Various Agglomerative Clustering on a 2D embedding of digits
- A demo of K-Means clustering on the handwritten digits data
- Pipelining: chaining a PCA and a logistic regression
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- The Digit Dataset
- Early stopping of Gradient Boosting
- Digits Classification Exercise
- Cross-validation on Digits Dataset Exercise
- Recursive feature elimination
- Comparing various online solvers
- L1 Penalty and Sparsity in Logistic Regression
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...
- Plotting Validation Curves
- Parameter estimation using grid search with cross-validation
- · Comparing randomized search and grid search for hyperparameter estimation
- Balance model complexity and cross-validated score
- Plotting Learning Curves
- Kernel Density Estimation
- Dimensionality Reduction with Neighborhood Components Analysis
- Restricted Boltzmann Machine features for digit classification
- Compare Stochastic learning strategies for MLPClassifier
- Label Propagation digits: Demonstrating performance
- · Label Propagation digits active learning

# sklearn.datasets.load files

```
sklearn.datasets. \textbf{load\_files} (container\_path, \\ load\_content=True, \\ shuffle=True, \\ encoding=None, \\ decode\_error='strict', random\_state=0)
```

Load text files with categories as subfolder names.

Individual samples are assumed to be files stored a two levels folder structure such as the following:

```
container_folder/
```

```
category_1_folder/ file_1.txt file_2.txt ... file_42.txt category_2_folder/ file_43.txt file_44.txt ...
```

The folder names are used as supervised signal label names. The individual file names are not important.

This function does not try to extract features into a numpy array or scipy sparse matrix. In addition, if load\_content is false it does not try to load the files in memory.

To use text files in a scikit-learn classification or clustering algorithm, you will need to use the <code>sklearn.feature\_extraction.text</code> module to build a feature extraction transformer that suits your problem.

If you set load\_content=True, you should also specify the encoding of the text using the 'encoding' parameter. For many modern text files, 'utf-8' will be the correct encoding. If you leave encoding equal to None, then the content will be made of bytes instead of Unicode, and you will not be able to use most functions in <code>sklearn.feature extraction.text</code>.

Similar feature extractors should be built for other kind of unstructured data input such as images, audio, video, ...

Read more in the *User Guide*.

#### **Parameters**

container\_path [string or unicode] Path to the main folder holding one subfolder per category

**description** [string or unicode, optional (default=None)] A paragraph describing the characteristic of the dataset: its source, reference, etc.

**categories** [A collection of strings or None, optional (default=None)] If None (default), load all the categories. If not None, list of category names to load (other categories ignored).

**load\_content** [boolean, optional (default=True)] Whether to load or not the content of the different files. If true a 'data' attribute containing the text information is present in the data structure returned. If not, a filenames attribute gives the path to the files.

**shuffle** [bool, optional (default=True)] Whether or not to shuffle the data: might be important for models that make the assumption that the samples are independent and identically distributed (i.i.d.), such as stochastic gradient descent.

encoding [string or None (default is None)] If None, do not try to decode the content of the files (e.g. for images or other non-text content). If not None, encoding to use to decode text files to Unicode if load\_content is True.

**decode\_error** [{'strict', 'ignore', 'replace'}, optional] Instruction on what to do if a byte sequence is given to analyze that contains characters not of the given encoding. Passed as keyword argument 'errors' to bytes.decode.

**random\_state** [int, RandomState instance or None (default=0)] Determines random number generation for dataset shuffling. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

**data** [Bunch] Dictionary-like object, the interesting attributes are: either data, the raw text data to learn, or 'filenames', the files holding it, 'target', the classification labels (integer index), 'target\_names', the meaning of the labels, and 'DESCR', the full description of the dataset.

# sklearn.datasets.load iris

```
sklearn.datasets.load_iris(return_X_y=False)
```

Load and return the iris dataset (classification).

The iris dataset is a classic and very easy multi-class classification dataset.

Classes	3
Samples per class	50
Samples total	150
Dimensionality	4
Features	real, positive

Read more in the User Guide.

#### **Parameters**

**return\_X\_y** [boolean, default=False.] If True, returns (data, target) instead of a Bunch object. See below for more information about the data and *target* object.

New in version 0.18.

#### Returns

**data** [Bunch] Dictionary-like object, the interesting attributes are: 'data', the data to learn, 'target', the classification labels, 'target\_names', the meaning of the labels, 'feature\_names', the meaning of the features, 'DESCR', the full description of the dataset, 'filename', the physical location of iris csv dataset (added in version 0.20).

(data, target) [tuple if return\_X\_y is True] New in version 0.18.

#### **Notes**

Changed in version 0.20: Fixed two wrong data points according to Fisher's paper. The new version is the same as in R, but not as in the UCI Machine Learning Repository.

# **Examples**

Let's say you are interested in the samples 10, 25, and 50, and want to know their class name.

```
>>> from sklearn.datasets import load_iris
>>> data = load_iris()
>>> data.target[[10, 25, 50]]
array([0, 0, 1])
>>> list(data.target_names)
['setosa', 'versicolor', 'virginica']
```

# Examples using sklearn.datasets.load\_iris

- Plot classification probability
- K-means Clustering
- Concatenating multiple feature extraction methods
- The Iris Dataset
- PCA example with Iris Data-set
- Incremental PCA
- · Comparison of LDA and PCA 2D projection of Iris dataset
- Plot the decision boundaries of a VotingClassifier

- Early stopping of Gradient Boosting
- Plot the decision surfaces of ensembles of trees on the iris dataset
- SVM Exercise
- Test with permutations the significance of a classification score
- Univariate Feature Selection
- Gaussian process classification (GPC) on iris dataset
- Regularization path of L1- Logistic Regression
- Logistic Regression 3-class Classifier
- Plot multi-class SGD on the iris dataset
- GMM covariances
- Receiver Operating Characteristic (ROC) with cross validation
- Nested versus non-nested cross-validation
- Confusion matrix
- Receiver Operating Characteristic (ROC)
- Precision-Recall
- Nearest Neighbors Classification
- Nearest Centroid Classification
- Comparing Nearest Neighbors with and without Neighborhood Components Analysis
- Compare Stochastic learning strategies for MLPClassifier
- Decision boundary of label propagation versus SVM on the Iris dataset
- SVM with custom kernel
- SVM-Anova: SVM with univariate feature selection
- Plot different SVM classifiers in the iris dataset
- RBF SVM parameters
- Plot the decision surface of a decision tree on the iris dataset
- Understanding the decision tree structure

# sklearn.datasets.load linnerud

 $\verb|sklearn.datasets.load_linnerud| (\textit{return}\_X\_y = False)$ 

Load and return the linnerud dataset (multivariate regression).

Samples total	20
Dimensionality	3 (for both data and target)
Features	integer
Targets	integer

Read more in the User Guide.

# **Parameters**

**return\_X\_y** [boolean, default=False.] If True, returns (data, target) instead of a Bunch object. See below for more information about the data and *target* object.

New in version 0.18.

#### Returns

data [Bunch] Dictionary-like object, the interesting attributes are: 'data' and 'target', the two multivariate datasets, with 'data' corresponding to the exercise and 'target' corresponding to the physiological measurements, as well as 'feature\_names' and 'target\_names'. In addition, you will also have access to 'data\_filename', the physical location of linnerud data csv dataset, and 'target\_filename', the physical location of linnerud targets csv datataset (added in version 0.20).

(data, target) [tuple if return\_X\_y is True] New in version 0.18.

# sklearn.datasets.load sample image

```
\verb|sklearn.datasets.load_sample_image|(image_name)|
```

Load the numpy array of a single sample image

Read more in the User Guide.

## **Parameters**

```
image_name [{china.jpg, flower.jpg}] The name of the sample image loaded
```

#### Returns

img [3D array] The image as a numpy array: height x width x color

# **Examples**

```
>>> from sklearn.datasets import load_sample_image
>>> china = load_sample_image('china.jpg')
>>> china.dtype
dtype('uint8')
>>> china.shape
(427, 640, 3)
>>> flower = load_sample_image('flower.jpg')
>>> flower.dtype
dtype('uint8')
>>> flower.shape
(427, 640, 3)
```

# Examples using sklearn.datasets.load\_sample\_image

• Color Quantization using K-Means

# sklearn.datasets.load sample images

```
sklearn.datasets.load_sample_images()
```

Load sample images for image manipulation.

Loads both, china and flower.

Read more in the *User Guide*.

#### Returns

**data** [Bunch] Dictionary-like object with the following attributes: 'images', the two sample images, 'filenames', the file names for the images, and 'DESCR' the full description of the dataset.

# **Examples**

To load the data and visualize the images:

```
>>> from sklearn.datasets import load_sample_images
>>> dataset = load_sample_images()
>>> len(dataset.images)
2
>>> first_img_data = dataset.images[0]
>>> first_img_data.shape
(427, 640, 3)
>>> first_img_data.dtype
dtype('uint8')
```

# sklearn.datasets.load symlight file

```
sklearn.datasets.load_svmlight_file (f, n_features=None, dtype=<class 'numpy.float64'>, multilabel=False, zero_based='auto', query_id=False, offset=0.length=-1)
```

Load datasets in the symlight / libsym format into sparse CSR matrix

This format is a text-based format, with one sample per line. It does not store zero valued features hence is suitable for sparse dataset.

The first element of each line can be used to store a target variable to predict.

This format is used as the default format for both symlight and the libsym command line programs.

Parsing a text based source can be expensive. When working on repeatedly on the same dataset, it is recommended to wrap this loader with joblib.Memory.cache to store a memmapped backup of the CSR results of the first call and benefit from the near instantaneous loading of memmapped structures for the subsequent calls.

In case the file contains a pairwise preference constraint (known as "qid" in the symlight format) these are ignored unless the query\_id parameter is set to True. These pairwise preference constraints can be used to constraint the combination of samples when using pairwise loss functions (as is the case in some learning to rank problems) so that only pairs with the same query\_id value are considered.

This implementation is written in Cython and is reasonably fast. However, a faster API-compatible loader is also available at:

https://github.com/mblondel/svmlight-loader

#### **Parameters**

f [{str, file-like, int}] (Path to) a file to load. If a path ends in ".gz" or ".bz2", it will be uncompressed on the fly. If an integer is passed, it is assumed to be a file descriptor. A file-like or file descriptor will not be closed by this function. A file-like object must be opened in binary mode.

- n\_features [int or None] The number of features to use. If None, it will be inferred. This argument is useful to load several files that are subsets of a bigger sliced dataset: each subset might not have examples of every feature, hence the inferred shape might vary from one slice to another. n\_features is only required if offset or length are passed a non-default value.
- **dtype** [numpy data type, default np.float64] Data type of dataset to be loaded. This will be the data type of the output numpy arrays X and y.
- **multilabel** [boolean, optional, default False] Samples may have several labels each (see https://www.csie.ntu.edu.tw/~cjlin/libsvmtools/datasets/multilabel.html)
- zero\_based [boolean or "auto", optional, default "auto"] Whether column indices in f are zero-based (True) or one-based (False). If column indices are one-based, they are transformed to zero-based to match Python/NumPy conventions. If set to "auto", a heuristic check is applied to determine this from the file contents. Both kinds of files occur "in the wild", but they are unfortunately not self-identifying. Using "auto" or True should always be safe when no offset or length is passed. If offset or length are passed, the "auto" mode falls back to zero\_based=True to avoid having the heuristic check yield inconsistent results on different segments of the file.
- query\_id [boolean, default False] If True, will return the query\_id array for each file.
- **offset** [integer, optional, default 0] Ignore the offset first bytes by seeking forward, then discarding the following bytes up until the next new line character.
- **length** [integer, optional, default -1] If strictly positive, stop reading any new line of data once the position in the file has reached the (offset + length) bytes threshold.

#### Returns

- **X** [scipy.sparse matrix of shape (n\_samples, n\_features)]
- y [ndarray of shape (n\_samples,), or, in the multilabel a list of] tuples of length n\_samples.
- **query\_id** [array of shape (n\_samples,)] query\_id for each sample. Only returned when query\_id is set to True.

## See also:

load\_svmlight\_files similar function for loading multiple files in this format, enforcing the same number of features/columns on all of them.

## **Examples**

To use joblib. Memory to cache the symlight file:

```
from joblib import Memory
from .datasets import load_svmlight_file
mem = Memory("./mycache")

@mem.cache
def get_data():
    data = load_svmlight_file("mysvmlightfile")
    return data[0], data[1]

X, y = get_data()
```

## sklearn.datasets.load symlight files

```
sklearn.datasets.load_svmlight_files(files, n_features=None, dtype=<class 'numpy.float64'>, multilabel=False, zero_based='auto', query_id=False, offset=0, length=-1)
```

Load dataset from multiple files in SVMlight format

This function is equivalent to mapping load\_symlight\_file over a list of files, except that the results are concatenated into a single, flat list and the samples vectors are constrained to all have the same number of features.

In case the file contains a pairwise preference constraint (known as "qid" in the symlight format) these are ignored unless the query\_id parameter is set to True. These pairwise preference constraints can be used to constraint the combination of samples when using pairwise loss functions (as is the case in some learning to rank problems) so that only pairs with the same query\_id value are considered.

#### **Parameters**

- **files** [iterable over {str, file-like, int}] (Paths of) files to load. If a path ends in ".gz" or ".bz2", it will be uncompressed on the fly. If an integer is passed, it is assumed to be a file descriptor. File-likes and file descriptors will not be closed by this function. File-like objects must be opened in binary mode.
- **n\_features** [int or None] The number of features to use. If None, it will be inferred from the maximum column index occurring in any of the files.
  - This can be set to a higher value than the actual number of features in any of the input files, but setting it to a lower value will cause an exception to be raised.
- **dtype** [numpy data type, default np.float64] Data type of dataset to be loaded. This will be the data type of the output numpy arrays X and y.
- **multilabel** [boolean, optional] Samples may have several labels each (see https://www.csie.ntu.edu.tw/~cjlin/libsvmtools/datasets/multilabel.html)
- zero\_based [boolean or "auto", optional] Whether column indices in f are zero-based (True) or one-based (False). If column indices are one-based, they are transformed to zero-based to match Python/NumPy conventions. If set to "auto", a heuristic check is applied to determine this from the file contents. Both kinds of files occur "in the wild", but they are unfortunately not self-identifying. Using "auto" or True should always be safe when no offset or length is passed. If offset or length are passed, the "auto" mode falls back to zero\_based=True to avoid having the heuristic check yield inconsistent results on different segments of the file.
- query\_id [boolean, defaults to False] If True, will return the query\_id array for each file.
- **offset** [integer, optional, default 0] Ignore the offset first bytes by seeking forward, then discarding the following bytes up until the next new line character.
- **length** [integer, optional, default -1] If strictly positive, stop reading any new line of data once the position in the file has reached the (offset + length) bytes threshold.

# Returns

```
[X1, y1, ..., Xn, yn]
where each (Xi, yi) pair is the result from load_svmlight_file(files[i]).
If query_id is set to True, this will return instead [X1, y1, q1, ..., Xn, yn, qn] where (Xi, yi, qi) is the result from load_svmlight_file(files[i])
```

See also:

#### load symlight file

#### **Notes**

When fitting a model to a matrix  $X_{train}$  and evaluating it against a matrix  $X_{train}$  it is essential that  $X_{train}$  and  $X_{test}$  have the same number of features ( $X_{train.shape}[1] == X_{test.shape}[1]$ ). This may not be the case if you load the files individually with load\_symlight\_file.

### sklearn.datasets.load wine

```
sklearn.datasets.load_wine(return_X_y=False)
```

Load and return the wine dataset (classification).

New in version 0.18.

The wine dataset is a classic and very easy multi-class classification dataset.

Classes	3
Samples per class	[59,71,48]
Samples total	178
Dimensionality	13
Features	real, positive

Read more in the User Guide.

#### **Parameters**

**return\_X\_y** [boolean, default=False.] If True, returns (data, target) instead of a Bunch object. See below for more information about the data and *target* object.

### Returns

data [Bunch] Dictionary-like object, the interesting attributes are: 'data', the data to learn, 'target', the classification labels, 'target\_names', the meaning of the labels, 'feature\_names', the meaning of the features, and 'DESCR', the full description of the dataset.

```
(data, target) [tuple if return_X_y is True]
```

The copy of UCI ML Wine Data Set dataset is downloaded and modified to fit standard format from:

https://archive.ics.uci.edu/ml/machine-learning-databases/wine/wine.data

### **Examples**

Let's say you are interested in the samples 10, 80, and 140, and want to know their class name.

```
>>> from sklearn.datasets import load_wine
>>> data = load_wine()
>>> data.target[[10, 80, 140]]
array([0, 1, 2])
>>> list(data.target_names)
['class_0', 'class_1', 'class_2']
```

# Examples using sklearn.datasets.load\_wine

• Importance of Feature Scaling

# 6.8.2 Samples generator

datasets.make_biclusters(shape, n_clusters)	Generate an array with constant block diagonal structure
	for biclustering.
datasets.make_blobs([n_samples, n_features,])	Generate isotropic Gaussian blobs for clustering.
datasets.make_checkerboard(shape, n_clusters)	Generate an array with block checkerboard structure for bi-
	clustering.
datasets.make_circles([n_samples, shuffle,])	Make a large circle containing a smaller circle in 2d.
datasets.make_classification([n_samples,	Generate a random n-class classification problem.
])	
datasets.make_friedman1([n_samples,])	Generate the "Friedman #1" regression problem
datasets.make_friedman2([n_samples, noise,	Generate the "Friedman #2" regression problem
])	
datasets.make_friedman3([n_samples, noise,	Generate the "Friedman #3" regression problem
])	
datasets.make_gaussian_quantiles([mean,	Generate isotropic Gaussian and label samples by quantile
])	
datasets.make_hastie_10_2([n_samples,])	Generates data for binary classification used in Hastie et al.
datasets.make_low_rank_matrix([n_samples,	Generate a mostly low rank matrix with bell-shaped singu-
])	lar values
datasets.make_moons([n_samples, shuffle,])	Make two interleaving half circles
datasets.make_multilabel_classification([	Generate a random multilabel classification problem.
datasets.make_regression([n_samples,])	Generate a random regression problem.
datasets.make_s_curve([n_samples, noise,])	Generate an S curve dataset.
datasets.make_sparse_coded_signal(n_sample	s,Generate a signal as a sparse combination of dictionary el-
)	ements.
datasets.make_sparse_spd_matrix([dim,])	Generate a sparse symmetric definite positive matrix.
datasets.make_sparse_uncorrelated([])	Generate a random regression problem with sparse uncor-
	related design
datasets.make_spd_matrix(n_dim[, ran-	Generate a random symmetric, positive-definite matrix.
dom_state])	-
datasets.make_swiss_roll([n_samples, noise,	Generate a swiss roll dataset.
])	

# sklearn.datasets.make\_biclusters

 $sklearn.datasets. \textbf{make\_biclusters} \ (shape, n\_clusters, noise=0.0, minval=10, maxval=100, shuffle=True, random\_state=None)$ 

Generate an array with constant block diagonal structure for biclustering.

Read more in the User Guide.

# **Parameters**

**shape** [iterable (n\_rows, n\_cols)] The shape of the result.

**n\_clusters** [integer] The number of biclusters.

**noise** [float, optional (default=0.0)] The standard deviation of the gaussian noise.

**minval** [int, optional (default=10)] Minimum value of a bicluster.

maxval [int, optional (default=100)] Maximum value of a bicluster.

**shuffle** [boolean, optional (default=True)] Shuffle the samples.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

**X** [array of shape shape] The generated array.

**rows** [array of shape (n\_clusters, X.shape[0],)] The indicators for cluster membership of each row.

**cols** [array of shape (n\_clusters, X.shape[1],)] The indicators for cluster membership of each column.

#### See also:

make\_checkerboard

#### References

*[11]* 

### Examples using sklearn.datasets.make\_biclusters

• A demo of the Spectral Co-Clustering algorithm

#### sklearn.datasets.make\_blobs

sklearn.datasets.make\_blobs ( $n\_samples=100$ ,  $n\_features=2$ , centers=None,  $cluster\_std=1.0$ ,  $center\_box=(-10.0, 10.0)$ , shuffle=True,  $random\_state=None$ ) Generate isotropic Gaussian blobs for clustering.

Read more in the *User Guide*.

### **Parameters**

- **n\_samples** [int or array-like, optional (default=100)] If int, it is the total number of points equally divided among clusters. If array-like, each element of the sequence indicates the number of samples per cluster.
- **n\_features** [int, optional (default=2)] The number of features for each sample.
- **centers** [int or array of shape [n\_centers, n\_features], optional] (default=None) The number of centers to generate, or the fixed center locations. If n\_samples is an int and centers is None, 3 centers are generated. If n\_samples is array-like, centers must be either None or an array of length equal to the length of n\_samples.
- **cluster\_std** [float or sequence of floats, optional (default=1.0)] The standard deviation of the clusters.
- **center\_box** [pair of floats (min, max), optional (default=(-10.0, 10.0))] The bounding box for each cluster center when centers are generated at random.

**shuffle** [boolean, optional (default=True)] Shuffle the samples.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

### Returns

- **X** [array of shape [n\_samples, n\_features]] The generated samples.
- y [array of shape [n\_samples]] The integer labels for cluster membership of each sample.

#### See also:

make\_classification a more intricate variant

# **Examples**

#### Examples using sklearn.datasets.make\_blobs

- Comparing anomaly detection algorithms for outlier detection on toy datasets
- Probability calibration of classifiers
- Probability Calibration for 3-class classification
- Normal and Shrinkage Linear Discriminant Analysis for classification
- A demo of the mean-shift clustering algorithm
- Demonstration of k-means assumptions
- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- Inductive Clustering
- Compare BIRCH and MiniBatchKMeans
- Comparison of the K-Means and MiniBatchKMeans clustering algorithms
- · Comparing different hierarchical linkage methods on toy datasets
- Selecting the number of clusters with silhouette analysis on KMeans clustering
- · Comparing different clustering algorithms on toy datasets

- Plot randomly generated classification dataset
- SGD: Maximum margin separating hyperplane
- Plot multinomial and One-vs-Rest Logistic Regression
- Demonstrating the different strategies of KBinsDiscretizer
- SVM: Maximum margin separating hyperplane
- SVM: Separating hyperplane for unbalanced classes

### sklearn.datasets.make checkerboard

sklearn.datasets.make\_checkerboard(shape, n\_clusters, noise=0.0, minval=10, maxval=100, shuffle=True, random state=None)

Generate an array with block checkerboard structure for biclustering.

Read more in the *User Guide*.

#### **Parameters**

**shape** [iterable (n\_rows, n\_cols)] The shape of the result.

n\_clusters [integer or iterable (n\_row\_clusters, n\_column\_clusters)] The number of row and column clusters.

**noise** [float, optional (default=0.0)] The standard deviation of the gaussian noise.

minval [int, optional (default=10)] Minimum value of a bicluster.

maxval [int, optional (default=100)] Maximum value of a bicluster.

**shuffle** [boolean, optional (default=True)] Shuffle the samples.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

**X** [array of shape shape] The generated array.

**rows** [array of shape (n\_clusters, X.shape[0],)] The indicators for cluster membership of each row.

**cols** [array of shape (n\_clusters, X.shape[1],)] The indicators for cluster membership of each column.

#### See also:

make\_biclusters

### References

[1]

# Examples using sklearn.datasets.make\_checkerboard

• A demo of the Spectral Biclustering algorithm

### sklearn.datasets.make circles

```
sklearn.datasets.make_circles (n_samples=100, shuffle=True, noise=None, random_state=None, factor=0.8)
```

Make a large circle containing a smaller circle in 2d.

A simple toy dataset to visualize clustering and classification algorithms.

Read more in the User Guide.

#### **Parameters**

**n\_samples** [int, optional (default=100)] The total number of points generated. If odd, the inner circle will have one point more than the outer circle.

**shuffle** [bool, optional (default=True)] Whether to shuffle the samples.

noise [double or None (default=None)] Standard deviation of Gaussian noise added to the data.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset shuffling and noise. Pass an int for reproducible output across multiple function calls. See *Glossary*.

**factor** [0 < double < 1 (default=.8)] Scale factor between inner and outer circle.

#### Returns

- **X** [array of shape [n\_samples, 2]] The generated samples.
- y [array of shape [n\_samples]] The integer labels (0 or 1) for class membership of each sample.

### Examples using sklearn.datasets.make\_circles

- Classifier comparison
- Comparing different hierarchical linkage methods on toy datasets
- · Comparing different clustering algorithms on toy datasets
- Kernel PCA
- Hashing feature transformation using Totally Random Trees
- t-SNE: The effect of various perplexity values on the shape
- Varying regularization in Multi-layer Perceptron
- Compare Stochastic learning strategies for MLPClassifier
- Feature discretization
- Label Propagation learning a complex structure

# sklearn.datasets.make\_classification

```
sklearn.datasets.make_classification (n\_samples=100, n\_features=20, n\_informative=2, n\_redundant=2, n\_repeated=0, n\_classes=2, n\_classes=2, n\_clusters\_per\_class=2, n\_class\_sep=1.0, n\_shuffle=True, n\_shuffle
```

Generate a random n-class classification problem.

This initially creates clusters of points normally distributed (std=1) about vertices of an n\_informative-dimensional hypercube with sides of length 2\*class\_sep and assigns an equal number of clusters to each class. It introduces interdependence between these features and adds various types of further noise to the data.

Without shuffling, X horizontally stacks features in the following order: the primary  $n_informative$  features, followed by  $n_redundant$  linear combinations of the informative features, followed by  $n_redundant$  duplicates, drawn randomly with replacement from the informative and redundant features. The remaining features are filled with random noise. Thus, without shuffling, all useful features are contained in the columns  $X[:, :n_informative + n_redundant + n_repeated]$ .

Read more in the User Guide.

#### **Parameters**

- **n\_samples** [int, optional (default=100)] The number of samples.
- n features [int, optional (default=20)] The total number of fea-These comprise n\_informative informative features. tures. n\_repeated duplicated redundant features, features and n\_redundant n\_features-n\_informative-n\_redundant-n\_repeated useless drawn at random.
- **n\_informative** [int, optional (default=2)] The number of informative features. Each class is composed of a number of gaussian clusters each located around the vertices of a hypercube in a subspace of dimension  $n_{informative}$ . For each cluster, informative features are drawn independently from N(0, 1) and then randomly linearly combined within each cluster in order to add covariance. The clusters are then placed on the vertices of the hypercube.
- **n\_redundant** [int, optional (default=2)] The number of redundant features. These features are generated as random linear combinations of the informative features.
- **n\_repeated** [int, optional (default=0)] The number of duplicated features, drawn randomly from the informative and the redundant features.
- n\_classes [int, optional (default=2)] The number of classes (or labels) of the classification problem.
- **n\_clusters\_per\_class** [int, optional (default=2)] The number of clusters per class.
- weights [list of floats or None (default=None)] The proportions of samples assigned to each class. If None, then classes are balanced. Note that if len (weights) == n\_classes 1, then the last class weight is automatically inferred. More than n\_samples samples may be returned if the sum of weights exceeds 1.
- **flip\_y** [float, optional (default=0.01)] The fraction of samples whose class are randomly exchanged. Larger values introduce noise in the labels and make the classification task harder.
- **class\_sep** [float, optional (default=1.0)] The factor multiplying the hypercube size. Larger values spread out the clusters/classes and make the classification task easier.
- **hypercube** [boolean, optional (default=True)] If True, the clusters are put on the vertices of a hypercube. If False, the clusters are put on the vertices of a random polytope.
- **shift** [float, array of shape [n\_features] or None, optional (default=0.0)] Shift features by the specified value. If None, then features are shifted by a random value drawn in [-class\_sep, class\_sep].
- **scale** [float, array of shape [n\_features] or None, optional (default=1.0)] Multiply features by the specified value. If None, then features are scaled by a random value drawn in [1, 100]. Note that scaling happens after shifting.
- **shuffle** [boolean, optional (default=True)] Shuffle the samples and the features.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

- **X** [array of shape [n\_samples, n\_features]] The generated samples.
- **y** [array of shape [n\_samples]] The integer labels for class membership of each sample.

#### See also:

```
make_blobs simplified variant
make_multilabel_classification unrelated generator for multilabel tasks
```

#### **Notes**

The algorithm is adapted from Guyon [1] and was designed to generate the "Madelon" dataset.

# References

[1]

# Examples using sklearn.datasets.make\_classification

- Comparison of Calibration of Classifiers
- Probability Calibration curves
- Classifier comparison
- Plot randomly generated classification dataset
- Feature importances with forests of trees
- OOB Errors for Random Forests
- Feature transformations with ensembles of trees
- Pipeline Anova SVM
- Recursive feature elimination with cross-validation
- Neighborhood Components Analysis Illustration
- Varying regularization in Multi-layer Perceptron
- Feature discretization
- Scaling the regularization parameter for SVCs

# sklearn.datasets.make\_friedman1

```
sklearn.datasets.make_friedman1 (n_samples=100, n_features=10, noise=0.0, ran-dom_state=None)

Generate the "Friedman #1" regression problem

This dataset is described in Friedman [1] and Breiman [2].
```

Inputs X are independent features uniformly distributed on the interval [0, 1]. The output y is created according to the formula:

```
y(X) = 10 * sin(pi * X[:, 0] * X[:, 1]) + 20 * (X[:, 2] - 0.5) ** 2 + 10 * X[:, 3] + 5 * X[:, 4] + noise * N(0, 1).
```

Out of the n\_features features, only 5 are actually used to compute y. The remaining features are independent of y.

The number of features has to be  $\geq 5$ .

Read more in the User Guide.

#### **Parameters**

- **n\_samples** [int, optional (default=100)] The number of samples.
- **n\_features** [int, optional (default=10)] The number of features. Should be at least 5.
- **noise** [float, optional (default=0.0)] The standard deviation of the gaussian noise applied to the output.
- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset noise. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

- **X** [array of shape [n\_samples, n\_features]] The input samples.
- y [array of shape [n\_samples]] The output values.

### References

[1], [2]

# ${\tt sklearn.datasets.make\_friedman2}$

```
sklearn.datasets.make_friedman2 (n_samples=100, noise=0.0, random_state=None)
Generate the "Friedman #2" regression problem
```

This dataset is described in Friedman [1] and Breiman [2].

Inputs *X* are 4 independent features uniformly distributed on the intervals:

```
0 <= X[:, 0] <= 100,

40 * pi <= X[:, 1] <= 560 * pi,

0 <= X[:, 2] <= 1,

1 <= X[:, 3] <= 11.
```

The output *y* is created according to the formula:

```
y(X) = (X[:, 0] ** 2 + (X[:, 1] * X[:, 2] - 1 / (X[:, 1] * X[:, 3])) ** 2) ** 0.
\hookrightarrow 5 + \text{noise} * N(0, 1).
```

Read more in the *User Guide*.

# **Parameters**

**n samples** [int, optional (default=100)] The number of samples.

**noise** [float, optional (default=0.0)] The standard deviation of the gaussian noise applied to the output.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset noise. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

- **X** [array of shape [n\_samples, 4]] The input samples.
- y [array of shape [n\_samples]] The output values.

#### References

[1], [2]

# sklearn.datasets.make\_friedman3

```
sklearn.datasets.make_friedman3 (n_samples=100, noise=0.0, random_state=None)
Generate the "Friedman #3" regression problem
```

This dataset is described in Friedman [1] and Breiman [2].

Inputs *X* are 4 independent features uniformly distributed on the intervals:

```
0 <= X[:, 0] <= 100,

40 * pi <= X[:, 1] <= 560 * pi,

0 <= X[:, 2] <= 1,

1 <= X[:, 3] <= 11.
```

The output *y* is created according to the formula:

```
y(X) = arctan((X[:, 1] * X[:, 2] - 1 / (X[:, 1] * X[:, 3])) / X[:, 0]) + noise *_ \limin N(0, 1).
```

Read more in the User Guide.

#### **Parameters**

- **n\_samples** [int, optional (default=100)] The number of samples.
- **noise** [float, optional (default=0.0)] The standard deviation of the gaussian noise applied to the output.
- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset noise. Pass an int for reproducible output across multiple function calls. See *Glossary*.

### Returns

- **X** [array of shape [n\_samples, 4]] The input samples.
- y [array of shape [n\_samples]] The output values.

### References

[1], [2]

### sklearn.datasets.make gaussian quantiles

```
sklearn.datasets.make_gaussian_quantiles (mean=None, cov=1.0, n\_samples=100, n\_features=2, n\_classes=3, shuffle=True, random\_state=None)
```

Generate isotropic Gaussian and label samples by quantile

This classification dataset is constructed by taking a multi-dimensional standard normal distribution and defining classes separated by nested concentric multi-dimensional spheres such that roughly equal numbers of samples are in each class (quantiles of the  $\chi^2$  distribution).

Read more in the User Guide.

#### **Parameters**

- **mean** [array of shape [n\_features], optional (default=None)] The mean of the multi-dimensional normal distribution. If None then use the origin (0, 0, ...).
- **cov** [float, optional (default=1.)] The covariance matrix will be this value times the unit matrix. This dataset only produces symmetric normal distributions.
- **n\_samples** [int, optional (default=100)] The total number of points equally divided among classes.
- **n\_features** [int, optional (default=2)] The number of features for each sample.
- **n\_classes** [int, optional (default=3)] The number of classes
- shuffle [boolean, optional (default=True)] Shuffle the samples.
- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

# Returns

- **X** [array of shape [n\_samples, n\_features]] The generated samples.
- y [array of shape [n\_samples]] The integer labels for quantile membership of each sample.

#### **Notes**

The dataset is from Zhu et al [1].

# References

[1]

### Examples using sklearn.datasets.make\_gaussian\_quantiles

- Plot randomly generated classification dataset
- Two-class AdaBoost
- Multi-class AdaBoosted Decision Trees

### sklearn.datasets.make hastie 10 2

sklearn.datasets.make\_hastie\_10\_2 (n\_samples=12000, random\_state=None) Generates data for binary classification used in Hastie et al. 2009, Example 10.2.

The ten features are standard independent Gaussian and the target y is defined by:

```
y[i] = 1 \text{ if } np.sum(X[i] ** 2) > 9.34 \text{ else } -1
```

Read more in the User Guide.

#### **Parameters**

**n\_samples** [int, optional (default=12000)] The number of samples.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

- **X** [array of shape [n\_samples, 10]] The input samples.
- y [array of shape [n\_samples]] The output values.

#### See also:

make\_gaussian\_quantiles a generalization of this dataset approach

#### References

[1]

#### Examples using sklearn.datasets.make\_hastie\_10\_2

- Gradient Boosting regularization
- Discrete versus Real AdaBoost
- Early stopping of Gradient Boosting
- Demonstration of multi-metric evaluation on cross\_val\_score and GridSearchCV

### sklearn.datasets.make\_low\_rank\_matrix

```
sklearn.datasets.make_low_rank_matrix(n_samples=100, n_features=100, effective_rank=10, tail_strength=0.5, random_state=None)
```

Generate a mostly low rank matrix with bell-shaped singular values

Most of the variance can be explained by a bell-shaped curve of width effective\_rank: the low rank part of the singular values profile is:

```
(1 - tail_strength) * exp(-1.0 * (i / effective_rank) ** 2)
```

The remaining singular values' tail is fat, decreasing as:

```
tail_strength * exp(-0.1 * i / effective_rank).
```

The low rank part of the profile can be considered the structured signal part of the data while the tail can be considered the noisy part of the data that cannot be summarized by a low number of linear components (singular vectors).

### This kind of singular profiles is often seen in practice, for instance:

- gray level pictures of faces
- TF-IDF vectors of text documents crawled from the web

Read more in the *User Guide*.

#### **Parameters**

- **n\_samples** [int, optional (default=100)] The number of samples.
- **n\_features** [int, optional (default=100)] The number of features.
- **effective\_rank** [int, optional (default=10)] The approximate number of singular vectors required to explain most of the data by linear combinations.
- **tail\_strength** [float between 0.0 and 1.0, optional (default=0.5)] The relative importance of the fat noisy tail of the singular values profile.
- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

**X** [array of shape [n\_samples, n\_features]] The matrix.

# sklearn.datasets.make moons

sklearn.datasets.make\_moons (n\_samples=100, shuffle=True, noise=None, random\_state=None) Make two interleaving half circles

A simple toy dataset to visualize clustering and classification algorithms. Read more in the *User Guide*.

### **Parameters**

- **n\_samples** [int, optional (default=100)] The total number of points generated.
- **shuffle** [bool, optional (default=True)] Whether to shuffle the samples.
- **noise** [double or None (default=None)] Standard deviation of Gaussian noise added to the data.
- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset shuffling and noise. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

- **X** [array of shape [n samples, 2]] The generated samples.
- y [array of shape [n\_samples]] The integer labels (0 or 1) for class membership of each sample.

### Examples using sklearn.datasets.make\_moons

- Comparing anomaly detection algorithms for outlier detection on toy datasets
- Classifier comparison
- Comparing different hierarchical linkage methods on toy datasets

- Comparing different clustering algorithms on toy datasets
- Varying regularization in Multi-layer Perceptron
- Compare Stochastic learning strategies for MLPClassifier
- Feature discretization

# sklearn.datasets.make\_multilabel\_classification

```
sklearn.datasets.make_multilabel_classification (n_samples=100, n_seatures=20, n_classes=5, n_slabels=2, length=50, allow_unlabeled=True, sparse=False, return_indicator='dense', return_distributions=False, random_state=None)
```

Generate a random multilabel classification problem.

# For each sample, the generative process is:

- pick the number of labels: n ~ Poisson(n\_labels)
- n times, choose a class c: c ~ Multinomial(theta)
- pick the document length: k ~ Poisson(length)
- k times, choose a word: w ~ Multinomial(theta\_c)

In the above process, rejection sampling is used to make sure that n is never zero or more than n\_classes, and that the document length is never zero. Likewise, we reject classes which have already been chosen.

Read more in the *User Guide*.

#### **Parameters**

- **n samples** [int, optional (default=100)] The number of samples.
- **n features** [int, optional (default=20)] The total number of features.
- n\_classes [int, optional (default=5)] The number of classes of the classification problem.
- **n\_labels** [int, optional (default=2)] The average number of labels per instance. More precisely, the number of labels per sample is drawn from a Poisson distribution with n\_labels as its expected value, but samples are bounded (using rejection sampling) by n\_classes, and must be nonzero if allow\_unlabeled is False.
- **length** [int, optional (default=50)] The sum of the features (number of words if documents) is drawn from a Poisson distribution with this expected value.
- **allow\_unlabeled** [bool, optional (default=True)] If True, some instances might not belong to any class.
- sparse [bool, optional (default=False)] If True, return a sparse feature matrix
  - New in version 0.17: parameter to allow *sparse* output.
- **return\_indicator** ['dense' (default) | 'sparse' | False] If dense return Y in the dense binary indicator format. If 'sparse' return Y in the sparse binary indicator format. False returns a list of lists of labels.
- **return\_distributions** [bool, optional (default=False)] If True, return the prior class probability and conditional probabilities of features given classes, from which the data was drawn.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

- **X** [array of shape [n\_samples, n\_features]] The generated samples.
- Y [array or sparse CSR matrix of shape [n\_samples, n\_classes]] The label sets.
- p\_c [array, shape [n\_classes]] The probability of each class being drawn. Only returned if return\_distributions=True.
- p\_w\_c [array, shape [n\_features, n\_classes]] The probability of each feature being drawn given each class. Only returned if return\_distributions=True.

### Examples using sklearn.datasets.make\_multilabel\_classification

- Multilabel classification
- Plot randomly generated multilabel dataset

### sklearn.datasets.make regression

```
sklearn.datasets.make_regression (n_samples=100, n_samples=100, n_sa
```

Generate a random regression problem.

The input set can either be well conditioned (by default) or have a low rank-fat tail singular profile. See make low rank matrix for more details.

The output is generated by applying a (potentially biased) random linear regression model with n\_informative nonzero regressors to the previously generated input and some gaussian centered noise with some adjustable scale.

Read more in the *User Guide*.

#### **Parameters**

- **n\_samples** [int, optional (default=100)] The number of samples.
- **n\_features** [int, optional (default=100)] The number of features.
- **n\_informative** [int, optional (default=10)] The number of informative features, i.e., the number of features used to build the linear model used to generate the output.
- **n\_targets** [int, optional (default=1)] The number of regression targets, i.e., the dimension of the y output vector associated with a sample. By default, the output is a scalar.

**bias** [float, optional (default=0.0)] The bias term in the underlying linear model.

**effective rank** [int or None, optional (default=None)]

**if not None:** The approximate number of singular vectors required to explain most of the input data by linear combinations. Using this kind of singular spectrum in the input allows the generator to reproduce the correlations often observed in practice.

if None: The input set is well conditioned, centered and gaussian with unit variance.

- **tail\_strength** [float between 0.0 and 1.0, optional (default=0.5)] The relative importance of the fat noisy tail of the singular values profile if effective\_rank is not None.
- **noise** [float, optional (default=0.0)] The standard deviation of the gaussian noise applied to the output.
- **shuffle** [boolean, optional (default=True)] Shuffle the samples and the features.
- **coef** [boolean, optional (default=False)] If True, the coefficients of the underlying linear model are returned.
- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

- **X** [array of shape [n\_samples, n\_features]] The input samples.
- y [array of shape [n\_samples] or [n\_samples, n\_targets]] The output values.
- **coef** [array of shape [n\_features] or [n\_features, n\_targets], optional] The coefficient of the underlying linear model. It is returned only if coef is True.

# Examples using sklearn.datasets.make\_regression

- Prediction Latency
- Effect of transforming the targets in regression model
- Plot Ridge coefficients as a function of the L2 regularization
- Robust linear model estimation using RANSAC
- Lasso on dense and sparse data
- · HuberRegressor vs Ridge on dataset with strong outliers

# sklearn.datasets.make\_s\_curve

sklearn.datasets.make\_s\_curve(n\_samples=100, noise=0.0, random\_state=None)
Generate an S curve dataset.

Read more in the *User Guide*.

### Parameters

- **n\_samples** [int, optional (default=100)] The number of sample points on the S curve.
- **noise** [float, optional (default=0.0)] The standard deviation of the gaussian noise.
- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

# Returns

- **X** [array of shape [n\_samples, 3]] The points.
- **t** [array of shape [n\_samples]] The univariate position of the sample according to the main dimension of the points in the manifold.

### Examples using sklearn.datasets.make\_s\_curve

- t-SNE: The effect of various perplexity values on the shape
- Comparison of Manifold Learning methods

### sklearn.datasets.make\_sparse\_coded\_signal

```
sklearn.datasets. \textbf{make\_sparse\_coded\_signal} \ (\textit{n\_samples}, \quad \textit{n\_components}, \quad \textit{n\_features}, \\ \textit{n\_nonzero\_coefs}, \textit{random\_state=None})
```

Generate a signal as a sparse combination of dictionary elements.

Returns a matrix Y = DX, such as D is (n\_features, n\_components), X is (n\_components, n\_samples) and each column of X has exactly n\_nonzero\_coefs non-zero elements.

Read more in the *User Guide*.

#### **Parameters**

- **n\_samples** [int] number of samples to generate
- **n\_components** [int,] number of components in the dictionary
- **n\_features** [int] number of features of the dataset to generate
- n\_nonzero\_coefs [int] number of active (non-zero) coefficients in each sample
- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

data [array of shape [n\_features, n\_samples]] The encoded signal (Y).

**dictionary** [array of shape [n\_features, n\_components]] The dictionary with normalized components (D).

**code** [array of shape [n\_components, n\_samples]] The sparse code such that each column of this matrix has exactly n\_nonzero coefs non-zero items (X).

### Examples using sklearn.datasets.make\_sparse\_coded\_signal

• Orthogonal Matching Pursuit

### sklearn.datasets.make\_sparse\_spd\_matrix

```
sklearn.datasets.\textbf{make\_sparse\_spd\_matrix} (dim=1, alpha=0.95, norm\_diag=False, smallest\_coef=0.1, largest\_coef=0.9, random\_state=None)
```

Generate a sparse symmetric definite positive matrix.

Read more in the User Guide.

#### **Parameters**

**dim** [integer, optional (default=1)] The size of the random matrix to generate.

**alpha** [float between 0 and 1, optional (default=0.95)] The probability that a coefficient is zero (see notes). Larger values enforce more sparsity.

**norm\_diag** [boolean, optional (default=False)] Whether to normalize the output matrix to make the leading diagonal elements all 1

smallest\_coef [float between 0 and 1, optional (default=0.1)] The value of the smallest coefficient.

largest\_coef [float between 0 and 1, optional (default=0.9)] The value of the largest coefficient.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

**prec** [sparse matrix of shape (dim, dim)] The generated matrix.

#### See also:

```
make_spd_matrix
```

#### **Notes**

The sparsity is actually imposed on the cholesky factor of the matrix. Thus alpha does not translate directly into the filling fraction of the matrix itself.

# Examples using sklearn.datasets.make\_sparse\_spd\_matrix

• Sparse inverse covariance estimation

### sklearn.datasets.make\_sparse\_uncorrelated

```
sklearn.datasets.make_sparse_uncorrelated(n_samples=100, n_features=10, ran-dom_state=None) ran-
```

Generate a random regression problem with sparse uncorrelated design

This dataset is described in Celeux et al [1]. as:

```
X \sim N(0, 1)

Y(X) = X[:, 0] + 2 * X[:, 1] - 2 * X[:, 2] - 1.5 * X[:, 3]
```

Only the first 4 features are informative. The remaining features are useless.

Read more in the User Guide.

#### **Parameters**

- **n\_samples** [int, optional (default=100)] The number of samples.
- **n\_features** [int, optional (default=10)] The number of features.
- **random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

- **X** [array of shape [n\_samples, n\_features]] The input samples.
- y [array of shape [n\_samples]] The output values.

### References

[1]

# sklearn.datasets.make spd matrix

sklearn.datasets.make\_spd\_matrix(n\_dim, random\_state=None)

Generate a random symmetric, positive-definite matrix.

Read more in the *User Guide*.

### **Parameters**

**n\_dim** [int] The matrix dimension.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

**X** [array of shape [n\_dim, n\_dim]] The random symmetric, positive-definite matrix.

#### See also:

make\_sparse\_spd\_matrix

# sklearn.datasets.make\_swiss\_roll

sklearn.datasets.make\_swiss\_roll(n\_samples=100, noise=0.0, random\_state=None)
Generate a swiss roll dataset.

Read more in the User Guide.

#### **Parameters**

**n\_samples** [int, optional (default=100)] The number of sample points on the S curve.

**noise** [float, optional (default=0.0)] The standard deviation of the gaussian noise.

**random\_state** [int, RandomState instance or None (default)] Determines random number generation for dataset creation. Pass an int for reproducible output across multiple function calls. See *Glossary*.

#### Returns

**X** [array of shape [n\_samples, 3]] The points.

t [array of shape [n\_samples]] The univariate position of the sample according to the main dimension of the points in the manifold.

### **Notes**

The algorithm is from Marsland [1].

### References

[1]

### Examples using sklearn.datasets.make\_swiss\_roll

- Hierarchical clustering: structured vs unstructured ward
- Swiss Roll reduction with LLE

# 6.9 sklearn.decomposition: Matrix Decomposition

The sklearn.decomposition module includes matrix decomposition algorithms, including among others PCA, NMF or ICA. Most of the algorithms of this module can be regarded as dimensionality reduction techniques.

**User guide:** See the *Decomposing signals in components (matrix factorization problems)* section for further details.

decomposition.DictionaryLearning([])	Dictionary learning
decomposition.FactorAnalysis([n_components,	Factor Analysis (FA)
])	
decomposition.FastICA([n_components,])	FastICA: a fast algorithm for Independent Component
	Analysis.
decomposition.IncrementalPCA([n_components,	Incremental principal components analysis (IPCA).
])	
decomposition.KernelPCA([n_components,])	Kernel Principal component analysis (KPCA)
decomposition.LatentDirichletAllocation([Latent Dirichlet Allocation with online variational Bayes	
	algorithm
decomposition.MiniBatchDictionaryLearnin	g (Mini) batch dictionary learning
$ extit{decomposition.MiniBatchSparsePCA([])}$	Mini-batch Sparse Principal Components Analysis
decomposition.NMF([n_components, init,])	Non-Negative Matrix Factorization (NMF)
decomposition.PCA([n_components, copy,])	Principal component analysis (PCA)
decomposition.SparsePCA([n_components,])	Sparse Principal Components Analysis (SparsePCA)
decomposition.SparseCoder(dictionary[,])	Sparse coding
decomposition.TruncatedSVD([n_components,	Dimensionality reduction using truncated SVD (aka LSA).
])	

# 6.9.1 sklearn.decomposition.DictionaryLearning

```
class sklearn.decomposition.DictionaryLearning (n_components=None,
                                                                                          alpha=1,
                                                           max_iter=1000,
                                                                                        tol=1e-08,
                                                          fit_algorithm='lars',
                                                                                             trans-
                                                          form_algorithm='omp',
                                                                                             trans-
                                                          form_n_nonzero_coefs=None,
                                                                                             trans-
                                                          form_alpha=None,
                                                                                     n_{jobs}=None,
                                                           code_init=None,
                                                                             dict_init=None,
                                                                                              ver-
                                                           bose=False,
                                                                          split_sign=False,
                                                                                              ran-
                                                           dom_state=None,
                                                                               positive_code=False,
                                                           positive_dict=False)
```

Dictionary learning

Finds a dictionary (a set of atoms) that can best be used to represent data using a sparse code.

Solves the optimization problem:

```
(U^*,V^*) = argmin 0.5 || Y - U V ||_2^2 + alpha * || U ||_1

(U,V)

with || V_k ||_2 = 1 for all 0 <= k < n_components
```

Read more in the User Guide.

#### **Parameters**

**n\_components** [int,] number of dictionary elements to extract

alpha [float,] sparsity controlling parameter

max iter [int,] maximum number of iterations to perform

tol [float,] tolerance for numerical error

**fit\_algorithm** [{'lars', 'cd'}] lars: uses the least angle regression method to solve the lasso problem (linear\_model.lars\_path) cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). Lars will be faster if the estimated components are sparse.

New in version 0.17: cd coordinate descent method to improve speed.

transform\_algorithm [{'lasso\_lars', 'lasso\_cd', 'lars', 'omp', 'threshold'}] Algorithm used to transform the data lars: uses the least angle regression method (linear\_model.lars\_path) lasso\_lars: uses Lars to compute the Lasso solution lasso\_cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). lasso\_lars will be faster if the estimated components are sparse. omp: uses orthogonal matching pursuit to estimate the sparse solution threshold: squashes to zero all coefficients less than alpha from the projection dictionary \* X'

New in version 0.17: *lasso\_cd* coordinate descent method to improve speed.

- **transform\_n\_nonzero\_coefs** [int, 0.1 \* n\_features by default] Number of nonzero coefficients to target in each column of the solution. This is only used by algorithm='lars' and algorithm='omp' and is overridden by alpha in the *Orthogonal Matching Pursuit (OMP)* case.
- transform\_alpha [float, 1. by default] If algorithm='lasso\_lars' or algorithm='lasso\_cd', alpha is the penalty applied to the L1 norm. If algorithm='threshold', alpha is the absolute value of the threshold below which coefficients will be squashed to zero. If algorithm='omp', alpha is the tolerance parameter: the value of the reconstruction error targeted. In this case, it overrides n\_nonzero\_coefs.
- n\_jobs [int or None, optional (default=None)] Number of parallel jobs to run. None means 1
   unless in a joblib.parallel\_backend context. -1 means using all processors. See
   Glossary for more details.
- code\_init [array of shape (n\_samples, n\_components),] initial value for the code, for warm
  restart
- dict\_init [array of shape (n\_components, n\_features),] initial values for the dictionary, for warm restart
- **verbose** [bool, optional (default: False)] To control the verbosity of the procedure.
- **split\_sign** [bool, False by default] Whether to split the sparse feature vector into the concatenation of its negative part and its positive part. This can improve the performance of downstream classifiers.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**positive\_code** [bool] Whether to enforce positivity when finding the code.

New in version 0.20.

positive\_dict [bool] Whether to enforce positivity when finding the dictionary

New in version 0.20.

#### Attributes

components\_ [array, [n\_components, n\_features]] dictionary atoms extracted from the data
 error\_ [array] vector of errors at each iteration
 n\_iter\_ [int] Number of iterations run.

#### See also:

SparseCoder

MiniBatchDictionaryLearning

SparsePCA

MiniBatchSparsePCA

### **Notes**

#### **References:**

J. Mairal, F. Bach, J. Ponce, G. Sapiro, 2009: Online dictionary learning for sparse coding (https://www.di.ens. fr/sierra/pdfs/icml09.pdf)

### **Methods**

fit(self, X[, y])	Fit the model from data in X.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Encode the data as a sparse combination of the dictio-
	nary atoms.

\_\_init\_\_ (self, n\_components=None, alpha=1, max\_iter=1000, tol=1e-08, fit\_algorithm='lars', transform\_algorithm='omp', transform\_n\_nonzero\_coefs=None, transform\_alpha=None, n\_jobs=None, code\_init=None, dict\_init=None, verbose=False, split\_sign=False, random\_state=None, positive\_code=False, positive\_dict=False)

**fit** (self, X, y=None)

Fit the model from data in X.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples in the number of samples and n\_features is the number of features.

y [Ignored]

### Returns

self [object] Returns the object itself

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- **y** [numpy array of shape [n\_samples]] Target values.

#### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

#### transform(self, X)

Encode the data as a sparse combination of the dictionary atoms.

Coding method is determined by the object parameter transform\_algorithm.

### **Parameters**

**X** [array of shape (n\_samples, n\_features)] Test data to be transformed, must have the same number of features as the data used to train the model.

#### Returns

X new [array, shape (n samples, n components)] Transformed data

# 6.9.2 sklearn.decomposition.FactorAnalysis

```
class sklearn.decomposition.FactorAnalysis (n\_components=None, tol=0.01, copy=True, max\_iter=1000, noise\_variance\_init=None, svd\_method='randomized', iterated\_power=3, random\_state=0)
```

Factor Analysis (FA)

A simple linear generative model with Gaussian latent variables.

The observations are assumed to be caused by a linear transformation of lower dimensional latent factors and added Gaussian noise. Without loss of generality the factors are distributed according to a Gaussian with zero mean and unit covariance. The noise is also zero mean and has an arbitrary diagonal covariance matrix.

If we would restrict the model further, by assuming that the Gaussian noise is even isotropic (all diagonal entries are the same) we would obtain PPCA.

FactorAnalysis performs a maximum likelihood estimate of the so-called loading matrix, the transformation of the latent variables to the observed ones, using expectation-maximization (EM).

Read more in the User Guide.

#### **Parameters**

**n\_components** [int | None] Dimensionality of latent space, the number of components of X that are obtained after transform. If None, n\_components is set to the number of features.

tol [float] Stopping tolerance for EM algorithm.

copy [bool] Whether to make a copy of X. If False, the input X gets overwritten during fitting.

max\_iter [int] Maximum number of iterations.

**noise\_variance\_init** [None | array, shape=(n\_features,)] The initial guess of the noise variance for each feature. If None, it defaults to np.ones(n\_features)

svd\_method [{'lapack', 'randomized'}] Which SVD method to use. If 'lapack' use standard SVD from scipy.linalg, if 'randomized' use fast randomized\_svd function. Defaults to 'randomized'. For most applications 'randomized' will be sufficiently precise while providing significant speed gains. Accuracy can also be improved by setting higher values for iterated\_power. If this is not sufficient, for maximum precision you should choose 'lapack'.

**iterated\_power** [int, optional] Number of iterations for the power method. 3 by default. Only used if svd\_method equals 'randomized'

random\_state [int, RandomState instance or None, optional (default=0)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Only used when svd\_method equals 'randomized'.

#### **Attributes**

**components**\_ [array, [n\_components, n\_features]] Components with maximum variance.

**loglike** [list, [n\_iterations]] The log likelihood at each iteration.

**noise\_variance** [array, shape=(n\_features,)] The estimated noise variance for each feature.

n\_iter\_ [int] Number of iterations run.

### See also:

**PCA** Principal component analysis is also a latent linear variable model which however assumes equal noise variance for each feature. This extra assumption makes probabilistic PCA faster as it can be computed in closed form.

FastICA Independent component analysis, a latent variable model with non-Gaussian latent variables.

### References

## **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.decomposition import FactorAnalysis
>>> X, _ = load_digits(return_X_y=True)
>>> transformer = FactorAnalysis(n_components=7, random_state=0)
>>> X_transformed = transformer.fit_transform(X)
>>> X_transformed.shape
(1797, 7)
```

#### **Methods**

fit(self, X[, y])	Fit the FactorAnalysis model to X using EM
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
get_covariance(self)	Compute data covariance with the FactorAnalysis
	model.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Compute data precision matrix with the FactorAnalysis
	model.
score(self, X[, y])	Compute the average log-likelihood of the samples
score_samples(self, X)	Compute the log-likelihood of each sample
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Apply dimensionality reduction to X using the model.

```
__init__ (self, n_components=None, tol=0.01, copy=True, max_iter=1000, noise_variance_init=None, svd_method='randomized', iterated_power=3, random_state=0)
```

### **fit** (self, X, y=None)

Fit the FactorAnalysis model to X using EM

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data.

y [Ignored]

### Returns

self

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

### get\_covariance (self)

Compute data covariance with the FactorAnalysis model.

```
cov = components_.T * components_ + diag(noise_variance)
```

#### Returns

**cov** [array, shape (n\_features, n\_features)] Estimated covariance of data.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

### get\_precision(self)

Compute data precision matrix with the Factor Analysis model.

#### Returns

**precision** [array, shape (n\_features, n\_features)] Estimated precision of data.

### score(self, X, y=None)

Compute the average log-likelihood of the samples

#### **Parameters**

- **X** [array, shape (n\_samples, n\_features)] The data
- y [Ignored]

#### **Returns**

II [float] Average log-likelihood of the samples under the current model

### $score\_samples(self, X)$

Compute the log-likelihood of each sample

#### **Parameters**

**X** [array, shape (n\_samples, n\_features)] The data

### Returns

**Il** [array, shape (n\_samples,)] Log-likelihood of each sample under the current model

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, X)

Apply dimensionality reduction to X using the model.

Compute the expected mean of the latent variables. See Barber, 21.2.33 (or Bishop, 12.66).

# **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data.

#### Returns

**X\_new** [array-like, shape (n\_samples, n\_components)] The latent variables of X.

# Examples using sklearn.decomposition.FactorAnalysis

- Model selection with Probabilistic PCA and Factor Analysis (FA)
- Faces dataset decompositions

# 6.9.3 sklearn.decomposition.FastICA

FastICA: a fast algorithm for Independent Component Analysis.

Read more in the User Guide.

#### **Parameters**

**n\_components** [int, optional] Number of components to use. If none is passed, all are used.

**algorithm** [{'parallel', 'deflation'}] Apply parallel or deflational algorithm for FastICA.

**whiten** [boolean, optional] If whiten is false, the data is already considered to be whitened, and no whitening is performed.

**fun** [string or function, optional. Default: 'logcosh'] The functional form of the G function used in the approximation to neg-entropy. Could be either 'logcosh', 'exp', or 'cube'. You can also provide your own function. It should return a tuple containing the value of the function, and of its derivative, in the point. Example:

```
def my_g(x): return x ** 3, (3 * x ** 2).mean(axis=-1)
```

**fun\_args** [dictionary, optional] Arguments to send to the functional form. If empty and if fun='logcosh', fun\_args will take value {'alpha': 1.0}.

max\_iter [int, optional] Maximum number of iterations during fit.

tol [float, optional] Tolerance on update at each iteration.

**w\_init** [None of an (n\_components, n\_components) ndarray] The mixing matrix to be used to initialize the algorithm.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### **Attributes**

**components**\_ [2D array, shape (n\_components, n\_features)] The unmixing matrix.

mixing\_ [array, shape (n\_features, n\_components)] The mixing matrix.

**n\_iter\_** [int] If the algorithm is "deflation", n\_iter is the maximum number of iterations run across all components. Else they are just the number of iterations taken to converge.

#### **Notes**

Implementation based on A. Hyvarinen and E. Oja, Independent Component Analysis: Algorithms and Applications, Neural Networks, 13(4-5), 2000, pp. 411-430

# **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.decomposition import FastICA
>>> X, _ = load_digits(return_X_y=True)
>>> transformer = FastICA(n_components=7,
... random_state=0)
>>> X_transformed = transformer.fit_transform(X)
>>> X_transformed.shape
(1797, 7)
```

#### **Methods**

fit(self, X[, y])	Fit the model to X.
fit_transform(self, X[, y])	Fit the model and recover the sources from X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>inverse_transform(self, X[, copy])</pre>	Transform the sources back to the mixed data (apply
	mixing matrix).
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X[, copy])	Recover the sources from X (apply the unmixing ma-
	trix).

```
__init__ (self, n_components=None, algorithm='parallel', whiten=True, fun='logcosh', fun_args=None, max_iter=200, tol=0.0001, w_init=None, random_state=None)
```

# fit (self, X, y=None)

Fit the model to X.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.

y [Ignored]

### Returns

self

# fit\_transform(self, X, y=None)

Fit the model and recover the sources from X.

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [Ignored]

### Returns

**X\_new** [array-like, shape (n\_samples, n\_components)]

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# inverse\_transform(self, X, copy=True)

Transform the sources back to the mixed data (apply mixing matrix).

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_components)] Sources, where n\_samples is the number of samples and n\_components is the number of components.

**copy** [bool (optional)] If False, data passed to fit are overwritten. Defaults to True.

#### **Returns**

**X\_new** [array-like, shape (n\_samples, n\_features)]

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

## transform(self, X, copy=True)

Recover the sources from X (apply the unmixing matrix).

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Data to transform, where n\_samples is the number of samples and n\_features is the number of features.

copy [bool (optional)] If False, data passed to fit are overwritten. Defaults to True.

### Returns

**X\_new** [array-like, shape (n\_samples, n\_components)]

# Examples using sklearn.decomposition.FastICA

- Blind source separation using FastICA
- FastICA on 2D point clouds
- Faces dataset decompositions

# 6.9.4 sklearn.decomposition.IncrementalPCA

Incremental principal components analysis (IPCA).

Linear dimensionality reduction using Singular Value Decomposition of the data, keeping only the most significant singular vectors to project the data to a lower dimensional space. The input data is centered but not scaled for each feature before applying the SVD.

Depending on the size of the input data, this algorithm can be much more memory efficient than a PCA.

This algorithm has constant memory complexity, on the order of batch\_size, enabling use of np.memmap files without loading the entire file into memory.

The computational overhead of each SVD is  $O(batch\_size * n\_features ** 2)$ , but only 2 \* batch\\_size samples remain in memory at a time. There will be n\_samples / batch\_size SVD computations to get the principal components, versus 1 large SVD of complexity  $O(n\_samples * n\_features ** 2)$  for PCA.

Read more in the *User Guide*.

#### **Parameters**

- n\_components [int or None, (default=None)] Number of components to keep. If
  n\_components `` is ``None, then n\_components is set to min (n\_samples,
  n\_features).
- whiten [bool, optional] When True (False by default) the components\_ vectors are divided by n\_samples times components\_ to ensure uncorrelated outputs with unit component-wise variances.

Whitening will remove some information from the transformed signal (the relative variance scales of the components) but can sometimes improve the predictive accuracy of the downstream estimators by making data respect some hard-wired assumptions.

- **copy** [bool, (default=True)] If False, X will be overwritten. copy=False can be used to save memory but is unsafe for general use.
- batch\_size [int or None, (default=None)] The number of samples to use for each batch. Only
   used when calling fit. If batch\_size is None, then batch\_size is inferred from the
   data and set to 5 \* n\_features, to provide a balance between approximation accuracy
   and memory consumption.

#### **Attributes**

- **components**\_ [array, shape (n\_components, n\_features)] Components with maximum variance.
- **explained\_variance\_** [array, shape (n\_components,)] Variance explained by each of the selected components.
- **explained\_variance\_ratio\_** [array, shape (n\_components,)] Percentage of variance explained by each of the selected components. If all components are stored, the sum of explained variances is equal to 1.0.
- **singular\_values\_** [array, shape (n\_components,)] The singular values corresponding to each of the selected components. The singular values are equal to the 2-norms of the n components variables in the lower-dimensional space.
- **mean\_** [array, shape (n\_features,)] Per-feature empirical mean, aggregate over calls to partial\_fit.

- var\_ [array, shape (n\_features,)] Per-feature empirical variance, aggregate over calls to partial\_fit.
- **noise\_variance** [float] The estimated noise covariance following the Probabilistic PCA model from Tipping and Bishop 1999. See "Pattern Recognition and Machine Learning" by C. Bishop, 12.2.1 p. 574 or http://www.miketipping.com/papers/met-mppca.pdf.
- **n\_components\_** [int] The estimated number of components. Relevant when n components=None.
- **n\_samples\_seen\_** [int] The number of samples processed by the estimator. Will be reset on new calls to fit, but increments across partial\_fit calls.

#### See also:

PCA

KernelPCA

SparsePCA

TruncatedSVD

#### **Notes**

Implements the incremental PCA model from: D. Ross, J. Lim, R. Lin, M. Yang, Incremental Learning for Robust Visual Tracking, International Journal of Computer Vision, Volume 77, Issue 1-3, pp. 125-141, May 2008. See https://www.cs.toronto.edu/~dross/ivt/RossLimLinYang\_ijcv.pdf

This model is an extension of the Sequential Karhunen-Loeve Transform from: A. Levy and M. Lindenbaum, Sequential Karhunen-Loeve Basis Extraction and its Application to Images, IEEE Transactions on Image Processing, Volume 9, Number 8, pp. 1371-1374, August 2000. See https://www.cs.technion.ac.il/~mic/doc/skl-ip.pdf

We have specifically abstained from an optimization used by authors of both papers, a QR decomposition used in specific situations to reduce the algorithmic complexity of the SVD. The source for this technique is *Matrix Computations, Third Edition, G. Holub and C. Van Loan, Chapter 5, section 5.4.4, pp 252-253.* This technique has been omitted because it is advantageous only when decomposing a matrix with n\_samples (rows) >=  $5/3 * n_features$  (columns), and hurts the readability of the implemented algorithm. This would be a good opportunity for future optimization, if it is deemed necessary.

# References

- D. Ross, J. Lim, R. Lin, M. Yang. Incremental Learning for Robust Visual Tracking, International Journal of Computer Vision, Volume 77, Issue 1-3, pp. 125-141, May 2008.
- G. Golub and C. Van Loan. Matrix Computations, Third Edition, Chapter 5, Section 5.4.4, pp. 252-253.

### **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.decomposition import IncrementalPCA
>>> X, _ = load_digits(return_X_y=True)
>>> transformer = IncrementalPCA(n_components=7, batch_size=200)
>>> # either partially fit on smaller batches of data
>>> transformer.partial_fit(X[:100, :])
IncrementalPCA(batch_size=200, copy=True, n_components=7, whiten=False)
```

```
>>> # or let the fit function itself divide the data into batches
>>> X_transformed = transformer.fit_transform(X)
>>> X_transformed.shape
(1797, 7)
```

### **Methods**

fit(self, X[, y])	Fit the model with X, using minibatches of size
	batch_size.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
get_covariance(self)	Compute data covariance with the generative model.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Compute data precision matrix with the generative
	model.
inverse_transform(self, X)	Transform data back to its original space.
<pre>partial_fit(self, X[, y, check_input])</pre>	Incremental fit with X.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Apply dimensionality reduction to X.

\_\_init\_\_ (self, n\_components=None, whiten=False, copy=True, batch\_size=None)

### **fit** (self, X, y=None)

Fit the model with X, using minibatches of size batch\_size.

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [Ignored]

### Returns

self [object] Returns the instance itself.

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- $y \hspace{0.1cm}$  [numpy array of shape [n\_samples]] Target values.

# Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_covariance (self)

Compute data covariance with the generative model.

```
cov = components_.T * S**2 * components_ + sigma2 * eye(n_features) where S**2 contains the explained variances, and sigma2 contains the noise variances.
```

## Returns

**cov** [array, shape=(n features, n features)] Estimated covariance of data.

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

#### get\_precision(self)

Compute data precision matrix with the generative model.

Equals the inverse of the covariance but computed with the matrix inversion lemma for efficiency.

#### Returns

**precision** [array, shape=(n\_features, n\_features)] Estimated precision of data.

### $inverse\_transform(self, X)$

Transform data back to its original space.

In other words, return an input X\_original whose transform would be X.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_components)] New data, where n\_samples is the number of samples and n\_components is the number of components.

#### **Returns**

X\_original array-like, shape (n\_samples, n\_features)

### **Notes**

If whitening is enabled, inverse\_transform will compute the exact inverse operation, which includes reversing whitening.

```
partial_fit (self, X, y=None, check_input=True)
```

Incremental fit with X. All of X is processed as a single batch.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.

check input [bool] Run check array on X.

y [Ignored]

### Returns

self [object] Returns the instance itself.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

#### self

#### transform(self, X)

Apply dimensionality reduction to X.

X is projected on the first principal components previously extracted from a training set.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] New data, where n\_samples is the number of samples and n\_features is the number of features.

#### **Returns**

**X\_new** [array-like, shape (n\_samples, n\_components)]

# **Examples**

```
>>> import numpy as np
>>> from sklearn.decomposition import IncrementalPCA
>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> ipca = IncrementalPCA(n_components=2, batch_size=3)
>>> ipca.fit(X)
IncrementalPCA(batch_size=3, copy=True, n_components=2, whiten=False)
>>> ipca.transform(X)
```

# Examples using sklearn.decomposition.IncrementalPCA

• Incremental PCA

# 6.9.5 sklearn.decomposition.KernelPCA

Kernel Principal component analysis (KPCA)

Non-linear dimensionality reduction through the use of kernels (see *Pairwise metrics, Affinities and Kernels*).

Read more in the *User Guide*.

#### **Parameters**

**n\_components** [int, default=None] Number of components. If None, all non-zero components are kept.

```
kernel ["linear" | "poly" | "rbf" | "sigmoid" | "cosine" | "precomputed"] Kernel. Default="linear".
```

**gamma** [float, default=1/n\_features] Kernel coefficient for rbf, poly and sigmoid kernels. Ignored by other kernels.

**degree** [int, default=3] Degree for poly kernels. Ignored by other kernels.

**coef0** [float, default=1] Independent term in poly and sigmoid kernels. Ignored by other kernels.

- **kernel\_params** [mapping of string to any, default=None] Parameters (keyword arguments) and values for kernel passed as callable object. Ignored by other kernels.
- **alpha** [int, default=1.0] Hyperparameter of the ridge regression that learns the inverse transform (when fit\_inverse\_transform=True).
- **fit\_inverse\_transform** [bool, default=False] Learn the inverse transform for non-precomputed kernels. (i.e. learn to find the pre-image of a point)
- **eigen\_solver** [string ['auto'|'dense'|'arpack'], default='auto'] Select eigensolver to use. If n\_components is much less than the number of training samples, arpack may be more efficient than the dense eigensolver.
- **tol** [float, default=0] Convergence tolerance for arpack. If 0, optimal value will be chosen by arpack.
- max\_iter [int, default=None] Maximum number of iterations for arpack. If None, optimal value will be chosen by arpack.
- **remove\_zero\_eig** [boolean, default=False] If True, then all components with zero eigenvalues are removed, so that the number of components in the output may be < n\_components (and sometimes even zero due to numerical instability). When n\_components is None, this parameter is ignored and components with zero eigenvalues are removed regardless.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when eigen\_solver == 'arpack'.

New in version 0.18.

**copy\_X** [boolean, default=True] If True, input X is copied and stored by the model in the X\_fit\_ attribute. If no further changes will be done to X, setting copy\_X=False saves memory by storing a reference.

New in version 0.18.

**n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

New in version 0.18.

#### Attributes

- **lambdas**\_ [array, (n\_components,)] Eigenvalues of the centered kernel matrix in decreasing order. If n\_components and remove\_zero\_eig are not set, then all values are stored.
- **alphas**\_ [array, (n\_samples, n\_components)] Eigenvectors of the centered kernel matrix. If *n\_components* and remove\_zero\_eig are not set, then all components are stored.
- dual\_coef\_ [array, (n\_samples, n\_features)] Inverse transform matrix. Only available when fit\_inverse\_transform is True.
- **X\_transformed\_fit\_** [array, (n\_samples, n\_components)] Projection of the fitted data on the kernel principal components. Only available when fit\_inverse\_transform is True.
- **X\_fit\_** [(n\_samples, n\_features)] The data used to fit the model. If copy\_X=False, then X\_fit\_ is a reference. This attribute is used for the calls to transform.

### References

**Kernel PCA was introduced in:** Bernhard Schoelkopf, Alexander J. Smola, and Klaus-Robert Mueller. 1999. Kernel principal component analysis. In Advances in kernel methods, MIT Press, Cambridge, MA, USA 327-352.

# **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.decomposition import KernelPCA
>>> X, _ = load_digits(return_X_y=True)
>>> transformer = KernelPCA(n_components=7, kernel='linear')
>>> X_transformed = transformer.fit_transform(X)
>>> X_transformed.shape
(1797, 7)
```

# **Methods**

fit(self, X[, y])	Fit the model from data in X.
fit_transform(self, X[, y])	Fit the model from data in X and transform X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Transform X back to original space.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform X.

```
__init__ (self, n_components=None, kernel='linear', gamma=None, degree=3, coef0=1, kernel_params=None, alpha=1.0, fit_inverse_transform=False, eigen_solver='auto', tol=0, max_iter=None, remove_zero_eig=False, random_state=None, copy_X=True, n_jobs=None)
```

### **fit** (self, X, y=None)

Fit the model from data in X.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples in the number of samples and n\_features is the number of features.

#### Returns

self [object] Returns the instance itself.

```
fit_transform(self, X, y=None, **params)
```

Fit the model from data in X and transform X.

# **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples in the number of samples and n\_features is the number of features.

# Returns

**X new** [array-like, shape (n samples, n components)]

```
get_params (self, deep=True)
```

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

**params** [mapping of string to any] Parameter names mapped to their values.

## $inverse\_transform(self, X)$

Transform X back to original space.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_components)]

### **Returns**

**X\_new** [array-like, shape (n\_samples, n\_features)]

#### References

"Learning to Find Pre-Images", G BakIr et al, 2004.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# transform(self, X)

Transform X.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

### Returns

**X\_new** [array-like, shape (n\_samples, n\_components)]

# Examples using sklearn.decomposition.KernelPCA

• Kernel PCA

# 6.9.6 sklearn.decomposition.LatentDirichletAllocation

class sklearn.decomposition.LatentDirichletAllocation(n\_components=10,

doc\_topic\_prior=None,
topic\_word\_prior=None,
learning\_method='batch',
learning\_decay=0.7,
learning\_offset=10.0,
max\_iter=10, batch\_size=128,
evaluate\_every=-1, total\_samples=1000000.0,
perp\_tol=0.1,
mean\_change\_tol=0.001,
max\_doc\_update\_iter=100,
n\_jobs=None, verbose=0, random\_state=None)

Latent Dirichlet Allocation with online variational Bayes algorithm

New in version 0.17.

Read more in the *User Guide*.

#### **Parameters**

**n\_components** [int, optional (default=10)] Number of topics.

doc\_topic\_prior [float, optional (default=None)] Prior of document topic distribution theta.
If the value is None, defaults to 1 / n\_components. In [1]\_, this is called alpha.

**topic\_word\_prior** [float, optional (default=None)] Prior of topic word distribution beta. If the value is None, defaults to 1 / n\_components. In [1]\_, this is called eta.

**learning\_method** ['batch' | 'online', default='batch'] Method used to update \_component. Only used in fit method. In general, if the data size is large, the online update will be much faster than the batch update.

Valid options:

```
'batch': Batch variational Bayes method. Use all training data in each EM update.

Old `components_` will be overwritten in each iteration.

'online': Online variational Bayes method. In each EM update, use mini-batch of training data to update the ``components_`` variable incrementally. The learning rate is controlled by the ``learning_decay`` and the ``learning_offset`` parameters.
```

Changed in version 0.20: The default learning method is now "batch".

**learning\_decay** [float, optional (default=0.7)] It is a parameter that control learning rate in the online learning method. The value should be set between (0.5, 1.0] to guarantee asymptotic convergence. When the value is 0.0 and batch\_size is n\_samples, the update method is same as batch learning. In the literature, this is called kappa.

**learning\_offset** [float, optional (default=10.)] A (positive) parameter that downweights early iterations in online learning. It should be greater than 1.0. In the literature, this is called tau\_0.

max\_iter [integer, optional (default=10)] The maximum number of iterations.

**batch\_size** [int, optional (default=128)] Number of documents to use in each EM iteration. Only used in online learning.

- **evaluate\_every** [int, optional (default=0)] How often to evaluate perplexity. Only used in fit method, set it to 0 or negative number to not evaluate perplexity in training at all. Evaluating perplexity can help you check convergence in training process, but it will also increase total training time. Evaluating perplexity in every iteration might increase training time up to two-fold.
- **total\_samples** [int, optional (default=1e6)] Total number of documents. Only used in the partial\_fit method.
- **perp\_tol** [float, optional (default=1e-1)] Perplexity tolerance in batch learning. Only used when evaluate\_every is greater than 0.
- **mean\_change\_tol** [float, optional (default=1e-3)] Stopping tolerance for updating document topic distribution in E-step.
- **max\_doc\_update\_iter** [int (default=100)] Max number of iterations for updating document topic distribution in the E-step.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use in the E-step. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- **verbose** [int, optional (default=0)] Verbosity level.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### **Attributes**

- components\_ [array, [n\_components, n\_features]] Variational parameters for topic word distribution. Since the complete conditional for topic word distribution is a Dirichlet, components\_[i, j] can be viewed as pseudocount that represents the number of times word j was assigned to topic i. It can also be viewed as distribution over the words for each topic after normalization: model.components\_ / model.components\_. sum(axis=1)[:, np.newaxis].
- **n\_batch\_iter\_** [int] Number of iterations of the EM step.
- **n\_iter\_** [int] Number of passes over the dataset.

### References

- [1] "Online Learning for Latent Dirichlet Allocation", Matthew D. Hoffman, David M. Blei, Francis Bach, 2010
- [2] "Stochastic Variational Inference", Matthew D. Hoffman, David M. Blei, Chong Wang, John Paisley, 2013
- [3] Matthew D. Hoffman's onlineIdavb code. Link: https://github.com/blei-lab/onlineIdavb

# **Examples**

```
>>> from sklearn.decomposition import LatentDirichletAllocation
>>> from sklearn.datasets import make_multilabel_classification
>>> # This produces a feature matrix of token counts, similar to what
>>> # CountVectorizer would produce on text.
```

### **Methods**

fit(self, X[, y])	Learn model for the data X with variational Bayes
	method.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X[, y])</pre>	Online VB with Mini-Batch update.
<pre>perplexity(self, X[, sub_sampling])</pre>	Calculate approximate perplexity for data X.
score(self, X[, y])	Calculate approximate log-likelihood as score.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform data X according to the fitted model.

```
__init__(self, n_components=10, doc_topic_prior=None, topic_word_prior=None, learning_method='batch', learning_decay=0.7, learning_offset=10.0, max_iter=10, batch_size=128, evaluate_every=-1, total_samples=1000000.0, perp_tol=0.1, mean_change_tol=0.001, max_doc_update_iter=100, n_jobs=None, verbose=0, random_state=None)
```

## **fit** (*self*, *X*, *y*=*None*)

Learn model for the data X with variational Bayes method.

When learning\_method is 'online', use mini-batch update. Otherwise, use batch update.

### **Parameters**

**X** [array-like or sparse matrix, shape=(n samples, n features)] Document word matrix.

y [Ignored]

# Returns

self

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

# **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
partial_fit (self, X, y=None)
```

Online VB with Mini-Batch update.

#### **Parameters**

**X** [array-like or sparse matrix, shape=(n\_samples, n\_features)] Document word matrix.

y [Ignored]

### **Returns**

self

```
perplexity (self, X, sub_sampling=False)
```

Calculate approximate perplexity for data X.

Perplexity is defined as exp(-1. \* log-likelihood per word)

Changed in version 0.19: *doc\_topic\_distr* argument has been deprecated and is ignored because user no longer has access to unnormalized distribution

### **Parameters**

**X** [array-like or sparse matrix, [n\_samples, n\_features]] Document word matrix.

sub\_sampling [bool] Do sub-sampling or not.

#### **Returns**

score [float] Perplexity score.

```
score (self, X, y=None)
```

Calculate approximate log-likelihood as score.

### **Parameters**

**X** [array-like or sparse matrix, shape=(n\_samples, n\_features)] Document word matrix.

y [Ignored]

### Returns

**score** [float] Use approximate bound as score.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

#### transform(self, X)

Transform data X according to the fitted model.

Changed in version 0.18: doc\_topic\_distr is now normalized

### **Parameters**

**X** [array-like or sparse matrix, shape=(n samples, n features)] Document word matrix.

#### Returns

**doc\_topic\_distr** [shape=(n\_samples, n\_components)] Document topic distribution for X.

# Examples using sklearn.decomposition.LatentDirichletAllocation

Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation

# 6.9.7 sklearn.decomposition.MiniBatchDictionaryLearning

```
class sklearn.decomposition.MiniBatchDictionaryLearning (n_components=None,
                                                                                               al-
                                                                      pha=1,
                                                                                      n_{iter}=1000,
                                                                      fit_algorithm='lars',
                                                                      n jobs=None,
                                                                       batch\_size=3,
                                                                                     shuffle=True,
                                                                       dict_init=None,
                                                                                            trans-
                                                                      form_algorithm='omp', trans-
                                                                      form_n_nonzero_coefs=None,
                                                                       transform_alpha=None, ver-
                                                                       bose=False, split sign=False,
                                                                       random state=None,
                                                                                             pos-
                                                                       itive_code=False,
                                                                                             posi-
                                                                       tive_dict=False)
```

Mini-batch dictionary learning

Finds a dictionary (a set of atoms) that can best be used to represent data using a sparse code.

Solves the optimization problem:

```
(U^*,V^*) = argmin 0.5 || Y - U V ||_2^2 + alpha * || U ||_1
(U,V)
with || V_k ||_2 = 1 for all 0 <= k < n_components
```

Read more in the User Guide.

#### **Parameters**

**n components** [int,] number of dictionary elements to extract

alpha [float,] sparsity controlling parameter

**n\_iter** [int,] total number of iterations to perform

**fit\_algorithm** [{'lars', 'cd'}] lars: uses the least angle regression method to solve the lasso problem (linear\_model.lars\_path) cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). Lars will be faster if the estimated components are sparse.

**n\_jobs** [int or None, optional (default=None)] Number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

batch\_size [int,] number of samples in each mini-batch

**shuffle** [bool,] whether to shuffle the samples before forming batches

- **dict\_init** [array of shape (n\_components, n\_features),] initial value of the dictionary for warm restart scenarios
- transform\_algorithm [{'lasso\_lars', 'lasso\_cd', 'lars', 'omp', 'threshold'}] Algorithm used to transform the data. lars: uses the least angle regression method (linear\_model.lars\_path) lasso\_lars: uses Lars to compute the Lasso solution lasso\_cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). lasso\_lars will be faster if the estimated components are sparse. omp: uses orthogonal matching pursuit to estimate the sparse solution threshold: squashes to zero all coefficients less than alpha from the projection dictionary \* X'
- transform\_n\_nonzero\_coefs [int, 0.1 \* n\_features by default] Number of nonzero coefficients to target in each column of the solution. This is only used by algorithm='lars' and algorithm='omp' and is overridden by alpha in the Orthogonal Matching Pursuit (OMP) case.
- transform\_alpha [float, 1. by default] If algorithm='lasso\_lars' or algorithm='lasso\_cd', alpha is the penalty applied to the L1 norm. If algorithm='threshold', alpha is the absolute value of the threshold below which coefficients will be squashed to zero. If algorithm='omp', alpha is the tolerance parameter: the value of the reconstruction error targeted. In this case, it overrides n\_nonzero\_coefs.

verbose [bool, optional (default: False)] To control the verbosity of the procedure.

- **split\_sign** [bool, False by default] Whether to split the sparse feature vector into the concatenation of its negative part and its positive part. This can improve the performance of downstream classifiers.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

positive\_code [bool] Whether to enforce positivity when finding the code.

New in version 0.20.

**positive dict** [bool] Whether to enforce positivity when finding the dictionary.

New in version 0.20.

### **Attributes**

components\_ [array, [n\_components, n\_features]] components extracted from the data

inner\_stats\_ [tuple of (A, B) ndarrays] Internal sufficient statistics that are kept by the algorithm. Keeping them is useful in online settings, to avoid loosing the history of the evolution, but they shouldn't have any use for the end user. A (n\_components, n\_components) is the dictionary covariance matrix. B (n\_features, n\_components) is the data approximation matrix

**n iter** [int] Number of iterations run.

See also:

SparseCoder

DictionaryLearning

SparsePCA

MiniBatchSparsePCA

### **Notes**

### **References:**

J. Mairal, F. Bach, J. Ponce, G. Sapiro, 2009: Online dictionary learning for sparse coding (https://www.di.ens.fr/sierra/pdfs/icml09.pdf)

### **Methods**

fit(self, X[, y])	Fit the model from data in X.
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X[, y, iter_offset])</pre>	Updates the model using the data in X as a mini-batch.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Encode the data as a sparse combination of the dictio-
	nary atoms.

\_\_init\_\_ (self, n\_components=None, alpha=1, n\_iter=1000, fit\_algorithm='lars', n\_jobs=None, batch\_size=3, shuffle=True, dict\_init=None, transform\_algorithm='omp', transform\_n\_nonzero\_coefs=None, transform\_alpha=None, verbose=False, split\_sign=False, random\_state=None, positive\_code=False, positive\_dict=False)

# fit (self, X, y=None)

Fit the model from data in X.

### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples in the number of samples and n\_features is the number of features.
- y [Ignored]

## Returns

self [object] Returns the instance itself.

fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

# Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# partial\_fit (self, X, y=None, iter\_offset=None)

Updates the model using the data in X as a mini-batch.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples in the number of samples and n\_features is the number of features.

y [Ignored]

**iter\_offset** [integer, optional] The number of iteration on data batches that has been performed before this call to partial\_fit. This is optional: if no number is passed, the memory of the object is used.

### Returns

self [object] Returns the instance itself.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# transform(self, X)

Encode the data as a sparse combination of the dictionary atoms.

Coding method is determined by the object parameter transform\_algorithm.

#### **Parameters**

**X** [array of shape (n\_samples, n\_features)] Test data to be transformed, must have the same number of features as the data used to train the model.

# Returns

**X\_new** [array, shape (n\_samples, n\_components)] Transformed data

### Examples using sklearn.decomposition.MiniBatchDictionaryLearning

- Image denoising using dictionary learning
- Faces dataset decompositions

# 6.9.8 sklearn.decomposition.MiniBatchSparsePCA

 $\begin{array}{llll} \textbf{class} & \textbf{sklearn.decomposition.MiniBatchSparsePCA} & (n\_components=None, & alpha=1, \\ & ridge\_alpha=0.01, & n\_iter=100, & call-\\ & back=None, & batch\_size=3, & ver-\\ & bose=False, & shuffle=True, & n\_jobs=None, \\ & method='lars', & random\_state=None, \\ & normalize\_components=False) \end{array}$ 

Mini-batch Sparse Principal Components Analysis

Finds the set of sparse components that can optimally reconstruct the data. The amount of sparseness is controllable by the coefficient of the L1 penalty, given by the parameter alpha.

Read more in the User Guide.

#### **Parameters**

**n\_components** [int,] number of sparse atoms to extract

alpha [int,] Sparsity controlling parameter. Higher values lead to sparser components.

**ridge\_alpha** [float,] Amount of ridge shrinkage to apply in order to improve conditioning when calling the transform method.

**n\_iter** [int,] number of iterations to perform for each mini batch

callback [callable or None, optional (default: None)] callable that gets invoked every five iterations

batch\_size [int,] the number of features to take in each mini batch

**verbose** [int] Controls the verbosity; the higher, the more messages. Defaults to 0.

**shuffle** [boolean,] whether to shuffle the data before splitting it in batches

**n\_jobs** [int or None, optional (default=None)] Number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

**method** [{'lars', 'cd'}] lars: uses the least angle regression method to solve the lasso problem (linear\_model.lars\_path) cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). Lars will be faster if the estimated components are sparse.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**normalize\_components** [boolean, optional (default=False)]

- if False, use a version of Sparse PCA without components normalization and without data centering. This is likely a bug and even though it's the default for backward compatibility, this should not be used.
- if True, use a version of Sparse PCA with components normalization and data centering.

New in version 0.20.

Deprecated since version 0.22: normalize\_components was added and set to False for backward compatibility. It would be set to True from 0.22 onwards.

# **Attributes**

components\_ [array, [n\_components, n\_features]] Sparse components extracted from the data.

**n\_iter\_** [int] Number of iterations run.

mean\_ [array, shape (n\_features,)] Per-feature empirical mean, estimated from the training set. Equal to X.mean (axis=0).

### See also:

PCA

SparsePCA

DictionaryLearning

# **Examples**

```
>>> import numpy as np
>>> from sklearn.datasets import make_friedman1
>>> from sklearn.decomposition import MiniBatchSparsePCA
>>> X, _ = make_friedman1(n_samples=200, n_features=30, random_state=0)
>>> transformer = MiniBatchSparsePCA(n_components=5,
          batch_size=50,
          normalize_components=True,
. . .
           random_state=0)
>>> transformer.fit(X)
MiniBatchSparsePCA(...)
>>> X_transformed = transformer.transform(X)
>>> X_transformed.shape
(200, 5)
>>> # most values in the components_ are zero (sparsity)
>>> np.mean(transformer.components_ == 0)
0.94
```

# **Methods**

fit(self, X[, y])	Fit the model from data in X.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Least Squares projection of the data onto the sparse
	components.

```
__init___(self, n_components=None, alpha=1, ridge_alpha=0.01, n_iter=100, callback=None, batch_size=3, verbose=False, shuffle=True, n_jobs=None, method='lars', random_state=None, normalize_components=False)
```

**fit** (*self*, *X*, *y*=*None*)

Fit the model from data in X.

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples in the number of samples and n\_features is the number of features.
- y [Ignored]

#### Returns

**self** [object] Returns the instance itself.

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

## transform(self, X)

Least Squares projection of the data onto the sparse components.

To avoid instability issues in case the system is under-determined, regularization can be applied (Ridge regression) via the ridge\_alpha parameter.

Note that Sparse PCA components orthogonality is not enforced as in PCA hence one cannot use a simple linear projection.

#### **Parameters**

X [array of shape (n\_samples, n\_features)] Test data to be transformed, must have the same number of features as the data used to train the model.

### Returns

X\_new array, shape (n\_samples, n\_components) Transformed data.

# Examples using sklearn.decomposition.MiniBatchSparsePCA

Faces dataset decompositions

# 6.9.9 sklearn.decomposition.NMF

```
class sklearn.decomposition.NMF (n\_components=None, init=None, solver='cd', beta\_loss='frobenius', tol=0.0001, max\_iter=200, random\_state=None, alpha=0.0, l1\_ratio=0.0, verbose=0, shuffle=False)
```

Non-Negative Matrix Factorization (NMF)

Find two non-negative matrices (W, H) whose product approximates the non-negative matrix X. This factorization can be used for example for dimensionality reduction, source separation or topic extraction.

The objective function is:

```
0.5 * ||X - WH||_Fro^2

+ alpha * l1_ratio * ||vec(W)||_1

+ alpha * l1_ratio * ||vec(H)||_1

+ 0.5 * alpha * (1 - l1_ratio) * ||W||_Fro^2

+ 0.5 * alpha * (1 - l1_ratio) * ||H||_Fro^2
```

### Where:

```
||A||_Fro^2 = \sum_{i,j} A_{ij}^2 (Frobenius norm)
||vec(A)||_1 = \sum_{i,j} abs(A_{ij}) (Elementwise L1 norm)
```

For multiplicative-update ('mu') solver, the Frobenius norm  $(0.5 * ||X - WH||_Fro^2)$  can be changed into another beta-divergence loss, by changing the beta\_loss parameter.

The objective function is minimized with an alternating minimization of W and H.

Read more in the *User Guide*.

#### **Parameters**

- **n\_components** [int or None] Number of components, if n\_components is not set all features are kept.
- init [None | 'random' | 'nndsvda' | 'nndsvda' | 'nndsvdar' | 'custom'] Method used to initialize the procedure. Default: None. Valid options:
  - None: 'nndsvd' if n\_components <= min(n\_samples, n\_features), otherwise random.
  - 'random': non-negative random matrices, scaled with: sqrt(X.mean() n\_components)
  - 'nndsvd': Nonnegative Double Singular Value Decomposition (NNDSVD) initialization (better for sparseness)
  - 'nndsvda': NNDSVD with zeros filled with the average of X (better when sparsity is not desired)
  - 'nndsvdar': NNDSVD with zeros filled with small random values (generally faster, less accurate alternative to NNDSVDa for when sparsity is not desired)
  - 'custom': use custom matrices W and H
- **solver** ['cd' | 'mu'] Numerical solver to use: 'cd' is a Coordinate Descent solver. 'mu' is a Multiplicative Update solver.

New in version 0.17: Coordinate Descent solver.

New in version 0.19: Multiplicative Update solver.

**beta\_loss** [float or string, default 'frobenius'] String must be in {'frobenius', 'kullback-leibler', 'itakura-saito'}. Beta divergence to be minimized, measuring the distance between X and the dot product WH. Note that values different from 'frobenius' (or 2) and 'kullback-leibler' (or 1) lead to significantly slower fits. Note that for beta\_loss <= 0 (or 'itakura-saito'), the input matrix X cannot contain zeros. Used only in 'mu' solver.

New in version 0.19.

tol [float, default: 1e-4] Tolerance of the stopping condition.

max\_iter [integer, default: 200] Maximum number of iterations before timing out.

random\_state [int, RandomState instance or None, optional, default: None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**alpha** [double, default: 0.] Constant that multiplies the regularization terms. Set it to zero to have no regularization.

New in version 0.17: alpha used in the Coordinate Descent solver.

11\_ratio [double, default: 0.] The regularization mixing parameter, with 0 <= 11\_ratio <= 1. For 11\_ratio = 0 the penalty is an elementwise L2 penalty (aka Frobenius Norm). For 11\_ratio = 1 it is an elementwise L1 penalty. For 0 < 11\_ratio < 1, the penalty is a combination of L1 and L2.

New in version 0.17: Regularization parameter *l1\_ratio* used in the Coordinate Descent solver.

verbose [bool, default=False] Whether to be verbose.

shuffle [boolean, default: False] If true, randomize the order of coordinates in the CD solver.

New in version 0.17: *shuffle* parameter used in the Coordinate Descent solver.

### **Attributes**

**components**\_ [array, [n\_components, n\_features]] Factorization matrix, sometimes called 'dictionary'.

**reconstruction\_err\_** [number] Frobenius norm of the matrix difference, or beta-divergence, between the training data X and the reconstructed data WH from the fitted model.

**n\_iter\_** [int] Actual number of iterations.

### References

Cichocki, Andrzej, and P. H. A. N. Anh-Huy. "Fast local algorithms for large scale nonnegative matrix and tensor factorizations." IEICE transactions on fundamentals of electronics, communications and computer sciences 92.3: 708-721, 2009.

Fevotte, C., & Idier, J. (2011). Algorithms for nonnegative matrix factorization with the beta-divergence. Neural Computation, 23(9).

## **Examples**

```
>>> import numpy as np
>>> X = np.array([[1, 1], [2, 1], [3, 1.2], [4, 1], [5, 0.8], [6, 1]])
>>> from sklearn.decomposition import NMF
>>> model = NMF(n_components=2, init='random', random_state=0)
>>> W = model.fit_transform(X)
>>> H = model.components_
```

### **Methods**

fit(self, X[, y])	Learn a NMF model for the data X.
<pre>fit_transform(self, X[, y, W, H])</pre>	Learn a NMF model for the data X and returns the trans-
	formed data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, W)	Transform data back to its original space.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform the data X according to the fitted NMF model

```
__init__ (self, n_components=None, init=None, solver='cd', beta_loss='frobenius', tol=0.0001, max_iter=200, random_state=None, alpha=0.0, l1_ratio=0.0, verbose=0, shuffle=False)
```

# fit (self, X, y=None, \*\*params)

Learn a NMF model for the data X.

#### **Parameters**

- X [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Data matrix to be decomposed
- y [Ignored]

# Returns

self

### fit transform(self, X, y=None, W=None, H=None)

Learn a NMF model for the data X and returns the transformed data.

This is more efficient than calling fit followed by transform.

### **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Data matrix to be decomposed
- y [Ignored]
- **W** [array-like, shape (n\_samples, n\_components)] If init='custom', it is used as initial guess for the solution.
- **H** [array-like, shape (n\_components, n\_features)] If init='custom', it is used as initial guess for the solution.

### Returns

W [array, shape (n\_samples, n\_components)] Transformed data.

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

#### inverse\_transform(self, W)

Transform data back to its original space.

#### **Parameters**

W [{array-like, sparse matrix}, shape (n\_samples, n\_components)] Transformed data matrix

### **Returns**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Data matrix of original shape New in version 0.18: ...

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

#### transform(self, X)

Transform the data X according to the fitted NMF model

# **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Data matrix to be transformed by the model

### **Returns**

W [array, shape (n\_samples, n\_components)] Transformed data

## Examples using sklearn.decomposition.NMF

- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Faces dataset decompositions

# 6.9.10 sklearn.decomposition.PCA

```
class sklearn.decomposition.PCA (n\_components=None, copy=True, whiten=False, svd\_solver='auto', tol=0.0, iterated\_power='auto', random\_state=None)
```

Principal component analysis (PCA)

Linear dimensionality reduction using Singular Value Decomposition of the data to project it to a lower dimensional space. The input data is centered but not scaled for each feature before applying the SVD.

It uses the LAPACK implementation of the full SVD or a randomized truncated SVD by the method of Halko et al. 2009, depending on the shape of the input data and the number of components to extract.

It can also use the scipy.sparse.linalg ARPACK implementation of the truncated SVD.

Notice that this class does not support sparse input. See *TruncatedSVD* for an alternative with sparse data. Read more in the *User Guide*.

#### **Parameters**

**n\_components** [int, float, None or string] Number of components to keep. if n\_components is not set all components are kept:

```
n_components == min(n_samples, n_features)
```

If n\_components == 'mle' and svd\_solver == 'full', Minka's MLE is used to guess the dimension. Use of n\_components == 'mle' will interpret svd\_solver == 'auto' as svd\_solver == 'full'.

If  $0 < n_{\text{components}} < 1$  and  $svd_{\text{solver}} == 'full'$ , select the number of components such that the amount of variance that needs to be explained is greater than the percentage specified by  $n_{\text{components}}$ .

If  $svd\_solver == 'arpack'$ , the number of components must be strictly less than the minimum of  $n\_features$  and  $n\_samples$ .

Hence, the None case results in:

```
n_components == min(n_samples, n_features) - 1
```

**copy** [bool (default True)] If False, data passed to fit are overwritten and running fit(X).transform(X) will not yield the expected results, use fit\_transform(X) instead.

**whiten** [bool, optional (default False)] When True (False by default) the *components*\_ vectors are multiplied by the square root of n\_samples and then divided by the singular values to ensure uncorrelated outputs with unit component-wise variances.

Whitening will remove some information from the transformed signal (the relative variance scales of the components) but can sometime improve the predictive accuracy of the downstream estimators by making their data respect some hard-wired assumptions.

```
svd_solver [string {'auto', 'full', 'arpack', 'randomized'}]
```

**auto:** the solver is selected by a default policy based on X.shape and n\_components: if the input data is larger than 500x500 and the number of components to extract is lower than 80% of the smallest dimension of the data, then the more efficient 'randomized' method is enabled. Otherwise the exact full SVD is computed and optionally truncated afterwards.

**full:** run exact full SVD calling the standard LAPACK solver via scipy.linalg.svd and select the components by postprocessing

**arpack:** run SVD truncated to n\_components calling ARPACK solver via scipy. sparse.linalg.svds. It requires strictly  $0 < n_components < min(X.shape)$ 

randomized: run randomized SVD by the method of Halko et al.

New in version 0.18.0.

**tol** [float >= 0, optional (default .0)] Tolerance for singular values computed by svd\_solver == 'arpack'.

New in version 0.18.0.

**iterated\_power** [int >= 0, or 'auto', (default 'auto')] Number of iterations for the power method computed by svd\_solver == 'randomized'.

New in version 0.18.0.

random\_state [int, RandomState instance or None, optional (default None)] If int, random\_state is the seed used by the random number generator; If RandomState instance,
random\_state is the random number generator; If None, the random number generator is
the RandomState instance used by np.random. Used when svd\_solver == 'arpack' or
'randomized'.

New in version 0.18.0.

### **Attributes**

**components**\_ [array, shape (n\_components, n\_features)] Principal axes in feature space, representing the directions of maximum variance in the data. The components are sorted by explained\_variance\_.

**explained\_variance\_** [array, shape (n\_components,)] The amount of variance explained by each of the selected components.

Equal to n\_components largest eigenvalues of the covariance matrix of X.

New in version 0.18.

**explained\_variance\_ratio\_** [array, shape (n\_components,)] Percentage of variance explained by each of the selected components.

If n\_components is not set then all components are stored and the sum of the ratios is equal to 1.0.

**singular\_values**\_ [array, shape (n\_components,)] The singular values corresponding to each of the selected components. The singular values are equal to the 2-norms of the n\_components variables in the lower-dimensional space.

New in version 0.19.

**mean**\_ [array, shape (n\_features,)] Per-feature empirical mean, estimated from the training set. Equal to X.mean (axis=0).

- n\_components\_ [int] The estimated number of components. When n\_components is set to 'mle' or a number between 0 and 1 (with svd\_solver == 'full') this number is estimated from input data. Otherwise it equals the parameter n\_components, or the lesser value of n\_features and n\_samples if n\_components is None.
- noise\_variance\_ [float] The estimated noise covariance following the Probabilistic PCA model from Tipping and Bishop 1999. See "Pattern Recognition and Machine Learning" by C. Bishop, 12.2.1 p. 574 or http://www.miketipping.com/papers/met-mppca.pdf. It is required to compute the estimated data covariance and score samples.

Equal to the average of  $(min(n\_features, n\_samples) - n\_components)$  smallest eigenvalues of the covariance matrix of X.

### See also:

KernelPCA

SparsePCA

**TruncatedSVD** 

IncrementalPCA

### References

For n\_components == 'mle', this class uses the method of *Minka*, *T. P.* "Automatic choice of dimensionality for PCA". In NIPS, pp. 598-604

Implements the probabilistic PCA model from: Tipping, M. E., and Bishop, C. M. (1999). "Probabilistic principal component analysis". Journal of the Royal Statistical Society: Series B (Statistical Methodology), 61(3), 611-622. via the score and score\_samples methods. See http://www.miketipping.com/papers/met-mppca.pdf

For svd\_solver == 'arpack', refer to scipy.sparse.linalg.svds.

For svd\_solver == 'randomized', see: Halko, N., Martinsson, P. G., and Tropp, J. A. (2011). "Finding structure with randomness: Probabilistic algorithms for constructing approximate matrix decompositions". SIAM review, 53(2), 217-288. and also Martinsson, P. G., Rokhlin, V., and Tygert, M. (2011). "A randomized algorithm for the decomposition of matrices". Applied and Computational Harmonic Analysis, 30(1), 47-68.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.decomposition import PCA
>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> pca = PCA(n_components=2)
>>> pca.fit(X)
PCA(copy=True, iterated_power='auto', n_components=2, random_state=None,
    svd_solver='auto', tol=0.0, whiten=False)
>>> print(pca.explained_variance_ratio_)
[0.9924... 0.0075...]
>>> print(pca.singular_values_)
[6.30061... 0.54980...]
```

```
>>> pca = PCA(n_components=2, svd_solver='full')
>>> pca.fit(X)
PCA(copy=True, iterated_power='auto', n_components=2, random_state=None,
    svd_solver='full', tol=0.0, whiten=False)
>>> print(pca.explained_variance_ratio_)
[0.9924... 0.00755...]
>>> print(pca.singular_values_)
[6.30061... 0.54980...]
```

```
>>> pca = PCA(n_components=1, svd_solver='arpack')
>>> pca.fit(X)
PCA(copy=True, iterated_power='auto', n_components=1, random_state=None,
    svd_solver='arpack', tol=0.0, whiten=False)
>>> print(pca.explained_variance_ratio_)
[0.99244...]
>>> print(pca.singular_values_)
[6.30061...]
```

### **Methods**

fit(self, X[, y]) Fit the model with X.

Continued on next page

Table 6.59 – continued from previous page

	1 1 5
fit_transform(self, X[, y])	Fit the model with X and apply the dimensionality re-
	duction on X.
get_covariance(self)	Compute data covariance with the generative model.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Compute data precision matrix with the generative
	model.
inverse_transform(self, X)	Transform data back to its original space.
score(self, X[, y])	Return the average log-likelihood of all samples.
score_samples(self, X)	Return the log-likelihood of each sample.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Apply dimensionality reduction to X.

\_\_init\_\_(self, n\_components=None, copy=True, whiten=False, svd\_solver='auto', tol=0.0, iter-ated\_power='auto', random\_state=None)

## **fit** (*self*, *X*, *y*=*None*)

Fit the model with X.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.

y [Ignored]

### Returns

self [object] Returns the instance itself.

## fit\_transform(self, X, y=None)

Fit the model with X and apply the dimensionality reduction on X.

# **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.

y [Ignored]

## Returns

**X\_new** [array-like, shape (n\_samples, n\_components)]

## get covariance(self)

Compute data covariance with the generative model.

cov = components\_.T \* S\*\*2 \* components\_ + sigma2 \* eye(n\_features) where S\*\*2 contains the explained variances, and sigma2 contains the noise variances.

#### Returns

**cov** [array, shape=(n\_features, n\_features)] Estimated covariance of data.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### get precision(self)

Compute data precision matrix with the generative model.

Equals the inverse of the covariance but computed with the matrix inversion lemma for efficiency.

### Returns

**precision** [array, shape=(n\_features, n\_features)] Estimated precision of data.

# $inverse\_transform(self, X)$

Transform data back to its original space.

In other words, return an input X\_original whose transform would be X.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_components)] New data, where n\_samples is the number of samples and n\_components is the number of components.

## Returns

X\_original array-like, shape (n\_samples, n\_features)

### **Notes**

If whitening is enabled, inverse\_transform will compute the exact inverse operation, which includes reversing whitening.

# score(self, X, y=None)

Return the average log-likelihood of all samples.

See. "Pattern Recognition and Machine Learning" by C. Bishop, 12.2.1 p. 574 or http://www.miketipping.com/papers/met-mppca.pdf

#### **Parameters**

**X** [array, shape(n\_samples, n\_features)] The data.

y [Ignored]

### Returns

**ll** [float] Average log-likelihood of the samples under the current model

### score samples(self, X)

Return the log-likelihood of each sample.

See. "Pattern Recognition and Machine Learning" by C. Bishop, 12.2.1 p. 574 or http://www.miketipping.com/papers/met-mppca.pdf

### **Parameters**

**X** [array, shape(n\_samples, n\_features)] The data.

### Returns

Il [array, shape (n\_samples,)] Log-likelihood of each sample under the current model

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

### transform(self, X)

Apply dimensionality reduction to X.

X is projected on the first principal components previously extracted from a training set.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] New data, where n\_samples is the number of samples and n\_features is the number of features.

### Returns

**X\_new** [array-like, shape (n\_samples, n\_components)]

# **Examples**

```
>>> import numpy as np
>>> from sklearn.decomposition import IncrementalPCA
>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> ipca = IncrementalPCA(n_components=2, batch_size=3)
>>> ipca.fit(X)
IncrementalPCA(batch_size=3, copy=True, n_components=2, whiten=False)
>>> ipca.transform(X)
```

## Examples using sklearn.decomposition.PCA

- Multilabel classification
- Explicit feature map approximation for RBF kernels
- Faces recognition example using eigenfaces and SVMs
- A demo of K-Means clustering on the handwritten digits data
- Concatenating multiple feature extraction methods
- Pipelining: chaining a PCA and a logistic regression
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- The Iris Dataset
- PCA example with Iris Data-set
- Incremental PCA
- · Comparison of LDA and PCA 2D projection of Iris dataset
- Blind source separation using FastICA
- Principal components analysis (PCA)
- FastICA on 2D point clouds
- Kernel PCA

- Model selection with Probabilistic PCA and Factor Analysis (FA)
- Faces dataset decompositions
- Multi-dimensional scaling
- · Balance model complexity and cross-validated score
- Kernel Density Estimation
- Dimensionality Reduction with Neighborhood Components Analysis
- Using FunctionTransformer to select columns
- Importance of Feature Scaling

# 6.9.11 sklearn.decomposition.SparsePCA

```
 \begin{array}{c} \textbf{class} \text{ sklearn.decomposition.SparsePCA} (n\_components=None, & alpha=1, & ridge\_alpha=0.01, \\ max\_iter=1000, & tol=1e-08, & method='lars', \\ n\_jobs=None, & U\_init=None, & V\_init=None, \\ verbose=False, & random\_state=None, & normalize & components=False) \end{array}
```

Sparse Principal Components Analysis (SparsePCA)

Finds the set of sparse components that can optimally reconstruct the data. The amount of sparseness is controllable by the coefficient of the L1 penalty, given by the parameter alpha.

Read more in the User Guide.

### **Parameters**

**n\_components** [int,] Number of sparse atoms to extract.

alpha [float,] Sparsity controlling parameter. Higher values lead to sparser components.

**ridge\_alpha** [float,] Amount of ridge shrinkage to apply in order to improve conditioning when calling the transform method.

max\_iter [int,] Maximum number of iterations to perform.

tol [float,] Tolerance for the stopping condition.

- **method** [{'lars', 'cd'}] lars: uses the least angle regression method to solve the lasso problem (linear\_model.lars\_path) cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). Lars will be faster if the estimated components are sparse.
- n\_jobs [int or None, optional (default=None)] Number of parallel jobs to run. None means 1
   unless in a joblib.parallel\_backend context. -1 means using all processors. See
   Glossary for more details.
- U\_init [array of shape (n\_samples, n\_components),] Initial values for the loadings for warm restart scenarios.
- **V\_init** [array of shape (n\_components, n\_features),] Initial values for the components for warm restart scenarios.

**verbose** [int] Controls the verbosity; the higher, the more messages. Defaults to 0.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**normalize\_components** [boolean, optional (default=False)]

- if False, use a version of Sparse PCA without components normalization and without data centering. This is likely a bug and even though it's the default for backward compatibility, this should not be used.
- if True, use a version of Sparse PCA with components normalization and data centering.

New in version 0.20.

Deprecated since version 0.22: normalize\_components was added and set to False for backward compatibility. It would be set to True from 0.22 onwards.

### **Attributes**

components\_ [array, [n\_components, n\_features]] Sparse components extracted from the data.

**error**\_ [array] Vector of errors at each iteration.

**n\_iter\_** [int] Number of iterations run.

mean\_ [array, shape (n\_features,)] Per-feature empirical mean, estimated from the training set. Equal to X.mean (axis=0).

#### See also:

#### PCA

MiniBatchSparsePCA

DictionaryLearning

# **Examples**

### **Methods**

fit(self, X[, y])	Fit the model from data in X.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.

Continued on next page

# Table 6.60 - continued from previous page

transform(self, X)

Least Squares projection of the data onto the sparse components.

\_\_init\_\_ (self, n\_components=None, alpha=1, ridge\_alpha=0.01, max\_iter=1000, tol=1e-08, method='lars', n\_jobs=None, U\_init=None, V\_init=None, verbose=False, random\_state=None, normalize\_components=False)

### **fit** (*self*, *X*, *y=None*)

Fit the model from data in X.

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples in the number of samples and n\_features is the number of features.
- y [Ignored]

### **Returns**

self [object] Returns the instance itself.

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

## Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

### set params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

## transform(self, X)

Least Squares projection of the data onto the sparse components.

To avoid instability issues in case the system is under-determined, regularization can be applied (Ridge regression) via the ridge\_alpha parameter.

Note that Sparse PCA components orthogonality is not enforced as in PCA hence one cannot use a simple linear projection.

#### **Parameters**

**X** [array of shape (n\_samples, n\_features)] Test data to be transformed, must have the same number of features as the data used to train the model.

#### Returns

X\_new array, shape (n\_samples, n\_components) Transformed data.

# 6.9.12 sklearn.decomposition.SparseCoder

```
class sklearn.decomposition.SparseCoder(dictionary, transform_algorithm='omp', transform_n_nonzero_coefs=None, transform_alpha=None, split_sign=False, n_jobs=None, positive_code=False)
```

Sparse coding

Finds a sparse representation of data against a fixed, precomputed dictionary.

Each row of the result is the solution to a sparse coding problem. The goal is to find a sparse array code such that:

```
X ~= code * dictionary
```

Read more in the User Guide.

#### **Parameters**

- **dictionary** [array, [n\_components, n\_features]] The dictionary atoms used for sparse coding. Lines are assumed to be normalized to unit norm.
- transform\_algorithm [{'lasso\_lars', 'lasso\_cd', 'lars', 'omp', 'threshold'}] Algorithm used to
   transform the data: lars: uses the least angle regression method (linear\_model.lars\_path)
   lasso\_lars: uses Lars to compute the Lasso solution lasso\_cd: uses the coordinate descent
   method to compute the Lasso solution (linear\_model.Lasso). lasso\_lars will be faster if
   the estimated components are sparse. omp: uses orthogonal matching pursuit to estimate
   the sparse solution threshold: squashes to zero all coefficients less than alpha from the
   projection dictionary \* X'
- transform\_n\_nonzero\_coefs [int, 0.1 \* n\_features by default] Number of nonzero coefficients to target in each column of the solution. This is only used by algorithm='lars' and algorithm='omp' and is overridden by alpha in the *Orthogonal Matching Pursuit (OMP)* case.
- transform\_alpha [float, 1. by default] If algorithm='lasso\_lars' or algorithm='lasso\_cd', alpha is the penalty applied to the L1 norm. If algorithm='threshold', alpha is the absolute value of the threshold below which coefficients will be squashed to zero. If algorithm='omp', alpha is the tolerance parameter: the value of the reconstruction error targeted. In this case, it overrides n nonzero coefs.
- **split\_sign** [bool, False by default] Whether to split the sparse feature vector into the concatenation of its negative part and its positive part. This can improve the performance of downstream classifiers.

**n\_jobs** [int or None, optional (default=None)] Number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

**positive\_code** [bool] Whether to enforce positivity when finding the code.

New in version 0.20.

#### Attributes

components\_ [array, [n\_components, n\_features]] The unchanged dictionary atoms

## See also:

DictionaryLearning

MiniBatchDictionaryLearning

SparsePCA

MiniBatchSparsePCA

sparse\_encode

### **Methods**

fit(self, X[, y])	Do nothing and return the estimator unchanged
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Encode the data as a sparse combination of the dictio-
	nary atoms.

\_\_init\_\_ (self, dictionary, transform\_algorithm='omp', transform\_n\_nonzero\_coefs=None, transform\_alpha=None, split\_sign=False, n\_jobs=None, positive\_code=False)

# fit (self, X, y=None)

Do nothing and return the estimator unchanged

This method is just there to implement the usual API and hence work in pipelines.

### **Parameters**

- X [Ignored]
- y [Ignored]

## Returns

self [object] Returns the object itself

fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

# **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, X)

Encode the data as a sparse combination of the dictionary atoms.

Coding method is determined by the object parameter transform\_algorithm.

#### **Parameters**

X [array of shape (n\_samples, n\_features)] Test data to be transformed, must have the same number of features as the data used to train the model.

## Returns

**X\_new** [array, shape (n\_samples, n\_components)] Transformed data

# Examples using sklearn.decomposition.SparseCoder

Sparse coding with a precomputed dictionary

# 6.9.13 sklearn.decomposition.TruncatedSVD

```
class sklearn.decomposition. TruncatedSVD (n\_components=2, algorithm='randomized', n\_iter=5, random\_state=None, tol=0.0)

Dimensionality reduction using truncated SVD (aka LSA).
```

Difficultion of the state of th

This transformer performs linear dimensionality reduction by means of truncated singular value decomposition (SVD). Contrary to PCA, this estimator does not center the data before computing the singular value decomposition. This means it can work with scipy.sparse matrices efficiently.

In particular, truncated SVD works on term count/tf-idf matrices as returned by the vectorizers in sklearn.feature\_extraction.text. In that context, it is known as latent semantic analysis (LSA).

This estimator supports two algorithms: a fast randomized SVD solver, and a "naive" algorithm that uses ARPACK as an eigensolver on (X \* X.T) or (X.T \* X), whichever is more efficient.

Read more in the User Guide.

## **Parameters**

- **n\_components** [int, default = 2] Desired dimensionality of output data. Must be strictly less than the number of features. The default value is useful for visualisation. For LSA, a value of 100 is recommended.
- **algorithm** [string, default = "randomized"] SVD solver to use. Either "arpack" for the ARPACK wrapper in SciPy (scipy.sparse.linalg.svds), or "randomized" for the randomized algorithm due to Halko (2009).
- **n\_iter** [int, optional (default 5)] Number of iterations for randomized SVD solver. Not used by ARPACK. The default is larger than the default in *randomized\_svd* to handle sparse matrices that may have large slowly decaying spectrum.
- random\_state [int, RandomState instance or None, optional, default = None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- tol [float, optional] Tolerance for ARPACK. 0 means machine precision. Ignored by randomized SVD solver.

#### Attributes

```
components_ [array, shape (n_components, n_features)]
```

- **explained\_variance\_** [array, shape (n\_components,)] The variance of the training samples transformed by a projection to each component.
- **explained\_variance\_ratio\_** [array, shape (n\_components,)] Percentage of variance explained by each of the selected components.
- **singular\_values\_** [array, shape (n\_components,)] The singular values corresponding to each of the selected components. The singular values are equal to the 2-norms of the n\_components variables in the lower-dimensional space.

### See also:

#### PCA

#### **Notes**

SVD suffers from a problem called "sign indeterminacy", which means the sign of the components\_ and the output from transform depend on the algorithm and random state. To work around this, fit instances of this class to data once, then keep the instance around to do transformations.

### References

Finding structure with randomness: Stochastic algorithms for constructing approximate matrix decompositions Halko, et al., 2009 (arXiv:909) https://arxiv.org/pdf/0909.4061.pdf

# **Examples**

```
>>> from sklearn.decomposition import TruncatedSVD
>>> from sklearn.random_projection import sparse_random_matrix
>>> X = sparse_random_matrix(100, 100, density=0.01, random_state=42)
>>> svd = TruncatedSVD(n_components=5, n_iter=7, random_state=42)
>>> svd.fit(X)
```

### **Methods**

fit(self, X[, y])	Fit LSI model on training data X.
fit_transform(self, X[, y])	Fit LSI model to X and perform dimensionality reduc-
	tion on X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Transform X back to its original space.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Perform dimensionality reduction on X.

```
__init__ (self, n_components=2, algorithm='randomized', n_iter=5, random_state=None, tol=0.0)
```

# **fit** (*self*, *X*, *y=None*)

Fit LSI model on training data X.

### **Parameters**

**X** [{array-like, sparse matrix}, shape (n samples, n features)] Training data.

y [Ignored]

# Returns

self [object] Returns the transformer object.

# fit\_transform(self, X, y=None)

Fit LSI model to X and perform dimensionality reduction on X.

### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training data.

y [Ignored]

## Returns

**X\_new** [array, shape (n\_samples, n\_components)] Reduced version of X. This will always be a dense array.

### get params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

**params** [mapping of string to any] Parameter names mapped to their values.

### inverse\_transform(self, X)

Transform X back to its original space.

Returns an array X\_original whose transform would be X.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_components)] New data.

#### Returns

**X\_original** [array, shape (n\_samples, n\_features)] Note that this is always a dense array.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## transform(self, X)

Perform dimensionality reduction on X.

### **Parameters**

**X** [{array-like, sparse matrix}, shape (n samples, n features)] New data.

#### Returns

**X\_new** [array, shape (n\_samples, n\_components)] Reduced version of X. This will always be a dense array.

# Examples using sklearn.decomposition.TruncatedSVD

- Column Transformer with Heterogeneous Data Sources
- Hashing feature transformation using Totally Random Trees
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...
- Clustering text documents using k-means

$decomposition.dict\_learning(X,$	Solves a dictionary learning matrix factorization problem.
n_components,)	
$decomposition.dict\_learning\_online(X[,$	Solves a dictionary learning matrix factorization problem
])	online.
$decomposition.fastica(X[, n\_components,])$	Perform Fast Independent Component Analysis.
decomposition.non_negative_factorization	(X)ompute Non-negative Matrix Factorization (NMF)
decomposition.sparse_encode(X, dictionary[,	Sparse coding
])	

# 6.9.14 sklearn.decomposition.dict learning

```
sklearn.decomposition.dict_learning(X, n_components, alpha, max_iter=100, tol=1e-08, method='lars', n_jobs=None, dict_init=None, code_init=None, callback=None, verbose=False, random_state=None, return_n_iter=False, positive_dict=False, positive_code=False)
```

Solves a dictionary learning matrix factorization problem.

Finds the best dictionary and the corresponding sparse code for approximating the data matrix X by solving:

```
(U^*, V^*) = argmin 0.5 || X - U V ||_2^2 + alpha * || U ||_1
(U,V)
with || V_k ||_2 = 1 for all 0 <= k < n_components
```

where V is the dictionary and U is the sparse code.

Read more in the *User Guide*.

#### **Parameters**

**X** [array of shape (n\_samples, n\_features)] Data matrix.

**n\_components** [int,] Number of dictionary atoms to extract.

alpha [int,] Sparsity controlling parameter.

max\_iter [int,] Maximum number of iterations to perform.

tol [float,] Tolerance for the stopping condition.

**method** [{'lars', 'cd'}] lars: uses the least angle regression method to solve the lasso problem (linear\_model.lars\_path) cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). Lars will be faster if the estimated components are sparse.

**n\_jobs** [int or None, optional (default=None)] Number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

**dict\_init** [array of shape (n\_components, n\_features),] Initial value for the dictionary for warm restart scenarios.

code\_init [array of shape (n\_samples, n\_components),] Initial value for the sparse code for warm restart scenarios.

callback [callable or None, optional (default: None)] Callable that gets invoked every five iterations

verbose [bool, optional (default: False)] To control the verbosity of the procedure.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**return\_n\_iter** [bool] Whether or not to return the number of iterations.

**positive\_dict** [bool] Whether to enforce positivity when finding the dictionary.

New in version 0.20.

**positive\_code** [bool] Whether to enforce positivity when finding the code.

New in version 0.20.

### Returns

**code** [array of shape (n\_samples, n\_components)] The sparse code factor in the matrix factorization.

**dictionary** [array of shape (n\_components, n\_features),] The dictionary factor in the matrix factorization.

errors [array] Vector of errors at each iteration.

**n iter** [int] Number of iterations run. Returned only if return n iter is set to True.

## See also:

dict\_learning\_online
DictionaryLearning
MiniBatchDictionaryLearning
SparsePCA
MiniBatchSparsePCA

# 6.9.15 sklearn.decomposition.dict learning online

```
sklearn.decomposition.dict_learning_online (X, n\_components=2, alpha=1, n\_iter=100, return\_code=True, dict\_init=None, call-back=None, batch\_size=3, verbose=False, shuffle=True, n\_jobs=None, method='lars', iter\_offset=0, random\_state=None, return\_inner\_stats=False, inner\_stats=None, return\_n\_iter=False, positive\_dict=False, positive\_dict=False, positive\_code=False)
```

Solves a dictionary learning matrix factorization problem online.

Finds the best dictionary and the corresponding sparse code for approximating the data matrix X by solving:

```
(U^*, V^*) = argmin 0.5 || X - U V ||_2^2 + alpha * || U ||_1
(U, V)
with || V_k ||_2 = 1 for all 0 <= k < n_components
```

where V is the dictionary and U is the sparse code. This is accomplished by repeatedly iterating over minibatches by slicing the input data.

Read more in the *User Guide*.

### **Parameters**

**X** [array of shape (n\_samples, n\_features)] Data matrix.

**n\_components** [int,] Number of dictionary atoms to extract.

alpha [float,] Sparsity controlling parameter.

**n\_iter** [int,] Number of iterations to perform.

**return\_code** [boolean,] Whether to also return the code U or just the dictionary V.

**dict\_init** [array of shape (n\_components, n\_features),] Initial value for the dictionary for warm restart scenarios.

callback [callable or None, optional (default: None)] callable that gets invoked every five iterations

**batch\_size** [int,] The number of samples to take in each batch.

**verbose** [bool, optional (default: False)] To control the verbosity of the procedure.

**shuffle** [boolean,] Whether to shuffle the data before splitting it in batches.

**n\_jobs** [int or None, optional (default=None)] Number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

**method** [{'lars', 'cd'}] lars: uses the least angle regression method to solve the lasso problem (linear\_model.lars\_path) cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). Lars will be faster if the estimated components are sparse.

iter\_offset [int, default 0] Number of previous iterations completed on the dictionary used for initialization.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**return\_inner\_stats** [boolean, optional] Return the inner statistics A (dictionary covariance) and B (data approximation). Useful to restart the algorithm in an online setting. If return\_inner\_stats is True, return\_code is ignored

**inner\_stats** [tuple of (A, B) ndarrays] Inner sufficient statistics that are kept by the algorithm. Passing them at initialization is useful in online settings, to avoid loosing the history of the evolution. A (n\_components, n\_components) is the dictionary covariance matrix. B (n\_features, n\_components) is the data approximation matrix

**return\_n\_iter** [bool] Whether or not to return the number of iterations.

**positive\_dict** [bool] Whether to enforce positivity when finding the dictionary.

New in version 0.20.

**positive\_code** [bool] Whether to enforce positivity when finding the code.

New in version 0.20.

### Returns

code [array of shape (n\_samples, n\_components),] the sparse code (only returned if return\_code=True)

**dictionary** [array of shape (n\_components, n\_features),] the solutions to the dictionary learning problem

**n\_iter** [int] Number of iterations run. Returned only if return\_n\_iter is set to True.

#### See also:

dict\_learning
DictionaryLearning
MiniBatchDictionaryLearning
SparsePCA
MiniBatchSparsePCA

# 6.9.16 sklearn.decomposition.fastica

sklearn.decomposition.fastica(X,  $n\_components=None$ , algorithm='parallel', whiten=True, fun='logcosh',  $fun\_args=None$ ,  $max\_iter=200$ , tol=0.0001,  $w\_init=None$ ,  $random\_state=None$ ,  $return\_X\_mean=False$ ,  $compute\_sources=True$ ,  $return\_n\_iter=False$ )

Perform Fast Independent Component Analysis.

Read more in the User Guide.

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples is the number of samples and n\_features is the number of features.
- **n\_components** [int, optional] Number of components to extract. If None no dimension reduction is performed.
- **algorithm** [{'parallel', 'deflation'}, optional] Apply a parallel or deflational FASTICA algorithm.
- whiten [boolean, optional] If True perform an initial whitening of the data. If False, the data is assumed to have already been preprocessed: it should be centered, normed and white. Otherwise you will get incorrect results. In this case the parameter n\_components will be ignored.
- **fun** [string or function, optional. Default: 'logcosh'] The functional form of the G function used in the approximation to neg-entropy. Could be either 'logcosh', 'exp', or 'cube'. You can also provide your own function. It should return a tuple containing the value of the function, and of its derivative, in the point. The derivative should be averaged along its last dimension. Example:

```
def my_g(x): return x ** 3, np.mean(3 * x ** 2, axis=-1)
```

- **fun\_args** [dictionary, optional] Arguments to send to the functional form. If empty or None and if fun='logcosh', fun\_args will take value {'alpha': 1.0}
- **max\_iter** [int, optional] Maximum number of iterations to perform.
- **tol** [float, optional] A positive scalar giving the tolerance at which the un-mixing matrix is considered to have converged.
- **w\_init** [(n\_components, n\_components) array, optional] Initial un-mixing array of dimension (n.comp,n.comp). If None (default) then an array of normal r.v.'s is used.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- **return\_X\_mean** [bool, optional] If True, X\_mean is returned too.
- **compute\_sources** [bool, optional] If False, sources are not computed, but only the rotation matrix. This can save memory when working with big data. Defaults to True.
- **return\_n\_iter** [bool, optional] Whether or not to return the number of iterations.

#### Returns

**K** [array, shape (n\_components, n\_features) | None.] If whiten is 'True', K is the pre-whitening matrix that projects data onto the first n\_components principal components. If whiten is 'False', K is 'None'.

**W** [array, shape (n\_components, n\_components)] Estimated un-mixing matrix. The mixing matrix can be obtained by:

```
w = np.dot(W, K.T)
A = w.T * (w * w.T).I
```

- **S** [array, shape (n\_samples, n\_components) | None] Estimated source matrix
- **X\_mean** [array, shape (n\_features, )] The mean over features. Returned only if return\_X\_mean is True.
- **n\_iter** [int] If the algorithm is "deflation", n\_iter is the maximum number of iterations run across all components. Else they are just the number of iterations taken to converge. This is returned only when return\_n\_iter is set to True.

#### **Notes**

The data matrix X is considered to be a linear combination of non-Gaussian (independent) components i.e. X = AS where columns of S contain the independent components and A is a linear mixing matrix. In short ICA attempts to un-mix' the data by estimating an un-mixing matrix W where ``S = W K X.`

This implementation was originally made for data of shape [n\_features, n\_samples]. Now the input is transposed before the algorithm is applied. This makes it slightly faster for Fortran-ordered input.

Implemented using FastICA: A. Hyvarinen and E. Oja, Independent Component Analysis: Algorithms and Applications, Neural Networks, 13(4-5), 2000, pp. 411-430

# 6.9.17 sklearn.decomposition.non\_negative\_factorization

Compute Non-negative Matrix Factorization (NMF)

Find two non-negative matrices (W, H) whose product approximates the non-negative matrix X. This factorization can be used for example for dimensionality reduction, source separation or topic extraction.

The objective function is:

```
0.5 * ||X - WH||_Fro^2

+ alpha * l1_ratio * ||vec(W)||_1

+ alpha * l1_ratio * ||vec(H)||_1

+ 0.5 * alpha * (1 - l1_ratio) * ||W||_Fro^2

+ 0.5 * alpha * (1 - l1_ratio) * ||H||_Fro^2
```

# Where:

For multiplicative-update ('mu') solver, the Frobenius norm  $(0.5 * \|X - WH\|_{Fro^2})$  can be changed into another beta-divergence loss, by changing the beta\_loss parameter.

The objective function is minimized with an alternating minimization of W and H. If H is given and update\_H=False, it solves for W only.

### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Constant matrix.
- W [array-like, shape (n\_samples, n\_components)] If init='custom', it is used as initial guess for the solution.
- **H** [array-like, shape (n\_components, n\_features)] If init='custom', it is used as initial guess for the solution. If update\_H=False, it is used as a constant, to solve for W only.
- **n\_components** [integer] Number of components, if n\_components is not set all features are kept.
- init [None | 'random' | 'nndsvda' | 'nndsvda' | 'nndsvdar' | 'custom'] Method used to initialize the procedure. Default: 'random'.

The default value will change from 'random' to None in version 0.23 to make it consistent with decomposition.NMF.

Valid options:

- None: 'nndsvd' if n\_components < n\_features, otherwise 'random'.
- 'random': non-negative random matrices, scaled with: sqrt(X.mean()
   n components)
- 'nndsvd': Nonnegative Double Singular Value Decomposition (NNDSVD) initialization (better for sparseness)
- 'nndsvda': NNDSVD with zeros filled with the average of X (better when sparsity is not desired)
- 'nndsvdar': NNDSVD with zeros filled with small random values (generally faster, less accurate alternative to NNDSVDa for when sparsity is not desired)
- 'custom': use custom matrices W and H
- **update\_H** [boolean, default: True] Set to True, both W and H will be estimated from initial guesses. Set to False, only W will be estimated.
- **solver** ['cd' | 'mu'] Numerical solver to use: 'cd' is a Coordinate Descent solver that uses Fast Hierarchical

Alternating Least Squares (Fast HALS).

'mu' is a Multiplicative Update solver.

New in version 0.17: Coordinate Descent solver.

New in version 0.19: Multiplicative Update solver.

**beta\_loss** [float or string, default 'frobenius'] String must be in { 'frobenius', 'kullback-leibler', 'itakura-saito'}. Beta divergence to be minimized, measuring the distance between X and the dot product WH. Note that values different from 'frobenius' (or 2) and 'kullback-leibler' (or 1) lead to significantly slower fits. Note that for beta\_loss <= 0 (or 'itakura-saito'), the input matrix X cannot contain zeros. Used only in 'mu' solver.

New in version 0.19.

**tol** [float, default: 1e-4] Tolerance of the stopping condition.

max\_iter [integer, default: 200] Maximum number of iterations before timing out.

**alpha** [double, default: 0.] Constant that multiplies the regularization terms.

- **11\_ratio** [double, default: 0.] The regularization mixing parameter, with 0 <= 11\_ratio <= 1. For 11\_ratio = 0 the penalty is an elementwise L2 penalty (aka Frobenius Norm). For 11\_ratio = 1 it is an elementwise L1 penalty. For 0 < 11\_ratio < 1, the penalty is a combination of L1 and L2.
- **regularization** ['both' | 'components' | 'transformation' | None] Select whether the regularization affects the components (H), the transformation (W), both or none of them.
- random\_state [int, RandomState instance or None, optional, default: None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

verbose [integer, default: 0] The verbosity level.

shuffle [boolean, default: False] If true, randomize the order of coordinates in the CD solver.

#### Returns

- **W** [array-like, shape (n\_samples, n\_components)] Solution to the non-negative least squares problem.
- **H** [array-like, shape (n\_components, n\_features)] Solution to the non-negative least squares problem.
- **n\_iter** [int] Actual number of iterations.

# References

Cichocki, Andrzej, and P. H. A. N. Anh-Huy. "Fast local algorithms for large scale nonnegative matrix and tensor factorizations." IEICE transactions on fundamentals of electronics, communications and computer sciences 92.3: 708-721, 2009.

Fevotte, C., & Idier, J. (2011). Algorithms for nonnegative matrix factorization with the beta-divergence. Neural Computation, 23(9).

# **Examples**

```
>>> import numpy as np
>>> X = np.array([[1,1], [2, 1], [3, 1.2], [4, 1], [5, 0.8], [6, 1]])
>>> from sklearn.decomposition import non_negative_factorization
>>> W, H, n_iter = non_negative_factorization(X, n_components=2,
... init='random', random_state=0)
```

# 6.9.18 sklearn.decomposition.sparse encode

```
sklearn.decomposition.sparse_encode (X, dictionary, gram=None, cov=None, algorithm='lasso\_lars', n\_nonzero\_coefs=None, alpha=None, copy\_cov=True, init=None, max\_iter=1000, n\_jobs=None, check\_input=True, verbose=0, positive=False)
```

Each row of the result is the solution to a sparse coding problem. The goal is to find a sparse array code such that:

```
X ~= code * dictionary
```

Read more in the *User Guide*.

#### **Parameters**

- **X** [array of shape (n\_samples, n\_features)] Data matrix
- **dictionary** [array of shape (n\_components, n\_features)] The dictionary matrix against which to solve the sparse coding of the data. Some of the algorithms assume normalized rows for meaningful output.
- **gram** [array, shape=(n\_components, n\_components)] Precomputed Gram matrix, dictionary \* dictionary'
- **cov** [array, shape=(n\_components, n\_samples)] Precomputed covariance, dictionary' \* X
- algorithm [{'lasso\_lars', 'lasso\_cd', 'lars', 'omp', 'threshold'}] lars: uses the least angle regression method (linear\_model.lars\_path) lasso\_lars: uses Lars to compute the Lasso solution lasso\_cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). lasso\_lars will be faster if the estimated components are sparse. omp: uses orthogonal matching pursuit to estimate the sparse solution threshold: squashes to zero all coefficients less than alpha from the projection dictionary \* X'
- **n\_nonzero\_coefs** [int, 0.1 \* n\_features by default] Number of nonzero coefficients to target in each column of the solution. This is only used by algorithm='lars' and algorithm='omp' and is overridden by alpha in the *Orthogonal Matching Pursuit* (*OMP*) case.
- alpha [float, 1. by default] If algorithm='lasso\_lars' or algorithm='lasso\_cd', alpha is the penalty applied to the L1 norm. If algorithm='threshold', alpha is the absolute value of the threshold below which coefficients will be squashed to zero. If algorithm='omp', alpha is the tolerance parameter: the value of the reconstruction error targeted. In this case, it overrides n nonzero coefs.
- **copy\_cov** [boolean, optional] Whether to copy the precomputed covariance matrix; if False, it may be overwritten.
- init [array of shape (n\_samples, n\_components)] Initialization value of the sparse codes. Only
   used if algorithm='lasso cd'.
- max\_iter [int, 1000 by default] Maximum number of iterations to perform if algorithm='lasso\_cd'.
- n\_jobs [int or None, optional (default=None)] Number of parallel jobs to run. None means 1
   unless in a joblib.parallel\_backend context. -1 means using all processors. See
   Glossary for more details.
- **check\_input** [boolean, optional] If False, the input arrays X and dictionary will not be checked.
- **verbose** [int, optional] Controls the verbosity; the higher, the more messages. Defaults to 0.
- **positive** [boolean, optional] Whether to enforce positivity when finding the encoding.

New in version 0.20.

#### Returns

code [array of shape (n\_samples, n\_components)] The sparse codes

#### See also:

```
sklearn.linear_model.lars_path
sklearn.linear_model.orthogonal_mp
sklearn.linear_model.Lasso
SparseCoder
```

# 6.10 sklearn.discriminant\_analysis: Discriminant Analysis

Linear Discriminant Analysis and Quadratic Discriminant Analysis

User guide: See the Linear and Quadratic Discriminant Analysis section for further details.

discriminant_analysis.	Linear Discriminant Analysis
LinearDiscriminantAnalysis $([\ldots])$	
discriminant_analysis.	Quadratic Discriminant Analysis
${\it Quadratic Discriminant Analysis} ([\dots])$	

# 6.10.1 sklearn.discriminant\_analysis.LinearDiscriminantAnalysis

Linear Discriminant Analysis

A classifier with a linear decision boundary, generated by fitting class conditional densities to the data and using Bayes' rule.

The model fits a Gaussian density to each class, assuming that all classes share the same covariance matrix.

The fitted model can also be used to reduce the dimensionality of the input by projecting it to the most discriminative directions.

New in version 0.17: LinearDiscriminantAnalysis.

Read more in the *User Guide*.

# **Parameters**

solver [string, optional]

#### Solver to use, possible values:

- 'svd': Singular value decomposition (default). Does not compute the covariance matrix, therefore this solver is recommended for data with a large number of features.
- 'lsqr': Least squares solution, can be combined with shrinkage.
- 'eigen': Eigenvalue decomposition, can be combined with shrinkage.

shrinkage [string or float, optional]

Shrinkage parameter, possible values:

- None: no shrinkage (default).
- 'auto': automatic shrinkage using the Ledoit-Wolf lemma.
- float between 0 and 1: fixed shrinkage parameter.

Note that shrinkage works only with 'lsqr' and 'eigen' solvers.

**priors** [array, optional, shape (n classes,)] Class priors.

n\_components [int, optional (default=None)] Number of components (<= min(n\_classes - 1, n\_features)) for dimensionality reduction. If None, will be set to min(n\_classes - 1, n\_features).</p>

**store\_covariance** [bool, optional] Additionally compute class covariance matrix (default False), used only in 'svd' solver.

New in version 0.17.

tol [float, optional, (default 1.0e-4)] Threshold used for rank estimation in SVD solver.

New in version 0.17.

#### **Attributes**

**coef**\_ [array, shape (n\_features,) or (n\_classes, n\_features)] Weight vector(s).

**intercept**\_ [array, shape (n\_features,)] Intercept term.

**covariance** [array-like, shape (n\_features, n\_features)] Covariance matrix (shared by all classes).

**explained\_variance\_ratio\_** [array, shape (n\_components,)] Percentage of variance explained by each of the selected components. If n\_components is not set then all components are stored and the sum of explained variances is equal to 1.0. Only available when eigen or svd solver is used.

means\_ [array-like, shape (n\_classes, n\_features)] Class means.

priors\_ [array-like, shape (n\_classes,)] Class priors (sum to 1).

**scalings**\_ [array-like, shape (rank, n\_classes - 1)] Scaling of the features in the space spanned by the class centroids.

xbar\_ [array-like, shape (n\_features,)] Overall mean.

classes\_ [array-like, shape (n\_classes,)] Unique class labels.

### See also:

sklearn.discriminant\_analysis.QuadraticDiscriminantAnalysis Quadratic
nant Analysis

# **Notes**

The default solver is 'svd'. It can perform both classification and transform, and it does not rely on the calculation of the covariance matrix. This can be an advantage in situations where the number of features is large. However, the 'svd' solver cannot be used with shrinkage.

The 'lsqr' solver is an efficient algorithm that only works for classification. It supports shrinkage.

The 'eigen' solver is based on the optimization of the between class scatter to within class scatter ratio. It can be used for both classification and transform, and it supports shrinkage. However, the 'eigen' solver needs to compute the covariance matrix, so it might not be suitable for situations with a high number of features.

# **Examples**

# **Methods**

decision_function(self, X)	Predict confidence scores for samples.
fit(self, X, y)	Fit LinearDiscriminantAnalysis model according to the
· · · · · · · · · · · · · · · · · · ·	given training data and parameters.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict class labels for samples in X.
predict_log_proba(self, X)	Estimate log probability.
predict_proba(self, X)	Estimate probability.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Project data to maximize class separation.

```
__init__(self, solver='svd', shrinkage=None, priors=None, n_components=None, store_covariance=False, tol=0.0001)
```

# $decision_function(self, X)$

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

# Returns

array, shape=(n\_samples,) if n\_classes == 2 else (n\_samples, n\_classes) Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes\_[1] where >0 means this class would be predicted.

 $\mathbf{fit}\;(\mathit{self},\mathit{X},\mathit{y})$ 

Fit LinearDiscriminantAnalysis model according to the given training data and parameters.

Changed in version 0.19: *store\_covariance* has been moved to main constructor.

Changed in version 0.19: tol has been moved to main constructor.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data.

y [array, shape (n\_samples,)] Target values.

### fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

### predict (self, X)

Predict class labels for samples in X.

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

# Returns

C [array, shape [n\_samples]] Predicted class label per sample.

# $predict_log_proba(self, X)$

Estimate log probability.

# **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Input data.

#### Returns

**C** [array, shape (n\_samples, n\_classes)] Estimated log probabilities.

### predict proba(self, X)

Estimate probability.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Input data.

#### Returns

**C** [array, shape (n\_samples, n\_classes)] Estimated probabilities.

# score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

sample\_weight [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### **Returns**

self

### transform(self, X)

Project data to maximize class separation.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Input data.

#### **Returns**

**X\_new** [array, shape (n\_samples, n\_components)] Transformed data.

# Examples using sklearn.discriminant\_analysis.LinearDiscriminantAnalysis

- Normal and Shrinkage Linear Discriminant Analysis for classification
- Linear and Quadratic Discriminant Analysis with covariance ellipsoid
- Comparison of LDA and PCA 2D projection of Iris dataset
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...
- Dimensionality Reduction with Neighborhood Components Analysis

# 6.10.2 sklearn.discriminant\_analysis.QuadraticDiscriminantAnalysis

 ${\bf class} \; {\tt sklearn.discriminant\_analysis.QuadraticDiscriminantAnalysis} \; ({\it priors=None}, \\$ 

reg\_param=0.0, store\_covariance=False, tol=0.0001)

Quadratic Discriminant Analysis

A classifier with a quadratic decision boundary, generated by fitting class conditional densities to the data and using Bayes' rule.

The model fits a Gaussian density to each class.

New in version 0.17: QuadraticDiscriminantAnalysis

Read more in the User Guide.

#### **Parameters**

**priors** [array, optional, shape = [n\_classes]] Priors on classes

reg\_param [float, optional] Regularizes the covariance estimate as
 (1-reg\_param) \*Sigma + reg\_param\*np.eye(n\_features)

**store\_covariance** [boolean] If True the covariance matrices are computed and stored in the self.covariance\_attribute.

New in version 0.17.

tol [float, optional, default 1.0e-4] Threshold used for rank estimation.

New in version 0.17.

#### **Attributes**

**covariance** [list of array-like, shape = [n\_features, n\_features]] Covariance matrices of each class.

**means**\_ [array-like, shape = [n\_classes, n\_features]] Class means.

**priors**\_ [array-like, shape = [n\_classes]] Class priors (sum to 1).

**rotations**\_ [list of arrays] For each class k an array of shape [n\_features, n\_k], with n\_k = min(n\_features, number of elements in class k) It is the rotation of the Gaussian distribution, i.e. its principal axis.

**scalings**\_ [list of arrays] For each class k an array of shape [n\_k]. It contains the scaling of the Gaussian distributions along its principal axes, i.e. the variance in the rotated coordinate system.

#### See also:

sklearn.discriminant\_analysis.LinearDiscriminantAnalysis Linear Discriminant Analysis

# **Examples**

### **Methods**

decision_function(self, X)	Apply decision function to an array of samples.
fit(self, X, y)	Fit the model according to the given training data and
	parameters.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
	Opention and an area area

Continued on next page

Table 6.66 - continued from previous page

predict(self, X)	Perform classification on an array of test vectors X.
predict_log_proba(self, X)	Return posterior probabilities of classification.
predict_proba(self, X)	Return posterior probabilities of classification.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_ (self, priors=None, reg\_param=0.0, store\_covariance=False, tol=0.0001)

# $decision\_function(self, X)$

Apply decision function to an array of samples.

### **Parameters**

 $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] Array of samples (test vectors).

#### Returns

**C** [array, shape = [n\_samples, n\_classes] or [n\_samples,]] Decision function values related to each class, per sample. In the two-class case, the shape is [n\_samples,], giving the log likelihood ratio of the positive class.

# fit(self, X, y)

Fit the model according to the given training data and parameters.

Changed in version 0.19: store\_covariances has been moved to main constructor as store\_covariance

Changed in version 0.19: tol has been moved to main constructor.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vector, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array, shape = [n\_samples]] Target values (integers)

# get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

#### predict (self, X)

Perform classification on an array of test vectors X.

The predicted class C for each sample in X is returned.

# **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

#### Returns

**C** [array, shape = [n\_samples]]

# predict\_log\_proba (self, X)

Return posterior probabilities of classification.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Array of samples/test vectors.

#### Returns

C [array, shape = [n\_samples, n\_classes]] Posterior log-probabilities of classification per class.

### predict\_proba (self, X)

Return posterior probabilities of classification.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] Array of samples/test vectors.

#### Returns

C [array, shape = [n\_samples, n\_classes]] Posterior probabilities of classification per class.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.discriminant\_analysis.QuadraticDiscriminantAnalysis

- Classifier comparison
- Linear and Quadratic Discriminant Analysis with covariance ellipsoid

# 6.11 sklearn.dummy: Dummy estimators

**User guide:** See the *Model evaluation: quantifying the quality of predictions* section for further details.

dummy.DummyClassifier([strategy,])	DummyClassifier is a classifier that makes predictions us-
	ing simple rules.
dummy.DummyRegressor([strategy, constant,])	DummyRegressor is a regressor that makes predictions us-
	ing simple rules.

# 6.11.1 sklearn.dummy.DummyClassifier

**class** sklearn.dummy.**DummyClassifier** (*strategy='stratified'*, *random\_state=None*, *constant=None*)

DummyClassifier is a classifier that makes predictions using simple rules.

This classifier is useful as a simple baseline to compare with other (real) classifiers. Do not use it for real problems.

Read more in the User Guide.

# **Parameters**

**strategy** [str, default="stratified"] Strategy to use to generate predictions.

- "stratified": generates predictions by respecting the training set's class distribution.
- "most\_frequent": always predicts the most frequent label in the training set.
- "prior": always predicts the class that maximizes the class prior (like "most\_frequent") and predict\_proba returns the class prior.
- "uniform": generates predictions uniformly at random.
- "constant": always predicts a constant label that is provided by the user. This is useful for metrics that evaluate a non-majority class

New in version 0.17: Dummy Classifier now supports prior fitting strategy using parameter *prior*.

random\_state [int, RandomState instance or None, optional, default=None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**constant** [int or str or array of shape = [n\_outputs]] The explicit constant as predicted by the "constant" strategy. This parameter is useful only for the "constant" strategy.

#### **Attributes**

**classes** [array or list of array of shape =  $[n_{classes}]$ ] Class labels for each output.

**n\_classes**\_ [array or list of array of shape = [n\_classes]] Number of label for each output.

**class\_prior**\_ [array or list of array of shape = [n\_classes]] Probability of each class for each output.

**n\_outputs\_** [int,] Number of outputs.

**sparse\_output\_** [bool,] True if the array returned from predict is to be in sparse CSC format. Is automatically set to True if the input y is passed in sparse format.

# **Methods**

fit(self, X, y[, sample_weight])	Fit the random classifier.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Perform classification on test vectors X.
predict_log_proba(self, X)	Return log probability estimates for the test vectors X.
predict_proba(self, X)	Return probability estimates for the test vectors X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, strategy='stratified', random\_state=None, constant=None)

fit (self, X, y, sample\_weight=None)

Fit the random classifier.

#### **Parameters**

- X [{array-like, object with finite length or shape}] Training data, requires length = n\_samples
- y [array-like, shape = [n\_samples] or [n\_samples, n\_outputs]] Target values.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

#### Returns

**self** [object]

# get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# predict (self, X)

Perform classification on test vectors X.

#### **Parameters**

**X** [{array-like, object with finite length or shape}] Training data, requires length = n\_samples

# Returns

y [array, shape = [n\_samples] or [n\_samples, n\_outputs]] Predicted target values for X.

# predict\_log\_proba (self, X)

Return log probability estimates for the test vectors X.

#### **Parameters**

X [{array-like, object with finite length or shape}] Training data, requires length = n\_samples

### Returns

**P** [array-like or list of array-like of shape = [n\_samples, n\_classes]] Returns the log probability of the sample for each class in the model, where classes are ordered arithmetically for each output.

#### predict proba (self, X)

Return probability estimates for the test vectors X.

#### **Parameters**

X [{array-like, object with finite length or shape}] Training data, requires length = n\_samples

#### Returns

**P** [array-like or list of array-lke of shape = [n\_samples, n\_classes]] Returns the probability of the sample for each class in the model, where classes are ordered arithmetically, for each output.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

- **X** [{array-like, None}] Test samples with shape = (n\_samples, n\_features) or None. Passing None as test samples gives the same result as passing real test samples, since DummyClassifier operates independently of the sampled observations.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

```
sample_weight [array-like, shape = [n_samples], optional] Sample weights.
```

#### **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# 6.11.2 sklearn.dummy.DummyRegressor

**class** sklearn.dummy.**DummyRegressor** (*strategy='mean'*, *constant=None*, *quantile=None*) DummyRegressor is a regressor that makes predictions using simple rules.

This regressor is useful as a simple baseline to compare with other (real) regressors. Do not use it for real problems.

Read more in the User Guide.

# **Parameters**

**strategy** [str] Strategy to use to generate predictions.

- "mean": always predicts the mean of the training set
- "median": always predicts the median of the training set
- "quantile": always predicts a specified quantile of the training set, provided with the quantile parameter.

• "constant": always predicts a constant value that is provided by the user.

**constant** [int or float or array of shape =  $[n\_outputs]$ ] The explicit constant as predicted by the "constant" strategy. This parameter is useful only for the "constant" strategy.

**quantile** [float in [0.0, 1.0]] The quantile to predict using the "quantile" strategy. A quantile of 0.5 corresponds to the median, while 0.0 to the minimum and 1.0 to the maximum.

#### Attributes

**constant**\_ [float or array of shape [n\_outputs]] Mean or median or quantile of the training targets or constant value given by the user.

**n\_outputs\_** [int,] Number of outputs.

#### **Methods**

fit(self, X, y[, sample_weight])	Fit the random regressor.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, return_std])</pre>	Perform classification on test vectors X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_ (self, strategy='mean', constant=None, quantile=None)

fit (self, X, y, sample\_weight=None)

Fit the random regressor.

### **Parameters**

- X [{array-like, object with finite length or shape}] Training data, requires length = n\_samples
- y [array-like, shape = [n\_samples] or [n\_samples, n\_outputs]] Target values.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

# Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

predict (self, X, return\_std=False)

Perform classification on test vectors X.

### **Parameters**

X [{array-like, object with finite length or shape}] Training data, requires length = n\_samples

**return\_std** [boolean, optional] Whether to return the standard deviation of posterior prediction. All zeros in this case.

#### Returns

- y [array, shape = [n\_samples] or [n\_samples, n\_outputs]] Predicted target values for X.
- y\_std [array, shape = [n\_samples] or [n\_samples, n\_outputs]] Standard deviation of predictive distribution of query points.

# score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

- X [{array-like, None}] Test samples with shape = (n\_samples, n\_features) or None. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator. Passing None as test samples gives the same result as passing real test samples, since DummyRegressor operates independently of the sampled observations.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.
- **sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# 6.12 sklearn.ensemble: Ensemble Methods

The sklearn.ensemble module includes ensemble-based methods for classification, regression and anomaly detection.

**User guide:** See the *Ensemble methods* section for further details.

ensemble. AdaBoostClassifier([])	An AdaBoost classifier.
ensemble.AdaBoostRegressor([base_estimator,	An AdaBoost regressor.
])	
ensemble.BaggingClassifier([base_estimator,	A Bagging classifier.
])	

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ensemble.BaggingRegressor([base_estimator,	A Bagging regressor.
])	
ensemble. ${\tt ExtraTreesClassifier}([\dots])$	An extra-trees classifier.
ensemble.ExtraTreesRegressor([n_estimators,	An extra-trees regressor.
])	
ensemble.GradientBoostingClassifier([loss,	Gradient Boosting for classification.
])	
ensemble.GradientBoostingRegressor([loss,	Gradient Boosting for regression.
])	
ensemble. Isolation $Forest([n_{estimators},])$	Isolation Forest Algorithm
ensemble.RandomForestClassifier([])	A random forest classifier.
ensemble.RandomForestRegressor([])	A random forest regressor.
ensemble. Random Trees Embedding ([])	An ensemble of totally random trees.
ensemble.VotingClassifier(estimators[,])	Soft Voting/Majority Rule classifier for unfitted estimators.
ensemble.VotingRegressor(estimators[,])	Prediction voting regressor for unfitted estimators.
$ensemble. {\it HistGradientBoostingRegressor} ([$	. Histogram-based Gradient Boosting Regression Tree.
ensemble.HistGradientBoostingClassifier(	. H]stogram-based Gradient Boosting Classification Tree.

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### 6.12.1 sklearn.ensemble.AdaBoostClassifier

class sklearn.ensemble.AdaBoostClassifier (base\_estimator=None, n\_estimators=50, learning\_rate=1.0, algorithm='SAMME.R', random state=None)

An AdaBoost classifier.

An AdaBoost [1] classifier is a meta-estimator that begins by fitting a classifier on the original dataset and then fits additional copies of the classifier on the same dataset but where the weights of incorrectly classified instances are adjusted such that subsequent classifiers focus more on difficult cases.

This class implements the algorithm known as AdaBoost-SAMME [2].

Read more in the *User Guide*.

#### **Parameters**

- base\_estimator [object, optional (default=None)] The base estimator from which the boosted
  ensemble is built. Support for sample weighting is required, as well as proper
  classes\_ and n\_classes\_ attributes. If None, then the base estimator is
  DecisionTreeClassifier(max\_depth=1)
- **n\_estimators** [integer, optional (default=50)] The maximum number of estimators at which boosting is terminated. In case of perfect fit, the learning procedure is stopped early.
- **learning\_rate** [float, optional (default=1.)] Learning rate shrinks the contribution of each classifier by learning\_rate. There is a trade-off between learning\_rate and n\_estimators.
- algorithm [{'SAMME', 'SAMME.R'}, optional (default='SAMME.R')] If 'SAMME.R' then use the SAMME.R real boosting algorithm. base\_estimator must support calculation of class probabilities. If 'SAMME' then use the SAMME discrete boosting algorithm. The SAMME.R algorithm typically converges faster than SAMME, achieving a lower test error with fewer boosting iterations.
- **random\_state** [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance,

random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### **Attributes**

```
estimators_ [list of classifiers] The collection of fitted sub-estimators.
```

**classes** [array of shape = [n\_classes]] The classes labels.

n\_classes\_ [int] The number of classes.

estimator\_weights\_ [array of floats] Weights for each estimator in the boosted ensemble.

**estimator\_errors\_** [array of floats] Classification error for each estimator in the boosted ensemble.

**feature\_importances** [array of shape = [n\_features]] Return the feature importances (the higher, the more important the feature).

# See also:

```
AdaBoostRegressor, GradientBoostingClassifier
sklearn.tree.DecisionTreeClassifier
```

# References

```
[R33e4ec8c4ad5-1], [R33e4ec8c4ad5-2]
```

# **Examples**

#### Methods

decision_function(self, X)	Compute the decision function of X.
fit(self, X, y[, sample_weight])	Build a boosted classifier from the training set (X, y).
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict classes for X.
predict_log_proba(self, X)	Predict class log-probabilities for X.
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	1 0
predict_proba(self, X)	Predict class probabilities for X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.
staged_decision_function(self, X)	Compute decision function of X for each boosting itera-
	tion.
staged_predict(self, X)	Return staged predictions for X.
staged_predict_proba(self, X)	Predict class probabilities for X.
<pre>staged_score(self, X, y[, sample_weight])</pre>	Return staged scores for X, y.

\_\_init\_\_ (self, base\_estimator=None, n\_estimators=50, learning\_rate=1.0, algorithm='SAMME.R', random\_state=None)

# $decision_function(self, X)$

Compute the decision function of X.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.

#### Returns

score [array, shape = [n\_samples, k]] The decision function of the input samples. The order of outputs is the same of that of the *classes*\_ attribute. Binary classification is a special cases with k == 1, otherwise k==n\_classes. For binary classification, values closer to -1 or 1 mean more like the first or second class in classes\_, respectively.

# feature\_importances\_

Return the feature importances (the higher, the more important the feature).

#### Returns

**feature\_importances**\_ [array, shape = [n\_features]]

**fit** (*self*, *X*, *y*, *sample\_weight=None*)

Build a boosted classifier from the training set (X, y).

#### **Parameters**

- **X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.
- y [array-like of shape = [n\_samples]] The target values (class labels).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights. If None, the sample weights are initialized to 1 / n\_samples.

#### Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

#### predict (self, X)

Predict classes for X.

The predicted class of an input sample is computed as the weighted mean prediction of the classifiers in the ensemble.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.

#### **Returns**

y [array of shape = [n\_samples]] The predicted classes.

### predict\_log\_proba (self, X)

Predict class log-probabilities for X.

The predicted class log-probabilities of an input sample is computed as the weighted mean predicted class log-probabilities of the classifiers in the ensemble.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.

# Returns

**p** [array of shape = [n\_samples, n\_classes]] The class probabilities of the input samples. The order of outputs is the same of that of the *classes*\_ attribute.

# $predict_proba(self, X)$

Predict class probabilities for X.

The predicted class probabilities of an input sample is computed as the weighted mean predicted class probabilities of the classifiers in the ensemble.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.

#### Returns

**p** [array of shape = [n\_samples, n\_classes]] The class probabilities of the input samples. The order of outputs is the same of that of the *classes*\_ attribute.

#### score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

# **Parameters**

X [array-like, shape = (n samples, n features)] Test samples.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# staged\_decision\_function(self, X)

Compute decision function of X for each boosting iteration.

This method allows monitoring (i.e. determine error on testing set) after each boosting iteration.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.

#### Returns

**score** [generator of array, shape = [n\_samples, k]] The decision function of the input samples. The order of outputs is the same of that of the *classes*\_ attribute. Binary classification is a special cases with k == 1, otherwise k==n\_classes. For binary classification, values closer to -1 or 1 mean more like the first or second class in classes\_, respectively.

# staged\_predict (self, X)

Return staged predictions for X.

The predicted class of an input sample is computed as the weighted mean prediction of the classifiers in the ensemble.

This generator method yields the ensemble prediction after each iteration of boosting and therefore allows monitoring, such as to determine the prediction on a test set after each boost.

### **Parameters**

**X** [array-like of shape = [n\_samples, n\_features]] The input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.

#### Returns

y [generator of array, shape = [n\_samples]] The predicted classes.

# $staged\_predict\_proba(self, X)$

Predict class probabilities for X.

The predicted class probabilities of an input sample is computed as the weighted mean predicted class probabilities of the classifiers in the ensemble.

This generator method yields the ensemble predicted class probabilities after each iteration of boosting and therefore allows monitoring, such as to determine the predicted class probabilities on a test set after each boost.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.

#### Returns

**p** [generator of array, shape = [n\_samples]] The class probabilities of the input samples. The order of outputs is the same of that of the *classes*\_ attribute.

```
staged_score (self, X, y, sample_weight=None)
```

Return staged scores for X, y.

This generator method yields the ensemble score after each iteration of boosting and therefore allows monitoring, such as to determine the score on a test set after each boost.

#### **Parameters**

- **X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.
- y [array-like, shape = [n samples]] Labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### **Returns**

z [float]

# Examples using sklearn.ensemble.AdaBoostClassifier

- Classifier comparison
- Two-class AdaBoost
- Multi-class AdaBoosted Decision Trees
- Discrete versus Real AdaBoost
- Plot the decision surfaces of ensembles of trees on the iris dataset

# 6.12.2 sklearn.ensemble.AdaBoostRegressor

class sklearn.ensemble.AdaBoostRegressor(base\_estimator=None, n\_estimators=50, learning\_rate=1.0, loss='linear', random\_state=None)

An AdaBoost regressor.

An AdaBoost [1] regressor is a meta-estimator that begins by fitting a regressor on the original dataset and then fits additional copies of the regressor on the same dataset but where the weights of instances are adjusted according to the error of the current prediction. As such, subsequent regressors focus more on difficult cases.

This class implements the algorithm known as AdaBoost.R2 [2].

Read more in the User Guide.

# **Parameters**

- base\_estimator [object, optional (default=None)] The base estimator from which the boosted
  ensemble is built. Support for sample weighting is required. If None, then the base estimator is DecisionTreeRegressor (max\_depth=3)
- **n\_estimators** [integer, optional (default=50)] The maximum number of estimators at which boosting is terminated. In case of perfect fit, the learning procedure is stopped early.

**learning\_rate** [float, optional (default=1.)] Learning rate shrinks the contribution of each regressor by learning\_rate. There is a trade-off between learning\_rate and n\_estimators.

**loss** [{'linear', 'square', 'exponential'}, optional (default='linear')] The loss function to use when updating the weights after each boosting iteration.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### **Attributes**

**estimators**\_ [list of classifiers] The collection of fitted sub-estimators.

**estimator\_weights\_** [array of floats] Weights for each estimator in the boosted ensemble.

**estimator\_errors\_** [array of floats] Regression error for each estimator in the boosted ensemble.

**feature\_importances** [array of shape = [n\_features]] Return the feature importances (the higher, the more important the feature).

#### See also:

 ${\it AdaBoostClassifier, Gradient Boosting Regressor}$ 

#### References

[R0c261b7dee9d-1], [R0c261b7dee9d-2]

sklearn.tree.DecisionTreeRegressor

# **Examples**

#### Methods

fit(self, X, y[, sample\_weight])

Build a boosted regressor from the training set (X, y).

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	, , ,
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict regression value for X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.
staged_predict(self, X)	Return staged predictions for X.
staged_score(self, X, y[, sample_weight])	Return staged scores for X, y.

\_\_init\_\_(self, base\_estimator=None, n\_estimators=50, learning\_rate=1.0, loss='linear', ran-dom state=None)

### feature\_importances\_

Return the feature importances (the higher, the more important the feature).

#### Returns

**feature\_importances**\_ [array, shape = [n\_features]]

fit (self, X, y, sample\_weight=None)

Build a boosted regressor from the training set (X, y).

#### **Parameters**

- **X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.
- $\mathbf{y}$  [array-like of shape = [n\_samples]] The target values (real numbers).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights. If None, the sample weights are initialized to 1 / n\_samples.

# Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

#### predict (self, X)

Predict regression value for X.

The predicted regression value of an input sample is computed as the weighted median prediction of the classifiers in the ensemble.

### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.

# Returns

y [array of shape =  $[n_samples]$ ] The predicted regression values.

# score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R<sup>2</sup> is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R<sup>2</sup> score of 0.0.

#### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape =  $(n_samples)$  or  $(n_samples, n_outputs)$ ] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# staged\_predict (self, X)

Return staged predictions for X.

The predicted regression value of an input sample is computed as the weighted median prediction of the classifiers in the ensemble.

This generator method yields the ensemble prediction after each iteration of boosting and therefore allows monitoring, such as to determine the prediction on a test set after each boost.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples.

# Returns

y [generator of array, shape = [n samples]] The predicted regression values.

```
staged_score (self, X, y, sample_weight=None)
Return staged scores for X, y.
```

This generator method yields the ensemble score after each iteration of boosting and therefore allows monitoring, such as to determine the score on a test set after each boost.

#### **Parameters**

- **X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. COO, DOK, and LIL are converted to CSR.
- y [array-like, shape = [n\_samples]] Labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

z [float]

# Examples using sklearn.ensemble.AdaBoostRegressor

• Decision Tree Regression with AdaBoost

# 6.12.3 sklearn.ensemble.BaggingClassifier

```
 \begin{array}{lll} \textbf{class} \ \textbf{sklearn.ensemble.BaggingClassifier} \ (base\_estimator = None, & n\_estimator = 10, \\ max\_samples = 1.0, & max\_features = 1.0, & bootstrap\_features = False, \\ strap = True, & bootstrap\_features = False, \\ oob\_score = False, \ warm\_start = False, \ n\_jobs = None, \\ random \ state = None, \ verbose = 0) \end{array}
```

A Bagging classifier.

A Bagging classifier is an ensemble meta-estimator that fits base classifiers each on random subsets of the original dataset and then aggregate their individual predictions (either by voting or by averaging) to form a final prediction. Such a meta-estimator can typically be used as a way to reduce the variance of a black-box estimator (e.g., a decision tree), by introducing randomization into its construction procedure and then making an ensemble out of it.

This algorithm encompasses several works from the literature. When random subsets of the dataset are drawn as random subsets of the samples, then this algorithm is known as Pasting [Rb1846455d0e5-1]. If samples are drawn with replacement, then the method is known as Bagging [Rb1846455d0e5-2]. When random subsets of the dataset are drawn as random subsets of the features, then the method is known as Random Subspaces [Rb1846455d0e5-3]. Finally, when base estimators are built on subsets of both samples and features, then the method is known as Random Patches [Rb1846455d0e5-4].

Read more in the *User Guide*.

### **Parameters**

**base\_estimator** [object or None, optional (default=None)] The base estimator to fit on random subsets of the dataset. If None, then the base estimator is a decision tree.

**n estimators** [int, optional (default=10)] The number of base estimators in the ensemble.

max\_samples [int or float, optional (default=1.0)] The number of samples to draw from X to train each base estimator.

- If int, then draw max\_samples samples.
- If float, then draw max\_samples \* X.shape[0] samples.

- max\_features [int or float, optional (default=1.0)] The number of features to draw from X to train each base estimator.
  - If int, then draw max\_features features.
  - If float, then draw max\_features \* X.shape[1] features.
- **bootstrap** [boolean, optional (default=True)] Whether samples are drawn with replacement. If False, sampling without replacement is performed.
- **bootstrap\_features** [boolean, optional (default=False)] Whether features are drawn with replacement.
- **oob\_score** [bool, optional (default=False)] Whether to use out-of-bag samples to estimate the generalization error.
- warm\_start [bool, optional (default=False)] When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new ensemble. See *the Glossary*.
  - New in version 0.17: *warm\_start* constructor parameter.
- n\_jobs [int or None, optional (default=None)] The number of jobs to run in parallel for both fit and predict. None means 1 unless in a joblib.parallel\_backend context.
  -1 means using all processors. See Glossary for more details.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- **verbose** [int, optional (default=0)] Controls the verbosity when fitting and predicting.

# **Attributes**

**base\_estimator\_** [estimator] The base estimator from which the ensemble is grown.

estimators\_ [list of estimators] The collection of fitted base estimators.

estimators\_samples\_ [list of arrays] The subset of drawn samples for each base estimator.

estimators\_features\_ [list of arrays] The subset of drawn features for each base estimator.

**classes** [array of shape = [n classes]] The classes labels.

n\_classes\_ [int or list] The number of classes.

oob\_score\_ [float] Score of the training dataset obtained using an out-of-bag estimate.

oob\_decision\_function\_ [array of shape = [n\_samples, n\_classes]] Decision function computed with out-of-bag estimate on the training set. If n\_estimators is small it might be possible that a data point was never left out during the bootstrap. In this case, oob\_decision\_function\_ might contain NaN.

### References

[Rb1846455d0e5-1], [Rb1846455d0e5-2], [Rb1846455d0e5-3], [Rb1846455d0e5-4]

# **Methods**

decision_function(self, X)	Average of the decision functions of the base classifiers.
fit(self, X, y[, sample_weight])	Build a Bagging ensemble of estimators from the train-
	ing set $(X, y)$ .
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict class for X.
predict_log_proba(self, X)	Predict class log-probabilities for X.
predict_proba(self, X)	Predict class probabilities for X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, base\_estimator=None, n\_estimators=10, max\_samples=1.0, max\_features=1.0, bootstrap=True, bootstrap\_features=False, oob\_score=False, warm\_start=False, n\_jobs=None, random\_state=None, verbose=0)

# $decision\_function(self, X)$

Average of the decision functions of the base classifiers.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

# Returns

**score** [array, shape = [n\_samples, k]] The decision function of the input samples. The columns correspond to the classes in sorted order, as they appear in the attribute classes\_. Regression and binary classification are special cases with k == 1, otherwise  $k == n_classes$ .

### estimators\_samples\_

The subset of drawn samples for each base estimator.

Returns a dynamically generated list of indices identifying the samples used for fitting each member of the ensemble, i.e., the in-bag samples.

Note: the list is re-created at each call to the property in order to reduce the object memory footprint by not storing the sampling data. Thus fetching the property may be slower than expected.

**fit** (*self*, *X*, *y*, *sample\_weight=None*)

Build a Bagging ensemble of estimators from the training set(X, y).

#### **Parameters**

- **X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.
- y [array-like, shape = [n\_samples]] The target values (class labels in classification, real numbers in regression).

**sample\_weight** [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted. Note that this is supported only if the base estimator supports sample weighting.

# Returns

self [object]

#### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

#### predict (self, X)

Predict class for X.

The predicted class of an input sample is computed as the class with the highest mean predicted probability. If base estimators do not implement a predict\_proba method, then it resorts to voting.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

#### Returns

y [array of shape = [n\_samples]] The predicted classes.

# predict\_log\_proba (self, X)

Predict class log-probabilities for X.

The predicted class log-probabilities of an input sample is computed as the log of the mean predicted class probabilities of the base estimators in the ensemble.

#### **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

#### **Returns**

**p** [array of shape = [n\_samples, n\_classes]] The class log-probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes*\_.

# $predict_proba(self, X)$

Predict class probabilities for X.

The predicted class probabilities of an input sample is computed as the mean predicted class probabilities of the base estimators in the ensemble. If base estimators do not implement a predict\_proba method, then it resorts to voting and the predicted class probabilities of an input sample represents the proportion of estimators predicting each class.

# **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

### Returns

**p** [array of shape = [n\_samples, n\_classes]] The class probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes*\_.

# score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### **Returns**

self

# 6.12.4 sklearn.ensemble.BaggingRegressor

```
 \begin{array}{lll} \textbf{class} \text{ sklearn.ensemble.BaggingRegressor} & (base\_estimator=None, & n\_estimators=10, \\ & max\_samples=1.0, & max\_features=1.0, & bootstrap\_True, & bootstrap\_features=False, \\ & oob\_score=False, & warm\_start=False, & n\_jobs=None, \\ & & random\_state=None, & verbose=0) \end{array}
```

A Bagging regressor.

A Bagging regressor is an ensemble meta-estimator that fits base regressors each on random subsets of the original dataset and then aggregate their individual predictions (either by voting or by averaging) to form a final prediction. Such a meta-estimator can typically be used as a way to reduce the variance of a black-box estimator (e.g., a decision tree), by introducing randomization into its construction procedure and then making an ensemble out of it.

This algorithm encompasses several works from the literature. When random subsets of the dataset are drawn as random subsets of the samples, then this algorithm is known as Pasting [R4d113ba76fc0-1]. If samples are drawn with replacement, then the method is known as Bagging [R4d113ba76fc0-2]. When random subsets of the dataset are drawn as random subsets of the features, then the method is known as Random Subspaces [R4d113ba76fc0-3]. Finally, when base estimators are built on subsets of both samples and features, then the method is known as Random Patches [R4d113ba76fc0-4].

Read more in the User Guide.

#### **Parameters**

**base\_estimator** [object or None, optional (default=None)] The base estimator to fit on random subsets of the dataset. If None, then the base estimator is a decision tree.

**n\_estimators** [int, optional (default=10)] The number of base estimators in the ensemble.

**max\_samples** [int or float, optional (default=1.0)] The number of samples to draw from X to train each base estimator.

- If int, then draw max\_samples samples.
- If float, then draw max\_samples \* X.shape[0] samples.

**max\_features** [int or float, optional (default=1.0)] The number of features to draw from X to train each base estimator.

- If int, then draw max features features.
- If float, then draw max\_features \* X.shape[1] features.

**bootstrap** [boolean, optional (default=True)] Whether samples are drawn with replacement. If False, sampling without replacement is performed.

**bootstrap\_features** [boolean, optional (default=False)] Whether features are drawn with replacement.

**oob score** [bool] Whether to use out-of-bag samples to estimate the generalization error.

warm\_start [bool, optional (default=False)] When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new ensemble. See *the Glossary*.

n\_jobs [int or None, optional (default=None)] The number of jobs to run in parallel for both fit and predict. None means 1 unless in a joblib.parallel\_backend context.
-1 means using all processors. See Glossary for more details.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

verbose [int, optional (default=0)] Controls the verbosity when fitting and predicting.

#### **Attributes**

estimators\_ [list of estimators] The collection of fitted sub-estimators.

estimators\_samples\_ [list of arrays] The subset of drawn samples for each base estimator.

estimators\_features\_ [list of arrays] The subset of drawn features for each base estimator.

**oob\_score**\_ [float] Score of the training dataset obtained using an out-of-bag estimate.

**oob\_prediction**\_ [array of shape = [n\_samples]] Prediction computed with out-of-bag estimate on the training set. If n\_estimators is small it might be possible that a data point was never left out during the bootstrap. In this case, oob\_prediction\_ might contain NaN.

#### References

[R4d113ba76fc0-1], [R4d113ba76fc0-2], [R4d113ba76fc0-3], [R4d113ba76fc0-4]

#### **Methods**

fit(self, X, y[, sample_weight])	Build a Bagging ensemble of estimators from the train-
	ing set $(X, y)$ .
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict regression target for X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, base\_estimator=None, n\_estimators=10, max\_samples=1.0, max\_features=1.0, bootstrap=True, bootstrap\_features=False, oob\_score=False, warm\_start=False, n\_jobs=None, random\_state=None, verbose=0)

# estimators\_samples\_

The subset of drawn samples for each base estimator.

Returns a dynamically generated list of indices identifying the samples used for fitting each member of the ensemble, i.e., the in-bag samples.

Note: the list is re-created at each call to the property in order to reduce the object memory footprint by not storing the sampling data. Thus fetching the property may be slower than expected.

fit (self, X, y, sample\_weight=None)

**Build a Bagging ensemble of estimators from the training** set (X, y).

#### **Parameters**

- **X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.
- y [array-like, shape = [n\_samples]] The target values (class labels in classification, real numbers in regression).

**sample\_weight** [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted. Note that this is supported only if the base estimator supports sample weighting.

#### **Returns**

self [object]

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

### predict (self, X)

Predict regression target for X.

The predicted regression target of an input sample is computed as the mean predicted regression targets of the estimators in the ensemble.

# **Parameters**

**X** [{array-like, sparse matrix} of shape = [n\_samples, n\_features]] The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

### Returns

y [array of shape = [n\_samples]] The predicted values.

# score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares  $((y_true - y_pred) ** 2).sum()$  and v is the total sum of squares  $((y_true - y_true.mean()) ** 2).sum()$ . The best possible score

is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

 $\mathbf{y}$  [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for  $\mathbf{X}$ .

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### **Returns**

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.ensemble.BaggingRegressor

• Single estimator versus bagging: bias-variance decomposition

# 6.12.5 sklearn.ensemble.lsolationForest

```
class sklearn.ensemble.IsolationForest (n\_estimators=100, max\_samples='auto', contamination='legacy', max\_features=1.0, bootstrap=False, n\_jobs=None, behaviour='old', random\_state=None, verbose=0, warm\_start=False)
```

Isolation Forest Algorithm

Return the anomaly score of each sample using the IsolationForest algorithm

The IsolationForest 'isolates' observations by randomly selecting a feature and then randomly selecting a split value between the maximum and minimum values of the selected feature.

Since recursive partitioning can be represented by a tree structure, the number of splittings required to isolate a sample is equivalent to the path length from the root node to the terminating node.

This path length, averaged over a forest of such random trees, is a measure of normality and our decision function.

Random partitioning produces noticeably shorter paths for anomalies. Hence, when a forest of random trees collectively produce shorter path lengths for particular samples, they are highly likely to be anomalies.

Read more in the *User Guide*.

New in version 0.18.

#### **Parameters**

**n\_estimators** [int, optional (default=100)] The number of base estimators in the ensemble.

max\_samples [int or float, optional (default="auto")]

# The number of samples to draw from X to train each base estimator.

- If int, then draw max\_samples samples.
- If float, then draw max\_samples \* X.shape[0] samples.
- If "auto", then max\_samples=min(256, n\_samples).

If max\_samples is larger than the number of samples provided, all samples will be used for all trees (no sampling).

**contamination** [float in (0., 0.5), optional (default=0.1)] The amount of contamination of the data set, i.e. the proportion of outliers in the data set. Used when fitting to define the threshold on the decision function. If 'auto', the decision function threshold is determined as in the original paper.

Changed in version 0.20: The default value of contamination will change from 0.1 in 0.20 to 'auto' in 0.22.

max\_features [int or float, optional (default=1.0)] The number of features to draw from X to train each base estimator.

- If int, then draw max\_features features.
- If float, then draw max\_features \* X.shape[1] features.

**bootstrap** [boolean, optional (default=False)] If True, individual trees are fit on random subsets of the training data sampled with replacement. If False, sampling without replacement is performed.

**n\_jobs** [int or None, optional (default=None)] The number of jobs to run in parallel for both fit and predict. None means 1 unless in a joblib.parallel\_backend context.

-1 means using all processors. See Glossary for more details.

behaviour [str, default='old'] Behaviour of the decision\_function which can be either 'old' or 'new'. Passing behaviour='new' makes the decision\_function change to match other anomaly detection algorithm API which will be the default behaviour in the future. As explained in details in the offset\_ attribute documentation, the decision\_function becomes dependent on the contamination parameter, in such a way that 0 becomes its natural threshold to detect outliers.

New in version 0.20: behaviour is added in 0.20 for back-compatibility purpose.

Deprecated since version 0.20: behaviour='old' is deprecated in 0.20 and will not be possible in 0.22.

Deprecated since version 0.22: behaviour parameter will be deprecated in 0.22 and removed in 0.24.

**random\_state** [int, RandomState instance or None, optional (default=None)] If int, random state is the seed used by the random number generator; If RandomState instance,

random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**verbose** [int, optional (default=0)] Controls the verbosity of the tree building process.

warm\_start [bool, optional (default=False)] When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new forest. See *the Glossary*.

New in version 0.21.

# **Attributes**

estimators\_ [list of DecisionTreeClassifier] The collection of fitted sub-estimators.

estimators\_samples\_ [list of arrays] The subset of drawn samples for each base estimator.

max\_samples\_ [integer] The actual number of samples

offset\_ [float] Offset used to define the decision function from the raw scores. We have the relation: decision\_function = score\_samples - offset\_. Assuming behaviour == 'new', offset\_ is defined as follows. When the contamination parameter is set to "auto", the offset is equal to -0.5 as the scores of inliers are close to 0 and the scores of outliers are close to -1. When a contamination parameter different than "auto" is provided, the offset is defined in such a way we obtain the expected number of outliers (samples with decision function < 0) in training. Assuming the behaviour parameter is set to 'old', we always have offset\_ = -0.5, making the decision function independent from the contamination parameter.

# **Notes**

The implementation is based on an ensemble of ExtraTreeRegressor. The maximum depth of each tree is set to  $ceil(log_2(n))$  where n is the number of samples used to build the tree (see (Liu et al., 2008) for more details).

#### References

[Rd7ae0a2ae688-1], [Rd7ae0a2ae688-2]

# **Methods**

decision_function(self, X)	Average anomaly score of X of the base classifiers.
fit(self, X[, y, sample_weight])	Fit estimator.
<pre>fit_predict(self, X[, y])</pre>	Performs fit on X and returns labels for X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict if a particular sample is an outlier or not.
score_samples(self, X)	Opposite of the anomaly score defined in the original
	paper.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_ (self, n\_estimators=100, max\_samples='auto', contamination='legacy', max\_features=1.0, bootstrap=False, n\_jobs=None, behaviour='old', random\_state=None, verbose=0, warm\_start=False)

#### decision function (self, X)

Average anomaly score of X of the base classifiers.

The anomaly score of an input sample is computed as the mean anomaly score of the trees in the forest.

The measure of normality of an observation given a tree is the depth of the leaf containing this observation, which is equivalent to the number of splittings required to isolate this point. In case of several observations n left in the leaf, the average path length of a n left samples isolation tree is added.

#### **Parameters**

X [array-like or sparse matrix, shape (n\_samples, n\_features)] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr matrix.

#### Returns

**scores** [array, shape (n\_samples,)] The anomaly score of the input samples. The lower, the more abnormal. Negative scores represent outliers, positive scores represent inliers.

# estimators\_samples\_

The subset of drawn samples for each base estimator.

Returns a dynamically generated list of indices identifying the samples used for fitting each member of the ensemble, i.e., the in-bag samples.

Note: the list is re-created at each call to the property in order to reduce the object memory footprint by not storing the sampling data. Thus fetching the property may be slower than expected.

fit (self, X, y=None, sample\_weight=None)

Fit estimator.

#### **Parameters**

X [array-like or sparse matrix, shape (n\_samples, n\_features)] The input samples. Use dtype=np.float32 for maximum efficiency. Sparse matrices are also supported, use sparse csc\_matrix for maximum efficiency.

**sample\_weight** [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted.

y [Ignored] not used, present for API consistency by convention.

#### Returns

self [object]

# fit\_predict (self, X, y=None)

Performs fit on X and returns labels for X.

Returns -1 for outliers and 1 for inliers.

#### **Parameters**

- X [ndarray, shape (n\_samples, n\_features)] Input data.
- y [Ignored] not used, present for API consistency by convention.

### Returns

y [ndarray, shape (n\_samples,)] 1 for inliers, -1 for outliers.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

### predict (self, X)

Predict if a particular sample is an outlier or not.

#### **Parameters**

X [array-like or sparse matrix, shape (n\_samples, n\_features)] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr matrix.

### **Returns**

**is\_inlier** [array, shape (n\_samples,)] For each observation, tells whether or not (+1 or -1) it should be considered as an inlier according to the fitted model.

#### score samples (self, X)

Opposite of the anomaly score defined in the original paper.

The anomaly score of an input sample is computed as the mean anomaly score of the trees in the forest.

The measure of normality of an observation given a tree is the depth of the leaf containing this observation, which is equivalent to the number of splittings required to isolate this point. In case of several observations n\_left in the leaf, the average path length of a n\_left samples isolation tree is added.

#### **Parameters**

**X** [array-like or sparse matrix, shape (n\_samples, n\_features)] The input samples.

### Returns

**scores** [array, shape (n\_samples,)] The anomaly score of the input samples. The lower, the more abnormal.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## Examples using sklearn.ensemble.IsolationForest

- Comparing anomaly detection algorithms for outlier detection on toy datasets
- IsolationForest example

## 6.12.6 sklearn.ensemble.RandomTreesEmbedding

```
 \textbf{class} \; \texttt{sklearn.ensemble.RandomTreesEmbedding} \; (\textit{n\_estimators='warn'}, & \textit{max\_depth=5}, \\ & \textit{min\_samples\_split=2}, & \textit{min\_samples\_leaf=1}, \\ & \textit{min\_weight\_fraction\_leaf=0.0}, \\ & \textit{max\_leaf\_nodes=None}, \\ & \textit{min\_impurity\_decrease=0.0}, \\ & \textit{min\_impurity\_split=None}, \; \textit{sparse\_output=True}, \\ & \textit{n\_jobs=None}, \; \textit{random\_state=None}, \; \textit{verbose=0}, \\ & \textit{warm\_start=False}) \\ \end{aligned}
```

An ensemble of totally random trees.

An unsupervised transformation of a dataset to a high-dimensional sparse representation. A datapoint is coded according to which leaf of each tree it is sorted into. Using a one-hot encoding of the leaves, this leads to a binary coding with as many ones as there are trees in the forest.

The dimensionality of the resulting representation is  $n_{out} \le n_{estimators} * max_leaf_nodes$ . If  $max_leaf_nodes == None$ , the number of leaf nodes is at most  $n_{estimators} * 2 ** max_depth$ .

Read more in the User Guide.

#### **Parameters**

**n\_estimators** [integer, optional (default=10)] Number of trees in the forest.

Changed in version 0.20: The default value of n\_estimators will change from 10 in version 0.20 to 100 in version 0.22.

- max\_depth [integer, optional (default=5)] The maximum depth of each tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than min\_samples\_split samples.
- min\_samples\_split [int, float, optional (default=2)] The minimum number of samples required to split an internal node:
  - If int, then consider min samples split as the minimum number.
  - If float, then min\_samples\_split is a fraction and ceil (min\_samples\_split
     \* n samples) is the minimum number of samples for each split.

Changed in version 0.18: Added float values for fractions.

- min\_samples\_leaf [int, float, optional (default=1)] The minimum number of samples required to be at a leaf node. A split point at any depth will only be considered if it leaves at least min\_samples\_leaf training samples in each of the left and right branches. This may have the effect of smoothing the model, especially in regression.
  - If int, then consider min\_samples\_leaf as the minimum number.
  - If float, then min\_samples\_leaf is a fraction and ceil (min\_samples\_leaf \* n\_samples) is the minimum number of samples for each node.

Changed in version 0.18: Added float values for fractions.

- min\_weight\_fraction\_leaf [float, optional (default=0.)] The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample weight is not provided.
- max\_leaf\_nodes [int or None, optional (default=None)] Grow trees with max\_leaf\_nodes in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

min\_impurity\_decrease [float, optional (default=0.)] A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

where N is the total number of samples,  $N_t$  is the number of samples at the current node,  $N_t$  is the number of samples in the left child, and  $N_t$  is the number of samples in the right child.

 ${\tt N, N\_t, N\_t\_R} \ and \ {\tt N\_t\_L} \ all \ refer \ to \ the \ weighted \ sum, if \ {\tt sample\_weight} \ is \ passed.$ 

New in version 0.19.

**min\_impurity\_split** [float, (default=1e-7)] Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: min\_impurity\_split has been deprecated in favor of min\_impurity\_decrease in 0.19. The default value of min\_impurity\_split will change from 1e-7 to 0 in 0.23 and it will be removed in 0.25. Use min\_impurity\_decrease instead.

- **sparse\_output** [bool, optional (default=True)] Whether or not to return a sparse CSR matrix, as default behavior, or to return a dense array compatible with dense pipeline operators.
- n\_jobs [int or None, optional (default=None)] The number of jobs to run in parallel for both fit and predict. None means 1 unless in a joblib.parallel\_backend context.
  -1 means using all processors. See Glossary for more details.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**verbose** [int, optional (default=0)] Controls the verbosity when fitting and predicting.

warm\_start [bool, optional (default=False)] When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new forest. See *the Glossary*.

## **Attributes**

estimators\_ [list of DecisionTreeClassifier] The collection of fitted sub-estimators.

### References

[R6e47e53bacbd-1], [R6e47e53bacbd-2]

#### **Methods**

apply(self, X)	Apply trees in the forest to X, return leaf indices.
$decision\_path(self, X)$	Return the decision path in the forest
fit(self, X[, y, sample_weight])	Fit estimator.
<pre>fit_transform(self, X[, y, sample_weight])</pre>	Fit estimator and transform dataset.

Continued on next page

Table 6.77 - continued from previous page

<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform dataset.

\_\_init\_\_ (self, n\_estimators='warn', max\_depth=5, min\_samples\_split=2, min\_samples\_leaf=1, min\_weight\_fraction\_leaf=0.0, max\_leaf\_nodes=None, min\_impurity\_decrease=0.0, min\_impurity\_split=None, sparse\_output=True, n\_jobs=None, random\_state=None, verbose=0, warm\_start=False)

## apply(self, X)

Apply trees in the forest to X, return leaf indices.

#### **Parameters**

X [array-like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr\_matrix.

### Returns

**X\_leaves** [array\_like, shape = [n\_samples, n\_estimators]] For each datapoint x in X and for each tree in the forest, return the index of the leaf x ends up in.

## $decision_path(self, X)$

Return the decision path in the forest

New in version 0.18.

#### **Parameters**

**X** [array-like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr\_matrix.

## Returns

**indicator** [sparse csr array, shape = [n\_samples, n\_nodes]] Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

**n\_nodes\_ptr** [array of size (n\_estimators + 1, )] The columns from indicator[n\_nodes\_ptr[i]:n\_nodes\_ptr[i+1]] gives the indicator value for the i-th estimator.

## feature\_importances\_

Return the feature importances (the higher, the more important the feature).

#### Returns

**feature\_importances**\_ [array, shape = [n\_features]] The values of this array sum to 1, unless all trees are single node trees consisting of only the root node, in which case it will be an array of zeros.

fit (self, X, y=None, sample\_weight=None)

Fit estimator.

### **Parameters**

X [array-like or sparse matrix, shape=(n\_samples, n\_features)] The input samples. Use dtype=np.float32 for maximum efficiency. Sparse matrices are also supported, use sparse csc\_matrix for maximum efficiency.

sample\_weight [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they would result in any single class carrying a negative weight in either child node.

### **Returns**

self [object]

fit\_transform(self, X, y=None, sample\_weight=None)

Fit estimator and transform dataset.

### **Parameters**

X [array-like or sparse matrix, shape=(n\_samples, n\_features)] Input data used to build forests. Use dtype=np.float32 for maximum efficiency.

**sample\_weight** [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they would result in any single class carrying a negative weight in either child node.

### Returns

**X\_transformed** [sparse matrix, shape=(n\_samples, n\_out)] Transformed dataset.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## transform(self, X)

Transform dataset.

#### **Parameters**

X [array-like or sparse matrix, shape=(n\_samples, n\_features)] Input data to be transformed. Use dtype=np.float32 for maximum efficiency. Sparse matrices are also supported, use sparse csr\_matrix for maximum efficiency.

## Returns

**X\_transformed** [sparse matrix, shape=(n\_samples, n\_out)] Transformed dataset.

### Examples using sklearn.ensemble.RandomTreesEmbedding

- Hashing feature transformation using Totally Random Trees
- Feature transformations with ensembles of trees
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap. . .

## 6.12.7 sklearn.ensemble.VotingClassifier

Soft Voting/Majority Rule classifier for unfitted estimators.

New in version 0.17.

Read more in the *User Guide*.

#### **Parameters**

- estimators [list of (string, estimator) tuples] Invoking the fit method on the VotingClassifier will fit clones of those original estimators that will be stored in the class attribute self.estimators\_. An estimator can be set to None or 'drop' using set\_params.
- **voting** [str, {'hard', 'soft'} (default='hard')] If 'hard', uses predicted class labels for majority rule voting. Else if 'soft', predicts the class label based on the argmax of the sums of the predicted probabilities, which is recommended for an ensemble of well-calibrated classifiers.
- weights [array-like, shape (n\_classifiers,), optional (default='None')] Sequence of weights (float or int) to weight the occurrences of predicted class labels (hard voting) or class probabilities before averaging (soft voting). Uses uniform weights if None.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to run in parallel for fit. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- **flatten\_transform** [bool, optional (default=True)] Affects shape of transform output only when voting='soft' If voting='soft' and flatten\_transform=True, transform method returns matrix with shape (n\_samples, n\_classifiers \* n\_classes). If flatten\_transform=False, it returns (n\_classifiers, n\_samples, n\_classes).

### **Attributes**

**estimators** [list of classifiers] The collection of fitted sub-estimators as defined in estimators that are not None.

**named\_estimators\_** [Bunch object, a dictionary with attribute access] Attribute to access any fitted sub-estimators by name.

New in version 0.20.

classes\_ [array-like, shape (n\_predictions,)] The classes labels.

## See also:

**VotingRegressor** Prediction voting regressor.

## **Examples**

```
>>> import numpy as np
>>> from sklearn.linear_model import LogisticRegression
>>> from sklearn.naive_bayes import GaussianNB
>>> from sklearn.ensemble import RandomForestClassifier, VotingClassifier
>>> clf1 = LogisticRegression(solver='lbfgs', multi_class='multinomial',
                              random_state=1)
>>> clf2 = RandomForestClassifier(n_estimators=50, random_state=1)
>>> clf3 = GaussianNB()
>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> y = np.array([1, 1, 1, 2, 2, 2])
>>> eclf1 = VotingClassifier(estimators=[
           ('lr', clf1), ('rf', clf2), ('gnb', clf3)], voting='hard')
>>> eclf1 = eclf1.fit(X, y)
>>> print(eclf1.predict(X))
[1 1 1 2 2 2]
>>> np.array_equal(eclf1.named_estimators_.lr.predict(X),
                   eclf1.named_estimators_['lr'].predict(X))
>>> eclf2 = VotingClassifier(estimators=[
           ('lr', clf1), ('rf', clf2), ('gnb', clf3)],
           voting='soft')
>>> eclf2 = eclf2.fit(X, y)
>>> print(eclf2.predict(X))
[1 1 1 2 2 2]
>>> eclf3 = VotingClassifier(estimators=[
          ('lr', clf1), ('rf', clf2), ('gnb', clf3)],
          voting='soft', weights=[2,1,1],
          flatten_transform=True)
. . .
>>> eclf3 = eclf3.fit(X, y)
>>> print (eclf3.predict(X))
[1 1 1 2 2 2]
>>> print(eclf3.transform(X).shape)
(6, 6)
```

## **Methods**

fit(self, X, y[, sample_weight])	Fit the estimators.
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get the parameters of the ensemble estimator
predict(self, X)	Predict class labels for X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Setting the parameters for the ensemble estimator
transform(self, X)	Return class labels or probabilities for X for each esti-
	mator.

```
__init__ (self, estimators, voting='hard', weights=None, n_jobs=None, flatten_transform=True)

fit (self, X, y, sample_weight=None)

Fit the estimators.
```

## **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape (n\_samples,)] Target values.

**sample\_weight** [array-like, shape (n\_samples,) or None] Sample weights. If None, then samples are equally weighted. Note that this is supported only if all underlying estimators support sample weights.

#### Returns

self [object]

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get the parameters of the ensemble estimator

#### **Parameters**

**deep** [bool] Setting it to True gets the various estimators and the parameters of the estimators as well

## predict (self, X)

Predict class labels for X.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input samples.

## Returns

**maj** [array-like, shape (n\_samples,)] Predicted class labels.

## predict\_proba

Compute probabilities of possible outcomes for samples in X.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input samples.

### Returns

**avg** [array-like, shape (n\_samples, n\_classes)] Weighted average probability for each class per sample.

## score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

## **Parameters**

X [array-like, shape = (n samples, n features)] Test samples.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

### set params (self, \*\*params)

Setting the parameters for the ensemble estimator

Valid parameter keys can be listed with get\_params().

### **Parameters**

\*\*params [keyword arguments] Specific parameters using e.g. set\_params(parameter\_name=new\_value) In addition, to setting the parameters of the ensemble estimator, the individual estimators of the ensemble estimator can also be set or replaced by setting them to None.

## **Examples**

# In this example, the RandomForestClassifier is removed clf1 = LogisticRegression() clf2 = Random-ForestClassifier() eclf = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2)] eclf.set\_params(rf=None)

## transform(self, X)

Return class labels or probabilities for X for each estimator.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.

## Returns

## probabilities\_or\_labels

- If voting='soft' and flatten\_transform=True: returns array-like of shape (n\_classifiers, n\_samples \* n\_classes), being class probabilities calculated by each classifier.
- **If voting='soft' and `flatten\_transform=False:** array-like of shape (n\_classifiers, n\_samples, n\_classes)
- **If voting='hard':** array-like of shape (n\_samples, n\_classifiers), being class labels predicted by each classifier.

## Examples using sklearn.ensemble.VotingClassifier

- Plot the decision boundaries of a VotingClassifier
- Plot class probabilities calculated by the Voting Classifier

## 6.12.8 sklearn.ensemble.VotingRegressor

class sklearn.ensemble.VotingRegressor(estimators, weights=None, n\_jobs=None)
 Prediction voting regressor for unfitted estimators.

New in version 0.21.

A voting regressor is an ensemble meta-estimator that fits base regressors each on the whole dataset. It, then, averages the individual predictions to form a final prediction.

Read more in the *User Guide*.

#### **Parameters**

estimators [list of (string, estimator) tuples] Invoking the fit method on the VotingRegressor will fit clones of those original estimators that will be stored in the class attribute self.estimators\_. An estimator can be set to None or 'drop' using set\_params.

weights [array-like, shape (n\_regressors,), optional (default='None')] Sequence of weights (float or int) to weight the occurrences of predicted values before averaging. Uses uniform weights if None.

**n\_jobs** [int or None, optional (default=None)] The number of jobs to run in parallel for fit. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### Attributes

**estimators** [list of regressors] The collection of fitted sub-estimators as defined in estimators that are not None.

**named\_estimators\_** [Bunch object, a dictionary with attribute access] Attribute to access any fitted sub-estimators by name.

### See also:

VotingClassifier Soft Voting/Majority Rule classifier.

## **Examples**

```
>>> import numpy as np
>>> from sklearn.linear_model import LinearRegression
>>> from sklearn.ensemble import RandomForestRegressor
>>> from sklearn.ensemble import VotingRegressor
>>> r1 = LinearRegression()
>>> r2 = RandomForestRegressor(n_estimators=10, random_state=1)
>>> X = np.array([[1, 1], [2, 4], [3, 9], [4, 16], [5, 25], [6, 36]])
>>> y = np.array([2, 6, 12, 20, 30, 42])
>>> er = VotingRegressor([('lr', r1), ('rf', r2)])
>>> print(er.fit(X, y).predict(X))
[ 3.3 5.7 11.8 19.7 28. 40.3]
```

## **Methods**

fit(self, X, y[, sample_weight])	Fit the estimators.
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get the parameters of the ensemble estimator
predict(self, X)	Predict regression target for X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Setting the parameters for the ensemble estimator

Continued on next page

\_\_\_init\_\_\_(self, estimators, weights=None, n\_jobs=None)

**fit** (*self*, *X*, *y*, *sample\_weight=None*)

Fit the estimators.

### **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape (n\_samples,)] Target values.

**sample\_weight** [array-like, shape (n\_samples,) or None] Sample weights. If None, then samples are equally weighted. Note that this is supported only if all underlying estimators support sample weights.

#### Returns

self [object]

fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

## **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- **y** [numpy array of shape [n\_samples]] Target values.

## Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get the parameters of the ensemble estimator

## **Parameters**

**deep** [bool] Setting it to True gets the various estimators and the parameters of the estimators as well

### predict (self, X)

Predict regression target for X.

The predicted regression target of an input sample is computed as the mean predicted regression targets of the estimators in the ensemble.

## **Parameters**

**X** [{array-like, sparse matrix} of shape (n\_samples, n\_features)] The input samples.

### **Returns**

y [array of shape (n\_samples,)] The predicted values.

## score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares  $((y_true - y_pred) ** 2).sum()$  and v is the total sum of squares  $((y_true - y_true.mean()) ** 2).sum()$ . The best possible score

is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n samples) or (n samples, n outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### **Returns**

**score** [float] R^2 of self.predict(X) wrt. y.

### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

## set\_params (self, \*\*params)

Setting the parameters for the ensemble estimator

Valid parameter keys can be listed with get\_params().

## **Parameters**

\*\*params [keyword arguments] Specific parameters using e.g. set\_params(parameter\_name=new\_value) In addition, to setting the parameters of the ensemble estimator, the individual estimators of the ensemble estimator can also be set or replaced by setting them to None.

## **Examples**

# In this example, the RandomForestClassifier is removed clf1 = LogisticRegression() clf2 = Random-ForestClassifier() eclf = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2)] eclf.set\_params(rf=None)

### transform(self, X)

Return predictions for X for each estimator.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input samples.

### **Returns**

**predictions** array-like of shape (n\_samples, n\_classifiers), being values predicted by each regressor.

### Examples using sklearn.ensemble.VotingRegressor

• Plot individual and voting regression predictions

## 6.12.9 sklearn.ensemble.HistGradientBoostingRegressor

```
class sklearn.ensemble.HistGradientBoostingRegressor(loss='least_squares',
                                                                                            learn-
                                                                   ing\_rate=0.1,
                                                                                     max_iter=100,
                                                                   max_leaf_nodes=31,
                                                                   max_depth=None,
                                                                   min_samples_leaf=20,
                                                                   l2_regularization=0.0,
                                                                   max\_bins=256,
                                                                                     scoring=None,
                                                                   validation\_fraction=0.1,
                                                                   n_iter_no_change=None,
                                                                   tol=1e-07,
                                                                                verbose=0,
                                                                                              ran-
                                                                   dom state=None)
```

Histogram-based Gradient Boosting Regression Tree.

This estimator is much faster than GradientBoostingRegressor for big datasets (n\_samples >= 10 000). The input data X is pre-binned into integer-valued bins, which considerably reduces the number of splitting points to consider, and allows the algorithm to leverage integer-based data structures. For small sample sizes, GradientBoostingRegressor might be preferred since binning may lead to split points that are too approximate in this setting.

This implementation is inspired by LightGBM.

**Note:** This estimator is still **experimental** for now: the predictions and the API might change without any deprecation cycle. To use it, you need to explicitly import <code>enable\_hist\_gradient\_boosting</code>:

```
>>> # explicitly require this experimental feature
>>> from sklearn.experimental import enable_hist_gradient_boosting # noqa
>>> # now you can import normally from ensemble
>>> from sklearn.ensemble import HistGradientBoostingClassifier
```

#### **Parameters**

- **loss** [{'least\_squares'}, optional (default='least\_squares')] The loss function to use in the boosting process. Note that the "least squares" loss actually implements an "half least squares loss" to simplify the computation of the gradient.
- **learning\_rate** [float, optional (default=0.1)] The learning rate, also known as *shrinkage*. This is used as a multiplicative factor for the leaves values. Use 1 for no shrinkage.
- max\_iter [int, optional (default=100)] The maximum number of iterations of the boosting process, i.e. the maximum number of trees.
- max\_leaf\_nodes [int or None, optional (default=31)] The maximum number of leaves for each tree. Must be strictly greater than 1. If None, there is no maximum limit.
- max\_depth [int or None, optional (default=None)] The maximum depth of each tree. The depth of a tree is the number of nodes to go from the root to the deepest leaf. Must be strictly greater than 1. Depth isn't constrained by default.
- min\_samples\_leaf [int, optional (default=20)] The minimum number of samples per leaf. For small datasets with less than a few hundred samples, it is recommended to lower this value since only very shallow trees would be built.
- **12\_regularization** [float, optional (default=0)] The L2 regularization parameter. Use 0 for no regularization (default).

- max\_bins [int, optional (default=256)] The maximum number of bins to use. Before training, each feature of the input array X is binned into at most max\_bins bins, which allows for a much faster training stage. Features with a small number of unique values may use less than max\_bins bins. Must be no larger than 256.
- scoring [str or callable or None, optional (default=None)] Scoring parameter to use for early stopping. It can be a single string (see *The scoring parameter: defining model evaluation rules*) or a callable (see *Defining your scoring strategy from metric functions*). If None, the estimator's default scorer is used. If scoring='loss', early stopping is checked w.r.t the loss value. Only used if n\_iter\_no\_change is not None.
- **validation\_fraction** [int or float or None, optional (default=0.1)] Proportion (or absolute size) of training data to set aside as validation data for early stopping. If None, early stopping is done on the training data. Only used if n\_iter\_no\_change is not None.
- n\_iter\_no\_change [int or None, optional (default=None)] Used to determine when to "early stop". The fitting process is stopped when none of the last n\_iter\_no\_change scores are better than the "n\_iter\_no\_change 1"th-to-last one, up to some tolerance. If None or 0, no early-stopping is done.
- **tol** [float or None, optional (default=1e-7)] The absolute tolerance to use when comparing scores during early stopping. The higher the tolerance, the more likely we are to early stop: higher tolerance means that it will be harder for subsequent iterations to be considered an improvement upon the reference score.
- **verbose: int, optional (default=0)** The verbosity level. If not zero, print some information about the fitting process.
- **random\_state** [int, np.random.RandomStateInstance or None, optional (default=None)] Pseudo-random number generator to control the subsampling in the binning process, and the train/validation data split if early stopping is enabled. See *random\_state*.

## **Attributes**

- **n\_iter\_** [int] The number of iterations as selected by early stopping (if n\_iter\_no\_change is not None). Otherwise it corresponds to max\_iter.
- **n\_trees\_per\_iteration\_** [int] The number of tree that are built at each iteration. For regressors, this is always 1.
- **train\_score** [ndarray, shape (max\_iter + 1,)] The scores at each iteration on the training data. The first entry is the score of the ensemble before the first iteration. Scores are computed according to the scoring parameter. If scoring is not 'loss', scores are computed on a subset of at most 10 000 samples. Empty if no early stopping.
- validation\_score\_ [ndarray, shape (max\_iter + 1,)] The scores at each iteration on the heldout validation data. The first entry is the score of the ensemble before the first iteration. Scores are computed according to the scoring parameter. Empty if no early stopping or if validation\_fraction is None.

## **Examples**

```
>>> # To use this experimental feature, we need to explicitly ask for it:
>>> from sklearn.experimental import enable_hist_gradient_boosting # noqa
>>> from sklearn.ensemble import HistGradientBoostingRegressor
>>> from sklearn.datasets import load_boston
>>> X, y = load_boston(return_X_y=True)
>>> est = HistGradientBoostingRegressor().fit(X, y)
```

```
>>> est.score(X, y)
0.98...
```

## **Methods**

fit(self, X, y)	Fit the gradient boosting model.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict values for X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_(self, loss='least\_squares', learning\_rate=0.1, max\_iter=100, max\_leaf\_nodes=31, max\_depth=None, min\_samples\_leaf=20, l2\_regularization=0.0, max\_bins=256, scoring=None, validation\_fraction=0.1, n\_iter\_no\_change=None, tol=1e-07, verbose=0, random state=None)

## **fit** (self, X, y)

Fit the gradient boosting model.

### **Parameters**

**X** [array-like, shape=(n\_samples, n\_features)] The input samples.

y [array-like, shape=(n\_samples,)] Target values.

#### Returns

self [object]

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict values for X.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The input samples.

## Returns

y [ndarray, shape (n\_samples,)] The predicted values.

## score (self, X, y, sample weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## 6.12.10 sklearn.ensemble.HistGradientBoostingClassifier

```
 \begin{array}{lll} \textbf{class} & \textbf{sklearn.ensemble.HistGradientBoostingClassifier} (loss='auto', & learn-ing\_rate=0.1, & max\_iter=100, \\ & & max\_leaf\_nodes=31, & max\_depth=None, \\ & & min\_samples\_leaf=20, \\ & l2\_regularization=0.0, & max\_bins=256, & scoring=None, \\ & & validation\_fraction=0.1, & n\_iter\_no\_change=None, \\ & & tol=1e\text{-}07, & verbose=0, & random\_state=None) \\ \end{array}
```

Histogram-based Gradient Boosting Classification Tree.

This estimator is much faster than <code>GradientBoostingClassifier</code> for big datasets (n\_samples >= 10 000). The input data X is pre-binned into integer-valued bins, which considerably reduces the number of splitting points to consider, and allows the algorithm to leverage integer-based data structures. For small sample sizes, <code>GradientBoostingClassifier</code> might be preferred since binning may lead to split points that are too approximate in this setting.

This implementation is inspired by LightGBM.

**Note:** This estimator is still **experimental** for now: the predictions and the API might change without any deprecation cycle. To use it, you need to explicitly import enable hist gradient boosting:

```
>>> # explicitly require this experimental feature
>>> from sklearn.experimental import enable_hist_gradient_boosting # noqa
>>> # now you can import normally from ensemble
>>> from sklearn.ensemble import HistGradientBoostingClassifier
```

### **Parameters**

- loss [{'auto', 'binary\_crossentropy', 'categorical\_crossentropy'}, optional (default='auto')]
  The loss function to use in the boosting process. 'binary\_crossentropy' (also known as logistic loss) is used for binary classification and generalizes to 'categorical\_crossentropy' for multiclass classification. 'auto' will automatically choose either loss depending on the nature of the problem.
- **learning\_rate** [float, optional (default=0.1)] The learning rate, also known as *shrinkage*. This is used as a multiplicative factor for the leaves values. Use 1 for no shrinkage.
- max\_iter [int, optional (default=100)] The maximum number of iterations of the boosting process, i.e. the maximum number of trees for binary classification. For multiclass classification, n\_classes trees per iteration are built.
- max\_leaf\_nodes [int or None, optional (default=31)] The maximum number of leaves for each tree. Must be strictly greater than 1. If None, there is no maximum limit.
- max\_depth [int or None, optional (default=None)] The maximum depth of each tree. The depth of a tree is the number of nodes to go from the root to the deepest leaf. Must be strictly greater than 1. Depth isn't constrained by default.
- min\_samples\_leaf [int, optional (default=20)] The minimum number of samples per leaf. For small datasets with less than a few hundred samples, it is recommended to lower this value since only very shallow trees would be built.
- **12\_regularization** [float, optional (default=0)] The L2 regularization parameter. Use 0 for no regularization.
- max\_bins [int, optional (default=256)] The maximum number of bins to use. Before training, each feature of the input array X is binned into at most max\_bins bins, which allows for a much faster training stage. Features with a small number of unique values may use less than max\_bins bins. Must be no larger than 256.
- scoring [str or callable or None, optional (default=None)] Scoring parameter to use for early stopping. It can be a single string (see *The scoring parameter: defining model evaluation rules*) or a callable (see *Defining your scoring strategy from metric functions*). If None, the estimator's default scorer is used. If scoring='loss', early stopping is checked w.r.t the loss value. Only used if n\_iter\_no\_change is not None.
- **validation\_fraction** [int or float or None, optional (default=0.1)] Proportion (or absolute size) of training data to set aside as validation data for early stopping. If None, early stopping is done on the training data.
- n\_iter\_no\_change [int or None, optional (default=None)] Used to determine when to "early stop". The fitting process is stopped when none of the last n\_iter\_no\_change scores are better than the "n\_iter\_no\_change 1"th-to-last one, up to some tolerance. If None or 0, no early-stopping is done.

- **tol** [float or None, optional (default=1e-7)] The absolute tolerance to use when comparing scores. The higher the tolerance, the more likely we are to early stop: higher tolerance means that it will be harder for subsequent iterations to be considered an improvement upon the reference score.
- **verbose: int, optional (default=0)** The verbosity level. If not zero, print some information about the fitting process.
- **random\_state** [int, np.random.RandomStateInstance or None, optional (default=None)] Pseudo-random number generator to control the subsampling in the binning process, and the train/validation data split if early stopping is enabled. See *random\_state*.

### **Attributes**

- **n\_iter\_** [int] The number of estimators as selected by early stopping (if n\_iter\_no\_change is not None). Otherwise it corresponds to max\_iter.
- **n\_trees\_per\_iteration\_** [int] The number of tree that are built at each iteration. This is equal to 1 for binary classification, and to n\_classes for multiclass classification.
- **train\_score\_** [ndarray, shape (max\_iter + 1,)] The scores at each iteration on the training data. The first entry is the score of the ensemble before the first iteration. Scores are computed according to the scoring parameter. If scoring is not 'loss', scores are computed on a subset of at most 10 000 samples. Empty if no early stopping.
- validation\_score\_ [ndarray, shape (max\_iter + 1,)] The scores at each iteration on the heldout validation data. The first entry is the score of the ensemble before the first iteration. Scores are computed according to the scoring parameter. Empty if no early stopping or if validation\_fraction is None.

## **Examples**

```
>>> # To use this experimental feature, we need to explicitly ask for it:
>>> from sklearn.experimental import enable_hist_gradient_boosting # noqa
>>> from sklearn.ensemble import HistGradientBoostingRegressor
>>> from sklearn.datasets import load_iris
>>> X, y = load_iris(return_X_y=True)
>>> clf = HistGradientBoostingClassifier().fit(X, y)
>>> clf.score(X, y)
1.0
```

#### **Methods**

decision_function(self, X)	Compute the decision function of X.
fit(self, X, y)	Fit the gradient boosting model.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict classes for X.
predict_proba(self, X)	Predict class probabilities for X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_\_(self, loss='auto', learning\_rate=0.1, max\_iter=100, max\_leaf\_nodes=31, max\_depth=None, min\_samples\_leaf=20, l2\_regularization=0.0, max\_bins=256, scoring=None, validation\_fraction=0.1, n\_iter\_no\_change=None, tol=1e-07, verbose=0, random\_state=None)

### decision function (self, X)

Compute the decision function of X.

## **Parameters**

**X** [array-like, shape (n samples, n features)] The input samples.

#### Returns

**decision** [ndarray, shape (n\_samples,) or (n\_samples, n\_trees\_per\_iteration)] The raw predicted values (i.e. the sum of the trees leaves) for each sample. n\_trees\_per\_iteration is equal to the number of classes in multiclass classification.

## fit (self, X, y)

Fit the gradient boosting model.

### **Parameters**

- **X** [array-like, shape=(n\_samples, n\_features)] The input samples.
- y [array-like, shape=(n\_samples,)] Target values.

#### Returns

self [object]

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict classes for X.

### **Parameters**

**X** [array-like, shape (n samples, n features)] The input samples.

### Returns

y [ndarray, shape (n\_samples,)] The predicted classes.

## $predict_proba(self, X)$

Predict class probabilities for X.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The input samples.

## Returns

**p** [ndarray, shape (n\_samples, n\_classes)] The class probabilities of the input samples.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

## **Parameters**

X [array-like, shape = (n\_samples, n\_features)] Test samples.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

6.13 sklearn.exceptions: Exceptions and warnings

# 0.13 Skiedin exceptions. Exceptions and warnings

The sklearn.exceptions module includes all custom warnings and error classes used across scikit-learn.

exceptions.ChangedBehaviorWarning	Warning class used to notify the user of any change in the
	behavior.
exceptions.ConvergenceWarning	Custom warning to capture convergence problems
exceptions.DataConversionWarning	Warning used to notify implicit data conversions happening
	in the code.
exceptions.DataDimensionalityWarning	Custom warning to notify potential issues with data dimen-
	sionality.
exceptions.EfficiencyWarning	Warning used to notify the user of inefficient computation.
exceptions.FitFailedWarning	Warning class used if there is an error while fitting the es-
	timator.
exceptions.NotFittedError	Exception class to raise if estimator is used before fitting.
exceptions.NonBLASDotWarning	Warning used when the dot operation does not use BLAS.
exceptions.UndefinedMetricWarning	Warning used when the metric is invalid

# 6.13.1 sklearn.exceptions.ChangedBehaviorWarning

class sklearn.exceptions.ChangedBehaviorWarning

Warning class used to notify the user of any change in the behavior.

Changed in version 0.18: Moved from sklearn.base.

**Attributes** 

args

## **Methods**

with_traceback()	Exception.with_traceback(tb) - set selftraceback
	to tb and return self.

### with traceback()

Exception.with\_traceback(tb) - set self.\_\_traceback\_\_ to tb and return self.

## 6.13.2 sklearn.exceptions.ConvergenceWarning

## class sklearn.exceptions.ConvergenceWarning

Custom warning to capture convergence problems

Changed in version 0.18: Moved from sklearn.utils.

Attributes

args

### **Methods**

with_traceback()	Exception.with_traceback(tb) - set selftraceback
	to tb and return self.

## with\_traceback()

Exception.with\_traceback(tb) - set self.\_\_traceback\_\_ to tb and return self.

## Examples using sklearn.exceptions.ConvergenceWarning

- Multiclass sparse logisitic regression on newgroups20
- Early stopping of Stochastic Gradient Descent
- Compare Stochastic learning strategies for MLPClassifier
- Feature discretization

## 6.13.3 sklearn.exceptions.DataConversionWarning

## class sklearn.exceptions.DataConversionWarning

Warning used to notify implicit data conversions happening in the code.

This warning occurs when some input data needs to be converted or interpreted in a way that may not match the user's expectations.

## For example, this warning may occur when the user

• passes an integer array to a function which expects float input and will convert the input

- requests a non-copying operation, but a copy is required to meet the implementation's data-type expectations;
- passes an input whose shape can be interpreted ambiguously.

Changed in version 0.18: Moved from sklearn.utils.validation.

### **Attributes**

args

### **Methods**

with_traceback()	Exception.with_traceback(tb) - set selftraceback
	to tb and return self.

#### with traceback()

Exception.with\_traceback(tb) - set self.\_\_traceback\_\_ to tb and return self.

## 6.13.4 sklearn.exceptions.DataDimensionalityWarning

## class sklearn.exceptions.DataDimensionalityWarning

Custom warning to notify potential issues with data dimensionality.

For example, in random projection, this warning is raised when the number of components, which quantifies the dimensionality of the target projection space, is higher than the number of features, which quantifies the dimensionality of the original source space, to imply that the dimensionality of the problem will not be reduced.

Changed in version 0.18: Moved from sklearn.utils.

### **Attributes**

args

### **Methods**

with_traceback()	Exception.with_traceback(tb) - set selftraceback
	to tb and return self.

### with traceback()

Exception.with\_traceback(tb) - set self.\_\_traceback\_\_ to tb and return self.

## 6.13.5 sklearn.exceptions.EfficiencyWarning

## class sklearn.exceptions.EfficiencyWarning

Warning used to notify the user of inefficient computation.

This warning notifies the user that the efficiency may not be optimal due to some reason which may be included as a part of the warning message. This may be subclassed into a more specific Warning class.

New in version 0.18.

Attributes

args

## **Methods**

with_traceback()	Exception.with_traceback(tb) - set selftraceback
	to tb and return self.

```
with traceback()
```

Exception.with\_traceback(tb) - set self.\_\_traceback\_\_ to tb and return self.

## 6.13.6 sklearn.exceptions.FitFailedWarning

class sklearn.exceptions.FitFailedWarning

Warning class used if there is an error while fitting the estimator.

This Warning is used in meta estimators GridSearchCV and RandomizedSearchCV and the cross-validation helper function cross\_val\_score to warn when there is an error while fitting the estimator.

#### **Attributes**

args

## **Examples**

```
>>> from sklearn.model_selection import GridSearchCV
>>> from sklearn.svm import LinearSVC
>>> from sklearn.exceptions import FitFailedWarning
>>> import warnings
>>> warnings.simplefilter('always', FitFailedWarning)
>>> gs = GridSearchCV(LinearSVC(), {'C': [-1, -2]}, error_score=0, cv=2)
>>> X, y = [[1, 2], [3, 4], [5, 6], [7, 8]], [0, 0, 1, 1]
>>> with warnings.catch_warnings(record=True) as w:
            gs.fit(X, y) # This will raise a ValueError since C is < 0
. . .
        except ValueError:
. . .
            pass
. . .
        print (repr (w[-1].message))
. . .
FitFailedWarning('Estimator fit failed. The score on this train-test
partition for these parameters will be set to 0.000000.
Details: \nValueError: Penalty term must be positive; got (C=-2)\n'...)
```

Changed in version 0.18: Moved from sklearn.cross\_validation.

## **Methods**

with_traceback()	Exception.with_traceback(tb) - set selftraceback
	to tb and return self.

```
with traceback()
```

Exception.with traceback(tb) – set self. traceback to tb and return self.

## 6.13.7 sklearn.exceptions.NotFittedError

```
class sklearn.exceptions.NotFittedError
```

Exception class to raise if estimator is used before fitting.

This class inherits from both ValueError and AttributeError to help with exception handling and backward compatibility.

### **Attributes**

args

## **Examples**

```
>>> from sklearn.svm import LinearSVC
>>> from sklearn.exceptions import NotFittedError
>>> try:
... LinearSVC().predict([[1, 2], [2, 3], [3, 4]])
... except NotFittedError as e:
... print(repr(e))
...
NotFittedError('This LinearSVC instance is not fitted yet'...)
```

Changed in version 0.18: Moved from sklearn.utils.validation.

## **Methods**

```
with_traceback() Exception.with_traceback(tb) - set self.__traceback_
to tb and return self.
```

```
with_traceback()
```

Exception.with\_traceback(tb) - set self.\_\_traceback\_\_ to tb and return self.

## 6.13.8 sklearn.exceptions.NonBLASDotWarning

```
class sklearn.exceptions.NonBLASDotWarning
```

Warning used when the dot operation does not use BLAS.

This warning is used to notify the user that BLAS was not used for dot operation and hence the efficiency may be affected.

Changed in version 0.18: Moved from sklearn.utils.validation, extends EfficiencyWarning.

## Attributes

args

## **Methods**

with_traceback()	Exception.with_traceback(tb) - set selftraceback
	to tb and return self.

### with\_traceback()

Exception.with\_traceback(tb) - set self.\_\_traceback\_\_ to tb and return self.

## 6.13.9 sklearn.exceptions.UndefinedMetricWarning

class sklearn.exceptions.UndefinedMetricWarning

Warning used when the metric is invalid

Changed in version 0.18: Moved from sklearn.base.

Attributes

args

#### **Methods**

with_traceback()	Exception.with_traceback(tb) - set selftraceback
	to tb and return self.

## with\_traceback()

Exception.with\_traceback(tb) - set self.\_\_traceback\_\_ to tb and return self.

# 6.14 sklearn.experimental: Experimental

The *sklearn.experimental* module provides importable modules that enable the use of experimental features or estimators.

The features and estimators that are experimental aren't subject to deprecation cycles. Use them at your own risks!

```
experimental.enable_hist_gradient_boostinEnables histogram-based gradient boosting estimators.

experimental.enable_iterative_imputer

Enables IterativeImputer
```

## 6.14.1 sklearn.experimental.enable hist gradient boosting

Enables histogram-based gradient boosting estimators.

The API and results of these estimators might change without any deprecation cycle.

Importing this file dynamically sets the sklearn.ensemble.HistGradientBoostingClassifier and sklearn.ensemble.HistGradientBoostingRegressor as attributes of the ensemble module:

```
>>> # explicitly require this experimental feature
>>> from sklearn.experimental import enable_hist_gradient_boosting # noqa
>>> # now you can import normally from ensemble
```

```
>>> from sklearn.ensemble import HistGradientBoostingClassifier
>>> from sklearn.ensemble import HistGradientBoostingRegressor
```

The # noqa comment comment can be removed: it just tells linters like flake8 to ignore the import, which appears as unused.

## 6.14.2 sklearn.experimental.enable iterative imputer

Enables IterativeImputer

The API and results of this estimator might change without any deprecation cycle.

Importing this file dynamically sets sklearn.impute.IterativeImputer as an attribute of the impute module:

```
>>> # explicitly require this experimental feature
>>> from sklearn.experimental import enable_iterative_imputer # noqa
>>> # now you can import normally from impute
>>> from sklearn.impute import IterativeImputer
```

# 6.15 sklearn.feature\_extraction: Feature Extraction

The sklearn.feature\_extraction module deals with feature extraction from raw data. It currently includes methods to extract features from text and images.

User guide: See the *Feature extraction* section for further details.

```
feature_extraction.DictVectorizer([dtype, ...])

feature_extraction.FeatureHasher([...])

Implements feature hashing, aka the hashing trick.
```

## 6.15.1 sklearn.feature extraction.DictVectorizer

```
class sklearn.feature_extraction.DictVectorizer(dtype=<class 'numpy.float64'>, separa-
tor='=', sparse=True, sort=True)
```

Transforms lists of feature-value mappings to vectors.

This transformer turns lists of mappings (dict-like objects) of feature names to feature values into Numpy arrays or scipy.sparse matrices for use with scikit-learn estimators.

When feature values are strings, this transformer will do a binary one-hot (aka one-of-K) coding: one boolean-valued feature is constructed for each of the possible string values that the feature can take on. For instance, a feature "f" that can take on the values "ham" and "spam" will become two features in the output, one signifying "f=ham", the other "f=spam".

However, note that this transformer will only do a binary one-hot encoding when feature values are of type string. If categorical features are represented as numeric values such as int, the DictVectorizer can be followed by <code>sklearn.preprocessing.OneHotEncoder</code> to complete binary one-hot encoding.

Features that do not occur in a sample (mapping) will have a zero value in the resulting array/matrix.

Read more in the *User Guide*.

### **Parameters**

**dtype** [callable, optional] The type of feature values. Passed to Numpy array/scipy.sparse matrix constructors as the dtype argument.

**separator** [string, optional] Separator string used when constructing new features for one-hot coding.

**sparse** [boolean, optional.] Whether transform should produce scipy.sparse matrices. True by default.

**sort** [boolean, optional.] Whether feature\_names\_ and vocabulary\_ should be sorted when fitting. True by default.

### **Attributes**

vocabulary\_ [dict] A dictionary mapping feature names to feature indices.

**feature\_names\_** [list] A list of length n\_features containing the feature names (e.g., "f=ham" and "f=spam").

### See also:

**FeatureHasher** performs vectorization using only a hash function.

**sklearn.preprocessing.OrdinalEncoder** handles nominal/categorical features encoded as columns of arbitrary data types.

## **Examples**

## **Methods**

fit(self, X[, y])	Learn a list of feature name -> indices mappings.
<pre>fit_transform(self, X[, y])</pre>	Learn a list of feature name -> indices mappings and
	transform X.
get_feature_names(self)	Returns a list of feature names, ordered by their indices.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>inverse_transform(self, X[, dict_type])</pre>	Transform array or sparse matrix X back to feature map-
	pings.
<pre>restrict(self, support[, indices])</pre>	Restrict the features to those in support using feature
	selection.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

Continued on next page

## Table 6.95 – continued from previous page

transform(self, X)

Transform feature->value dicts to array or sparse matrix.

\_\_init\_\_ (self, dtype=<class 'numpy.float64'>, separator='=', sparse=True, sort=True)

### **fit** (self, X, y=None)

Learn a list of feature name -> indices mappings.

### **Parameters**

- **X** [Mapping or iterable over Mappings] Dict(s) or Mapping(s) from feature names (arbitrary Python objects) to feature values (strings or convertible to dtype).
- y [(ignored)]

### Returns

self

## fit\_transform(self, X, y=None)

Learn a list of feature name -> indices mappings and transform X.

Like fit(X) followed by transform(X), but does not require materializing X in memory.

### **Parameters**

- **X** [Mapping or iterable over Mappings] Dict(s) or Mapping(s) from feature names (arbitrary Python objects) to feature values (strings or convertible to dtype).
- y [(ignored)]

#### **Returns**

**Xa** [{array, sparse matrix}] Feature vectors; always 2-d.

## $\mathtt{get\_feature\_names}$ (self)

Returns a list of feature names, ordered by their indices.

If one-of-K coding is applied to categorical features, this will include the constructed feature names but not the original ones.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

## inverse\_transform(self, X, dict\_type=<class 'dict'>)

Transform array or sparse matrix X back to feature mappings.

X must have been produced by this DictVectorizer's transform or fit\_transform method; it may only have passed through transformers that preserve the number of features and their order.

In the case of one-hot/one-of-K coding, the constructed feature names and values are returned rather than the original ones.

#### **Parameters**

X [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Sample matrix.

**dict\_type** [callable, optional] Constructor for feature mappings. Must conform to the collections.Mapping API.

#### Returns

**D** [list of dict\_type objects, length = n\_samples] Feature mappings for the samples in X.

```
restrict (self, support, indices=False)
```

Restrict the features to those in support using feature selection.

This function modifies the estimator in-place.

#### **Parameters**

**support** [array-like] Boolean mask or list of indices (as returned by the get\_support member of feature selectors).

**indices** [boolean, optional] Whether support is a list of indices.

### **Returns**

self

## **Examples**

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

### transform(self, X)

Transform feature->value dicts to array or sparse matrix.

Named features not encountered during fit or fit\_transform will be silently ignored.

### **Parameters**

**X** [Mapping or iterable over Mappings, length = n\_samples] Dict(s) or Mapping(s) from feature names (arbitrary Python objects) to feature values (strings or convertible to dtype).

## Returns

**Xa** [{array, sparse matrix}] Feature vectors; always 2-d.

## Examples using sklearn.feature\_extraction.DictVectorizer

- Column Transformer with Heterogeneous Data Sources
- FeatureHasher and DictVectorizer Comparison

## 6.15.2 sklearn.feature\_extraction.FeatureHasher

Implements feature hashing, aka the hashing trick.

This class turns sequences of symbolic feature names (strings) into scipy.sparse matrices, using a hash function to compute the matrix column corresponding to a name. The hash function employed is the signed 32-bit version of Murmurhash3.

Feature names of type byte string are used as-is. Unicode strings are converted to UTF-8 first, but no Unicode normalization is done. Feature values must be (finite) numbers.

This class is a low-memory alternative to DictVectorizer and CountVectorizer, intended for large-scale (online) learning and situations where memory is tight, e.g. when running prediction code on embedded devices.

Read more in the *User Guide*.

#### **Parameters**

- **n\_features** [integer, optional] The number of features (columns) in the output matrices. Small numbers of features are likely to cause hash collisions, but large numbers will cause larger coefficient dimensions in linear learners.
- input\_type [string, optional, default "dict"] Either "dict" (the default) to accept dictionaries over (feature\_name, value); "pair" to accept pairs of (feature\_name, value); or "string" to accept single strings. feature\_name should be a string, while value should be a number. In the case of "string", a value of 1 is implied. The feature\_name is hashed to find the appropriate column for the feature. The value's sign might be flipped in the output (but see non\_negative, below).
- **dtype** [numpy type, optional, default np.float64] The type of feature values. Passed to scipy.sparse matrix constructors as the dtype argument. Do not set this to bool, np.boolean or any unsigned integer type.
- **alternate\_sign** [boolean, optional, default True] When True, an alternating sign is added to the features as to approximately conserve the inner product in the hashed space even for small n features. This approach is similar to sparse random projection.

### See also:

**DictVectorizer** vectorizes string-valued features using a hash table.

sklearn.preprocessing.OneHotEncoder handles nominal/categorical features.

## **Examples**

## **Methods**

fit(self[, X, y])	No-op.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, raw_X)	Transform a sequence of instances to a scipy.sparse ma-
	trix.

```
__init__ (self, n_features=1048576, input_type='dict', dtype=<class 'numpy.float64'>, alternate_sign=True)
```

fit (self, X=None, y=None)

No-op.

This method doesn't do anything. It exists purely for compatibility with the scikit-learn transformer API.

### **Parameters**

X [array-like]

## Returns

**self** [FeatureHasher]

fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

## **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

## Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## transform(self, raw\_X)

Transform a sequence of instances to a scipy.sparse matrix.

#### **Parameters**

raw\_X [iterable over iterable over raw features, length = n\_samples] Samples. Each sample must be iterable an (e.g., a list or tuple) containing/generating feature names (and optionally values, see the input\_type constructor argument) which will be hashed. raw\_X need not support the len function, so it can be the result of a generator; n\_samples is determined on the fly.

#### Returns

**X** [scipy.sparse matrix, shape = (n\_samples, self.n\_features)] Feature matrix, for use with estimators or further transformers.

## Examples using sklearn.feature\_extraction.FeatureHasher

• FeatureHasher and DictVectorizer Comparison

## 6.15.3 From images

The sklearn.feature\_extraction.image submodule gathers utilities to extract features from images.

feature_extraction.image.	Reshape a 2D image into a collection of patches
extract_patches_2d()	
feature_extraction.image.	Graph of the pixel-to-pixel connections
grid_to_graph(n_x,n_y)	
feature_extraction.image.	Graph of the pixel-to-pixel gradient connections
$img\_to\_graph(img[,])$	
feature_extraction.image.	Reconstruct the image from all of its patches.
reconstruct_from_patches_2d()	
feature_extraction.image.	Extracts patches from a collection of images
PatchExtractor([])	

### sklearn.feature\_extraction.image.extract patches 2d

```
sklearn.feature\_extraction.image.extract\_patches\_2d(image, patch\_size, \\ max\_patches=None, \\ dom\_state=None) \\ patch\_size, \\ random\_state=None)
```

Reshape a 2D image into a collection of patches

The resulting patches are allocated in a dedicated array.

Read more in the User Guide.

#### **Parameters**

image [array, shape = (image\_height, image\_width) or] (image\_height, image\_width,
 n\_channels) The original image data. For color images, the last dimension specifies the
 channel: a RGB image would have n\_channels=3.

patch\_size [tuple of ints (patch\_height, patch\_width)] the dimensions of one patch

**max\_patches** [integer or float, optional default is None] The maximum number of patches to extract. If max\_patches is a float between 0 and 1, it is taken to be a proportion of the total number of patches.

random\_state [int, RandomState instance or None, optional (default=None)] Pseudo number generator state used for random sampling to use if max\_patches is not None. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### Returns

**patches** [array, shape = (n\_patches, patch\_height, patch\_width) or] (n\_patches, patch\_height, patch\_width, n\_channels) The collection of patches extracted from the image, where n\_patches is either max\_patches or the total number of patches that can be extracted.

## **Examples**

```
>>> from sklearn.datasets import load_sample_image
>>> from sklearn.feature_extraction import image
>>> # Use the array data from the first image in this dataset:
>>> one_image = load_sample_image("china.jpg")
>>> print('Image shape: {}'.format(one_image.shape))
Image shape: (427, 640, 3)
>>> patches = image.extract_patches_2d(one_image, (2, 2))
>>> print('Patches shape: {}'.format(patches.shape))
Patches shape: (272214, 2, 2, 3)
>>> # Here are just two of these patches:
>>> print(patches[1])
[[[174 201 231]
  [174 201 231]]
 [[173 200 230]
  [173 200 230]]]
>>> print(patches[800])
[[[187 214 243]
  [188 215 244]]
 [[187 214 243]
  [188 215 244]]]
```

## Examples using sklearn.feature\_extraction.image.extract\_patches\_2d

- Online learning of a dictionary of parts of faces
- Image denoising using dictionary learning

### sklearn.feature\_extraction.image.grid to graph

```
sklearn.feature\_extraction.image.grid\_to\_graph (n\_x, n\_y, n\_z=1,\\ mask=None, return\_as=<class `scipy.sparse.coo.coo\_matrix'>,\\ dtype=<class `int'>)
```

Graph of the pixel-to-pixel connections

Edges exist if 2 voxels are connected.

#### **Parameters**

- **n\_x** [int] Dimension in x axis
- **n\_y** [int] Dimension in y axis
- **n\_z** [int, optional, default 1] Dimension in z axis

**mask** [ndarray of booleans, optional] An optional mask of the image, to consider only part of the pixels.

**return\_as** [np.ndarray or a sparse matrix class, optional] The class to use to build the returned adjacency matrix.

dtype [dtype, optional, default int] The data of the returned sparse matrix. By default it is int

### **Notes**

For scikit-learn versions 0.14.1 and prior, return\_as=np.ndarray was handled by returning a dense np.matrix instance. Going forward, np.ndarray returns an np.ndarray, as expected.

For compatibility, user code relying on this method should wrap its calls in np.asarray to avoid type issues.

## sklearn.feature\_extraction.image.img\_to\_graph

Graph of the pixel-to-pixel gradient connections

Edges are weighted with the gradient values.

Read more in the *User Guide*.

### **Parameters**

```
img [ndarray, 2D or 3D] 2D or 3D image
```

**mask** [ndarray of booleans, optional] An optional mask of the image, to consider only part of the pixels.

**return\_as** [np.ndarray or a sparse matrix class, optional] The class to use to build the returned adjacency matrix.

**dtype** [None or dtype, optional] The data of the returned sparse matrix. By default it is the dtype of img

## **Notes**

For scikit-learn versions 0.14.1 and prior, return\_as=np.ndarray was handled by returning a dense np.matrix instance. Going forward, np.ndarray returns an np.ndarray, as expected.

For compatibility, user code relying on this method should wrap its calls in np.asarray to avoid type issues.

### sklearn.feature extraction.image.reconstruct from patches 2d

```
sklearn.feature_extraction.image.reconstruct_from_patches_2d(patches, image size)
```

Reconstruct the image from all of its patches.

Patches are assumed to overlap and the image is constructed by filling in the patches from left to right, top to bottom, averaging the overlapping regions.

Read more in the *User Guide*.

### **Parameters**

patches [array, shape = (n\_patches, patch\_height, patch\_width) or] (n\_patches, patch\_height,
 patch\_width, n\_channels) The complete set of patches. If the patches contain colour
 information, channels are indexed along the last dimension: RGB patches would have
 n\_channels=3.

**image\_size** [tuple of ints (image\_height, image\_width) or] (image\_height, image\_width, n\_channels) the size of the image that will be reconstructed

### Returns

**image** [array, shape = image\_size] the reconstructed image

## Examples using sklearn.feature\_extraction.image.reconstruct\_from\_patches\_2d

• Image denoising using dictionary learning

### sklearn.feature\_extraction.image.PatchExtractor

Extracts patches from a collection of images

Read more in the User Guide.

### **Parameters**

patch\_size [tuple of ints (patch\_height, patch\_width)] the dimensions of one patch

**max\_patches** [integer or float, optional default is None] The maximum number of patches per image to extract. If max\_patches is a float in (0, 1), it is taken to mean a proportion of the total number of patches.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

## **Examples**

```
>>> from sklearn.datasets import load_sample_images
>>> from sklearn.feature_extraction import image
>>> # Use the array data from the second image in this dataset:
>>> X = load_sample_images().images[1]
>>> print('Image shape: {}'.format(X.shape))
Image shape: (427, 640, 3)
>>> pe = image.PatchExtractor(patch_size=(2, 2))
>>> pe_fit = pe.fit(X)
>>> pe_trans = pe.transform(X)
>>> print('Patches shape: {}'.format(pe_trans.shape))
Patches shape: (545706, 2, 2)
```

#### **Methods**

fit(self, X[, y])	Do nothing and return the estimator unchanged
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transforms the image samples in X into a matrix of
	patch data.

```
__init__ (self, patch_size=None, max_patches=None, random_state=None)
```

### **fit** (self, X, y=None)

Do nothing and return the estimator unchanged

This method is just there to implement the usual API and hence work in pipelines.

### **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] Training data.

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

### set params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

### transform(self, X)

Transforms the image samples in X into a matrix of patch data.

## **Parameters**

X [array, shape = (n\_samples, image\_height, image\_width) or] (n\_samples, image\_height, image\_width, n\_channels) Array of images from which to extract patches. For color images, the last dimension specifies the channel: a RGB image would have n\_channels=3.

#### Returns

patches [array, shape = (n\_patches, patch\_height, patch\_width) or] (n\_patches,
 patch\_height, patch\_width, n\_channels) The collection of patches extracted from the images, where n\_patches is either n\_samples \* max\_patches or the total number
 of patches that can be extracted.

# **6.15.4 From text**

The sklearn.feature\_extraction.text submodule gathers utilities to build feature vectors from text documents.

feature_extraction.text.	Convert a collection of text documents to a matrix of token
${\it CountVectorizer}([\ldots])$	counts
feature_extraction.text.	Convert a collection of text documents to a matrix of token
HashingVectorizer([])	occurrences
feature_extraction.text.	Transform a count matrix to a normalized tf or tf-idf repre-
$ extit{TfidfTransformer}([\dots])$	sentation
feature_extraction.text.	Convert a collection of raw documents to a matrix of TF-
TfidfVectorizer([])	IDF features.

# sklearn.feature extraction.text.CountVectorizer

```
class sklearn.feature_extraction.text.CountVectorizer(input='content', encoding='utf-
                                                                               decode error='strict',
                                                                      8',
                                                                     strip accents=None,
                                                                                                low-
                                                                     ercase=True,
                                                                                          preproces-
                                                                     sor=None.
                                                                                    tokenizer=None,
                                                                     stop_words=None,
                                                                     ken \ pattern='(?u)\b\w\w+\b',
                                                                     ngram\ range=(1,
                                                                                        1),
                                                                     lyzer='word',
                                                                                        max df=1.0,
                                                                     min df=1, max features=None,
                                                                      vocabulary=None, binary=False,
                                                                      dtype = \langle class 'numpy.int64' \rangle
```

Convert a collection of text documents to a matrix of token counts

This implementation produces a sparse representation of the counts using scipy.sparse.csr\_matrix.

If you do not provide an a-priori dictionary and you do not use an analyzer that does some kind of feature selection then the number of features will be equal to the vocabulary size found by analyzing the data.

Read more in the User Guide.

# **Parameters**

**input** [string {'filename', 'file', 'content'}] If 'filename', the sequence passed as an argument to fit is expected to be a list of filenames that need reading to fetch the raw content to analyze.

If 'file', the sequence items must have a 'read' method (file-like object) that is called to fetch the bytes in memory.

Otherwise the input is expected to be the sequence strings or bytes items are expected to be analyzed directly.

- **encoding** [string, 'utf-8' by default.] If bytes or files are given to analyze, this encoding is used to decode.
- **decode\_error** [{'strict', 'ignore', 'replace'}] Instruction on what to do if a byte sequence is given to analyze that contains characters not of the given encoding. By default, it is 'strict', meaning that a UnicodeDecodeError will be raised. Other values are 'ignore' and 'replace'.
- strip\_accents [{'ascii', 'unicode', None}] Remove accents and perform other character normalization during the preprocessing step. 'ascii' is a fast method that only works on characters that have an direct ASCII mapping. 'unicode' is a slightly slower method that works on any characters. None (default) does nothing.

Both 'ascii' and 'unicode' use NFKD normalization from unicodedata.normalize.

- lowercase [boolean, True by default] Convert all characters to lowercase before tokenizing.
- **preprocessor** [callable or None (default)] Override the preprocessing (string transformation) stage while preserving the tokenizing and n-grams generation steps.
- **tokenizer** [callable or None (default)] Override the string tokenization step while preserving the preprocessing and n-grams generation steps. Only applies if analyzer == 'word'.
- **stop\_words** [string {'english'}, list, or None (default)] If 'english', a built-in stop word list for English is used. There are several known issues with 'english' and you should consider an alternative (see *Using stop words*).

If a list, that list is assumed to contain stop words, all of which will be removed from the resulting tokens. Only applies if analyzer == 'word'.

If None, no stop words will be used. max\_df can be set to a value in the range [0.7, 1.0) to automatically detect and filter stop words based on intra corpus document frequency of terms.

- **token\_pattern** [string] Regular expression denoting what constitutes a "token", only used if analyzer == 'word'. The default regexp select tokens of 2 or more alphanumeric characters (punctuation is completely ignored and always treated as a token separator).
- ngram\_range [tuple (min\_n, max\_n)] The lower and upper boundary of the range of n-values
  for different n-grams to be extracted. All values of n such that min\_n <= n <= max\_n will
  be used.</pre>
- **analyzer** [string, {'word', 'char', 'char\_wb'} or callable] Whether the feature should be made of word or character n-grams. Option 'char\_wb' creates character n-grams only from text inside word boundaries; n-grams at the edges of words are padded with space.

If a callable is passed it is used to extract the sequence of features out of the raw, unprocessed input.

Changed in version 0.21.

Since v0.21, if input is filename or file, the data is first read from the file and then passed to the given callable analyzer.

max\_df [float in range [0.0, 1.0] or int, default=1.0] When building the vocabulary ignore terms that have a document frequency strictly higher than the given threshold (corpus-specific stop

words). If float, the parameter represents a proportion of documents, integer absolute counts. This parameter is ignored if vocabulary is not None.

min\_df [float in range [0.0, 1.0] or int, default=1] When building the vocabulary ignore terms that have a document frequency strictly lower than the given threshold. This value is also called cut-off in the literature. If float, the parameter represents a proportion of documents, integer absolute counts. This parameter is ignored if vocabulary is not None.

max\_features [int or None, default=None] If not None, build a vocabulary that only consider the top max\_features ordered by term frequency across the corpus.

This parameter is ignored if vocabulary is not None.

**vocabulary** [Mapping or iterable, optional] Either a Mapping (e.g., a dict) where keys are terms and values are indices in the feature matrix, or an iterable over terms. If not given, a vocabulary is determined from the input documents. Indices in the mapping should not be repeated and should not have any gap between 0 and the largest index.

**binary** [boolean, default=False] If True, all non zero counts are set to 1. This is useful for discrete probabilistic models that model binary events rather than integer counts.

**dtype** [type, optional] Type of the matrix returned by fit\_transform() or transform().

#### Attributes

vocabulary\_ [dict] A mapping of terms to feature indices.

**stop\_words\_** [set] Terms that were ignored because they either:

- occurred in too many documents (max\_df)
- occurred in too few documents (min\_df)
- were cut off by feature selection (max\_features).

This is only available if no vocabulary was given.

#### See also:

HashingVectorizer, TfidfVectorizer

### **Notes**

The stop\_words\_attribute can get large and increase the model size when pickling. This attribute is provided only for introspection and can be safely removed using delattr or set to None before pickling.

# **Examples**

```
>>> from sklearn.feature_extraction.text import CountVectorizer
>>> corpus = [
...    'This is the first document.',
...    'This document is the second document.',
...    'And this is the third one.',
...    'Is this the first document?',
...    |
>>> vectorizer = CountVectorizer()
>>> X = vectorizer.fit_transform(corpus)
>>> print(vectorizer.get_feature_names())
['and', 'document', 'first', 'is', 'one', 'second', 'the', 'third', 'this']
```

```
>>> print(X.toarray())
[[0 1 1 1 0 0 1 0 1]
[[0 2 0 1 0 1 1 0 1]
[[1 0 0 1 1 0 1 1 1]
[[0 1 1 1 0 0 1 0 1]]
```

# **Methods**

build analyzer(self)	Return a callable that handles preprocessing and tok-
,	enization
build_preprocessor(self)	Return a function to preprocess the text before tokeniza-
	tion
build_tokenizer(self)	Return a function that splits a string into a sequence of
	tokens
decode(self, doc)	Decode the input into a string of unicode symbols
fit(self, raw_documents[, y])	Learn a vocabulary dictionary of all tokens in the raw
	documents.
<pre>fit_transform(self, raw_documents[, y])</pre>	Learn the vocabulary dictionary and return term-
	document matrix.
<pre>get_feature_names(self)</pre>	Array mapping from feature integer indices to feature
	name
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_stop_words(self)	Build or fetch the effective stop words list
inverse_transform(self, X)	Return terms per document with nonzero entries in X.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, raw_documents)	Transform documents to document-term matrix.

\_\_init\_\_ (self, input='content', encoding='utf-8', decode\_error='strict', strip\_accents=None, lowercase=True, preprocessor=None, tokenizer=None, stop\_words=None, token\_pattern='(?u)\b\w\w+\b', ngram\_range=(1, 1), analyzer='word', max\_df=1.0, min\_df=1, max\_features=None, vocabulary=None, binary=False, dtype=<class 'numpy.int64'>)

# build\_analyzer(self)

Return a callable that handles preprocessing and tokenization

# build\_preprocessor(self)

Return a function to preprocess the text before tokenization

# build\_tokenizer(self)

Return a function that splits a string into a sequence of tokens

# decode (self, doc)

Decode the input into a string of unicode symbols

The decoding strategy depends on the vectorizer parameters.

# **Parameters**

doc [string] The string to decode

# fit (self, raw\_documents, y=None)

Learn a vocabulary dictionary of all tokens in the raw documents.

# **Parameters**

raw\_documents [iterable] An iterable which yields either str, unicode or file objects.

#### Returns

self

# fit\_transform(self, raw\_documents, y=None)

Learn the vocabulary dictionary and return term-document matrix.

This is equivalent to fit followed by transform, but more efficiently implemented.

# **Parameters**

raw\_documents [iterable] An iterable which yields either str, unicode or file objects.

#### Returns

**X** [array, [n\_samples, n\_features]] Document-term matrix.

## get\_feature\_names (self)

Array mapping from feature integer indices to feature name

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

# get\_stop\_words(self)

Build or fetch the effective stop words list

# inverse\_transform(self, X)

Return terms per document with nonzero entries in X.

### **Parameters**

**X** [{array, sparse matrix}, shape = [n\_samples, n\_features]]

# Returns

**X\_inv** [list of arrays, len =  $n_samples$ ] List of arrays of terms.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# transform (self, raw\_documents)

Transform documents to document-term matrix.

Extract token counts out of raw text documents using the vocabulary fitted with fit or the one provided to the constructor.

#### **Parameters**

raw documents [iterable] An iterable which yields either str, unicode or file objects.

### Returns

**X** [sparse matrix, [n samples, n features]] Document-term matrix.

## Examples using sklearn.feature\_extraction.text.CountVectorizer

- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation
- Sample pipeline for text feature extraction and evaluation

# sklearn.feature\_extraction.text.HashingVectorizer

```
class sklearn.feature_extraction.text.HashingVectorizer(input='content',
                                                                       encoding='utf-8',
                                                                                                de-
                                                                       code_error='strict',
                                                                       strip accents=None,
                                                                                               low-
                                                                       ercase=True,
                                                                                         preproces-
                                                                       sor=None, tokenizer=None,
                                                                       stop_words=None,
                                                                       ken_pattern='(?u)\b\w\w+\b',
                                                                       ngram_range=(1,
                                                                       1),
                                                                                  analyzer='word'.
                                                                       n features=1048576,
                                                                                                bi-
                                                                       nary=False,
                                                                                        norm='l2'.
                                                                       alternate_sign=True,
                                                                       dtype = < class
                                                                        'numpy.float64'>)
```

Convert a collection of text documents to a matrix of token occurrences

It turns a collection of text documents into a scipy.sparse matrix holding token occurrence counts (or binary occurrence information), possibly normalized as token frequencies if norm='11' or projected on the euclidean unit sphere if norm='12'.

This text vectorizer implementation uses the hashing trick to find the token string name to feature integer index mapping.

This strategy has several advantages:

- it is very low memory scalable to large datasets as there is no need to store a vocabulary dictionary in memory
- it is fast to pickle and un-pickle as it holds no state besides the constructor parameters
- it can be used in a streaming (partial fit) or parallel pipeline as there is no state computed during fit.

There are also a couple of cons (vs using a CountVectorizer with an in-memory vocabulary):

- there is no way to compute the inverse transform (from feature indices to string feature names) which can be a problem when trying to introspect which features are most important to a model.
- there can be collisions: distinct tokens can be mapped to the same feature index. However in practice this is rarely an issue if n features is large enough (e.g. 2 \*\* 18 for text classification problems).
- no IDF weighting as this would render the transformer stateful.

The hash function employed is the signed 32-bit version of Murmurhash3.

Read more in the User Guide.

#### **Parameters**

- **input** [string {'filename', 'file', 'content'}] If 'filename', the sequence passed as an argument to fit is expected to be a list of filenames that need reading to fetch the raw content to analyze.
  - If 'file', the sequence items must have a 'read' method (file-like object) that is called to fetch the bytes in memory.
  - Otherwise the input is expected to be the sequence strings or bytes items are expected to be analyzed directly.
- **encoding** [string, default='utf-8'] If bytes or files are given to analyze, this encoding is used to decode.
- **decode\_error** [{'strict', 'ignore', 'replace'}] Instruction on what to do if a byte sequence is given to analyze that contains characters not of the given encoding. By default, it is 'strict', meaning that a UnicodeDecodeError will be raised. Other values are 'ignore' and 'replace'.
- **strip\_accents** [{'ascii', 'unicode', None}] Remove accents and perform other character normalization during the preprocessing step. 'ascii' is a fast method that only works on characters that have an direct ASCII mapping. 'unicode' is a slightly slower method that works on any characters. None (default) does nothing.
  - Both 'ascii' and 'unicode' use NFKD normalization from unicodedata.normalize.
- lowercase [boolean, default=True] Convert all characters to lowercase before tokenizing.
- **preprocessor** [callable or None (default)] Override the preprocessing (string transformation) stage while preserving the tokenizing and n-grams generation steps.
- **tokenizer** [callable or None (default)] Override the string tokenization step while preserving the preprocessing and n-grams generation steps. Only applies if analyzer == 'word'.
- **stop\_words** [string {'english'}, list, or None (default)] If 'english', a built-in stop word list for English is used. There are several known issues with 'english' and you should consider an alternative (see *Using stop words*).
  - If a list, that list is assumed to contain stop words, all of which will be removed from the resulting tokens. Only applies if analyzer == 'word'.
- **token\_pattern** [string] Regular expression denoting what constitutes a "token", only used if analyzer == 'word'. The default regexp selects tokens of 2 or more alphanumeric characters (punctuation is completely ignored and always treated as a token separator).
- ngram\_range [tuple (min\_n, max\_n), default=(1, 1)] The lower and upper boundary of the
  range of n-values for different n-grams to be extracted. All values of n such that min\_n <=
  n <= max\_n will be used.</pre>
- **analyzer** [string, {'word', 'char', 'char\_wb'} or callable] Whether the feature should be made of word or character n-grams. Option 'char\_wb' creates character n-grams only from text inside word boundaries; n-grams at the edges of words are padded with space.
  - If a callable is passed it is used to extract the sequence of features out of the raw, unprocessed input.
  - Changed in version 0.21.
  - Since v0.21, if input is filename or file, the data is first read from the file and then passed to the given callable analyzer.
- **n\_features** [integer, default=(2 \*\* 20)] The number of features (columns) in the output matrices. Small numbers of features are likely to cause hash collisions, but large numbers will cause larger coefficient dimensions in linear learners.

**binary** [boolean, default=False.] If True, all non zero counts are set to 1. This is useful for discrete probabilistic models that model binary events rather than integer counts.

**norm** ['11', '12' or None, optional] Norm used to normalize term vectors. None for no normalization.

**alternate\_sign** [boolean, optional, default True] When True, an alternating sign is added to the features as to approximately conserve the inner product in the hashed space even for small n\_features. This approach is similar to sparse random projection.

New in version 0.19.

**dtype** [type, optional] Type of the matrix returned by fit\_transform() or transform().

### See also:

CountVectorizer, TfidfVectorizer

# **Examples**

```
>>> from sklearn.feature_extraction.text import HashingVectorizer
>>> corpus = [
...    'This is the first document.',
...    'This document is the second document.',
...    'And this is the third one.',
...    'Is this the first document?',
...    |
>>> vectorizer = HashingVectorizer(n_features=2**4)
>>> X = vectorizer.fit_transform(corpus)
>>> print(X.shape)
(4, 16)
```

### **Methods**

build_analyzer(self)	Return a callable that handles preprocessing and tok-
	enization
build_preprocessor(self)	Return a function to preprocess the text before tokeniza-
	tion
build_tokenizer(self)	Return a function that splits a string into a sequence of
	tokens
decode(self, doc)	Decode the input into a string of unicode symbols
fit(self, X[, y])	Does nothing: this transformer is stateless.
$fit_transform(self, X[, y])$	Transform a sequence of documents to a document-term
	matrix.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_stop_words(self)	Build or fetch the effective stop words list
partial_fit(self, X[, y])	Does nothing: this transformer is stateless.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform a sequence of documents to a document-term
	matrix.

\_\_init\_\_ (self, input='content', encoding='utf-8', decode\_error='strict', strip\_accents=None, lowercase=True, preprocessor=None, tokenizer=None, stop\_words=None, token\_pattern='('?u)\b\w\w+\b', ngram\_range=(1, 1), analyzer='word', n\_features=1048576, binary=False, norm='l2', alternate\_sign=True, dtype=<class 'numpy,float64'>)

# build\_analyzer(self)

Return a callable that handles preprocessing and tokenization

# build\_preprocessor(self)

Return a function to preprocess the text before tokenization

## build\_tokenizer(self)

Return a function that splits a string into a sequence of tokens

# decode(self, doc)

Decode the input into a string of unicode symbols

The decoding strategy depends on the vectorizer parameters.

#### **Parameters**

doc [string] The string to decode

# **fit** (*self*, *X*, *y*=*None*)

Does nothing: this transformer is stateless.

#### **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] Training data.

# fit\_transform(self, X, y=None)

Transform a sequence of documents to a document-term matrix.

### **Parameters**

- **X** [iterable over raw text documents, length = n\_samples] Samples. Each sample must be a text document (either bytes or unicode strings, file name or file object depending on the constructor argument) which will be tokenized and hashed.
- y [any] Ignored. This parameter exists only for compatibility with sklearn.pipeline.Pipeline.

### **Returns**

**X** [scipy.sparse matrix, shape = (n\_samples, self.n\_features)] Document-term matrix.

# get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# $\mathtt{get\_stop\_words}$ (self)

Build or fetch the effective stop words list

### partial\_fit (self, X, y=None)

Does nothing: this transformer is stateless.

This method is just there to mark the fact that this transformer can work in a streaming setup.

# **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] Training data.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, X)

Transform a sequence of documents to a document-term matrix.

#### **Parameters**

**X** [iterable over raw text documents, length = n\_samples] Samples. Each sample must be a text document (either bytes or unicode strings, file name or file object depending on the constructor argument) which will be tokenized and hashed.

#### Returns

**X** [scipy.sparse matrix, shape = (n\_samples, self.n\_features)] Document-term matrix.

## Examples using sklearn.feature\_extraction.text.HashingVectorizer

- Out-of-core classification of text documents
- Clustering text documents using k-means
- Classification of text documents using sparse features

# sklearn.feature\_extraction.text.TfidfTransformer

Transform a count matrix to a normalized tf or tf-idf representation

Tf means term-frequency while tf-idf means term-frequency times inverse document-frequency. This is a common term weighting scheme in information retrieval, that has also found good use in document classification.

The goal of using tf-idf instead of the raw frequencies of occurrence of a token in a given document is to scale down the impact of tokens that occur very frequently in a given corpus and that are hence empirically less informative than features that occur in a small fraction of the training corpus.

The formula that is used to compute the tf-idf for a term t of a document d in a document set is tf-idf(t, d) = tf(t, d) \* idf(t), and the idf is computed as idf(t) =  $\log [n/df(t)] + 1$  (if smooth\_idf=False), where n is the total number of documents in the document set and df(t) is the document frequency of t; the document frequency is the number of documents in the document set that contain the term t. The effect of adding "1" to the idf in the equation above is that terms with zero idf, i.e., terms that occur in all documents in a training set, will not be entirely ignored. (Note that the idf formula above differs from the standard textbook notation that defines the idf as idf(t) =  $\log [n/(df(t) + 1)]$ ).

If smooth\_idf=True (the default), the constant "1" is added to the numerator and denominator of the idf as if an extra document was seen containing every term in the collection exactly once, which prevents zero divisions: idf(d, t) = log [(1 + n) / (1 + df(d, t))] + 1.

Furthermore, the formulas used to compute tf and idf depend on parameter settings that correspond to the SMART notation used in IR as follows:

Tf is "n" (natural) by default, "l" (logarithmic) when sublinear\_tf=True. Idf is "t" when use\_idf is given, "n" (none) otherwise. Normalization is "c" (cosine) when norm='12', "n" (none) when norm=None.

Read more in the User Guide.

#### **Parameters**

norm ['11', '12' or None, optional (default='12')] Each output row will have unit norm, either:
 \* '12': Sum of squares of vector elements is 1. The cosine similarity between two vectors is
 their dot product when 12 norm has been applied. \* '11': Sum of absolute values of vector
 elements is 1. See preprocessing.normalize

use\_idf [boolean (default=True)] Enable inverse-document-frequency reweighting.

**smooth\_idf** [boolean (default=True)] Smooth idf weights by adding one to document frequencies, as if an extra document was seen containing every term in the collection exactly once. Prevents zero divisions.

**sublinear\_tf** [boolean (default=False)] Apply sublinear tf scaling, i.e. replace tf with 1 + log(tf).

### Attributes

idf\_ [array, shape (n\_features)] The inverse document frequency (IDF) vector; only defined if use\_idf is True.

### References

[R1b90ac3ca370-Yates2011], [R1b90ac3ca370-MRS2008]

# **Methods**

fit(self, X[, y])	Learn the idf vector (global term weights)
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X[, copy])	Transform a count matrix to a tf or tf-idf representation

\_\_init\_\_ (self, norm='l2', use\_idf=True, smooth\_idf=True, sublinear\_tf=False)

fit (self, X, y=None)

Learn the idf vector (global term weights)

#### **Parameters**

**X** [sparse matrix, [n\_samples, n\_features]] a matrix of term/token counts

fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

X [numpy array of shape [n\_samples, n\_features]] Training set.

y [numpy array of shape [n\_samples]] Target values.

### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, X, copy=True)

Transform a count matrix to a tf or tf-idf representation

### **Parameters**

X [sparse matrix, [n\_samples, n\_features]] a matrix of term/token counts

**copy** [boolean, default True] Whether to copy X and operate on the copy or perform in-place operations.

### **Returns**

**vectors** [sparse matrix, [n\_samples, n\_features]]

# Examples using sklearn.feature\_extraction.text.TfidfTransformer

- Sample pipeline for text feature extraction and evaluation
- Clustering text documents using k-means

### sklearn.feature extraction.text.TfidfVectorizer

```
class sklearn.feature extraction.text.TfidfVectorizer(input='content', encoding='utf-
                                                                                decode_error='strict',
                                                                      strip_accents=None,
                                                                                                 low-
                                                                       ercase=True,
                                                                                           preproces-
                                                                      sor=None, tokenizer=None, ana-
                                                                       lyzer='word', stop_words=None,
                                                                       token\_pattern='(?u)\b\w\w+\b',
                                                                      ngram_range=(1,
                                                                      max_df=1.0,
                                                                                           min_df=1,
                                                                      max features=None,
                                                                                              vocab-
                                                                       ulary=None,
                                                                                        binary=False,
                                                                      dtype = \langle class 'numpy.float64' \rangle,
                                                                       norm='l2',
                                                                                        use_idf=True,
                                                                      smooth idf=True,
                                                                                               sublin-
                                                                       ear tf=False)
```

Convert a collection of raw documents to a matrix of TF-IDF features.

Equivalent to CountVectorizer followed by TfidfTransformer.

Read more in the *User Guide*.

#### **Parameters**

**input** [string {'filename', 'file', 'content'}] If 'filename', the sequence passed as an argument to fit is expected to be a list of filenames that need reading to fetch the raw content to analyze.

If 'file', the sequence items must have a 'read' method (file-like object) that is called to fetch the bytes in memory.

Otherwise the input is expected to be the sequence strings or bytes items are expected to be analyzed directly.

**encoding** [string, 'utf-8' by default.] If bytes or files are given to analyze, this encoding is used to decode.

**decode\_error** [{'strict', 'ignore', 'replace'} (default='strict')] Instruction on what to do if a byte sequence is given to analyze that contains characters not of the given encoding. By default, it is 'strict', meaning that a UnicodeDecodeError will be raised. Other values are 'ignore' and 'replace'.

**strip\_accents** [{'ascii', 'unicode', None} (default=None)] Remove accents and perform other character normalization during the preprocessing step. 'ascii' is a fast method that only works on characters that have an direct ASCII mapping. 'unicode' is a slightly slower method that works on any characters. None (default) does nothing.

Both 'ascii' and 'unicode' use NFKD normalization from unicodedata.normalize.

**lowercase** [boolean (default=True)] Convert all characters to lowercase before tokenizing.

**preprocessor** [callable or None (default=None)] Override the preprocessing (string transformation) stage while preserving the tokenizing and n-grams generation steps.

**tokenizer** [callable or None (default=None)] Override the string tokenization step while preserving the preprocessing and n-grams generation steps. Only applies if analyzer == 'word'.

**analyzer** [string, {'word', 'char', 'char\_wb'} or callable] Whether the feature should be made of word or character n-grams. Option 'char\_wb' creates character n-grams only from text inside word boundaries; n-grams at the edges of words are padded with space.

If a callable is passed it is used to extract the sequence of features out of the raw, unprocessed input.

Changed in version 0.21.

Since v0.21, if input is filename or file, the data is first read from the file and then passed to the given callable analyzer.

**stop\_words** [string {'english'}, list, or None (default=None)] If a string, it is passed to \_check\_stop\_list and the appropriate stop list is returned. 'english' is currently the only supported string value. There are several known issues with 'english' and you should consider an alternative (see *Using stop words*).

If a list, that list is assumed to contain stop words, all of which will be removed from the resulting tokens. Only applies if analyzer == 'word'.

If None, no stop words will be used. max\_df can be set to a value in the range [0.7, 1.0) to automatically detect and filter stop words based on intra corpus document frequency of terms.

- **token\_pattern** [string] Regular expression denoting what constitutes a "token", only used if analyzer == 'word'. The default regexp selects tokens of 2 or more alphanumeric characters (punctuation is completely ignored and always treated as a token separator).
- **ngram\_range** [tuple (min\_n, max\_n) (default=(1, 1))] The lower and upper boundary of the range of n-values for different n-grams to be extracted. All values of n such that min\_n <= n <= max\_n will be used.
- max\_df [float in range [0.0, 1.0] or int (default=1.0)] When building the vocabulary ignore terms that have a document frequency strictly higher than the given threshold (corpusspecific stop words). If float, the parameter represents a proportion of documents, integer absolute counts. This parameter is ignored if vocabulary is not None.
- min\_df [float in range [0.0, 1.0] or int (default=1)] When building the vocabulary ignore terms that have a document frequency strictly lower than the given threshold. This value is also called cut-off in the literature. If float, the parameter represents a proportion of documents, integer absolute counts. This parameter is ignored if vocabulary is not None.
- max\_features [int or None (default=None)] If not None, build a vocabulary that only consider the top max\_features ordered by term frequency across the corpus.

This parameter is ignored if vocabulary is not None.

- **vocabulary** [Mapping or iterable, optional (default=None)] Either a Mapping (e.g., a dict) where keys are terms and values are indices in the feature matrix, or an iterable over terms. If not given, a vocabulary is determined from the input documents.
- **binary** [boolean (default=False)] If True, all non-zero term counts are set to 1. This does not mean outputs will have only 0/1 values, only that the tf term in tf-idf is binary. (Set idf and normalization to False to get 0/1 outputs.)
- **dtype** [type, optional (default=float64)] Type of the matrix returned by fit\_transform() or transform().
- norm ['11', '12' or None, optional (default='12')] Each output row will have unit norm, either:
  \* '12': Sum of squares of vector elements is 1. The cosine similarity between two vectors is their dot product when 12 norm has been applied. \* '11': Sum of absolute values of vector elements is 1. See preprocessing.normalize
- use\_idf [boolean (default=True)] Enable inverse-document-frequency reweighting.

**smooth\_idf** [boolean (default=True)] Smooth idf weights by adding one to document frequencies, as if an extra document was seen containing every term in the collection exactly once. Prevents zero divisions.

**sublinear\_tf** [boolean (default=False)] Apply sublinear tf scaling, i.e. replace tf with 1 + log(tf).

#### **Attributes**

vocabulary\_ [dict] A mapping of terms to feature indices.

idf\_ [array, shape (n\_features)] The inverse document frequency (IDF) vector; only defined if use\_idf is True.

**stop\_words\_** [set] Terms that were ignored because they either:

- occurred in too many documents (max\_df)
- occurred in too few documents (min\_df)
- were cut off by feature selection (max\_features).

This is only available if no vocabulary was given.

### See also:

CountVectorizer Transforms text into a sparse matrix of n-gram counts.

**TfidfTransformer** Performs the TF-IDF transformation from a provided matrix of counts.

# **Notes**

The stop\_words\_attribute can get large and increase the model size when pickling. This attribute is provided only for introspection and can be safely removed using delattr or set to None before pickling.

# **Examples**

```
>>> from sklearn.feature_extraction.text import TfidfVectorizer
>>> corpus = [
        'This is the first document.',
. . .
        'This document is the second document.',
. . .
        'And this is the third one.',
. . .
        'Is this the first document?',
. . .
...]
>>> vectorizer = TfidfVectorizer()
>>> X = vectorizer.fit_transform(corpus)
>>> print (vectorizer.get_feature_names())
['and', 'document', 'first', 'is', 'one', 'second', 'the', 'third', 'this']
>>> print(X.shape)
(4, 9)
```

#### **Methods**

build_analyzer(self)	Return a callable that handles preprocessing and tok-
	enization

Continued on next page

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build_preprocessor(self)	Return a function to preprocess the text before tokeniza-
	tion
build_tokenizer(self)	Return a function that splits a string into a sequence of
	tokens
decode(self, doc)	Decode the input into a string of unicode symbols
fit(self, raw_documents[, y])	Learn vocabulary and idf from training set.
<pre>fit_transform(self, raw_documents[, y])</pre>	Learn vocabulary and idf, return term-document matrix.
<pre>get_feature_names(self)</pre>	Array mapping from feature integer indices to feature
	name
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_stop_words(self)	Build or fetch the effective stop words list

Table 6.103 – continued from previous page

\_\_init\_\_ (self, input='content', encoding='utf-8', decode\_error='strict', strip\_accents=None, low-ercase=True, preprocessor=None, tokenizer=None, analyzer='word', stop\_words=None, token\_pattern='(?u)\b\w\w+\b', ngram\_range=(1, 1), max\_df=1.0, min\_df=1, max\_features=None, vocabulary=None, binary=False, dtype=<class 'numpy.float64'>, norm='l2', use\_idf=True, smooth\_idf=True, sublinear\_tf=False)

Return terms per document with nonzero entries in X.

Transform documents to document-term matrix.

Set the parameters of this estimator.

# build\_analyzer(self)

inverse transform(self, X)

set\_params(self, \\*\\*params)

transform(self, raw\_documents[, copy])

Return a callable that handles preprocessing and tokenization

## build\_preprocessor(self)

Return a function to preprocess the text before tokenization

# build\_tokenizer(self)

Return a function that splits a string into a sequence of tokens

### decode (self, doc)

Decode the input into a string of unicode symbols

The decoding strategy depends on the vectorizer parameters.

## **Parameters**

doc [string] The string to decode

## **fit** (*self*, *raw documents*, *y=None*)

Learn vocabulary and idf from training set.

# **Parameters**

raw\_documents [iterable] an iterable which yields either str, unicode or file objects

### Returns

**self** [TfidfVectorizer]

# fit\_transform(self, raw\_documents, y=None)

Learn vocabulary and idf, return term-document matrix.

This is equivalent to fit followed by transform, but more efficiently implemented.

### **Parameters**

raw\_documents [iterable] an iterable which yields either str, unicode or file objects

# Returns

**X** [sparse matrix, [n\_samples, n\_features]] Tf-idf-weighted document-term matrix.

### get feature names (self)

Array mapping from feature integer indices to feature name

# get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

# get\_stop\_words(self)

Build or fetch the effective stop words list

# $inverse\_transform(self, X)$

Return terms per document with nonzero entries in X.

#### **Parameters**

**X** [{array, sparse matrix}, shape = [n\_samples, n\_features]]

#### Returns

**X\_inv** [list of arrays, len =  $n_samples$ ] List of arrays of terms.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# transform(self, raw\_documents, copy=True)

Transform documents to document-term matrix.

Uses the vocabulary and document frequencies (df) learned by fit (or fit\_transform).

### **Parameters**

raw\_documents [iterable] an iterable which yields either str, unicode or file objects

**copy** [boolean, default True] Whether to copy X and operate on the copy or perform in-place operations.

# Returns

**X** [sparse matrix, [n\_samples, n\_features]] Tf-idf-weighted document-term matrix.

# **Examples using** sklearn.feature\_extraction.text.TfidfVectorizer

- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation
- Biclustering documents with the Spectral Co-clustering algorithm
- Column Transformer with Heterogeneous Data Sources
- Clustering text documents using k-means

• Classification of text documents using sparse features

# 6.16 sklearn.feature\_selection: Feature Selection

The sklearn.feature\_selection module implements feature selection algorithms. It currently includes univariate filter selection methods and the recursive feature elimination algorithm.

**User guide:** See the *Feature selection* section for further details.

feature_selection.	Univariate feature selector with configurable strategy.
$ extit{GenericUnivariateSelect([])}$	
feature_selection.SelectPercentile([])	Select features according to a percentile of the highest
	scores.
feature_selection.SelectKBest([score_func,	Select features according to the k highest scores.
[k])	
<pre>feature_selection.SelectFpr([score_func, al-</pre>	Filter: Select the pvalues below alpha based on a FPR test.
pha])	
feature_selection.SelectFdr([score_func, al-	Filter: Select the p-values for an estimated false discovery
pha])	rate
feature_selection.	Meta-transformer for selecting features based on impor-
SelectFromModel(estimator)	tance weights.
feature_selection.SelectFwe([score_func, al-	Filter: Select the p-values corresponding to Family-wise
pha])	error rate
<pre>feature_selection.RFE(estimator[,])</pre>	Feature ranking with recursive feature elimination.
<pre>feature_selection.RFECV(estimator[, step,])</pre>	Feature ranking with recursive feature elimination and
	cross-validated selection of the best number of features.
feature_selection.	Feature selector that removes all low-variance features.
VarianceThreshold([threshold])	

# 6.16.1 sklearn.feature\_selection.GenericUnivariateSelect

class sklearn.feature\_selection.GenericUnivariateSelect ( $score\_func = < function$   $f\_classif>$ , mode = 'percentile', param = 1e-05)

Univariate feature selector with configurable strategy.

Read more in the *User Guide*.

### **Parameters**

**score\_func** [callable] Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues). For modes 'percentile' or 'kbest' it can return a single array scores.

mode [{'percentile', 'k\_best', 'fpr', 'fdr', 'fwe'}] Feature selection mode.

**param** [float or int depending on the feature selection mode] Parameter of the corresponding mode.

# Attributes

**scores**\_ [array-like, shape=(n\_features,)] Scores of features.

**pvalues**\_ [array-like, shape=(n\_features,)] p-values of feature scores, None if score\_func returned scores only.

See also:

**f\_classif** ANOVA F-value between label/feature for classification tasks.

mutual\_info\_classif Mutual information for a discrete target.

chi2 Chi-squared stats of non-negative features for classification tasks.

**f\_regression** F-value between label/feature for regression tasks.

mutual info regression Mutual information for a continuous target.

SelectPercentile Select features based on percentile of the highest scores.

SelectKBest Select features based on the k highest scores.

**SelectFpr** Select features based on a false positive rate test.

SelectFdr Select features based on an estimated false discovery rate.

**SelectFwe** Select features based on family-wise error rate.

# **Examples**

```
>>> from sklearn.datasets import load_breast_cancer
>>> from sklearn.feature_selection import GenericUnivariateSelect, chi2
>>> X, y = load_breast_cancer(return_X_y=True)
>>> X.shape
(569, 30)
>>> transformer = GenericUnivariateSelect(chi2, 'k_best', param=20)
>>> X_new = transformer.fit_transform(X, y)
>>> X_new.shape
(569, 20)
```

### Methods

fit(self, X, y)	Run score function on (X, y) and get the appropriate
	features.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

```
__init__ (self, score_func=<function f_classif at 0x7efe30bb2158>, mode='percentile', param=1e-05)
```

# **fit** (self, X, y)

Run score function on (X, y) and get the appropriate features.

### **Parameters**

- $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] The training input samples.
- y [array-like, shape = [n\_samples]] The target values (class labels in classification, real numbers in regression).

# Returns

self [object]

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

# get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

### **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

# Returns

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

# $inverse\_transform(self, X)$

Reverse the transformation operation

#### **Parameters**

**X** [array of shape [n samples, n selected features]] The input samples.

# Returns

**X\_r** [array of shape [n\_samples, n\_original\_features]] X with columns of zeros inserted where features would have been removed by transform.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

### transform(self, X)

Reduce X to the selected features.

#### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

### Returns

**X\_r** [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

# 6.16.2 sklearn.feature\_selection.SelectPercentile

Select features according to a percentile of the highest scores.

Read more in the *User Guide*.

#### **Parameters**

**score\_func** [callable] Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues) or a single array with scores. Default is f\_classif (see below "See also"). The default function only works with classification tasks.

percentile [int, optional, default=10] Percent of features to keep.

## **Attributes**

scores\_ [array-like, shape=(n\_features,)] Scores of features.

**pvalues**\_ [array-like, shape=(n\_features,)] p-values of feature scores, None if score\_func returned only scores.

### See also:

f classif ANOVA F-value between label/feature for classification tasks.

mutual info classif Mutual information for a discrete target.

chi2 Chi-squared stats of non-negative features for classification tasks.

**f\_regression** F-value between label/feature for regression tasks.

mutual\_info\_regression Mutual information for a continuous target.

**SelectKBest** Select features based on the k highest scores.

SelectFpr Select features based on a false positive rate test.

**SelectFdr** Select features based on an estimated false discovery rate.

**SelectFwe** Select features based on family-wise error rate.

GenericUnivariateSelect Univariate feature selector with configurable mode.

# **Notes**

Ties between features with equal scores will be broken in an unspecified way.

# **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.feature_selection import SelectPercentile, chi2
>>> X, y = load_digits(return_X_y=True)
>>> X.shape
(1797, 64)
>>> X_new = SelectPercentile(chi2, percentile=10).fit_transform(X, y)
>>> X_new.shape
(1797, 7)
```

### **Methods**

fit(self, X, y)	Run score function on (X, y) and get the appropriate
	features.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

```
__init__ (self, score_func=<function f_classif at 0x7f3c10e93840>, percentile=10)
```

fit (self, X, y)

Run score function on (X, y) and get the appropriate features.

# **Parameters**

- $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] The training input samples.
- y [array-like, shape = [n\_samples]] The target values (class labels in classification, real numbers in regression).

# Returns

self [object]

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

# **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

## **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

#### get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

#### **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

#### Returns

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

### $inverse\_transform(self, X)$

Reverse the transformation operation

#### **Parameters**

**X** [array of shape [n\_samples, n\_selected\_features]] The input samples.

#### Returns

**X\_r** [array of shape [n\_samples, n\_original\_features]] X with columns of zeros inserted where features would have been removed by transform.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# ${\tt transform}\,(\mathit{self},X)$

Reduce X to the selected features.

### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

# Returns

**X\_r** [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

# Examples using sklearn.feature\_selection.SelectPercentile

- Feature agglomeration vs. univariate selection
- Univariate Feature Selection
- SVM-Anova: SVM with univariate feature selection

# 6.16.3 sklearn.feature selection.SelectKBest

class sklearn.feature\_selection.SelectKBest ( $score\_func = < function f\_classif >$ , k=10) Select features according to the k highest scores.

Read more in the User Guide.

#### **Parameters**

**score\_func** [callable] Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues) or a single array with scores. Default is f\_classif (see below "See also"). The default function only works with classification tasks.

**k** [int or "all", optional, default=10] Number of top features to select. The "all" option bypasses selection, for use in a parameter search.

#### **Attributes**

scores\_ [array-like, shape=(n\_features,)] Scores of features.

**pvalues**\_ [array-like, shape=(n\_features,)] p-values of feature scores, None if score\_func returned only scores.

#### See also:

**f\_classif** ANOVA F-value between label/feature for classification tasks.

mutual\_info\_classif Mutual information for a discrete target.

chi2 Chi-squared stats of non-negative features for classification tasks.

**f\_regression** F-value between label/feature for regression tasks.

mutual\_info\_regression Mutual information for a continuous target.

SelectPercentile Select features based on percentile of the highest scores.

**SelectFpr** Select features based on a false positive rate test.

SelectFdr Select features based on an estimated false discovery rate.

**SelectFwe** Select features based on family-wise error rate.

GenericUnivariateSelect Univariate feature selector with configurable mode.

# **Notes**

Ties between features with equal scores will be broken in an unspecified way.

# **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.feature_selection import SelectKBest, chi2
>>> X, y = load_digits(return_X_y=True)
>>> X.shape
(1797, 64)
>>> X_new = SelectKBest(chi2, k=20).fit_transform(X, y)
>>> X_new.shape
(1797, 20)
```

# **Methods**

fit(self, X, y)	Run score function on (X, y) and get the appropriate
	features.
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

**\_\_init\_\_** (self, score\_func=<function f\_classif at 0x7f3c10e93840>, k=10)

# **fit** (self, X, y)

Run score function on (X, y) and get the appropriate features.

#### **Parameters**

- $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] The training input samples.
- y [array-like, shape = [n\_samples]] The target values (class labels in classification, real numbers in regression).

### Returns

self [object]

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit params and returns a transformed version of X.

# **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

#### **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

# Returns

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

# inverse\_transform(self, X)

Reverse the transformation operation

#### **Parameters**

**X** [array of shape [n\_samples, n\_selected\_features]] The input samples.

### Returns

**X\_r** [array of shape [n\_samples, n\_original\_features]] *X* with columns of zeros inserted where features would have been removed by *transform*.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# transform(self, X)

Reduce X to the selected features.

### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

#### Returns

**X\_r** [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

# Examples using sklearn.feature\_selection.SelectKBest

- Concatenating multiple feature extraction methods
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Pipeline Anova SVM
- Classification of text documents using sparse features

# 6.16.4 sklearn.feature\_selection.SelectFpr

class sklearn.feature\_selection.SelectFpr (score\_func=<function f\_classif>, alpha=0.05)
Filter: Select the pvalues below alpha based on a FPR test.

FPR test stands for False Positive Rate test. It controls the total amount of false detections.

Read more in the User Guide.

# Parameters

**score\_func** [callable] Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues). Default is f\_classif (see below "See also"). The default function only works with classification tasks.

**alpha** [float, optional] The highest p-value for features to be kept.

# **Attributes**

**scores**\_ [array-like, shape=(n\_features,)] Scores of features.

**pvalues**\_ [array-like, shape=(n\_features,)] p-values of feature scores.

# See also:

**f\_classif** ANOVA F-value between label/feature for classification tasks.

*chi2* Chi-squared stats of non-negative features for classification tasks.

mutual\_info\_classif

**f\_regression** F-value between label/feature for regression tasks.

mutual\_info\_regression Mutual information between features and the target.

SelectPercentile Select features based on percentile of the highest scores.

**SelectKBest** Select features based on the k highest scores.

**SelectFdr** Select features based on an estimated false discovery rate.

SelectFwe Select features based on family-wise error rate.

GenericUnivariateSelect Univariate feature selector with configurable mode.

# **Examples**

```
>>> from sklearn.datasets import load_breast_cancer
>>> from sklearn.feature_selection import SelectFpr, chi2
>>> X, y = load_breast_cancer(return_X_y=True)
>>> X.shape
(569, 30)
>>> X_new = SelectFpr(chi2, alpha=0.01).fit_transform(X, y)
>>> X_new.shape
(569, 16)
```

### Methods

fit(self, X, y)	Run score function on (X, y) and get the appropriate
	features.
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

\_\_init\_\_ (self, score\_func=<function f\_classif at 0x7efe30bb2158>, alpha=0.05)

### fit (self, X, y)

Run score function on (X, y) and get the appropriate features.

#### **Parameters**

- $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] The training input samples.
- **y** [array-like, shape = [n\_samples]] The target values (class labels in classification, real numbers in regression).

#### Returns

self [object]

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

# **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

## **Returns**

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

# $inverse\_transform(self, X)$

Reverse the transformation operation

# **Parameters**

**X** [array of shape [n\_samples, n\_selected\_features]] The input samples.

# Returns

**X\_r** [array of shape [n\_samples, n\_original\_features]] *X* with columns of zeros inserted where features would have been removed by *transform*.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

## transform(self, X)

Reduce X to the selected features.

#### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

### Returns

**X\_r** [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

# 6.16.5 sklearn.feature\_selection.SelectFdr

class sklearn.feature\_selection.SelectFdr(score\_func=<function f\_classif>, alpha=0.05)
Filter: Select the p-values for an estimated false discovery rate

This uses the Benjamini-Hochberg procedure. alpha is an upper bound on the expected false discovery rate.

Read more in the User Guide.

# **Parameters**

**score\_func** [callable] Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues). Default is f\_classif (see below "See also"). The default function only works with classification tasks.

alpha [float, optional] The highest uncorrected p-value for features to keep.

# **Attributes**

**scores**\_ [array-like, shape=(n\_features,)] Scores of features.

**pvalues**\_ [array-like, shape=(n\_features,)] p-values of feature scores.

### See also:

f classif ANOVA F-value between label/feature for classification tasks.

mutual\_info\_classif Mutual information for a discrete target.

*chi2* Chi-squared stats of non-negative features for classification tasks.

**f\_regression** F-value between label/feature for regression tasks.

mutual\_info\_regression Mutual information for a contnuous target.

SelectPercentile Select features based on percentile of the highest scores.

SelectKBest Select features based on the k highest scores.

SelectFpr Select features based on a false positive rate test.

**SelectFwe** Select features based on family-wise error rate.

GenericUnivariateSelect Univariate feature selector with configurable mode.

## References

https://en.wikipedia.org/wiki/False\_discovery\_rate

# **Examples**

```
>>> from sklearn.datasets import load_breast_cancer
>>> from sklearn.feature_selection import SelectFdr, chi2
>>> X, y = load_breast_cancer(return_X_y=True)
>>> X.shape
(569, 30)
>>> X_new = SelectFdr(chi2, alpha=0.01).fit_transform(X, y)
>>> X_new.shape
(569, 16)
```

#### **Methods**

fit(self, X, y)	Run score function on (X, y) and get the appropriate
	features.
$fit_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

```
__init__ (self, score_func=<function f_classif at 0x7efe30bb2158>, alpha=0.05)
```

fit (self, X, y)

Run score function on (X, y) and get the appropriate features.

### **Parameters**

- $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] The training input samples.
- y [array-like, shape = [n\_samples]] The target values (class labels in classification, real numbers in regression).

### **Returns**

self [object]

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

**X** [numpy array of shape [n samples, n features]] Training set.

y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

# get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

#### **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

### **Returns**

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

# $inverse\_transform(self, X)$

Reverse the transformation operation

### **Parameters**

X [array of shape [n\_samples, n\_selected\_features]] The input samples.

# Returns

**X\_r** [array of shape [n\_samples, n\_original\_features]] *X* with columns of zeros inserted where features would have been removed by *transform*.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

### transform(self, X)

Reduce X to the selected features.

# **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

#### Returns

**X\_r** [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

# 6.16.6 sklearn.feature\_selection.SelectFromModel

class sklearn.feature\_selection.SelectFromModel(estimator, threshold=None, prefit=False, norm order=1, max\_features=None)

Meta-transformer for selecting features based on importance weights.

New in version 0.17.

#### **Parameters**

estimator [object] The base estimator from which the transformer is built. This can be both a fitted (if prefit is set to True) or a non-fitted estimator. The estimator must have either a feature\_importances\_ or coef\_ attribute after fitting.

**threshold** [string, float, optional default None] The threshold value to use for feature selection. Features whose importance is greater or equal are kept while the others are discarded. If "median" (resp. "mean"), then the threshold value is the median (resp. the mean) of the feature importances. A scaling factor (e.g., "1.25\*mean") may also be used. If None and if the estimator has a parameter penalty set to 11, either explicitly or implicitly (e.g., Lasso), the threshold used is 1e-5. Otherwise, "mean" is used by default.

prefit [bool, default False] Whether a prefit model is expected to be passed into the constructor directly or not. If True, transform must be called directly and SelectFromModel cannot be used with cross\_val\_score, GridSearchCV and similar utilities that clone the estimator. Otherwise train the model using fit and then transform to do feature selection.

**norm\_order** [non-zero int, inf, -inf, default 1] Order of the norm used to filter the vectors of coefficients below threshold in the case where the coef\_ attribute of the estimator is of dimension 2.

max\_features [int or None, optional] The maximum number of features selected scoring above threshold. To disable threshold and only select based on max\_features, set threshold=-np.inf.

New in version 0.20.

### Attributes

**estimator** [an estimator] The base estimator from which the transformer is built. This is stored only when a non-fitted estimator is passed to the SelectFromModel, i.e when prefit is False.

**threshold** [float] The threshold value used for feature selection.

# Methods

fit(self, X[, y])	Fit the SelectFromModel meta-transformer.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
<pre>partial_fit(self, X[, y])</pre>	Fit the SelectFromModel meta-transformer only once.
	Continued on next page

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Table 6.110 – continued from previous page

	· · · · · · · · · · · · · · · · · · ·
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

**\_\_init\_\_**(self, estimator, threshold=None, prefit=False, norm\_order=1, max\_features=None)

fit (self, X, y=None, \*\*fit\_params)

Fit the SelectFromModel meta-transformer.

#### **Parameters**

- **X** [array-like of shape (n\_samples, n\_features)] The training input samples.
- **y** [array-like, shape (n\_samples,)] The target values (integers that correspond to classes in classification, real numbers in regression).
- \*\*fit\_params [Other estimator specific parameters]

### Returns

self [object]

fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- **y** [numpy array of shape [n\_samples]] Target values.

# Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

# get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

# **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

### **Returns**

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

### inverse transform (self, X)

Reverse the transformation operation

#### **Parameters**

**X** [array of shape [n\_samples, n\_selected\_features]] The input samples.

### **Returns**

**X\_r** [array of shape [n\_samples, n\_original\_features]] X with columns of zeros inserted where features would have been removed by transform.

```
partial_fit (self, X, y=None, **fit_params)
```

Fit the SelectFromModel meta-transformer only once.

#### **Parameters**

- **X** [array-like of shape (n\_samples, n\_features)] The training input samples.
- **y** [array-like, shape (n\_samples,)] The target values (integers that correspond to classes in classification, real numbers in regression).

\*\*fit\_params [Other estimator specific parameters]

### **Returns**

self [object]

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# transform(self, X)

Reduce X to the selected features.

# **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

### Returns

X\_r [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

# Examples using sklearn.feature\_selection.SelectFromModel

- Feature selection using SelectFromModel and LassoCV
- Classification of text documents using sparse features

# 6.16.7 sklearn.feature\_selection.SelectFwe

 ${\bf class} \; {\tt sklearn.feature\_selection.SelectFwe} \; ({\it score\_func=<\! \it function} \; f\_{\it classif}\!\!>, \\ {\it alpha=0.05})$ 

Filter: Select the p-values corresponding to Family-wise error rate

Read more in the User Guide.

### **Parameters**

**score\_func** [callable] Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues). Default is f\_classif (see below "See also"). The default function only works with classification tasks.

**alpha** [float, optional] The highest uncorrected p-value for features to keep.

## **Attributes**

scores\_ [array-like, shape=(n\_features,)] Scores of features.
pvalues\_ [array-like, shape=(n\_features,)] p-values of feature scores.

### See also:

**f\_classif** ANOVA F-value between label/feature for classification tasks.

chi2 Chi-squared stats of non-negative features for classification tasks.

**f\_regression** F-value between label/feature for regression tasks.

**SelectPercentile** Select features based on percentile of the highest scores.

**SelectKBest** Select features based on the k highest scores.

SelectFpr Select features based on a false positive rate test.

**SelectFdr** Select features based on an estimated false discovery rate.

GenericUnivariateSelect Univariate feature selector with configurable mode.

# **Examples**

```
>>> from sklearn.datasets import load_breast_cancer
>>> from sklearn.feature_selection import SelectFwe, chi2
>>> X, y = load_breast_cancer(return_X_y=True)
>>> X.shape
(569, 30)
>>> X_new = SelectFwe(chi2, alpha=0.01).fit_transform(X, y)
>>> X_new.shape
(569, 15)
```

#### **Methods**

fit(self, X, y)	Run score function on (X, y) and get the appropriate
	features.
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

```
__init__ (self, score_func=<function f_classif at 0x7efe30bb2158>, alpha=0.05)

fit (self, X, y)
```

Run score function on (X, y) and get the appropriate features.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] The training input samples.
- y [array-like, shape = [n\_samples]] The target values (class labels in classification, real numbers in regression).

#### Returns

self [object]

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

# **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

### **Returns**

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

# $\verb"inverse_transform" (\textit{self}, X)$

Reverse the transformation operation

#### **Parameters**

X [array of shape [n\_samples, n\_selected\_features]] The input samples.

# Returns

**X\_r** [array of shape [n\_samples, n\_original\_features]] *X* with columns of zeros inserted where features would have been removed by *transform*.

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### transform(self, X)

Reduce X to the selected features.

#### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

#### Returns

X\_r [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

# 6.16.8 sklearn.feature\_selection.RFE

**class** sklearn.feature\_selection.**RFE** (*estimator*, *n\_features\_to\_select=None*, *step=1*, *verbose=0*) Feature ranking with recursive feature elimination.

Given an external estimator that assigns weights to features (e.g., the coefficients of a linear model), the goal of recursive feature elimination (RFE) is to select features by recursively considering smaller and smaller sets of features. First, the estimator is trained on the initial set of features and the importance of each feature is obtained either through a coef\_attribute or through a feature\_importances\_ attribute. Then, the least important features are pruned from current set of features. That procedure is recursively repeated on the pruned set until the desired number of features to select is eventually reached.

Read more in the *User Guide*.

### **Parameters**

estimator [object] A supervised learning estimator with a fit method that provides information about feature importance either through a coef\_ attribute or through a feature importances attribute.

**n\_features\_to\_select** [int or None (default=None)] The number of features to select. If None, half of the features are selected.

**step** [int or float, optional (default=1)] If greater than or equal to 1, then step corresponds to the (integer) number of features to remove at each iteration. If within (0.0, 1.0), then step corresponds to the percentage (rounded down) of features to remove at each iteration.

**verbose** [int, (default=0)] Controls verbosity of output.

### **Attributes**

**n\_features\_** [int] The number of selected features.

**support**\_ [array of shape [n\_features]] The mask of selected features.

**ranking** [array of shape [n\_features]] The feature ranking, such that ranking\_[i] corresponds to the ranking position of the i-th feature. Selected (i.e., estimated best) features are assigned rank 1.

estimator\_ [object] The external estimator fit on the reduced dataset.

### See also:

**RFECV** Recursive feature elimination with built-in cross-validated selection of the best number of features

### References

[Re310f679c81e-1]

### **Examples**

The following example shows how to retrieve the 5 right informative features in the Friedman #1 dataset.

```
>>> from sklearn.datasets import make_friedman1
>>> from sklearn.feature_selection import RFE
>>> from sklearn.svm import SVR
>>> X, y = make_friedman1(n_samples=50, n_features=10, random_state=0)
>>> estimator = SVR(kernel="linear")
>>> selector = RFE(estimator, 5, step=1)
>>> selector = selector.fit(X, y)
>>> selector.support_
array([ True, True, True, True, True, False, False, False, False])
>>> selector.ranking_
array([1, 1, 1, 1, 6, 4, 3, 2, 5])
```

### **Methods**

decision_function(self, X)	Compute the decision function of X.
fit(self, X, y)	Fit the RFE model and then the underlying estimator on
	the selected features.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
predict(self, X)	Reduce X to the selected features and then predict using
	the underlying estimator.
<pre>predict_log_proba(self, X)</pre>	Predict class log-probabilities for X.
predict_proba(self, X)	Predict class probabilities for X.
score(self, X, y)	Reduce X to the selected features and then return the
	score of the underlying estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

```
__init__ (self, estimator, n_features_to_select=None, step=1, verbose=0)
```

## $decision_function(self, X)$

Compute the decision function of X.

### **Parameters**

X [array-like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to

a sparse csr\_matrix.

### **Returns**

**score** [array, shape = [n\_samples, n\_classes] or [n\_samples]] The decision function of the input samples. The order of the classes corresponds to that in the attribute *classes*. Regression and binary classification produce an array of shape [n\_samples].

fit (self, X, y)

Fit the RFE model and then the underlying estimator on the selected features.

### **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] The training input samples.
- y [array-like, shape = [n\_samples]] The target values.

### fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit params and returns a transformed version of X.

#### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

#### **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

### Returns

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

### $inverse\_transform(self, X)$

Reverse the transformation operation

#### **Parameters**

**X** [array of shape [n\_samples, n\_selected\_features]] The input samples.

### **Returns**

**X\_r** [array of shape [n\_samples, n\_original\_features]] *X* with columns of zeros inserted where features would have been removed by *transform*.

predict (self, X)

Reduce X to the selected features and then predict using the underlying estimator.

### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

#### Returns

y [array of shape [n\_samples]] The predicted target values.

### $predict_log_proba(self, X)$

Predict class log-probabilities for X.

### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

### Returns

**p** [array of shape = [n\_samples, n\_classes]] The class log-probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes*.

### predict\_proba (self, X)

Predict class probabilities for X.

### **Parameters**

X [array-like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

### Returns

**p** [array of shape = [n\_samples, n\_classes]] The class probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes*\_.

 $\mathtt{score}\,(\mathit{self},\mathit{X},\mathit{y})$ 

Reduce X to the selected features and then return the score of the underlying estimator.

### **Parameters**

- **X** [array of shape [n\_samples, n\_features]] The input samples.
- y [array of shape [n\_samples]] The target values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

### transform(self, X)

Reduce X to the selected features.

#### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

#### Returns

**X\_r** [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

# Examples using sklearn.feature\_selection.RFE

• Recursive feature elimination

# 6.16.9 sklearn.feature selection.RFECV

Feature ranking with recursive feature elimination and cross-validated selection of the best number of features.

See glossary entry for cross-validation estimator.

Read more in the User Guide.

#### **Parameters**

- **estimator** [object] A supervised learning estimator with a fit method that provides information about feature importance either through a coef\_ attribute or through a feature\_importances\_ attribute.
- step [int or float, optional (default=1)] If greater than or equal to 1, then step corresponds to the (integer) number of features to remove at each iteration. If within (0.0, 1.0), then step corresponds to the percentage (rounded down) of features to remove at each iteration. Note that the last iteration may remove fewer than step features in order to reach min\_features\_to\_select.
- min\_features\_to\_select [int, (default=1)] The minimum number of features to be selected. This number of features will always be scored, even if the difference between the original feature count and min\_features\_to\_select isn't divisible by step.
- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross-validation,
  - integer, to specify the number of folds.
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if y is binary or multiclass,  $sklearn.model\_selection$ . StratifiedKFold is used. If the estimator is a classifier or if y is neither binary nor multiclass,  $sklearn.model\_selection.KFold$  is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value of None will change from 3-fold to 5-fold in v0.22.

verbose [int, (default=0)] Controls verbosity of output.

**n\_jobs** [int or None, optional (default=None)] Number of cores to run in parallel while fitting across folds. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

### Attributes

**n\_features\_** [int] The number of selected features with cross-validation.

**support**\_ [array of shape [n\_features]] The mask of selected features.

**ranking** [array of shape [n\_features]] The feature ranking, such that ranking\_[i] corresponds to the ranking position of the i-th feature. Selected (i.e., estimated best) features are assigned rank 1.

**grid\_scores** [array of shape [n\_subsets\_of\_features]] The cross-validation scores such that grid scores [i] corresponds to the CV score of the i-th subset of features.

**estimator**\_ [object] The external estimator fit on the reduced dataset.

### See also:

**RFE** Recursive feature elimination

### **Notes**

The size of grid\_scores\_ is equal to ceil((n\_features - min\_features\_to\_select) / step) + 1, where step is the number of features removed at each iteration.

### References

[R6f4d61ceb411-1]

### **Examples**

The following example shows how to retrieve the a-priori not known 5 informative features in the Friedman #1 dataset.

```
>>> from sklearn.datasets import make_friedman1
>>> from sklearn.feature_selection import RFECV
>>> from sklearn.svm import SVR
>>> X, y = make_friedman1(n_samples=50, n_features=10, random_state=0)
>>> estimator = SVR(kernel="linear")
>>> selector = RFECV(estimator, step=1, cv=5)
>>> selector = selector.fit(X, y)
>>> selector.support_
array([ True,  True,  True,  True,  False,  False,  False,  False])
>>> selector.ranking_
array([1, 1, 1, 1, 1, 6, 4, 3, 2, 5])
```

### **Methods**

decision_function(self, X)	Compute the decision function of X.
fit(self, X, y[, groups])	Fit the RFE model and automatically tune the number
	of selected features.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
predict(self, X)	Reduce X to the selected features and then predict using
	the underlying estimator.
predict_log_proba(self, X)	Predict class log-probabilities for X.
predict_proba(self, X)	Predict class probabilities for X.
score(self, X, y)	Reduce X to the selected features and then return the
	score of the underlying estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

\_\_init\_\_ (self, estimator, step=1, min\_features\_to\_select=1, cv='warn', scoring=None, verbose=0, n\_jobs=None)

### $decision_function(self, X)$

Compute the decision function of X.

#### **Parameters**

X [array-like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr matrix.

### Returns

**score** [array, shape = [n\_samples, n\_classes] or [n\_samples]] The decision function of the input samples. The order of the classes corresponds to that in the attribute *classes*. Regression and binary classification produce an array of shape [n\_samples].

fit (self, X, y, groups=None)

Fit the RFE model and automatically tune the number of selected features.

### **Parameters**

- **X** [{array-like, sparse matrix}, shape =  $[n_samples, n_features]$ ] Training vector, where  $n_samples$  is the number of samples and  $n_features$  is the total number of features.
- **y** [array-like, shape = [n\_samples]] Target values (integers for classification, real numbers for regression).

**groups** [array-like, shape = [n\_samples], optional] Group labels for the samples used while splitting the dataset into train/test set. Only used in conjunction with a "Group" *cv* instance (e.g., *GroupKFold*).

### fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

### get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

#### **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

### Returns

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

# $inverse\_transform(self, X)$

Reverse the transformation operation

### **Parameters**

X [array of shape [n\_samples, n\_selected\_features]] The input samples.

### Returns

**X\_r** [array of shape [n\_samples, n\_original\_features]] *X* with columns of zeros inserted where features would have been removed by *transform*.

### predict (self, X)

Reduce X to the selected features and then predict using the underlying estimator.

### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

### **Returns**

y [array of shape [n\_samples]] The predicted target values.

### $predict_log_proba(self, X)$

Predict class log-probabilities for X.

### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

### **Returns**

**p** [array of shape = [n\_samples, n\_classes]] The class log-probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes*\_.

### predict\_proba (self, X)

Predict class probabilities for X.

#### **Parameters**

X [array-like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

### Returns

**p** [array of shape = [n\_samples, n\_classes]] The class probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes*\_.

score(self, X, y)

Reduce X to the selected features and then return the score of the underlying estimator.

#### **Parameters**

- **X** [array of shape [n\_samples, n\_features]] The input samples.
- y [array of shape [n\_samples]] The target values.

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

### transform(self, X)

Reduce X to the selected features.

### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

### Returns

**X\_r** [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

### Examples using sklearn.feature\_selection.RFECV

• Recursive feature elimination with cross-validation

# 6.16.10 sklearn.feature selection.VarianceThreshold

class sklearn.feature\_selection.VarianceThreshold(threshold=0.0)

Feature selector that removes all low-variance features.

This feature selection algorithm looks only at the features (X), not the desired outputs (y), and can thus be used for unsupervised learning.

Read more in the *User Guide*.

#### **Parameters**

**threshold** [float, optional] Features with a training-set variance lower than this threshold will be removed. The default is to keep all features with non-zero variance, i.e. remove the features that have the same value in all samples.

### **Attributes**

variances\_ [array, shape (n\_features,)] Variances of individual features.

## **Examples**

The following dataset has integer features, two of which are the same in every sample. These are removed with the default setting for threshold:

### Methods

fit(self, X[, y])	Learn empirical variances from X.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>get_support(self[, indices])</pre>	Get a mask, or integer index, of the features selected
inverse_transform(self, X)	Reverse the transformation operation
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Reduce X to the selected features.

```
\_\_init\_\_(self, threshold=0.0)
```

fit (self, X, y=None)

Learn empirical variances from X.

### **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Sample vectors from which to compute variances.
- y [any] Ignored. This parameter exists only for compatibility with sklearn.pipeline.Pipeline.

#### **Returns**

self

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### Returns

**X new** [numpy array of shape [n samples, n features new]] Transformed array.

### get params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

### get\_support (self, indices=False)

Get a mask, or integer index, of the features selected

#### **Parameters**

**indices** [boolean (default False)] If True, the return value will be an array of integers, rather than a boolean mask.

#### Returns

support [array] An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

### $inverse\_transform(self, X)$

Reverse the transformation operation

### **Parameters**

**X** [array of shape [n\_samples, n\_selected\_features]] The input samples.

### Returns

**X\_r** [array of shape [n\_samples, n\_original\_features]] *X* with columns of zeros inserted where features would have been removed by *transform*.

### set params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

### transform(self, X)

Reduce X to the selected features.

#### **Parameters**

**X** [array of shape [n\_samples, n\_features]] The input samples.

### Returns

**X\_r** [array of shape [n\_samples, n\_selected\_features]] The input samples with only the selected features.

$feature\_selection.chi2(X,y)$	Compute chi-squared stats between each non-negative feature and class.
$feature\_selection.f\_classif(X, y)$	Compute the ANOVA F-value for the provided sample.
feature_selection.f_regression(X, y[, cen-	Univariate linear regression tests.
ter])	
feature_selection.	Estimate mutual information for a discrete target variable.
$ exttt{mutual\_info\_classif}(X,y)$	
feature_selection.	Estimate mutual information for a continuous target vari-
${\it mutual\_info\_regression}(X,y)$	able.

# 6.16.11 sklearn.feature\_selection.chi2

```
sklearn.feature_selection.chi2(X, y)
```

Compute chi-squared stats between each non-negative feature and class.

This score can be used to select the n\_features features with the highest values for the test chi-squared statistic from X, which must contain only non-negative features such as booleans or frequencies (e.g., term counts in document classification), relative to the classes.

Recall that the chi-square test measures dependence between stochastic variables, so using this function "weeds out" the features that are the most likely to be independent of class and therefore irrelevant for classification.

Read more in the User Guide.

### **Parameters**

- **X** [{array-like, sparse matrix}, shape = (n\_samples, n\_features\_in)] Sample vectors.
- y [array-like, shape = (n\_samples,)] Target vector (class labels).

### Returns

```
chi2 [array, shape = (n_features,)] chi2 statistics of each feature.
```

**pval** [array, shape = (n\_features,)] p-values of each feature.

### See also:

**f\_classif** ANOVA F-value between label/feature for classification tasks.

**f\_regression** F-value between label/feature for regression tasks.

### **Notes**

Complexity of this algorithm is  $O(n\_classes * n\_features)$ .

## Examples using sklearn.feature\_selection.chi2

- Selecting dimensionality reduction with Pipeline and GridSearchCV
- SVM-Anova: SVM with univariate feature selection
- Classification of text documents using sparse features

# 6.16.12 sklearn.feature\_selection.f\_classif

```
sklearn.feature_selection.\mathbf{f}_classif(X, y)
```

Compute the ANOVA F-value for the provided sample.

Read more in the User Guide.

#### **Parameters**

- **X** [{array-like, sparse matrix} shape = [n\_samples, n\_features]] The set of regressors that will be tested sequentially.
- y [array of shape(n\_samples)] The data matrix.

### Returns

```
F [array, shape = [n_features,]] The set of F values.
```

**pval** [array, shape = [n\_features,]] The set of p-values.

### See also:

chi2 Chi-squared stats of non-negative features for classification tasks.

**f\_regression** F-value between label/feature for regression tasks.

### Examples using sklearn.feature\_selection.f\_classif

• Univariate Feature Selection

# 6.16.13 sklearn.feature\_selection.f\_regression

```
sklearn.feature_selection.f_regression(X, y, center=True)
```

Univariate linear regression tests.

Linear model for testing the individual effect of each of many regressors. This is a scoring function to be used in a feature selection procedure, not a free standing feature selection procedure.

This is done in 2 steps:

- 1. The correlation between each regressor and the target is computed, that is, ((X[:, i] mean(X[:, i])) \* (y mean\_y)) / (std(X[:, i]) \* std(y)).
- 2. It is converted to an F score then to a p-value.

For more on usage see the *User Guide*.

#### **Parameters**

- **X** [{array-like, sparse matrix} shape = (n\_samples, n\_features)] The set of regressors that will be tested sequentially.
- y [array of shape(n\_samples).] The data matrix

**center** [True, bool,] If true, X and y will be centered.

### Returns

**F** [array, shape=(n\_features,)] F values of features.

**pval** [array, shape=(n\_features,)] p-values of F-scores.

See also:

```
mutual_info_regression Mutual information for a continuous target.
```

f classif ANOVA F-value between label/feature for classification tasks.

chi2 Chi-squared stats of non-negative features for classification tasks.

**SelectKBest** Select features based on the k highest scores.

**SelectFpr** Select features based on a false positive rate test.

**SelectFdr** Select features based on an estimated false discovery rate.

**SelectFwe** Select features based on family-wise error rate.

**SelectPercentile** Select features based on percentile of the highest scores.

### Examples using sklearn.feature\_selection.f\_regression

- Feature agglomeration vs. univariate selection
- Comparison of F-test and mutual information
- Pipeline Anova SVM

# 6.16.14 sklearn.feature\_selection.mutual\_info\_classif

```
sklearn.feature_selection.mutual_info_classif(X, y, discrete_features='auto', n_neighbors=3, copy=True, random_state=None)
```

Estimate mutual information for a discrete target variable.

Mutual information (MI) [1] between two random variables is a non-negative value, which measures the dependency between the variables. It is equal to zero if and only if two random variables are independent, and higher values mean higher dependency.

The function relies on nonparametric methods based on entropy estimation from k-nearest neighbors distances as described in [2] and [3]. Both methods are based on the idea originally proposed in [4].

It can be used for univariate features selection, read more in the *User Guide*.

### **Parameters**

- **X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Feature matrix.
- y [array\_like, shape (n\_samples,)] Target vector.
- **discrete\_features** [{'auto', bool, array\_like}, default 'auto'] If bool, then determines whether to consider all features discrete or continuous. If array, then it should be either a boolean mask with shape (n\_features,) or array with indices of discrete features. If 'auto', it is assigned to False for dense *X* and to True for sparse *X*.
- **n\_neighbors** [int, default 3] Number of neighbors to use for MI estimation for continuous variables, see [2] and [3]. Higher values reduce variance of the estimation, but could introduce a bias.
- **copy** [bool, default True] Whether to make a copy of the given data. If set to False, the initial data will be overwritten.
- random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator for adding small noise to continuous variables in order to remove repeated values. If int, random\_state is the seed used by the random number

generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### Returns

**mi** [ndarray, shape (n\_features,)] Estimated mutual information between each feature and the target.

### **Notes**

- 1. The term "discrete features" is used instead of naming them "categorical", because it describes the essence more accurately. For example, pixel intensities of an image are discrete features (but hardly categorical) and you will get better results if mark them as such. Also note, that treating a continuous variable as discrete and vice versa will usually give incorrect results, so be attentive about that.
- 2. True mutual information can't be negative. If its estimate turns out to be negative, it is replaced by zero.

### References

[1], [2], [3], [4]

# 6.16.15 sklearn.feature\_selection.mutual\_info\_regression

```
sklearn.feature_selection.mutual_info_regression(X, y, discrete_features='auto', n\_neighbors=3, copy=True, random state=None)
```

Estimate mutual information for a continuous target variable.

Mutual information (MI) [1] between two random variables is a non-negative value, which measures the dependency between the variables. It is equal to zero if and only if two random variables are independent, and higher values mean higher dependency.

The function relies on nonparametric methods based on entropy estimation from k-nearest neighbors distances as described in [2] and [3]. Both methods are based on the idea originally proposed in [4].

It can be used for univariate features selection, read more in the *User Guide*.

### **Parameters**

- **X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Feature matrix.
- y [array\_like, shape (n\_samples,)] Target vector.
- **discrete\_features** [{'auto', bool, array\_like}, default 'auto'] If bool, then determines whether to consider all features discrete or continuous. If array, then it should be either a boolean mask with shape (n\_features,) or array with indices of discrete features. If 'auto', it is assigned to False for dense *X* and to True for sparse *X*.
- **n\_neighbors** [int, default 3] Number of neighbors to use for MI estimation for continuous variables, see [2] and [3]. Higher values reduce variance of the estimation, but could introduce a bias.
- **copy** [bool, default True] Whether to make a copy of the given data. If set to False, the initial data will be overwritten.
- random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator for adding small noise to continuous variables in order to remove repeated values. If int, random\_state is the seed used by the random number

generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### Returns

**mi** [ndarray, shape (n\_features,)] Estimated mutual information between each feature and the target.

### **Notes**

- 1. The term "discrete features" is used instead of naming them "categorical", because it describes the essence more accurately. For example, pixel intensities of an image are discrete features (but hardly categorical) and you will get better results if mark them as such. Also note, that treating a continuous variable as discrete and vice versa will usually give incorrect results, so be attentive about that.
- 2. True mutual information can't be negative. If its estimate turns out to be negative, it is replaced by zero.

### References

[1], [2], [3], [4]

### Examples using sklearn.feature\_selection.mutual\_info\_regression

• Comparison of F-test and mutual information

# 6.17 sklearn.gaussian\_process: Gaussian Processes

The sklearn.gaussian\_process module implements Gaussian Process based regression and classification.

**User guide:** See the *Gaussian Processes* section for further details.

```
gaussian_process.GaussianProcessClassifie Caussian process classification (GPC) based on Laplace approximation.

gaussian_process.GaussianProcessRegressor (Gaussian process regression (GPR).
```

# 6.17.1 sklearn.gaussian\_process.GaussianProcessClassifier

Gaussian process classification (GPC) based on Laplace approximation.

The implementation is based on Algorithm 3.1, 3.2, and 5.1 of Gaussian Processes for Machine Learning (GPML) by Rasmussen and Williams.

Internally, the Laplace approximation is used for approximating the non-Gaussian posterior by a Gaussian.

Currently, the implementation is restricted to using the logistic link function. For multi-class classification, several binary one-versus rest classifiers are fitted. Note that this class thus does not implement a true multi-class Laplace approximation.

### **Parameters**

- **kernel** [kernel object] The kernel specifying the covariance function of the GP. If None is passed, the kernel "1.0 \* RBF(1.0)" is used as default. Note that the kernel's hyperparameters are optimized during fitting.
- **optimizer** [string or callable, optional (default: "fmin\_l\_bfgs\_b")] Can either be one of the internally supported optimizers for optimizing the kernel's parameters, specified by a string, or an externally defined optimizer passed as a callable. If a callable is passed, it must have the signature:

```
def optimizer(obj_func, initial_theta, bounds):
    # * 'obj_func' is the objective function to be maximized, which
    # takes the hyperparameters theta as parameter and an
    # optional flag eval_gradient, which determines if the
    # gradient is returned additionally to the function value
    # * 'initial_theta': the initial value for theta, which can be
    # used by local optimizers
    # * 'bounds': the bounds on the values of theta
    ....
    # Returned are the best found hyperparameters theta and
    # the corresponding value of the target function.
    return theta_opt, func_min
```

Per default, the 'fmin\_l\_bfgs\_b' algorithm from scipy.optimize is used. If None is passed, the kernel's parameters are kept fixed. Available internal optimizers are:

```
'fmin_l_bfgs_b'
```

- n\_restarts\_optimizer [int, optional (default: 0)] The number of restarts of the optimizer for finding the kernel's parameters which maximize the log-marginal likelihood. The first run of the optimizer is performed from the kernel's initial parameters, the remaining ones (if any) from thetas sampled log-uniform randomly from the space of allowed theta-values. If greater than 0, all bounds must be finite. Note that n\_restarts\_optimizer=0 implies that one run is performed.
- **max\_iter\_predict** [int, optional (default: 100)] The maximum number of iterations in Newton's method for approximating the posterior during predict. Smaller values will reduce computation time at the cost of worse results.
- warm\_start [bool, optional (default: False)] If warm-starts are enabled, the solution of the last Newton iteration on the Laplace approximation of the posterior mode is used as initialization for the next call of \_posterior\_mode(). This can speed up convergence when \_posterior\_mode is called several times on similar problems as in hyperparameter optimization. See the Glossary.
- **copy\_X\_train** [bool, optional (default: True)] If True, a persistent copy of the training data is stored in the object. Otherwise, just a reference to the training data is stored, which might cause predictions to change if the data is modified externally.
- **random\_state** [int, RandomState instance or None, optional (default: None)] The generator used to initialize the centers. If int, random\_state is the seed used by the random number

generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

- multi\_class [string, default] Specifies how multi-class classification problems are handled. Supported are "one\_vs\_rest" and "one\_vs\_one". In "one\_vs\_rest", one binary Gaussian process classifier is fitted for each class, which is trained to separate this class from the rest. In "one\_vs\_one", one binary Gaussian process classifier is fitted for each pair of classes, which is trained to separate these two classes. The predictions of these binary predictors are combined into multi-class predictions. Note that "one\_vs\_one" does not support predicting probability estimates.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### **Attributes**

**kernel**\_ [kernel object] The kernel used for prediction. In case of binary classification, the structure of the kernel is the same as the one passed as parameter but with optimized hyperparameters. In case of multi-class classification, a CompoundKernel is returned which consists of the different kernels used in the one-versus-rest classifiers.

log\_marginal\_likelihood\_value\_ [float] The log-marginal-likelihood of self.kernel\_.
theta

**classes**\_ [array-like, shape = (n\_classes,)] Unique class labels.

n\_classes\_ [int] The number of classes in the training data

### **Examples**

New in version 0.18.

### **Methods**

fit(self, X, y)	Fit Gaussian process classification model
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
log_marginal_likelihood(self[, theta,])	Returns log-marginal likelihood of theta for training
	data.
predict(self, X)	Perform classification on an array of test vectors X.
predict_proba(self, X)	Return probability estimates for the test vector X.
	Continued on next page

Table 6.117 – continued from previous page

score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, kernel=None, optimizer='fmin\_l\_bfgs\_b', n\_restarts\_optimizer=0, max\_iter\_predict=100, warm\_start=False, copy\_X\_train=True, random\_state=None, multi\_class='one\_vs\_rest', n\_jobs=None)

### fit (self, X, y)

Fit Gaussian process classification model

#### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Training data
- y [array-like, shape = (n\_samples,)] Target values, must be binary

### Returns

**self** [returns an instance of self.]

### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

### log marginal likelihood(self, theta=None, eval gradient=False)

Returns log-marginal likelihood of theta for training data.

In the case of multi-class classification, the mean log-marginal likelihood of the one-versus-rest classifiers are returned.

### **Parameters**

theta [array-like, shape = (n\_kernel\_params,) or none] Kernel hyperparameters for which the log-marginal likelihood is evaluated. In the case of multi-class classification, theta may be the hyperparameters of the compound kernel or of an individual kernel. In the latter case, all individual kernel get assigned the same theta values. If None, the precomputed log\_marginal\_likelihood of self.kernel\_.theta is returned.

**eval\_gradient** [bool, default: False] If True, the gradient of the log-marginal likelihood with respect to the kernel hyperparameters at position theta is returned additionally. Note that gradient computation is not supported for non-binary classification. If True, theta must not be None.

### Returns

**log\_likelihood** [float] Log-marginal likelihood of theta for training data.

**log\_likelihood\_gradient** [array, shape = (n\_kernel\_params,), optional] Gradient of the log-marginal likelihood with respect to the kernel hyperparameters at position theta. Only returned when eval\_gradient is True.

### predict (self, X)

Perform classification on an array of test vectors X.

### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)]

### **Returns**

C [array, shape = (n\_samples,)] Predicted target values for X, values are from classes\_

### predict proba(self, X)

Return probability estimates for the test vector X.

### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)]

### **Returns**

**C** [array-like, shape = (n\_samples, n\_classes)] Returns the probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
X [array-like, shape = (n samples, n features)] Test samples.
```

y [array-like, shape = (n samples) or (n samples, n outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

### Examples using sklearn.gaussian\_process.GaussianProcessClassifier

- Plot classification probability
- Classifier comparison
- Illustration of Gaussian process classification (GPC) on the XOR dataset
- Gaussian process classification (GPC) on iris dataset
- Iso-probability lines for Gaussian Processes classification (GPC)
- Probabilistic predictions with Gaussian process classification (GPC)

# 6.17.2 sklearn.gaussian process.GaussianProcessRegressor

```
 \textbf{class} \texttt{ sklearn.gaussian\_process.GaussianProcessRegressor} (\textit{kernel=None}, & \textit{alpha=1e-10}, \\ \textit{optimizer='fmin\_l\_bfgs\_b'}, \\ \textit{n\_restarts\_optimizer=0}, \\ \textit{normalize\_y=False}, \\ \textit{copy\_X\_train=True}, & \textit{random\_state=None})
```

Gaussian process regression (GPR).

The implementation is based on Algorithm 2.1 of Gaussian Processes for Machine Learning (GPML) by Rasmussen and Williams.

In addition to standard scikit-learn estimator API, GaussianProcessRegressor:

- allows prediction without prior fitting (based on the GP prior)
- provides an additional method sample\_y(X), which evaluates samples drawn from the GPR (prior or posterior) at given inputs
- exposes a method log\_marginal\_likelihood(theta), which can be used externally for other ways of selecting hyperparameters, e.g., via Markov chain Monte Carlo.

Read more in the *User Guide*.

New in version 0.18.

#### **Parameters**

**kernel** [kernel object] The kernel specifying the covariance function of the GP. If None is passed, the kernel "1.0 \* RBF(1.0)" is used as default. Note that the kernel's hyperparameters are optimized during fitting.

alpha [float or array-like, optional (default: 1e-10)] Value added to the diagonal of the kernel matrix during fitting. Larger values correspond to increased noise level in the observations. This can also prevent a potential numerical issue during fitting, by ensuring that the calculated values form a positive definite matrix. If an array is passed, it must have the same number of entries as the data used for fitting and is used as datapoint-dependent noise level. Note that this is equivalent to adding a WhiteKernel with c=alpha. Allowing to specify the noise level directly as a parameter is mainly for convenience and for consistency with Ridge.

**optimizer** [string or callable, optional (default: "fmin\_l\_bfgs\_b")] Can either be one of the internally supported optimizers for optimizing the kernel's parameters, specified by a string, or an externally defined optimizer passed as a callable. If a callable is passed, it must have the signature:

```
def optimizer(obj_func, initial_theta, bounds):
    # * 'obj_func' is the objective function to be minimized, which
    # takes the hyperparameters theta as parameter and an
    # optional flag eval_gradient, which determines if the
    # gradient is returned additionally to the function value
    # * 'initial_theta': the initial value for theta, which can be
    # used by local optimizers
    # * 'bounds': the bounds on the values of theta
    ....
    # Returned are the best found hyperparameters theta and
    # the corresponding value of the target function.
    return theta_opt, func_min
```

Per default, the 'fmin\_l\_bfgs\_b' algorithm from scipy.optimize is used. If None is passed, the kernel's parameters are kept fixed. Available internal optimizers are:

```
'fmin_l_bfgs_b'
```

- **n\_restarts\_optimizer** [int, optional (default: 0)] The number of restarts of the optimizer for finding the kernel's parameters which maximize the log-marginal likelihood. The first run of the optimizer is performed from the kernel's initial parameters, the remaining ones (if any) from thetas sampled log-uniform randomly from the space of allowed theta-values. If greater than 0, all bounds must be finite. Note that n\_restarts\_optimizer == 0 implies that one run is performed.
- normalize\_y [boolean, optional (default: False)] Whether the target values y are normalized, i.e., the mean of the observed target values become zero. This parameter should be set to True if the target values' mean is expected to differ considerable from zero. When enabled, the normalization effectively modifies the GP's prior based on the data, which contradicts the likelihood principle; normalization is thus disabled per default.
- **copy\_X\_train** [bool, optional (default: True)] If True, a persistent copy of the training data is stored in the object. Otherwise, just a reference to the training data is stored, which might cause predictions to change if the data is modified externally.
- random\_state [int, RandomState instance or None, optional (default: None)] The generator used to initialize the centers. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

### **Attributes**

- **X\_train**\_ [array-like, shape = (n\_samples, n\_features)] Feature values in training data (also required for prediction)
- y\_train\_ [array-like, shape = (n\_samples, [n\_output\_dims])] Target values in training data (also required for prediction)
- **kernel**\_ [kernel object] The kernel used for prediction. The structure of the kernel is the same as the one passed as parameter but with optimized hyperparameters
- L\_ [array-like, shape = (n\_samples, n\_samples)] Lower-triangular Cholesky decomposition of
  the kernel in X\_train\_
- **alpha**\_ [array-like, shape = (n\_samples,)] Dual coefficients of training data points in kernel space
- log\_marginal\_likelihood\_value\_ [float] The log-marginal-likelihood of self.kernel\_.
  theta

### **Examples**

```
>>> from sklearn.datasets import make_friedman2
>>> from sklearn.gaussian_process import GaussianProcessRegressor
>>> from sklearn.gaussian_process.kernels import DotProduct, WhiteKernel
>>> X, y = make_friedman2(n_samples=500, noise=0, random_state=0)
>>> kernel = DotProduct() + WhiteKernel()
>>> gpr = GaussianProcessRegressor(kernel=kernel,
... random_state=0).fit(X, y)
>>> gpr.score(X, y)
0.3680...
>>> gpr.predict(X[:2,:], return_std=True)
(array([653.0..., 592.1...]), array([316.6..., 316.6...]))
```

### **Methods**

fit(self, X, y)	Fit Gaussian process regression model.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
log_marginal_likelihood(self[, theta,])	Returns log-marginal likelihood of theta for training
	data.
<pre>predict(self, X[, return_std, return_cov])</pre>	Predict using the Gaussian process regression model
sample_y(self, X[, n_samples, random_state])	Draw samples from Gaussian process and evaluate at X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, kernel=None, alpha=1e-10, optimizer='fmin\_l\_bfgs\_b', n\_restarts\_optimizer=0, nor-malize\_y=False, copy\_X\_train=True, random\_state=None)

### **fit** (self, X, y)

Fit Gaussian process regression model.

#### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Training data

y [array-like, shape = (n\_samples, [n\_output\_dims])] Target values

### Returns

self [returns an instance of self.]

### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

log marginal likelihood(self, theta=None, eval gradient=False)

Returns log-marginal likelihood of theta for training data.

### **Parameters**

theta [array-like, shape = (n\_kernel\_params,) or None] Kernel hyperparameters for
which the log-marginal likelihood is evaluated. If None, the precomputed
log\_marginal\_likelihood of self.kernel\_.theta is returned.

**eval\_gradient** [bool, default: False] If True, the gradient of the log-marginal likelihood with respect to the kernel hyperparameters at position theta is returned additionally. If True, theta must not be None.

## Returns

log likelihood [float] Log-marginal likelihood of theta for training data.

**log\_likelihood\_gradient** [array, shape = (n\_kernel\_params,), optional] Gradient of the log-marginal likelihood with respect to the kernel hyperparameters at position theta. Only returned when eval\_gradient is True.

predict (self, X, return std=False, return cov=False)

Predict using the Gaussian process regression model

We can also predict based on an unfitted model by using the GP prior. In addition to the mean of the predictive distribution, also its standard deviation (return\_std=True) or covariance (return\_cov=True). Note that at most one of the two can be requested.

#### **Parameters**

 $\mathbf{X}$  [array-like, shape = (n\_samples, n\_features)] Query points where the GP is evaluated

**return\_std** [bool, default: False] If True, the standard-deviation of the predictive distribution at the query points is returned along with the mean.

**return\_cov** [bool, default: False] If True, the covariance of the joint predictive distribution at the query points is returned along with the mean

### Returns

- **y\_mean** [array, shape = (n\_samples, [n\_output\_dims])] Mean of predictive distribution a query points
- **y\_std** [array, shape = (n\_samples,), optional] Standard deviation of predictive distribution at query points. Only returned when return\_std is True.
- **y\_cov** [array, shape = (n\_samples, n\_samples), optional] Covariance of joint predictive distribution a query points. Only returned when return\_cov is True.

**sample y** ( $self, X, n \ samples=1, random \ state=0$ )

Draw samples from Gaussian process and evaluate at X.

#### **Parameters**

- **X** [array-like, shape = (n\_samples\_X, n\_features)] Query points where the GP samples are evaluated
- **n\_samples** [int, default: 1] The number of samples drawn from the Gaussian process
- random\_state [int, RandomState instance or None, optional (default=0)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

### Returns

**y\_samples** [array, shape = (n\_samples\_X, [n\_output\_dims], n\_samples)] Values of n\_samples samples drawn from Gaussian process and evaluated at query points.

score (self, X, y, sample weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares  $((y_true - y_pred) ** 2).sum()$  and v is the total sum of squares  $((y_true - y_true.mean()) ** 2).sum()$ . The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample weight** [array-like, shape = [n samples], optional] Sample weights.

### **Returns**

**score** [float] R^2 of self.predict(X) wrt. y.

### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

### Examples using sklearn.gaussian\_process.GaussianProcessRegressor

- · Comparison of kernel ridge and Gaussian process regression
- Illustration of prior and posterior Gaussian process for different kernels
- Gaussian process regression (GPR) with noise-level estimation
- Gaussian Processes regression: basic introductory example
- Gaussian process regression (GPR) on Mauna Loa CO2 data.

### Kernels:

gaussian_process.kernels.	Kernel which is composed of a set of other kernels.
CompoundKernel(kernels)	
gaussian_process.kernels.	Constant kernel.
ConstantKernel([])	
gaussian_process.kernels.	Dot-Product kernel.
$ extit{DotProduct([])}$	
gaussian_process.kernels.	Exp-Sine-Squared kernel.
$\textit{ExpSineSquared}([\dots])$	
gaussian_process.kernels.	Exponentiate kernel by given exponent.
Exponentiation $()$	
gaussian_process.kernels.Hyperparameter	A kernel hyperparameter's specification in form of a namedtuple.
gaussian_process.kernels.Kernel	Base class for all kernels.
<pre>gaussian_process.kernels.Matern([])</pre>	Matern kernel.
gaussian_process.kernels.	Wrapper for kernels in sklearn.metrics.pairwise.
PairwiseKernel([])	
gaussian_process.kernels.Product(k1, k2)	Product-kernel k1 * k2 of two kernels k1 and k2.

Continued on next page

Table 6.119 – continued from previous page

gaussian_process.kernels.RBF([length_scale,	Radial-basis function kernel (aka squared-exponential ker-
])	nel).
gaussian_process.kernels.	Rational Quadratic kernel.
RationalQuadratic $([\dots])$	
gaussian_process.kernels.Sum(k1, k2)	Sum-kernel k1 + k2 of two kernels k1 and k2.
gaussian_process.kernels.	White kernel.
WhiteKernel([])	

# 6.17.3 sklearn.gaussian\_process.kernels.CompoundKernel

class sklearn.gaussian\_process.kernels.CompoundKernel (kernels)

Kernel which is composed of a set of other kernels.

New in version 0.18.

### **Parameters**

kernels [list of Kernel objects] The other kernels

### **Attributes**

**bounds** Returns the log-transformed bounds on the theta.

hyperparameters Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

### **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel $k(X, Y)$ and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel k(X, X).
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this kernel.

\_\_init\_\_ (self, kernels)

**\_\_call**\_\_(self, X, Y=None, eval\_gradient=False)

Return the kernel k(X, Y) and optionally its gradient.

Note that this compound kernel returns the results of all simple kernel stacked along an additional axis.

### **Parameters**

- **X** [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)
- Y [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined.

### **Returns**

**K** [array, shape (n\_samples\_X, n\_samples\_Y, n\_kernels)] Kernel k(X, Y)

**K\_gradient** [array, shape (n\_samples\_X, n\_samples\_X, n\_dims, n\_kernels)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

#### bounds

Returns the log-transformed bounds on the theta.

#### Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

### clone\_with\_theta (self, theta)

Returns a clone of self with given hyperparameters theta.

### **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

### diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

#### **Parameters**

**X** [array, shape (n samples X, n features)] Left argument of the returned kernel k(X, Y)

#### Returns

**K\_diag** [array, shape (n\_samples\_X, n\_kernels)] Diagonal of kernel k(X, X)

### get\_params (self, deep=True)

Get parameters of this kernel.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# hyperparameters

Returns a list of all hyperparameter specifications.

### is stationary (self)

Returns whether the kernel is stationary.

### n\_dims

Returns the number of non-fixed hyperparameters of the kernel.

# set\_params (self, \*\*params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

#### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

#### Returns

theta [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

# 6.17.4 sklearn.gaussian\_process.kernels.ConstantKernel

Constant kernel.

Can be used as part of a product-kernel where it scales the magnitude of the other factor (kernel) or as part of a sum-kernel, where it modifies the mean of the Gaussian process.

 $k(x_1, x_2) = constant_value for all x_1, x_2$ 

New in version 0.18.

### **Parameters**

**constant\_value** [float, default: 1.0] The constant value which defines the covariance:  $k(x_1, x_2) = constant_value$ 

**constant\_value\_bounds** [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on constant value

#### **Attributes**

**bounds** Returns the log-transformed bounds on the theta.

### hyperparameter\_constant\_value

hyperparameters Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

### **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel $k(X, Y)$ and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this kernel.

```
__init__ (self, constant_value=1.0, constant_value_bounds=(1e-05, 100000.0))
```

\_\_\_call\_\_ (self, X, Y=None, eval\_gradient=False)

Return the kernel k(X, Y) and optionally its gradient.

### **Parameters**

- **X** [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)
- **Y** [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

#### Returns

**K** [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

#### bounds

Returns the log-transformed bounds on the theta.

#### Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

### clone with theta(self, theta)

Returns a clone of self with given hyperparameters theta.

#### **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

### diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

### **Parameters**

X [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

### Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

# get\_params (self, deep=True)

Get parameters of this kernel.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

#### hyperparameters

Returns a list of all hyperparameter specifications.

### is\_stationary(self)

Returns whether the kernel is stationary.

#### n dims

Returns the number of non-fixed hyperparameters of the kernel.

```
set_params (self, **params)
```

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

#### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

### Returns

theta [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

### Examples using sklearn.gaussian\_process.kernels.ConstantKernel

- Illustration of prior and posterior Gaussian process for different kernels
- Iso-probability lines for Gaussian Processes classification (GPC)
- Gaussian Processes regression: basic introductory example

# 6.17.5 sklearn.gaussian\_process.kernels.DotProduct

class sklearn.gaussian\_process.kernels.DotProduct(sigma\_0=1.0, sigma\_0\_bounds=(1e05,100000.0))

Dot-Product kernel.

The DotProduct kernel is non-stationary and can be obtained from linear regression by putting N(0, 1) priors on the coefficients of  $x_d$  ( $d = 1, \ldots, D$ ) and a prior of  $N(0, sigma_0^2)$  on the bias. The DotProduct kernel is invariant to a rotation of the coordinates about the origin, but not translations. It is parameterized by a parameter  $sigma_0^2$ . For  $sigma_0^2 = 0$ , the kernel is called the homogeneous linear kernel, otherwise it is inhomogeneous. The kernel is given by

```
k(x_i, x_j) = sigma_0 \wedge 2 + x_i \cdot cdot \cdot x_j
```

The DotProduct kernel is commonly combined with exponentiation.

New in version 0.18.

### **Parameters**

**sigma\_0** [float >= 0, default: 1.0] Parameter controlling the inhomogenity of the kernel. If sigma\_0=0, the kernel is homogenous.

sigma\_0\_bounds [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on 1

### **Attributes**

bounds Returns the log-transformed bounds on the theta.

### hyperparameter\_sigma\_0

hyperparameters Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

### **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel k(X, Y) and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
set_params(self, \*\*params)	Set the parameters of this kernel.

\_\_init\_\_ (self, sigma\_0=1.0, sigma\_0\_bounds=(1e-05, 100000.0))

 $\_\_$ call $\_\_$ (self, X, Y=None, eval $\_$ gradient=False)

Return the kernel k(X, Y) and optionally its gradient.

#### **Parameters**

- X [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)
- Y [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

### **Returns**

K [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval gradient is True.

### bounds

Returns the log-transformed bounds on the theta.

### Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

### clone\_with\_theta (self, theta)

Returns a clone of self with given hyperparameters theta.

### **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

### diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

### **Parameters**

**X** [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

#### Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

### get\_params (self, deep=True)

Get parameters of this kernel.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### hyperparameters

Returns a list of all hyperparameter specifications.

### is\_stationary(self)

Returns whether the kernel is stationary.

### n dims

Returns the number of non-fixed hyperparameters of the kernel.

```
set_params (self, **params)
```

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

### Returns

theta [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

### Examples using sklearn.gaussian\_process.kernels.DotProduct

- Illustration of Gaussian process classification (GPC) on the XOR dataset
- Illustration of prior and posterior Gaussian process for different kernels
- Iso-probability lines for Gaussian Processes classification (GPC)

# 6.17.6 sklearn.gaussian\_process.kernels.ExpSineSquared

```
 \begin{array}{ll} \textbf{class} \ \texttt{sklearn.gaussian\_process.kernels.ExpSineSquared} \ (length\_scale=1.0, \\ periodicity=1.0, \\ length\_scale\_bounds=(1e-05, \\ 100000.0), \\ periodicity\_bounds=(1e-05, \\ 100000.0)) \end{array}
```

Exp-Sine-Squared kernel.

The ExpSineSquared kernel allows modeling periodic functions. It is parameterized by a length-scale parameter length\_scale>0 and a periodicity parameter periodicity>0. Only the isotropic variant where 1 is a scalar is supported at the moment. The kernel given by:

 $k(x_i, x_j) = \exp(-2 (\sin(pi / periodicity * d(x_i, x_j)) / length_scale) ^ 2)$ 

New in version 0.18.

#### **Parameters**

**length\_scale** [float > 0, default: 1.0] The length scale of the kernel.

**periodicity** [float > 0, default: 1.0] The periodicity of the kernel.

**length\_scale\_bounds** [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on length\_scale

**periodicity\_bounds** [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on periodicity

### **Attributes**

**bounds** Returns the log-transformed bounds on the theta.

hyperparameter\_length\_scale

hyperparameter\_periodicity

hyperparameters Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

#### **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel $k(X, Y)$ and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
set_params(self, \*\*params)	Set the parameters of this kernel.

 $\_$ **call** $\_$  (self, X, Y=None,  $eval\_gradient$ =False)

Return the kernel k(X, Y) and optionally its gradient.

### **Parameters**

- **X** [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)
- **Y** [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

### Returns

**K** [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

#### bounds

Returns the log-transformed bounds on the theta.

#### Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

### clone\_with\_theta (self, theta)

Returns a clone of self with given hyperparameters theta.

### **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

#### diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

#### **Parameters**

**X** [array, shape (n samples X, n features)] Left argument of the returned kernel k(X, Y)

#### Returns

**K\_diag** [array, shape  $(n_samples_X)$ ] Diagonal of kernel k(X, X)

### get\_params (self, deep=True)

Get parameters of this kernel.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### hyperparameters

Returns a list of all hyperparameter specifications.

### is stationary (self)

Returns whether the kernel is stationary.

### n\_dims

Returns the number of non-fixed hyperparameters of the kernel.

# set\_params (self, \*\*params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

#### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

#### Returns

theta [array, shape (n dims,)] The non-fixed, log-transformed hyperparameters of the kernel

# Examples using sklearn.gaussian\_process.kernels.ExpSineSquared

- · Comparison of kernel ridge and Gaussian process regression
- Illustration of prior and posterior Gaussian process for different kernels
- Gaussian process regression (GPR) on Mauna Loa CO2 data.

# 6.17.7 sklearn.gaussian\_process.kernels.Exponentiation

The resulting kernel is defined as  $k_{exp}(X, Y) = k(X, Y) ** exponent$ 

New in version 0.18.

### **Parameters**

**kernel** [Kernel object] The base kernel

**exponent** [float] The exponent for the base kernel

### **Attributes**

**bounds** Returns the log-transformed bounds on the theta.

hyperparameters Returns a list of all hyperparameter.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

### **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel k(X, Y) and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
set_params(self, \*\*params)	Set the parameters of this kernel.

```
__init__ (self, kernel, exponent)
```

**\_\_call\_\_** (*self*, *X*, *Y*=*None*, *eval\_gradient*=*False*)

Return the kernel k(X, Y) and optionally its gradient.

### **Parameters**

- ${f X}$  [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)
- **Y** [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined.

#### Returns

**K** [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

#### bounds

Returns the log-transformed bounds on the theta.

#### Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

### clone with theta(self, theta)

Returns a clone of self with given hyperparameters theta.

#### **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

### diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

### **Parameters**

 $\mathbf{X}$  [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

### Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

# get\_params (self, deep=True)

Get parameters of this kernel.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

#### hyperparameters

Returns a list of all hyperparameter.

### is\_stationary(self)

Returns whether the kernel is stationary.

#### n dims

Returns the number of non-fixed hyperparameters of the kernel.

```
set_params (self, **params)
```

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

#### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

## Returns

theta [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

## 6.17.8 sklearn.gaussian\_process.kernels.Hyperparameter

```
class sklearn.gaussian_process.kernels.Hyperparameter
```

A kernel hyperparameter's specification in form of a namedtuple.

New in version 0.18.

## **Attributes**

```
name [string] Alias for field number 0
value_type [string] Alias for field number 1
bounds [pair of floats >= 0 or "fixed"] Alias for field number 2
n_elements [int, default=1] Alias for field number 3
fixed [bool, default: None] Alias for field number 4
```

## **Methods**

# count() index()

Raises ValueError if the value is not present.

Raises ValueError if the value is not present.

### n elements

Alias for field number 3

#### name

Alias for field number 0

## value\_type

Alias for field number 1

## 6.17.9 sklearn.gaussian\_process.kernels.Kernel

class sklearn.gaussian\_process.kernels.Kernel

Base class for all kernels.

New in version 0.18.

## Attributes

**bounds** Returns the log-transformed bounds on the theta.

hyperparameters Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

#### **Methods**

call(self, X[, Y, eval_gradient])	Evaluate the kernel.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
set_params(self, \*\*params)	Set the parameters of this kernel.

```
___init___(self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

\_\_call\_\_ (self, X, Y=None, eval\_gradient=False)

Evaluate the kernel.

### bounds

Returns the log-transformed bounds on the theta.

## Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

## clone\_with\_theta(self, theta)

Returns a clone of self with given hyperparameters theta.

## **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

## diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

## **Parameters**

 $\mathbf{X}$  [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

#### Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

## get\_params (self, deep=True)

Get parameters of this kernel.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## hyperparameters

Returns a list of all hyperparameter specifications.

## is\_stationary(self)

Returns whether the kernel is stationary.

### n dims

Returns the number of non-fixed hyperparameters of the kernel.

## set\_params (self, \*\*params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

## Returns

theta [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

## 6.17.10 sklearn.gaussian\_process.kernels.Matern

```
class sklearn.gaussian_process.kernels.Matern (length\_scale=1.0, length\_scale\_bounds=(1e-05, 100000.0), nu=1.5)
```

Matern kernel.

The class of Matern kernels is a generalization of the RBF and the absolute exponential kernel parameterized by an additional parameter nu. The smaller nu, the less smooth the approximated function is. For nu=inf, the kernel

becomes equivalent to the RBF kernel and for nu=0.5 to the absolute exponential kernel. Important intermediate values are nu=1.5 (once differentiable functions) and nu=2.5 (twice differentiable functions).

See Rasmussen and Williams 2006, pp84 for details regarding the different variants of the Matern kernel.

New in version 0.18.

## **Parameters**

**length\_scale** [float or array with shape (n\_features,), default: 1.0] The length scale of the kernel. If a float, an isotropic kernel is used. If an array, an anisotropic kernel is used where each dimension of l defines the length-scale of the respective feature dimension.

**length\_scale\_bounds** [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on length\_scale

nu [float, default: 1.5] The parameter nu controlling the smoothness of the learned function. The smaller nu, the less smooth the approximated function is. For nu=inf, the kernel becomes equivalent to the RBF kernel and for nu=0.5 to the absolute exponential kernel. Important intermediate values are nu=1.5 (once differentiable functions) and nu=2.5 (twice differentiable functions). Note that values of nu not in [0.5, 1.5, 2.5, inf] incur a considerably higher computational cost (appr. 10 times higher) since they require to evaluate the modified Bessel function. Furthermore, in contrast to l, nu is kept fixed to its initial value and not optimized.

## Attributes

## anisotropic

**bounds** Returns the log-transformed bounds on the theta.

## hyperparameter\_length\_scale

hyperparameters Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

## **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel $k(X, Y)$ and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this kernel.

**\_\_init\_\_**(self, length\_scale=1.0, length\_scale\_bounds=(1e-05, 100000.0), nu=1.5)

**\_\_call\_\_**(*self*, *X*, *Y=None*, *eval\_gradient=False*)

Return the kernel k(X, Y) and optionally its gradient.

## **Parameters**

X [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

**Y** [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

#### Returns

**K** [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

### bounds

Returns the log-transformed bounds on the theta.

#### Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

## clone\_with\_theta (self, theta)

Returns a clone of self with given hyperparameters theta.

#### **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

## diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

### **Parameters**

X [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

## Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

### get\_params (self, deep=True)

Get parameters of this kernel.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### hyperparameters

Returns a list of all hyperparameter specifications.

## is\_stationary(self)

Returns whether the kernel is stationary.

#### n dims

Returns the number of non-fixed hyperparameters of the kernel.

## set\_params (self, \*\*params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

#### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

### **Returns**

theta [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

## Examples using sklearn.gaussian\_process.kernels.Matern

• Illustration of prior and posterior Gaussian process for different kernels

## 6.17.11 sklearn.gaussian\_process.kernels.PairwiseKernel

Wrapper for kernels in sklearn.metrics.pairwise.

A thin wrapper around the functionality of the kernels in sklearn.metrics.pairwise.

**Note:** Evaluation of eval\_gradient is not analytic but numeric and all kernels support only isotropic distances. The parameter gamma is considered to be a hyperparameter and may be optimized. The other kernel parameters are set directly at initialization and are kept fixed.

New in version 0.18.

## **Parameters**

gamma [float >= 0, default: 1.0] Parameter gamma of the pairwise kernel specified by metric

**gamma\_bounds** [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on gamma

metric [string, or callable, default: "linear"] The metric to use when calculating kernel between instances in a feature array. If metric is a string, it must be one of the metrics in pairwise.PAIRWISE\_KERNEL\_FUNCTIONS. If metric is "precomputed", X is assumed to be a kernel matrix. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them.

**pairwise\_kernels\_kwargs** [dict, default: None] All entries of this dict (if any) are passed as keyword arguments to the pairwise kernel function.

## Attributes

**bounds** Returns the log-transformed bounds on the theta.

## hyperparameter\_gamma

hyperparameters Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

## **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel $k(X, Y)$ and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
set_params(self, \*\*params)	Set the parameters of this kernel.

\_\_init\_\_(self, gamma=1.0, gamma\_bounds=(1e-05, 100000.0), metric='linear', pair-wise\_kernels\_kwargs=None)

\_\_call\_\_ (self, X, Y=None, eval\_gradient=False)

Return the kernel k(X, Y) and optionally its gradient.

#### **Parameters**

- $\mathbf{X}$  [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)
- Y [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

## Returns

**K** [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval gradient is True.

### bounds

Returns the log-transformed bounds on the theta.

## Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

## clone\_with\_theta (self, theta)

Returns a clone of self with given hyperparameters theta.

## **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

## diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

## **Parameters**

 $\mathbf{X}$  [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

### Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

## get\_params (self, deep=True)

Get parameters of this kernel.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

## hyperparameters

Returns a list of all hyperparameter specifications.

## is\_stationary(self)

Returns whether the kernel is stationary.

#### n dims

Returns the number of non-fixed hyperparameters of the kernel.

## set\_params (self, \*\*params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

## Returns

**theta** [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

## 6.17.12 sklearn.gaussian\_process.kernels.Product

```
class sklearn.gaussian_process.kernels.Product (k1, k2)
```

Product-kernel k1 \* k2 of two kernels k1 and k2.

The resulting kernel is defined as  $k_prod(X, Y) = k1(X, Y) * k2(X, Y)$ 

New in version 0.18.

## **Parameters**

- **k1** [Kernel object] The first base-kernel of the product-kernel
- **k2** [Kernel object] The second base-kernel of the product-kernel

## **Attributes**

bounds Returns the log-transformed bounds on the theta.

hyperparameters Returns a list of all hyperparameter.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

## **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel $k(X, Y)$ and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this kernel.

\_\_\_init\_\_\_(self, k1, k2)

 $\_$ **call** $\_$  (self, X, Y=None, eval\_gradient=False)

Return the kernel k(X, Y) and optionally its gradient.

#### **Parameters**

- $\mathbf{X}$  [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)
- **Y** [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined.

## Returns

**K** [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

## bounds

Returns the log-transformed bounds on the theta.

## Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

## clone\_with\_theta (self, theta)

Returns a clone of self with given hyperparameters theta.

## **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

## diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

#### **Parameters**

 $\mathbf{X}$  [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

#### Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

## get\_params (self, deep=True)

Get parameters of this kernel.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

### hyperparameters

Returns a list of all hyperparameter.

## is\_stationary(self)

Returns whether the kernel is stationary.

#### n dims

Returns the number of non-fixed hyperparameters of the kernel.

## set\_params (self, \*\*params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

## Returns

**theta** [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

## 6.17.13 sklearn.gaussian\_process.kernels.RBF

Radial-basis function kernel (aka squared-exponential kernel).

The RBF kernel is a stationary kernel. It is also known as the "squared exponential" kernel. It is parameterized by a length-scale parameter length\_scale>0, which can either be a scalar (isotropic variant of the kernel) or a vector with the same number of dimensions as the inputs X (anisotropic variant of the kernel). The kernel is given by:

```
k(x_i, x_j) = \exp(-1/2 d(x_i/length_scale, x_j/length_scale)^2)
```

This kernel is infinitely differentiable, which implies that GPs with this kernel as covariance function have mean square derivatives of all orders, and are thus very smooth.

New in version 0.18.

#### **Parameters**

**length\_scale** [float or array with shape (n\_features,), default: 1.0] The length scale of the kernel. If a float, an isotropic kernel is used. If an array, an anisotropic kernel is used where each dimension of l defines the length-scale of the respective feature dimension.

**length\_scale\_bounds** [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on length\_scale

#### Attributes

## anisotropic

**bounds** Returns the log-transformed bounds on the theta.

## hyperparameter\_length\_scale

hyperparameters Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

## **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel k(X, Y) and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this kernel.

**\_\_\_init\_\_** (self, length\_scale=1.0, length\_scale\_bounds=(1e-05, 100000.0))

**call** (self, X, Y=None, eval gradient=False)

Return the kernel k(X, Y) and optionally its gradient.

## **Parameters**

- X [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)
- Y [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

## Returns

 ${f K}$  [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

## bounds

Returns the log-transformed bounds on the theta.

#### Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

## clone\_with\_theta (self, theta)

Returns a clone of self with given hyperparameters theta.

#### **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

## diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

#### **Parameters**

X [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

### Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

### get\_params (self, deep=True)

Get parameters of this kernel.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

## hyperparameters

Returns a list of all hyperparameter specifications.

## is\_stationary(self)

Returns whether the kernel is stationary.

### n\_dims

Returns the number of non-fixed hyperparameters of the kernel.

## set\_params (self, \*\*params)

Set the parameters of this kernel.

#### Returns

self

## theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

## Returns

theta [array, shape (n dims,)] The non-fixed, log-transformed hyperparameters of the kernel

## Examples using sklearn.gaussian\_process.kernels.RBF

- Plot classification probability
- Classifier comparison
- Illustration of Gaussian process classification (GPC) on the XOR dataset
- Gaussian process classification (GPC) on iris dataset
- Illustration of prior and posterior Gaussian process for different kernels
- Probabilistic predictions with Gaussian process classification (GPC)
- Gaussian process regression (GPR) with noise-level estimation
- Gaussian Processes regression: basic introductory example
- Gaussian process regression (GPR) on Mauna Loa CO2 data.

## 6.17.14 sklearn.gaussian\_process.kernels.RationalQuadratic

```
 \begin{array}{ll} \textbf{class} \; \texttt{sklearn.gaussian\_process.kernels.RationalQuadratic} \; (\textit{length\_scale=1.0}, \\ & \textit{alpha=1.0}, \\ & \textit{length\_scale\_bounds=(1e-05, \\ & \textit{alpha\_bounds=(1e-05, \\ 100000.0)}) \end{array}
```

Rational Quadratic kernel.

The RationalQuadratic kernel can be seen as a scale mixture (an infinite sum) of RBF kernels with different characteristic length-scales. It is parameterized by a length-scale parameter length\_scale>0 and a scale mixture parameter alpha>0. Only the isotropic variant where length\_scale is a scalar is supported at the moment. The kernel given by:

```
k(x_i, x_j) = (1 + d(x_i, x_j)^2 / (2*alpha * length_scale^2))^--alpha New in version 0.18.
```

## **Parameters**

```
length_scale [float > 0, default: 1.0] The length scale of the kernel.
```

**alpha** [float > 0, default: 1.0] Scale mixture parameter

**length\_scale\_bounds** [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on length\_scale

**alpha\_bounds** [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on alpha

## Attributes

**bounds** Returns the log-transformed bounds on the theta.

hyperparameter\_alpha

hyperparameter\_length\_scale

hyperparameters Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

## **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel $k(X, Y)$ and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
set_params(self, \*\*params)	Set the parameters of this kernel.

 $\_$ call $\_$  (self, X, Y=None,  $eval\_gradient$ =False)

Return the kernel k(X, Y) and optionally its gradient.

## **Parameters**

- $\boldsymbol{X} \; \left[ \text{array, shape (n\_samples\_X, n\_features)} \right] \; \text{Left argument of the returned kernel k}(X, \, Y)$
- **Y** [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

#### Returns

**K** [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

## bounds

Returns the log-transformed bounds on the theta.

#### Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

## clone\_with\_theta (self, theta)

Returns a clone of self with given hyperparameters theta.

## **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

## diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

## **Parameters**

X [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

## Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

### get\_params (self, deep=True)

Get parameters of this kernel.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

## hyperparameters

Returns a list of all hyperparameter specifications.

## is\_stationary(self)

Returns whether the kernel is stationary.

#### n dims

Returns the number of non-fixed hyperparameters of the kernel.

```
set params (self, **params)
```

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

#### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

#### Returns

**theta** [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

## Examples using sklearn.gaussian\_process.kernels.RationalQuadratic

- Illustration of prior and posterior Gaussian process for different kernels
- Gaussian process regression (GPR) on Mauna Loa CO2 data.

## 6.17.15 sklearn.gaussian\_process.kernels.Sum

```
class sklearn.gaussian_process.kernels.Sum (k1, k2)
```

Sum-kernel k1 + k2 of two kernels k1 and k2.

The resulting kernel is defined as  $k_{sum}(X, Y) = k1(X, Y) + k2(X, Y)$ 

New in version 0.18.

## **Parameters**

- **k1** [Kernel object] The first base-kernel of the sum-kernel
- **k2** [Kernel object] The second base-kernel of the sum-kernel

### **Attributes**

**bounds** Returns the log-transformed bounds on the theta.

hyperparameters Returns a list of all hyperparameter.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

### **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel k(X, Y) and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
set_params(self, \*\*params)	Set the parameters of this kernel.

\_\_\_init\_\_\_(self, k1, k2)

\_\_call\_\_(self, X, Y=None, eval\_gradient=False)

Return the kernel k(X, Y) and optionally its gradient.

## **Parameters**

 $\mathbf{X}$  [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

**Y** [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined.

## **Returns**

**K** [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

#### bounds

Returns the log-transformed bounds on the theta.

## Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

## clone\_with\_theta (self, theta)

Returns a clone of self with given hyperparameters theta.

## **Parameters**

**theta** [array, shape (n\_dims,)] The hyperparameters

## diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

#### **Parameters**

 $\mathbf{X}$  [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

### Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

## get\_params (self, deep=True)

Get parameters of this kernel.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

**params** [mapping of string to any] Parameter names mapped to their values.

## hyperparameters

Returns a list of all hyperparameter.

## is\_stationary(self)

Returns whether the kernel is stationary.

#### n dims

Returns the number of non-fixed hyperparameters of the kernel.

## set\_params (self, \*\*params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

### Returns

theta [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

## 6.17.16 sklearn.gaussian\_process.kernels.WhiteKernel

White kernel.

The main use-case of this kernel is as part of a sum-kernel where it explains the noise-component of the signal. Tuning its parameter corresponds to estimating the noise-level.

```
k(x_1, x_2) = noise_level if x_1 == x_2 else 0
```

New in version 0.18.

#### **Parameters**

noise\_level [float, default: 1.0] Parameter controlling the noise level

**noise\_level\_bounds** [pair of floats >= 0, default: (1e-5, 1e5)] The lower and upper bound on noise\_level

### **Attributes**

**bounds** Returns the log-transformed bounds on the theta.

## hyperparameter\_noise\_level

**hyperparameters** Returns a list of all hyperparameter specifications.

**n\_dims** Returns the number of non-fixed hyperparameters of the kernel.

theta Returns the (flattened, log-transformed) non-fixed hyperparameters.

#### **Methods**

call(self, X[, Y, eval_gradient])	Return the kernel k(X, Y) and optionally its gradient.
clone_with_theta(self, theta)	Returns a clone of self with given hyperparameters
	theta.
diag(self, X)	Returns the diagonal of the kernel $k(X, X)$ .
<pre>get_params(self[, deep])</pre>	Get parameters of this kernel.
is_stationary(self)	Returns whether the kernel is stationary.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this kernel.

```
__init__ (self, noise_level=1.0, noise_level_bounds=(1e-05, 100000.0))
```

**\_\_call\_\_**(*self*, *X*, *Y=None*, *eval\_gradient=False*)

Return the kernel k(X, Y) and optionally its gradient.

## Parameters

- X [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)
- $\mathbf{Y}$  [array, shape (n\_samples\_Y, n\_features), (optional, default=None)] Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

**eval\_gradient** [bool (optional, default=False)] Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

## Returns

**K** [array, shape (n\_samples\_X, n\_samples\_Y)] Kernel k(X, Y)

**K\_gradient** [array (opt.), shape (n\_samples\_X, n\_samples\_X, n\_dims)] The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval\_gradient is True.

## bounds

Returns the log-transformed bounds on the theta.

## Returns

**bounds** [array, shape (n\_dims, 2)] The log-transformed bounds on the kernel's hyperparameters theta

### clone with theta (self, theta)

Returns a clone of self with given hyperparameters theta.

#### **Parameters**

theta [array, shape (n\_dims,)] The hyperparameters

#### diag(self, X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

### **Parameters**

**X** [array, shape (n\_samples\_X, n\_features)] Left argument of the returned kernel k(X, Y)

## Returns

**K\_diag** [array, shape (n\_samples\_X,)] Diagonal of kernel k(X, X)

## get\_params (self, deep=True)

Get parameters of this kernel.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## hyperparameters

Returns a list of all hyperparameter specifications.

## is\_stationary(self)

Returns whether the kernel is stationary.

#### n dims

Returns the number of non-fixed hyperparameters of the kernel.

## set\_params (self, \*\*params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

### theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

#### Returns

theta [array, shape (n\_dims,)] The non-fixed, log-transformed hyperparameters of the kernel

## Examples using sklearn.gaussian\_process.kernels.WhiteKernel

- Comparison of kernel ridge and Gaussian process regression
- Gaussian process regression (GPR) with noise-level estimation
- Gaussian process regression (GPR) on Mauna Loa CO2 data.

## 6.18 sklearn.isotonic: Isotonic regression

**User guide:** See the *Isotonic regression* section for further details.

```
isotonic.IsotonicRegression([y_min, y_max, Isotonic regression model.
...])
```

## 6.18.1 sklearn.isotonic.lsotonicRegression

Isotonic regression model.

The isotonic regression optimization problem is defined by:

```
min sum w_i (y[i] - y_[i]) ** 2
subject to y_[i] <= y_[j] whenever X[i] <= X[j]
and min(y_) = y_min, max(y_) = y_max</pre>
```

#### where:

- y[i] are inputs (real numbers)
- y\_[i] are fitted
- X specifies the order. If X is non-decreasing then y\_ is non-decreasing.
- w[i] are optional strictly positive weights (default to 1.0)

Read more in the User Guide.

## **Parameters**

**y\_min** [optional, default: None] If not None, set the lowest value of the fit to y\_min.

**y\_max** [optional, default: None] If not None, set the highest value of the fit to y\_max.

**increasing** [boolean or string, optional, default: True] If boolean, whether or not to fit the isotonic regression with y increasing or decreasing.

The string value "auto" determines whether y should increase or decrease based on the Spearman correlation estimate's sign.

out\_of\_bounds [string, optional, default: "nan"] The out\_of\_bounds parameter handles how x-values outside of the training domain are handled. When set to "nan", predicted y-values will be NaN. When set to "clip", predicted y-values will be set to the value corresponding to the nearest train interval endpoint. When set to "raise", allow interpld to throw ValueError.

### **Attributes**

**X\_min\_** [float] Minimum value of input array X\_ for left bound.

**X\_max**\_ [float] Maximum value of input array X\_ for right bound.

**f**\_ [function] The stepwise interpolating function that covers the input domain X.

### **Notes**

Ties are broken using the secondary method from Leeuw, 1977.

### References

Isotonic Median Regression: A Linear Programming Approach Nilotpal Chakravarti Mathematics of Operations Research Vol. 14, No. 2 (May, 1989), pp. 303-308

Isotone Optimization in R: Pool-Adjacent-Violators Algorithm (PAVA) and Active Set Methods Leeuw, Hornik, Mair Journal of Statistical Software 2009

Correctness of Kruskal's algorithms for monotone regression with ties Leeuw, Psychometrica, 1977

## **Examples**

```
>>> from sklearn.datasets import make_regression
>>> from sklearn.isotonic import IsotonicRegression
>>> X, y = make_regression(n_samples=10, n_features=1, random_state=41)
>>> iso_reg = IsotonicRegression().fit(X.flatten(), y)
>>> iso_reg.predict([.1, .2])
array([1.8628..., 3.7256...])
```

## **Methods**

fit(self, X, y[, sample_weight])	Fit the model using X, y as training data.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, T)	Predict new data by linear interpolation.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R <sup>2</sup> of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, T)	Transform new data by linear interpolation

```
__init__ (self, y_min=None, y_max=None, increasing=True, out_of_bounds='nan')

fit (self, X, y, sample_weight=None)

Fit the model using X, y as training data.
```

## **Parameters**

**X** [array-like, shape=(n\_samples,)] Training data.

**y** [array-like, shape=(n\_samples,)] Training target.

**sample\_weight** [array-like, shape=(n\_samples,), optional, default: None] Weights. If set to None, all weights will be set to 1 (equal weights).

#### Returns

self [object] Returns an instance of self.

### **Notes**

X is stored for future use, as transform needs X to interpolate new input data.

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

## **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, T)

Predict new data by linear interpolation.

## **Parameters**

**T** [array-like, shape=(n\_samples,)] Data to transform.

#### Returns

**T**\_ [array, shape=(n\_samples,)] Transformed data.

```
score (self, X, y, sample weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### **Returns**

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## transform(self, T)

Transform new data by linear interpolation

### **Parameters**

**T** [array-like, shape=(n\_samples,)] Data to transform.

#### Returns

**T**\_ [array, shape=(n\_samples,)] The transformed data

## Examples using sklearn.isotonic.IsotonicRegression

• Isotonic Regression

isotonic.check_increasing(x, y)	Determine whether y is monotonically correlated with x.
$isotonic.isotonic\_regression(y[,])$	Solve the isotonic regression model:

## 6.18.2 sklearn.isotonic.check\_increasing

```
sklearn.isotonic.check_increasing(x, y)
```

Determine whether y is monotonically correlated with x.

y is found increasing or decreasing with respect to x based on a Spearman correlation test.

## **Parameters**

- **x** [array-like, shape=(n\_samples,)] Training data.
- y [array-like, shape=(n\_samples,)] Training target.

### Returns

**increasing\_bool** [boolean] Whether the relationship is increasing or decreasing.

### **Notes**

The Spearman correlation coefficient is estimated from the data, and the sign of the resulting estimate is used as the result.

In the event that the 95% confidence interval based on Fisher transform spans zero, a warning is raised.

#### References

Fisher transformation. Wikipedia. https://en.wikipedia.org/wiki/Fisher\_transformation

## 6.18.3 sklearn.isotonic.isotonic\_regression

sklearn.isotonic\_regression(y, sample\_weight=None, y\_min=None, y\_max=None, increasing=True)

Solve the isotonic regression model:

```
min sum w[i] (y[i] - y_[i]) ** 2
subject to y_min = y_[1] <= y_[2] ... <= y_[n] = y_max
```

### where:

- y[i] are inputs (real numbers)
- y\_[i] are fitted
- w[i] are optional strictly positive weights (default to 1.0)

Read more in the *User Guide*.

## **Parameters**

y [iterable of floats] The data.

**sample\_weight** [iterable of floats, optional, default: None] Weights on each point of the regression. If None, weight is set to 1 (equal weights).

**y\_min** [optional, default: None] If not None, set the lowest value of the fit to y\_min.

y\_max [optional, default: None] If not None, set the highest value of the fit to y\_max.

**increasing** [boolean, optional, default: True] Whether to compute y\_ is increasing (if set to True) or decreasing (if set to False)

#### Returns

y\_ [list of floats] Isotonic fit of y.

## References

"Active set algorithms for isotonic regression; A unifying framework" by Michael J. Best and Nilotpal Chakravarti, section 3.

## 6.19 sklearn.impute: Impute

Transformers for missing value imputation

**User guide:** See the *Imputation of missing values* section for further details.

<pre>impute.SimpleImputer([missing_values,])</pre>	Imputation transformer for completing missing values.
<pre>impute.IterativeImputer([estimator,])</pre>	Multivariate imputer that estimates each feature from all
	the others.
<pre>impute.MissingIndicator([missing_values,])</pre>	Binary indicators for missing values.

## 6.19.1 sklearn.impute.SimpleImputer

class sklearn.impute.SimpleImputer (missing\_values=nan, strategy='mean', fill\_value=None, verbose=0, copy=True, add\_indicator=False)

Imputation transformer for completing missing values.

Read more in the User Guide.

#### **Parameters**

missing\_values [number, string, np.nan (default) or None] The placeholder for the missing values. All occurrences of missing\_values will be imputed.

strategy [string, optional (default="mean")] The imputation strategy.

- If "mean", then replace missing values using the mean along each column. Can only be used with numeric data.
- If "median", then replace missing values using the median along each column. Can only be used with numeric data.
- If "most\_frequent", then replace missing using the most frequent value along each column. Can be used with strings or numeric data.
- If "constant", then replace missing values with fill\_value. Can be used with strings or numeric data.

New in version 0.20: strategy="constant" for fixed value imputation.

**fill\_value** [string or numerical value, optional (default=None)] When strategy == "constant", fill\_value is used to replace all occurrences of missing\_values. If left to the default, fill\_value will be 0 when imputing numerical data and "missing\_value" for strings or object data types.

**verbose** [integer, optional (default=0)] Controls the verbosity of the imputer.

- **copy** [boolean, optional (default=True)] If True, a copy of X will be created. If False, imputation will be done in-place whenever possible. Note that, in the following cases, a new copy will always be made, even if copy=False:
  - If X is not an array of floating values;
  - If X is encoded as a CSR matrix;
  - If add indicator=True.

add\_indicator [boolean, optional (default=False)] If True, a MissingIndicator transform will stack onto output of the imputer's transform. This allows a predictive estimator to account for missingness despite imputation. If a feature has no missing values at fit/train

time, the feature won't appear on the missing indicator even if there are missing values at transform/test time.

#### **Attributes**

**statistics**\_ [array of shape (n\_features,)] The imputation fill value for each feature.

**indicator**\_ [sklearn.impute.MissingIndicator] Indicator used to add binary indicators for missing values. None if add\_indicator is False.

#### See also:

IterativeImputer Multivariate imputation of missing values.

### **Notes**

Columns which only contained missing values at fit are discarded upon transform if strategy is not "constant".

## **Examples**

### Methods

fit(self, X[, y])	Fit the imputer on X.
$fit_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Impute all missing values in X.

```
__init__(self, missing_values=nan, strategy='mean', fill_value=None, verbose=0, copy=True, add_indicator=False)
```

```
fit (self, X, y=None)
```

Fit the imputer on X.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Input data, where n\_samples is the number of samples and n\_features is the number of features.

## **Returns**

**self** [SimpleImputer]

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

## transform(self, X)

Impute all missing values in X.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data to complete.

## Examples using sklearn.impute.SimpleImputer

- Column Transformer with Mixed Types
- Imputing missing values with variants of IterativeImputer
- Imputing missing values before building an estimator

## 6.19.2 sklearn.impute.lterativelmputer

Multivariate imputer that estimates each feature from all the others.

A strategy for imputing missing values by modeling each feature with missing values as a function of other features in a round-robin fashion.

Read more in the User Guide.

**Note:** This estimator is still **experimental** for now: the predictions and the API might change without any deprecation cycle. To use it, you need to explicitly import enable\_iterative\_imputer:

```
>>> # explicitly require this experimental feature
>>> from sklearn.experimental import enable_iterative_imputer # noqa
>>> # now you can import normally from sklearn.impute
>>> from sklearn.impute import IterativeImputer
```

#### **Parameters**

**estimator** [estimator object, default=BayesianRidge()] The estimator to use at each step of the round-robin imputation. If sample\_posterior is True, the estimator must support return\_std in its predict method.

**missing\_values** [int, np.nan, optional (default=np.nan)] The placeholder for the missing values. All occurrences of missing\_values will be imputed.

**sample\_posterior** [boolean, default=False] Whether to sample from the (Gaussian) predictive posterior of the fitted estimator for each imputation. Estimator must support return\_std in its predict method if set to True. Set to True if using IterativeImputer for multiple imputations.

<code>max\_iter</code> [int, optional (default=10)] Maximum number of imputation rounds to perform before returning the imputations computed during the final round. A round is a single imputation of each feature with missing values. The stopping criterion is met once  $abs(max(X_t - X_{t-1}))/abs(max(X[known_vals])) < tol, where X_t is X at iteration t. Note that early stopping is only applied if ``sample_posterior=False`.$ 

tol [float, optional (default=1e-3)] Tolerance of the stopping condition.

n\_nearest\_features [int, optional (default=None)] Number of other features to use to estimate the missing values of each feature column. Nearness between features is measured using the absolute correlation coefficient between each feature pair (after initial imputation). To ensure coverage of features throughout the imputation process, the neighbor features are not necessarily nearest, but are drawn with probability proportional to correlation for each imputed target feature. Can provide significant speed-up when the number of features is huge. If None, all features will be used.

initial\_strategy [str, optional (default="mean")] Which strategy to use to initialize the missing
 values. Same as the strategy parameter in sklearn.impute.SimpleImputer
 Valid values: {"mean", "median", "most\_frequent", or "constant"}.

- **imputation\_order** [str, optional (default="ascending")] The order in which the features will be imputed. Possible values:
  - "ascending" From features with fewest missing values to most.
  - "descending" From features with most missing values to fewest.
  - "roman" Left to right.
  - "arabic" Right to left.
  - "random" A random order for each round.
- **min\_value** [float, optional (default=None)] Minimum possible imputed value. Default of None will set minimum to negative infinity.
- **max\_value** [float, optional (default=None)] Maximum possible imputed value. Default of None will set maximum to positive infinity.
- **verbose** [int, optional (default=0)] Verbosity flag, controls the debug messages that are issued as functions are evaluated. The higher, the more verbose. Can be 0, 1, or 2.
- random\_state [int, RandomState instance or None, optional (default=None)] The seed of the
   pseudo random number generator to use. Randomizes selection of estimator features if
   n\_nearest\_features is not None, the imputation\_order if random, and the sampling
   from posterior if sample\_posterior is True. Use an integer for determinism. See the
   Glossary.
- **add\_indicator** [boolean, optional (default=False)] If True, a <code>MissingIndicator</code> transform will stack onto output of the imputer's transform. This allows a predictive estimator to account for missingness despite imputation. If a feature has no missing values at fit/train time, the feature won't appear on the missing indicator even if there are missing values at transform/test time.

## **Attributes**

- initial\_imputer\_ [object of type sklearn.impute.SimpleImputer] Imputer used to initialize the missing values.
- imputation\_sequence\_ [list of tuples] Each tuple has (feat\_idx,
   neighbor\_feat\_idx, estimator), where feat\_idx is the current feature
  to be imputed, neighbor\_feat\_idx is the array of other features used to impute the
   current feature, and estimator is the trained estimator used for the imputation. Length
   is self.n\_features\_with\_missing\_ \* self.n\_iter\_.
- **n\_iter\_** [int] Number of iteration rounds that occurred. Will be less than self.max\_iter if early stopping criterion was reached.
- **n features with missing** [int] Number of features with missing values.
- **indicator**\_ [sklearn.impute.MissingIndicator] Indicator used to add binary indicators for missing values. None if add\_indicator is False.

## See also:

**SimpleImputer** Univariate imputation of missing values.

### **Notes**

To support imputation in inductive mode we store each feature's estimator during the fit phase, and predict without refitting (in order) during the transform phase.

Features which contain all missing values at fit are discarded upon transform.

Features with missing values during transform which did not have any missing values during fit will be imputed with the initial imputation method only.

#### References

[Rcd31b817a31e-1], [Rcd31b817a31e-2]

## **Methods**

fit(self, X[, y])	Fits the imputer on X and return self.
<pre>fit_transform(self, X[, y])</pre>	Fits the imputer on X and return the transformed X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Imputes all missing values in X.

```
__init__(self, estimator=None, missing_values=nan, sample_posterior=False, max_iter=10, tol=0.001, n_nearest_features=None, initial_strategy='mean', imputation_order='ascending', min_value=None, max_value=None, verbose=0, random_state=None, add_indicator=False)
```

**fit** (*self*, *X*, *y*=*None*)

Fits the imputer on X and return self.

### **Parameters**

- $\mathbf{X}$  [array-like, shape (n\_samples, n\_features)] Input data, where "n\_samples" is the number of samples and "n\_features" is the number of features.
- y [ignored]

## Returns

self [object] Returns self.

## fit\_transform(self, X, y=None)

Fits the imputer on X and return the transformed X.

### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Input data, where "n\_samples" is the number of samples and "n\_features" is the number of features.
- y [ignored.]

#### **Returns**

Xt [array-like, shape (n\_samples, n\_features)] The imputed input data.

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## **Returns**

params [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## transform(self, X)

Imputes all missing values in X.

Note that this is stochastic, and that if random\_state is not fixed, repeated calls, or permuted input, will yield different results.

### **Parameters**

 $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] The input data to complete.

#### Returns

**Xt** [array-like, shape (n\_samples, n\_features)] The imputed input data.

## Examples using sklearn.impute.IterativeImputer

- Imputing missing values with variants of IterativeImputer
- Imputing missing values before building an estimator

## 6.19.3 sklearn.impute.MissingIndicator

Binary indicators for missing values.

Note that this component typically should not be used in a vanilla Pipeline consisting of transformers and a classifier, but rather could be added using a FeatureUnion or ColumnTransformer.

Read more in the *User Guide*.

## **Parameters**

**missing\_values** [number, string, np.nan (default) or None] The placeholder for the missing values. All occurrences of missing\_values will be indicated (True in the output array), the other values will be marked as False.

**features** [str, optional] Whether the imputer mask should represent all or a subset of features.

- If "missing-only" (default), the imputer mask will only represent features containing missing values during fit time.
- If "all", the imputer mask will represent all features.

**sparse** [boolean or "auto", optional] Whether the imputer mask format should be sparse or dense.

- If "auto" (default), the imputer mask will be of same type as input.
- If True, the imputer mask will be a sparse matrix.

• If False, the imputer mask will be a numpy array.

**error\_on\_new** [boolean, optional] If True (default), transform will raise an error when there are features with missing values in transform that have no missing values in fit. This is applicable only when features="missing-only".

## **Attributes**

**features\_** [ndarray, shape (n\_missing\_features,) or (n\_features,)] The features indices which will be returned when calling transform. They are computed during fit. For features='all', it is to range (n\_features).

## **Examples**

```
>>> import numpy as np
>>> from sklearn.impute import MissingIndicator
>>> X1 = np.array([[np.nan, 1, 3],
                   [4, 0, np.nan],
                   [8, 1, 0]])
>>> X2 = np.array([[5, 1, np.nan],
                   [np.nan, 2, 3],
. . .
                   [2, 4, 0]])
. . .
>>> indicator = MissingIndicator()
>>> indicator.fit(X1)
MissingIndicator(error_on_new=True, features='missing-only',
         missing_values=nan, sparse='auto')
>>> X2_tr = indicator.transform(X2)
>>> X2_tr
array([[False, True],
       [ True, False],
       [False, False]])
```

## **Methods**

fit(self, X[, y])	Fit the transformer on X.
$fit\_transform(self, X[, y])$	Generate missing values indicator for X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Generate missing values indicator for X.

```
__init__(self, missing_values=nan, features='missing-only', sparse='auto', error_on_new=True)
```

### **fit** (self, X, y=None)

Fit the transformer on X.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Input data, where n\_samples is the number of samples and n\_features is the number of features.

### **Returns**

**self** [object] Returns self.

```
fit_transform(self, X, y=None)
```

Generate missing values indicator for X.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data to complete.

## Returns

**Xt** [{ndarray or sparse matrix}, shape (n\_samples, n\_features)] The missing indicator for input data. The data type of Xt will be boolean.

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### **Returns**

self

## transform(self, X)

Generate missing values indicator for X.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data to complete.

#### Returns

**Xt** [{ndarray or sparse matrix}, shape (n\_samples, n\_features)] The missing indicator for input data. The data type of Xt will be boolean.

## Examples using sklearn.impute.MissingIndicator

• Imputing missing values before building an estimator

## 6.20 sklearn.kernel\_approximation Kernel Approximation

The sklearn.kernel\_approximation module implements several approximate kernel feature maps base on Fourier transforms.

**User guide:** See the *Kernel Approximation* section for further details.

kernel_approximation.	Approximate feature map for additive chi2 kernel.
$AdditiveChi2Sampler([\dots])$	
kernel_approximation.Nystroem([kernel,])	Approximate a kernel map using a subset of the training
	data.
	Continued on next page

## Table 6.141 – continued from previous page

kernel_approximation.RBFSampler([gamma,	Approximates feature map of an RBF kernel by Monte
])	Carlo approximation of its Fourier transform.
kernel_approximation.	Approximates feature map of the "skewed chi-squared"
SkewedChi2Sampler([])	kernel by Monte Carlo approximation of its Fourier trans-
	form.

## 6.20.1 sklearn.kernel\_approximation.AdditiveChi2Sampler

Approximate feature map for additive chi2 kernel.

Uses sampling the fourier transform of the kernel characteristic at regular intervals.

Since the kernel that is to be approximated is additive, the components of the input vectors can be treated separately. Each entry in the original space is transformed into 2\*sample\_steps+1 features, where sample\_steps is a parameter of the method. Typical values of sample\_steps include 1, 2 and 3.

Optimal choices for the sampling interval for certain data ranges can be computed (see the reference). The default values should be reasonable.

Read more in the *User Guide*.

#### **Parameters**

**sample\_steps** [int, optional] Gives the number of (complex) sampling points.

**sample\_interval** [float, optional] Sampling interval. Must be specified when sample\_steps not in {1,2,3}.

### See also:

**SkewedChi2Sampler** A Fourier-approximation to a non-additive variant of the chi squared kernel.

sklearn.metrics.pairwise.chi2\_kernel The exact chi squared kernel.

sklearn.metrics.pairwise.additive\_chi2\_kernel The exact additive chi squared kernel.

## **Notes**

This estimator approximates a slightly different version of the additive chi squared kernel then metric. additive\_chi2 computes.

### References

See "Efficient additive kernels via explicit feature maps" A. Vedaldi and A. Zisserman, Pattern Analysis and Machine Intelligence, 2011

## **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.linear_model import SGDClassifier
>>> from sklearn.kernel_approximation import AdditiveChi2Sampler
>>> X, y = load_digits(return_X_y=True)
```

## **Methods**

fit(self, X[, y])	Set the parameters
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Apply approximate feature map to X.

```
__init__ (self, sample_steps=2, sample_interval=None)

fit (self, X, y=None)

Set the parameters
```

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples in the number of samples and n\_features is the number of features.

### **Returns**

self [object] Returns the transformer.

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

## Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## transform(self, X)

Apply approximate feature map to X.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape = (n\_samples, n\_features)]

### Returns

**X\_new** [{array, sparse matrix}, shape =  $(n_samples, n_features * (2*sample_steps + 1))]$  Whether the return value is an array of sparse matrix depends on the type of the input X.

## 6.20.2 sklearn.kernel\_approximation.Nystroem

```
 \begin{array}{ll} \textbf{class} \; \textbf{sklearn.kernel\_approximation.Nystroem} \; (\textit{kernel='rbf'}, & \textit{gamma=None}, & \textit{coef0=None}, \\ \textit{degree=None}, & \textit{kernel\_params=None}, \\ \textit{n\_components=100}, \textit{random\_state=None}) \end{array}
```

Approximate a kernel map using a subset of the training data.

Constructs an approximate feature map for an arbitrary kernel using a subset of the data as basis.

Read more in the User Guide.

#### **Parameters**

**kernel** [string or callable, default="rbf"] Kernel map to be approximated. A callable should accept two arguments and the keyword arguments passed to this object as kernel\_params, and should return a floating point number.

**gamma** [float, default=None] Gamma parameter for the RBF, laplacian, polynomial, exponential chi2 and sigmoid kernels. Interpretation of the default value is left to the kernel; see the documentation for sklearn.metrics.pairwise. Ignored by other kernels.

**coef0** [float, default=None] Zero coefficient for polynomial and sigmoid kernels. Ignored by other kernels.

degree [float, default=None] Degree of the polynomial kernel. Ignored by other kernels.

**kernel\_params** [mapping of string to any, optional] Additional parameters (keyword arguments) for kernel function passed as callable object.

**n\_components** [int] Number of features to construct. How many data points will be used to construct the mapping.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

## **Attributes**

**components**\_ [array, shape (n\_components, n\_features)] Subset of training points used to construct the feature map.

component\_indices\_ [array, shape (n\_components)] Indices of components\_ in the training
 set.

**normalization**\_ [array, shape (n\_components, n\_components)] Normalization matrix needed for embedding. Square root of the kernel matrix on components\_.

#### See also:

**RBFSampler** An approximation to the RBF kernel using random Fourier features.

sklearn.metrics.pairwise.kernel\_metrics List of built-in kernels.

## References

- Williams, C.K.I. and Seeger, M. "Using the Nystroem method to speed up kernel machines", Advances in neural information processing systems 2001
- T. Yang, Y. Li, M. Mahdavi, R. Jin and Z. Zhou "Nystroem Method vs Random Fourier Features: A Theoretical and Empirical Comparison", Advances in Neural Information Processing Systems 2012

# **Examples**

```
>>> from sklearn import datasets, svm
>>> from sklearn.kernel_approximation import Nystroem
>>> digits = datasets.load_digits(n_class=9)
>>> data = digits.data / 16.
>>> clf = svm.LinearSVC()
>>> feature_map_nystroem = Nystroem(gamma=.2,
                                    random_state=1,
                                    n_components=300)
. . .
>>> data_transformed = feature_map_nystroem.fit_transform(data)
>>> clf.fit(data_transformed, digits.target)
LinearSVC(C=1.0, class_weight=None, dual=True, fit_intercept=True,
     intercept_scaling=1, loss='squared_hinge', max_iter=1000,
     multi_class='ovr', penalty='12', random_state=None, tol=0.0001,
     verbose=0)
>>> clf.score(data_transformed, digits.target)
0.9987...
```

# Methods

fit(self, X[, y])	Fit estimator to data.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Apply feature map to X.

\_\_init\_\_(self, kernel='rbf', gamma=None, coef0=None, degree=None, kernel\_params=None, n\_components=100, random\_state=None)

### **fit** (self, X, y=None)

Fit estimator to data.

Samples a subset of training points, computes kernel on these and computes normalization matrix.

#### **Parameters**

**X** [array-like, shape=(n\_samples, n\_feature)] Training data.

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

## **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

## **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# transform(self, X)

Apply feature map to X.

Computes an approximate feature map using the kernel between some training points and X.

# **Parameters**

**X** [array-like, shape=(n\_samples, n\_features)] Data to transform.

## Returns

**X\_transformed** [array, shape=(n\_samples, n\_components)] Transformed data.

# Examples using sklearn.kernel\_approximation.Nystroem

• Explicit feature map approximation for RBF kernels

# 6.20.3 sklearn.kernel\_approximation.RBFSampler

Approximates feature map of an RBF kernel by Monte Carlo approximation of its Fourier transform.

It implements a variant of Random Kitchen Sinks.[1]

Read more in the User Guide.

#### **Parameters**

**gamma** [float] Parameter of RBF kernel: exp(-gamma \* x^2)

**n\_components** [int] Number of Monte Carlo samples per original feature. Equals the dimensionality of the computed feature space.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

### **Notes**

See "Random Features for Large-Scale Kernel Machines" by A. Rahimi and Benjamin Recht.

[1] "Weighted Sums of Random Kitchen Sinks: Replacing minimization with randomization in learning" by A. Rahimi and Benjamin Recht. (https://people.eecs.berkeley.edu/~brecht/papers/08.rah.rec.nips.pdf)

# **Examples**

```
>>> from sklearn.kernel_approximation import RBFSampler
>>> from sklearn.linear_model import SGDClassifier
>>> X = [[0, 0], [1, 1], [1, 0], [0, 1]]
>>> y = [0, 0, 1, 1]
>>> rbf feature = RBFSampler(gamma=1, random state=1)
>>> X_features = rbf_feature.fit_transform(X)
>>> clf = SGDClassifier(max_iter=5, tol=1e-3)
>>> clf.fit(X_features, y)
SGDClassifier(alpha=0.0001, average=False, class_weight=None,
       early_stopping=False, epsilon=0.1, eta0=0.0, fit_intercept=True,
       11_ratio=0.15, learning_rate='optimal', loss='hinge', max_iter=5,
      n_iter_no_change=5, n_jobs=None, penalty='12', power_t=0.5,
       random_state=None, shuffle=True, tol=0.001, validation_fraction=0.1,
       verbose=0, warm_start=False)
>>> clf.score(X_features, y)
1.0
```

## Methods

fit(self, X[, y])	Fit the model with X.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.

Continued on next page

Table 6.144 – continued from previous page

<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Apply the approximate feature map to X.

\_\_init\_\_ (self, gamma=1.0, n\_components=100, random\_state=None)

# **fit** (self, X, y=None)

Fit the model with X.

Samples random projection according to n\_features.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training data, where n\_samples in the number of samples and n\_features is the number of features.

#### Returns

self [object] Returns the transformer.

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# transform(self, X)

Apply the approximate feature map to X.

# **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] New data, where n\_samples in the number of samples and n\_features is the number of features.

## Returns

**X\_new** [array-like, shape (n\_samples, n\_components)]

# Examples using sklearn.kernel\_approximation.RBFSampler

• Explicit feature map approximation for RBF kernels

# 6.20.4 sklearn.kernel\_approximation.SkewedChi2Sampler

Approximates feature map of the "skewed chi-squared" kernel by Monte Carlo approximation of its Fourier transform.

Read more in the User Guide.

## **Parameters**

**skewedness** [float] "skewedness" parameter of the kernel. Needs to be cross-validated.

**n\_components** [int] number of Monte Carlo samples per original feature. Equals the dimensionality of the computed feature space.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

# See also:

**AdditiveChi2Sampler** A different approach for approximating an additive variant of the chi squared kernel.

**sklearn.metrics.pairwise.chi2\_kernel** The exact chi squared kernel.

# References

See "Random Fourier Approximations for Skewed Multiplicative Histogram Kernels" by Fuxin Li, Catalin Ionescu and Cristian Sminchisescu.

# **Examples**

## **Methods**

fit(self, X[, y])	Fit the model with X.
$fit_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Apply the approximate feature map to X.

```
__init__ (self, skewedness=1.0, n_components=100, random_state=None)
```

# fit (self, X, y=None)

Fit the model with X.

Samples random projection according to n\_features.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples in the number of samples and n\_features is the number of features.

## **Returns**

self [object] Returns the transformer.

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

# Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, X)

Apply the approximate feature map to X.

#### **Parameters**

X [array-like, shape (n\_samples, n\_features)] New data, where n\_samples in the number of samples and n\_features is the number of features. All values of X must be strictly greater than "-skewedness".

## **Returns**

**X\_new** [array-like, shape (n\_samples, n\_components)]

# 6.21 sklearn.kernel\_ridge Kernel Ridge Regression

Module <code>sklearn.kernel\_ridge</code> implements kernel ridge regression.

User guide: See the Kernel ridge regression section for further details.

kernel ridge.KernelRidge([alpha, kernel,...])

Kernel ridge regression.

# 6.21.1 sklearn.kernel\_ridge.KernelRidge

Kernel ridge regression.

Kernel ridge regression (KRR) combines ridge regression (linear least squares with 12-norm regularization) with the kernel trick. It thus learns a linear function in the space induced by the respective kernel and the data. For non-linear kernels, this corresponds to a non-linear function in the original space.

The form of the model learned by KRR is identical to support vector regression (SVR). However, different loss functions are used: KRR uses squared error loss while support vector regression uses epsilon-insensitive loss, both combined with 12 regularization. In contrast to SVR, fitting a KRR model can be done in closed-form and is typically faster for medium-sized datasets. On the other hand, the learned model is non-sparse and thus slower than SVR, which learns a sparse model for epsilon > 0, at prediction-time.

This estimator has built-in support for multi-variate regression (i.e., when y is a 2d-array of shape [n\_samples, n\_targets]).

Read more in the *User Guide*.

# **Parameters**

**alpha** [{float, array-like}, shape =  $[n_{targets}]$ ] Small positive values of alpha improve the conditioning of the problem and reduce the variance of the estimates. Alpha corresponds to  $(2 \times C)^{-1}$  in other linear models such as LogisticRegression or LinearSVC. If an array is

passed, penalties are assumed to be specific to the targets. Hence they must correspond in number.

**kernel** [string or callable, default="linear"] Kernel mapping used internally. A callable should accept two arguments and the keyword arguments passed to this object as kernel\_params, and should return a floating point number. Set to "precomputed" in order to pass a precomputed kernel matrix to the estimator methods instead of samples.

**gamma** [float, default=None] Gamma parameter for the RBF, laplacian, polynomial, exponential chi2 and sigmoid kernels. Interpretation of the default value is left to the kernel; see the documentation for sklearn.metrics.pairwise. Ignored by other kernels.

degree [float, default=3] Degree of the polynomial kernel. Ignored by other kernels.

coef0 [float, default=1] Zero coefficient for polynomial and sigmoid kernels. Ignored by other kernels.

**kernel\_params** [mapping of string to any, optional] Additional parameters (keyword arguments) for kernel function passed as callable object.

#### **Attributes**

**dual\_coef\_** [array, shape = [n\_samples] or [n\_samples, n\_targets]] Representation of weight vector(s) in kernel space

**X\_fit\_** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training data, which is also required for prediction. If kernel == "precomputed" this is instead the precomputed training matrix, shape = [n\_samples, n\_samples].

#### See also:

```
sklearn.linear_model.Ridge Linear ridge regression.
sklearn.svm.SVR Support Vector Regression implemented using libsvm.
```

# References

• Kevin P. Murphy "Machine Learning: A Probabilistic Perspective", The MIT Press chapter 14.4.3, pp. 492-493

# **Examples**

```
>>> from sklearn.kernel_ridge import KernelRidge
>>> import numpy as np
>>> n_samples, n_features = 10, 5
>>> rng = np.random.RandomState(0)
>>> y = rng.randn(n_samples)
>>> X = rng.randn(n_samples, n_features)
>>> clf = KernelRidge(alpha=1.0)
>>> clf.fit(X, y)
KernelRidge(alpha=1.0, coef0=1, degree=3, gamma=None, kernel='linear', kernel_params=None)
```

## **Methods**

fit(self, X[, y, sample_weight])	Fit Kernel Ridge regression model
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the kernel ridge model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_ (self, alpha=1, kernel='linear', gamma=None, degree=3, coef0=1, kernel\_params=None)

fit (self, X, y=None, sample\_weight=None)

Fit Kernel Ridge regression model

#### **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training data. If kernel == "precomputed" this is instead a precomputed kernel matrix, shape = [n\_samples, n\_samples].
- y [array-like, shape = [n\_samples] or [n\_samples, n\_targets]] Target values

**sample\_weight** [float or array-like of shape [n\_samples]] Individual weights for each sample, ignored if None is passed.

#### Returns

**self** [returns an instance of self.]

get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

predict (self, X)

Predict using the kernel ridge model

#### **Parameters**

X [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Samples. If kernel == "precomputed" this is instead a precomputed kernel matrix, shape = [n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for this estimator.

## Returns

C [array, shape = [n\_samples] or [n\_samples, n\_targets]] Returns predicted values.

score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

## **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.kernel\_ridge.KernelRidge

- · Comparison of kernel ridge regression and SVR
- · Comparison of kernel ridge and Gaussian process regression

# 6.22 sklearn.linear\_model: Generalized Linear Models

The sklearn.linear\_model module implements generalized linear models. It includes Ridge regression, Bayesian Regression, Lasso and Elastic Net estimators computed with Least Angle Regression and coordinate descent. It also implements Stochastic Gradient Descent related algorithms.

**User guide:** See the *Generalized Linear Models* section for further details.

linear_model.ARDRegression([n_iter, tol,])	Bayesian ARD regression.
linear_model.BayesianRidge([n_iter, tol,])	Bayesian ridge regression.
<pre>linear_model.ElasticNet([alpha, 11_ratio,])</pre>	Linear regression with combined L1 and L2 priors as regu-
	larizer.
<pre>linear_model.ElasticNetCV([l1_ratio, eps,])</pre>	Elastic Net model with iterative fitting along a regulariza-
	tion path.
linear_model.HuberRegressor([epsilon,])	Linear regression model that is robust to outliers.
<pre>linear_model.Lars([fit_intercept, verbose,])</pre>	Least Angle Regression model a.k.a.

Continued on next page

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<pre>linear_model.LarsCV([fit_intercept,])</pre>	Cross-validated Least Angle Regression model.
linear_model.Lasso([alpha, fit_intercept,])	Linear Model trained with L1 prior as regularizer (aka the
	Lasso)
linear_model.LassoCV([eps, n_alphas,])	Lasso linear model with iterative fitting along a regulariza-
	tion path.
linear_model.LassoLars([alpha,])	Lasso model fit with Least Angle Regression a.k.a.
linear_model.LassoLarsCV([fit_intercept,])	Cross-validated Lasso, using the LARS algorithm.
linear_model.LassoLarsIC([criterion,])	Lasso model fit with Lars using BIC or AIC for model se-
	lection
linear_model.LinearRegression([])	Ordinary least squares Linear Regression.
linear_model.LogisticRegression([penalty,	Logistic Regression (aka logit, MaxEnt) classifier.
])	
linear_model.LogisticRegressionCV([Cs,	Logistic Regression CV (aka logit, MaxEnt) classifier.
])	
linear_model.MultiTaskLasso([alpha,])	Multi-task Lasso model trained with L1/L2 mixed-norm as
· · ·	regularizer.
linear_model.MultiTaskElasticNet([alpha,	Multi-task ElasticNet model trained with L1/L2 mixed-
])	norm as regularizer
linear_model.MultiTaskLassoCV([eps,])	Multi-task Lasso model trained with L1/L2 mixed-norm as
-	regularizer.
linear_model.MultiTaskElasticNetCV([])	Multi-task L1/L2 ElasticNet with built-in cross-validation.
linear_model.OrthogonalMatchingPursuit([	Orthogonal Matching Pursuit model (OMP)
linear_model.OrthogonalMatchingPursuitCV	([Cross-validated Orthogonal Matching Pursuit model
	(OMP).
linear_model.PassiveAggressiveClassifier	([Passive Aggressive Classifier
linear_model.PassiveAggressiveRegressor(	CPassive Aggressive Regressor
])	
linear_model.Perceptron([penalty, alpha,])	Read more in the <i>User Guide</i> .
linear_model.RANSACRegressor([])	RANSAC (RANdom SAmple Consensus) algorithm.
<pre>linear_model.Ridge([alpha, fit_intercept,])</pre>	Linear least squares with 12 regularization.
linear_model.RidgeClassifier([alpha,])	Classifier using Ridge regression.
linear_model.RidgeClassifierCV([alphas,	Ridge classifier with built-in cross-validation.
])	
linear_model.RidgeCV([alphas,])	Ridge regression with built-in cross-validation.
linear_model.SGDClassifier([loss, penalty,	Linear classifiers (SVM, logistic regression, a.o.) with
])	SGD training.
linear_model.SGDRegressor([loss, penalty,])	Linear model fitted by minimizing a regularized empirical
	loss with SGD
linear_model.TheilSenRegressor([])	Theil-Sen Estimator: robust multivariate regression model.

# 6.22.1 sklearn.linear\_model.ARDRegression

```
 \begin{array}{lll} \textbf{class} \; \texttt{sklearn.linear\_model.ARDRegression} \; (n\_iter=300, & tol=0.001, & alpha\_l=1e-06, \\ 06, & alpha\_2=1e-06, & lambda\_l=1e-06, \\ lambda\_2=1e-06, & compute\_score=False, & threshold\_lambda=10000.0, & fit\_intercept=True, & normalize=False, & copy\_X=True, & verbose=False) \end{array}
```

Bayesian ARD regression.

Fit the weights of a regression model, using an ARD prior. The weights of the regression model are assumed to be in Gaussian distributions. Also estimate the parameters lambda (precisions of the distributions of the weights) and alpha (precision of the distribution of the noise). The estimation is done by an iterative procedures

(Evidence Maximization)

Read more in the *User Guide*.

# **Parameters**

- **n\_iter** [int, optional] Maximum number of iterations. Default is 300
- tol [float, optional] Stop the algorithm if w has converged. Default is 1.e-3.
- **alpha\_1** [float, optional] Hyper-parameter: shape parameter for the Gamma distribution prior over the alpha parameter. Default is 1.e-6.
- **alpha\_2** [float, optional] Hyper-parameter: inverse scale parameter (rate parameter) for the Gamma distribution prior over the alpha parameter. Default is 1.e-6.
- **lambda\_1** [float, optional] Hyper-parameter: shape parameter for the Gamma distribution prior over the lambda parameter. Default is 1.e-6.
- **lambda\_2** [float, optional] Hyper-parameter: inverse scale parameter (rate parameter) for the Gamma distribution prior over the lambda parameter. Default is 1.e-6.
- **compute\_score** [boolean, optional] If True, compute the objective function at each step of the model. Default is False.
- **threshold\_lambda** [float, optional] threshold for removing (pruning) weights with high precision from the computation. Default is 1.e+4.
- **fit\_intercept** [boolean, optional] whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered). Default is True.
- normalize [boolean, optional, default False] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.
- **copy\_X** [boolean, optional, default True.] If True, X will be copied; else, it may be overwritten. **verbose** [boolean, optional, default False] Verbose mode when fitting the model.

# **Attributes**

- $\mathbf{coef}_{\_}$  [array, shape = (n\_features)] Coefficients of the regression model (mean of distribution)
- alpha\_ [float] estimated precision of the noise.
- **lambda**\_ [array, shape = (n\_features)] estimated precisions of the weights.
- **sigma**\_ [array, shape = (n\_features, n\_features)] estimated variance-covariance matrix of the weights
- scores\_ [float] if computed, value of the objective function (to be maximized)

# **Notes**

For an example, see examples/linear\_model/plot\_ard.py.

## References

D. J. C. MacKay, Bayesian nonlinear modeling for the prediction competition, ASHRAE Transactions, 1994.

R. Salakhutdinov, Lecture notes on Statistical Machine Learning, http://www.utstat.toronto.edu/~rsalakhu/sta4273/notes/Lecture2.pdf#page=15 Their beta is our self.alpha\_ Their alpha is our self.lambda\_ ARD is a little different than the slide: only dimensions/features for which self.lambda\_ < self.threshold\_lambda are kept and the rest are discarded.

# **Examples**

## **Methods**

fit(self, X, y)	Fit the ARDRegression model according to the given
	training data and parameters.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, return_std])</pre>	Predict using the linear model.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, n_iter=300, tol=0.001, alpha_1=1e-06, alpha_2=1e-06, lambda_1=1e-06, lambda_2=1e-06, compute_score=False, threshold_lambda=10000.0, fit_intercept=True, normalize=False, copy_X=True, verbose=False)
```

# fit (self, X, y)

Fit the ARDRegression model according to the given training data and parameters.

Iterative procedure to maximize the evidence

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vector, where n\_samples in the number of samples and n\_features is the number of features.
- y [array, shape = [n\_samples]] Target values (integers). Will be cast to X's dtype if necessary

#### Returns

**self** [returns an instance of self.]

# get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
predict (self, X, return_std=False)
```

Predict using the linear model.

In addition to the mean of the predictive distribution, also its standard deviation can be returned.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape = (n\_samples, n\_features)] Samples.

**return\_std** [boolean, optional] Whether to return the standard deviation of posterior prediction.

## **Returns**

**y\_mean** [array, shape = (n\_samples,)] Mean of predictive distribution of query points.

**y\_std** [array, shape = (n\_samples,)] Standard deviation of predictive distribution of query points.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

# **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float]  $R^2$  of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# Examples using sklearn.linear\_model.ARDRegression

• Automatic Relevance Determination Regression (ARD)

# 6.22.2 sklearn.linear\_model.BayesianRidge

```
 \begin{array}{lll} \textbf{class} \; \textbf{sklearn.linear\_model.BayesianRidge} \; (n\_iter=300, & tol=0.001, & alpha\_1=1e-06, \\ & alpha\_2=1e-06, \; lambda\_1=1e-06, \; lambda\_2=1e-06, & compute\_score=False, & fit\_intercept=True, \\ & normalize=False, \; copy\_X=True, \; verbose=False) \end{array}
```

Bayesian ridge regression.

Fit a Bayesian ridge model. See the Notes section for details on this implementation and the optimization of the regularization parameters lambda (precision of the weights) and alpha (precision of the noise).

Read more in the *User Guide*.

#### **Parameters**

- **n\_iter** [int, optional] Maximum number of iterations. Default is 300. Should be greater than or equal to 1.
- tol [float, optional] Stop the algorithm if w has converged. Default is 1.e-3.
- **alpha\_1** [float, optional] Hyper-parameter: shape parameter for the Gamma distribution prior over the alpha parameter. Default is 1.e-6
- **alpha\_2** [float, optional] Hyper-parameter: inverse scale parameter (rate parameter) for the Gamma distribution prior over the alpha parameter. Default is 1.e-6.
- **lambda\_1** [float, optional] Hyper-parameter: shape parameter for the Gamma distribution prior over the lambda parameter. Default is 1.e-6.
- **lambda\_2** [float, optional] Hyper-parameter: inverse scale parameter (rate parameter) for the Gamma distribution prior over the lambda parameter. Default is 1.e-6
- **compute\_score** [boolean, optional] If True, compute the log marginal likelihood at each iteration of the optimization. Default is False.
- **fit\_intercept** [boolean, optional, default True] Whether to calculate the intercept for this model. The intercept is not treated as a probabilistic parameter and thus has no associated variance. If set to False, no intercept will be used in calculations (e.g. data is expected to be already centered).
- **normalize** [boolean, optional, default False] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use <code>sklearn.preprocessing.StandardScaler</code> before calling fit on an estimator with normalize=False.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.verbose [boolean, optional, default False] Verbose mode when fitting the model.

# **Attributes**

**coef**\_ [array, shape = (n\_features,)] Coefficients of the regression model (mean of distribution).

intercept\_ [float] Independent term in decision function. Set to 0.0 if fit\_intercept =
 False.

alpha\_ [float] Estimated precision of the noise.

lambda\_ [float] Estimated precision of the weights.

**sigma**\_ [array, shape = (n\_features, n\_features)] Estimated variance-covariance matrix of the weights.

**scores**\_ [array, shape = (**n\_iter\_** + 1,)] If computed\_score is True, value of the log marginal likelihood (to be maximized) at each iteration of the optimization. The array starts with the value of the log marginal likelihood obtained for the initial values of alpha and lambda and ends with the value obtained for the estimated alpha and lambda.

**n\_iter\_** [int] The actual number of iterations to reach the stopping criterion.

## **Notes**

There exist several strategies to perform Bayesian ridge regression. This implementation is based on the algorithm described in Appendix A of (Tipping, 2001) where updates of the regularization parameters are done as suggested in (MacKay, 1992). Note that according to A New View of Automatic Relevance Determination (Wipf and Nagarajan, 2008) these update rules do not guarantee that the marginal likelihood is increasing between two consecutive iterations of the optimization.

#### References

D. J. C. MacKay, Bayesian Interpolation, Computation and Neural Systems, Vol. 4, No. 3, 1992.

M. E. Tipping, Sparse Bayesian Learning and the Relevance Vector Machine, Journal of Machine Learning Research, Vol. 1, 2001.

# **Examples**

#### Methods

fit(self, X, y[, sample_weight])	Fit the model
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, return_std])</pre>	Predict using the linear model.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.

Continued on next page

Set the parameters of this estimator.

\_\_init\_\_(self, n\_iter=300, tol=0.001, alpha\_1=1e-06, alpha\_2=1e-06, lambda\_1=1e-06, lambda\_2=1e-06, compute\_score=False, fit\_intercept=True, normalize=False, copy\_X=True, verbose=False)

**fit** (*self*, *X*, *y*, *sample\_weight=None*)

Fit the model

## **Parameters**

**X** [numpy array of shape [n\_samples,n\_features]] Training data

y [numpy array of shape [n\_samples]] Target values. Will be cast to X's dtype if necessary

sample\_weight [numpy array of shape [n\_samples]] Individual weights for each sample

New in version 0.20: parameter *sample\_weight* support to BayesianRidge.

## Returns

**self** [returns an instance of self.]

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

predict (self, X, return\_std=False)

Predict using the linear model.

In addition to the mean of the predictive distribution, also its standard deviation can be returned.

### **Parameters**

**X** [{array-like, sparse matrix}, shape = (n\_samples, n\_features)] Samples.

**return\_std** [boolean, optional] Whether to return the standard deviation of posterior prediction.

# Returns

**y\_mean** [array, shape = (n\_samples,)] Mean of predictive distribution of query points.

y\_std [array, shape = (n\_samples,)] Standard deviation of predictive distribution of query
points.

score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

# **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float]  $R^2$  of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses <code>multioutput='uniform\_average'</code>).

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.linear\_model.BayesianRidge

- Feature agglomeration vs. univariate selection
- Imputing missing values with variants of IterativeImputer
- Bayesian Ridge Regression

# 6.22.3 sklearn.linear\_model.ElasticNet

Linear regression with combined L1 and L2 priors as regularizer.

Minimizes the objective function:

```
1 / (2 * n_samples) * ||y - Xw||^2_2
+ alpha * l1_ratio * ||w||_1
+ 0.5 * alpha * (1 - l1_ratio) * ||w||^2_2
```

If you are interested in controlling the L1 and L2 penalty separately, keep in mind that this is equivalent to:

```
a * L1 + b * L2
```

#### where:

```
alpha = a + b and l1_ratio = a / (a + b)
```

The parameter 11\_ratio corresponds to alpha in the glmnet R package while alpha corresponds to the lambda parameter in glmnet. Specifically, 11\_ratio = 1 is the lasso penalty. Currently, 11\_ratio <= 0.01 is not reliable, unless you supply your own sequence of alpha.

Read more in the User Guide.

## **Parameters**

- **alpha** [float, optional] Constant that multiplies the penalty terms. Defaults to 1.0. See the notes for the exact mathematical meaning of this parameter. "alpha = 0" is equivalent to an ordinary least square, solved by the LinearRegression object. For numerical reasons, using alpha = 0 with the Lasso object is not advised. Given this, you should use the LinearRegression object.
- I1\_ratio [float] The ElasticNet mixing parameter, with 0 <= l1\_ratio <= 1. For
  l1\_ratio = 0 the penalty is an L2 penalty. For l1\_ratio = 1 it is an L1 penalty.
  For 0 < l1\_ratio < 1, the penalty is a combination of L1 and L2.</pre>
- **fit\_intercept** [bool] Whether the intercept should be estimated or not. If False, the data is assumed to be already centered.
- normalize [boolean, optional, default False] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.
- **precompute** [True | False | array-like] Whether to use a precomputed Gram matrix to speed up calculations. The Gram matrix can also be passed as argument. For sparse input this option is always True to preserve sparsity.
- max iter [int, optional] The maximum number of iterations
- copy X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- **tol** [float, optional] The tolerance for the optimization: if the updates are smaller than tol, the optimization code checks the dual gap for optimality and continues until it is smaller than tol.
- warm\_start [bool, optional] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.
- positive [bool, optional] When set to True, forces the coefficients to be positive.
- random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator that selects a random feature to update. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == 'random'.
- **selection** [str, default 'cyclic'] If set to 'random', a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to 'random') often leads to significantly faster convergence especially when tol is higher than 1e-4.

#### Attributes

coef\_ [array, shape (n\_features,) | (n\_targets, n\_features)] parameter vector (w in the cost function formula) **sparse\_coef\_** [scipy.sparse matrix, shape (n\_features, 1) | (n\_targets, n\_features)] sparse representation of the fitted coef\_

**intercept**\_ [float | array, shape (n\_targets,)] independent term in decision function.

**n\_iter\_** [array-like, shape (n\_targets,)] number of iterations run by the coordinate descent solver to reach the specified tolerance.

# See also:

**ElasticNetCV** Elastic net model with best model selection by cross-validation.

**SGDRegressor** implements elastic net regression with incremental training.

```
SGDClassifier implements logistic regression with elastic net penalty (SGDClassifier(loss="log", penalty="elasticnet")).
```

# **Notes**

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

# **Examples**

```
>>> from sklearn.linear_model import ElasticNet
>>> from sklearn.datasets import make_regression
```

#### **Methods**

fit(self, X, y[, check_input])	Fit model with coordinate descent.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
path(X, y[, l1_ratio, eps, n_alphas,])	Compute elastic net path with coordinate descent
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R <sup>2</sup> of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__(self, alpha=1.0, l1_ratio=0.5, fit_intercept=True, normalize=False, precompute=False, max_iter=1000, copy_X=True, tol=0.0001, warm_start=False, positive=False, random_state=None, selection='cyclic')
```

# **fit** (*self*, *X*, *y*, *check input=True*)

Fit model with coordinate descent.

## **Parameters**

- X [ndarray or scipy.sparse matrix, (n samples, n features)] Data
- y [ndarray, shape (n\_samples,) or (n\_samples, n\_targets)] Target. Will be cast to X's dtype if necessary

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

## **Notes**

Coordinate descent is an algorithm that considers each column of data at a time hence it will automatically convert the X input as a Fortran-contiguous numpy array if necessary.

To avoid memory re-allocation it is advised to allocate the initial data in memory directly using that format.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

```
1 / (2 * n_samples) * ||y - Xw||^2_2
+ alpha * 11_ratio * ||w||_1
+ 0.5 * alpha * (1 - 11_ratio) * ||w||^2_2
```

For multi-output tasks it is:

```
(1 / (2 * n_samples)) * ||Y - XW||^Fro_2
+ alpha * l1_ratio * ||W||_21
+ 0.5 * alpha * (1 - l1_ratio) * ||W||_Fro^2
```

# Where:

i.e. the sum of norm of each row.

Read more in the *User Guide*.

## **Parameters**

- **X** [{array-like}, shape (n\_samples, n\_features)] Training data. Pass directly as Fortrancontiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.
- y [ndarray, shape (n\_samples,) or (n\_samples, n\_outputs)] Target values
- **11\_ratio** [float, optional] float between 0 and 1 passed to elastic net (scaling between 11 and 12 penalties). 11 ratio=1 corresponds to the Lasso
- eps [float] Length of the path. eps=1e-3 means that alpha\_min / alpha\_max = 1e-3
- **n\_alphas** [int, optional] Number of alphas along the regularization path
- **alphas** [ndarray, optional] List of alphas where to compute the models. If None alphas are set automatically
- **precompute** [True | False | 'auto' | array-like] Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument.
- $\mathbf{X}\mathbf{y}$  [array-like, optional]  $\mathbf{X}\mathbf{y} = \text{np.dot}(\mathbf{X}.\mathbf{T}, \mathbf{y})$  that can be precomputed. It is useful only when the Gram matrix is precomputed.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- **coef\_init** [array, shape (n\_features, ) | None] The initial values of the coefficients.
- verbose [bool or integer] Amount of verbosity.
- return\_n\_iter [bool] whether to return the number of iterations or not.
- **positive** [bool, default False] If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).
- **check\_input** [bool, default True] Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check\_input=False.
- \*\*params [kwargs] keyword arguments passed to the coordinate descent solver.

# Returns

- **alphas** [array, shape (n\_alphas,)] The alphas along the path where models are computed.
- **coefs** [array, shape (n\_features, n\_alphas) or (n\_outputs, n\_features, n\_alphas)] Coefficients along the path.
- **dual\_gaps** [array, shape (n\_alphas,)] The dual gaps at the end of the optimization for each alpha.
- **n\_iters** [array-like, shape (n\_alphas,)] The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return\_n\_iter is set to True).

## See also:

MultiTaskElasticNet
MultiTaskElasticNetCV
ElasticNet
ElasticNetCV

## **Notes**

For an example, see examples/linear\_model/plot\_lasso\_coordinate\_descent\_path.py.

## predict (self, X)

Predict using the linear model

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

#### Returns

C [array, shape (n\_samples,)] Returns predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

## **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] R^2 of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

#### sparse\_coef\_

sparse representation of the fitted coef\_

## Examples using sklearn.linear\_model.ElasticNet

- Lasso and Elastic Net for Sparse Signals
- Train error vs Test error

# 6.22.4 sklearn.linear\_model.HuberRegressor

The Huber Regressor optimizes the squared loss for the samples where |(y - X'w)| / sigma| < epsilon and the absolute loss for the samples where |(y - X'w)| / sigma| > epsilon, where w and sigma are parameters to be optimized. The parameter sigma makes sure that if y is scaled up or down by a certain factor, one does not need to rescale epsilon to achieve the same robustness. Note that this does not take into account the fact that the different features of X may be of different scales.

This makes sure that the loss function is not heavily influenced by the outliers while not completely ignoring their effect.

Read more in the User Guide

New in version 0.18.

#### **Parameters**

**epsilon** [float, greater than 1.0, default 1.35] The parameter epsilon controls the number of samples that should be classified as outliers. The smaller the epsilon, the more robust it is to outliers.

max\_iter [int, default 100] Maximum number of iterations that scipy.optimize.fmin\_l\_bfgs\_b should run for.

**alpha** [float, default 0.0001] Regularization parameter.

warm\_start [bool, default False] This is useful if the stored attributes of a previously used model has to be reused. If set to False, then the coefficients will be rewritten for every call to fit. See the Glossary.

**fit\_intercept** [bool, default True] Whether or not to fit the intercept. This can be set to False if the data is already centered around the origin.

tol [float, default 1e-5] The iteration will stop when max{|proj g\_i | i = 1, ..., n} <= tol where pg\_i is the i-th component of the projected gradient.

# Attributes

**coef**\_ [array, shape (n\_features,)] Features got by optimizing the Huber loss.

intercept\_ [float] Bias.

scale\_ [float] The value by which | y - X'w - c | is scaled down.

**n\_iter\_** [int] Number of iterations that fmin\_l\_bfgs\_b has run for.

Changed in version 0.20: In SciPy <= 1.0.0 the number of lbfgs iterations may exceed max\_iter. n\_iter\_will now report at most max\_iter.

**outliers**\_ [array, shape (n\_samples,)] A boolean mask which is set to True where the samples are identified as outliers.

## References

[Re4616ef910fb-1], [Re4616ef910fb-2]

# **Examples**

```
>>> import numpy as np
>>> from sklearn.linear_model import HuberRegressor, LinearRegression
>>> from sklearn.datasets import make_regression
>>> rng = np.random.RandomState(0)
>>> X, y, coef = make_regression(
       n_samples=200, n_features=2, noise=4.0, coef=True, random_state=0)
>>> X[:4] = rng.uniform(10, 20, (4, 2))
>>> y[:4] = rnq.uniform(10, 20, 4)
>>> huber = HuberRegressor().fit(X, y)
>>> huber.score(X, y)
-7.284608623514573
>>> huber.predict(X[:1,])
array([806.7200...])
>>> linear = LinearRegression().fit(X, y)
>>> print("True coefficients:", coef)
True coefficients: [20.4923... 34.1698...]
>>> print("Huber coefficients:", huber.coef_)
Huber coefficients: [17.7906... 31.0106...]
>>> print("Linear Regression coefficients:", linear.coef_)
Linear Regression coefficients: [-1.9221... 7.0226...]
```

## Methods

fit(self, X, y[, sample_weight])	Fit the model according to the given training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__(self, epsilon=1.35, max_iter=100, alpha=0.0001, warm_start=False, fit_intercept=True, tol=1e-05)
```

fit (self, X, y, sample\_weight=None)

Fit the model according to the given training data.

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples in the number of samples and n\_features is the number of features.
- **y** [array-like, shape (n\_samples,)] Target vector relative to X.

**sample\_weight** [array-like, shape (n\_samples,)] Weight given to each sample.

## Returns

self [object]

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
predict (self, X)
```

Predict using the linear model

## **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

## **Returns**

C [array, shape (n\_samples,)] Returns predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

X [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape =  $(n_samples)$  or  $(n_samples, n_outputs)$ ] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

# Returns

**score** [float] R^2 of self.predict(X) wrt. y.

# **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.linear\_model.HuberRegressor

- HuberRegressor vs Ridge on dataset with strong outliers
- Robust linear estimator fitting

# 6.22.5 sklearn.linear\_model.Lars

class sklearn.linear\_model.Lars (fit\_intercept=True, verbose=False, normalize=True, precompute='auto', n\_nonzero\_coefs=500, eps=2.220446049250313e16, copy\_X=True, fit\_path=True, positive=False)

Least Angle Regression model a.k.a. LAR

Read more in the User Guide.

#### **Parameters**

- **fit\_intercept** [boolean] Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).
- verbose [boolean or integer, optional] Sets the verbosity amount
- **normalize** [boolean, optional, default True] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.
- **precompute** [True | False | 'auto' | array-like] Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument.
- n\_nonzero\_coefs [int, optional] Target number of non-zero coefficients. Use np.inf for no limit.
- **eps** [float, optional] The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems. Unlike the tol parameter in some iterative optimization-based algorithms, this parameter does not control the tolerance of the optimization.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- fit\_path [boolean] If True the full path is stored in the coef\_path\_ attribute. If you compute the solution for a large problem or many targets, setting fit\_path to False will lead to a speedup, especially with a small alpha.
- **positive** [boolean (default=False)] Restrict coefficients to be >= 0. Be aware that you might want to remove fit\_intercept which is set True by default.

Deprecated since version 0.20: The option is broken and deprecated. It will be removed in v0.22.

## **Attributes**

alphas\_ [array, shape (n\_alphas + 1,) | list of n\_targets such arrays] Maximum of covariances (in absolute value) at each iteration. n\_alphas is either n\_nonzero\_coefs or n\_features, whichever is smaller.

- active\_ [list, length = n\_alphas | list of n\_targets such lists] Indices of active variables at the end of the path.
- coef\_path\_ [array, shape (n\_features, n\_alphas + 1) | list of n\_targets such arrays] The varying
  values of the coefficients along the path. It is not present if the fit\_path parameter is
  False.
- **coef**\_ [array, shape (n\_features,) or (n\_targets, n\_features)] Parameter vector (w in the formulation formula).
- intercept\_ [float | array, shape (n\_targets,)] Independent term in decision function.
- **n\_iter\_** [array-like or int] The number of iterations taken by lars\_path to find the grid of alphas for each target.

#### See also:

```
lars_path, LarsCV
sklearn.decomposition.sparse_encode
```

# **Examples**

# Methods

fit(self, X, y[, Xy])	Fit the model using X, y as training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, fit_intercept=True, verbose=False, normalize=True, precompute='auto', n_nonzero_coefs=500, eps=2.220446049250313e-16, copy_X=True, fit_path=True, positive=False)
```

fit (self, X, y, Xy=None)

Fit the model using X, y as training data.

# **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data.
- y [array-like, shape (n\_samples,) or (n\_samples, n\_targets)] Target values.
- Xy [array-like, shape (n\_samples,) or (n\_samples, n\_targets), optional] Xy = np.dot(X.T, y)

that can be precomputed. It is useful only when the Gram matrix is precomputed.

## Returns

self [object] returns an instance of self.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## **Returns**

params [mapping of string to any] Parameter names mapped to their values.

# predict (self, X)

Predict using the linear model

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

#### Returns

C [array, shape (n\_samples,)] Returns predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample weight** [array-like, shape = [n samples], optional] Sample weights.

## Returns

**score** [float] R^2 of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# 6.22.6 sklearn.linear model.Lasso

Linear Model trained with L1 prior as regularizer (aka the Lasso)

The optimization objective for Lasso is:

```
(1 / (2 * n_samples)) * ||y - Xw||^2_2 + alpha * ||w||_1
```

Technically the Lasso model is optimizing the same objective function as the Elastic Net with  $l1\_ratio=1.0$  (no L2 penalty).

Read more in the *User Guide*.

## **Parameters**

- **alpha** [float, optional] Constant that multiplies the L1 term. Defaults to 1.0. alpha = 0 is equivalent to an ordinary least square, solved by the *LinearRegression* object. For numerical reasons, using alpha = 0 with the Lasso object is not advised. Given this, you should use the *LinearRegression* object.
- **fit\_intercept** [boolean, optional, default True] Whether to calculate the intercept for this model. If set to False, no intercept will be used in calculations (e.g. data is expected to be already centered).
- normalize [boolean, optional, default False] This parameter is ignored when
  fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to
  standardize, please use sklearn.preprocessing.StandardScaler before
  calling fit on an estimator with normalize=False.
- **precompute** [True | False | array-like, default=False] Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument. For sparse input this option is always True to preserve sparsity.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- max\_iter [int, optional] The maximum number of iterations
- tol [float, optional] The tolerance for the optimization: if the updates are smaller than tol, the optimization code checks the dual gap for optimality and continues until it is smaller than tol.
- warm\_start [bool, optional] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.
- positive [bool, optional] When set to True, forces the coefficients to be positive.

random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator that selects a random feature to update. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == 'random'.

**selection** [str, default 'cyclic'] If set to 'random', a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to 'random') often leads to significantly faster convergence especially when tol is higher than 1e-4.

## **Attributes**

coef\_ [array, shape (n\_features,) | (n\_targets, n\_features)] parameter vector (w in the cost function formula)

**sparse\_coef\_** [scipy.sparse matrix, shape (n\_features, 1) | (n\_targets, n\_features)] sparse representation of the fitted coef\_

intercept\_ [float | array, shape (n\_targets,)] independent term in decision function.

**n\_iter\_** [int | array-like, shape (n\_targets,)] number of iterations run by the coordinate descent solver to reach the specified tolerance.

#### See also:

```
lars_path
lasso_path
LassoLars
LassoCV
LassoLarsCV
sklearn.decomposition.sparse_encode
```

# **Notes**

The algorithm used to fit the model is coordinate descent.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

# **Examples**

# **Methods**

fit(self, X, y[, check_input])	Fit model with coordinate descent.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
path(X, y[, 11_ratio, eps, n_alphas,])	Compute elastic net path with coordinate descent
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, alpha=1.0, fit_intercept=True, normalize=False, precompute=False, copy_X=True, max_iter=1000, tol=0.0001, warm_start=False, positive=False, random_state=None, selection='cyclic')
```

# **fit** (*self*, *X*, *y*, *check\_input=True*)

Fit model with coordinate descent.

# **Parameters**

X [ndarray or scipy.sparse matrix, (n\_samples, n\_features)] Data

**y** [ndarray, shape (n\_samples,) or (n\_samples, n\_targets)] Target. Will be cast to X's dtype if necessary

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

## **Notes**

Coordinate descent is an algorithm that considers each column of data at a time hence it will automatically convert the X input as a Fortran-contiguous numpy array if necessary.

To avoid memory re-allocation it is advised to allocate the initial data in memory directly using that format.

# get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

```
1 / (2 * n_samples) * ||y - Xw||^2_2
+ alpha * 11_ratio * ||w||_1
+ 0.5 * alpha * (1 - 11_ratio) * ||w||^2_2
```

## For multi-output tasks it is:

```
(1 / (2 * n_samples)) * ||Y - XW||^Fro_2
+ alpha * l1_ratio * ||W||_21
+ 0.5 * alpha * (1 - l1_ratio) * ||W||_Fro^2
```

#### Where:

```
|||\|||_21 = \sum_i \sqrt{\sum_j w_{ij}^2}
```

i.e. the sum of norm of each row.

Read more in the *User Guide*.

#### **Parameters**

- **X** [{array-like}, shape (n\_samples, n\_features)] Training data. Pass directly as Fortrancontiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.
- y [ndarray, shape (n\_samples,) or (n\_samples, n\_outputs)] Target values
- **11\_ratio** [float, optional] float between 0 and 1 passed to elastic net (scaling between 11 and 12 penalties). 11\_ratio=1 corresponds to the Lasso
- eps [float] Length of the path. eps=1e-3 means that alpha\_min / alpha\_max =
  1e-3
- n\_alphas [int, optional] Number of alphas along the regularization path
- **alphas** [ndarray, optional] List of alphas where to compute the models. If None alphas are set automatically
- **precompute** [True | False | 'auto' | array-like] Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument.
- $\mathbf{X}\mathbf{y}$  [array-like, optional]  $\mathbf{X}\mathbf{y} = \text{np.dot}(\mathbf{X}.\mathbf{T}, \mathbf{y})$  that can be precomputed. It is useful only when the Gram matrix is precomputed.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- **coef\_init** [array, shape (n\_features, ) | None] The initial values of the coefficients.
- **verbose** [bool or integer] Amount of verbosity.
- return\_n\_iter [bool] whether to return the number of iterations or not.
- **positive** [bool, default False] If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).
- **check\_input** [bool, default True] Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check\_input=False.
- \*\*params [kwargs] keyword arguments passed to the coordinate descent solver.

# Returns

- **alphas** [array, shape (n alphas,)] The alphas along the path where models are computed.
- **coefs** [array, shape (n\_features, n\_alphas) or (n\_outputs, n\_features, n\_alphas)] Coefficients along the path.

- **dual\_gaps** [array, shape (n\_alphas,)] The dual gaps at the end of the optimization for each alpha.
- **n\_iters** [array-like, shape (n\_alphas,)] The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return\_n\_iter is set to True).

#### See also:

MultiTaskElasticNet
MultiTaskElasticNetCV
ElasticNet
ElasticNet

## **Notes**

For an example, see examples/linear\_model/plot\_lasso\_coordinate\_descent\_path.py.

# predict (self, X)

Predict using the linear model

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

## Returns

C [array, shape (n\_samples,)] Returns predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

# **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n samples fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n samples) or (n samples, n outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] R^2 of self.predict(X) wrt. y.

# **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score

directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## sparse\_coef\_

sparse representation of the fitted coef\_

# Examples using sklearn.linear\_model.Lasso

- Compressive sensing: tomography reconstruction with L1 prior (Lasso)
- Cross-validation on diabetes Dataset Exercise
- Lasso on dense and sparse data
- Joint feature selection with multi-task Lasso
- Lasso and Elastic Net for Sparse Signals

# 6.22.7 sklearn.linear\_model.LassoLars

```
 \begin{array}{c} \textbf{class} \; \text{sklearn.linear\_model.LassoLars} \; (alpha=1.0, \quad \textit{fit\_intercept=True}, \quad \textit{verbose=False}, \quad \textit{nor-malize=True}, \quad \textit{precompute='auto'}, \quad \textit{max\_iter=500}, \\ eps=2.220446049250313e-16, \quad & copy\_X=True, \\ \textit{fit\_path=True}, \; \textit{positive=False}) \end{array}
```

Lasso model fit with Least Angle Regression a.k.a. Lars

It is a Linear Model trained with an L1 prior as regularizer.

The optimization objective for Lasso is:

```
(1 / (2 * n_samples)) * ||y - Xw||^2_2 + alpha * ||w||_1
```

Read more in the *User Guide*.

#### **Parameters**

**alpha** [float] Constant that multiplies the penalty term. Defaults to 1.0. alpha = 0 is equivalent to an ordinary least square, solved by LinearRegression. For numerical reasons, using alpha = 0 with the LassoLars object is not advised and you should prefer the LinearRegression object.

**fit\_intercept** [boolean] whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

verbose [boolean or integer, optional] Sets the verbosity amount

**normalize** [boolean, optional, default True] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use

sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

- **precompute** [True | False | 'auto' | array-like] Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument.
- max\_iter [integer, optional] Maximum number of iterations to perform.
- **eps** [float, optional] The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems. Unlike the tol parameter in some iterative optimization-based algorithms, this parameter does not control the tolerance of the optimization.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- **fit\_path** [boolean] If True the full path is stored in the coef\_path\_ attribute. If you compute the solution for a large problem or many targets, setting fit\_path to False will lead to a speedup, especially with a small alpha.
- positive [boolean (default=False)] Restrict coefficients to be >= 0. Be aware that you might want to remove fit\_intercept which is set True by default. Under the positive restriction the model coefficients will not converge to the ordinary-least-squares solution for small values of alpha. Only coefficients up to the smallest alpha value (alphas\_[alphas\_ > 0.]. min() when fit\_path=True) reached by the stepwise Lars-Lasso algorithm are typically in congruence with the solution of the coordinate descent Lasso estimator.

#### Attributes

- **alphas**\_ [array, shape (n\_alphas + 1,) | list of n\_targets such arrays] Maximum of covariances (in absolute value) at each iteration. n\_alphas is either max\_iter, n\_features, or the number of nodes in the path with correlation greater than alpha, whichever is smaller.
- active\_ [list, length = n\_alphas | list of n\_targets such lists] Indices of active variables at the end of the path.
- coef\_path\_ [array, shape (n\_features, n\_alphas + 1) or list] If a list is passed it's expected to be
   one of n\_targets such arrays. The varying values of the coefficients along the path. It is not
   present if the fit\_path parameter is False.
- **coef**\_ [array, shape (n\_features,) or (n\_targets, n\_features)] Parameter vector (w in the formulation formula).
- intercept\_ [float | array, shape (n\_targets,)] Independent term in decision function.
- **n\_iter\_** [array-like or int.] The number of iterations taken by lars\_path to find the grid of alphas for each target.

# See also:

```
lars_path
lasso_path
Lasso
LassoCV
LassoLarsCV
LassoLarsIC
sklearn.decomposition.sparse_encode
```

# **Examples**

#### Methods

fit(self, X, y[, Xy])	Fit the model using X, y as training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, alpha=1.0, fit_intercept=True, verbose=False, normalize=True, precompute='auto', max_iter=500, eps=2.220446049250313e-16, copy_X=True, fit_path=True, positive=False)
```

## fit (self, X, y, Xy=None)

Fit the model using X, y as training data.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data.

**y** [array-like, shape (n\_samples,) or (n\_samples, n\_targets)] Target values.

**Xy** [array-like, shape (n\_samples,) or (n\_samples, n\_targets), optional] Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.

# Returns

**self** [object] returns an instance of self.

# get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### predict (self, X)

Predict using the linear model

# **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

### Returns

C [array, shape (n\_samples,)] Returns predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float]  $R^2$  of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# 6.22.8 sklearn.linear\_model.LinearRegression

# **Parameters**

**fit\_intercept** [boolean, optional, default True] whether to calculate the intercept for this model. If set to False, no intercept will be used in calculations (e.g. data is expected to be already centered).

- normalize [boolean, optional, default False] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- n\_jobs [int or None, optional (default=None)] The number of jobs to use for the computation. This will only provide speedup for n\_targets > 1 and sufficient large problems. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

## **Attributes**

coef\_ [array, shape (n\_features, ) or (n\_targets, n\_features)] Estimated coefficients for the linear regression problem. If multiple targets are passed during the fit (y 2D), this is a 2D array of shape (n\_targets, n\_features), while if only one target is passed, this is a 1D array of length n\_features.

**intercept**\_ [array] Independent term in the linear model.

### **Notes**

From the implementation point of view, this is just plain Ordinary Least Squares (scipy.linalg.lstsq) wrapped as a predictor object.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.linear_model import LinearRegression
>>> X = np.array([[1, 1], [1, 2], [2, 2], [2, 3]])
>>> # y = 1 * x_0 + 2 * x_1 + 3
>>> y = np.dot(X, np.array([1, 2])) + 3
>>> reg = LinearRegression().fit(X, y)
>>> reg.score(X, y)
1.0
>>> reg.coef_
array([1., 2.])
>>> reg.intercept_
3.0000...
>>> reg.predict(np.array([[3, 5]]))
array([16.])
```

## **Methods**

fit(self, X, y[, sample_weight])	Fit linear model.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, fit_intercept=True, normalize=False, copy_X=True, n_jobs=None)

fit (self, X, y, sample_weight=None)

Fit linear model.
```

#### **Parameters**

- **X** [array-like or sparse matrix, shape (n\_samples, n\_features)] Training data
- y [array\_like, shape (n\_samples, n\_targets)] Target values. Will be cast to X's dtype if necessary

**sample\_weight** [numpy array of shape [n\_samples]] Individual weights for each sample New in version 0.17: parameter *sample\_weight* support to LinearRegression.

#### Returns

**self** [returns an instance of self.]

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict using the linear model

# **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

#### **Returns**

C [array, shape (n\_samples,)] Returns predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

## **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- $\mathbf{y}$  [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

# Returns

**score** [float] R^2 of self.predict(X) wrt. y.

### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform average').

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## Examples using sklearn.linear model.LinearRegression

- Isotonic Regression
- Face completion with a multi-output estimators
- Plot individual and voting regression predictions
- Ordinary Least Squares and Ridge Regression Variance
- Logistic function
- Linear Regression Example
- Robust linear model estimation using RANSAC
- Sparsity Example: Fitting only features 1 and 2
- Theil-Sen Regression
- Robust linear estimator fitting
- Automatic Relevance Determination Regression (ARD)
- Bayesian Ridge Regression
- Plotting Cross-Validated Predictions
- Underfitting vs. Overfitting
- Using KBinsDiscretizer to discretize continuous features

# 6.22.9 sklearn.linear\_model.LogisticRegression

```
 \begin{array}{c} \textbf{class} \; \texttt{sklearn.linear\_model.LogisticRegression} \; (penalty='l2', \quad dual=False, \quad tol=0.0001, \\ C=1.0, \quad fit\_intercept=True, \quad intercept\_scaling=1, \quad class\_weight=None, \\ random\_state=None, \quad solver='warn', \\ max\_iter=100, \quad multi\_class='warn', \quad verbose=0, \quad warm\_start=False, \quad n\_jobs=None, \\ l1\_ratio=None) \end{array}
```

Logistic Regression (aka logit, MaxEnt) classifier.

In the multiclass case, the training algorithm uses the one-vs-rest (OvR) scheme if the 'multi\_class' option is set to 'ovr', and uses the cross-entropy loss if the 'multi\_class' option is set to 'multinomial'. (Currently the 'multinomial' option is supported only by the 'lbfgs', 'sag', 'saga' and 'newton-cg' solvers.)

This class implements regularized logistic regression using the 'liblinear' library, 'newton-cg', 'sag', 'saga' and 'lbfgs' solvers. **Note that regularization is applied by default**. It can handle both dense and sparse input. Use C-ordered arrays or CSR matrices containing 64-bit floats for optimal performance; any other input format will be converted (and copied).

The 'newton-cg', 'sag', and 'lbfgs' solvers support only L2 regularization with primal formulation, or no regularization. The 'liblinear' solver supports both L1 and L2 regularization, with a dual formulation only for the L2 penalty. The Elastic-Net regularization is only supported by the 'saga' solver.

Read more in the *User Guide*.

#### **Parameters**

**penalty** [str, '11', '12', 'elasticnet' or 'none', optional (default='12')] Used to specify the norm used in the penalization. The 'newton-cg', 'sag' and 'lbfgs' solvers support only 12 penalties. 'elasticnet' is only supported by the 'saga' solver. If 'none' (not supported by the liblinear solver), no regularization is applied.

New in version 0.19: 11 penalty with SAGA solver (allowing 'multinomial' + L1)

- **dual** [bool, optional (default=False)] Dual or primal formulation. Dual formulation is only implemented for 12 penalty with liblinear solver. Prefer dual=False when n\_samples > n features.
- tol [float, optional (default=1e-4)] Tolerance for stopping criteria.
- **C** [float, optional (default=1.0)] Inverse of regularization strength; must be a positive float. Like in support vector machines, smaller values specify stronger regularization.
- **fit\_intercept** [bool, optional (default=True)] Specifies if a constant (a.k.a. bias or intercept) should be added to the decision function.
- intercept\_scaling [float, optional (default=1)] Useful only when the solver 'liblinear' is used
   and self.fit\_intercept is set to True. In this case, x becomes [x, self.intercept\_scaling],
   i.e. a "synthetic" feature with constant value equal to intercept\_scaling is ap pended to the instance vector. The intercept becomes intercept\_scaling \*
   synthetic\_feature\_weight.

Note! the synthetic feature weight is subject to 11/12 regularization as all other features. To lessen the effect of regularization on synthetic feature weight (and therefore on the intercept) intercept scaling has to be increased.

class\_weight [dict or 'balanced', optional (default=None)] Weights associated with classes in
 the form {class\_label: weight}. If not given, all classes are supposed to have
 weight one.

The "balanced" mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as  $n_{samples} / (n_{classes} * np. bincount(y))$ .

Note that these weights will be multiplied with sample\_weight (passed through the fit method) if sample\_weight is specified.

New in version 0.17: class weight='balanced'

- random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == 'sag' or 'liblinear'.
- **solver** [str, {'newton-cg', 'lbfgs', 'liblinear', 'sag', 'saga'}, optional (default='liblinear').] Algorithm to use in the optimization problem.
  - For small datasets, 'liblinear' is a good choice, whereas 'sag' and 'saga' are faster for large ones.
  - For multiclass problems, only 'newton-cg', 'sag', 'saga' and 'lbfgs' handle multinomial loss; 'liblinear' is limited to one-versus-rest schemes.
  - 'newton-cg', 'lbfgs', 'sag' and 'saga' handle L2 or no penalty
  - 'liblinear' and 'saga' also handle L1 penalty
  - · 'saga' also supports 'elasticnet' penalty
  - 'liblinear' does not handle no penalty

Note that 'sag' and 'saga' fast convergence is only guaranteed on features with approximately the same scale. You can preprocess the data with a scaler from sklearn.preprocessing.

New in version 0.17: Stochastic Average Gradient descent solver.

New in version 0.19: SAGA solver.

Changed in version 0.20: Default will change from 'liblinear' to 'lbfgs' in 0.22.

- **max\_iter** [int, optional (default=100)] Maximum number of iterations taken for the solvers to converge.
- **multi\_class** [str, {'ovr', 'multinomial', 'auto'}, optional (default='ovr')] If the option chosen is 'ovr', then a binary problem is fit for each label. For 'multinomial' the loss minimised is the multinomial loss fit across the entire probability distribution, *even when the data is binary*. 'multinomial' is unavailable when solver='liblinear'. 'auto' selects 'ovr' if the data is binary, or if solver='liblinear', and otherwise selects 'multinomial'.

New in version 0.18: Stochastic Average Gradient descent solver for 'multinomial' case.

Changed in version 0.20: Default will change from 'ovr' to 'auto' in 0.22.

- **verbose** [int, optional (default=0)] For the liblinear and lbfgs solvers set verbose to any positive number for verbosity.
- warm\_start [bool, optional (default=False)] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. Useless for liblinear solver. See *the Glossary*.

New in version 0.17: warm\_start to support lbfgs, newton-cg, sag, saga solvers.

**n\_jobs** [int or None, optional (default=None)] Number of CPU cores used when parallelizing over classes if multi\_class='ovr'". This parameter is ignored when the solver is set to

'liblinear' regardless of whether 'multi\_class' is specified or not. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

### **Attributes**

**classes**\_ [array, shape (n\_classes, )] A list of class labels known to the classifier.

**coef**\_ [array, shape (1, n\_features) or (n\_classes, n\_features)] Coefficient of the features in the decision function.

*coef*\_ is of shape (1, n\_features) when the given problem is binary. In particular, when multi\_class='multinomial', *coef*\_ corresponds to outcome 1 (True) and -coef\_ corresponds to outcome 0 (False).

intercept\_ [array, shape (1,) or (n\_classes,)] Intercept (a.k.a. bias) added to the decision function.

If fit\_intercept is set to False, the intercept is set to zero. intercept\_ is of shape (1,) when the given problem is binary. In particular, when multi\_class='multinomial', intercept\_corresponds to outcome 1 (True) and -intercept\_corresponds to outcome 0 (False).

**n\_iter\_** [array, shape (n\_classes,) or (1, )] Actual number of iterations for all classes. If binary or multinomial, it returns only 1 element. For liblinear solver, only the maximum number of iteration across all classes is given.

Changed in version 0.20: In SciPy <= 1.0.0 the number of lbfgs iterations may exceed max\_iter. n\_iter\_will now report at most max\_iter.

#### See also:

**SGDClassifier** incrementally trained logistic regression (when given the parameter loss="log"). **LogisticRegressionCV** Logistic regression with built-in cross validation

## **Notes**

The underlying C implementation uses a random number generator to select features when fitting the model. It is thus not uncommon, to have slightly different results for the same input data. If that happens, try with a smaller tol parameter.

Predict output may not match that of standalone liblinear in certain cases. See *differences from liblinear* in the narrative documentation.

## References

LIBLINEAR - A Library for Large Linear Classification https://www.csie.ntu.edu.tw/~cjlin/liblinear/

SAG – Mark Schmidt, Nicolas Le Roux, and Francis Bach Minimizing Finite Sums with the Stochastic Average Gradient https://hal.inria.fr/hal-00860051/document

- SAGA Defazio, A., Bach F. & Lacoste-Julien S. (2014). SAGA: A Fast Incremental Gradient Method With Support for Non-Strongly Convex Composite Objectives https://arxiv.org/abs/1407.0202
- Hsiang-Fu Yu, Fang-Lan Huang, Chih-Jen Lin (2011). Dual coordinate descent methods for logistic regression and maximum entropy models. Machine Learning 85(1-2):41-75. https://www.csie.ntu.edu.tw/~cjlin/papers/maxent\_dual.pdf

# **Examples**

## **Methods**

decision_function(self, X)	Predict confidence scores for samples.
densify(self)	Convert coefficient matrix to dense array format.
fit(self, X, y[, sample_weight])	Fit the model according to the given training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict class labels for samples in X.
predict_log_proba(self, X)	Log of probability estimates.
predict_proba(self, X)	Probability estimates.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.
sparsify(self)	Convert coefficient matrix to sparse format.

```
__init__ (self, penalty='l2', dual=False, tol=0.0001, C=1.0, fit_intercept=True, intercept_scaling=1, class_weight=None, random_state=None, solver='warn', max_iter=100, multi_class='warn', verbose=0, warm_start=False, n_jobs=None, l1_ratio=None)
```

## $decision_function(self, X)$

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

# Returns

array, shape=(n\_samples,) if n\_classes == 2 else (n\_samples, n\_classes) Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes [1] where >0 means this class would be predicted.

### densify (self)

Convert coefficient matrix to dense array format.

Converts the <code>coef\_</code> member (back) to a numpy.ndarray. This is the default format of <code>coef\_</code> and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

#### Returns

**self** [estimator]

**fit** (*self*, *X*, *y*, *sample\_weight=None*)

Fit the model according to the given training data.

#### **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training vector, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape (n\_samples,)] Target vector relative to X.

**sample\_weight** [array-like, shape (n\_samples,) optional] Array of weights that are assigned to individual samples. If not provided, then each sample is given unit weight.

New in version 0.17: sample\_weight support to LogisticRegression.

### **Returns**

self [object]

## **Notes**

The SAGA solver supports both float64 and float32 bit arrays.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict class labels for samples in X.

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

#### Returns

C [array, shape [n\_samples]] Predicted class label per sample.

### predict\_log\_proba (self, X)

Log of probability estimates.

The returned estimates for all classes are ordered by the label of classes.

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

# Returns

T [array-like, shape = [n\_samples, n\_classes]] Returns the log-probability of the sample for each class in the model, where classes are ordered as they are in self.classes\_.

# predict\_proba (self, X)

Probability estimates.

The returned estimates for all classes are ordered by the label of classes.

For a multi\_class problem, if multi\_class is set to be "multinomial" the softmax function is used to find the predicted probability of each class. Else use a one-vs-rest approach, i.e calculate the probability of each class assuming it to be positive using the logistic function. and normalize these values across all the classes.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

### **Returns**

T [array-like, shape = [n\_samples, n\_classes]] Returns the probability of the sample for each class in the model, where classes are ordered as they are in self.classes\_.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
    X [array-like, shape = (n_samples, n_features)] Test samples.
    y [array-like, shape = (n_samples) or (n_samples, n_outputs)] True labels for X.
```

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### **Returns**

self

# sparsify(self)

Convert coefficient matrix to sparse format.

Converts the <code>coef\_</code> member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept\_ member is not converted.

# Returns

**self** [estimator]

## **Notes**

For non-sparse models, i.e. when there are not many zeros in  $coef_$ , this may actually *increase* memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with  $(coef_ == 0).sum()$ , must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial\_fit method (if any) will not work until you call densify.

## Examples using sklearn.linear\_model.LogisticRegression

- Compact estimator representations
- Comparison of Calibration of Classifiers
- Probability Calibration curves
- Plot classification probability
- Column Transformer with Mixed Types
- Plot class probabilities calculated by the Voting Classifier
- Feature transformations with ensembles of trees
- Digits Classification Exercise
- Regularization path of L1- Logistic Regression
- Logistic function
- Logistic Regression 3-class Classifier
- Comparing various online solvers
- MNIST classfification using multinomial logistic + L1
- Plot multinomial and One-vs-Rest Logistic Regression
- L1 Penalty and Sparsity in Logistic Regression
- Multiclass sparse logisitic regression on newgroups20
- Classifier Chain
- Restricted Boltzmann Machine features for digit classification
- Feature discretization

# 6.22.10 sklearn.linear\_model.MultiTaskLasso

Multi-task Lasso model trained with L1/L2 mixed-norm as regularizer.

The optimization objective for Lasso is:

```
(1 / (2 * n_samples)) * ||Y - XW||^2_Fro + alpha * ||W||_21
```

Where:

```
||W||_21 = \sum_i \sqrt{\sum_i w_{ij}^2}
```

i.e. the sum of norm of each row.

Read more in the *User Guide*.

## **Parameters**

alpha [float, optional] Constant that multiplies the L1/L2 term. Defaults to 1.0

**fit\_intercept** [boolean] whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

**normalize** [boolean, optional, default False] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use <code>sklearn.preprocessing.StandardScaler</code> before calling fit on an estimator with normalize=False.

copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.

max\_iter [int, optional] The maximum number of iterations

tol [float, optional] The tolerance for the optimization: if the updates are smaller than tol, the optimization code checks the dual gap for optimality and continues until it is smaller than tol.

warm\_start [bool, optional] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.

random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator that selects a random feature to update. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == 'random'.

**selection** [str, default 'cyclic'] If set to 'random', a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to 'random') often leads to significantly faster convergence especially when tol is higher than 1e-4

# Attributes

coef\_ [array, shape (n\_tasks, n\_features)] Parameter vector (W in the cost function formula).
Note that coef\_ stores the transpose of W, W.T.

**intercept**\_ [array, shape (n\_tasks,)] independent term in decision function.

n\_iter\_ [int] number of iterations run by the coordinate descent solver to reach the specified tolerance.

### See also:

MultiTaskLasso Multi-task L1/L2 Lasso with built-in cross-validation

Lasso

MultiTaskElasticNet

### **Notes**

The algorithm used to fit the model is coordinate descent.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

# **Examples**

#### Methods

fit(self, X, y)	Fit MultiTaskElasticNet model with coordinate descent
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
path(X, y[, 11_ratio, eps, n_alphas,])	Compute elastic net path with coordinate descent
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, alpha=1.0, fit_intercept=True, normalize=False, copy_X=True, max_iter=1000, tol=0.0001, warm_start=False, random_state=None, selection='cyclic')
```

## fit (self, X, y)

Fit MultiTaskElasticNet model with coordinate descent

## **Parameters**

```
X [ndarray, shape (n_samples, n_features)] Data
```

y [ndarray, shape (n\_samples, n\_tasks)] Target. Will be cast to X's dtype if necessary

## **Notes**

Coordinate descent is an algorithm that considers each column of data at a time hence it will automatically convert the X input as a Fortran-contiguous numpy array if necessary.

To avoid memory re-allocation it is advised to allocate the initial data in memory directly using that format.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

```
1 / (2 * n_samples) * ||y - Xw||^2_2
+ alpha * l1_ratio * ||w||_1
+ 0.5 * alpha * (1 - l1_ratio) * ||w||^2_2
```

For multi-output tasks it is:

```
(1 / (2 * n_samples)) * ||Y - XW||^Fro_2
+ alpha * 11_ratio * ||W||_21
+ 0.5 * alpha * (1 - 11_ratio) * ||W||_Fro^2
```

#### Where:

```
||W||_21 = \sum_i \sqrt{\sum_i w_{ij}^2}
```

i.e. the sum of norm of each row.

Read more in the User Guide.

## **Parameters**

- **X** [{array-like}, shape (n\_samples, n\_features)] Training data. Pass directly as Fortrancontiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.
- y [ndarray, shape (n\_samples,) or (n\_samples, n\_outputs)] Target values
- **l1\_ratio** [float, optional] float between 0 and 1 passed to elastic net (scaling between 11 and 12 penalties). l1\_ratio=1 corresponds to the Lasso
- eps [float] Length of the path. eps=1e-3 means that alpha\_min / alpha\_max =
  1e-3
- **n alphas** [int, optional] Number of alphas along the regularization path
- **alphas** [ndarray, optional] List of alphas where to compute the models. If None alphas are set automatically
- precompute [True | False | 'auto' | array-like] Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument.
- $\mathbf{X}\mathbf{y}$  [array-like, optional]  $\mathbf{X}\mathbf{y} = \text{np.dot}(\mathbf{X}.\mathbf{T}, \mathbf{y})$  that can be precomputed. It is useful only when the Gram matrix is precomputed.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten
- coef\_init [array, shape (n\_features, ) | None] The initial values of the coefficients.

verbose [bool or integer] Amount of verbosity.

**return n iter** [bool] whether to return the number of iterations or not.

**positive** [bool, default False] If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).

**check\_input** [bool, default True] Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check\_input=False.

\*\*params [kwargs] keyword arguments passed to the coordinate descent solver.

#### Returns

alphas [array, shape (n\_alphas,)] The alphas along the path where models are computed.

**coefs** [array, shape (n\_features, n\_alphas) or (n\_outputs, n\_features, n\_alphas)] Coefficients along the path.

**dual\_gaps** [array, shape (n\_alphas,)] The dual gaps at the end of the optimization for each alpha.

**n\_iters** [array-like, shape (n\_alphas,)] The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return\_n\_iter is set to True).

#### See also:

MultiTaskElasticNet
MultiTaskElasticNetCV
ElasticNet
ElasticNetCV

#### **Notes**

For an example, see examples/linear\_model/plot\_lasso\_coordinate\_descent\_path.py.

# predict (self, X)

Predict using the linear model

# **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

#### Returns

C [array, shape (n samples,)] Returns predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

# **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n samples) or (n samples, n outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### **Returns**

**score** [float]  $R^2$  of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## sparse\_coef\_

sparse representation of the fitted coef

## Examples using sklearn.linear model.MultiTaskLasso

• Joint feature selection with multi-task Lasso

# 6.22.11 sklearn.linear\_model.MultiTaskElasticNet

```
 \begin{array}{lll} \textbf{class} \; \textbf{sklearn.linear\_model.MultiTaskElasticNet} \; (alpha=1.0, & l1\_ratio=0.5, \\ & \textit{fit\_intercept=True}, & \textit{normalize=False}, \\ & \textit{copy\_X=True}, \; \textit{max\_iter=1000}, \; \textit{tol=0.0001}, \\ & \textit{warm\_start=False}, & \textit{random\_state=None}, \\ & \textit{selection='cyclic'}) \end{array}
```

Multi-task ElasticNet model trained with L1/L2 mixed-norm as regularizer

The optimization objective for MultiTaskElasticNet is:

```
(1 / (2 * n_samples)) * ||Y - XW||_Fro^2
+ alpha * l1_ratio * ||W||_21
+ 0.5 * alpha * (1 - l1_ratio) * ||W||_Fro^2
```

### Where:

```
|||W||_21 = sum_i sqrt(sum_j w_ij ^ 2)
```

i.e. the sum of norm of each row.

Read more in the User Guide.

# **Parameters**

- **alpha** [float, optional] Constant that multiplies the L1/L2 term. Defaults to 1.0
- **11\_ratio** [float] The ElasticNet mixing parameter, with 0 < 11\_ratio <= 1. For 11\_ratio = 1 the penalty is an L1/L2 penalty. For 11\_ratio = 0 it is an L2 penalty. For 0 < 11\_ratio < 1, the penalty is a combination of L1/L2 and L2.
- **fit\_intercept** [boolean] whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).
- normalize [boolean, optional, default False] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- max\_iter [int, optional] The maximum number of iterations
- tol [float, optional] The tolerance for the optimization: if the updates are smaller than tol, the optimization code checks the dual gap for optimality and continues until it is smaller than tol.
- warm\_start [bool, optional] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.
- random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator that selects a random feature to update. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == 'random'.
- **selection** [str, default 'cyclic'] If set to 'random', a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to 'random') often leads to significantly faster convergence especially when tol is higher than 1e-4.

#### **Attributes**

- **intercept**\_ [array, shape (n\_tasks,)] Independent term in decision function.
- coef\_ [array, shape (n\_tasks, n\_features)] Parameter vector (W in the cost function formula). If a 1D y is passed in at fit (non multi-task usage), coef\_ is then a 1D array. Note that coef\_ stores the transpose of W, W.T.
- n\_iter\_ [int] number of iterations run by the coordinate descent solver to reach the specified tolerance.

## See also:

MultiTaskElasticNet Multi-task L1/L2 ElasticNet with built-in cross-validation.

**ElasticNet** 

MultiTaskLasso

## **Notes**

The algorithm used to fit the model is coordinate descent.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

# **Examples**

### **Methods**

fit(self, X, y)	Fit MultiTaskElasticNet model with coordinate descent
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
path(X, y[, 11_ratio, eps, n_alphas,])	Compute elastic net path with coordinate descent
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, alpha=1.0, l1_ratio=0.5, fit_intercept=True, normalize=False, copy_X=True, max_iter=1000, tol=0.0001, warm_start=False, random_state=None, selection='cyclic')

fit (self, X, y)
```

Fit MultiTaskElasticNet model with coordinate descent

# **Parameters**

**X** [ndarray, shape (n\_samples, n\_features)] Data

y [ndarray, shape (n\_samples, n\_tasks)] Target. Will be cast to X's dtype if necessary

## Notes

Coordinate descent is an algorithm that considers each column of data at a time hence it will automatically convert the X input as a Fortran-contiguous numpy array if necessary.

To avoid memory re-allocation it is advised to allocate the initial data in memory directly using that format.

```
get params (self, deep=True)
```

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

```
1 / (2 * n_samples) * ||y - Xw||^2_2
+ alpha * 11_ratio * ||w||_1
+ 0.5 * alpha * (1 - 11_ratio) * ||w||^2_2
```

### For multi-output tasks it is:

```
(1 / (2 * n_samples)) * ||Y - XW||^Fro_2
+ alpha * 11_ratio * ||W||_21
+ 0.5 * alpha * (1 - 11_ratio) * ||W||_Fro^2
```

# Where:

```
||W||_{21} = \sum_{sum_i \ sqrt{\sum_j w_{ij}^2}}
```

i.e. the sum of norm of each row.

Read more in the *User Guide*.

### **Parameters**

- **X** [{array-like}, shape (n\_samples, n\_features)] Training data. Pass directly as Fortrancontiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.
- y [ndarray, shape (n\_samples,) or (n\_samples, n\_outputs)] Target values
- **11\_ratio** [float, optional] float between 0 and 1 passed to elastic net (scaling between 11 and 12 penalties). 11\_ratio=1 corresponds to the Lasso
- **eps** [float] Length of the path. eps=1e-3 means that alpha\_min / alpha\_max = 1e-3
- **n alphas** [int, optional] Number of alphas along the regularization path
- **alphas** [ndarray, optional] List of alphas where to compute the models. If None alphas are set automatically
- **precompute** [True | False | 'auto' | array-like] Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument.
- $\mathbf{X}\mathbf{y}$  [array-like, optional]  $\mathbf{X}\mathbf{y} = \text{np.dot}(\mathbf{X}.\mathbf{T}, \mathbf{y})$  that can be precomputed. It is useful only when the Gram matrix is precomputed.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- **coef\_init** [array, shape (n\_features, ) | None] The initial values of the coefficients.

**verbose** [bool or integer] Amount of verbosity.

- **return n iter** [bool] whether to return the number of iterations or not.
- **positive** [bool, default False] If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).

**check\_input** [bool, default True] Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check\_input=False.

\*\*params [kwargs] keyword arguments passed to the coordinate descent solver.

## Returns

**alphas** [array, shape (n\_alphas,)] The alphas along the path where models are computed.

**coefs** [array, shape (n\_features, n\_alphas) or (n\_outputs, n\_features, n\_alphas)] Coefficients along the path.

**dual\_gaps** [array, shape (n\_alphas,)] The dual gaps at the end of the optimization for each alpha.

**n\_iters** [array-like, shape (n\_alphas,)] The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return\_n\_iter is set to True).

### See also:

MultiTaskElasticNet
MultiTaskElasticNetCV
ElasticNet
ElasticNet

### **Notes**

For an example, see examples/linear\_model/plot\_lasso\_coordinate\_descent\_path.py.

## predict (self, X)

Predict using the linear model

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

# Returns

C [array, shape (n\_samples,)] Returns predicted values.

score (self, X, y, sample\_weight=None)

Returns the coefficient of determination  $R^2$  of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

## **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# sparse\_coef\_

sparse representation of the fitted coef\_

# 6.22.12 sklearn.linear\_model.OrthogonalMatchingPursuit

Orthogonal Matching Pursuit model (OMP)

Read more in the User Guide.

# **Parameters**

- **n\_nonzero\_coefs** [int, optional] Desired number of non-zero entries in the solution. If None (by default) this value is set to 10% of n\_features.
- tol [float, optional] Maximum norm of the residual. If not None, overrides n\_nonzero\_coefs.
- **fit\_intercept** [boolean, optional] whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).
- **normalize** [boolean, optional, default True] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use <code>sklearn.preprocessing.StandardScaler</code> before calling fit on an estimator with normalize=False.
- **precompute** [{True, False, 'auto'}, default 'auto'] Whether to use a precomputed Gram and Xy matrix to speed up calculations. Improves performance when *n\_targets* or *n\_samples* is very large. Note that if you already have such matrices, you can pass them directly to the fit method.

#### **Attributes**

**coef**\_ [array, shape (n\_features,) or (n\_targets, n\_features)] parameter vector (w in the formula) **intercept**\_ [float or array, shape (n\_targets,)] independent term in decision function.

**n\_iter\_** [int or array-like] Number of active features across every target.

## See also:

```
orthogonal_mp
orthogonal_mp_gram
lars_path
Lars
LassoLars
decomposition.sparse_encode
OrthogonalMatchingPursuitCV
```

### **Notes**

Orthogonal matching pursuit was introduced in G. Mallat, Z. Zhang, Matching pursuits with time-frequency dictionaries, IEEE Transactions on Signal Processing, Vol. 41, No. 12. (December 1993), pp. 3397-3415. (http://blanche.polytechnique.fr/~mallat/papiers/MallatPursuit93.pdf)

This implementation is based on Rubinstein, R., Zibulevsky, M. and Elad, M., Efficient Implementation of the K-SVD Algorithm using Batch Orthogonal Matching Pursuit Technical Report - CS Technion, April 2008. https://www.cs.technion.ac.il/~ronrubin/Publications/KSVD-OMP-v2.pdf

# **Examples**

```
>>> from sklearn.linear_model import OrthogonalMatchingPursuit
>>> from sklearn.datasets import make_regression
>>> X, y = make_regression(noise=4, random_state=0)
>>> reg = OrthogonalMatchingPursuit().fit(X, y)
>>> reg.score(X, y)
0.9991...
>>> reg.predict(X[:1,])
array([-78.3854...])
```

## **Methods**

Fit the model using X, y as training data.
Get parameters for this estimator.
Predict using the linear model
Returns the coefficient of determination R^2 of the pre-
diction.
Set the parameters of this estimator.

```
__init__(self, n_nonzero_coefs=None, tol=None, fit_intercept=True, normalize=True, precompute='auto')

fit (self, X, y)
```

Fit the model using X, y as training data.

## **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data.
- y [array-like, shape (n\_samples,) or (n\_samples, n\_targets)] Target values. Will be cast to X's dtype if necessary

#### Returns

self [object] returns an instance of self.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict using the linear model

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

### Returns

C [array, shape (n samples,)] Returns predicted values.

```
score (self, X, y, sample weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares  $((y_true - y_pred) ** 2).sum()$  and v is the total sum of squares  $((y_true - y_true.mean()) ** 2).sum()$ . The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

## **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## Examples using sklearn.linear\_model.OrthogonalMatchingPursuit

• Orthogonal Matching Pursuit

# 6.22.13 sklearn.linear\_model.PassiveAggressiveClassifier

```
class sklearn.linear_model.PassiveAggressiveClassifier (C=1.0,
                                                                                  fit_intercept=True,
                                                                       max_iter=1000,
                                                                                          tol=0.001,
                                                                       early_stopping=False,
                                                                       validation_fraction=0.1,
                                                                       n_{iter}_{no}_{change}=5,
                                                                                         verbose=0,
                                                                       shuffle=True,
                                                                                      n\_jobs=None.
                                                                       loss='hinge',
                                                                       random state=None,
                                                                       warm_start=False,
                                                                       class_weight=None,
                                                                                               aver-
                                                                       age=False)
```

Passive Aggressive Classifier

Read more in the User Guide.

## **Parameters**

- **C** [float] Maximum step size (regularization). Defaults to 1.0.
- **fit\_intercept** [bool, default=False] Whether the intercept should be estimated or not. If False, the data is assumed to be already centered.
- max\_iter [int, optional (default=1000)] The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the fit method, and not the partial\_fit.

New in version 0.19.

**tol** [float or None, optional (default=1e-3)] The stopping criterion. If it is not None, the iterations will stop when (loss > previous\_loss - tol).

New in version 0.19.

early\_stopping [bool, default=False] Whether to use early stopping to terminate training when validation. score is not improving. If set to True, it will automatically set aside a stratified fraction of training data as validation and terminate training when validation score is not improving by at least tol for n\_iter\_no\_change consecutive epochs.

New in version 0.20.

**validation\_fraction** [float, default=0.1] The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if early\_stopping is True.

New in version 0.20.

**n\_iter\_no\_change** [int, default=5] Number of iterations with no improvement to wait before early stopping.

New in version 0.20.

**shuffle** [bool, default=True] Whether or not the training data should be shuffled after each epoch.

verbose [integer, optional] The verbosity level

- **loss** [string, optional] The loss function to be used: hinge: equivalent to PA-I in the reference paper. squared\_hinge: equivalent to PA-II in the reference paper.
- n\_jobs [int or None, optional (default=None)] The number of CPUs to use to do the OVA (One Versus All, for multi-class problems) computation. None means 1 unless in a joblib. parallel\_backend context. -1 means using all processors. See Glossary for more details.
- random\_state [int, RandomState instance or None, optional, default=None] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- warm\_start [bool, optional] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.

Repeatedly calling fit or partial\_fit when warm\_start is True can result in a different solution than when calling fit a single time because of the way the data is shuffled.

**class\_weight** [dict, {class\_label: weight} or "balanced" or None, optional] Preset for the class\_weight fit parameter.

Weights associated with classes. If not given, all classes are supposed to have weight one.

The "balanced" mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as  $n_{samples} / (n_{classes} * np. bincount(y))$ 

New in version 0.17: parameter *class\_weight* to automatically weight samples.

**average** [bool or int, optional] When set to True, computes the averaged SGD weights and stores the result in the <code>coef\_</code> attribute. If set to an int greater than 1, averaging will begin once the total number of samples seen reaches average. So average=10 will begin averaging after seeing 10 samples.

New in version 0.19: parameter average to use weights averaging in SGD

# **Attributes**

**coef**\_ [array, shape = [1, n\_features] if n\_classes == 2 else [n\_classes, n\_features]] Weights assigned to the features.

 $intercept_{-}$  [array, shape = [1] if n\_classes == 2 else [n\_classes]] Constants in decision function.

**n\_iter\_** [int] The actual number of iterations to reach the stopping criterion. For multiclass fits, it is the maximum over every binary fit.

# See also:

SGDClassifier

Perceptron

### References

Online Passive-Aggressive Algorithms <a href="http://jmlr.csail.mit.edu/papers/volume7/crammer06a/crammer06a.pdf">http://jmlr.csail.mit.edu/papers/volume7/crammer06a/crammer06a.pdf</a> K. Crammer, O. Dekel, J. Keshat, S. Shalev-Shwartz, Y. Singer - JMLR (2006)

# **Examples**

```
>>> from sklearn.linear_model import PassiveAggressiveClassifier
>>> from sklearn.datasets import make_classification
```

#### **Methods**

decision_function(self, X)	Predict confidence scores for samples.
densify(self)	Convert coefficient matrix to dense array format.
fit(self, X, y[, coef_init, intercept_init])	Fit linear model with Passive Aggressive algorithm.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X, y[, classes])</pre>	Fit linear model with Passive Aggressive algorithm.
predict(self, X)	Predict class labels for samples in X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*args, \*\*kwargs)	
sparsify(self)	Convert coefficient matrix to sparse format.

```
__init___(self, C=1.0, fit_intercept=True, max_iter=1000, tol=0.001, early_stopping=False, val-
idation_fraction=0.1, n_iter_no_change=5, shuffle=True, verbose=0, loss='hinge',
n_jobs=None, random_state=None, warm_start=False, class_weight=None, aver-
age=False)
```

# $decision_function(self, X)$

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

#### **Parameters**

 $\textbf{X} \ [\text{array\_like or sparse matrix}, \text{shape } (\text{n\_samples}, \text{n\_features})] \ Samples.$ 

### Returns

array, shape=(n\_samples,) if n\_classes == 2 else (n\_samples, n\_classes) Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes\_[1] where >0 means this class would be predicted.

## densify (self)

Convert coefficient matrix to dense array format.

Converts the <code>coef\_</code> member (back) to a numpy.ndarray. This is the default format of <code>coef\_</code> and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

#### **Returns**

**self** [estimator]

fit (self, X, y, coef\_init=None, intercept\_init=None)

Fit linear model with Passive Aggressive algorithm.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training data

y [numpy array of shape [n\_samples]] Target values

**coef\_init** [array, shape = [n\_classes,n\_features]] The initial coefficients to warm-start the optimization.

**intercept\_init** [array, shape = [n\_classes]] The initial intercept to warm-start the optimization.

#### Returns

self [returns an instance of self.]

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

partial\_fit (self, X, y, classes=None)

Fit linear model with Passive Aggressive algorithm.

#### **Parameters**

X [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Subset of the training data

y [numpy array of shape [n\_samples]] Subset of the target values

classes [array, shape = [n\_classes]] Classes across all calls to partial\_fit. Can be obtained
by via np.unique(y\_all), where y\_all is the target vector of the entire dataset. This
argument is required for the first call to partial\_fit and can be omitted in the subsequent
calls. Note that y doesn't need to contain all labels in classes.

# Returns

**self** [returns an instance of self.]

# predict (self, X)

Predict class labels for samples in X.

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

### Returns

C [array, shape [n\_samples]] Predicted class label per sample.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

#### sparsify (self)

Convert coefficient matrix to sparse format.

Converts the <code>coef\_</code> member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept\_ member is not converted.

## Returns

**self** [estimator]

## **Notes**

For non-sparse models, i.e. when there are not many zeros in  $coef_$ , this may actually *increase* memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with  $(coef_ == 0).sum()$ , must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial\_fit method (if any) will not work until you call densify.

## Examples using sklearn.linear\_model.PassiveAggressiveClassifier

- Out-of-core classification of text documents
- Comparing various online solvers
- · Classification of text documents using sparse features

# 6.22.14 sklearn.linear\_model.PassiveAggressiveRegressor

 $\begin{array}{c} \textbf{class} \text{ sklearn.linear\_model.PassiveAggressiveRegressor} (\textit{C=1.0}, & \textit{fit\_intercept=True}, \\ & \textit{max\_iter=1000}, & \textit{tol=0.001}, \\ & \textit{early\_stopping=False}, \\ & \textit{validation\_fraction=0.1}, \\ & \textit{n\_iter\_no\_change=5}, & \textit{shuf-fle=True}, & \textit{verbose=0}, \\ & \textit{loss='epsilon\_insensitive'}, & \textit{epsilon=0.1}, & \textit{random\_state=None}, \\ & \textit{warm\_start=False}, & \textit{average=False}) \end{array}$ 

Passive Aggressive Regressor

Read more in the *User Guide*.

#### **Parameters**

- C [float] Maximum step size (regularization). Defaults to 1.0.
- **fit\_intercept** [bool] Whether the intercept should be estimated or not. If False, the data is assumed to be already centered. Defaults to True.
- max\_iter [int, optional (default=1000)] The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the fit method, and not the partial\_fit. New in version 0.19.
- **tol** [float or None, optional (default=1e-3)] The stopping criterion. If it is not None, the iterations will stop when (loss > previous\_loss tol).

New in version 0.19.

**early\_stopping** [bool, default=False] Whether to use early stopping to terminate training when validation. score is not improving. If set to True, it will automatically set aside a fraction of training data as validation and terminate training when validation score is not improving by at least tol for n\_iter\_no\_change consecutive epochs.

New in version 0.20.

**validation\_fraction** [float, default=0.1] The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if early\_stopping is True.

New in version 0.20.

**n\_iter\_no\_change** [int, default=5] Number of iterations with no improvement to wait before early stopping.

New in version 0.20.

**shuffle** [bool, default=True] Whether or not the training data should be shuffled after each epoch.

verbose [integer, optional] The verbosity level

- **loss** [string, optional] The loss function to be used: epsilon\_insensitive: equivalent to PA-I in the reference paper. squared\_epsilon\_insensitive: equivalent to PA-II in the reference paper.
- **epsilon** [float] If the difference between the current prediction and the correct label is below this threshold, the model is not updated.
- **random\_state** [int, RandomState instance or None, optional, default=None] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is

the random number generator; If None, the random number generator is the RandomState instance used by np.random.

warm\_start [bool, optional] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.

Repeatedly calling fit or partial\_fit when warm\_start is True can result in a different solution than when calling fit a single time because of the way the data is shuffled.

average [bool or int, optional] When set to True, computes the averaged SGD weights and stores the result in the coef\_ attribute. If set to an int greater than 1, averaging will begin once the total number of samples seen reaches average. So average=10 will begin averaging after seeing 10 samples.

New in version 0.19: parameter average to use weights averaging in SGD

#### **Attributes**

**coef**\_ [array, shape = [1, n\_features] if n\_classes == 2 else [n\_classes, n\_features]] Weights assigned to the features.

 $intercept_{-}$  [array, shape = [1] if n\_classes == 2 else [n\_classes]] Constants in decision function.

**n\_iter\_** [int] The actual number of iterations to reach the stopping criterion.

## See also:

**SGDRegressor** 

### References

Online Passive-Aggressive Algorithms <a href="http://jmlr.csail.mit.edu/papers/volume7/crammer06a/crammer06a.pdf">http://jmlr.csail.mit.edu/papers/volume7/crammer06a/crammer06a.pdf</a>> K. Crammer, O. Dekel, J. Keshat, S. Shalev-Shwartz, Y. Singer - JMLR (2006)

# **Examples**

```
>>> from sklearn.linear_model import PassiveAggressiveRegressor
>>> from sklearn.datasets import make_regression
```

## **Methods**

densify(self)	Convert coefficient matrix to dense array format.
fit(self, X, y[, coef_init, intercept_init])	Fit linear model with Passive Aggressive algorithm.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
partial_fit(self, X, y)	Fit linear model with Passive Aggressive algorithm.
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*args, \*\*kwargs)	
sparsify(self)	Convert coefficient matrix to sparse format.

\_\_init\_\_ (self, C=1.0, fit\_intercept=True, max\_iter=1000, tol=0.001, early\_stopping=False, validation\_fraction=0.1, n\_iter\_no\_change=5, shuffle=True, verbose=0, loss='epsilon\_insensitive', epsilon=0.1, random\_state=None, warm\_start=False, average=False)

# densify(self)

Convert coefficient matrix to dense array format.

Converts the <code>coef\_</code> member (back) to a numpy.ndarray. This is the default format of <code>coef\_</code> and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

#### Returns

**self** [estimator]

fit (self, X, y, coef\_init=None, intercept\_init=None)

Fit linear model with Passive Aggressive algorithm.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training data

y [numpy array of shape [n\_samples]] Target values

 $coef\_init$  [array, shape = [n\_features]] The initial coefficients to warm-start the optimization.

**intercept\_init** [array, shape = [1]] The initial intercept to warm-start the optimization.

#### **Returns**

**self** [returns an instance of self.]

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# partial\_fit (self, X, y)

Fit linear model with Passive Aggressive algorithm.

### **Parameters**

**X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Subset of training data

y [numpy array of shape [n\_samples]] Subset of target values

## Returns

**self** [returns an instance of self.]

## predict (self, X)

Predict using the linear model

### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)]

#### Returns

array, shape (n\_samples,) Predicted target values per element in X.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n samples fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses <code>multioutput='uniform\_average'</code>).

# sparsify(self)

Convert coefficient matrix to sparse format.

Converts the coef\_ member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept\_ member is not converted.

# Returns

self [estimator]

### **Notes**

For non-sparse models, i.e. when there are not many zeros in coef, this may actually *increase* memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with (coef == 0). sum(), must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial\_fit method (if any) will not work until you call densify.

# 6.22.15 sklearn.linear\_model.Perceptron

```
 \begin{array}{llll} \textbf{class} & \texttt{sklearn.linear\_model.Perceptron} \ (penalty=None, & alpha=0.0001, & fit\_intercept=True, \\ & max\_iter=1000, & tol=0.001, & shuffle=True, & ver-\\ & bose=0, & eta0=1.0, & n\_jobs=None, & random\_state=0, \\ & early\_stopping=False, & validation\_fraction=0.1, \\ & n\_iter\_no\_change=5, & class\_weight=None, \\ & warm\_start=False) \end{array}
```

Read more in the *User Guide*.

#### **Parameters**

**penalty** [None, '12' or '11' or 'elasticnet'] The penalty (aka regularization term) to be used. Defaults to None.

**alpha** [float] Constant that multiplies the regularization term if regularization is used. Defaults to 0.0001

**fit\_intercept** [bool] Whether the intercept should be estimated or not. If False, the data is assumed to be already centered. Defaults to True.

max\_iter [int, optional (default=1000)] The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the fit method, and not the partial\_fit. New in version 0.19.

**tol** [float or None, optional (default=1e-3)] The stopping criterion. If it is not None, the iterations will stop when (loss > previous\_loss - tol).

New in version 0.19.

**shuffle** [bool, optional, default True] Whether or not the training data should be shuffled after each epoch.

verbose [integer, optional] The verbosity level

**eta0** [double] Constant by which the updates are multiplied. Defaults to 1.

- n\_jobs [int or None, optional (default=None)] The number of CPUs to use to do the OVA (One
   Versus All, for multi-class problems) computation. None means 1 unless in a joblib.
   parallel\_backend context. -1 means using all processors. See Glossary for more
   details.
- random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- **early\_stopping** [bool, default=False] Whether to use early stopping to terminate training when validation. score is not improving. If set to True, it will automatically set aside a stratified

fraction of training data as validation and terminate training when validation score is not improving by at least tol for n\_iter\_no\_change consecutive epochs.

New in version 0.20.

**validation\_fraction** [float, default=0.1] The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if early\_stopping is True.

New in version 0.20.

**n\_iter\_no\_change** [int, default=5] Number of iterations with no improvement to wait before early stopping.

New in version 0.20.

**class\_weight** [dict, {class\_label: weight} or "balanced" or None, optional] Preset for the class\_weight fit parameter.

Weights associated with classes. If not given, all classes are supposed to have weight one.

The "balanced" mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as  $n_{samples} / (n_{classes} * np. bincount(y))$ 

warm\_start [bool, optional] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.

### Attributes

**coef**\_ [array, shape = [1, n\_features] if n\_classes == 2 else [n\_classes, n\_features]] Weights assigned to the features.

**intercept** [array, shape = [1] if  $n_{classes} == 2$  else  $[n_{classes}]$  Constants in decision function.

n\_iter\_ [int] The actual number of iterations to reach the stopping criterion. For multiclass fits,
it is the maximum over every binary fit.

### See also:

**SGDClassifier** 

### **Notes**

Perceptron is a classification algorithm which shares the same underlying implementation with SGDClassifier. In fact, Perceptron() is equivalent to SGDClassifier(loss="perceptron", eta0=1, learning\_rate="constant", penalty=None).

### References

https://en.wikipedia.org/wiki/Perceptron and references therein.

# **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.linear_model import Perceptron
>>> X, y = load_digits(return_X_y=True)
>>> clf = Perceptron(tol=1e-3, random_state=0)
>>> clf.fit(X, y)
```

```
Perceptron(alpha=0.0001, class_weight=None, early_stopping=False, eta0=1.0, fit_intercept=True, max_iter=1000, n_iter_no_change=5, n_jobs=None, penalty=None, random_state=0, shuffle=True, tol=0.001, validation_fraction=0.1, verbose=0, warm_start=False)
>>> clf.score(X, y)
0.939...
```

### **Methods**

decision_function(self, X)	Predict confidence scores for samples.
densify(self)	Convert coefficient matrix to dense array format.
fit(self, X, y[, coef_init, intercept_init,])	Fit linear model with Stochastic Gradient Descent.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X, y[, classes, sample_weight])</pre>	Perform one epoch of stochastic gradient descent on
	given samples.
predict(self, X)	Predict class labels for samples in X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*args, \*\*kwargs)	
sparsify(self)	Convert coefficient matrix to sparse format.

\_\_init\_\_ (self, penalty=None, alpha=0.0001, fit\_intercept=True, max\_iter=1000, tol=0.001, shuf-fle=True, verbose=0, eta0=1.0, n\_jobs=None, random\_state=0, early\_stopping=False, validation\_fraction=0.1, n\_iter\_no\_change=5, class\_weight=None, warm\_start=False)

# $decision_function(self, X)$

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

## Returns

array, shape=(n\_samples,) if n\_classes == 2 else (n\_samples, n\_classes) Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes\_[1] where >0 means this class would be predicted.

### densify (self)

Convert coefficient matrix to dense array format.

Converts the <code>coef\_</code> member (back) to a numpy.ndarray. This is the default format of <code>coef\_</code> and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

#### Returns

**self** [estimator]

**fit** (*self*, *X*, *y*, *coef\_init=None*, *intercept\_init=None*, *sample\_weight=None*) Fit linear model with Stochastic Gradient Descent.

#### **Parameters**

X [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training data

y [numpy array, shape (n\_samples,)] Target values

coef\_init [array, shape (n\_classes, n\_features)] The initial coefficients to warm-start the optimization.

intercept\_init [array, shape (n\_classes,)] The initial intercept to warm-start the optimization.

**sample\_weight** [array-like, shape (n\_samples,), optional] Weights applied to individual samples. If not provided, uniform weights are assumed. These weights will be multiplied with class\_weight (passed through the constructor) if class\_weight is specified

### Returns

**self** [returns an instance of self.]

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
partial_fit (self, X, y, classes=None, sample_weight=None)
```

Perform one epoch of stochastic gradient descent on given samples.

Internally, this method uses max\_iter = 1. Therefore, it is not guaranteed that a minimum of the cost function is reached after calling it once. Matters such as objective convergence and early stopping should be handled by the user.

### **Parameters**

- X [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Subset of the training data
- y [numpy array, shape (n\_samples,)] Subset of the target values
- classes [array, shape (n\_classes,)] Classes across all calls to partial\_fit. Can be obtained by via np.unique(y\_all), where y\_all is the target vector of the entire dataset. This argument is required for the first call to partial\_fit and can be omitted in the subsequent calls. Note that y doesn't need to contain all labels in classes.
- **sample\_weight** [array-like, shape (n\_samples,), optional] Weights applied to individual samples. If not provided, uniform weights are assumed.

#### **Returns**

**self** [returns an instance of self.]

## predict (self, X)

Predict class labels for samples in X.

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

## Returns

C [array, shape [n\_samples]] Predicted class label per sample.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

## sparsify(self)

Convert coefficient matrix to sparse format.

Converts the coef\_member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept member is not converted.

#### Returns

**self** [estimator]

#### **Notes**

For non-sparse models, i.e. when there are not many zeros in coef, this may actually *increase* memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with (coef == 0). sum(), must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial\_fit method (if any) will not work until you call densify.

## Examples using sklearn.linear\_model.Perceptron

- Out-of-core classification of text documents
- Comparing various online solvers
- Classification of text documents using sparse features

## 6.22.16 sklearn.linear\_model.RANSACRegressor

RANSAC (RANdom SAmple Consensus) algorithm.

RANSAC is an iterative algorithm for the robust estimation of parameters from a subset of inliers from the complete data set. More information can be found in the general documentation of linear models.

A detailed description of the algorithm can be found in the documentation of the linear\_model sub-package. Read more in the *User Guide*.

### **Parameters**

**base\_estimator** [object, optional] Base estimator object which implements the following methods:

- fit (X, y): Fit model to given training data and target values.
- score (X, y): Returns the mean accuracy on the given test data, which is used for the stop criterion defined by stop\_score. Additionally, the score is used to decide which of two equally large consensus sets is chosen as the better one.
- predict (X): Returns predicted values using the linear model, which is used to compute residual error using loss function.

If base\_estimator is None, then base\_estimator=sklearn.linear\_model. LinearRegression() is used for target values of dtype float.

Note that the current implementation only supports regression estimators.

- min\_samples [int (>= 1) or float ([0, 1]), optional] Minimum number of samples chosen randomly from original data. Treated as an absolute number of samples for min\_samples >= 1, treated as a relative number ceil(min\_samples \* X. shape[0]) for min\_samples < 1. This is typically chosen as the minimal number of samples necessary to estimate the given base\_estimator. By default a sklearn. linear\_model.LinearRegression() estimator is assumed and min\_samples is chosen as X.shape[1] + 1.
- **residual\_threshold** [float, optional] Maximum residual for a data sample to be classified as an inlier. By default the threshold is chosen as the MAD (median absolute deviation) of the target values *y*.
- **is\_data\_valid** [callable, optional] This function is called with the randomly selected data before the model is fitted to it: is\_data\_valid(X, y). If its return value is False the current randomly chosen sub-sample is skipped.
- is\_model\_valid [callable, optional] This function is called with the estimated model and the randomly selected data: is\_model\_valid(model, X, y). If its return value is False the current randomly chosen sub-sample is skipped. Rejecting samples with this function is computationally costlier than with is\_data\_valid. is\_model\_valid should therefore only be used if the estimated model is needed for making the rejection decision.
- max trials [int, optional] Maximum number of iterations for random sample selection.
- max\_skips [int, optional] Maximum number of iterations that can be skipped due to finding zero inliers or invalid data defined by is\_data\_valid or invalid models defined by is\_model\_valid.

New in version 0.19.

- **stop\_n\_inliers** [int, optional] Stop iteration if at least this number of inliers are found.
- **stop\_score** [float, optional] Stop iteration if score is greater equal than this threshold.
- **stop\_probability** [float in range [0, 1], optional] RANSAC iteration stops if at least one outlier-free set of the training data is sampled in RANSAC. This requires to generate at least N samples (iterations):

```
\mathbb{N} >= \log(1 - \text{probability}) / \log(1 - e **m)
```

where the probability (confidence) is typically set to high value such as 0.99 (the default) and e is the current fraction of inliers w.r.t. the total number of samples.

**loss** [string, callable, optional, default "absolute\_loss"] String inputs, "absolute\_loss" and "squared\_loss" are supported which find the absolute loss and squared loss per sample respectively.

If loss is a callable, then it should be a function that takes two arrays as inputs, the true and predicted value and returns a 1-D array with the i-th value of the array corresponding to the loss on X[i].

If the loss on a sample is greater than the residual\_threshold, then this sample is classified as an outlier.

random\_state [int, RandomState instance or None, optional, default None] The generator used to initialize the centers. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

### **Attributes**

```
estimator_ [object] Best fitted model (copy of the base_estimator object).
```

n\_trials\_ [int] Number of random selection trials until one of the stop criteria is met. It is always <= max\_trials.</pre>

inlier\_mask\_ [bool array of shape [n\_samples]] Boolean mask of inliers classified as True.

**n\_skips\_no\_inliers\_** [int] Number of iterations skipped due to finding zero inliers.

New in version 0.19.

n\_skips\_invalid\_data\_ [int] Number of iterations skipped due to invalid data defined by is\_data\_valid.

New in version 0.19.

n\_skips\_invalid\_model\_ [int] Number of iterations skipped due to an invalid model defined by is\_model\_valid.

New in version 0.19.

#### References

[R80ce5b25cf9d-1], [R80ce5b25cf9d-2], [R80ce5b25cf9d-3]

## **Examples**

## **Methods**

fit(self, X, y[, sample_weight])	Fit estimator using RANSAC algorithm.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the estimated model.
score(self, X, y)	Returns the score of the prediction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_ (self, base\_estimator=None, min\_samples=None, residual\_threshold=None, is\_data\_valid=None, is\_model\_valid=None, max\_trials=100, max\_skips=inf, stop\_n\_inliers=inf, stop\_score=inf, stop\_probability=0.99, loss='absolute\_loss', random\_state=None)

fit (self, X, y, sample\_weight=None)

Fit estimator using RANSAC algorithm.

#### **Parameters**

- **X** [array-like or sparse matrix, shape [n\_samples, n\_features]] Training data.
- y [array-like, shape = [n\_samples] or [n\_samples, n\_targets]] Target values.

**sample\_weight** [array-like, shape = [n\_samples]] Individual weights for each sample raises error if sample\_weight is passed and base\_estimator fit method does not support it.

#### Raises

**ValueError** If no valid consensus set could be found. This occurs if is\_data\_valid and is\_model\_valid return False for all max\_trials randomly chosen sub-samples.

#### get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

# predict (self, X)

Predict using the estimated model.

This is a wrapper for estimator\_.predict(X).

## **Parameters**

**X** [numpy array of shape [n\_samples, n\_features]]

### Returns

**y** [array, shape = [n\_samples] or [n\_samples, n\_targets]] Returns predicted values.

### score(self, X, y)

Returns the score of the prediction.

This is a wrapper for estimator\_.score(X, y).

### **Parameters**

X [numpy array or sparse matrix of shape [n\_samples, n\_features]] Training data.

y [array, shape = [n\_samples] or [n\_samples, n\_targets]] Target values.

#### Returns

**z** [float] Score of the prediction.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### Examples using sklearn.linear model.RANSACRegressor

- Robust linear model estimation using RANSAC
- Theil-Sen Regression
- Robust linear estimator fitting

## 6.22.17 sklearn.linear model.Ridge

```
 \begin{array}{lll} \textbf{class} \; \texttt{sklearn.linear\_model.Ridge} \; (alpha=1.0, & \textit{fit\_intercept=True}, & \textit{normalize=False}, \\ & \textit{copy\_X=True}, & \textit{max\_iter=None}, & \textit{tol=0.001}, & \textit{solver='auto'}, \\ & & \textit{random state=None}) \end{array}
```

Linear least squares with 12 regularization.

Minimizes the objective function:

```
||y - Xw||^2_2 + alpha * ||w||^2_2
```

This model solves a regression model where the loss function is the linear least squares function and regularization is given by the 12-norm. Also known as Ridge Regression or Tikhonov regularization. This estimator has built-in support for multi-variate regression (i.e., when y is a 2d-array of shape [n\_samples, n\_targets]).

Read more in the *User Guide*.

## **Parameters**

- **alpha** [{float, array-like}, shape (n\_targets)] Regularization strength; must be a positive float. Regularization improves the conditioning of the problem and reduces the variance of the estimates. Larger values specify stronger regularization. Alpha corresponds to C^-1 in other linear models such as LogisticRegression or LinearSVC. If an array is passed, penalties are assumed to be specific to the targets. Hence they must correspond in number.
- **fit\_intercept** [boolean] Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).
- **normalize** [boolean, optional, default False] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use <code>sklearn.preprocessing.StandardScaler</code> before calling fit on an estimator with normalize=False.
- **copy\_X** [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.

max\_iter [int, optional] Maximum number of iterations for conjugate gradient solver. For 'sparse\_cg' and 'lsqr' solvers, the default value is determined by scipy.sparse.linalg. For 'sag' solver, the default value is 1000.

tol [float] Precision of the solution.

**solver** [{'auto', 'svd', 'cholesky', 'lsqr', 'sparse\_cg', 'sag', 'saga'}] Solver to use in the computational routines:

- 'auto' chooses the solver automatically based on the type of data.
- 'svd' uses a Singular Value Decomposition of X to compute the Ridge coefficients. More stable for singular matrices than 'cholesky'.
- 'cholesky' uses the standard scipy.linalg.solve function to obtain a closed-form solution.
- 'sparse\_cg' uses the conjugate gradient solver as found in scipy.sparse.linalg.cg. As an iterative algorithm, this solver is more appropriate than 'cholesky' for large-scale data (possibility to set tol and max\_iter).
- 'lsqr' uses the dedicated regularized least-squares routine scipy.sparse.linalg.lsqr. It is the fastest and uses an iterative procedure.
- 'sag' uses a Stochastic Average Gradient descent, and 'saga' uses its improved, unbiased version named SAGA. Both methods also use an iterative procedure, and are often faster than other solvers when both n\_samples and n\_features are large. Note that 'sag' and 'saga' fast convergence is only guaranteed on features with approximately the same scale. You can preprocess the data with a scaler from sklearn.preprocessing.

All last five solvers support both dense and sparse data. However, only 'sag' and 'sparse\_cg' supports sparse input when fit\_intercept is True.

New in version 0.17: Stochastic Average Gradient descent solver.

New in version 0.19: SAGA solver.

random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == 'sag'.

New in version 0.17: random\_state to support Stochastic Average Gradient.

#### **Attributes**

**coef**\_ [array, shape (n\_features,) or (n\_targets, n\_features)] Weight vector(s).

intercept\_ [float | array, shape = (n\_targets,)] Independent term in decision function. Set to 0.0
if fit\_intercept = False.

**n\_iter\_** [array or None, shape (n\_targets,)] Actual number of iterations for each target. Available only for sag and lsqr solvers. Other solvers will return None.

New in version 0.17.

### See also:

RidgeClassifier Ridge classifier

**RidgeCV** Ridge regression with built-in cross validation

sklearn.kernel\_ridge.KernelRidge Kernel ridge regression combines ridge regression with the kernel trick

## **Examples**

```
>>> from sklearn.linear_model import Ridge
>>> import numpy as np
>>> n_samples, n_features = 10, 5
>>> rng = np.random.RandomState(0)
>>> y = rng.randn(n_samples)
>>> X = rng.randn(n_samples, n_features)
>>> clf = Ridge(alpha=1.0)
>>> clf.fit(X, y)
Ridge(alpha=1.0, copy_X=True, fit_intercept=True, max_iter=None, normalize=False, random_state=None, solver='auto', tol=0.001)
```

#### **Methods**

fit(self, X, y[, sample_weight])	Fit Ridge regression model
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, alpha=1.0, fit_intercept=True, normalize=False, copy_X=True, max_iter=None, tol=0.001, solver='auto', random_state=None)
```

fit (self, X, y, sample\_weight=None)

Fit Ridge regression model

### **Parameters**

**X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training data

 $\mathbf{y}$  [array-like, shape = [n\_samples] or [n\_samples, n\_targets]] Target values

**sample\_weight** [float or numpy array of shape [n\_samples]] Individual weights for each sample

### Returns

**self** [returns an instance of self.]

### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

#### predict (self, X)

Predict using the linear model

# **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

#### Returns

C [array, shape (n samples,)] Returns predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape =  $(n_samples)$  or  $(n_samples, n_outputs)$ ] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float]  $R^2$  of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# Examples using sklearn.linear\_model.Ridge

- Compressive sensing: tomography reconstruction with L1 prior (Lasso)
- Prediction Latency
- Plot Ridge coefficients as a function of the regularization
- Ordinary Least Squares and Ridge Regression Variance
- Plot Ridge coefficients as a function of the L2 regularization
- Polynomial interpolation
- · HuberRegressor vs Ridge on dataset with strong outliers

## 6.22.18 sklearn.linear model.RidgeClassifier

Classifier using Ridge regression.

Read more in the *User Guide*.

#### **Parameters**

- **alpha** [float] Regularization strength; must be a positive float. Regularization improves the conditioning of the problem and reduces the variance of the estimates. Larger values specify stronger regularization. Alpha corresponds to C^-1 in other linear models such as LogisticRegression or LinearSVC.
- **fit\_intercept** [boolean] Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).
- **normalize** [boolean, optional, default False] This parameter is ignored when fit\_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the 12-norm. If you wish to standardize, please use <code>sklearn.preprocessing.StandardScaler</code> before calling fit on an estimator with normalize=False.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- **max\_iter** [int, optional] Maximum number of iterations for conjugate gradient solver. The default value is determined by scipy.sparse.linalg.
- tol [float] Precision of the solution.
- class\_weight [dict or 'balanced', optional] Weights associated with classes in the form
  {class\_label: weight}. If not given, all classes are supposed to have weight one.
  - The "balanced" mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as  $n_{samples} / (n_{classes} * np. bincount(y))$
- **solver** [{'auto', 'svd', 'cholesky', 'lsqr', 'sparse\_cg', 'sag', 'saga'}] Solver to use in the computational routines:
  - 'auto' chooses the solver automatically based on the type of data.
  - 'svd' uses a Singular Value Decomposition of X to compute the Ridge coefficients. More stable for singular matrices than 'cholesky'.
  - 'cholesky' uses the standard scipy.linalg.solve function to obtain a closed-form solution.
  - 'sparse\_cg' uses the conjugate gradient solver as found in scipy.sparse.linalg.cg. As an iterative algorithm, this solver is more appropriate than 'cholesky' for large-scale data (possibility to set tol and max\_iter).
  - 'lsqr' uses the dedicated regularized least-squares routine scipy.sparse.linalg.lsqr. It is the fastest and uses an iterative procedure.
  - 'sag' uses a Stochastic Average Gradient descent, and 'saga' uses its unbiased and more flexible version named SAGA. Both methods use an iterative procedure, and are often faster than other solvers when both n\_samples and n\_features are large. Note that 'sag' and 'saga' fast convergence is only guaranteed on features with approximately the same scale. You can preprocess the data with a scaler from sklearn.preprocessing.

New in version 0.17: Stochastic Average Gradient descent solver.

New in version 0.19: SAGA solver.

random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == 'sag'.

#### Attributes

**coef**\_ [array, shape (1, n\_features) or (n\_classes, n\_features)] Coefficient of the features in the decision function.

coef\_ is of shape (1, n\_features) when the given problem is binary.

intercept\_ [float | array, shape = (n\_targets,)] Independent term in decision function. Set to 0.0
if fit\_intercept = False.

**n\_iter\_** [array or None, shape (n\_targets,)] Actual number of iterations for each target. Available only for sag and lsqr solvers. Other solvers will return None.

#### See also:

**Ridge** Ridge regression

RidgeClassifierCV Ridge classifier with built-in cross validation

### **Notes**

For multi-class classification, n\_class classifiers are trained in a one-versus-all approach. Concretely, this is implemented by taking advantage of the multi-variate response support in Ridge.

## **Examples**

```
>>> from sklearn.datasets import load_breast_cancer
>>> from sklearn.linear_model import RidgeClassifier
>>> X, y = load_breast_cancer(return_X_y=True)
>>> clf = RidgeClassifier().fit(X, y)
>>> clf.score(X, y)
0.9595...
```

### **Methods**

$decision\_function(self, X)$	Predict confidence scores for samples.
fit(self, X, y[, sample_weight])	Fit Ridge regression model.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict class labels for samples in X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, alpha=1.0, fit_intercept=True, normalize=False, copy_X=True, max_iter=None, tol=0.001, class_weight=None, solver='auto', random_state=None)
```

### decision function (self, X)

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

#### Returns

array, shape=(n\_samples,) if n\_classes == 2 else (n\_samples, n\_classes) Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes\_[1] where >0 means this class would be predicted.

**fit** (*self*, *X*, *y*, *sample\_weight=None*)

Fit Ridge regression model.

#### **Parameters**

```
X [{array-like, sparse matrix}, shape = [n_samples,n_features]] Training data
```

**y** [array-like, shape = [n\_samples]] Target values

sample\_weight [float or numpy array of shape (n\_samples,)] Sample weight.

New in version 0.17: *sample\_weight* support to Classifier.

### Returns

**self** [returns an instance of self.]

### get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

**params** [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict class labels for samples in X.

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

### Returns

C [array, shape [n\_samples]] Predicted class label per sample.

## score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

X [array-like, shape = (n\_samples, n\_features)] Test samples.

 $\mathbf{y}$  [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for  $\mathbf{X}$ .

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### Examples using sklearn.linear model.RidgeClassifier

• Classification of text documents using sparse features

## 6.22.19 sklearn.linear model.SGDClassifier

Linear classifiers (SVM, logistic regression, a.o.) with SGD training.

This estimator implements regularized linear models with stochastic gradient descent (SGD) learning: the gradient of the loss is estimated each sample at a time and the model is updated along the way with a decreasing strength schedule (aka learning rate). SGD allows minibatch (online/out-of-core) learning, see the partial\_fit method. For best results using the default learning rate schedule, the data should have zero mean and unit variance.

This implementation works with data represented as dense or sparse arrays of floating point values for the features. The model it fits can be controlled with the loss parameter; by default, it fits a linear support vector machine (SVM).

The regularizer is a penalty added to the loss function that shrinks model parameters towards the zero vector using either the squared euclidean norm L2 or the absolute norm L1 or a combination of both (Elastic Net). If the parameter update crosses the 0.0 value because of the regularizer, the update is truncated to 0.0 to allow for learning sparse models and achieve online feature selection.

Read more in the *User Guide*.

### **Parameters**

**loss** [str, default: 'hinge'] The loss function to be used. Defaults to 'hinge', which gives a linear SVM.

The possible options are 'hinge', 'log', 'modified\_huber', 'squared\_hinge', 'perceptron', or a regression loss: 'squared\_loss', 'huber', 'epsilon\_insensitive', or 'squared\_epsilon\_insensitive'.

- The 'log' loss gives logistic regression, a probabilistic classifier. 'modified\_huber' is another smooth loss that brings tolerance to outliers as well as probability estimates. 'squared\_hinge' is like hinge but is quadratically penalized. 'perceptron' is the linear loss used by the perceptron algorithm. The other losses are designed for regression but can be useful in classification as well; see SGDRegressor for a description.
- **penalty** [str, 'none', '12', '11', or 'elasticnet'] The penalty (aka regularization term) to be used. Defaults to '12' which is the standard regularizer for linear SVM models. '11' and 'elasticnet' might bring sparsity to the model (feature selection) not achievable with '12'.
- **alpha** [float] Constant that multiplies the regularization term. Defaults to 0.0001 Also used to compute learning\_rate when set to 'optimal'.
- **11\_ratio** [float] The Elastic Net mixing parameter, with 0 <= 11\_ratio <= 1. 11\_ratio=0 corresponds to L2 penalty, 11\_ratio=1 to L1. Defaults to 0.15.
- **fit\_intercept** [bool] Whether the intercept should be estimated or not. If False, the data is assumed to be already centered. Defaults to True.
- max\_iter [int, optional (default=1000)] The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the fit method, and not the partial\_fit. New in version 0.19.
- tol [float or None, optional (default=1e-3)] The stopping criterion. If it is not None, the iterations will stop when (loss > best\_loss tol) for n\_iter\_no\_change consecutive epochs. New in version 0.19.
- **shuffle** [bool, optional] Whether or not the training data should be shuffled after each epoch. Defaults to True.
- verbose [integer, optional] The verbosity level
- epsilon [float] Epsilon in the epsilon-insensitive loss functions; only if loss is 'huber', 'epsilon\_insensitive', or 'squared\_epsilon\_insensitive'. For 'huber', determines the threshold at which it becomes less important to get the prediction exactly right. For epsilon-insensitive, any differences between the current prediction and the correct label are ignored if they are less than this threshold.
- n\_jobs [int or None, optional (default=None)] The number of CPUs to use to do the OVA (One
   Versus All, for multi-class problems) computation. None means 1 unless in a joblib.
   parallel\_backend context. -1 means using all processors. See Glossary for more
   details.
- random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- learning\_rate [string, optional] The learning rate schedule:

```
'constant': eta = eta0
```

**'optimal':** [default] eta = 1.0 / (alpha \* (t + t0)) where t0 is chosen by a heuristic proposed by Leon Bottou.

```
'invscaling': eta = eta0 / pow(t, power_t)
```

'adaptive': eta = eta0, as long as the training keeps decreasing. Each time n\_iter\_no\_change consecutive epochs fail to decrease the training loss by tol or fail to

increase validation score by tol if early\_stopping is True, the current learning rate is divided by 5.

**eta0** [double] The initial learning rate for the 'constant', 'invscaling' or 'adaptive' schedules. The default value is 0.0 as eta0 is not used by the default schedule 'optimal'.

**power\_t** [double] The exponent for inverse scaling learning rate [default 0.5].

**early\_stopping** [bool, default=False] Whether to use early stopping to terminate training when validation score is not improving. If set to True, it will automatically set aside a stratified fraction of training data as validation and terminate training when validation score is not improving by at least tol for n\_iter\_no\_change consecutive epochs.

New in version 0.20.

**validation\_fraction** [float, default=0.1] The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if early\_stopping is True.

New in version 0.20.

**n\_iter\_no\_change** [int, default=5] Number of iterations with no improvement to wait before early stopping.

New in version 0.20.

**class\_weight** [dict, {class\_label: weight} or "balanced" or None, optional] Preset for the class\_weight fit parameter.

Weights associated with classes. If not given, all classes are supposed to have weight one.

The "balanced" mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as  $n_samples / (n_classes * np. bincount(y))$ 

warm\_start [bool, optional] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.

Repeatedly calling fit or partial\_fit when warm\_start is True can result in a different solution than when calling fit a single time because of the way the data is shuffled. If a dynamic learning rate is used, the learning rate is adapted depending on the number of samples already seen. Calling fit resets this counter, while partial\_fit will result in increasing the existing counter.

average [bool or int, optional] When set to True, computes the averaged SGD weights and stores the result in the <code>coef\_</code> attribute. If set to an int greater than 1, averaging will begin once the total number of samples seen reaches average. So <code>average=10</code> will begin averaging after seeing 10 samples.

### **Attributes**

**coef**\_ [array, shape (1, n\_features) if n\_classes == 2 else (n\_classes, n\_features)] Weights assigned to the features.

**intercept**\_ [array, shape (1,) if n\_classes == 2 else (n\_classes,)] Constants in decision function.

**n\_iter\_** [int] The actual number of iterations to reach the stopping criterion. For multiclass fits, it is the maximum over every binary fit.

loss\_function\_ [concrete LossFunction]

### See also:

sklearn.svm.LinearSVC, LogisticRegression, Perceptron

## **Examples**

```
>>> print(clf.predict([[-0.8, -1]]))
[1]
```

#### **Methods**

decision_function(self, X)	Predict confidence scores for samples.
densify(self)	Convert coefficient matrix to dense array format.
fit(self, X, y[, coef_init, intercept_init,])	Fit linear model with Stochastic Gradient Descent.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X, y[, classes, sample_weight])</pre>	Perform one epoch of stochastic gradient descent on
	given samples.
predict(self, X)	Predict class labels for samples in X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*args, \*\*kwargs)	
sparsify(self)	Convert coefficient matrix to sparse format.

```
__init__ (self, loss='hinge', penalty='l2', alpha=0.0001, l1_ratio=0.15, fit_intercept=True, max_iter=1000, tol=0.001, shuffle=True, verbose=0, epsilon=0.1, n_jobs=None, random_state=None, learning_rate='optimal', eta0=0.0, power_t=0.5, early_stopping=False, validation_fraction=0.1, n_iter_no_change=5, class_weight=None, warm_start=False, average=False)
```

### $decision\_function(self, X)$

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

## **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

### Returns

array, shape=(n\_samples,) if n\_classes == 2 else (n\_samples, n\_classes) Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes\_[1] where >0 means this class would be predicted.

### densify (self)

Convert coefficient matrix to dense array format.

Converts the <code>coef\_</code> member (back) to a numpy.ndarray. This is the default format of <code>coef\_</code> and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

#### Returns

**self** [estimator]

**fit** (*self*, *X*, *y*, *coef\_init=None*, *intercept\_init=None*, *sample\_weight=None*) Fit linear model with Stochastic Gradient Descent.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training data

y [numpy array, shape (n\_samples,)] Target values

coef\_init [array, shape (n\_classes, n\_features)] The initial coefficients to warm-start the optimization.

intercept\_init [array, shape (n\_classes,)] The initial intercept to warm-start the optimization.

**sample\_weight** [array-like, shape (n\_samples,), optional] Weights applied to individual samples. If not provided, uniform weights are assumed. These weights will be multiplied with class\_weight (passed through the constructor) if class\_weight is specified

#### Returns

**self** [returns an instance of self.]

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

partial\_fit (self, X, y, classes=None, sample\_weight=None)

Perform one epoch of stochastic gradient descent on given samples.

Internally, this method uses max\_iter = 1. Therefore, it is not guaranteed that a minimum of the cost function is reached after calling it once. Matters such as objective convergence and early stopping should be handled by the user.

#### **Parameters**

X [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Subset of the training data

y [numpy array, shape (n\_samples,)] Subset of the target values

classes [array, shape (n\_classes,)] Classes across all calls to partial\_fit. Can be obtained by via np.unique(y\_all), where y\_all is the target vector of the entire dataset. This argument is required for the first call to partial\_fit and can be omitted in the subsequent calls. Note that y doesn't need to contain all labels in classes.

**sample\_weight** [array-like, shape (n\_samples,), optional] Weights applied to individual samples. If not provided, uniform weights are assumed.

#### Returns

**self** [returns an instance of self.]

## predict (self, X)

Predict class labels for samples in X.

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

#### **Returns**

C [array, shape [n\_samples]] Predicted class label per sample.

### predict\_log\_proba

Log of probability estimates.

This method is only available for log loss and modified Huber loss.

When loss="modified\_huber", probability estimates may be hard zeros and ones, so taking the logarithm is not possible.

See predict\_proba for details.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

#### **Returns**

T [array-like, shape (n\_samples, n\_classes)] Returns the log-probability of the sample for each class in the model, where classes are ordered as they are in self.classes.

### predict\_proba

Probability estimates.

This method is only available for log loss and modified Huber loss.

Multiclass probability estimates are derived from binary (one-vs.-rest) estimates by simple normalization, as recommended by Zadrozny and Elkan.

Binary probability estimates for loss="modified\_huber" are given by  $(\text{clip}(\text{decision\_function}(X), -1, 1) + 1) / 2$ . For other loss functions it is necessary to perform proper probability calibration by wrapping the classifier with sklearn.calibration.CalibratedClassifierCV instead.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)]

#### Returns

**array, shape (n\_samples, n\_classes)** Returns the probability of the sample for each class in the model, where classes are ordered as they are in self.classes\_.

### References

Zadrozny and Elkan, "Transforming classifier scores into multiclass probability estimates", SIGKDD'02, http://www.research.ibm.com/people/z/zadrozny/kdd2002-Transf.pdf

The justification for the formula in the loss="modified\_huber" case is in the appendix B in: http://jmlr.csail.mit.edu/papers/volume2/zhang02c/zhang02c.pdf

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

## sparsify(self)

Convert coefficient matrix to sparse format.

Converts the coef\_member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept\_ member is not converted.

#### Returns

**self** [estimator]

#### **Notes**

For non-sparse models, i.e. when there are not many zeros in  $coef_$ , this may actually *increase* memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with  $(coef_ == 0).sum()$ , must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial\_fit method (if any) will not work until you call densify.

## Examples using sklearn.linear\_model.SGDClassifier

- Model Complexity Influence
- Out-of-core classification of text documents
- Pipelining: chaining a PCA and a logistic regression
- SGD: Maximum margin separating hyperplane
- SGD: Weighted samples
- Comparing various online solvers
- Plot multi-class SGD on the iris dataset
- Early stopping of Stochastic Gradient Descent
- Sample pipeline for text feature extraction and evaluation
- Classification of text documents using sparse features

## 6.22.20 sklearn.linear\_model.SGDRegressor

Linear model fitted by minimizing a regularized empirical loss with SGD

SGD stands for Stochastic Gradient Descent: the gradient of the loss is estimated each sample at a time and the model is updated along the way with a decreasing strength schedule (aka learning rate).

The regularizer is a penalty added to the loss function that shrinks model parameters towards the zero vector using either the squared euclidean norm L2 or the absolute norm L1 or a combination of both (Elastic Net). If the parameter update crosses the 0.0 value because of the regularizer, the update is truncated to 0.0 to allow for learning sparse models and achieve online feature selection.

This implementation works with data represented as dense numpy arrays of floating point values for the features.

Read more in the *User Guide*.

#### **Parameters**

**loss** [str, default: 'squared\_loss'] The loss function to be used. The possible values are 'squared\_loss', 'huber', 'epsilon\_insensitive', or 'squared\_epsilon\_insensitive'

The 'squared\_loss' refers to the ordinary least squares fit. 'huber' modifies 'squared\_loss' to focus less on getting outliers correct by switching from squared to linear loss past a distance of epsilon. 'epsilon\_insensitive' ignores errors less than epsilon and is linear past that; this is the loss function used in SVR. 'squared\_epsilon\_insensitive' is the same but becomes squared loss past a tolerance of epsilon.

- **penalty** [str, 'none', '12', '11', or 'elasticnet'] The penalty (aka regularization term) to be used. Defaults to '12' which is the standard regularizer for linear SVM models. '11' and 'elasticnet' might bring sparsity to the model (feature selection) not achievable with '12'.
- **alpha** [float] Constant that multiplies the regularization term. Defaults to 0.0001 Also used to compute learning\_rate when set to 'optimal'.
- **11\_ratio** [float] The Elastic Net mixing parameter, with 0 <= 11\_ratio <= 1. 11\_ratio=0 corresponds to L2 penalty, 11\_ratio=1 to L1. Defaults to 0.15.
- **fit\_intercept** [bool] Whether the intercept should be estimated or not. If False, the data is assumed to be already centered. Defaults to True.
- max\_iter [int, optional (default=1000)] The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the fit method, and not the partial\_fit. New in version 0.19.
- tol [float or None, optional (default=1e-3)] The stopping criterion. If it is not None, the iterations will stop when (loss > best\_loss tol) for n\_iter\_no\_change consecutive epochs. New in version 0.19.
- **shuffle** [bool, optional] Whether or not the training data should be shuffled after each epoch. Defaults to True.

verbose [integer, optional] The verbosity level.

- **epsilon** [float] Epsilon in the epsilon-insensitive loss functions; only if loss is 'huber', 'epsilon\_insensitive', or 'squared\_epsilon\_insensitive'. For 'huber', determines the threshold at which it becomes less important to get the prediction exactly right. For epsilon-insensitive, any differences between the current prediction and the correct label are ignored if they are less than this threshold.
- random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**learning\_rate** [string, optional] The learning rate schedule:

'constant': eta = eta0

**'optimal':** eta = 1.0 / (alpha \* (t + t0)) where t0 is chosen by a heuristic proposed by Leon Bottou.

'invscaling': [default] eta = eta0 / pow(t, power\_t)

**'adaptive':** eta = eta0, as long as the training keeps decreasing. Each time n\_iter\_no\_change consecutive epochs fail to decrease the training loss by tol or fail to increase validation score by tol if early\_stopping is True, the current learning rate is divided by 5.

**eta0** [double] The initial learning rate for the 'constant', 'invscaling' or 'adaptive' schedules. The default value is 0.01.

**power\_t** [double] The exponent for inverse scaling learning rate [default 0.5].

**early\_stopping** [bool, default=False] Whether to use early stopping to terminate training when validation score is not improving. If set to True, it will automatically set aside a fraction of training data as validation and terminate training when validation score is not improving by at least tol for n\_iter\_no\_change consecutive epochs.

New in version 0.20.

**validation\_fraction** [float, default=0.1] The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if early\_stopping is True.

New in version 0.20.

**n\_iter\_no\_change** [int, default=5] Number of iterations with no improvement to wait before early stopping.

New in version 0.20.

warm\_start [bool, optional] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.

Repeatedly calling fit or partial\_fit when warm\_start is True can result in a different solution than when calling fit a single time because of the way the data is shuffled. If a dynamic learning rate is used, the learning rate is adapted depending on the number of samples already seen. Calling fit resets this counter, while partial\_fit will result in increasing the existing counter.

average [bool or int, optional] When set to True, computes the averaged SGD weights and stores the result in the <code>coef\_</code> attribute. If set to an int greater than 1, averaging will begin once the total number of samples seen reaches average. So <code>average=10</code> will begin averaging after seeing 10 samples.

Attributes

```
coef_ [array, shape (n_features,)] Weights assigned to the features.
```

**intercept**\_ [array, shape (1,)] The intercept term.

average\_coef\_ [array, shape (n\_features,)] Averaged weights assigned to the features.

**average\_intercept\_** [array, shape (1,)] The averaged intercept term.

**n\_iter\_** [int] The actual number of iterations to reach the stopping criterion.

#### See also:

```
Ridge, ElasticNet, Lasso, sklearn.svm.SVR
```

## **Examples**

### **Methods**

densify(self)	Convert coefficient matrix to dense array format.
fit(self, X, y[, coef_init, intercept_init,])	Fit linear model with Stochastic Gradient Descent.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X, y[, sample_weight])</pre>	Perform one epoch of stochastic gradient descent on
	given samples.
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*args, \*\*kwargs)	
sparsify(self)	Convert coefficient matrix to sparse format.

```
__init___(self, loss='squared_loss', penalty='l2', alpha=0.0001, l1_ratio=0.15, fit_intercept=True, max_iter=1000, tol=0.001, shuffle=True, verbose=0, epsilon=0.1, random_state=None, learning_rate='invscaling', eta0=0.01, power_t=0.25, early_stopping=False, validation_fraction=0.1, n_iter_no_change=5, warm_start=False, average=False)
```

## densify(self)

Convert coefficient matrix to dense array format.

Converts the <code>coef\_</code> member (back) to a numpy.ndarray. This is the default format of <code>coef\_</code> and is required for fitting, so calling this method is only required on models that have previously been sparsified;

otherwise, it is a no-op.

#### Returns

**self** [estimator]

**fit** (*self*, *X*, *y*, *coef\_init=None*, *intercept\_init=None*, *sample\_weight=None*) Fit linear model with Stochastic Gradient Descent.

#### **Parameters**

X [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training data

y [numpy array, shape (n\_samples,)] Target values

coef\_init [array, shape (n\_features,)] The initial coefficients to warm-start the optimization.

**intercept\_init** [array, shape (1,)] The initial intercept to warm-start the optimization.

**sample\_weight** [array-like, shape (n\_samples,), optional] Weights applied to individual samples (1. for unweighted).

#### Returns

**self** [returns an instance of self.]

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

```
partial_fit (self, X, y, sample_weight=None)
```

Perform one epoch of stochastic gradient descent on given samples.

Internally, this method uses max\_iter = 1. Therefore, it is not guaranteed that a minimum of the cost function is reached after calling it once. Matters such as objective convergence and early stopping should be handled by the user.

### **Parameters**

X [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Subset of training data

y [numpy array of shape (n\_samples,)] Subset of target values

**sample\_weight** [array-like, shape (n\_samples,), optional] Weights applied to individual samples. If not provided, uniform weights are assumed.

#### Returns

**self** [returns an instance of self.]

### predict (self, X)

Predict using the linear model

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)]

### Returns

array, shape (n\_samples,) Predicted target values per element in X.

```
score (self, X, y, sample weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R<sup>2</sup> is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R<sup>2</sup> score of 0.0.

#### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### **Returns**

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

## sparsify(self)

Convert coefficient matrix to sparse format.

Converts the <code>coef\_</code> member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept\_ member is not converted.

### Returns

**self** [estimator]

## **Notes**

For non-sparse models, i.e. when there are not many zeros in  $coef_$ , this may actually *increase* memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with  $(coef_ == 0).sum()$ , must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial\_fit method (if any) will not work until you call densify.

## Examples using sklearn.linear\_model.SGDRegressor

• Prediction Latency

## 6.22.21 sklearn.linear model.TheilSenRegressor

```
class sklearn.linear_model.TheilSenRegressor (fit\_intercept=True, copy\_X=True, max\_subpopulation=10000.0, n\_subsamples=None, max\_iter=300, tol=0.001, random\_state=None, n\_jobs=None, verbose=False)
```

Theil-Sen Estimator: robust multivariate regression model.

The algorithm calculates least square solutions on subsets with size n\_subsamples of the samples in X. Any value of n\_subsamples between the number of features and samples leads to an estimator with a compromise between robustness and efficiency. Since the number of least square solutions is "n\_samples choose n\_subsamples", it can be extremely large and can therefore be limited with max\_subpopulation. If this limit is reached, the subsets are chosen randomly. In a final step, the spatial median (or L1 median) is calculated of all least square solutions.

Read more in the User Guide.

#### **Parameters**

- **fit\_intercept** [boolean, optional, default True] Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- max\_subpopulation [int, optional, default 1e4] Instead of computing with a set of cardinality 'n choose k', where n is the number of samples and k is the number of subsamples (at least number of features), consider only a stochastic subpopulation of a given maximal size if 'n choose k' is larger than max\_subpopulation. For other than small problem sizes this parameter will determine memory usage and runtime if n\_subsamples is not changed.
- **n\_subsamples** [int, optional, default None] Number of samples to calculate the parameters. This is at least the number of features (plus 1 if fit\_intercept=True) and the number of samples as a maximum. A lower number leads to a higher breakdown point and a low efficiency while a high number leads to a low breakdown point and a high efficiency. If None, take the minimum number of subsamples leading to maximal robustness. If n\_subsamples is set to n\_samples, Theil-Sen is identical to least squares.
- max\_iter [int, optional, default 300] Maximum number of iterations for the calculation of spatial median.
- tol [float, optional, default 1.e-3] Tolerance when calculating spatial median.
- random\_state [int, RandomState instance or None, optional, default None] A random number generator instance to define the state of the random permutations generator. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- **n\_jobs** [int or None, optional (default=None)] Number of CPUs to use during the cross validation. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

**verbose** [boolean, optional, default False] Verbose mode when fitting the model.

#### Attributes

**coef** [array, shape = (n features)] Coefficients of the regression model (median of distribution).

**intercept** [float] Estimated intercept of regression model.

**breakdown** [float] Approximated breakdown point.

**n\_iter\_** [int] Number of iterations needed for the spatial median.

**n\_subpopulation\_** [int] Number of combinations taken into account from 'n choose k', where n is the number of samples and k is the number of subsamples.

### References

 Theil-Sen Estimators in a Multiple Linear Regression Model, 2009 Xin Dang, Hanxiang Peng, Xueqin Wang and Heping Zhang http://home.olemiss.edu/~xdang/papers/MTSE.pdf

# **Examples**

## **Methods**

fit(self, X, y)	Fit linear model.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, fit_intercept=True, copy_X=True, max_subpopulation=10000.0, n_subsamples=None, max_iter=300, tol=0.001, random_state=None, n_jobs=None, verbose=False)
```

#### fit (self, X, y)

Fit linear model.

## **Parameters**

- **X** [numpy array of shape [n samples, n features]] Training data
- y [numpy array of shape [n\_samples]] Target values

## Returns

**self** [returns an instance of self.]

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict using the linear model

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

#### Returns

C [array, shape (n\_samples,)] Returns predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R<sup>2</sup> is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R<sup>2</sup> score of 0.0.

#### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

## Examples using sklearn.linear\_model.TheilSenRegressor

- Theil-Sen Regression
- Robust linear estimator fitting

linear_model.enet_path(X, y[, l1_ratio,])	Compute elastic net path with coordinate descent
linear_model.lars_path(X, y[, Xy, Gram,])	Compute Least Angle Regression or Lasso path using
	LARS algorithm [1]
linear_model.lars_path_gram(Xy, Gram,	lars_path in the sufficient stats mode [1]
n_samples)	
$linear_model.lasso_path(X, y[, eps,])$	Compute Lasso path with coordinate descent
$linear\_model.orthogonal\_mp(X, y[,])$	Orthogonal Matching Pursuit (OMP)
linear_model.orthogonal_mp_gram(Gram, Xy[,	Gram Orthogonal Matching Pursuit (OMP)
])	
linear_model.ridge_regression(X, y, alpha[,	Solve the ridge equation by the method of normal equa-
])	tions.

# 6.22.22 sklearn.linear\_model.enet\_path

```
sklearn.linear_model.enet_path(X, y, ll_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, precompute='auto', Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, check_input=True, **params)
```

Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

```
1 / (2 * n_samples) * ||y - Xw||^2_2
+ alpha * 11_ratio * ||w||_1
+ 0.5 * alpha * (1 - 11_ratio) * ||w||^2_2
```

## For multi-output tasks it is:

```
(1 / (2 * n_samples)) * ||Y - XW||^Fro_2
+ alpha * l1_ratio * ||W||_21
+ 0.5 * alpha * (1 - l1_ratio) * ||W||_Fro^2
```

### Where:

i.e. the sum of norm of each row.

Read more in the User Guide.

### **Parameters**

- **X** [{array-like}, shape (n\_samples, n\_features)] Training data. Pass directly as Fortrancontiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.
- ${f y}$  [ndarray, shape (n\_samples,) or (n\_samples, n\_outputs)] Target values
- **l1\_ratio** [float, optional] float between 0 and 1 passed to elastic net (scaling between 11 and 12 penalties). l1\_ratio=1 corresponds to the Lasso
- eps [float] Length of the path. eps=1e-3 means that alpha\_min / alpha\_max = 1e-3
- **n\_alphas** [int, optional] Number of alphas along the regularization path

- **alphas** [ndarray, optional] List of alphas where to compute the models. If None alphas are set automatically
- **precompute** [True | False | 'auto' | array-like] Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument.
- $\mathbf{X}\mathbf{y}$  [array-like, optional]  $\mathbf{X}\mathbf{y} = \text{np.dot}(\mathbf{X}.\mathbf{T}, \mathbf{y})$  that can be precomputed. It is useful only when the Gram matrix is precomputed.
- copy\_X [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- **coef\_init** [array, shape (n\_features, ) | None] The initial values of the coefficients.

verbose [bool or integer] Amount of verbosity.

return\_n\_iter [bool] whether to return the number of iterations or not.

**positive** [bool, default False] If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).

**check\_input** [bool, default True] Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check\_input=False.

\*\*params [kwargs] keyword arguments passed to the coordinate descent solver.

### Returns

- **alphas** [array, shape (n\_alphas,)] The alphas along the path where models are computed.
- **coefs** [array, shape (n\_features, n\_alphas) or (n\_outputs, n\_features, n\_alphas)] Coefficients along the path.
- **dual\_gaps** [array, shape (n\_alphas,)] The dual gaps at the end of the optimization for each alpha.
- n\_iters [array-like, shape (n\_alphas,)] The number of iterations taken by the coordinate
   descent optimizer to reach the specified tolerance for each alpha. (Is returned when
   return\_n\_iter is set to True).

### See also:

MultiTaskElasticNet
MultiTaskElasticNetCV
ElasticNet
ElasticNetCV

#### **Notes**

For an example, see examples/linear\_model/plot\_lasso\_coordinate\_descent\_path.py.

## Examples using sklearn.linear\_model.enet\_path

• Lasso and Elastic Net

## 6.22.23 sklearn.linear\_model.lars\_path

```
sklearn.linear_model.lars_path (X, y, Xy=None, Gram=None, max\_iter=500, alpha\_min=0, method='lar', copy\_X=True, eps=2.220446049250313e-16, copy\_Gram=True, verbose=0, return\_path=True, return\_n\_iter=False, positive=False)
```

Compute Least Angle Regression or Lasso path using LARS algorithm [1]

The optimization objective for the case method='lasso' is:

```
(1 / (2 * n_samples)) * ||y - Xw||^2_2 + alpha * ||w||_1
```

in the case of method='lars', the objective function is only known in the form of an implicit equation (see discussion in [1])

Read more in the *User Guide*.

#### **Parameters**

**X** [None or array, shape (n\_samples, n\_features)] Input data. Note that if X is None then the Gram matrix must be specified, i.e., cannot be None or False.

Deprecated since version 0.21: The use of X is None in combination with Gram is not None will be removed in v0.23. Use <code>lars\_path\_gram</code> instead.

- y [None or array, shape (n\_samples,)] Input targets.
- **Xy** [array-like, shape (n\_samples,) or (n\_samples, n\_targets), optional] Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.
- **Gram** [None, 'auto', array, shape (n\_features, n\_features), optional] Precomputed Gram matrix (X' \* X), if 'auto', the Gram matrix is precomputed from the given X, if there are more samples than features.

Deprecated since version 0.21: The use of X is None in combination with Gram is not None will be removed in v0.23. Use <code>lars\_path\_gram</code> instead.

- **max\_iter** [integer, optional (default=500)] Maximum number of iterations to perform, set to infinity for no limit.
- **alpha\_min** [float, optional (default=0)] Minimum correlation along the path. It corresponds to the regularization parameter alpha parameter in the Lasso.
- method [{'lar', 'lasso'}, optional (default='lar')] Specifies the returned model. Select 'lar' for Least Angle Regression, 'lasso' for the Lasso.
- copy\_X [bool, optional (default=True)] If False, X is overwritten.
- **eps** [float, optional (default="np.finfo(np.float).eps")] The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems.
- **copy\_Gram** [bool, optional (default=True)] If False, Gram is overwritten.

**verbose** [int (default=0)] Controls output verbosity.

- **return\_path** [bool, optional (default=True)] If return\_path==True returns the entire path, else returns only the last point of the path.
- **return\_n\_iter** [bool, optional (default=False)] Whether to return the number of iterations.
- **positive** [boolean (default=False)] Restrict coefficients to be >= 0. This option is only allowed with method 'lasso'. Note that the model coefficients will not converge to the ordinary-least-squares solution for small values of alpha. Only coefficients up to the smallest alpha

value (alphas\_[alphas\_ > 0.].min() when fit\_path=True) reached by the stepwise Lars-Lasso algorithm are typically in congruence with the solution of the coordinate descent lasso\_path function.

#### Returns

```
alphas [array, shape (n_alphas + 1,)] Maximum of covariances (in absolute value) at each iteration. n_alphas is either max_iter, n_features or the number of nodes in the path with alpha >= alpha_min, whichever is smaller.
```

active [array, shape [n\_alphas]] Indices of active variables at the end of the path.

**coefs** [array, shape (n\_features, n\_alphas + 1)] Coefficients along the path

**n\_iter** [int] Number of iterations run. Returned only if return\_n\_iter is set to True.

#### See also:

```
lars_path_gram
```

lasso\_path

lasso\_path\_gram

LassoLars

Lars

LassoLarsCV

LarsCV

sklearn.decomposition.sparse\_encode

#### References

[1], [2], [3]

## Examples using sklearn.linear\_model.lars\_path

• Lasso path using LARS

## 6.22.24 sklearn.linear\_model.lars path gram

```
sklearn.linear_model.lars_path_gram (Xy, Gram, n_samples, max_iter=500, al-pha_min=0, method='lar', copy_X=True, eps=2.220446049250313e-16, copy_Gram=True, verbose=0, return_path=True, return_n_iter=False, positive=False)
```

lars\_path in the sufficient stats mode [1]

The optimization objective for the case method='lasso' is:

```
(1 / (2 * n_samples)) * ||y - Xw||^2_2 + alpha * ||w||_1
```

in the case of method='lars', the objective function is only known in the form of an implicit equation (see discussion in [1])

Read more in the *User Guide*.

#### **Parameters**

**Xy** [array-like, shape (n\_samples,) or (n\_samples, n\_targets)] Xy = np.dot(X.T, y).

**Gram** [array, shape (n\_features, n\_features)] Gram = np.dot(X.T \* X).

**n\_samples** [integer or float] Equivalent size of sample.

**max\_iter** [integer, optional (default=500)] Maximum number of iterations to perform, set to infinity for no limit.

**alpha\_min** [float, optional (default=0)] Minimum correlation along the path. It corresponds to the regularization parameter alpha parameter in the Lasso.

method [{'lar', 'lasso'}, optional (default='lar')] Specifies the returned model. Select 'lar' for Least Angle Regression, 'lasso' for the Lasso.

copy\_X [bool, optional (default=True)] If False, X is overwritten.

**eps** [float, optional (default="np.finfo(np.float).eps")] The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems.

copy\_Gram [bool, optional (default=True)] If False, Gram is overwritten.

verbose [int (default=0)] Controls output verbosity.

**return\_path** [bool, optional (default=True)] If return\_path==True returns the entire path, else returns only the last point of the path.

**return\_n\_iter** [bool, optional (default=False)] Whether to return the number of iterations.

positive [boolean (default=False)] Restrict coefficients to be >= 0. This option is only allowed with method 'lasso'. Note that the model coefficients will not converge to the ordinary-least-squares solution for small values of alpha. Only coefficients up to the smallest alpha value (alphas\_[alphas\_ > 0.].min() when fit\_path=True) reached by the stepwise Lars-Lasso algorithm are typically in congruence with the solution of the coordinate descent lasso\_path function.

#### Returns

alphas [array, shape (n\_alphas + 1,)] Maximum of covariances (in absolute value) at each iteration. n\_alphas is either max\_iter, n\_features or the number of nodes in the path with alpha >= alpha\_min, whichever is smaller.

active [array, shape [n\_alphas]] Indices of active variables at the end of the path.

 $\pmb{coefs} \;\; [array, shape \; (n\_features, \, n\_alphas + 1)] \; Coefficients \; along \; the \; path$ 

**n iter** [int] Number of iterations run. Returned only if return n iter is set to True.

## See also:

```
lars_path
lasso_path
lasso_path_gram
LassoLars
Lars
Lars
LassoLarsCV
LarsCV
```

#### sklearn.decomposition.sparse encode

#### References

[1], [2], [3]

## 6.22.25 sklearn.linear model.lasso path

```
sklearn.linear_model.lasso_path(X, y, eps=0.001, n_alphas=100, alphas=None, precompute='auto', Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, **params)
```

Compute Lasso path with coordinate descent

The Lasso optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

```
(1 / (2 * n_samples)) * ||y - Xw||^2_2 + alpha * ||w||_1
```

For multi-output tasks it is:

```
(1 / (2 * n_samples)) * ||Y - XW||^2_Fro + alpha * ||W||_21
```

Where:

```
||W||_21 = \sum_{\substack{i \in \mathbb{Z}_2}} w_{ij}^2
```

i.e. the sum of norm of each row.

Read more in the User Guide.

## **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.
- y [ndarray, shape (n\_samples,), or (n\_samples, n\_outputs)] Target values
- eps [float, optional] Length of the path. eps=1e-3 means that alpha\_min / alpha\_max
  = 1e-3
- **n\_alphas** [int, optional] Number of alphas along the regularization path
- **alphas** [ndarray, optional] List of alphas where to compute the models. If None alphas are set automatically
- **precompute** [True | False | 'auto' | array-like] Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument.
- $\mathbf{X}\mathbf{y}$  [array-like, optional]  $\mathbf{X}\mathbf{y} = \text{np.dot}(\mathbf{X}.\mathbf{T}, \mathbf{y})$  that can be precomputed. It is useful only when the Gram matrix is precomputed.
- **copy\_X** [boolean, optional, default True] If True, X will be copied; else, it may be overwritten.
- **coef\_init** [array, shape (n\_features, ) | None] The initial values of the coefficients.
- **verbose** [bool or integer] Amount of verbosity.
- return\_n\_iter [bool] whether to return the number of iterations or not.

**positive** [bool, default False] If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).

\*\*params [kwargs] keyword arguments passed to the coordinate descent solver.

#### Returns

**alphas** [array, shape (n\_alphas,)] The alphas along the path where models are computed.

**coefs** [array, shape (n\_features, n\_alphas) or (n\_outputs, n\_features, n\_alphas)] Coefficients along the path.

**dual\_gaps** [array, shape (n\_alphas,)] The dual gaps at the end of the optimization for each alpha.

**n\_iters** [array-like, shape (n\_alphas,)] The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha.

### See also:

```
lars_path
Lasso
LassoLars
LassoCV
LassoLarsCV
sklearn.decomposition.sparse_encode
```

### **Notes**

For an example, see examples/linear model/plot lasso coordinate descent path.py.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

Note that in certain cases, the Lars solver may be significantly faster to implement this functionality. In particular, linear interpolation can be used to retrieve model coefficients between the values output by lars\_path

## **Examples**

Comparing lasso\_path and lars\_path with interpolation:

```
>>> # Now use lars_path and 1D linear interpolation to compute the
>>> # same path
>>> from sklearn.linear_model import lars_path
>>> alphas, active, coef_path_lars = lars_path(X, y, method='lasso')
>>> from scipy import interpolate
>>> coef_path_continuous = interpolate.interp1d(alphas[::-1],
```

### Examples using sklearn.linear model.lasso path

· Lasso and Elastic Net

# 6.22.26 sklearn.linear\_model.orthogonal\_mp

```
sklearn.linear_model.orthogonal_mp(X, y, n_nonzero_coefs=None, tol=None, precom-
pute=False, copy_X=True, return_path=False, re-
turn_n_iter=False)
```

Orthogonal Matching Pursuit (OMP)

Solves n\_targets Orthogonal Matching Pursuit problems. An instance of the problem has the form:

When parametrized by the number of non-zero coefficients using n\_nonzero\_coefs: argmin  $||y - Xgamma||^2$  subject to  $||gamma||_0 \le n_{nonzero coeff}$ 

When parametrized by error using the parameter tol: argmin ||gamma||\_0 subject to ||y - Xgamma||^2 <= tol Read more in the *User Guide*.

#### **Parameters**

- X [array, shape (n\_samples, n\_features)] Input data. Columns are assumed to have unit norm.
- y [array, shape (n\_samples,) or (n\_samples, n\_targets)] Input targets
- **n\_nonzero\_coefs** [int] Desired number of non-zero entries in the solution. If None (by default) this value is set to 10% of n\_features.
- tol [float] Maximum norm of the residual. If not None, overrides n\_nonzero\_coefs.
- **precompute** [{True, False, 'auto'},] Whether to perform precomputations. Improves performance when n\_targets or n\_samples is very large.
- **copy\_X** [bool, optional] Whether the design matrix X must be copied by the algorithm. A false value is only helpful if X is already Fortran-ordered, otherwise a copy is made anyway.
- **return\_path** [bool, optional. Default: False] Whether to return every value of the nonzero coefficients along the forward path. Useful for cross-validation.
- return\_n\_iter [bool, optional default False] Whether or not to return the number of iterations.

#### Returns

- coef [array, shape (n\_features,) or (n\_features, n\_targets)] Coefficients of the OMP solution. If
   return\_path=True, this contains the whole coefficient path. In this case its shape is
   (n\_features, n\_features) or (n\_features, n\_targets, n\_features) and iterating over the last axis
   yields coefficients in increasing order of active features.
- **n\_iters** [array-like or int] Number of active features across every target. Returned only if return\_n\_iter is set to True.

### See also:

OrthogonalMatchingPursuit

```
orthogonal_mp_gram
lars_path
decomposition.sparse_encode
```

#### **Notes**

Orthogonal matching pursuit was introduced in S. Mallat, Z. Zhang, Matching pursuits with time-frequency dictionaries, IEEE Transactions on Signal Processing, Vol. 41, No. 12. (December 1993), pp. 3397-3415. (http://blanche.polytechnique.fr/~mallat/papiers/MallatPursuit93.pdf)

This implementation is based on Rubinstein, R., Zibulevsky, M. and Elad, M., Efficient Implementation of the K-SVD Algorithm using Batch Orthogonal Matching Pursuit Technical Report - CS Technion, April 2008. https://www.cs.technion.ac.il/~ronrubin/Publications/KSVD-OMP-v2.pdf

# 6.22.27 sklearn.linear\_model.orthogonal mp gram

```
sklearn.linear_model.orthogonal_mp_gram(Gram, Xy, n_nonzero_coefs=None, tol=None, norms_squared=None, copy_Gram=True, copy_Xy=True, return_path=False, return_n_iter=False)
```

Gram Orthogonal Matching Pursuit (OMP)

Solves n\_targets Orthogonal Matching Pursuit problems using only the Gram matrix X.T \* X and the product X.T \* y.

Read more in the User Guide.

#### **Parameters**

**Gram** [array, shape (n\_features, n\_features)] Gram matrix of the input data: X.T \* X

**Xy** [array, shape (n\_features,) or (n\_features, n\_targets)] Input targets multiplied by X: X.T \* y

**n\_nonzero\_coefs** [int] Desired number of non-zero entries in the solution. If None (by default) this value is set to 10% of n\_features.

tol [float] Maximum norm of the residual. If not None, overrides n nonzero coefs.

**norms\_squared** [array-like, shape (n\_targets,)] Squared L2 norms of the lines of y. Required if tol is not None.

**copy\_Gram** [bool, optional] Whether the gram matrix must be copied by the algorithm. A false value is only helpful if it is already Fortran-ordered, otherwise a copy is made anyway.

copy\_Xy [bool, optional] Whether the covariance vector Xy must be copied by the algorithm.
If False, it may be overwritten.

**return\_path** [bool, optional. Default: False] Whether to return every value of the nonzero coefficients along the forward path. Useful for cross-validation.

**return\_n\_iter** [bool, optional default False] Whether or not to return the number of iterations.

### Returns

coef [array, shape (n\_features,) or (n\_features, n\_targets)] Coefficients of the OMP solution. If return\_path=True, this contains the whole coefficient path. In this case its shape is (n\_features, n\_features) or (n\_features, n\_targets, n\_features) and iterating over the last axis yields coefficients in increasing order of active features. **n\_iters** [array-like or int] Number of active features across every target. Returned only if return\_n\_iter is set to True.

#### See also:

```
OrthogonalMatchingPursuit
orthogonal_mp
lars_path
decomposition.sparse_encode
```

#### **Notes**

Orthogonal matching pursuit was introduced in G. Mallat, Z. Zhang, Matching pursuits with time-frequency dictionaries, IEEE Transactions on Signal Processing, Vol. 41, No. 12. (December 1993), pp. 3397-3415. (http://blanche.polytechnique.fr/~mallat/papiers/MallatPursuit93.pdf)

This implementation is based on Rubinstein, R., Zibulevsky, M. and Elad, M., Efficient Implementation of the K-SVD Algorithm using Batch Orthogonal Matching Pursuit Technical Report - CS Technion, April 2008. https://www.cs.technion.ac.il/~ronrubin/Publications/KSVD-OMP-v2.pdf

# 6.22.28 sklearn.linear\_model.ridge\_regression

```
sklearn.linear_model.ridge_regression(X, y, alpha, sample_weight=None, solver='auto', max_iter=None, tol=0.001, verbose=0, ran-dom_state=None, return_n_iter=False, return_intercept=False, check_input=True)
```

Solve the ridge equation by the method of normal equations.

Read more in the User Guide.

### **Parameters**

**X** [{array-like, sparse matrix, LinearOperator},] shape = [n\_samples, n\_features] Training data

y [array-like, shape = [n\_samples] or [n\_samples, n\_targets]] Target values

**alpha** [{float, array-like},] shape = [n\_targets] if array-like Regularization strength; must be a positive float. Regularization improves the conditioning of the problem and reduces the variance of the estimates. Larger values specify stronger regularization. Alpha corresponds to C^-1 in other linear models such as LogisticRegression or LinearSVC. If an array is passed, penalties are assumed to be specific to the targets. Hence they must correspond in number.

**sample\_weight** [float or numpy array of shape [n\_samples]] Individual weights for each sample. If sample\_weight is not None and solver='auto', the solver will be set to 'cholesky'.

New in version 0.17.

**solver** [{'auto', 'svd', 'cholesky', 'lsqr', 'sparse\_cg', 'sag', 'saga'}] Solver to use in the computational routines:

- 'auto' chooses the solver automatically based on the type of data.
- 'svd' uses a Singular Value Decomposition of X to compute the Ridge coefficients. More stable for singular matrices than 'cholesky'.

- 'cholesky' uses the standard scipy.linalg.solve function to obtain a closed-form solution via a Cholesky decomposition of dot(X.T, X)
- 'sparse\_cg' uses the conjugate gradient solver as found in scipy.sparse.linalg.cg. As an iterative algorithm, this solver is more appropriate than 'cholesky' for large-scale data (possibility to set tol and max\_iter).
- 'lsqr' uses the dedicated regularized least-squares routine scipy.sparse.linalg.lsqr. It is the
  fastest and uses an iterative procedure.
- 'sag' uses a Stochastic Average Gradient descent, and 'saga' uses its improved, unbiased version named SAGA. Both methods also use an iterative procedure, and are often faster than other solvers when both n\_samples and n\_features are large. Note that 'sag' and 'saga' fast convergence is only guaranteed on features with approximately the same scale. You can preprocess the data with a scaler from sklearn.preprocessing.

All last five solvers support both dense and sparse data. However, only 'sag' and 'sparse\_cg' supports sparse input when 'fit\_intercept' is True.

New in version 0.17: Stochastic Average Gradient descent solver.

New in version 0.19: SAGA solver.

max\_iter [int, optional] Maximum number of iterations for conjugate gradient solver. For the 'sparse\_cg' and 'lsqr' solvers, the default value is determined by scipy.sparse.linalg. For 'sag' and saga solver, the default value is 1000.

tol [float] Precision of the solution.

**verbose** [int] Verbosity level. Setting verbose > 0 will display additional information depending on the solver used.

random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == 'sag'.

**return\_n\_iter** [boolean, default False] If True, the method also returns n\_iter, the actual number of iteration performed by the solver.

New in version 0.17.

**return\_intercept** [boolean, default False] If True and if X is sparse, the method also returns the intercept, and the solver is automatically changed to 'sag'. This is only a temporary fix for fitting the intercept with sparse data. For dense data, use sklearn.linear model. preprocess data before your regression.

New in version 0.17.

**check\_input** [boolean, default True] If False, the input arrays X and y will not be checked.

New in version 0.21.

#### Returns

**coef** [array, shape = [n\_features] or [n\_targets, n\_features]] Weight vector(s).

**n\_iter** [int, optional] The actual number of iteration performed by the solver. Only returned if return\_n\_iter is True.

**intercept** [float or array, shape = [n\_targets]] The intercept of the model. Only returned if return intercept is True and if X is a scipy sparse array.

### **Notes**

This function won't compute the intercept.

# 6.23 sklearn.manifold: Manifold Learning

The sklearn.manifold module implements data embedding techniques.

**User guide:** See the *Manifold learning* section for further details.

manifold. Isomap([n_neighbors, n_components,])	Isomap Embedding
manifold.LocallyLinearEmbedding([])	Locally Linear Embedding
manifold.MDS([n_components, metric, n_init,])	Multidimensional scaling
manifold.SpectralEmbedding([n_components,	Spectral embedding for non-linear dimensionality reduc-
])	tion.
manifold. TSNE([n_components, perplexity,])	t-distributed Stochastic Neighbor Embedding.

# 6.23.1 sklearn.manifold.lsomap

```
class sklearn.manifold.Isomap (n_neighbors=5, n_ncomponents=2, eigen_nsolver='auto', tol=0, max_iter=None, path_method='auto', neighbors_algorithm='auto', n_ncomponents=2, n_ncomponents
```

Isomap Embedding

Non-linear dimensionality reduction through Isometric Mapping

Read more in the *User Guide*.

#### **Parameters**

- **n\_neighbors** [integer] number of neighbors to consider for each point.
- **n\_components** [integer] number of coordinates for the manifold
- **eigen\_solver** [['auto'l'arpack'l'dense']] 'auto' : Attempt to choose the most efficient solver for the given problem.

'arpack': Use Arnoldi decomposition to find the eigenvalues and eigenvectors.

'dense': Use a direct solver (i.e. LAPACK) for the eigenvalue decomposition.

**tol** [float] Convergence tolerance passed to arpack or lobpcg. not used if eigen\_solver == 'dense'.

**max\_iter** [integer] Maximum number of iterations for the arpack solver. not used if eigen\_solver == 'dense'.

path\_method [string ['auto'|'FW'|'D']] Method to use in finding shortest path.

'auto': attempt to choose the best algorithm automatically.

'FW': Floyd-Warshall algorithm.

'D': Dijkstra's algorithm.

**neighbors\_algorithm** [string ['auto'|'brute'|'kd\_tree'|'ball\_tree']] Algorithm to use for nearest neighbors search, passed to neighbors. NearestNeighbors instance.

**n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

### Attributes

**embedding** [array-like, shape (n\_samples, n\_components)] Stores the embedding vectors.

**kernel\_pca\_** [object] *KernelPCA* object used to implement the embedding.

training\_data\_ [array-like, shape (n\_samples, n\_features)] Stores the training data.

**nbrs**\_ [sklearn.neighbors.NearestNeighbors instance] Stores nearest neighbors instance, including BallTree or KDtree if applicable.

**dist\_matrix**\_ [array-like, shape (n\_samples, n\_samples)] Stores the geodesic distance matrix of training data.

#### References

[R7f4d308f5054-1]

# **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.manifold import Isomap
>>> X, _ = load_digits(return_X_y=True)
>>> X.shape
(1797, 64)
>>> embedding = Isomap(n_components=2)
>>> X_transformed = embedding.fit_transform(X[:100])
>>> X_transformed.shape
(100, 2)
```

#### **Methods**

fit(self, X[, y])	Compute the embedding vectors for data X
$fit\_transform(self, X[, y])$	Fit the model from data in X and transform X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
reconstruction_error(self)	Compute the reconstruction error for the embedding.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform X.

```
__init__ (self, n_neighbors=5, n_components=2, eigen_solver='auto', tol=0, max_iter=None, path_method='auto', neighbors_algorithm='auto', n_jobs=None)
```

**fit** (self, X, y=None)

Compute the embedding vectors for data X

#### **Parameters**

**X** [{array-like, sparse matrix, BallTree, KDTree, NearestNeighbors}] Sample data, shape = (n\_samples, n\_features), in the form of a numpy array, precomputed tree, or Nearest-Neighbors object.

#### y [Ignored]

#### Returns

**self** [returns an instance of self.]

# fit\_transform(self, X, y=None)

Fit the model from data in X and transform X.

#### **Parameters**

**X** [{array-like, sparse matrix, BallTree, KDTree}] Training vector, where n\_samples in the number of samples and n\_features is the number of features.

y [Ignored]

#### Returns

**X\_new** [array-like, shape (n\_samples, n\_components)]

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

### reconstruction\_error(self)

Compute the reconstruction error for the embedding.

#### Returns

reconstruction\_error [float]

### **Notes**

The cost function of an isomap embedding is

```
E = frobenius_norm[K(D) - K(D_fit)] / n_samples
```

Where D is the matrix of distances for the input data X, D\_fit is the matrix of distances for the output embedding X\_fit, and K is the isomap kernel:

```
K(D) = -0.5 * (I - 1/n \text{ samples}) * D^2 * (I - 1/n \text{ samples})
```

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, X)

Transform X.

This is implemented by linking the points X into the graph of geodesic distances of the training data. First the n\_neighbors nearest neighbors of X are found in the training data, and from these the shortest geodesic distances from each point in X to each point in the training data are computed in order to construct the kernel. The embedding of X is the projection of this kernel onto the embedding vectors of the training set.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

## Returns

**X\_new** [array-like, shape (n\_samples, n\_components)]

## Examples using sklearn.manifold.Isomap

- · Comparison of Manifold Learning methods
- · Manifold Learning methods on a severed sphere
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

# 6.23.2 sklearn.manifold.LocallyLinearEmbedding

```
class sklearn.manifold.LocallyLinearEmbedding (n_neighbors=5, n_ncomponents=2, reg=0.001, eigen_nsolver=nuto, tol=1e-06, max_iter=100, method=nutous nutous nutous
```

Locally Linear Embedding

Read more in the *User Guide*.

### **Parameters**

- **n\_neighbors** [integer] number of neighbors to consider for each point.
- **n\_components** [integer] number of coordinates for the manifold
- **reg** [float] regularization constant, multiplies the trace of the local covariance matrix of the distances.
- eigen\_solver [string, {'auto', 'arpack', 'dense'}] auto : algorithm will attempt to choose the best method for input data
  - **arpack** [use arnoldi iteration in shift-invert mode.] For this method, M may be a dense matrix, sparse matrix, or general linear operator. Warning: ARPACK can be unstable for some problems. It is best to try several random seeds in order to check results.
  - **dense** [use standard dense matrix operations for the eigenvalue] decomposition. For this method, M must be an array or matrix type. This method should be avoided for large problems.
- tol [float, optional] Tolerance for 'arpack' method Not used if eigen\_solver=='dense'.
- **max\_iter** [integer] maximum number of iterations for the arpack solver. Not used if eigen\_solver=='dense'.

```
method [string ('standard', 'hessian', 'modified' or 'ltsa')]
```

standard [use the standard locally linear embedding algorithm. see] reference [1]

```
hessian [use the Hessian eigenmap method. This method requires] n_neighbors > n_components * (1 + (n_components + 1) / 2 see reference [2]
```

modified [use the modified locally linear embedding algorithm.] see reference [3]

**Itsa** [use local tangent space alignment algorithm] see reference [4]

- hessian\_tol [float, optional] Tolerance for Hessian eigenmapping method. Only used if
  method == 'hessian'
- modified\_tol [float, optional] Tolerance for modified LLE method. Only used if method ==
  'modified'
- **neighbors\_algorithm** [string ['auto'|'brute'|'kd\_tree'|'ball\_tree']] algorithm to use for nearest neighbors search, passed to neighbors.NearestNeighbors instance
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the
  RandomState instance used by np.random. Used when eigen\_solver == 'arpack'.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

### Attributes

```
embedding_ [array-like, shape [n_samples, n_components]] Stores the embedding vectors reconstruction_error_ [float] Reconstruction error associated with embedding_
```

nbrs\_ [NearestNeighbors object] Stores nearest neighbors instance, including BallTree or KDtree if applicable.

#### References

[R62e36dd1b056-1], [R62e36dd1b056-2], [R62e36dd1b056-3], [R62e36dd1b056-4]

# **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.manifold import LocallyLinearEmbedding
>>> X, _ = load_digits(return_X_y=True)
>>> X.shape
(1797, 64)
>>> embedding = LocallyLinearEmbedding(n_components=2)
>>> X_transformed = embedding.fit_transform(X[:100])
>>> X_transformed.shape
(100, 2)
```

## **Methods**

fit(self, X[, y])	Compute the embedding vectors for data X
$fit\_transform(self, X[, y])$	Compute the embedding vectors for data X and transform X.
	Continued on next page

Table 6.173 – continued from previous page

<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform new points into embedding space.

\_\_init\_\_ (self, n\_neighbors=5, n\_components=2, reg=0.001, eigen\_solver='auto', tol=1e-06, max\_iter=100, method='standard', hessian\_tol=0.0001, modified\_tol=1e-12, neighbors\_algorithm='auto', random\_state=None, n\_jobs=None)

### **fit** (*self*, *X*, *y*=*None*)

Compute the embedding vectors for data X

### **Parameters**

**X** [array-like of shape [n\_samples, n\_features]] training set.

y [Ignored]

#### **Returns**

**self** [returns an instance of self.]

### fit\_transform(self, X, y=None)

Compute the embedding vectors for data X and transform X.

### **Parameters**

**X** [array-like of shape [n\_samples, n\_features]] training set.

y [Ignored]

#### Returns

**X\_new** [array-like, shape (n\_samples, n\_components)]

#### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

**params** [mapping of string to any] Parameter names mapped to their values.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# transform(self, X)

Transform new points into embedding space.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

### Returns

**X\_new** [array, shape = [n\_samples, n\_components]]

### **Notes**

Because of scaling performed by this method, it is discouraged to use it together with methods that are not scale-invariant (like SVMs)

### Examples using sklearn.manifold.LocallyLinearEmbedding

- Visualizing the stock market structure
- Comparison of Manifold Learning methods
- · Manifold Learning methods on a severed sphere
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

### 6.23.3 sklearn.manifold.MDS

class sklearn.manifold.MDS (n\_components=2, metric=True, n\_init=4, max\_iter=300, verbose=0, eps=0.001, n\_jobs=None, random\_state=None, dissimilarity='euclidean')

Multidimensional scaling

Read more in the *User Guide*.

#### **Parameters**

- n\_components [int, optional, default: 2] Number of dimensions in which to immerse the dissimilarities.
- **metric** [boolean, optional, default: True] If True, perform metric MDS; otherwise, perform nonmetric MDS.
- **n\_init** [int, optional, default: 4] Number of times the SMACOF algorithm will be run with different initializations. The final results will be the best output of the runs, determined by the run with the smallest final stress.
- **max\_iter** [int, optional, default: 300] Maximum number of iterations of the SMACOF algorithm for a single run.
- verbose [int, optional, default: 0] Level of verbosity.
- **eps** [float, optional, default: 1e-3] Relative tolerance with respect to stress at which to declare convergence.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. If multiple initializations are used (n\_init), each run of the algorithm is computed in parallel.
  - None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- random\_state [int, RandomState instance or None, optional, default: None] The generator used to initialize the centers. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**dissimilarity** ['euclidean' | 'precomputed', optional, default: 'euclidean'] Dissimilarity measure to use:

- 'euclidean': Pairwise Euclidean distances between points in the dataset.
- 'precomputed': Pre-computed dissimilarities are passed directly to fit and fit\_transform.

#### **Attributes**

**embedding**\_ [array-like, shape (n\_samples, n\_components)] Stores the position of the dataset in the embedding space.

**stress**\_ [float] The final value of the stress (sum of squared distance of the disparities and the distances for all constrained points).

#### References

"Modern Multidimensional Scaling - Theory and Applications" Borg, I.; Groenen P. Springer Series in Statistics (1997)

"Nonmetric multidimensional scaling: a numerical method" Kruskal, J. Psychometrika, 29 (1964)

"Multidimensional scaling by optimizing goodness of fit to a nonmetric hypothesis" Kruskal, J. Psychometrika, 29, (1964)

# **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.manifold import MDS
>>> X, _ = load_digits(return_X_y=True)
>>> X.shape
(1797, 64)
>>> embedding = MDS(n_components=2)
>>> X_transformed = embedding.fit_transform(X[:100])
>>> X_transformed.shape
(100, 2)
```

### **Methods**

fit(self, X[, y, init])	Computes the position of the points in the embedding
	space
<pre>fit_transform(self, X[, y, init])</pre>	Fit the data from X, and returns the embedded coordi-
	nates
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, n_components=2, metric=True, n_init=4, max_iter=300, verbose=0, eps=0.001, n_jobs=None, random_state=None, dissimilarity='euclidean')
```

**fit** (*self*, *X*, *y=None*, *init=None*)

Computes the position of the points in the embedding space

#### **Parameters**

- X [array, shape (n\_samples, n\_features) or (n\_samples, n\_samples)] Input data. If dissimilarity=='precomputed', the input should be the dissimilarity matrix.
- y [Ignored]

**init** [ndarray, shape (n\_samples,), optional, default: None] Starting configuration of the embedding to initialize the SMACOF algorithm. By default, the algorithm is initialized with a randomly chosen array.

#### **fit** transform (*self*, *X*, *y*=*None*, *init*=*None*)

Fit the data from X, and returns the embedded coordinates

#### **Parameters**

- X [array, shape (n\_samples, n\_features) or (n\_samples, n\_samples)] Input data. If dissimilarity=='precomputed', the input should be the dissimilarity matrix.
- y [Ignored]

**init** [ndarray, shape (n\_samples,), optional, default: None] Starting configuration of the embedding to initialize the SMACOF algorithm. By default, the algorithm is initialized with a randomly chosen array.

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

### Examples using sklearn.manifold.MDS

- Multi-dimensional scaling
- Comparison of Manifold Learning methods
- · Manifold Learning methods on a severed sphere
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

# 6.23.4 sklearn.manifold.SpectralEmbedding

```
 \begin{array}{lll} \textbf{class} & \textbf{sklearn.manifold.SpectralEmbedding} (n\_components=2, & affinity='nearest\_neighbors', \\ & gamma=None, & random\_state=None, \\ & eigen\_solver=None, & n\_neighbors=None, \\ & n & jobs=None) \end{array}
```

Spectral embedding for non-linear dimensionality reduction.

Forms an affinity matrix given by the specified function and applies spectral decomposition to the corresponding graph laplacian. The resulting transformation is given by the value of the eigenvectors for each data point.

Note: Laplacian Eigenmaps is the actual algorithm implemented here.

Read more in the User Guide.

#### **Parameters**

**n\_components** [integer, default: 2] The dimension of the projected subspace.

**affinity** [string or callable, default]

# How to construct the affinity matrix.

- 'nearest\_neighbors' : construct affinity matrix by knn graph
- 'rbf': construct affinity matrix by rbf kernel
- 'precomputed' : interpret X as precomputed affinity matrix
- callable: use passed in function as affinity the function takes in data matrix (n\_samples, n\_features) and return affinity matrix (n\_samples, n\_samples).

gamma [float, optional, default] Kernel coefficient for rbf kernel.

- random\_state [int, RandomState instance or None, optional, default: None] A pseudo random number generator used for the initialization of the lobpcg eigenvectors. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == 'amg'.
- **eigen\_solver** [{None, 'arpack', 'lobpcg', or 'amg'}] The eigenvalue decomposition strategy to use. AMG requires pyamg to be installed. It can be faster on very large, sparse problems, but may also lead to instabilities.
- **n neighbors** [int, default] Number of nearest neighbors for nearest neighbors graph building.
- n\_jobs [int or None, optional (default=None)] The number of parallel jobs to run. None means
  1 unless in a joblib.parallel\_backend context. -1 means using all processors. See
  Glossary for more details.

#### **Attributes**

**embedding**\_ [array, shape = (n\_samples, n\_components)] Spectral embedding of the training matrix.

**affinity\_matrix** [array, shape = (n\_samples, n\_samples)] Affinity\_matrix constructed from samples or precomputed.

# References

 A Tutorial on Spectral Clustering, 2007 Ulrike von Luxburg http://citeseerx.ist.psu.edu/viewdoc/ summary?doi=10.1.1.165.9323

- On Spectral Clustering: Analysis and an algorithm, 2001 Andrew Y. Ng, Michael I. Jordan, Yair Weiss http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.19.8100
- Normalized cuts and image segmentation, 2000 Jianbo Shi, Jitendra Malik http://citeseer.ist.psu.edu/ viewdoc/summary?doi=10.1.1.160.2324

## **Examples**

```
>>> from sklearn.datasets import load_digits
>>> from sklearn.manifold import SpectralEmbedding
>>> X, _ = load_digits(return_X_y=True)
>>> X.shape
(1797, 64)
>>> embedding = SpectralEmbedding(n_components=2)
>>> X_transformed = embedding.fit_transform(X[:100])
>>> X_transformed.shape
(100, 2)
```

### **Methods**

fit(self, X[, y])	Fit the model from data in X.
$fit\_transform(self, X[, y])$	Fit the model from data in X and transform X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, n_components=2, affinity='nearest_neighbors', gamma=None, random_state=None, eigen_solver=None, n_neighbors=None, n_jobs=None)
```

# fit (self, X, y=None)

Fit the model from data in X.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples is the number of samples and n\_features is the number of features.

If affinity is "precomputed" X: array-like, shape (n\_samples, n\_samples), Interpret X as precomputed adjacency graph computed from samples.

#### **Returns**

self [object] Returns the instance itself.

#### fit\_transform(self, X, y=None)

Fit the model from data in X and transform X.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples is the number of samples and n\_features is the number of features.

If affinity is "precomputed" X : array-like, shape (n\_samples, n\_samples), Interpret X as precomputed adjacency graph computed from samples.

# Returns

**X new** [array-like, shape (n samples, n components)]

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### Examples using sklearn.manifold.SpectralEmbedding

- · Various Agglomerative Clustering on a 2D embedding of digits
- · Comparison of Manifold Learning methods
- · Manifold Learning methods on a severed sphere
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

#### 6.23.5 sklearn.manifold.TSNE

t-SNE [1] is a tool to visualize high-dimensional data. It converts similarities between data points to joint probabilities and tries to minimize the Kullback-Leibler divergence between the joint probabilities of the low-dimensional embedding and the high-dimensional data. t-SNE has a cost function that is not convex, i.e. with different initializations we can get different results.

It is highly recommended to use another dimensionality reduction method (e.g. PCA for dense data or TruncatedSVD for sparse data) to reduce the number of dimensions to a reasonable amount (e.g. 50) if the number of features is very high. This will suppress some noise and speed up the computation of pairwise distances between samples. For more tips see Laurens van der Maaten's FAQ [2].

Read more in the User Guide.

### **Parameters**

**n\_components** [int, optional (default: 2)] Dimension of the embedded space.

**perplexity** [float, optional (default: 30)] The perplexity is related to the number of nearest neighbors that is used in other manifold learning algorithms. Larger datasets usually require a larger perplexity. Consider selecting a value between 5 and 50. Different values can result in significantly different results.

- early\_exaggeration [float, optional (default: 12.0)] Controls how tight natural clusters in the original space are in the embedded space and how much space will be between them. For larger values, the space between natural clusters will be larger in the embedded space. Again, the choice of this parameter is not very critical. If the cost function increases during initial optimization, the early exaggeration factor or the learning rate might be too high.
- **learning\_rate** [float, optional (default: 200.0)] The learning rate for t-SNE is usually in the range [10.0, 1000.0]. If the learning rate is too high, the data may look like a 'ball' with any point approximately equidistant from its nearest neighbours. If the learning rate is too low, most points may look compressed in a dense cloud with few outliers. If the cost function gets stuck in a bad local minimum increasing the learning rate may help.
- **n\_iter** [int, optional (default: 1000)] Maximum number of iterations for the optimization. Should be at least 250.
- **n\_iter\_without\_progress** [int, optional (default: 300)] Maximum number of iterations without progress before we abort the optimization, used after 250 initial iterations with early exaggeration. Note that progress is only checked every 50 iterations so this value is rounded to the next multiple of 50.
  - New in version 0.17: parameter  $n\_iter\_without\_progress$  to control stopping criteria.
- **min\_grad\_norm** [float, optional (default: 1e-7)] If the gradient norm is below this threshold, the optimization will be stopped.
- metric [string or callable, optional] The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by scipy.spatial.distance.pdist for its metric parameter, or a metric listed in pairwise.PAIRWISE\_DISTANCE\_FUNCTIONS. If metric is "precomputed", X is assumed to be a distance matrix. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them. The default is "euclidean" which is interpreted as squared euclidean distance.
- init [string or numpy array, optional (default: "random")] Initialization of embedding. Possible options are 'random', 'pca', and a numpy array of shape (n\_samples, n\_components). PCA initialization cannot be used with precomputed distances and is usually more globally stable than random initialization.
- verbose [int, optional (default: 0)] Verbosity level.
- random\_state [int, RandomState instance or None, optional (default: None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Note that different initializations might result in different local minima of the cost function.
- **method** [string (default: 'barnes\_hut')] By default the gradient calculation algorithm uses Barnes-Hut approximation running in O(NlogN) time. method='exact' will run on the slower, but exact, algorithm in O(N^2) time. The exact algorithm should be used when nearest-neighbor errors need to be better than 3%. However, the exact method cannot scale to millions of examples.
  - New in version 0.17: Approximate optimization *method* via the Barnes-Hut.
- angle [float (default: 0.5)] Only used if method='barnes\_hut' This is the trade-off between speed and accuracy for Barnes-Hut T-SNE. 'angle' is the angular size (referred to as theta in [3]) of a distant node as measured from a point. If this size is below 'angle' then it is used as a summary node of all points contained within it. This method is not very sensitive to

changes in this parameter in the range of 0.2 - 0.8. Angle less than 0.2 has quickly increasing computation time and angle greater 0.8 has quickly increasing error.

#### **Attributes**

```
embedding_ [array-like, shape (n_samples, n_components)] Stores the embedding vectors.
kl_divergence_ [float] Kullback-Leibler divergence after optimization.
n_iter_ [int] Number of iterations run.
```

### References

- [1] van der Maaten, L.J.P.; Hinton, G.E. Visualizing High-Dimensional Data Using t-SNE. Journal of Machine Learning Research 9:2579-2605, 2008.
- [2] van der Maaten, L.J.P. t-Distributed Stochastic Neighbor Embedding https://lvdmaaten.github.io/tsne/
- [3] L.J.P. van der Maaten. Accelerating t-SNE using Tree-Based Algorithms. Journal of Machine Learning Research 15(Oct):3221-3245, 2014. https://lvdmaaten.github.io/publications/papers/JMLR\_2014.pdf

# **Examples**

```
>>> import numpy as np
>>> from sklearn.manifold import TSNE
>>> X = np.array([[0, 0, 0], [0, 1, 1], [1, 0, 1], [1, 1, 1]])
>>> X_embedded = TSNE(n_components=2).fit_transform(X)
>>> X_embedded.shape
(4, 2)
```

#### Methods

fit(self, X[, y])	Fit X into an embedded space.
fit_transform(self, X[, y])	Fit X into an embedded space and return that trans-
	formed output.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, n_components=2, perplexity=30.0, early_exaggeration=12.0, learning_rate=200.0, n_iter=1000, n_iter_without_progress=300, min_grad_norm=1e-07, metric='euclidean', init='random', verbose=0, random_state=None, method='barnes_hut', angle=0.5)
```

### **fit** (self, X, y=None)

Fit X into an embedded space.

### **Parameters**

- **X** [array, shape (n\_samples, n\_features) or (n\_samples, n\_samples)] If the metric is 'precomputed' X must be a square distance matrix. Otherwise it contains a sample per row. If the method is 'exact', X may be a sparse matrix of type 'csr', 'csc' or 'coo'.
- y [Ignored]

```
fit_transform(self, X, y=None)
```

Fit X into an embedded space and return that transformed output.

#### **Parameters**

**X** [array, shape (n\_samples, n\_features) or (n\_samples, n\_samples)] If the metric is 'precomputed' X must be a square distance matrix. Otherwise it contains a sample per row.

y [Ignored]

### **Returns**

**X\_new** [array, shape (n\_samples, n\_components)] Embedding of the training data in low-dimensional space.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### Examples using sklearn.manifold.TSNE

- t-SNE: The effect of various perplexity values on the shape
- Comparison of Manifold Learning methods
- Manifold Learning methods on a severed sphere
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

manifold.locally_linear_embedding( $X, \ldots$ [,	Perform a Locally Linear Embedding analysis on the data.
])	
<pre>manifold.smacof(dissimilarities[, metric,])</pre>	Computes multidimensional scaling using the SMACOF
	algorithm.
manifold.spectral_embedding(adjacency[,])	Project the sample on the first eigenvectors of the graph
	Laplacian.

# 6.23.6 sklearn.manifold.locally\_linear\_embedding

Perform a Locally Linear Embedding analysis on the data.

Read more in the User Guide.

#### **Parameters**

- **X** [{array-like, NearestNeighbors}] Sample data, shape = (n\_samples, n\_features), in the form of a numpy array or a NearestNeighbors object.
- **n\_neighbors** [integer] number of neighbors to consider for each point.
- **n\_components** [integer] number of coordinates for the manifold.
- **reg** [float] regularization constant, multiplies the trace of the local covariance matrix of the distances.
- eigen\_solver [string, {'auto', 'arpack', 'dense'}] auto : algorithm will attempt to choose the best method for input data
  - **arpack** [use arnoldi iteration in shift-invert mode.] For this method, M may be a dense matrix, sparse matrix, or general linear operator. Warning: ARPACK can be unstable for some problems. It is best to try several random seeds in order to check results.
  - **dense** [use standard dense matrix operations for the eigenvalue] decomposition. For this method, M must be an array or matrix type. This method should be avoided for large problems.
- tol [float, optional] Tolerance for 'arpack' method Not used if eigen\_solver=='dense'.
- **max\_iter** [integer] maximum number of iterations for the arpack solver.
- method [{'standard', 'hessian', 'modified', 'ltsa'}]
  - **standard** [use the standard locally linear embedding algorithm.] see reference [1]
  - **hessian** [use the Hessian eigenmap method. This method requires] n\_neighbors >  $n_{\text{components}} * (1 + (n_{\text{components}} + 1) / 2$ . see reference [2]
  - **modified** [use the modified locally linear embedding algorithm.] see reference [3]
  - **Itsa** [use local tangent space alignment algorithm] see reference [4]
- **hessian\_tol** [float, optional] Tolerance for Hessian eigenmapping method. Only used if method == 'hessian'
- modified\_tol [float, optional] Tolerance for modified LLE method. Only used if method ==
   'modified'
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == 'arpack'.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### Returns

- Y [array-like, shape [n\_samples, n\_components]] Embedding vectors.
- **squared\_error** [float] Reconstruction error for the embedding vectors. Equivalent to norm (Y W Y, 'fro') \*\*2, where W are the reconstruction weights.

#### References

[1], [2], [3], [4]

### Examples using sklearn.manifold.locally\_linear\_embedding

• Swiss Roll reduction with LLE

### 6.23.7 sklearn.manifold.smacof

sklearn.manifold.smacof(dissimilarities, metric=True, n\_components=2, init=None, n\_init=8, n\_jobs=None, max\_iter=300, verbose=0, eps=0.001, random\_state=None, return n\_iter=False)

Computes multidimensional scaling using the SMACOF algorithm.

The SMACOF (Scaling by MAjorizing a COmplicated Function) algorithm is a multidimensional scaling algorithm which minimizes an objective function (the *stress*) using a majorization technique. Stress majorization, also known as the Guttman Transform, guarantees a monotone convergence of stress, and is more powerful than traditional techniques such as gradient descent.

The SMACOF algorithm for metric MDS can summarized by the following steps:

- 1. Set an initial start configuration, randomly or not.
- 2. Compute the stress
- 3. Compute the Guttman Transform
- 4. Iterate 2 and 3 until convergence.

The nonmetric algorithm adds a monotonic regression step before computing the stress.

#### **Parameters**

**dissimilarities** [ndarray, shape (n\_samples, n\_samples)] Pairwise dissimilarities between the points. Must be symmetric.

metric [boolean, optional, default: True] Compute metric or nonmetric SMACOF algorithm.

- **n\_components** [int, optional, default: 2] Number of dimensions in which to immerse the dissimilarities. If an init array is provided, this option is overridden and the shape of init is used to determine the dimensionality of the embedding space.
- **init** [ndarray, shape (n\_samples, n\_components), optional, default: None] Starting configuration of the embedding to initialize the algorithm. By default, the algorithm is initialized with a randomly chosen array.
- n\_init [int, optional, default: 8] Number of times the SMACOF algorithm will be run with different initializations. The final results will be the best output of the runs, determined by the run with the smallest final stress. If init is provided, this option is overridden and a single run is performed.
- n\_jobs [int or None, optional (default=None)] The number of jobs to use for the computation.
  If multiple initializations are used (n\_init), each run of the algorithm is computed in parallel.

None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

max\_iter [int, optional, default: 300] Maximum number of iterations of the SMACOF algorithm for a single run.

verbose [int, optional, default: 0] Level of verbosity.

**eps** [float, optional, default: 1e-3] Relative tolerance with respect to stress at which to declare convergence.

random\_state [int, RandomState instance or None, optional, default: None] The generator used to initialize the centers. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**return\_n\_iter** [bool, optional, default: False] Whether or not to return the number of iterations.

#### Returns

**X** [ndarray, shape (n\_samples, n\_components)] Coordinates of the points in a n\_components-space.

**stress** [float] The final value of the stress (sum of squared distance of the disparities and the distances for all constrained points).

**n\_iter** [int] The number of iterations corresponding to the best stress. Returned only if return\_n\_iter is set to True.

#### **Notes**

"Modern Multidimensional Scaling - Theory and Applications" Borg, I.; Groenen P. Springer Series in Statistics (1997)

"Nonmetric multidimensional scaling: a numerical method" Kruskal, J. Psychometrika, 29 (1964)

"Multidimensional scaling by optimizing goodness of fit to a nonmetric hypothesis" Kruskal, J. Psychometrika, 29, (1964)

# 6.23.8 sklearn.manifold.spectral embedding

sklearn.manifold.spectral\_embedding(adjacency, n\_components=8, eigen\_solver=None, random\_state=None, eigen\_tol=0.0, norm\_laplacian=True, drop\_first=True)

Project the sample on the first eigenvectors of the graph Laplacian.

The adjacency matrix is used to compute a normalized graph Laplacian whose spectrum (especially the eigenvectors associated to the smallest eigenvalues) has an interpretation in terms of minimal number of cuts necessary to split the graph into comparably sized components.

This embedding can also 'work' even if the adjacency variable is not strictly the adjacency matrix of a graph but more generally an affinity or similarity matrix between samples (for instance the heat kernel of a euclidean distance matrix or a k-NN matrix).

However care must taken to always make the affinity matrix symmetric so that the eigenvector decomposition works as expected.

Note: Laplacian Eigenmaps is the actual algorithm implemented here.

Read more in the User Guide.

# Parameters

- **adjacency** [array-like or sparse matrix, shape: (n\_samples, n\_samples)] The adjacency matrix of the graph to embed.
- **n\_components** [integer, optional, default 8] The dimension of the projection subspace.
- **eigen\_solver** [{None, 'arpack', 'lobpcg', or 'amg'}, default None] The eigenvalue decomposition strategy to use. AMG requires pyamg to be installed. It can be faster on very large, sparse problems, but may also lead to instabilities.
- random\_state [int, RandomState instance or None, optional, default: None] A pseudo random number generator used for the initialization of the lobpcg eigenvectors decomposition. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == 'amg'.
- **eigen\_tol** [float, optional, default=0.0] Stopping criterion for eigendecomposition of the Laplacian matrix when using arpack eigen\_solver.
- norm\_laplacian [bool, optional, default=True] If True, then compute normalized Laplacian.
- **drop\_first** [bool, optional, default=True] Whether to drop the first eigenvector. For spectral embedding, this should be True as the first eigenvector should be constant vector for connected graph, but for spectral clustering, this should be kept as False to retain the first eigenvector.

#### Returns

**embedding** [array, shape=(n\_samples, n\_components)] The reduced samples.

#### **Notes**

Spectral Embedding (Laplacian Eigenmaps) is most useful when the graph has one connected component. If there graph has many components, the first few eigenvectors will simply uncover the connected components of the graph.

### References

- · https://en.wikipedia.org/wiki/LOBPCG
- Toward the Optimal Preconditioned Eigensolver: Locally Optimal Block Preconditioned Conjugate Gradient Method Andrew V. Knyazev https://doi.org/10.1137%2FS1064827500366124

# 6.24 sklearn.metrics: Metrics

See the *Model evaluation: quantifying the quality of predictions* section and the *Pairwise metrics, Affinities and Kernels* section of the user guide for further details. The <code>sklearn.metrics</code> module includes score functions, performance metrics and pairwise metrics and distance computations.

# 6.24.1 Model Selection Interface

See the *The scoring parameter: defining model evaluation rules* section of the user guide for further details.

<pre>metrics.check_scoring(estimator[, scoring,])</pre>	Determine scorer from user options.
metrics.get_scorer(scoring)	Get a scorer from string
	Continued on next page

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# Table 6.178 - continued from previous page

metrics.make scorer(score func[,...])

Make a scorer from a performance metric or loss function.

## sklearn.metrics.check\_scoring

sklearn.metrics.check\_scoring(estimator, scoring=None, allow\_none=False)

Determine scorer from user options.

A TypeError will be thrown if the estimator cannot be scored.

#### **Parameters**

estimator [estimator object implementing 'fit'] The object to use to fit the data.

**allow\_none** [boolean, optional, default: False] If no scoring is specified and the estimator has no score function, we can either return None or raise an exception.

#### Returns

scoring [callable] A scorer callable object / function with signature scorer (estimator,
 X, y).

#### sklearn.metrics.get scorer

```
sklearn.metrics.get_scorer(scoring)
```

Get a scorer from string

#### **Parameters**

scoring [str | callable] scoring method as string. If callable it is returned as is.

### Returns

scorer [callable] The scorer.

### sklearn.metrics.make\_scorer

```
sklearn.metrics.make_scorer(score_func, greater_is_better=True, needs_proba=False, needs_threshold=False, **kwargs)
```

Make a scorer from a performance metric or loss function.

This factory function wraps scoring functions for use in GridSearchCV and cross\_val\_score. It takes a score function, such as accuracy\_score, mean\_squared\_error, adjusted\_rand\_index or average\_precision and returns a callable that scores an estimator's output.

Read more in the *User Guide*.

#### **Parameters**

```
score_func [callable,] Score function (or loss function) with signature score_func(y,
    y_pred, **kwargs).
```

greater\_is\_better [boolean, default=True] Whether score\_func is a score function (default), meaning high is good, or a loss function, meaning low is good. In the latter case, the scorer object will sign-flip the outcome of the score\_func.

**needs\_proba** [boolean, default=False] Whether score\_func requires predict\_proba to get probability estimates out of a classifier.

If True, for binary y\_true, the score function is supposed to accept a 1D y\_pred (i.e., probability of the positive class, shape (n\_samples,)).

**needs\_threshold** [boolean, default=False] Whether score\_func takes a continuous decision certainty. This only works for binary classification using estimators that have either a decision function or predict proba method.

If True, for binary y\_true, the score function is supposed to accept a 1D y\_pred (i.e., probability of the positive class or the decision function, shape (n\_samples,)).

For example average\_precision or the area under the roc curve can not be computed using discrete predictions alone.

\*\*kwargs [additional arguments] Additional parameters to be passed to score\_func.

#### Returns

**scorer** [callable] Callable object that returns a scalar score; greater is better.

# **Examples**

```
>>> from sklearn.metrics import fbeta_score, make_scorer
>>> ftwo_scorer = make_scorer(fbeta_score, beta=2)
>>> ftwo_scorer
make_scorer(fbeta_score, beta=2)
>>> from sklearn.model_selection import GridSearchCV
>>> from sklearn.svm import LinearSVC
>>> grid = GridSearchCV(LinearSVC(), param_grid={'C': [1, 10]},
... scoring=ftwo_scorer)
```

# Examples using sklearn.metrics.make\_scorer

 $\bullet \ \ Demonstration \ of \ multi-metric \ evaluation \ on \ cross\_val\_score \ and \ Grid Search CV$ 

# 6.24.2 Classification metrics

See the Classification metrics section of the user guide for further details.

<pre>metrics.accuracy_score(y_true, y_pred[,])</pre>	Accuracy classification score.
<pre>metrics.auc(x, y[, reorder])</pre>	Compute Area Under the Curve (AUC) using the trape-
	zoidal rule
metrics.average_precision_score(y_true,	Compute average precision (AP) from prediction scores
y_score)	
metrics.balanced_accuracy_score(y_true,	Compute the balanced accuracy
y_pred)	
<pre>metrics.brier_score_loss(y_true, y_prob[,])</pre>	Compute the Brier score.
metrics.classification_report(y_true,	Build a text report showing the main classification metrics
y_pred)	
metrics.cohen_kappa_score(y1, y2[, labels,])	Cohen's kappa: a statistic that measures inter-annotator
	agreement.
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<pre>metrics.confusion_matrix(y_true, y_pred[,])</pre>	Compute confusion matrix to evaluate the accuracy of a
	classification
<pre>metrics.f1_score(y_true, y_pred[, labels,])</pre>	Compute the F1 score, also known as balanced F-score or
	F-measure
<pre>metrics.fbeta_score(y_true, y_pred, beta[,])</pre>	Compute the F-beta score
<pre>metrics.hamming_loss(y_true, y_pred[,])</pre>	Compute the average Hamming loss.
<pre>metrics.hinge_loss(y_true, pred_decision[,])</pre>	Average hinge loss (non-regularized)
metrics.jaccard_score(y_true, y_pred[,])	Jaccard similarity coefficient score
<pre>metrics.log_loss(y_true, y_pred[, eps,])</pre>	Log loss, aka logistic loss or cross-entropy loss.
metrics.matthews_corrcoef(y_true, y_pred[,	Compute the Matthews correlation coefficient (MCC)
])	
metrics.multilabel_confusion_matrix(y_true	, Compute a confusion matrix for each class or sample
)	
metrics.precision_recall_curve(y_true,)	Compute precision-recall pairs for different probability
	thresholds
metrics.precision_recall_fscore_support(.	. Compute precision, recall, F-measure and support for each
	class
metrics.precision_score(y_true, y_pred[,])	Compute the precision
<pre>metrics.recall_score(y_true, y_pred[,])</pre>	Compute the recall
<pre>metrics.roc_auc_score(y_true, y_score[,])</pre>	Compute Area Under the Receiver Operating Characteris-
	tic Curve (ROC AUC) from prediction scores.
<pre>metrics.roc_curve(y_true, y_score[,])</pre>	Compute Receiver operating characteristic (ROC)
metrics.zero_one_loss(y_true, y_pred[,])	Zero-one classification loss.

### sklearn.metrics.accuracy\_score

sklearn.metrics.accuracy\_score(y\_true, y\_pred, normalize=True, sample\_weight=None)
Accuracy classification score.

In multilabel classification, this function computes subset accuracy: the set of labels predicted for a sample must *exactly* match the corresponding set of labels in y\_true.

Read more in the *User Guide*.

### **Parameters**

- **y\_true** [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) labels.
- **y\_pred** [1d array-like, or label indicator array / sparse matrix] Predicted labels, as returned by a classifier.

**normalize** [bool, optional (default=True)] If False, return the number of correctly classified samples. Otherwise, return the fraction of correctly classified samples.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] If normalize == True, return the fraction of correctly classified samples (float), else returns the number of correctly classified samples (int).

The best performance is 1 with normalize == True and the number of samples with normalize == False.

### See also:

jaccard\_score, hamming\_loss, zero\_one\_loss

### **Notes**

In binary and multiclass classification, this function is equal to the jaccard\_score function.

# **Examples**

```
>>> from sklearn.metrics import accuracy_score
>>> y_pred = [0, 2, 1, 3]
>>> y_true = [0, 1, 2, 3]
>>> accuracy_score(y_true, y_pred)
0.5
>>> accuracy_score(y_true, y_pred, normalize=False)
2
```

In the multilabel case with binary label indicators:

```
>>> import numpy as np
>>> accuracy_score(np.array([[0, 1], [1, 1]]), np.ones((2, 2)))
0.5
```

### Examples using sklearn.metrics.accuracy\_score

- Plot classification probability
- Multi-class AdaBoosted Decision Trees
- Probabilistic predictions with Gaussian process classification (GPC)
- Demonstration of multi-metric evaluation on cross\_val\_score and GridSearchCV
- Importance of Feature Scaling
- · Classification of text documents using sparse features

### sklearn.metrics.auc

```
sklearn.metrics.auc(x, y, reorder='deprecated')
```

Compute Area Under the Curve (AUC) using the trapezoidal rule

This is a general function, given points on a curve. For computing the area under the ROC-curve, see <code>roc\_auc\_score</code>. For an alternative way to summarize a precision-recall curve, see <code>average\_precision\_score</code>.

#### **Parameters**

- $\mathbf{x}$  [array, shape = [n]] x coordinates. These must be either monotonic increasing or monotonic decreasing.
- y [array, shape = [n]] y coordinates.

**reorder** [boolean, optional (default='deprecated')] Whether to sort x before computing. If False, assume that x must be either monotonic increasing or monotonic decreasing. If True, y is used to break ties when sorting x. Make sure that y has a monotonic relation to x when setting reorder to True.

Deprecated since version 0.20: Parameter reorder has been deprecated in version 0.20 and will be removed in 0.22. It's introduced for roc\_auc\_score (not for general use) and is

no longer used there. What's more, the result from auc will be significantly influenced if x is sorted unexpectedly due to slight floating point error (See issue #9786). Future (and default) behavior is equivalent to reorder=False.

#### Returns

auc [float]

#### See also:

roc\_auc\_score Compute the area under the ROC curve
average\_precision\_score Compute average precision from prediction scores
precision\_recall\_curve Compute precision-recall pairs for different probability thresholds

## **Examples**

```
>>> import numpy as np
>>> from sklearn import metrics
>>> y = np.array([1, 1, 2, 2])
>>> pred = np.array([0.1, 0.4, 0.35, 0.8])
>>> fpr, tpr, thresholds = metrics.roc_curve(y, pred, pos_label=2)
>>> metrics.auc(fpr, tpr)
0.75
```

### Examples using sklearn.metrics.auc

- Species distribution modeling
- Receiver Operating Characteristic (ROC) with cross validation
- Receiver Operating Characteristic (ROC)

## sklearn.metrics.average precision score

Compute average precision (AP) from prediction scores

AP summarizes a precision-recall curve as the weighted mean of precisions achieved at each threshold, with the increase in recall from the previous threshold used as the weight:

$$AP = \sum_{n} (R_n - R_{n-1}) P_n$$

where  $P_n$  and  $R_n$  are the precision and recall at the nth threshold [1]. This implementation is not interpolated and is different from computing the area under the precision-recall curve with the trapezoidal rule, which uses linear interpolation and can be too optimistic.

Note: this implementation is restricted to the binary classification task or multilabel classification task.

Read more in the *User Guide*.

### **Parameters**

y\_true [array, shape = [n\_samples] or [n\_samples, n\_classes]] True binary labels or binary label indicators.

- **y\_score** [array, shape = [n\_samples] or [n\_samples, n\_classes]] Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by "decision function" on some classifiers).
- **average** [string, [None, 'micro', 'macro' (default), 'samples', 'weighted']] If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:
  - 'micro': Calculate metrics globally by considering each element of the label indicator matrix as a label.
  - 'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
  - 'weighted': Calculate metrics for each label, and find their average, weighted by support (the number of true instances for each label).
  - 'samples': Calculate metrics for each instance, and find their average.

Will be ignored when y\_true is binary.

**pos\_label** [int or str (default=1)] The label of the positive class. Only applied to binary y\_true. For multilabel-indicator y\_true, pos\_label is fixed to 1.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

#### Returns

average\_precision [float]

#### See also:

roc\_auc\_score Compute the area under the ROC curve

precision\_recall\_curve Compute precision-recall pairs for different probability thresholds

# **Notes**

Changed in version 0.19: Instead of linearly interpolating between operating points, precisions are weighted by the change in recall since the last operating point.

### References

[1]

# **Examples**

```
>>> import numpy as np
>>> from sklearn.metrics import average_precision_score
>>> y_true = np.array([0, 0, 1, 1])
>>> y_scores = np.array([0.1, 0.4, 0.35, 0.8])
>>> average_precision_score(y_true, y_scores)
0.83...
```

### Examples using sklearn.metrics.average\_precision\_score

• Precision-Recall

### sklearn.metrics.balanced accuracy score

```
sklearn.metrics.balanced_accuracy_score(y_true, y_pred, sample_weight=None, ad-
justed=False)
```

Compute the balanced accuracy

The balanced accuracy in binary and multiclass classification problems to deal with imbalanced datasets. It is defined as the average of recall obtained on each class.

The best value is 1 and the worst value is 0 when adjusted=False.

Read more in the *User Guide*.

#### **Parameters**

```
y_true [1d array-like] Ground truth (correct) target values.
```

```
y_pred [1d array-like] Estimated targets as returned by a classifier.
```

```
sample_weight [array-like of shape = [n_samples], optional] Sample weights.
```

**adjusted** [bool, default=False] When true, the result is adjusted for chance, so that random performance would score 0, and perfect performance scores 1.

#### Returns

```
balanced_accuracy [float]
```

#### See also:

```
recall_score, roc_auc_score
```

### **Notes**

Some literature promotes alternative definitions of balanced accuracy. Our definition is equivalent to accuracy\_score with class-balanced sample weights, and shares desirable properties with the binary case. See the *User Guide*.

### References

[1], [2]

# **Examples**

```
>>> from sklearn.metrics import balanced_accuracy_score
>>> y_true = [0, 1, 0, 0, 1, 0]
>>> y_pred = [0, 1, 0, 0, 0, 1]
>>> balanced_accuracy_score(y_true, y_pred)
0.625
```

#### sklearn.metrics.brier score loss

```
sklearn.metrics.brier_score_loss(y_true, y_prob, sample_weight=None, pos_label=None)
```

Compute the Brier score. The smaller the Brier score, the better, hence the naming with "loss". Across all items in a set N predictions, the Brier score measures the mean squared difference between (1) the predicted probability assigned to the possible outcomes for item i, and (2) the actual outcome. Therefore, the lower the Brier score is for a set of predictions, the better the predictions are calibrated. Note that the Brier score always takes on a value between zero and one, since this is the largest possible difference between a predicted probability (which must be between zero and one) and the actual outcome (which can take on values of only 0 and 1). The Brier loss is composed of refinement loss and calibration loss. The Brier score is appropriate for binary and categorical outcomes that can be structured as true or false, but is inappropriate for ordinal variables which can take on three or more values (this is because the Brier score assumes that all possible outcomes are equivalently "distant" from one another). Which label is considered to be the positive label is controlled via the parameter pos label, which defaults to 1. Read more in the *User Guide*.

#### **Parameters**

```
y_true [array, shape (n_samples,)] True targets.
y_prob [array, shape (n_samples,)] Probabilities of the positive class.
sample_weight [array-like of shape = [n_samples], optional] Sample weights.
pos_label [int or str, default=None] Label of the positive class. Defaults to the greater label
```

unless y\_true is all 0 or all -1 in which case pos\_label defaults to 1.

#### Returns

score [float] Brier score

#### References

[1]

## **Examples**

# Examples using sklearn.metrics.brier\_score\_loss

• Probability Calibration curves

• Probability calibration of classifiers

### sklearn.metrics.classification report

```
sklearn.metrics.classification_report(y_true, y_pred, labels=None, target_names=None, sample_weight=None, digits=2, output_dict=False)
```

Build a text report showing the main classification metrics

Read more in the *User Guide*.

#### **Parameters**

- y\_true [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) target values.
- **y\_pred** [1d array-like, or label indicator array / sparse matrix] Estimated targets as returned by a classifier.

**labels** [array, shape =  $[n_labels]$ ] Optional list of label indices to include in the report.

target\_names [list of strings] Optional display names matching the labels (same order).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

**digits** [int] Number of digits for formatting output floating point values. When output\_dict is True, this will be ignored and the returned values will not be rounded.

output\_dict [bool (default = False)] If True, return output as dict

#### Returns

**report** [string / dict] Text summary of the precision, recall, F1 score for each class. Dictionary returned if output\_dict is True. Dictionary has the following structure:

The reported averages include macro average (averaging the unweighted mean per label), weighted average (averaging the support-weighted mean per label), sample average (only for multilabel classification) and micro average (averaging the total true positives, false negatives and false positives) it is only shown for multilabel or multi-class with a subset of classes because it is accuracy otherwise. See also:func:precision\_recall\_fscore\_support for more details on averages.

Note that in binary classification, recall of the positive class is also known as "sensitivity"; recall of the negative class is "specificity".

#### See also:

```
precision_recall_fscore_support, confusion_matrix
multilabel confusion matrix
```

# **Examples**

```
>>> from sklearn.metrics import classification_report
>>> y_true = [0, 1, 2, 2, 2]
>>> y_pred = [0, 0, 2, 2, 1]
>>> target_names = ['class 0', 'class 1', 'class 2']
>>> print(classification_report(y_true, y_pred, target_names=target_names))
             precision recall f1-score support
                0.50
    class 0
                         1.00
                                    0.67
                                                1
                0.00
                          0.00
                                    0.00
                                                1
    class 1
                          0.67
    class 2
                1.00
                                    0.80
                                                3
                                    0.60
                                                5
   accuracy
  macro avg
                0.50
                         0.56
                                   0.49
                                                5
weighted avg
                0.70
                          0.60
                                    0.61
>>> y_pred = [1, 1, 0]
>>> y_true = [1, 1, 1]
>>> print(classification_report(y_true, y_pred, labels=[1, 2, 3]))
            precision recall f1-score support
                                0.80
                1.00 0.67
0.00 0.00
          1
                                                3
          2
                                                0
          3
                 0.00
                          0.00
                                    0.00
                                                \cap
  micro avq
                1.00
                         0.67
                                    0.80
                                                3
  macro avg
                0.33
                         0.22
                                    0.27
                                                 3
weighted avg
                 1.00
                         0.67
                                    0.80
```

### Examples using sklearn.metrics.classification\_report

- Faces recognition example using eigenfaces and SVMs
- Recognizing hand-written digits
- Column Transformer with Heterogeneous Data Sources
- Pipeline Anova SVM
- Parameter estimation using grid search with cross-validation
- Restricted Boltzmann Machine features for digit classification
- Label Propagation digits: Demonstrating performance
- · Label Propagation digits active learning
- Classification of text documents using sparse features

### sklearn.metrics.cohen kappa score

```
sklearn.metrics.cohen_kappa_score (y1, y2, labels=None, weights=None, sam-ple\_weight=None)

Cohen's kappa: a statistic that measures inter-annotator agreement.
```

This function computes Cohen's kappa [1], a score that expresses the level of agreement between two annotators on a classification problem. It is defined as

$$\kappa = (p_o - p_e)/(1 - p_e)$$

where  $p_o$  is the empirical probability of agreement on the label assigned to any sample (the observed agreement ratio), and  $p_e$  is the expected agreement when both annotators assign labels randomly.  $p_e$  is estimated using a per-annotator empirical prior over the class labels [2].

Read more in the User Guide.

#### **Parameters**

- **y1** [array, shape = [n\_samples]] Labels assigned by the first annotator.
- y2 [array, shape =  $[n_samples]$ ] Labels assigned by the second annotator. The kappa statistic is symmetric, so swapping y1 and y2 doesn't change the value.

**labels** [array, shape =  $[n_{classes}]$ , optional] List of labels to index the matrix. This may be used to select a subset of labels. If None, all labels that appear at least once in y1 or y2 are used.

weights [str, optional] List of weighting type to calculate the score. None means no weighted; "linear" means linear weighted; "quadratic" means quadratic weighted.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

#### Returns

**kappa** [float] The kappa statistic, which is a number between -1 and 1. The maximum value means complete agreement; zero or lower means chance agreement.

### References

[1], [2], [3]

### sklearn.metrics.confusion\_matrix

sklearn.metrics.confusion\_matrix (y\_true, y\_pred, labels=None, sample\_weight=None)
Compute confusion matrix to evaluate the accuracy of a classification

By definition a confusion matrix C is such that  $C_{i,j}$  is equal to the number of observations known to be in group i but predicted to be in group j.

Thus in binary classification, the count of true negatives is  $C_{0,0}$ , false negatives is  $C_{1,0}$ , true positives is  $C_{1,1}$  and false positives is  $C_{0,1}$ .

Read more in the *User Guide*.

#### **Parameters**

**y\_true** [array, shape = [n\_samples]] Ground truth (correct) target values.

**y\_pred** [array, shape = [n\_samples]] Estimated targets as returned by a classifier.

**labels** [array, shape = [n\_classes], optional] List of labels to index the matrix. This may be used to reorder or select a subset of labels. If none is given, those that appear at least once in y\_true or y\_pred are used in sorted order.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

#### **Returns**

C [array, shape = [n\_classes, n\_classes]] Confusion matrix

### References

[1]

# **Examples**

In the binary case, we can extract true positives, etc as follows:

```
>>> tn, fp, fn, tp = confusion_matrix([0, 1, 0, 1], [1, 1, 1, 0]).ravel()
>>> (tn, fp, fn, tp)
(0, 2, 1, 1)
```

#### Examples using sklearn.metrics.confusion\_matrix

- Faces recognition example using eigenfaces and SVMs
- · Recognizing hand-written digits
- Confusion matrix
- Label Propagation digits: Demonstrating performance
- · Label Propagation digits active learning
- Classification of text documents using sparse features

### sklearn.metrics.f1 score

```
sklearn.metrics.fl_score(y_true, y_pred, labels=None, pos_label=1, average='binary', sam-ple_weight=None)
```

Compute the F1 score, also known as balanced F-score or F-measure

The F1 score can be interpreted as a weighted average of the precision and recall, where an F1 score reaches its best value at 1 and worst score at 0. The relative contribution of precision and recall to the F1 score are equal. The formula for the F1 score is:

```
F1 = 2 * (precision * recall) / (precision + recall)
```

In the multi-class and multi-label case, this is the average of the F1 score of each class with weighting depending on the average parameter.

Read more in the *User Guide*.

#### **Parameters**

- y\_true [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) target values.
- **y\_pred** [1d array-like, or label indicator array / sparse matrix] Estimated targets as returned by a classifier.
- labels [list, optional] The set of labels to include when average != 'binary', and their order if average is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in y\_true and y\_pred are used in sorted order.

Changed in version 0.17: parameter *labels* improved for multiclass problem.

- pos\_label [str or int, 1 by default] The class to report if average='binary' and the
   data is binary. If the data are multiclass or multilabel, this will be ignored; setting
   labels=[pos\_label] and average != 'binary' will report scores for that la bel only.
- **average** [string, [None, 'binary' (default), 'micro', 'macro', 'samples', 'weighted']] This parameter is required for multiclass/multilabel targets. If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:
  - 'binary': Only report results for the class specified by pos\_label. This is applicable only if targets (y\_{true,pred}) are binary.
  - 'micro': Calculate metrics globally by counting the total true positives, false negatives and false positives.
  - 'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
  - 'weighted': Calculate metrics for each label, and find their average weighted by support (the number of true instances for each label). This alters 'macro' to account for label imbalance; it can result in an F-score that is not between precision and recall.
  - 'samples': Calculate metrics for each instance, and find their average (only meaningful for multilabel classification where this differs from accuracy\_score).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

**f1\_score** [float or array of float, shape = [n\_unique\_labels]] F1 score of the positive class in binary classification or weighted average of the F1 scores of each class for the multiclass task.

#### See also:

fbeta\_score, precision\_recall\_fscore\_support, jaccard\_score
multilabel\_confusion\_matrix

### **Notes**

When true positive + false positive == 0 or true positive + false negative == 0, f-score returns 0 and raises UndefinedMetricWarning.

#### References

[1]

# **Examples**

```
>>> from sklearn.metrics import f1_score
>>> y_true = [0, 1, 2, 0, 1, 2]
>>> y_pred = [0, 2, 1, 0, 0, 1]
>>> f1_score(y_true, y_pred, average='macro')
0.26...
>>> f1_score(y_true, y_pred, average='micro')
0.33...
>>> f1_score(y_true, y_pred, average='weighted')
0.26...
>>> f1_score(y_true, y_pred, average='weighted')
array([0.8, 0., 0.])
```

# Examples using sklearn.metrics.fl\_score

• Probability Calibration curves

#### sklearn.metrics.fbeta score

Compute the F-beta score

The F-beta score is the weighted harmonic mean of precision and recall, reaching its optimal value at 1 and its worst value at 0.

The beta parameter determines the weight of recall in the combined score. beta < 1 lends more weight to precision, while beta > 1 favors recall (beta -> 0 considers only precision, beta -> inf only recall).

Read more in the User Guide.

## **Parameters**

- y\_true [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) target values.
- **y\_pred** [1d array-like, or label indicator array / sparse matrix] Estimated targets as returned by a classifier.

beta [float] Weight of precision in harmonic mean.

labels [list, optional] The set of labels to include when average != 'binary', and their order if average is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in

the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in y\_true and y\_pred are used in sorted order.

Changed in version 0.17: parameter *labels* improved for multiclass problem.

- pos\_label [str or int, 1 by default] The class to report if average='binary' and the
   data is binary. If the data are multiclass or multilabel, this will be ignored; setting
   labels=[pos\_label] and average != 'binary' will report scores for that la bel only.
- **average** [string, [None, 'binary' (default), 'micro', 'macro', 'samples', 'weighted']] This parameter is required for multiclass/multilabel targets. If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:
  - 'binary': Only report results for the class specified by pos\_label. This is applicable only if targets (y\_{true,pred}) are binary.
  - 'micro': Calculate metrics globally by counting the total true positives, false negatives and false positives.
  - 'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
  - 'weighted': Calculate metrics for each label, and find their average weighted by support (the number of true instances for each label). This alters 'macro' to account for label imbalance; it can result in an F-score that is not between precision and recall.
  - 'samples': Calculate metrics for each instance, and find their average (only meaningful for multilabel classification where this differs from accuracy score).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

## Returns

**fbeta\_score** [float (if average is not None) or array of float, shape = [n\_unique\_labels]] F-beta score of the positive class in binary classification or weighted average of the F-beta score of each class for the multiclass task.

#### See also:

```
precision recall fscore support, multilabel confusion matrix
```

# **Notes**

When true positive + false positive == 0 or true positive + false negative == 0, f-score returns 0 and raises UndefinedMetricWarning.

# References

[1], [2]

### **Examples**

```
>>> from sklearn.metrics import fbeta_score
>>> y_true = [0, 1, 2, 0, 1, 2]
>>> y_pred = [0, 2, 1, 0, 0, 1]
>>> fbeta_score(y_true, y_pred, average='macro', beta=0.5)
```

```
0.23...
>>> fbeta_score(y_true, y_pred, average='micro', beta=0.5)
...
0.33...
>>> fbeta_score(y_true, y_pred, average='weighted', beta=0.5)
...
0.23...
>>> fbeta_score(y_true, y_pred, average=None, beta=0.5)
...
array([0.71..., 0. , 0. ])
```

## sklearn.metrics.hamming\_loss

sklearn.metrics.hamming\_loss (y\_true, y\_pred, labels=None, sample\_weight=None) Compute the average Hamming loss.

The Hamming loss is the fraction of labels that are incorrectly predicted.

Read more in the *User Guide*.

### **Parameters**

**y\_true** [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) labels.

**y\_pred** [1d array-like, or label indicator array / sparse matrix] Predicted labels, as returned by a classifier.

**labels** [array, shape = [n\_labels], optional (default='deprecated')] Integer array of labels. If not provided, labels will be inferred from y\_true and y\_pred.

New in version 0.18.

Deprecated since version 0.21: This parameter labels is deprecated in version 0.21 and will be removed in version 0.23. Hamming loss uses  $y_true.shape[1]$  for the number of labels when  $y_true$  is binary label indicators, so it is unnecessary for the user to specify.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

New in version 0.18.

### Returns

loss [float or int,] Return the average Hamming loss between element of y\_true and y\_pred.

### See also:

```
accuracy_score, jaccard_score, zero_one_loss
```

### **Notes**

In multiclass classification, the Hamming loss corresponds to the Hamming distance between y\_true and y\_pred which is equivalent to the subset zero\_one\_loss function, when normalize parameter is set to True.

In multilabel classification, the Hamming loss is different from the subset zero-one loss. The zero-one loss considers the entire set of labels for a given sample incorrect if it does not entirely match the true set of labels. Hamming loss is more forgiving in that it penalizes only the individual labels.

The Hamming loss is upperbounded by the subset zero-one loss, when normalize parameter is set to True. It is always between 0 and 1, lower being better.

### References

[1], [2]

## **Examples**

```
>>> from sklearn.metrics import hamming_loss

>>> y_pred = [1, 2, 3, 4]

>>> y_true = [2, 2, 3, 4]

>>> hamming_loss(y_true, y_pred)

0.25
```

In the multilabel case with binary label indicators:

```
>>> import numpy as np
>>> hamming_loss(np.array([[0, 1], [1, 1]]), np.zeros((2, 2)))
0.75
```

## Examples using sklearn.metrics.hamming loss

• Model Complexity Influence

### sklearn.metrics.hinge loss

```
sklearn.metrics.hinge_loss (y_true, pred_decision, labels=None, sample_weight=None)
Average hinge loss (non-regularized)
```

In binary class case, assuming labels in y\_true are encoded with +1 and -1, when a prediction mistake is made, margin = y\_true \* pred\_decision is always negative (since the signs disagree), implying 1 - margin is always greater than 1. The cumulated hinge loss is therefore an upper bound of the number of mistakes made by the classifier.

In multiclass case, the function expects that either all the labels are included in y\_true or an optional labels argument is provided which contains all the labels. The multilabel margin is calculated according to Crammer-Singer's method. As in the binary case, the cumulated hinge loss is an upper bound of the number of mistakes made by the classifier.

Read more in the User Guide.

## **Parameters**

**y\_true** [array, shape = [n\_samples]] True target, consisting of integers of two values. The positive label must be greater than the negative label.

**pred\_decision** [array, shape = [n\_samples] or [n\_samples, n\_classes]] Predicted decisions, as output by decision\_function (floats).

**labels** [array, optional, default None] Contains all the labels for the problem. Used in multiclass hinge loss.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

loss [float]

### References

[1], [2], [3]

## **Examples**

## In the multiclass case:

## sklearn.metrics.jaccard\_score

Jaccard similarity coefficient score

The Jaccard index [1], or Jaccard similarity coefficient, defined as the size of the intersection divided by the size of the union of two label sets, is used to compare set of predicted labels for a sample to the corresponding set of labels in y\_true.

Read more in the User Guide.

### **Parameters**

- y true [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) labels.
- y\_pred [1d array-like, or label indicator array / sparse matrix] Predicted labels, as returned by a classifier.
- labels [list, optional] The set of labels to include when average != 'binary', and their order if average is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in y\_true and y\_pred are used in sorted order.
- pos\_label [str or int, 1 by default] The class to report if average='binary' and the
   data is binary. If the data are multiclass or multilabel, this will be ignored; setting
   labels=[pos\_label] and average != 'binary' will report scores for that la bel only.
- **average** [string, [None, 'binary' (default), 'micro', 'macro', 'samples', 'weighted']] If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:
  - 'binary': Only report results for the class specified by pos\_label. This is applicable only if targets (y\_{true,pred}) are binary.
  - 'micro': Calculate metrics globally by counting the total true positives, false negatives and false positives.
  - 'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
  - 'weighted': Calculate metrics for each label, and find their average, weighted by support (the number of true instances for each label). This alters 'macro' to account for label imbalance.
  - 'samples': Calculate metrics for each instance, and find their average (only meaningful for multilabel classification).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float (if average is not None) or array of floats, shape = [n\_unique\_labels]]

### See also:

```
accuracy_score, f_score, multilabel_confusion_matrix
```

### **Notes**

jaccard\_score may be a poor metric if there are no positives for some samples or classes. Jaccard is undefined if there are no true or predicted labels, and our implementation will return a score of 0 with a warning.

### References

[1]

# **Examples**

## In the binary case:

```
>>> jaccard_score(y_true[0], y_pred[0])
0.6666...
```

### In the multilabel case:

```
>>> jaccard_score(y_true, y_pred, average='samples')
0.5833...
>>> jaccard_score(y_true, y_pred, average='macro')
0.6666...
>>> jaccard_score(y_true, y_pred, average=None)
array([0.5, 0.5, 1.])
```

### In the multiclass case:

```
>>> y_pred = [0, 2, 1, 2]

>>> y_true = [0, 1, 2, 2]

>>> jaccard_score(y_true, y_pred, average=None)

...

array([1., 0., 0.33...])
```

## Examples using sklearn.metrics.jaccard\_score

• Classifier Chain

## sklearn.metrics.log\_loss

```
sklearn.metrics.log_loss(y_true, y_pred, eps=1e-15, normalize=True, sample_weight=None, labels=None)
```

Log loss, aka logistic loss or cross-entropy loss.

This is the loss function used in (multinomial) logistic regression and extensions of it such as neural networks, defined as the negative log-likelihood of the true labels given a probabilistic classifier's predictions. The log loss is only defined for two or more labels. For a single sample with true label yt in  $\{0,1\}$  and estimated probability yp that yt = 1, the log loss is

```
-\log P(yt|yp) = -(yt \log(yp) + (1 - yt) \log(1 - yp))
```

Read more in the User Guide.

### **Parameters**

**y\_true** [array-like or label indicator matrix] Ground truth (correct) labels for n\_samples samples.

- y\_pred [array-like of float, shape = (n\_samples, n\_classes) or (n\_samples,)] Predicted probabilities, as returned by a classifier's predict\_proba method. If y\_pred.shape =
   (n\_samples,) the probabilities provided are assumed to be that of the positive class. The
   labels in y\_pred are assumed to be ordered alphabetically, as done by preprocessing.
   LabelBinarizer.
- eps [float] Log loss is undefined for p=0 or p=1, so probabilities are clipped to max(eps, min(1 eps, p)).
- **normalize** [bool, optional (default=True)] If true, return the mean loss per sample. Otherwise, return the sum of the per-sample losses.
- **sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.
- labels [array-like, optional (default=None)] If not provided, labels will be inferred from y\_true. If labels is None and y\_pred has shape (n\_samples,) the labels are assumed to be binary and are inferred from y\_true. .. versionadded:: 0.18

### Returns

loss [float]

### **Notes**

The logarithm used is the natural logarithm (base-e).

## References

C.M. Bishop (2006). Pattern Recognition and Machine Learning. Springer, p. 209.

### **Examples**

```
>>> from sklearn.metrics import log_loss
>>> log_loss(["spam", "ham", "spam"],
... [[.1, .9], [.9, .1], [.8, .2], [.35, .65]])
0.21616...
```

### Examples using sklearn.metrics.log\_loss

- Probability Calibration for 3-class classification
- Probabilistic predictions with Gaussian process classification (GPC)

### sklearn.metrics.matthews corrcoef

```
sklearn.metrics.matthews_corrcoef(y_true, y_pred, sample_weight=None)
Compute the Matthews correlation coefficient (MCC)
```

The Matthews correlation coefficient is used in machine learning as a measure of the quality of binary and multiclass classifications. It takes into account true and false positives and negatives and is generally regarded as a balanced measure which can be used even if the classes are of very different sizes. The MCC is in essence a correlation coefficient value between -1 and +1. A coefficient of +1 represents a perfect prediction, 0 an average

random prediction and -1 an inverse prediction. The statistic is also known as the phi coefficient. [source: Wikipedia]

Binary and multiclass labels are supported. Only in the binary case does this relate to information about true and false positives and negatives. See references below.

Read more in the User Guide.

### **Parameters**

```
    y_true [array, shape = [n_samples]] Ground truth (correct) target values.
    y_pred [array, shape = [n_samples]] Estimated targets as returned by a classifier.
    sample_weight [array-like of shape = [n_samples], default None] Sample weights.
```

#### Returns

**mcc** [float] The Matthews correlation coefficient (+1 represents a perfect prediction, 0 an average random prediction and -1 and inverse prediction).

### References

[1], [2], [3], [4]

# **Examples**

```
>>> from sklearn.metrics import matthews_corrcoef
>>> y_true = [+1, +1, +1, -1]
>>> y_pred = [+1, -1, +1, +1]
>>> matthews_corrcoef(y_true, y_pred)
-0.33...
```

## sklearn.metrics.multilabel confusion matrix

```
sklearn.metrics.multilabel_confusion_matrix(y_true, y_pred, sample_weight=None, labels=None, samplewise=False)
```

Compute a confusion matrix for each class or sample

New in version 0.21.

Compute class-wise (default) or sample-wise (samplewise=True) multilabel confusion matrix to evaluate the accuracy of a classification, and output confusion matrices for each class or sample.

In multilabel confusion matrix MCM, the count of true negatives is  $MCM_{:,0,0}$ , false negatives is  $MCM_{:,1,0}$ , true positives is  $MCM_{:,1,1}$  and false positives is  $MCM_{:,0,1}$ .

Multiclass data will be treated as if binarized under a one-vs-rest transformation. Returned confusion matrices will be in the order of sorted unique labels in the union of (y\_true, y\_pred).

Read more in the User Guide.

### **Parameters**

- **y\_true** [1d array-like, or label indicator array / sparse matrix] of shape (n\_samples, n\_outputs) or (n\_samples,) Ground truth (correct) target values.
- **y\_pred** [1d array-like, or label indicator array / sparse matrix] of shape (n\_samples, n\_outputs) or (n\_samples,) Estimated targets as returned by a classifier

**sample\_weight** [array-like of shape = (n\_samples,), optional] Sample weights

**labels** [array-like] A list of classes or column indices to select some (or to force inclusion of classes absent from the data)

**samplewise** [bool, default=False] In the multilabel case, this calculates a confusion matrix per sample

### Returns

multi\_confusion [array, shape (n\_outputs, 2, 2)] A 2x2 confusion matrix corresponding to each output in the input. When calculating class-wise multi\_confusion (default), then n\_outputs = n\_labels; when calculating sample-wise multi\_confusion (samplewise=True), n\_outputs = n\_samples. If labels is defined, the results will be returned in the order specified in labels, otherwise the results will be returned in sorted order by default.

### See also:

confusion matrix

### **Notes**

The multilabel\_confusion\_matrix calculates class-wise or sample-wise multilabel confusion matrices, and in multiclass tasks, labels are binarized under a one-vs-rest way; while confusion\_matrix calculates one confusion matrix for confusion between every two classes.

## **Examples**

Multilabel-indicator case:

### Multiclass case:

```
[[2, 1],
[1, 2]]])
```

## sklearn.metrics.precision\_recall\_curve

```
sklearn.metrics.precision_recall_curve(y_true, probas_pred, pos_label=None, sample weight=None)
```

Compute precision-recall pairs for different probability thresholds

Note: this implementation is restricted to the binary classification task.

The precision is the ratio tp / (tp + fp) where tp is the number of true positives and fp the number of false positives. The precision is intuitively the ability of the classifier not to label as positive a sample that is negative.

The recall is the ratio tp / (tp + fn) where tp is the number of true positives and fn the number of false negatives. The recall is intuitively the ability of the classifier to find all the positive samples.

The last precision and recall values are 1. and 0. respectively and do not have a corresponding threshold. This ensures that the graph starts on the y axis.

Read more in the User Guide.

### **Parameters**

**y\_true** [array, shape =  $[n_samples]$ ] True binary labels. If labels are not either  $\{-1, 1\}$  or  $\{0, 1\}$ , then pos\_label should be explicitly given.

**probas\_pred** [array, shape = [n\_samples]] Estimated probabilities or decision function.

**pos\_label** [int or str, default=None] The label of the positive class. When pos\_label=None, if y\_true is in {-1, 1} or {0, 1}, pos\_label is set to 1, otherwise an error will be raised.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

**precision** [array, shape = [n\_thresholds + 1]] Precision values such that element i is the precision of predictions with score >= thresholds[i] and the last element is 1.

**recall** [array, shape = [n\_thresholds + 1]] Decreasing recall values such that element i is the recall of predictions with score >= thresholds[i] and the last element is 0.

**thresholds** [array, shape = [n\_thresholds <= len(np.unique(probas\_pred))]] Increasing thresholds on the decision function used to compute precision and recall.

### See also:

```
average_precision_score Compute average precision from prediction scores
roc_curve Compute Receiver operating characteristic (ROC) curve
```

## **Examples**

```
>>> import numpy as np
>>> from sklearn.metrics import precision_recall_curve
>>> y_true = np.array([0, 0, 1, 1])
>>> y_scores = np.array([0.1, 0.4, 0.35, 0.8])
```

```
>>> precision, recall, thresholds = precision_recall_curve(
... y_true, y_scores)
>>> precision
array([0.66666667, 0.5 , 1. , 1. ])
>>> recall
array([1., 0.5, 0.5, 0.])
>>> thresholds
array([0.35, 0.4 , 0.8])
```

## Examples using sklearn.metrics.precision\_recall\_curve

• Precision-Recall

## sklearn.metrics.precision recall fscore support

```
sklearn.metrics.precision_recall_fscore_support (y_true, y_pred, beta=1.0, la-bels=None, pos_label=1, average=None, warn_for=('precision', 'recall', 'f-score'), sample_weight=None)
```

Compute precision, recall, F-measure and support for each class

The precision is the ratio tp / (tp + fp) where tp is the number of true positives and fp the number of false positives. The precision is intuitively the ability of the classifier not to label as positive a sample that is negative.

The recall is the ratio tp / (tp + fn) where tp is the number of true positives and fn the number of false negatives. The recall is intuitively the ability of the classifier to find all the positive samples.

The F-beta score can be interpreted as a weighted harmonic mean of the precision and recall, where an F-beta score reaches its best value at 1 and worst score at 0.

The F-beta score weights recall more than precision by a factor of beta. beta == 1.0 means recall and precision are equally important.

The support is the number of occurrences of each class in y\_true.

If pos\_label is None and in binary classification, this function returns the average precision, recall and F-measure if average is one of 'micro', 'macro', 'weighted' or 'samples'.

Read more in the User Guide.

### **Parameters**

- **y\_true** [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) target values.
- **y\_pred** [1d array-like, or label indicator array / sparse matrix] Estimated targets as returned by a classifier.

**beta** [float, 1.0 by default] The strength of recall versus precision in the F-score.

labels [list, optional] The set of labels to include when average != 'binary', and their order if average is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in y true and y pred are used in sorted order.

- pos\_label [str or int, 1 by default] The class to report if average='binary' and the
   data is binary. If the data are multiclass or multilabel, this will be ignored; setting
   labels=[pos\_label] and average != 'binary' will report scores for that la bel only.
- **average** [string, [None (default), 'binary', 'micro', 'macro', 'samples', 'weighted']] If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:
  - 'binary': Only report results for the class specified by pos\_label. This is applicable only if targets (y\_{true,pred}) are binary.
  - 'micro': Calculate metrics globally by counting the total true positives, false negatives and false positives.
  - 'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
  - 'weighted': Calculate metrics for each label, and find their average weighted by support (the number of true instances for each label). This alters 'macro' to account for label imbalance; it can result in an F-score that is not between precision and recall.
  - 'samples': Calculate metrics for each instance, and find their average (only meaningful for multilabel classification where this differs from accuracy\_score).
- warn\_for [tuple or set, for internal use] This determines which warnings will be made in the case that this function is being used to return only one of its metrics.
- **sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

```
\label{eq:precision} \textbf{[float (if average is not None) or array of float, shape = [n\_unique\_labels]]}
```

**recall** [float (if average is not None) or array of float, , shape = [n unique labels]]

**fbeta\_score** [float (if average is not None) or array of float, shape = [n\_unique\_labels]]

**support** [int (if average is not None) or array of int, shape = [n\_unique\_labels]] The number of occurrences of each label in y\_true.

### **Notes**

When true positive + false positive == 0, precision is undefined; When true positive + false negative == 0, recall is undefined. In such cases, the metric will be set to 0, as will f-score, and UndefinedMetricWarning will be raised.

### References

[1], [2], [3]

# **Examples**

```
>>> import numpy as np
>>> from sklearn.metrics import precision_recall_fscore_support
>>> y_true = np.array(['cat', 'dog', 'pig', 'cat', 'dog', 'pig'])
>>> y_pred = np.array(['cat', 'pig', 'dog', 'cat', 'cat', 'dog'])
```

```
>>> precision_recall_fscore_support(y_true, y_pred, average='macro')
...
(0.22..., 0.33..., 0.26..., None)
>>> precision_recall_fscore_support(y_true, y_pred, average='micro')
...
(0.33..., 0.33..., 0.33..., None)
>>> precision_recall_fscore_support(y_true, y_pred, average='weighted')
...
(0.22..., 0.33..., 0.26..., None)
```

It is possible to compute per-label precisions, recalls, F1-scores and supports instead of averaging:

```
>>> precision_recall_fscore_support(y_true, y_pred, average=None,
... labels=['pig', 'dog', 'cat'])
...
(array([0. , 0. , 0.66...]),
array([0., 0., 1.]), array([0. , 0. , 0.8]),
array([2, 2, 2]))
```

## sklearn.metrics.precision score

Compute the precision

The precision is the ratio tp / (tp + fp) where tp is the number of true positives and fp the number of false positives. The precision is intuitively the ability of the classifier not to label as positive a sample that is negative.

The best value is 1 and the worst value is 0.

Read more in the User Guide.

## **Parameters**

- y\_true [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) target values.
- **y\_pred** [1d array-like, or label indicator array / sparse matrix] Estimated targets as returned by a classifier.
- labels [list, optional] The set of labels to include when average != 'binary', and their order if average is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in y\_true and y\_pred are used in sorted order.

Changed in version 0.17: parameter *labels* improved for multiclass problem.

- pos\_label [str or int, 1 by default] The class to report if average='binary' and the
   data is binary. If the data are multiclass or multilabel, this will be ignored; setting
   labels=[pos\_label] and average != 'binary' will report scores for that la bel only.
- **average** [string, [None, 'binary' (default), 'micro', 'macro', 'samples', 'weighted']] This parameter is required for multiclass/multilabel targets. If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:

- 'binary': Only report results for the class specified by pos\_label. This is applicable only if targets (y\_{true,pred}) are binary.
- 'micro': Calculate metrics globally by counting the total true positives, false negatives and false positives.
- 'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
- 'weighted': Calculate metrics for each label, and find their average weighted by support (the number of true instances for each label). This alters 'macro' to account for label imbalance; it can result in an F-score that is not between precision and recall.
- 'samples': Calculate metrics for each instance, and find their average (only meaningful for multilabel classification where this differs from accuracy\_score).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

**precision** [float (if average is not None) or array of float, shape = [n\_unique\_labels]] Precision of the positive class in binary classification or weighted average of the precision of each class for the multiclass task.

### See also:

precision\_recall\_fscore\_support, multilabel\_confusion\_matrix

### **Notes**

When true positive + false positive == 0, precision returns 0 and raises UndefinedMetricWarning.

# **Examples**

```
>>> from sklearn.metrics import precision_score
>>> y_true = [0, 1, 2, 0, 1, 2]
>>> y_pred = [0, 2, 1, 0, 0, 1]
>>> precision_score(y_true, y_pred, average='macro')
0.22...
>>> precision_score(y_true, y_pred, average='micro')
0.33...
>>> precision_score(y_true, y_pred, average='weighted')
...
0.22...
>>> precision_score(y_true, y_pred, average=None)
array([0.66..., 0. , 0. ])
```

# Examples using sklearn.metrics.precision\_score

• Probability Calibration curves

### sklearn.metrics.recall score

sklearn.metrics.recall\_score(y\_true, y\_pred, labels=None, pos\_label=1, average='binary', sam-ple\_weight=None)

Compute the recall

The recall is the ratio tp / (tp + fn) where tp is the number of true positives and fn the number of false negatives. The recall is intuitively the ability of the classifier to find all the positive samples.

The best value is 1 and the worst value is 0.

Read more in the *User Guide*.

### **Parameters**

- y\_true [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) target values.
- **y\_pred** [1d array-like, or label indicator array / sparse matrix] Estimated targets as returned by a classifier.
- labels [list, optional] The set of labels to include when average != 'binary', and their order if average is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in y\_true and y\_pred are used in sorted order.

Changed in version 0.17: parameter *labels* improved for multiclass problem.

- pos\_label [str or int, 1 by default] The class to report if average='binary' and the
   data is binary. If the data are multiclass or multilabel, this will be ignored; setting
   labels=[pos\_label] and average != 'binary' will report scores for that label only.
- **average** [string, [None, 'binary' (default), 'micro', 'macro', 'samples', 'weighted']] This parameter is required for multiclass/multilabel targets. If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:
  - 'binary': Only report results for the class specified by pos\_label. This is applicable only if targets (y\_{true,pred}) are binary.
  - 'micro': Calculate metrics globally by counting the total true positives, false negatives and false positives.
  - 'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
  - 'weighted': Calculate metrics for each label, and find their average weighted by support (the number of true instances for each label). This alters 'macro' to account for label imbalance; it can result in an F-score that is not between precision and recall.
  - 'samples': Calculate metrics for each instance, and find their average (only meaningful for multilabel classification where this differs from accuracy\_score).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

**recall** [float (if average is not None) or array of float, shape = [n\_unique\_labels]] Recall of the positive class in binary classification or weighted average of the recall of each class for the multiclass task.

See also:

```
precision_recall_fscore_support, balanced_accuracy_score
multilabel_confusion_matrix
```

### **Notes**

When true positive + false negative == 0, recall returns 0 and raises UndefinedMetricWarning.

## **Examples**

```
>>> from sklearn.metrics import recall_score
>>> y_true = [0, 1, 2, 0, 1, 2]
>>> y_pred = [0, 2, 1, 0, 0, 1]
>>> recall_score(y_true, y_pred, average='macro')
0.33...
>>> recall_score(y_true, y_pred, average='micro')
0.33...
>>> recall_score(y_true, y_pred, average='weighted')
0.33...
>>> recall_score(y_true, y_pred, average='weighted')
0.33...
>>> recall_score(y_true, y_pred, average=None)
array([1., 0., 0.])
```

# Examples using sklearn.metrics.recall\_score

• Probability Calibration curves

## sklearn.metrics.roc\_auc\_score

```
sklearn.metrics.roc_auc_score(y_true, y_score, average='macro', sample_weight=None, max fpr=None)
```

Compute Area Under the Receiver Operating Characteristic Curve (ROC AUC) from prediction scores.

Note: this implementation is restricted to the binary classification task or multilabel classification task in label indicator format.

Read more in the User Guide.

# **Parameters**

- y\_true [array, shape = [n\_samples] or [n\_samples, n\_classes]] True binary labels or binary label indicators.
- **y\_score** [array, shape = [n\_samples] or [n\_samples, n\_classes]] Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by "decision\_function" on some classifiers). For binary y\_true, y\_score is supposed to be the score of the class with greater label.
- **average** [string, [None, 'micro', 'macro' (default), 'samples', 'weighted']] If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:
  - 'micro': Calculate metrics globally by considering each element of the label indicator matrix as a label.

- 'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
- 'weighted': Calculate metrics for each label, and find their average, weighted by support (the number of true instances for each label).
- 'samples': Calculate metrics for each instance, and find their average.

Will be ignored when y\_true is binary.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

max\_fpr [float > 0 and <= 1, optional] If not None, the standardized partial AUC [3] over the range [0, max\_fpr] is returned.

### Returns

auc [float]

### See also:

average\_precision\_score Area under the precision-recall curve
roc\_curve Compute Receiver operating characteristic (ROC) curve

## References

[1], [2], [3]

## **Examples**

```
>>> import numpy as np
>>> from sklearn.metrics import roc_auc_score
>>> y_true = np.array([0, 0, 1, 1])
>>> y_scores = np.array([0.1, 0.4, 0.35, 0.8])
>>> roc_auc_score(y_true, y_scores)
0.75
```

# sklearn.metrics.roc\_curve

```
sklearn.metrics.roc_curve(y_true, y_score, pos_label=None, sample_weight=None, drop_intermediate=True)
```

Compute Receiver operating characteristic (ROC)

Note: this implementation is restricted to the binary classification task.

Read more in the User Guide.

# **Parameters**

- **y\_true** [array, shape =  $[n_samples]$ ] True binary labels. If labels are not either  $\{-1, 1\}$  or  $\{0, 1\}$ , then pos\_label should be explicitly given.
- **y\_score** [array, shape = [n\_samples]] Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by "decision function" on some classifiers).
- **pos\_label** [int or str, default=None] The label of the positive class. When  $pos_label=None$ , if y\_true is in  $\{-1, 1\}$  or  $\{0, 1\}$ ,  $pos_label$  is set to 1, otherwise an error will be raised.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

**drop\_intermediate** [boolean, optional (default=True)] Whether to drop some suboptimal thresholds which would not appear on a plotted ROC curve. This is useful in order to create lighter ROC curves.

New in version 0.17: parameter *drop\_intermediate*.

### Returns

- **fpr** [array, shape = [>2]] Increasing false positive rates such that element i is the false positive rate of predictions with score >= thresholds[i].
- **tpr** [array, shape = [>2]] Increasing true positive rates such that element i is the true positive rate of predictions with score >= thresholds[i].
- thresholds [array, shape = [n\_thresholds]] Decreasing thresholds on the decision function used to compute fpr and tpr. thresholds[0] represents no instances being predicted and is arbitrarily set to max(y\_score) + 1.

## See also:

roc\_auc\_score Compute the area under the ROC curve

## **Notes**

Since the thresholds are sorted from low to high values, they are reversed upon returning them to ensure they correspond to both fpr and tpr, which are sorted in reversed order during their calculation.

### References

[1], [2]

# **Examples**

```
>>> import numpy as np
>>> from sklearn import metrics
>>> y = np.array([1, 1, 2, 2])
>>> scores = np.array([0.1, 0.4, 0.35, 0.8])
>>> fpr, tpr, thresholds = metrics.roc_curve(y, scores, pos_label=2)
>>> fpr
array([0., 0., 0.5, 0.5, 1.])
>>> tpr
array([0., 0.5, 0.5, 1., 1.])
>>> thresholds
array([1.8, 0.8, 0.4, 0.35, 0.1])
```

## Examples using sklearn.metrics.roc\_curve

- Species distribution modeling
- Feature transformations with ensembles of trees
- Receiver Operating Characteristic (ROC) with cross validation

• Receiver Operating Characteristic (ROC)

## sklearn.metrics.zero\_one\_loss

```
sklearn.metrics.zero_one_loss(y_true, y_pred, normalize=True, sample_weight=None)
Zero-one classification loss.
```

If normalize is True, return the fraction of misclassifications (float), else it returns the number of misclassifications (int). The best performance is 0.

Read more in the User Guide.

### **Parameters**

- **y\_true** [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) labels.
- y\_pred [1d array-like, or label indicator array / sparse matrix] Predicted labels, as returned by a classifier.
- **normalize** [bool, optional (default=True)] If False, return the number of misclassifications. Otherwise, return the fraction of misclassifications.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

**loss** [float or int,] If normalize == True, return the fraction of misclassifications (float), else it returns the number of misclassifications (int).

### See also:

```
accuracy_score, hamming_loss, jaccard_score
```

## **Notes**

In multilabel classification, the zero\_one\_loss function corresponds to the subset zero-one loss: for each sample, the entire set of labels must be correctly predicted, otherwise the loss for that sample is equal to one.

## **Examples**

```
>>> from sklearn.metrics import zero_one_loss
>>> y_pred = [1, 2, 3, 4]
>>> y_true = [2, 2, 3, 4]
>>> zero_one_loss(y_true, y_pred)
0.25
>>> zero_one_loss(y_true, y_pred, normalize=False)
1
```

In the multilabel case with binary label indicators:

```
>>> import numpy as np
>>> zero_one_loss(np.array([[0, 1], [1, 1]]), np.ones((2, 2)))
0.5
```

## Examples using sklearn.metrics.zero\_one\_loss

• Discrete versus Real AdaBoost

# 6.24.3 Regression metrics

See the *Regression metrics* section of the user guide for further details.

metrics.explained_variance_score(y_true,	Explained variance regression score function
y_pred)	
metrics.max_error(y_true, y_pred)	max_error metric calculates the maximum residual error.
metrics.mean_absolute_error(y_true, y_pred)	Mean absolute error regression loss
<pre>metrics.mean_squared_error(y_true, y_pred[,</pre>	Mean squared error regression loss
])	
metrics.mean_squared_log_error(y_true,	Mean squared logarithmic error regression loss
y_pred)	
metrics.median_absolute_error(y_true,	Median absolute error regression loss
y_pred)	
<pre>metrics.r2_score(y_true, y_pred[,])</pre>	R^2 (coefficient of determination) regression score func-
	tion.

## sklearn.metrics.explained variance score

sklearn.metrics.explained\_variance\_score (y\_true, y\_pred, sample\_weight=None, multiout-put='uniform\_average')

Explained variance regression score function

Best possible score is 1.0, lower values are worse.

Read more in the User Guide.

### **Parameters**

**y\_true** [array-like of shape = (n\_samples) or (n\_samples, n\_outputs)] Ground truth (correct) target values.

**y pred** [array-like of shape = (n samples) or (n samples, n outputs)] Estimated target values.

**sample\_weight** [array-like of shape = (n\_samples), optional] Sample weights.

**multioutput** [string in ['raw\_values', 'uniform\_average', 'variance\_weighted'] or array-like of shape (n\_outputs)] Defines aggregating of multiple output scores. Array-like value defines weights used to average scores.

'raw\_values': Returns a full set of scores in case of multioutput input.

'uniform\_average': Scores of all outputs are averaged with uniform weight.

'variance\_weighted': Scores of all outputs are averaged, weighted by the variances of each individual output.

## Returns

**score** [float or ndarray of floats] The explained variance or ndarray if 'multioutput' is 'raw\_values'.

## **Notes**

This is not a symmetric function.

# **Examples**

```
>>> from sklearn.metrics import explained_variance_score
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> explained_variance_score(y_true, y_pred)
0.957...
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> explained_variance_score(y_true, y_pred, multioutput='uniform_average')
...
0.983...
```

### sklearn.metrics.max\_error

```
sklearn.metrics.max_error(y_true, y_pred)
```

max\_error metric calculates the maximum residual error.

Read more in the *User Guide*.

### **Parameters**

```
y_true [array-like of shape = (n_samples)] Ground truth (correct) target values.
```

**y\_pred** [array-like of shape = (n\_samples)] Estimated target values.

## Returns

max\_error [float] A positive floating point value (the best value is 0.0).

## **Examples**

```
>>> from sklearn.metrics import max_error
>>> y_true = [3, 2, 7, 1]
>>> y_pred = [4, 2, 7, 1]
>>> max_error(y_true, y_pred)
1
```

## sklearn.metrics.mean\_absolute\_error

```
sklearn.metrics.mean_absolute_error(y_true, y_pred, sample_weight=None, multiout-put='uniform_average')
```

Mean absolute error regression loss

Read more in the *User Guide*.

### **Parameters**

**y\_true** [array-like of shape = (n\_samples) or (n\_samples, n\_outputs)] Ground truth (correct) target values.

 $y_pred$  [array-like of shape = (n\_samples) or (n\_samples, n\_outputs)] Estimated target values.

**sample\_weight** [array-like of shape = (n\_samples), optional] Sample weights.

**multioutput** [string in ['raw\_values', 'uniform\_average']] or array-like of shape (n\_outputs) Defines aggregating of multiple output values. Array-like value defines weights used to average errors.

'raw\_values': Returns a full set of errors in case of multioutput input.

'uniform average': Errors of all outputs are averaged with uniform weight.

### Returns

**loss** [float or ndarray of floats] If multioutput is 'raw\_values', then mean absolute error is returned for each output separately. If multioutput is 'uniform\_average' or an ndarray of weights, then the weighted average of all output errors is returned.

MAE output is non-negative floating point. The best value is 0.0.

# **Examples**

```
>>> from sklearn.metrics import mean_absolute_error
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> mean_absolute_error(y_true, y_pred)
0.5
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> mean_absolute_error(y_true, y_pred)
0.75
>>> mean_absolute_error(y_true, y_pred, multioutput='raw_values')
array([0.5, 1. ])
>>> mean_absolute_error(y_true, y_pred, multioutput=[0.3, 0.7])
...
0.85...
```

## sklearn.metrics.mean\_squared\_error

sklearn.metrics.mean\_squared\_error(y\_true, y\_pred, sample\_weight=None, multioutput='uniform\_average') multiout-

Mean squared error regression loss

Read more in the User Guide.

### **Parameters**

**y\_true** [array-like of shape = (n\_samples) or (n\_samples, n\_outputs)] Ground truth (correct) target values.

y\_pred [array-like of shape = (n\_samples) or (n\_samples, n\_outputs)] Estimated target values.

**sample\_weight** [array-like of shape = (n\_samples), optional] Sample weights.

**multioutput** [string in ['raw\_values', 'uniform\_average']] or array-like of shape (n\_outputs) Defines aggregating of multiple output values. Array-like value defines weights used to average errors.

'raw\_values': Returns a full set of errors in case of multioutput input.

**'uniform\_average':** Errors of all outputs are averaged with uniform weight.

### Returns

**loss** [float or ndarray of floats] A non-negative floating point value (the best value is 0.0), or an array of floating point values, one for each individual target.

## **Examples**

# Examples using sklearn.metrics.mean\_squared\_error

- Model Complexity Influence
- Gradient Boosting regression
- Plot Ridge coefficients as a function of the L2 regularization
- Linear Regression Example
- Robust linear estimator fitting

# sklearn.metrics.mean\_squared\_log\_error

```
sklearn.metrics.mean_squared_log_error(y_true, y_pred, sample_weight=None, multiout-put='uniform_average')
```

Mean squared logarithmic error regression loss

Read more in the *User Guide*.

## **Parameters**

- **y\_true** [array-like of shape = (n\_samples) or (n\_samples, n\_outputs)] Ground truth (correct) target values.
- **y\_pred** [array-like of shape = (n\_samples) or (n\_samples, n\_outputs)] Estimated target values.
- **sample\_weight** [array-like of shape = (n\_samples), optional] Sample weights.
- **multioutput** [string in ['raw\_values', 'uniform\_average'] or array-like of shape = (n\_outputs)] Defines aggregating of multiple output values. Array-like value defines weights used to average errors.

'raw\_values': Returns a full set of errors when the input is of multioutput format.

'uniform\_average': Errors of all outputs are averaged with uniform weight.

### Returns

**loss** [float or ndarray of floats] A non-negative floating point value (the best value is 0.0), or an array of floating point values, one for each individual target.

# **Examples**

```
>>> from sklearn.metrics import mean_squared_log_error
>>> y_true = [3, 5, 2.5, 7]
>>> y_pred = [2.5, 5, 4, 8]
>>> mean_squared_log_error(y_true, y_pred)
0.039...
>>> y_true = [[0.5, 1], [1, 2], [7, 6]]
>>> y_pred = [[0.5, 2], [1, 2.5], [8, 8]]
>>> mean_squared_log_error(y_true, y_pred)
0.044...
>>> mean_squared_log_error(y_true, y_pred, multioutput='raw_values')
...
array([0.00462428, 0.08377444])
>>> mean_squared_log_error(y_true, y_pred, multioutput=[0.3, 0.7])
...
0.060...
```

## sklearn.metrics.median\_absolute\_error

```
sklearn.metrics.median_absolute_error(y_true, y_pred)
```

Median absolute error regression loss

Read more in the *User Guide*.

## **Parameters**

```
y_true [array-like of shape = (n_samples)] Ground truth (correct) target values.
```

 $y_pred$  [array-like of shape =  $(n_samples)$ ] Estimated target values.

### Returns

loss [float] A positive floating point value (the best value is 0.0).

## **Examples**

```
>>> from sklearn.metrics import median_absolute_error
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> median_absolute_error(y_true, y_pred)
0.5
```

## Examples using sklearn.metrics.median\_absolute\_error

• Effect of transforming the targets in regression model

### sklearn.metrics.r2 score

sklearn.metrics.**r2\_score** (*y\_true*, *y\_pred*, *sample\_weight=None*, *multioutput='uniform\_average'*)

R^2 (coefficient of determination) regression score function.

Best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

Read more in the *User Guide*.

### **Parameters**

- **y\_true** [array-like of shape = (n\_samples) or (n\_samples, n\_outputs)] Ground truth (correct) target values.
- **y\_pred** [array-like of shape = (n\_samples) or (n\_samples, n\_outputs)] Estimated target values.
- **sample\_weight** [array-like of shape = (n\_samples), optional] Sample weights.
- **multioutput** [string in ['raw\_values', 'uniform\_average', 'variance\_weighted'] or None or array-like of shape (n\_outputs)] Defines aggregating of multiple output scores. Array-like value defines weights used to average scores. Default is "uniform\_average".
  - 'raw\_values': Returns a full set of scores in case of multioutput input.
  - 'uniform\_average': Scores of all outputs are averaged with uniform weight.
  - 'variance\_weighted': Scores of all outputs are averaged, weighted by the variances of each individual output.

Changed in version 0.19: Default value of multioutput is 'uniform\_average'.

### Returns

z [float or ndarray of floats] The R^2 score or ndarray of scores if 'multioutput' is 'raw\_values'.

## Notes

This is not a symmetric function.

Unlike most other scores, R^2 score may be negative (it need not actually be the square of a quantity R).

This metric is not well-defined for single samples and will return a NaN value if n\_samples is less than two.

### References

[1]

## **Examples**

```
>>> from sklearn.metrics import r2_score
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> r2_score(y_true, y_pred)
0.948...
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> r2_score(y_true, y_pred,
... multioutput='variance_weighted')
```

```
0.938...
>>> y_true = [1, 2, 3]
>>> y_pred = [1, 2, 3]
>>> r2_score(y_true, y_pred)
1.0
>>> y_true = [1, 2, 3]
>>> y_pred = [2, 2, 2]
>>> r2_score(y_true, y_pred)
0.0
>>> y_true = [1, 2, 3]
>>> y_pred = [3, 2, 1]
>>> r2_score(y_true, y_pred)
-3.0
```

# Examples using sklearn.metrics.r2\_score

- Effect of transforming the targets in regression model
- Linear Regression Example
- Lasso and Elastic Net for Sparse Signals

# 6.24.4 Multilabel ranking metrics

See the Multilabel ranking metrics section of the user guide for further details.

<pre>metrics.coverage_error(y_true, y_score[,])</pre>	Coverage error measure
metrics.label_ranking_average_precision_	s Comp(ute) ranking-based average precision
metrics.label_ranking_loss(y_true, y_score)	Compute Ranking loss measure

### sklearn.metrics.coverage\_error

```
sklearn.metrics.coverage_error(y_true, y_score, sample_weight=None)
Coverage error measure
```

Compute how far we need to go through the ranked scores to cover all true labels. The best value is equal to the average number of labels in y\_true per sample.

Ties in y\_scores are broken by giving maximal rank that would have been assigned to all tied values.

Note: Our implementation's score is 1 greater than the one given in Tsoumakas et al., 2010. This extends it to handle the degenerate case in which an instance has 0 true labels.

Read more in the User Guide.

### **Parameters**

- $y_{true}$  [array, shape = [n\_samples, n\_labels]] True binary labels in binary indicator format.
- **y\_score** [array, shape = [n\_samples, n\_labels]] Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by "decision\_function" on some classifiers).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

## Returns

coverage\_error [float]

### References

[1]

## sklearn.metrics.label ranking average precision score

```
sklearn.metrics.label_ranking_average_precision_score(y_true, y_score, sam-ple_weight=None)
```

Compute ranking-based average precision

Label ranking average precision (LRAP) is the average over each ground truth label assigned to each sample, of the ratio of true vs. total labels with lower score.

This metric is used in multilabel ranking problem, where the goal is to give better rank to the labels associated to each sample.

The obtained score is always strictly greater than 0 and the best value is 1.

Read more in the User Guide.

### **Parameters**

- y\_true [array or sparse matrix, shape = [n\_samples, n\_labels]] True binary labels in binary indicator format.
- **y\_score** [array, shape = [n\_samples, n\_labels]] Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by "decision\_function" on some classifiers).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

score [float]

# **Examples**

```
>>> import numpy as np
>>> from sklearn.metrics import label_ranking_average_precision_score
>>> y_true = np.array([[1, 0, 0], [0, 0, 1]])
>>> y_score = np.array([[0.75, 0.5, 1], [1, 0.2, 0.1]])
>>> label_ranking_average_precision_score(y_true, y_score)
0.416...
```

# sklearn.metrics.label\_ranking\_loss

```
sklearn.metrics.label_ranking_loss(y_true, y_score, sample_weight=None)
Compute Ranking loss measure
```

Compute the average number of label pairs that are incorrectly ordered given y\_score weighted by the size of the label set and the number of labels not in the label set.

This is similar to the error set size, but weighted by the number of relevant and irrelevant labels. The best performance is achieved with a ranking loss of zero.

Read more in the User Guide.

New in version 0.17: A function *label\_ranking\_loss* 

### **Parameters**

- **y\_true** [array or sparse matrix, shape = [n\_samples, n\_labels]] True binary labels in binary indicator format.
- **y\_score** [array, shape = [n\_samples, n\_labels]] Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by "decision\_function" on some classifiers).

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

loss [float]

### References

[1]

# 6.24.5 Clustering metrics

See the *Clustering performance evaluation* section of the user guide for further details. The *sklearn.metrics*. *cluster* submodule contains evaluation metrics for cluster analysis results. There are two forms of evaluation:

- supervised, which uses a ground truth class values for each sample.
- unsupervised, which does not and measures the 'quality' of the model itself.

<pre>metrics.adjusted_mutual_info_score([,</pre>	Adjusted Mutual Information between two clusterings.
])	
<pre>metrics.adjusted_rand_score(labels_true,)</pre>	Rand index adjusted for chance.
metrics.calinski_harabasz_score(X, labels)	Compute the Calinski and Harabasz score.
metrics.davies_bouldin_score(X, labels)	Computes the Davies-Bouldin score.
metrics.completeness_score(labels_true,)	Completeness metric of a cluster labeling given a ground
	truth.
metrics.cluster.contingency_matrix([,	Build a contingency matrix describing the relationship be-
])	tween labels.
metrics.fowlkes_mallows_score(labels_true,	Measure the similarity of two clusterings of a set of points.
)	
metrics.homogeneity_completeness_v_measu	recompute the homogeneity and completeness and V-
	Measure scores at once.
<pre>metrics.homogeneity_score(labels_true,)</pre>	Homogeneity metric of a cluster labeling given a ground
	truth.
metrics.mutual_info_score(labels_true,)	Mutual Information between two clusterings.
metrics.normalized_mutual_info_score([,	Normalized Mutual Information between two clusterings.
])	
$metrics.silhouette\_score(X, labels[,])$	Compute the mean Silhouette Coefficient of all samples.
<pre>metrics.silhouette_samples(X, labels[, metric])</pre>	Compute the Silhouette Coefficient for each sample.
metrics.v_measure_score(labels_true, la-	V-measure cluster labeling given a ground truth.
bels_pred)	

### sklearn.metrics.adjusted mutual info score

```
sklearn.metrics.adjusted_mutual_info_score(labels_true, labels_pred, average_method='warn')
```

Adjusted Mutual Information between two clusterings.

Adjusted Mutual Information (AMI) is an adjustment of the Mutual Information (MI) score to account for chance. It accounts for the fact that the MI is generally higher for two clusterings with a larger number of clusters, regardless of whether there is actually more information shared. For two clusterings U and V, the AMI is given as:

```
AMI(U, V) = [MI(U, V) - E(MI(U, V))] / [avg(H(U), H(V)) - E(MI(U, V))]
```

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won't change the score value in any way.

This metric is furthermore symmetric: switching label\_true with label\_pred will return the same score value. This can be useful to measure the agreement of two independent label assignments strategies on the same dataset when the real ground truth is not known.

Be mindful that this function is an order of magnitude slower than other metrics, such as the Adjusted Rand Index.

Read more in the User Guide.

### **Parameters**

**labels\_true** [int array, shape = [n\_samples]] A clustering of the data into disjoint subsets.

**labels\_pred** [array, shape = [n\_samples]] A clustering of the data into disjoint subsets.

**average\_method** [string, optional (default: 'warn')] How to compute the normalizer in the denominator. Possible options are 'min', 'geometric', 'arithmetic', and 'max'. If 'warn', 'max' will be used. The default will change to 'arithmetic' in version 0.22.

New in version 0.20.

## Returns

**ami: float** (**upperlimited by 1.0**) The AMI returns a value of 1 when the two partitions are identical (ie perfectly matched). Random partitions (independent labellings) have an expected AMI around 0 on average hence can be negative.

## See also:

```
adjusted_rand_score Adjusted Rand Index
mutual_info_score Mutual Information (not adjusted for chance)
```

## References

[1], [2]

## **Examples**

Perfect labelings are both homogeneous and complete, hence have score 1.0:

```
>>> from sklearn.metrics.cluster import adjusted_mutual_info_score
>>> adjusted_mutual_info_score([0, 0, 1, 1], [0, 0, 1, 1])
...
1.0
>>> adjusted_mutual_info_score([0, 0, 1, 1], [1, 1, 0, 0])
...
1.0
```

If classes members are completely split across different clusters, the assignment is totally in-complete, hence the AMI is null:

```
>>> adjusted_mutual_info_score([0, 0, 0, 0], [0, 1, 2, 3])
...
0.0
```

## Examples using sklearn.metrics.adjusted mutual info score

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- Adjustment for chance in clustering performance evaluation
- A demo of K-Means clustering on the handwritten digits data

# sklearn.metrics.adjusted\_rand\_score

```
sklearn.metrics.adjusted_rand_score(labels_true, labels_pred)
```

Rand index adjusted for chance.

The Rand Index computes a similarity measure between two clusterings by considering all pairs of samples and counting pairs that are assigned in the same or different clusters in the predicted and true clusterings.

The raw RI score is then "adjusted for chance" into the ARI score using the following scheme:

```
ARI = (RI - Expected_RI) / (max(RI) - Expected_RI)
```

The adjusted Rand index is thus ensured to have a value close to 0.0 for random labeling independently of the number of clusters and samples and exactly 1.0 when the clusterings are identical (up to a permutation).

ARI is a symmetric measure:

```
adjusted_rand_score(a, b) == adjusted_rand_score(b, a)
```

Read more in the *User Guide*.

### **Parameters**

**labels\_true** [int array, shape = [n\_samples]] Ground truth class labels to be used as a reference **labels\_pred** [array, shape = [n\_samples]] Cluster labels to evaluate

## Returns

**ari** [float] Similarity score between -1.0 and 1.0. Random labelings have an ARI close to 0.0. 1.0 stands for perfect match.

See also:

adjusted\_mutual\_info\_score Adjusted Mutual Information

### References

[Hubert1985], [wk]

## **Examples**

Perfectly matching labelings have a score of 1 even

```
>>> from sklearn.metrics.cluster import adjusted_rand_score
>>> adjusted_rand_score([0, 0, 1, 1], [0, 0, 1, 1])
1.0
>>> adjusted_rand_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

Labelings that assign all classes members to the same clusters are complete be not always pure, hence penalized:

```
>>> adjusted_rand_score([0, 0, 1, 2], [0, 0, 1, 1])
0.57...
```

ARI is symmetric, so labelings that have pure clusters with members coming from the same classes but unnecessary splits are penalized:

```
>>> adjusted_rand_score([0, 0, 1, 1], [0, 0, 1, 2])
0.57...
```

If classes members are completely split across different clusters, the assignment is totally incomplete, hence the ARI is very low:

```
>>> adjusted_rand_score([0, 0, 0, 0], [0, 1, 2, 3])
0.0
```

# Examples using sklearn.metrics.adjusted\_rand\_score

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- Adjustment for chance in clustering performance evaluation
- A demo of K-Means clustering on the handwritten digits data
- Clustering text documents using k-means

### sklearn.metrics.calinski harabasz score

```
sklearn.metrics.calinski_harabasz_score(X, labels)
```

Compute the Calinski and Harabasz score.

It is also known as the Variance Ratio Criterion.

The score is defined as ratio between the within-cluster dispersion and the between-cluster dispersion.

Read more in the *User Guide*.

### **Parameters**

X [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

labels [array-like, shape (n\_samples,)] Predicted labels for each sample.

### Returns

score [float] The resulting Calinski-Harabasz score.

## References

[1]

## sklearn.metrics.davies bouldin score

```
sklearn.metrics.davies_bouldin_score(X, labels)
```

Computes the Davies-Bouldin score.

The score is defined as the average similarity measure of each cluster with its most similar cluster, where similarity is the ratio of within-cluster distances to between-cluster distances. Thus, clusters which are farther apart and less dispersed will result in a better score.

The minimum score is zero, with lower values indicating better clustering.

Read more in the User Guide.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

labels [array-like, shape (n\_samples,)] Predicted labels for each sample.

## Returns

**score:** float The resulting Davies-Bouldin score.

# References

[1]

# sklearn.metrics.completeness\_score

```
sklearn.metrics.completeness score (labels true, labels pred)
```

Completeness metric of a cluster labeling given a ground truth.

A clustering result satisfies completeness if all the data points that are members of a given class are elements of the same cluster.

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won't change the score value in any way.

This metric is not symmetric: switching label\_true with label\_pred will return the homogeneity\_score which will be different in general.

Read more in the User Guide.

### **Parameters**

**labels\_true** [int array, shape = [n\_samples]] ground truth class labels to be used as a reference **labels\_pred** [array, shape = [n\_samples]] cluster labels to evaluate

### Returns

**completeness** [float] score between 0.0 and 1.0. 1.0 stands for perfectly complete labeling

### See also:

```
homogeneity_score
v_measure_score
```

## References

[1]

# **Examples**

Perfect labelings are complete:

```
>>> from sklearn.metrics.cluster import completeness_score
>>> completeness_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

Non-perfect labelings that assign all classes members to the same clusters are still complete:

```
>>> print(completeness_score([0, 0, 1, 1], [0, 0, 0, 0]))
1.0
>>> print(completeness_score([0, 1, 2, 3], [0, 0, 1, 1]))
0.999...
```

If classes members are split across different clusters, the assignment cannot be complete:

```
>>> print(completeness_score([0, 0, 1, 1], [0, 1, 0, 1]))
0.0
>>> print(completeness_score([0, 0, 0, 0], [0, 1, 2, 3]))
0.0
```

## Examples using sklearn.metrics.completeness\_score

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- A demo of K-Means clustering on the handwritten digits data
- Clustering text documents using k-means

## sklearn.metrics.cluster.contingency\_matrix

sklearn.metrics.cluster.contingency\_matrix(labels\_true, labels\_pred, eps=None, sparse=False)

Build a contingency matrix describing the relationship between labels.

### **Parameters**

labels\_true [int array, shape = [n\_samples]] Ground truth class labels to be used as a reference

**labels\_pred** [array, shape = [n\_samples]] Cluster labels to evaluate

**eps** [None or float, optional.] If a float, that value is added to all values in the contingency matrix. This helps to stop NaN propagation. If None, nothing is adjusted.

**sparse** [boolean, optional.] If True, return a sparse CSR continency matrix. If eps is not None, and sparse is True, will throw ValueError.

New in version 0.18.

### Returns

**contingency** [{array-like, sparse}, shape=[n\_classes\_true, n\_classes\_pred]] Matrix C such that  $C_{i,j}$  is the number of samples in true class i and in predicted class j. If eps is None, the dtype of this array will be integer. If eps is given, the dtype will be float. Will be a scipy.sparse.csr\_matrix if sparse=True.

## sklearn.metrics.fowlkes\_mallows\_score

sklearn.metrics.fowlkes\_mallows\_score(labels\_true, labels\_pred, sparse=False)

Measure the similarity of two clusterings of a set of points.

The Fowlkes-Mallows index (FMI) is defined as the geometric mean between of the precision and recall:

```
FMI = TP / sqrt((TP + FP) * (TP + FN))
```

Where TP is the number of **True Positive** (i.e. the number of pair of points that belongs in the same clusters in both labels\_true and labels\_pred), FP is the number of **False Positive** (i.e. the number of pair of points that belongs in the same clusters in labels\_true and not in labels\_pred) and FN is the number of **False Negative** (i.e the number of pair of points that belongs in the same clusters in labels\_pred and not in labels\_True).

The score ranges from 0 to 1. A high value indicates a good similarity between two clusters.

Read more in the User Guide.

### **Parameters**

labels\_true [int array, shape = (n\_samples,)] A clustering of the data into disjoint subsets.

**labels\_pred** [array, shape = (n\_samples, )] A clustering of the data into disjoint subsets.

**sparse** [bool] Compute contingency matrix internally with sparse matrix.

### Returns

**score** [float] The resulting Fowlkes-Mallows score.

### References

[1],[2]

## **Examples**

Perfect labelings are both homogeneous and complete, hence have score 1.0:

```
>>> from sklearn.metrics.cluster import fowlkes_mallows_score
>>> fowlkes_mallows_score([0, 0, 1, 1], [0, 0, 1, 1])
1.0
>>> fowlkes_mallows_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

If classes members are completely split across different clusters, the assignment is totally random, hence the FMI is null:

```
>>> fowlkes_mallows_score([0, 0, 0, 0], [0, 1, 2, 3])
0.0
```

## sklearn.metrics.homogeneity\_completeness\_v\_measure

```
sklearn.metrics.homogeneity_completeness_v_measure(labels_true, labels_pred, beta=1.0)
```

Compute the homogeneity and completeness and V-Measure scores at once.

Those metrics are based on normalized conditional entropy measures of the clustering labeling to evaluate given the knowledge of a Ground Truth class labels of the same samples.

A clustering result satisfies homogeneity if all of its clusters contain only data points which are members of a single class.

A clustering result satisfies completeness if all the data points that are members of a given class are elements of the same cluster.

Both scores have positive values between 0.0 and 1.0, larger values being desirable.

Those 3 metrics are independent of the absolute values of the labels: a permutation of the class or cluster label values won't change the score values in any way.

V-Measure is furthermore symmetric: swapping labels\_true and label\_pred will give the same score. This does not hold for homogeneity and completeness. V-Measure is identical to normalized\_mutual\_info\_score with the arithmetic averaging method.

Read more in the User Guide.

### **Parameters**

```
labels_true [int array, shape = [n_samples]] ground truth class labels to be used as a reference labels_pred [array, shape = [n_samples]] cluster labels to evaluate
```

beta [float] Ratio of weight attributed to homogeneity vs completeness. If beta is greater than 1, completeness is weighted more strongly in the calculation. If beta is less than 1, homogeneity is weighted more strongly.

### Returns

**homogeneity** [float] score between 0.0 and 1.0. 1.0 stands for perfectly homogeneous labeling **completeness** [float] score between 0.0 and 1.0. 1.0 stands for perfectly complete labeling **v\_measure** [float] harmonic mean of the first two

See also:

```
homogeneity_score
completeness_score
v_measure_score
```

## sklearn.metrics.homogeneity\_score

```
sklearn.metrics.homogeneity_score(labels_true, labels_pred)
```

Homogeneity metric of a cluster labeling given a ground truth.

A clustering result satisfies homogeneity if all of its clusters contain only data points which are members of a single class.

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won't change the score value in any way.

This metric is not symmetric: switching label\_true with label\_pred will return the completeness\_score which will be different in general.

Read more in the User Guide.

## **Parameters**

**labels\_true** [int array, shape = [n\_samples]] ground truth class labels to be used as a reference **labels\_pred** [array, shape = [n\_samples]] cluster labels to evaluate

### Returns

**homogeneity** [float] score between 0.0 and 1.0. 1.0 stands for perfectly homogeneous labeling

## See also:

```
completeness_score
v_measure_score
```

### References

[1]

## **Examples**

Perfect labelings are homogeneous:

```
>>> from sklearn.metrics.cluster import homogeneity_score
>>> homogeneity_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

Non-perfect labelings that further split classes into more clusters can be perfectly homogeneous:

```
>>> print("%.6f" % homogeneity_score([0, 0, 1, 1], [0, 0, 1, 2]))
...
1.000000
>>> print("%.6f" % homogeneity_score([0, 0, 1, 1], [0, 1, 2, 3]))
...
1.000000
```

Clusters that include samples from different classes do not make for an homogeneous labeling:

```
>>> print("%.6f" % homogeneity_score([0, 0, 1, 1], [0, 1, 0, 1]))
...
0.0...
>>> print("%.6f" % homogeneity_score([0, 0, 1, 1], [0, 0, 0, 0]))
...
0.0...
```

# Examples using sklearn.metrics.homogeneity\_score

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- A demo of K-Means clustering on the handwritten digits data
- Clustering text documents using k-means

## sklearn.metrics.mutual\_info\_score

sklearn.metrics.mutual\_info\_score (labels\_true, labels\_pred, contingency=None)
Mutual Information between two clusterings.

The Mutual Information is a measure of the similarity between two labels of the same data. Where  $|U_i|$  is the number of the samples in cluster  $U_i$  and  $|V_j|$  is the number of the samples in cluster  $V_j$ , the Mutual Information between clusterings U and V is given as:

$$MI(U, V) = \sum_{i=1}^{|U|} \sum_{i=1}^{|V|} \frac{|U_i \cap V_j|}{N} \log \frac{N|U_i \cap V_j|}{|U_i||V_j|}$$

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won't change the score value in any way.

This metric is furthermore symmetric: switching label\_true with label\_pred will return the same score value. This can be useful to measure the agreement of two independent label assignments strategies on the same dataset when the real ground truth is not known.

Read more in the *User Guide*.

### **Parameters**

**labels\_true** [int array, shape = [n\_samples]] A clustering of the data into disjoint subsets.

**labels\_pred** [array, shape = [n\_samples]] A clustering of the data into disjoint subsets.

contingency [{None, array, sparse matrix}, shape = [n\_classes\_true, n\_classes\_pred]] A contingency matrix given by the contingency\_matrix function. If value is None, it will
be computed, otherwise the given value is used, with labels\_true and labels\_pred
ignored.

## Returns

mi [float] Mutual information, a non-negative value

### See also:

adjusted\_mutual\_info\_score Adjusted against chance Mutual Information
normalized\_mutual\_info\_score Normalized Mutual Information

### Examples using sklearn.metrics.mutual\_info\_score

• Adjustment for chance in clustering performance evaluation

### sklearn.metrics.normalized mutual info score

```
sklearn.metrics.normalized_mutual_info_score(labels_true, labels_pred, average_method='warn')
```

Normalized Mutual Information between two clusterings.

Normalized Mutual Information (NMI) is a normalization of the Mutual Information (MI) score to scale the results between 0 (no mutual information) and 1 (perfect correlation). In this function, mutual information is normalized by some generalized mean of H(labels\_true) and H(labels\_pred)), defined by the average method.

This measure is not adjusted for chance. Therefore adjusted\_mutual\_info\_score might be preferred.

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won't change the score value in any way.

This metric is furthermore symmetric: switching label\_true with label\_pred will return the same score value. This can be useful to measure the agreement of two independent label assignments strategies on the same dataset when the real ground truth is not known.

Read more in the User Guide.

### **Parameters**

```
labels_true [int array, shape = [n_samples]] A clustering of the data into disjoint subsets.
```

**labels\_pred** [array, shape = [n\_samples]] A clustering of the data into disjoint subsets.

**average\_method** [string, optional (default: 'warn')] How to compute the normalizer in the denominator. Possible options are 'min', 'geometric', 'arithmetic', and 'max'. If 'warn', 'geometric' will be used. The default will change to 'arithmetic' in version 0.22.

New in version 0.20.

#### Returns

**nmi** [float] score between 0.0 and 1.0. 1.0 stands for perfectly complete labeling

## See also:

```
v_measure_score V-Measure (NMI with arithmetic mean option.)
adjusted_rand_score Adjusted Rand Index
adjusted_mutual_info_score Adjusted Mutual Information (adjusted against chance)
```

### **Examples**

Perfect labelings are both homogeneous and complete, hence have score 1.0:

```
>>> from sklearn.metrics.cluster import normalized_mutual_info_score
>>> normalized_mutual_info_score([0, 0, 1, 1], [0, 0, 1, 1])
...
1.0
>>> normalized_mutual_info_score([0, 0, 1, 1], [1, 1, 0, 0])
```

```
1.0
```

If classes members are completely split across different clusters, the assignment is totally in-complete, hence the NMI is null:

```
>>> normalized_mutual_info_score([0, 0, 0, 0], [0, 1, 2, 3])
...
0.0
```

## sklearn.metrics.silhouette score

```
sklearn.metrics.silhouette_score(X, labels, metric='euclidean', sample_size=None, ran-
dom state=None, **kwds)
```

Compute the mean Silhouette Coefficient of all samples.

The Silhouette Coefficient is calculated using the mean intra-cluster distance (a) and the mean nearest-cluster distance (b) for each sample. The Silhouette Coefficient for a sample is  $(b - a) / \max(a, b)$ . To clarify, b is the distance between a sample and the nearest cluster that the sample is not a part of. Note that Silhouette Coefficient is only defined if number of labels is  $2 <= n_{a}$  samples - 1.

This function returns the mean Silhouette Coefficient over all samples. To obtain the values for each sample, use <code>silhouette\_samples</code>.

The best value is 1 and the worst value is -1. Values near 0 indicate overlapping clusters. Negative values generally indicate that a sample has been assigned to the wrong cluster, as a different cluster is more similar.

Read more in the *User Guide*.

### **Parameters**

X [array [n\_samples\_a, n\_samples\_a] if metric == "precomputed", or, [n\_samples\_a, n\_features] otherwise] Array of pairwise distances between samples, or a feature array.

**labels** [array, shape = [n\_samples]] Predicted labels for each sample.

metric [string, or callable] The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by metrics.pairwise.pairwise\_distances. If X is the distance array itself, use metric="precomputed".

**sample\_size** [int or None] The size of the sample to use when computing the Silhouette Coefficient on a random subset of the data. If sample\_size is None, no sampling is used.

random\_state [int, RandomState instance or None, optional (default=None)] The generator
used to randomly select a subset of samples. If int, random\_state is the seed used by the
random number generator; If RandomState instance, random\_state is the random number
generator; If None, the random number generator is the RandomState instance used by np.
random. Used when sample\_size is not None.

\*\*kwds [optional keyword parameters] Any further parameters are passed directly to the distance function. If using a scipy.spatial.distance metric, the parameters are still metric dependent. See the scipy docs for usage examples.

### Returns

silhouette [float] Mean Silhouette Coefficient for all samples.

#### References

[1], [2]

### Examples using sklearn.metrics.silhouette\_score

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- A demo of K-Means clustering on the handwritten digits data
- Selecting the number of clusters with silhouette analysis on KMeans clustering
- Clustering text documents using k-means

### sklearn.metrics.silhouette samples

sklearn.metrics.silhouette\_samples (X, labels, metric='euclidean', \*\*kwds)
Compute the Silhouette Coefficient for each sample.

The Silhouette Coefficient is a measure of how well samples are clustered with samples that are similar to themselves. Clustering models with a high Silhouette Coefficient are said to be dense, where samples in the same cluster are similar to each other, and well separated, where samples in different clusters are not very similar to each other.

The Silhouette Coefficient is calculated using the mean intra-cluster distance (a) and the mean nearest-cluster distance (b) for each sample. The Silhouette Coefficient for a sample is  $(b - a) / \max(a, b)$ . Note that Silhouette Coefficient is only defined if number of labels is 2 <= n\_labels <= n\_samples - 1.

This function returns the Silhouette Coefficient for each sample.

The best value is 1 and the worst value is -1. Values near 0 indicate overlapping clusters.

Read more in the User Guide.

### **Parameters**

**X** [array [n\_samples\_a, n\_samples\_a] if metric == "precomputed", or, [n\_samples\_a, n\_features] otherwise] Array of pairwise distances between samples, or a feature array.

**labels** [array, shape = [n\_samples]] label values for each sample

metric [string, or callable] The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by sklearn. metrics.pairwise.pairwise\_distances. If X is the distance array itself, use "precomputed" as the metric.

\*\*\*kwds\* [optional keyword parameters] Any further parameters are passed directly to the distance function. If using a scipy.spatial.distance metric, the parameters are still metric dependent. See the scipy docs for usage examples.

#### Returns

**silhouette** [array, shape = [n\_samples]] Silhouette Coefficient for each samples.

#### References

[1], [2]

### Examples using sklearn.metrics.silhouette\_samples

Selecting the number of clusters with silhouette analysis on KMeans clustering

### sklearn.metrics.v\_measure\_score

```
sklearn.metrics.v_measure_score (labels_true, labels_pred, beta=1.0)
```

V-measure cluster labeling given a ground truth.

This score is identical to normalized\_mutual\_info\_score with the 'arithmetic' option for averaging.

The V-measure is the harmonic mean between homogeneity and completeness:

```
v = (1 + beta) * homogeneity * completeness
/ (beta * homogeneity + completeness)
```

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won't change the score value in any way.

This metric is furthermore symmetric: switching label\_true with label\_pred will return the same score value. This can be useful to measure the agreement of two independent label assignments strategies on the same dataset when the real ground truth is not known.

Read more in the *User Guide*.

#### **Parameters**

labels\_true [int array, shape = [n\_samples]] ground truth class labels to be used as a reference

**labels\_pred** [array, shape = [n\_samples]] cluster labels to evaluate

**beta** [float] Ratio of weight attributed to homogeneity vs completeness. If beta is greater than 1, completeness is weighted more strongly in the calculation. If beta is less than 1, homogeneity is weighted more strongly.

### Returns

v\_measure [float] score between 0.0 and 1.0. 1.0 stands for perfectly complete labeling

#### See also:

```
homogeneity_score
completeness_score
normalized_mutual_info_score
```

## References

[1]

### **Examples**

Perfect labelings are both homogeneous and complete, hence have score 1.0:

```
>>> from sklearn.metrics.cluster import v_measure_score

>>> v_measure_score([0, 0, 1, 1], [0, 0, 1, 1])

1.0

>>> v_measure_score([0, 0, 1, 1], [1, 1, 0, 0])

1.0
```

Labelings that assign all classes members to the same clusters are complete be not homogeneous, hence penalized:

```
>>> print("%.6f" % v_measure_score([0, 0, 1, 2], [0, 0, 1, 1]))
...
0.8...
>>> print("%.6f" % v_measure_score([0, 1, 2, 3], [0, 0, 1, 1]))
...
0.66...
```

Labelings that have pure clusters with members coming from the same classes are homogeneous but unnecessary splits harms completeness and thus penalize V-measure as well:

```
>>> print("%.6f" % v_measure_score([0, 0, 1, 1], [0, 0, 1, 2]))
...
0.8...
>>> print("%.6f" % v_measure_score([0, 0, 1, 1], [0, 1, 2, 3]))
...
0.66...
```

If classes members are completely split across different clusters, the assignment is totally incomplete, hence the V-Measure is null:

```
>>> print("%.6f" % v_measure_score([0, 0, 0, 0], [0, 1, 2, 3]))
...
0.0...
```

Clusters that include samples from totally different classes totally destroy the homogeneity of the labeling, hence:

```
>>> print("%.6f" % v_measure_score([0, 0, 1, 1], [0, 0, 0, 0]))
...
0.0...
```

#### Examples using sklearn.metrics.v\_measure\_score

- Biclustering documents with the Spectral Co-clustering algorithm
- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- Adjustment for chance in clustering performance evaluation
- A demo of K-Means clustering on the handwritten digits data
- Clustering text documents using k-means

# 6.24.6 Biclustering metrics

See the Biclustering evaluation section of the user guide for further details.

metrics.consensus_score(a, b[, similarity])	The similarity of two sets of biclusters.
---	---

### sklearn.metrics.consensus\_score

sklearn.metrics.consensus\_score(a, b, similarity='jaccard')

The similarity of two sets of biclusters.

Similarity between individual biclusters is computed. Then the best matching between sets is found using the Hungarian algorithm. The final score is the sum of similarities divided by the size of the larger set.

Read more in the *User Guide*.

#### **Parameters**

- a [(rows, columns)] Tuple of row and column indicators for a set of biclusters.
- **b** [(rows, columns)] Another set of biclusters like a.

**similarity** [string or function, optional, default: "jaccard"] May be the string "jaccard" to use the Jaccard coefficient, or any function that takes four arguments, each of which is a 1d indicator vector: (a\_rows, a\_columns, b\_rows, b\_columns).

#### References

• Hochreiter, Bodenhofer, et. al., 2010. FABIA: factor analysis for bicluster acquisition.

# $\textbf{Examples using } \textbf{sklearn.metrics.consensus\_score}$

- A demo of the Spectral Co-Clustering algorithm
- A demo of the Spectral Biclustering algorithm

## 6.24.7 Pairwise metrics

See the *Pairwise metrics*, *Affinities and Kernels* section of the user guide for further details.

metrics.pairwise.additive_chi2_kernel(X[,	Computes the additive chi-squared kernel between obser-
Y])	vations in X and Y
<pre>metrics.pairwise.chi2_kernel(X[, Y, gamma])</pre>	Computes the exponential chi-squared kernel X and Y.
metrics.pairwise.cosine_similarity(X[, Y,	Compute cosine similarity between samples in X and Y.
])	
metrics.pairwise.cosine_distances(X[, Y])	Compute cosine distance between samples in X and Y.
<pre>metrics.pairwise.distance_metrics()</pre>	Valid metrics for pairwise_distances.
metrics.pairwise.euclidean_distances(X[,	Considering the rows of X (and Y=X) as vectors, compute
$Y, \dots])$	the distance matrix between each pair of vectors.
metrics.pairwise.haversine_distances(X[,	Compute the Haversine distance between samples in X and
Y])	Y
metrics.pairwise.kernel_metrics()	Valid metrics for pairwise_kernels
metrics.pairwise.laplacian_kernel(X[, Y,	Compute the laplacian kernel between X and Y.
gamma])	
$metrics.pairwise.linear\_kernel(X[,Y,])$	Compute the linear kernel between X and Y.
	Continued on next nage

Continued on next page

## Table 6.184 – continued from previous page

metrics.pairwise.manhattan_distances(X[,	Compute the L1 distances between the vectors in X and Y.
Y,])	1
metrics.pairwise.pairwise_kernels(X[, Y,	Compute the kernel between arrays X and optional array Y.
])	
metrics.pairwise.polynomial_kernel(X[, Y,	Compute the polynomial kernel between X and Y:
])	
<pre>metrics.pairwise.rbf_kernel(X[, Y, gamma])</pre>	Compute the rbf (gaussian) kernel between X and Y:
$metrics.pairwise.sigmoid\_kernel(X[, Y,])$	Compute the sigmoid kernel between X and Y:
metrics.pairwise.paired_euclidean_distan	c€o(Xputes the paired euclidean distances between X and Y
Y)	
metrics.pairwise.paired_manhattan_distan	c € o(X) pute the L1 distances between the vectors in X and Y.
Y)	
metrics.pairwise.paired_cosine_distances	(XComputes the paired cosine distances between X and Y
	(
Y)	(-3,F
Y) metrics.pairwise.paired_distances(X, Y[,	Computes the paired distances between X and Y.
metrics.pairwise.paired_distances(X, Y[,	
<pre>metrics.pairwise.paired_distances(X, Y[, metric])</pre>	Computes the paired distances between X and Y.
<pre>metrics.pairwise.paired_distances(X, Y[, metric])</pre>	Computes the paired distances between X and Y.  Compute the distance matrix from a vector array X and op-
<pre>metrics.pairwise.paired_distances(X, Y[, metric]) metrics.pairwise_distances(X[, Y, metric,])  metrics.pairwise_distances_argmin(X, Y[,])</pre>	Computes the paired distances between X and Y.  Compute the distance matrix from a vector array X and optional Y.
<pre>metrics.pairwise.paired_distances(X, Y[, metric]) metrics.pairwise_distances(X[, Y, metric,]) metrics.pairwise_distances_argmin(X, Y[,</pre>	Computes the paired distances between X and Y.  Compute the distance matrix from a vector array X and optional Y.  Compute minimum distances between one point and a set
<pre>metrics.pairwise.paired_distances(X, Y[, metric]) metrics.pairwise_distances(X[, Y, metric,])  metrics.pairwise_distances_argmin(X, Y[,])</pre>	Computes the paired distances between X and Y.  Compute the distance matrix from a vector array X and optional Y.  Compute minimum distances between one point and a set of points.
<pre>metrics.pairwise.paired_distances(X, Y[, metric])  metrics.pairwise_distances(X[, Y, metric,])  metrics.pairwise_distances_argmin(X, Y[,])  metrics.pairwise_distances_argmin_min(X,</pre>	Computes the paired distances between X and Y.  Compute the distance matrix from a vector array X and optional Y.  Compute minimum distances between one point and a set of points.  Compute minimum distances between one point and a set

## sklearn.metrics.pairwise.additive\_chi2\_kernel

```
sklearn.metrics.pairwise.additive_chi2_kernel(X, Y=None)
```

Computes the additive chi-squared kernel between observations in X and Y

The chi-squared kernel is computed between each pair of rows in X and Y. X and Y have to be non-negative. This kernel is most commonly applied to histograms.

The chi-squared kernel is given by:

```
k(x, y) = -Sum [(x - y)^2 / (x + y)]
```

It can be interpreted as a weighted difference per entry.

Read more in the *User Guide*.

#### **Parameters**

**X** [array-like of shape (n\_samples\_X, n\_features)]

**Y** [array of shape (n\_samples\_Y, n\_features)]

### Returns

**kernel\_matrix** [array of shape (n\_samples\_X, n\_samples\_Y)]

## See also:

chi2\_kernel The exponentiated version of the kernel, which is usually preferable.

**sklearn.kernel\_approximation.AdditiveChi2Sampler** A Fourier approximation to this kernel.

#### **Notes**

As the negative of a distance, this kernel is only conditionally positive definite.

#### References

• Zhang, J. and Marszalek, M. and Lazebnik, S. and Schmid, C. Local features and kernels for classification of texture and object categories: A comprehensive study International Journal of Computer Vision 2007 <a href="https://research.microsoft.com/en-us/um/people/manik/projects/trade-off/papers/ZhangIJCV06.pdf">https://research.microsoft.com/en-us/um/people/manik/projects/trade-off/papers/ZhangIJCV06.pdf</a>

## sklearn.metrics.pairwise.chi2\_kernel

```
sklearn.metrics.pairwise.chi2\_kernel(X, Y=None, gamma=1.0)
```

Computes the exponential chi-squared kernel X and Y.

The chi-squared kernel is computed between each pair of rows in X and Y. X and Y have to be non-negative. This kernel is most commonly applied to histograms.

The chi-squared kernel is given by:

```
k(x, y) = exp(-gamma Sum [(x - y)^2 / (x + y)])
```

It can be interpreted as a weighted difference per entry.

Read more in the User Guide.

### **Parameters**

```
X [array-like of shape (n_samples_X, n_features)]
```

Y [array of shape (n\_samples\_Y, n\_features)]

**gamma** [float, default=1.] Scaling parameter of the chi2 kernel.

### Returns

**kernel\_matrix** [array of shape (n\_samples\_X, n\_samples\_Y)]

#### See also:

```
additive_chi2_kernel The additive version of this kernel
```

sklearn.kernel\_approximation.AdditiveChi2Sampler A Fourier approximation to the additive version of this kernel.

#### References

Zhang, J. and Marszalek, M. and Lazebnik, S. and Schmid, C. Local features and kernels for classification
of texture and object categories: A comprehensive study International Journal of Computer Vision 2007
https://research.microsoft.com/en-us/um/people/manik/projects/trade-off/papers/ZhangIJCV06.pdf

#### sklearn.metrics.pairwise.cosine similarity

```
sklearn.metrics.pairwise.cosine_similarity (X, Y=None, dense\_output=True) Compute cosine similarity between samples in X and Y.
```

Cosine similarity, or the cosine kernel, computes similarity as the normalized dot product of X and Y:

```
K(X, Y) = \langle X, Y \rangle / (||X|| * ||Y||)
```

On L2-normalized data, this function is equivalent to linear\_kernel.

Read more in the User Guide.

#### **Parameters**

- **X** [ndarray or sparse array, shape: (n samples X, n features)] Input data.
- Y [ndarray or sparse array, shape: (n\_samples\_Y, n\_features)] Input data. If None, the output will be the pairwise similarities between all samples in X.

**dense\_output** [boolean (optional), default True] Whether to return dense output even when the input is sparse. If False, the output is sparse if both input arrays are sparse.

New in version 0.17: parameter dense\_output for dense output.

### Returns

**kernel matrix** [array] An array with shape (n\_samples\_X, n\_samples\_Y).

## sklearn.metrics.pairwise.cosine\_distances

```
sklearn.metrics.pairwise.cosine_distances(X, Y=None)
```

Compute cosine distance between samples in X and Y.

Cosine distance is defined as 1.0 minus the cosine similarity.

Read more in the User Guide.

#### **Parameters**

- **X** [array like, sparse matrix] with shape (n samples X, n features).
- Y [array\_like, sparse matrix (optional)] with shape (n\_samples\_Y, n\_features).

### Returns

**distance matrix** [array] An array with shape (n\_samples\_X, n\_samples\_Y).

## See also:

```
sklearn.metrics.pairwise.cosine_similarity
scipy.spatial.distance.cosine dense matrices only
```

## sklearn.metrics.pairwise.distance\_metrics

```
sklearn.metrics.pairwise.distance_metrics()
```

Valid metrics for pairwise\_distances.

This function simply returns the valid pairwise distance metrics. It exists to allow for a description of the mapping for each of the valid strings.

The valid distance metrics, and the function they map to, are:

metric	Function
'cityblock'	metrics.pairwise.manhattan_distances
'cosine'	metrics.pairwise.cosine_distances
'euclidean'	metrics.pairwise.euclidean_distances
'haversine'	metrics.pairwise.haversine_distances
<b>'11'</b>	metrics.pairwise.manhattan_distances
<b>'12'</b>	metrics.pairwise.euclidean_distances
'manhattan'	metrics.pairwise.manhattan_distances

Read more in the *User Guide*.

### sklearn.metrics.pairwise.euclidean distances

```
sklearn.metrics.pairwise.euclidean_distances (X, Y=None, Y\_norm\_squared=None, squared=False, X\_norm\_squared=None)
Considering the rows of X (and Y=X) as vectors, compute the distance matrix between each pair of vectors.
```

For efficiency reasons, the euclidean distance between a pair of row vector x and y is computed as:

This formulation has two advantages over other ways of computing distances. First, it is computationally efficient when dealing with sparse data. Second, if one argument varies but the other remains unchanged, then dot(x, x) and/or dot(y, y) can be pre-computed.

However, this is not the most precise way of doing this computation, and the distance matrix returned by this function may not be exactly symmetric as required by, e.g., scipy.spatial.distance functions.

Read more in the *User Guide*.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples\_1, n\_features)]

dist(x, y) = sqrt(dot(x, x) - 2 \* dot(x, y) + dot(y, y))

- Y [{array-like, sparse matrix}, shape (n\_samples\_2, n\_features)]
- **Y\_norm\_squared** [array-like, shape (n\_samples\_2, ), optional] Pre-computed dot-products of vectors in Y (e.g., (Y\*\*2) . sum (axis=1)) May be ignored in some cases, see the note below.

**squared** [boolean, optional] Return squared Euclidean distances.

**X\_norm\_squared** [array-like, shape = [n\_samples\_1], optional] Pre-computed dot-products of vectors in X (e.g., (X\*\*2) . sum (axis=1)) May be ignored in some cases, see the note below.

#### Returns

**distances** [array, shape (n\_samples\_1, n\_samples\_2)]

## See also:

**paired\_distances** distances betweens pairs of elements of X and Y.

## **Notes**

To achieve better accuracy, X\_norm\_squared and Y\_norm\_squared may be unused if they are passed as float 32.

## **Examples**

## sklearn.metrics.pairwise.haversine\_distances

```
sklearn.metrics.pairwise.haversine_distances (X, Y=None)
Compute the Haversine distance between samples in X and Y
```

The Haversine (or great circle) distance is the angular distance between two points on the surface of a sphere. The first distance of each point is assumed to be the latitude, the second is the longitude, given in radians. The dimension of the data must be 2.

$$D(x,y) = 2\arcsin\left[\sqrt{\sin^2((x^2 - y^2)/2) + \cos(x^2)\cos(y^2)\sin^2((x^2 - y^2)/2)}\right]$$

#### **Parameters**

```
X [array_like, shape (n_samples_1, 2)]
```

Y [array\_like, shape (n\_samples\_2, 2), optional]

### Returns

```
distance [{array}, shape (n_samples_1, n_samples_2)]
```

### **Notes**

As the Earth is nearly spherical, the haversine formula provides a good approximation of the distance between two points of the Earth surface, with a less than 1% error on average.

### **Examples**

We want to calculate the distance between the Ezeiza Airport (Buenos Aires, Argentina) and the Charles de Gaulle Airport (Paris, France)

## sklearn.metrics.pairwise.kernel metrics

```
sklearn.metrics.pairwise.kernel_metrics()
```

Valid metrics for pairwise\_kernels

This function simply returns the valid pairwise distance metrics. It exists, however, to allow for a verbose description of the mapping for each of the valid strings.

## The valid distance metrics, and the function they map to, are:

metric	Function
'additive_chi2'	sklearn.pairwise.additive_chi2_kernel
'chi2'	sklearn.pairwise.chi2_kernel
'linear'	sklearn.pairwise.linear_kernel
'poly'	sklearn.pairwise.polynomial_kernel
'polynomial'	sklearn.pairwise.polynomial_kernel
'rbf'	sklearn.pairwise.rbf_kernel
'laplacian'	sklearn.pairwise.laplacian_kernel
'sigmoid'	sklearn.pairwise.sigmoid_kernel
'cosine'	sklearn.pairwise.cosine_similarity

Read more in the *User Guide*.

## sklearn.metrics.pairwise.laplacian\_kernel

sklearn.metrics.pairwise.laplacian\_kernel(X, Y=None, gamma=None)

Compute the laplacian kernel between X and Y.

The laplacian kernel is defined as:

```
K(x, y) = \exp(-\text{gamma} ||x-y||_1)
```

for each pair of rows x in X and y in Y. Read more in the *User Guide*.

New in version 0.17.

## **Parameters**

**X** [array of shape (n\_samples\_X, n\_features)]

**Y** [array of shape (n\_samples\_Y, n\_features)]

gamma [float, default None] If None, defaults to 1.0 / n\_features

#### Returns

**kernel\_matrix** [array of shape (n\_samples\_X, n\_samples\_Y)]

## sklearn.metrics.pairwise.linear\_kernel

sklearn.metrics.pairwise.linear\_kernel(X, Y=None, dense\_output=True)

Compute the linear kernel between X and Y.

Read more in the User Guide.

## **Parameters**

**X** [array of shape (n\_samples\_1, n\_features)]

Y [array of shape (n\_samples\_2, n\_features)]

**dense\_output** [boolean (optional), default True] Whether to return dense output even when the input is sparse. If False, the output is sparse if both input arrays are sparse.

New in version 0.20.

#### Returns

**Gram matrix** [array of shape (n\_samples\_1, n\_samples\_2)]

### sklearn.metrics.pairwise.manhattan distances

```
sklearn.metrics.pairwise.manhattan_distances (X, Y=None, sum_over_features=True) Compute the L1 distances between the vectors in X and Y.
```

With sum\_over\_features equal to False it returns the componentwise distances.

Read more in the User Guide.

### **Parameters**

- **X** [array\_like] An array with shape (n\_samples\_X, n\_features).
- Y [array\_like, optional] An array with shape (n\_samples\_Y, n\_features).
- sum\_over\_features [bool, default=True] If True the function returns the pairwise distance matrix else it returns the componentwise L1 pairwise-distances. Not supported for sparse matrix inputs.

#### Returns

**D** [array] If sum\_over\_features is False shape is (n\_samples\_X \* n\_samples\_Y, n\_features) and D contains the componentwise L1 pairwise-distances (ie. absolute difference), else shape is (n\_samples\_X, n\_samples\_Y) and D contains the pairwise L1 distances.

## **Examples**

```
>>> from sklearn.metrics.pairwise import manhattan_distances
>>> manhattan_distances([[3]], [[3]])
array([[0.]])
>>> manhattan_distances([[3]], [[2]])
array([[1.]])
>>> manhattan_distances([[2]], [[3]])
array([[1.]])
>>> manhattan_distances([[1, 2], [3, 4]],
                                                  [[1, 2], [0, 3]])
array([[0., 2.],
       [4., 4.]])
>>> import numpy as np
>>> X = np.ones((1, 2))
>>> y = np.full((2, 2), 2.)
>>> manhattan_distances(X, y, sum_over_features=False)
array([[1., 1.],
       [1., 1.]])
```

#### sklearn.metrics.pairwise.pairwise kernels

```
sklearn.metrics.pairwise_pairwise_kernels(X, Y=None, metric='linear', fil-
ter_params=False, n_jobs=None, **kwds)
```

Compute the kernel between arrays X and optional array Y.

This method takes either a vector array or a kernel matrix, and returns a kernel matrix. If the input is a vector array, the kernels are computed. If the input is a kernel matrix, it is returned instead.

This method provides a safe way to take a kernel matrix as input, while preserving compatibility with many other algorithms that take a vector array.

If Y is given (default is None), then the returned matrix is the pairwise kernel between the arrays from both X and Y.

#### Valid values for metric are::

```
['additive_chi2', 'chi2', 'linear', 'poly', 'polynomial', 'rbf', 'laplacian', 'sigmoid', 'cosine']
```

Read more in the *User Guide*.

#### **Parameters**

- **X** [array [n\_samples\_a, n\_samples\_a] if metric == "precomputed", or, [n\_samples\_a, n features] otherwise] Array of pairwise kernels between samples, or a feature array.
- Y [array [n\_samples\_b, n\_features]] A second feature array only if X has shape [n\_samples\_a, n\_features].
- metric [string, or callable] The metric to use when calculating kernel between instances in a feature array. If metric is a string, it must be one of the metrics in pairwise.PAIRWISE\_KERNEL\_FUNCTIONS. If metric is "precomputed", X is assumed to be a kernel matrix. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them.

filter\_params [boolean] Whether to filter invalid parameters or not.

**n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. This works by breaking down the pairwise matrix into n\_jobs even slices and computing them in parallel.

None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

\*\*kwds [optional keyword parameters] Any further parameters are passed directly to the kernel function.

### Returns

**K** [array [n\_samples\_a, n\_samples\_a] or [n\_samples\_a, n\_samples\_b]] A kernel matrix K such that K\_{i, j} is the kernel between the ith and jth vectors of the given matrix X, if Y is None. If Y is not None, then K\_{i, j} is the kernel between the ith array from X and the jth array from Y.

#### **Notes**

If metric is 'precomputed', Y is ignored and X is returned.

### sklearn.metrics.pairwise.polynomial kernel

```
sklearn.metrics.pairwise.polynomial_kernel(X, Y=None, degree=3, gamma=None, coef0=1)
```

Compute the polynomial kernel between X and Y:

```
K(X, Y) = (gamma < X, Y > + coef0)^degree
```

Read more in the *User Guide*.

#### **Parameters**

**X** [ndarray of shape (n\_samples\_1, n\_features)]

Y [ndarray of shape (n\_samples\_2, n\_features)]

**degree** [int, default 3]

gamma [float, default None] if None, defaults to 1.0 / n\_features

coef0 [float, default 1]

#### Returns

**Gram matrix** [array of shape (n\_samples\_1, n\_samples\_2)]

## sklearn.metrics.pairwise.rbf\_kernel

```
sklearn.metrics.pairwise.rbf_kernel(X, Y=None, gamma=None)
```

Compute the rbf (gaussian) kernel between X and Y:

```
K(x, y) = \exp(-\text{gamma} ||x-y||^2)
```

for each pair of rows x in X and y in Y.

Read more in the *User Guide*.

### **Parameters**

**X** [array of shape (n\_samples\_X, n\_features)]

Y [array of shape (n\_samples\_Y, n\_features)]

gamma [float, default None] If None, defaults to 1.0 / n\_features

### Returns

**kernel\_matrix** [array of shape (n\_samples\_X, n\_samples\_Y)]

## sklearn.metrics.pairwise.sigmoid\_kernel

sklearn.metrics.pairwise.sigmoid\_kernel(X, Y=None, gamma=None, coef0=1)
Compute the sigmoid kernel between X and Y:

```
K(X, Y) = tanh(gamma < X, Y> + coef0)
```

Read more in the *User Guide*.

### **Parameters**

**X** [ndarray of shape (n\_samples\_1, n\_features)]

Y [ndarray of shape (n\_samples\_2, n\_features)]

```
gamma [float, default None] If None, defaults to 1.0 / n_features
              coef0 [float, default 1]
          Returns
              Gram matrix [array of shape (n_samples_1, n_samples_2)]
sklearn.metrics.pairwise.paired_euclidean_distances
sklearn.metrics.pairwise.paired_euclidean_distances(X, Y)
     Computes the paired euclidean distances between X and Y
     Read more in the User Guide.
          Parameters
              X [array-like, shape (n_samples, n_features)]
              Y [array-like, shape (n_samples, n_features)]
          Returns
              distances [ndarray (n_samples, )]
sklearn.metrics.pairwise.paired_manhattan_distances
sklearn.metrics.pairwise.paired_manhattan_distances(X, Y)
     Compute the L1 distances between the vectors in X and Y.
     Read more in the User Guide.
          Parameters
              X [array-like, shape (n samples, n features)]
              Y [array-like, shape (n_samples, n_features)]
          Returns
              distances [ndarray (n_samples, )]
sklearn.metrics.pairwise.paired_cosine_distances
sklearn.metrics.pairwise.paired cosine distances (X, Y)
     Computes the paired cosine distances between X and Y
     Read more in the User Guide.
          Parameters
              X [array-like, shape (n_samples, n_features)]
              Y [array-like, shape (n_samples, n_features)]
          Returns
              distances [ndarray, shape (n_samples, )]
```

#### **Notes**

The cosine distance is equivalent to the half the squared euclidean distance if each sample is normalized to unit norm

### sklearn.metrics.pairwise.paired distances

```
sklearn.metrics.pairwise.paired_distances (X, Y, metric='euclidean', **kwds)
Computes the paired distances between X and Y.
```

Computes the distances between (X[0], Y[0]), (X[1], Y[1]), etc...

Read more in the *User Guide*.

#### **Parameters**

- **X** [ndarray (n\_samples, n\_features)] Array 1 for distance computation.
- Y [ndarray (n\_samples, n\_features)] Array 2 for distance computation.

metric [string or callable] The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options specified in PAIRED\_DISTANCES, including "euclidean", "manhattan", or "cosine". Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them.

#### Returns

```
distances [ndarray (n_samples, )]
```

See also:

**pairwise\_distances** Computes the distance between every pair of samples

## **Examples**

```
>>> from sklearn.metrics.pairwise import paired_distances
>>> X = [[0, 1], [1, 1]]
>>> Y = [[0, 1], [2, 1]]
>>> paired_distances(X, Y)
array([0., 1.])
```

## sklearn.metrics.pairwise\_distances

```
sklearn.metrics.pairwise_distances (X, Y=None, metric='euclidean', n_jobs=None, **kwds)

Compute the distance matrix from a vector array X and optional Y.
```

This method takes either a vector array or a distance matrix, and returns a distance matrix. If the input is a vector array, the distances are computed. If the input is a distances matrix, it is returned instead.

This method provides a safe way to take a distance matrix as input, while preserving compatibility with many other algorithms that take a vector array.

If Y is given (default is None), then the returned matrix is the pairwise distance between the arrays from both X and Y.

Valid values for metric are:

- From scikit-learn: ['cityblock', 'cosine', 'euclidean', '11', '12', 'manhattan']. These metrics support sparse matrix inputs.
- From scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule'] See the documentation for scipy.spatial.distance for details on these metrics. These metrics do not support sparse matrix inputs.

Note that in the case of 'cityblock', 'cosine' and 'euclidean' (which are valid scipy.spatial.distance metrics), the scikit-learn implementation will be used, which is faster and has support for sparse matrices (except for 'cityblock'). For a verbose description of the metrics from scikit-learn, see the \_\_doc\_\_ of the sklearn.pairwise.distance\_metrics function.

Read more in the *User Guide*.

### **Parameters**

- **X** [array [n\_samples\_a, n\_samples\_a] if metric == "precomputed", or, [n\_samples\_a, n\_features] otherwise] Array of pairwise distances between samples, or a feature array.
- Y [array [n\_samples\_b, n\_features], optional] An optional second feature array. Only allowed if metric != "precomputed".
- metric [string, or callable] The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by scipy.spatial.distance.pdist for its metric parameter, or a metric listed in pairwise.PAIRWISE\_DISTANCE\_FUNCTIONS. If metric is "precomputed", X is assumed to be a distance matrix. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. This works by breaking down the pairwise matrix into n\_jobs even slices and computing them in parallel.
  - None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- \*\*kwds [optional keyword parameters] Any further parameters are passed directly to the distance function. If using a scipy.spatial.distance metric, the parameters are still metric dependent. See the scipy docs for usage examples.

#### Returns

**D** [array [n\_samples\_a, n\_samples\_a] or [n\_samples\_a, n\_samples\_b]] A distance matrix D such that D\_{i, j} is the distance between the ith and jth vectors of the given matrix X, if Y is None. If Y is not None, then D\_{i, j} is the distance between the ith array from X and the jth array from Y.

### See also:

paired\_distances Computes the distances between corresponding elements of two arrays

### Examples using sklearn.metrics.pairwise\_distances

• Agglomerative clustering with different metrics

### sklearn.metrics.pairwise distances argmin

```
sklearn.metrics.pairwise\_distances\_argmin(X, Y, axis=1, metric='euclidean', batch\_size=None, metric\_kwargs=None)
```

Compute minimum distances between one point and a set of points.

This function computes for each row in X, the index of the row of Y which is closest (according to the specified distance).

This is mostly equivalent to calling:

```
pairwise_distances(X, Y=Y, metric=metric).argmin(axis=axis)
```

but uses much less memory, and is faster for large arrays.

This function works with dense 2D arrays only.

#### **Parameters**

- **X** [array-like] Arrays containing points. Respective shapes (n\_samples1, n\_features) and (n\_samples2, n\_features)
- Y [array-like] Arrays containing points. Respective shapes (n\_samples1, n\_features) and (n\_samples2, n\_features)

axis [int, optional, default 1] Axis along which the argmin and distances are to be computed.

**metric** [string or callable] metric to use for distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.

If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating the distance between them. This works for Scipy's metrics, but is less efficient than passing the metric name as a string.

Distance matrices are not supported.

Valid values for metric are:

- from scikit-learn: ['cityblock', 'cosine', 'euclidean', '11', '12', 'manhattan']
- from scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule']

See the documentation for scipy.spatial.distance for details on these metrics.

**batch\_size** [integer] Deprecated since version 0.20: Deprecated for removal in 0.22. Use sklearn.set\_config(working\_memory=...) instead.

metric\_kwargs [dict] keyword arguments to pass to specified metric function.

### Returns

**argmin** [numpy.ndarray] Y[argmin[i], :] is the row in Y that is closest to X[i, :].

### See also:

sklearn.metrics.pairwise\_distances

sklearn.metrics.pairwise distances argmin min

## Examples using sklearn.metrics.pairwise\_distances\_argmin

- Color Quantization using K-Means
- Comparison of the K-Means and MiniBatchKMeans clustering algorithms

### sklearn.metrics.pairwise\_distances\_argmin\_min

```
sklearn.metrics.pairwise\_distances\_argmin\_min (X, Y, axis=1, metric='euclidean', batch\_size=None, metric\_kwargs=None)
```

Compute minimum distances between one point and a set of points.

This function computes for each row in X, the index of the row of Y which is closest (according to the specified distance). The minimal distances are also returned.

This is mostly equivalent to calling:

```
(pairwise_distances(X, Y=Y, metric=metric).argmin(axis=axis), pairwise_distances(X, Y=Y, metric=metric).min(axis=axis))
```

but uses much less memory, and is faster for large arrays.

### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples1, n\_features)] Array containing points.

Y [{array-like, sparse matrix}, shape (n\_samples2, n\_features)] Arrays containing points.

axis [int, optional, default 1] Axis along which the argmin and distances are to be computed.

**metric** [string or callable, default 'euclidean'] metric to use for distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.

If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating the distance between them. This works for Scipy's metrics, but is less efficient than passing the metric name as a string.

Distance matrices are not supported.

Valid values for metric are:

- from scikit-learn: ['cityblock', 'cosine', 'euclidean', '11', '12', 'manhattan']
- from scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule']

See the documentation for scipy.spatial.distance for details on these metrics.

**batch\_size** [integer] Deprecated since version 0.20: Deprecated for removal in 0.22. Use sklearn.set\_config(working\_memory=...) instead.

metric\_kwargs [dict, optional] Keyword arguments to pass to specified metric function.

## Returns

```
argmin [numpy.ndarray] Y[argmin[i], :] is the row in Y that is closest to X[i, :].
```

**distances** [numpy.ndarray] distances[i] is the distance between the i-th row in X and the argmin[i]-th row in Y.

#### See also:

```
sklearn.metrics.pairwise_distances
sklearn.metrics.pairwise_distances_argmin
```

### sklearn.metrics.pairwise distances chunked

```
sklearn.metrics.pairwise_distances_chunked(X, Y=None, reduce_func=None, metric='euclidean', n_jobs=None, work-ing_memory=None, **kwds)
```

Generate a distance matrix chunk by chunk with optional reduction

In cases where not all of a pairwise distance matrix needs to be stored at once, this is used to calculate pairwise distances in working\_memory-sized chunks. If reduce\_func is given, it is run on each chunk and its return values are concatenated into lists, arrays or sparse matrices.

### **Parameters**

- **X** [array [n\_samples\_a, n\_samples\_a] if metric == "precomputed", or,] [n\_samples\_a, n\_features] otherwise Array of pairwise distances between samples, or a feature array.
- Y [array [n\_samples\_b, n\_features], optional] An optional second feature array. Only allowed if metric != "precomputed".
- reduce\_func [callable, optional] The function which is applied on each chunk of the distance
   matrix, reducing it to needed values. reduce\_func(D\_chunk, start) is called re peatedly, where D\_chunk is a contiguous vertical slice of the pairwise distance matrix,
   starting at row start. It should return an array, a list, or a sparse matrix of length
   D\_chunk.shape[0], or a tuple of such objects.
  - If None, pairwise\_distances\_chunked returns a generator of vertical chunks of the distance matrix.
- metric [string, or callable] The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by scipy.spatial.distance.pdist for its metric parameter, or a metric listed in pairwise.PAIRWISE\_DISTANCE\_FUNCTIONS. If metric is "precomputed", X is assumed to be a distance matrix. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them.
- **n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. This works by breaking down the pairwise matrix into n\_jobs even slices and computing them in parallel.
  - None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- working\_memory [int, optional] The sought maximum memory for temporary
  distance matrix chunks. When None (default), the value of sklearn.
  get\_config()['working\_memory'] is used.
- \*\*\*kwds\* [optional keyword parameters] Any further parameters are passed directly to the distance function. If using a scipy.spatial.distance metric, the parameters are still metric dependent. See the scipy docs for usage examples.

### **Yields**

**D\_chunk** [array or sparse matrix] A contiguous slice of distance matrix, optionally processed by reduce\_func.

## **Examples**

Without reduce func:

Retrieve all neighbors and average distance within radius r:

Where r is defined per sample, we need to make use of start:

Force row-by-row generation by reducing working\_memory:

# 6.25 sklearn.mixture: Gaussian Mixture Models

The sklearn.mixture module implements mixture modeling algorithms.

**User guide:** See the *Gaussian mixture models* section for further details.

mixture.BayesianGaussianMixture([])	Variational Bayesian estimation of a Gaussian mixture.
mixture.GaussianMixture([n_components,])	Gaussian Mixture.

## 6.25.1 sklearn.mixture.BayesianGaussianMixture

```
covariance_type='full',
class sklearn.mixture.BayesianGaussianMixture (n_components=1,
                                                         tol=0.001, reg_covar=1e-06, max_iter=100,
                                                         n_{init}=1.
                                                                             init_params='kmeans',
                                                          weight concentration prior type='dirichlet process',
                                                         weight_concentration_prior=None,
                                                         mean precision prior=None,
                                                         mean_prior=None,
                                                                                               de-
                                                          grees_of_freedom_prior=None,
                                                                                           covari-
                                                         ance_prior=None,
                                                                               random_state=None,
                                                          warm start=False.
                                                                               verbose=0.
                                                         bose_interval=10)
```

Variational Bayesian estimation of a Gaussian mixture.

This class allows to infer an approximate posterior distribution over the parameters of a Gaussian mixture distribution. The effective number of components can be inferred from the data.

This class implements two types of prior for the weights distribution: a finite mixture model with Dirichlet distribution and an infinite mixture model with the Dirichlet Process. In practice Dirichlet Process inference algorithm is approximated and uses a truncated distribution with a fixed maximum number of components (called the Stick-breaking representation). The number of components actually used almost always depends on the data.

New in version 0.18.

Read more in the *User Guide*.

### **Parameters**

- n\_components [int, defaults to 1.] The number of mixture components. Depending on the data and the value of the weight\_concentration\_prior the model can decide to not use all the components by setting some component weights\_ to values very close to zero. The number of effective components is therefore smaller than n\_components.
- **covariance\_type** [{'full', 'tied', 'diag', 'spherical'}, defaults to 'full'] String describing the type of covariance parameters to use. Must be one of:

```
'full' (each component has its own general covariance matrix),
'tied' (all components share the same general covariance matrix),
'diag' (each component has its own diagonal covariance matrix),
'spherical' (each component has its own single variance).
```

- **tol** [float, defaults to 1e-3.] The convergence threshold. EM iterations will stop when the lower bound average gain on the likelihood (of the training data with respect to the model) is below this threshold.
- **reg\_covar** [float, defaults to 1e-6.] Non-negative regularization added to the diagonal of covariance. Allows to assure that the covariance matrices are all positive.

max\_iter [int, defaults to 100.] The number of EM iterations to perform.

- **n\_init** [int, defaults to 1.] The number of initializations to perform. The result with the highest lower bound value on the likelihood is kept.
- **init\_params** [{'kmeans', 'random'}, defaults to 'kmeans'.] The method used to initialize the weights, the means and the covariances. Must be one of:

```
'kmeans' : responsibilities are initialized using kmeans.
'random' : responsibilities are initialized randomly.
```

weight\_concentration\_prior\_type [str, defaults to 'dirichlet\_process'.] String describing the type of the weight concentration prior. Must be one of:

```
'dirichlet_process' (using the Stick-breaking representation),
'dirichlet_distribution' (can favor more uniform weights).
```

- weight\_concentration\_prior [float | None, optional.] The dirichlet concentration of each component on the weight distribution (Dirichlet). This is commonly called gamma in the literature. The higher concentration puts more mass in the center and will lead to more components being active, while a lower concentration parameter will lead to more mass at the edge of the mixture weights simplex. The value of the parameter must be greater than 0. If it is None, it's set to 1. / n\_components.
- mean\_precision\_prior [float | None, optional.] The precision prior on the mean distribution (Gaussian). Controls the extend to where means can be placed. Larger values concentrate the means of each clusters around mean\_prior. The value of the parameter must be greater than 0. If it is None, it's set to 1.
- **mean\_prior** [array-like, shape (n\_features,), optional] The prior on the mean distribution (Gaussian). If it is None, it's set to the mean of X.
- **degrees\_of\_freedom\_prior** [float | None, optional.] The prior of the number of degrees of freedom on the covariance distributions (Wishart). If it is None, it's set to *n\_features*.
- covariance\_prior [float or array-like, optional] The prior on the covariance distribution (Wishart). If it is None, the emiprical covariance prior is initialized using the covariance of X. The shape depends on covariance\_type:

```
(n_features, n_features) if 'full',
(n_features, n_features) if 'tied',
(n_features) if 'diag',
float if 'spherical'
```

- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- warm\_start [bool, default to False.] If 'warm\_start' is True, the solution of the last fitting is used as initialization for the next call of fit(). This can speed up convergence when fit is called several times on similar problems. See *the Glossary*.
- **verbose** [int, default to 0.] Enable verbose output. If 1 then it prints the current initialization and each iteration step. If greater than 1 then it prints also the log probability and the time needed for each step.
- **verbose\_interval** [int, default to 10.] Number of iteration done before the next print.

### Attributes

weights [array-like, shape (n\_components,)] The weights of each mixture components.

means\_ [array-like, shape (n\_components, n\_features)] The mean of each mixture component.

**covariances**\_ [array-like] The covariance of each mixture component. The shape depends on covariance\_type:

precisions\_ [array-like] The precision matrices for each component in the mixture. A precision matrix is the inverse of a covariance matrix. A covariance matrix is symmetric positive definite so the mixture of Gaussian can be equivalently parameterized by the precision matrices. Storing the precision matrices instead of the covariance matrices makes it more efficient to compute the log-likelihood of new samples at test time. The shape depends on covariance\_type:

```
(n_components,)
    if 'spherical',
    (n_features, n_features)
    if 'tied',
    (n_components, n_features)
    if 'diag',
    (n_components, n_features, n_features)
if 'full'
```

precisions\_cholesky\_ [array-like] The cholesky decomposition of the precision matrices of each mixture component. A precision matrix is the inverse of a covariance matrix. A covariance matrix is symmetric positive definite so the mixture of Gaussian can be equivalently parameterized by the precision matrices. Storing the precision matrices instead of the covariance matrices makes it more efficient to compute the log-likelihood of new samples at test time. The shape depends on covariance\_type:

```
(n_components,)
  (n_features, n_features)
    if 'spherical',
    (n_components, n_features)
    if 'tied',
    if 'diag',
    (n_components, n_features, n_features)
    if 'full'
```

**converged** [bool] True when convergence was reached in fit(), False otherwise.

n\_iter\_ [int] Number of step used by the best fit of inference to reach the convergence.

**lower\_bound\_** [float] Lower bound value on the likelihood (of the training data with respect to the model) of the best fit of inference.

weight\_concentration\_prior\_ [tuple or float] The dirichlet concentration of each
component on the weight distribution (Dirichlet). The type depends on
weight\_concentration\_prior\_type:

The higher concentration puts more mass in the center and will lead to more components being active, while a lower concentration parameter will lead to more mass at the edge of the simplex.

**weight\_concentration\_** [array-like, shape (n\_components,)] The dirichlet concentration of each component on the weight distribution (Dirichlet).

**mean\_precision\_prior** [float] The precision prior on the mean distribution (Gaussian). Controls the extend to where means can be placed. Larger values concentrate the means of each clusters around mean\_prior.

**mean\_precision\_** [array-like, shape (n\_components,)] The precision of each components on the mean distribution (Gaussian).

mean\_prior\_ [array-like, shape (n\_features,)] The prior on the mean distribution (Gaussian).

**degrees\_of\_freedom\_prior\_** [float] The prior of the number of degrees of freedom on the covariance distributions (Wishart).

**degrees\_of\_freedom\_** [array-like, shape (n\_components,)] The number of degrees of freedom of each components in the model.

**covariance\_prior\_** [float or array-like] The prior on the covariance distribution (Wishart). The shape depends on covariance\_type:

```
(n_features, n_features) if 'full',
(n_features, n_features) if 'tied',
(n_features) if 'diag',
float if 'spherical'
```

### See also:

GaussianMixture Finite Gaussian mixture fit with EM.

#### References

[R16529824bff2-1], [R16529824bff2-2], [R16529824bff2-3]

#### **Methods**

fit(self, X[, y])	Estimate model parameters with the EM algorithm.
<pre>fit_predict(self, X[, y])</pre>	Estimate model parameters using X and predict the la-
	bels for X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict the labels for the data samples in X using trained
	model.
predict_proba(self, X)	Predict posterior probability of each component given
	the data.
sample(self[, n_samples])	Generate random samples from the fitted Gaussian dis-
	tribution.
score(self, X[, y])	Compute the per-sample average log-likelihood of the
	given data X.
score_samples(self, X)	Compute the weighted log probabilities for each sam-
	ple.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, n_components=1, covariance_type='full', tol=0.001, reg_covar=1e-06, max_iter=100, n_init=1, init_params='kmeans', weight_concentration_prior_type='dirichlet_process', weight_concentration_prior=None, mean_precision_prior=None, mean_prior=None, degrees_of_freedom_prior=None, covariance_prior=None, random_state=None, warm_start=False, verbose=0, verbose_interval=10)
```

**fit** (self, X, y=None)

Estimate model parameters with the EM algorithm.

The method fits the model n\_init times and sets the parameters with which the model has the largest likelihood or lower bound. Within each trial, the method iterates between E-step and M-step for max\_iter times until the change of likelihood or lower bound is less than tol, otherwise, a ConvergenceWarning is raised. If warm\_start is True, then n\_init is ignored and a single initialization is performed upon the first call. Upon consecutive calls, training starts where it left off.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

#### **Returns**

self

## fit\_predict (self, X, y=None)

Estimate model parameters using X and predict the labels for X.

The method fits the model n\_init times and sets the parameters with which the model has the largest likelihood or lower bound. Within each trial, the method iterates between E-step and M-step for *max\_iter* times until the change of likelihood or lower bound is less than tol, otherwise, a *ConvergenceWarning* is raised. After fitting, it predicts the most probable label for the input data points.

New in version 0.20.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

#### Returns

labels [array, shape (n\_samples,)] Component labels.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### predict (self, X)

Predict the labels for the data samples in X using trained model.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

#### Returns

labels [array, shape (n\_samples,)] Component labels.

#### predict\_proba (self, X)

Predict posterior probability of each component given the data.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

#### Returns

**resp** [array, shape (n\_samples, n\_components)] Returns the probability each Gaussian (state) in the model given each sample.

### sample (self, n\_samples=1)

Generate random samples from the fitted Gaussian distribution.

#### **Parameters**

**n\_samples** [int, optional] Number of samples to generate. Defaults to 1.

#### **Returns**

- **X** [array, shape (n\_samples, n\_features)] Randomly generated sample
- y [array, shape (nsamples,)] Component labels

### score(self, X, y=None)

Compute the per-sample average log-likelihood of the given data X.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_dimensions)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

### Returns

**log\_likelihood** [float] Log likelihood of the Gaussian mixture given X.

### $score\_samples(self, X)$

Compute the weighted log probabilities for each sample.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

#### Returns

**log\_prob** [array, shape (n\_samples,)] Log probabilities of each data point in X.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# Examples using sklearn.mixture.BayesianGaussianMixture

- Gaussian Mixture Model Ellipsoids
- Gaussian Mixture Model Sine Curve
- Concentration Prior Type Analysis of Variation Bayesian Gaussian Mixture

## 6.25.2 sklearn.mixture.GaussianMixture

```
 \begin{array}{c} \textbf{class} \text{ sklearn.mixture.} \textbf{ GaussianMixture} \ (n\_components=1, \quad covariance\_type='full', \quad tol=0.001, \\ reg\_covar=1e-06, \quad max\_iter=100, \quad n\_init=1, \\ init\_params='kmeans', \quad weights\_init=None, \\ means\_init=None, \quad precisions\_init=None, \quad random\_state=None, \quad warm\_start=False, \quad verbose=0, \\ verbose\_interval=10) \end{array}
```

Gaussian Mixture.

Representation of a Gaussian mixture model probability distribution. This class allows to estimate the parameters of a Gaussian mixture distribution.

Read more in the User Guide.

New in version 0.18.

#### **Parameters**

**n\_components** [int, defaults to 1.] The number of mixture components.

covariance\_type [{'full' (default), 'tied', 'diag', 'spherical'}] String describing the type of covariance parameters to use. Must be one of:

'full' each component has its own general covariance matrix

'tied' all components share the same general covariance matrix

'diag' each component has its own diagonal covariance matrix

'spherical' each component has its own single variance

**tol** [float, defaults to 1e-3.] The convergence threshold. EM iterations will stop when the lower bound average gain is below this threshold.

**reg\_covar** [float, defaults to 1e-6.] Non-negative regularization added to the diagonal of covariance. Allows to assure that the covariance matrices are all positive.

max\_iter [int, defaults to 100.] The number of EM iterations to perform.

**n** init [int, defaults to 1.] The number of initializations to perform. The best results are kept.

**init\_params** [{'kmeans', 'random'}, defaults to 'kmeans'.] The method used to initialize the weights, the means and the precisions. Must be one of:

```
'kmeans' : responsibilities are initialized using kmeans.
'random' : responsibilities are initialized randomly.
```

weights\_init [array-like, shape (n\_components, ), optional] The user-provided initial weights, defaults to None. If it None, weights are initialized using the init\_params method.

**means\_init** [array-like, shape (n\_components, n\_features), optional] The user-provided initial means, defaults to None, If it None, means are initialized using the init\_params method.

precisions\_init [array-like, optional.] The user-provided initial precisions (inverse of the covariance matrices), defaults to None. If it None, precisions are initialized using the 'init\_params' method. The shape depends on 'covariance\_type':

```
(n_components,)
    if 'spherical',
    (n_features, n_features)
    if 'tied',
    (n_components, n_features)
    if 'diag',
    (n_components, n_features, n_features)
if 'full'
```

- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- warm\_start [bool, default to False.] If 'warm\_start' is True, the solution of the last fitting is used as initialization for the next call of fit(). This can speed up convergence when fit is called several times on similar problems. In that case, 'n\_init' is ignored and only a single initialization occurs upon the first call. See *the Glossary*.
- **verbose** [int, default to 0.] Enable verbose output. If 1 then it prints the current initialization and each iteration step. If greater than 1 then it prints also the log probability and the time needed for each step.

verbose\_interval [int, default to 10.] Number of iteration done before the next print.

### **Attributes**

weights\_ [array-like, shape (n\_components,)] The weights of each mixture components.

means\_ [array-like, shape (n\_components, n\_features)] The mean of each mixture component.

**covariances**\_ [array-like] The covariance of each mixture component. The shape depends on covariance\_type:

precisions\_ [array-like] The precision matrices for each component in the mixture. A precision matrix is the inverse of a covariance matrix. A covariance matrix is symmetric positive definite so the mixture of Gaussian can be equivalently parameterized by the precision matrices. Storing the precision matrices instead of the covariance matrices makes it more efficient to compute the log-likelihood of new samples at test time. The shape depends on covariance\_type:

precisions\_cholesky\_ [array-like] The cholesky decomposition of the precision matrices of each mixture component. A precision matrix is the inverse of a covariance matrix. A covariance matrix is symmetric positive definite so the mixture of Gaussian can be equivalently parameterized by the precision matrices. Storing the precision matrices instead of the covariance matrices makes it more efficient to compute the log-likelihood of new samples at test time. The shape depends on covariance\_type:

converged\_ [bool] True when convergence was reached in fit(), False otherwise.

**n\_iter\_** [int] Number of step used by the best fit of EM to reach the convergence.

**lower\_bound** [float] Lower bound value on the log-likelihood (of the training data with respect to the model) of the best fit of EM.

### See also:

BayesianGaussianMixture Gaussian mixture model fit with a variational inference.

#### **Methods**

- ( 10 X7)	
aic(self, X)	Akaike information criterion for the current model on
	the input X.
bic(self, X)	Bayesian information criterion for the current model on
	the input X.
fit(self, X[, y])	Estimate model parameters with the EM algorithm.
<pre>fit_predict(self, X[, y])</pre>	Estimate model parameters using X and predict the la-
	bels for X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict the labels for the data samples in X using trained
	model.
predict_proba(self, X)	Predict posterior probability of each component given
	the data.
sample(self[, n_samples])	Generate random samples from the fitted Gaussian dis-
	tribution.
score(self, X[, y])	Compute the per-sample average log-likelihood of the
	given data X.
score_samples(self, X)	Compute the weighted log probabilities for each sam-
	ple.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, n\_components=1, covariance\_type='full', tol=0.001, reg\_covar=1e-06, max\_iter=100, n\_init=1, init\_params='kmeans', weights\_init=None, means\_init=None, precisions\_init=None, random\_state=None, warm\_start=False, verbose=0, verbose\_interval=10)

## $\mathtt{aic}(\mathit{self},X)$

Akaike information criterion for the current model on the input X.

#### **Parameters**

**X** [array of shape (n\_samples, n\_dimensions)]

## Returns

aic [float] The lower the better.

## bic(self, X)

Bayesian information criterion for the current model on the input X.

### **Parameters**

**X** [array of shape (n\_samples, n\_dimensions)]

## Returns

**bic** [float] The lower the better.

### **fit** (self, X, y=None)

Estimate model parameters with the EM algorithm.

The method fits the model  $n_{init}$  times and sets the parameters with which the model has the largest likelihood or lower bound. Within each trial, the method iterates between E-step and M-step

for max\_iter times until the change of likelihood or lower bound is less than tol, otherwise, a ConvergenceWarning is raised. If warm\_start is True, then n\_init is ignored and a single initialization is performed upon the first call. Upon consecutive calls, training starts where it left off.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

#### Returns

self

## fit\_predict (self, X, y=None)

Estimate model parameters using X and predict the labels for X.

The method fits the model n\_init times and sets the parameters with which the model has the largest likelihood or lower bound. Within each trial, the method iterates between E-step and M-step for *max\_iter* times until the change of likelihood or lower bound is less than tol, otherwise, a *ConvergenceWarning* is raised. After fitting, it predicts the most probable label for the input data points.

New in version 0.20.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

#### Returns

labels [array, shape (n samples,)] Component labels.

### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### predict (self, X)

Predict the labels for the data samples in X using trained model.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

### Returns

**labels** [array, shape (n\_samples,)] Component labels.

### predict\_proba (self, X)

Predict posterior probability of each component given the data.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

#### **Returns**

**resp** [array, shape (n\_samples, n\_components)] Returns the probability each Gaussian (state) in the model given each sample.

### sample (self, n\_samples=1)

Generate random samples from the fitted Gaussian distribution.

#### **Parameters**

**n\_samples** [int, optional] Number of samples to generate. Defaults to 1.

#### Returns

**X** [array, shape (n\_samples, n\_features)] Randomly generated sample

y [array, shape (nsamples,)] Component labels

### score(self, X, y=None)

Compute the per-sample average log-likelihood of the given data X.

#### **Parameters**

X [array-like, shape (n\_samples, n\_dimensions)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

#### Returns

**log\_likelihood** [float] Log likelihood of the Gaussian mixture given X.

### $score\_samples(self, X)$

Compute the weighted log probabilities for each sample.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

### Returns

**log\_prob** [array, shape (n\_samples,)] Log probabilities of each data point in X.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## Examples using sklearn.mixture.GaussianMixture

- Comparing different clustering algorithms on toy datasets
- Density Estimation for a Gaussian mixture
- Gaussian Mixture Model Ellipsoids
- Gaussian Mixture Model Selection
- GMM covariances
- Gaussian Mixture Model Sine Curve

# 6.26 sklearn.model\_selection: Model Selection

**User guide:** See the *Cross-validation: evaluating estimator performance, Tuning the hyper-parameters of an estimator* and *Learning curve* sections for further details.

## 6.26.1 Splitter Classes

model_selection.GroupKFold([n_splits])	K-fold iterator variant with non-overlapping groups.
<pre>model_selection.GroupShuffleSplit([])</pre>	Shuffle-Group(s)-Out cross-validation iterator
model_selection.KFold([n_splits, shuffle,])	K-Folds cross-validator
model_selection.LeaveOneGroupOut	Leave One Group Out cross-validator
model_selection.LeavePGroupsOut(n_groups)	Leave P Group(s) Out cross-validator
model_selection.LeaveOneOut	Leave-One-Out cross-validator
model_selection.LeavePOut(p)	Leave-P-Out cross-validator
model_selection.PredefinedSplit(test_fold)	Predefined split cross-validator
model_selection.RepeatedKFold([n_splits,	Repeated K-Fold cross validator.
])	
model_selection.RepeatedStratifiedKFold()	Repeated Stratified K-Fold cross validator.
<pre>model_selection.ShuffleSplit([n_splits,])</pre>	Random permutation cross-validator
model_selection.StratifiedKFold([n_splits,	Stratified K-Folds cross-validator
])	
model_selection.StratifiedShuffleSplit([	. Stratified ShuffleSplit cross-validator
<pre>model_selection.TimeSeriesSplit([n_splits,</pre>	Time Series cross-validator
])	

## sklearn.model\_selection.GroupKFold

class sklearn.model\_selection.GroupKFold(n\_splits='warn')

K-fold iterator variant with non-overlapping groups.

The same group will not appear in two different folds (the number of distinct groups has to be at least equal to the number of folds).

The folds are approximately balanced in the sense that the number of distinct groups is approximately the same in each fold.

### **Parameters**

**n\_splits** [int, default=3] Number of folds. Must be at least 2.

Changed in version 0.20: n\_splits default value will change from 3 to 5 in v0.22.

### See also:

LeaveOneGroupOut For splitting the data according to explicit domain-specific stratification of the dataset.

## **Examples**

```
>>> import numpy as np
>>> from sklearn.model_selection import GroupKFold
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> y = np.array([1, 2, 3, 4])
>>> groups = np.array([0, 0, 2, 2])
```

```
>>> group_kfold = GroupKFold(n_splits=2)
>>> group_kfold.get_n_splits(X, y, groups)
>>> print(group_kfold)
GroupKFold(n_splits=2)
>>> for train_index, test_index in group_kfold.split(X, y, groups):
       print("TRAIN:", train_index, "TEST:", test_index)
       X_train, X_test = X[train_index], X[test_index]
. . .
       y_train, y_test = y[train_index], y[test_index]
. . .
        print(X_train, X_test, y_train, y_test)
TRAIN: [0 1] TEST: [2 3]
[[1 2]
[3 4]] [[5 6]
[7 8]] [1 2] [3 4]
TRAIN: [2 3] TEST: [0 1]
[[5 6]
[7 8]] [[1 2]
 [3 4]] [3 4] [1 2]
```

#### **Methods**

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-validator
split(self, X[, y, groups])	Generate indices to split data into training and test set.

```
init (self, n splits='warn')
```

get\_n\_splits (self, X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

### **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.

groups [object] Always ignored, exists for compatibility.

## Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X, y=None, groups=None)
```

Generate indices to split data into training and test set.

## **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape (n\_samples,), optional] The target variable for supervised learning problems.
- **groups** [array-like, with shape (n\_samples,)] Group labels for the samples used while splitting the dataset into train/test set.

## **Yields**

**train** [ndarray] The training set indices for that split. **test** [ndarray] The testing set indices for that split.

## Examples using sklearn.model\_selection.GroupKFold

• Visualizing cross-validation behavior in scikit-learn

### sklearn.model\_selection.GroupShuffleSplit

Shuffle-Group(s)-Out cross-validation iterator

Provides randomized train/test indices to split data according to a third-party provided group. This group information can be used to encode arbitrary domain specific stratifications of the samples as integers.

For instance the groups could be the year of collection of the samples and thus allow for cross-validation against time-based splits.

The difference between LeavePGroupsOut and GroupShuffleSplit is that the former generates splits using all subsets of size p unique groups, whereas GroupShuffleSplit generates a user-determined number of random test splits, each with a user-determined fraction of unique groups.

For example, a less computationally intensive alternative to LeavePGroupsOut(p=10) would be GroupShuffleSplit(test\_size=10, n\_splits=100).

Note: The parameters test\_size and train\_size refer to groups, and not to samples, as in ShuffleSplit.

### **Parameters**

**n** splits [int (default 5)] Number of re-shuffling & splitting iterations.

test\_size [float, int, None, optional (default=None)] If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test groups. If None, the value is set to the complement of the train size. If train\_size is also None, it will be set to 0.2.

**train\_size** [float, int, or None, default is None] If float, should be between 0.0 and 1.0 and represent the proportion of the groups to include in the train split. If int, represents the absolute number of train groups. If None, the value is automatically set to the complement of the test size.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

### **Methods**

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-
	validator
split(self, X[, y, groups])	Generate indices to split data into training and test set.

\_\_init\_\_ (self, n\_splits=5, test\_size=None, train\_size=None, random\_state=None)

# get\_n\_splits (self, X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

#### **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.

**groups** [object] Always ignored, exists for compatibility.

# Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X, y=None, groups=None)
```

Generate indices to split data into training and test set.

## **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape (n\_samples,), optional] The target variable for supervised learning problems.

**groups** [array-like, with shape (n\_samples,)] Group labels for the samples used while splitting the dataset into train/test set.

#### **Yields**

train [ndarray] The training set indices for that split.

test [ndarray] The testing set indices for that split.

## **Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random\_state to an integer.

# Examples using sklearn.model\_selection.GroupShuffleSplit

• Visualizing cross-validation behavior in scikit-learn

# sklearn.model\_selection.KFold

class sklearn.model\_selection.KFold(n\_splits='warn', shuffle=False, random\_state=None)
 K-Folds cross-validator

Provides train/test indices to split data in train/test sets. Split dataset into k consecutive folds (without shuffling by default).

Each fold is then used once as a validation while the k - 1 remaining folds form the training set.

Read more in the User Guide.

## **Parameters**

**n\_splits** [int, default=3] Number of folds. Must be at least 2.

Changed in version 0.20: n\_splits default value will change from 3 to 5 in v0.22.

**shuffle** [boolean, optional] Whether to shuffle the data before splitting into batches.

random\_state [int, RandomState instance or None, optional, default=None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when shuffle == True.

#### See also:

**Stratified**KFold Takes group information into account to avoid building folds with imbalanced class distributions (for binary or multiclass classification tasks).

**GroupKFold** K-fold iterator variant with non-overlapping groups.

RepeatedKFold Repeats K-Fold n times.

## **Notes**

The first n\_samples % n\_splits folds have size n\_samples // n\_splits + 1, other folds have size n\_samples // n\_splits, where n\_samples is the number of samples.

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random\_state to an integer.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.model_selection import KFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([1, 2, 3, 4])
>>> kf = KFold(n_splits=2)
>>> kf.get_n_splits(X)
2
>>> print(kf)
KFold(n_splits=2, random_state=None, shuffle=False)
>>> for train_index, test_index in kf.split(X):
       print("TRAIN:", train_index, "TEST:", test_index)
       X_train, X_test = X[train_index], X[test_index]
       y_train, y_test = y[train_index], y[test_index]
. . .
TRAIN: [2 3] TEST: [0 1]
TRAIN: [0 1] TEST: [2 3]
```

# **Methods**

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-
	validator
split(self, X[, y, groups])	Generate indices to split data into training and test set.

```
___init___ (self, n_splits='warn', shuffle=False, random_state=None)
```

```
get_n_splits (self, X=None, y=None, groups=None)
```

Returns the number of splitting iterations in the cross-validator

# **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.
- groups [object] Always ignored, exists for compatibility.

## Returns

**n splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X, y=None, groups=None)
```

Generate indices to split data into training and test set.

## **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array-like, shape (n\_samples,)] The target variable for supervised learning problems.
- **groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set.

## **Yields**

train [ndarray] The training set indices for that split.

test [ndarray] The testing set indices for that split.

## Examples using sklearn.model\_selection.KFold

- Feature agglomeration vs. univariate selection
- Gradient Boosting Out-of-Bag estimates
- Cross-validation on diabetes Dataset Exercise
- Nested versus non-nested cross-validation
- Visualizing cross-validation behavior in scikit-learn

## sklearn.model\_selection.LeaveOneGroupOut

```
class sklearn.model_selection.LeaveOneGroupOut
```

Leave One Group Out cross-validator

Provides train/test indices to split data according to a third-party provided group. This group information can be used to encode arbitrary domain specific stratifications of the samples as integers.

For instance the groups could be the year of collection of the samples and thus allow for cross-validation against time-based splits.

Read more in the *User Guide*.

```
>>> import numpy as np
>>> from sklearn.model_selection import LeaveOneGroupOut
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> y = np.array([1, 2, 1, 2])
>>> groups = np.array([1, 1, 2, 2])
```

```
>>> logo = LeaveOneGroupOut()
>>> logo.get_n_splits(X, y, groups)
>>> logo.get_n_splits(groups=groups) # 'groups' is always required
>>> print(logo)
LeaveOneGroupOut()
>>> for train_index, test_index in logo.split(X, y, groups):
      print("TRAIN:", train_index, "TEST:", test_index)
      X_train, X_test = X[train_index], X[test_index]
      y_train, y_test = y[train_index], y[test_index]
      print(X_train, X_test, y_train, y_test)
TRAIN: [2 3] TEST: [0 1]
[[5 6]
[7 8]] [[1 2]
[3 4]] [1 2] [1 2]
TRAIN: [0 1] TEST: [2 3]
[[1 2]
[3 4]] [[5 6]
[7 8]] [1 2] [1 2]
```

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-validator
split(self, X[, y, groups])	Generate indices to split data into training and test set.

```
init (self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

```
get_n_splits (self, X=None, y=None, groups=None)
```

Returns the number of splitting iterations in the cross-validator

## **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.

**groups** [array-like, with shape (n\_samples,)] Group labels for the samples used while splitting the dataset into train/test set. This 'groups' parameter must always be specified to calculate the number of splits, though the other parameters can be omitted.

### Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X, y=None, groups=None)
```

Generate indices to split data into training and test set.

## **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, of length n\_samples, optional] The target variable for supervised learning problems.

**groups** [array-like, with shape (n\_samples,)] Group labels for the samples used while splitting the dataset into train/test set.

#### **Yields**

train [ndarray] The training set indices for that split.

**test** [ndarray] The testing set indices for that split.

# sklearn.model\_selection.LeavePGroupsOut

```
class sklearn.model_selection.LeavePGroupsOut (n_groups)
    Leave P Group(s) Out cross-validator
```

Provides train/test indices to split data according to a third-party provided group. This group information can be used to encode arbitrary domain specific stratifications of the samples as integers.

For instance the groups could be the year of collection of the samples and thus allow for cross-validation against time-based splits.

The difference between LeavePGroupsOut and LeaveOneGroupOut is that the former builds the test sets with all the samples assigned to p different values of the groups while the latter uses samples all assigned the same groups.

Read more in the User Guide.

## **Parameters**

**n\_groups** [int] Number of groups (p) to leave out in the test split.

## See also:

**GroupKFold** K-fold iterator variant with non-overlapping groups.

```
>>> import numpy as np
>>> from sklearn.model selection import LeavePGroupsOut
>>> X = np.array([[1, 2], [3, 4], [5, 6]])
>>> y = np.array([1, 2, 1])
>>> groups = np.array([1, 2, 3])
>>> lpgo = LeavePGroupsOut (n_groups=2)
>>> lpgo.get_n_splits(X, y, groups)
>>> lpgo.get_n_splits(groups=groups) # 'groups' is always required
3
>>> print(lpgo)
LeavePGroupsOut (n_groups=2)
>>> for train_index, test_index in lpgo.split(X, y, groups):
      print("TRAIN:", train_index, "TEST:", test_index)
      X_train, X_test = X[train_index], X[test_index]
      y_train, y_test = y[train_index], y[test_index]
      print(X_train, X_test, y_train, y_test)
TRAIN: [2] TEST: [0 1]
[[5 6]] [[1 2]
[3 4]] [1] [1 2]
TRAIN: [1] TEST: [0 2]
[[3 4]] [[1 2]
[5 6]] [2] [1 1]
```

```
TRAIN: [0] TEST: [1 2]
[[1 2]] [[3 4]
[5 6]] [1] [2 1]
```

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-validator
split(self, X[, y, groups])	Generate indices to split data into training and test set.

```
___init___(self, n_groups)
```

get\_n\_splits (self, X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

# **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.

**groups** [array-like, with shape (n\_samples,)] Group labels for the samples used while splitting the dataset into train/test set. This 'groups' parameter must always be specified to calculate the number of splits, though the other parameters can be omitted.

#### Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X, y=None, groups=None)
```

Generate indices to split data into training and test set.

### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array-like, of length n\_samples, optional] The target variable for supervised learning problems.

**groups** [array-like, with shape (n\_samples,)] Group labels for the samples used while splitting the dataset into train/test set.

# **Yields**

train [ndarray] The training set indices for that split.

test [ndarray] The testing set indices for that split.

# sklearn.model selection.LeaveOneOut

```
class sklearn.model_selection.LeaveOneOut
```

Leave-One-Out cross-validator

Provides train/test indices to split data in train/test sets. Each sample is used once as a test set (singleton) while the remaining samples form the training set.

Note: LeaveOneOut() is equivalent to  $KFold(n\_splits=n)$  and LeavePOut(p=1) where n is the number of samples.

Due to the high number of test sets (which is the same as the number of samples) this cross-validation method can be very costly. For large datasets one should favor <code>KFold</code>, <code>ShuffleSplit</code> or <code>StratifiedKFold</code>.

Read more in the *User Guide*.

#### See also:

**LeaveOneGroupOut** For splitting the data according to explicit, domain-specific stratification of the dataset. **GroupKFold** K-fold iterator variant with non-overlapping groups.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.model_selection import LeaveOneOut
>>> X = np.array([[1, 2], [3, 4]])
>>> y = np.array([1, 2])
>>> loo = LeaveOneOut()
>>> loo.get_n_splits(X)
>>> print(loo)
LeaveOneOut()
>>> for train_index, test_index in loo.split(X):
      print("TRAIN:", train_index, "TEST:", test_index)
      X_train, X_test = X[train_index], X[test_index]
       y_train, y_test = y[train_index], y[test_index]
      print(X_train, X_test, y_train, y_test)
TRAIN: [1] TEST: [0]
[[3 4]] [[1 2]] [2] [1]
TRAIN: [0] TEST: [1]
[[1 2]] [[3 4]] [1] [2]
```

# Methods

<pre>get_n_splits(self, X[, y, groups])</pre>	Returns the number of splitting iterations in the cross-
	validator
split(self, X[, y, groups])	Generate indices to split data into training and test set.

```
__init__(self, /, *args, **kwargs)
Initialize self. See help(type(self)) for accurate signature.
```

```
get_n_splits (self, X, y=None, groups=None)
```

Returns the number of splitting iterations in the cross-validator

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [object] Always ignored, exists for compatibility.

groups [object] Always ignored, exists for compatibility.

## **Returns**

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X, y=None, groups=None)
```

Generate indices to split data into training and test set.

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, of length n\_samples] The target variable for supervised learning problems.

**groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set.

## **Yields**

train [ndarray] The training set indices for that split.

**test** [ndarray] The testing set indices for that split.

# sklearn.model\_selection.LeavePOut

```
class sklearn.model_selection.LeavePOut(p)
```

Leave-P-Out cross-validator

Provides train/test indices to split data in train/test sets. This results in testing on all distinct samples of size p, while the remaining n - p samples form the training set in each iteration.

Note: LeavePout (p) is NOT equivalent to KFold(n\_splits=n\_samples // p) which creates non-overlapping test sets.

Due to the high number of iterations which grows combinatorically with the number of samples this cross-validation method can be very costly. For large datasets one should favor <code>KFold</code>, <code>StratifiedKFold</code> or <code>ShuffleSplit</code>.

Read more in the *User Guide*.

### **Parameters**

**p** [int] Size of the test sets. Must be strictly greater than the number of samples.

```
>>> import numpy as np
>>> from sklearn.model_selection import LeavePOut
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> y = np.array([1, 2, 3, 4])
>>> lpo = LeavePOut(2)
>>> lpo.get_n_splits(X)
>>> print(lpo)
LeavePOut (p=2)
>>> for train_index, test_index in lpo.split(X):
     print("TRAIN:", train_index, "TEST:", test_index)
      X_train, X_test = X[train_index], X[test_index]
      y_train, y_test = y[train_index], y[test_index]
TRAIN: [2 3] TEST: [0 1]
TRAIN: [1 3] TEST: [0 2]
TRAIN: [1 2] TEST: [0 3]
TRAIN: [0 3] TEST: [1 2]
```

```
TRAIN: [0 2] TEST: [1 3]
TRAIN: [0 1] TEST: [2 3]
```

<pre>get_n_splits(self, X[, y, groups])</pre>	Returns the number of splitting iterations in the cross-
	validator
split(self, X[, y, groups])	Generate indices to split data into training and test set.

```
___init___(self, p)
```

get\_n\_splits (self, X, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

## **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [object] Always ignored, exists for compatibility.

groups [object] Always ignored, exists for compatibility.

**split** (*self*, *X*, *y=None*, *groups=None*)

Generate indices to split data into training and test set.

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array-like, of length n\_samples] The target variable for supervised learning problems.

**groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set.

# **Yields**

train [ndarray] The training set indices for that split.

test [ndarray] The testing set indices for that split.

# sklearn.model\_selection.PredefinedSplit

class sklearn.model\_selection.PredefinedSplit (test\_fold)

Predefined split cross-validator

Provides train/test indices to split data into train/test sets using a predefined scheme specified by the user with the test\_fold parameter.

Read more in the *User Guide*.

# **Parameters**

**test\_fold** [array-like, shape (n\_samples,)] The entry test\_fold[i] represents the index of the test set that sample i belongs to. It is possible to exclude sample i from any test set (i.e. include sample i in every training set) by setting test\_fold[i] equal to -1.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.model_selection import PredefinedSplit
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> test_fold = [0, 1, -1, 1]
>>> ps = PredefinedSplit(test_fold)
>>> ps.get_n_splits()
2
>>> print(ps)
PredefinedSplit(test_fold=array([ 0,  1, -1,  1]))
>>> for train_index, test_index in ps.split():
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
TRAIN: [1 2 3] TEST: [0]
TRAIN: [0 2] TEST: [1 3]
```

#### Methods

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-
	validator
split(self[, X, y, groups])	Generate indices to split data into training and test set.

```
__init___(self, test_fold)
```

get\_n\_splits (self, X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

### **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.
- groups [object] Always ignored, exists for compatibility.

### Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X=None, y=None, groups=None)
```

Generate indices to split data into training and test set.

## **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.
- groups [object] Always ignored, exists for compatibility.

## **Yields**

train [ndarray] The training set indices for that split.

test [ndarray] The testing set indices for that split.

## sklearn.model\_selection.RepeatedKFold

Repeated K-Fold cross validator.

Repeats K-Fold n times with different randomization in each repetition.

Read more in the User Guide.

#### **Parameters**

- **n\_splits** [int, default=5] Number of folds. Must be at least 2.
- **n\_repeats** [int, default=10] Number of times cross-validator needs to be repeated.

random\_state [int, RandomState instance or None, optional, default=None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

## See also:

RepeatedStratifiedKFold Repeats Stratified K-Fold n times.

## **Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random\_state to an integer.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.model_selection import RepeatedKFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> rkf = RepeatedKFold(n_splits=2, n_repeats=2, random_state=2652124)
>>> for train_index, test_index in rkf.split(X):
        print("TRAIN:", train_index, "TEST:", test_index)
. . .
. . .
        X_train, X_test = X[train_index], X[test_index]
        y_train, y_test = y[train_index], y[test_index]
. . .
TRAIN: [0 1] TEST: [2 3]
TRAIN: [2 3] TEST: [0 1]
TRAIN: [1 2] TEST: [0 3]
TRAIN: [0 3] TEST: [1 2]
```

## **Methods**

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-
	validator
split(self, X[, y, groups])	Generates indices to split data into training and test set.

```
__init__ (self, n_splits=5, n_repeats=10, random_state=None)
```

## get\_n\_splits (self, X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

#### **Parameters**

- X [object] Always ignored, exists for compatibility. np.zeros(n\_samples) may be used as a placeholder.
- y [object] Always ignored, exists for compatibility. np.zeros(n\_samples) may be used as a placeholder.

**groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set.

#### Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X, y=None, groups=None)
```

Generates indices to split data into training and test set.

#### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, of length n\_samples] The target variable for supervised learning problems.
- **groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set.

#### **Yields**

**train** [ndarray] The training set indices for that split.

**test** [ndarray] The testing set indices for that split.

# sklearn.model\_selection.RepeatedStratifiedKFold

Repeated Stratified K-Fold cross validator.

Repeats Stratified K-Fold n times with different randomization in each repetition.

Read more in the User Guide.

## **Parameters**

- **n\_splits** [int, default=5] Number of folds. Must be at least 2.
- **n\_repeats** [int, default=10] Number of times cross-validator needs to be repeated.
- **random\_state** [None, int or RandomState, default=None] Random state to be used to generate random state for each repetition.

## See also:

**RepeatedKFold** Repeats K-Fold n times.

## **Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random\_state to an integer.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.model_selection import RepeatedStratifiedKFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> rskf = RepeatedStratifiedKFold(n_splits=2, n_repeats=2,
       random_state=36851234)
. . .
>>> for train_index, test_index in rskf.split(X, y):
        print("TRAIN:", train_index, "TEST:", test_index)
        X_train, X_test = X[train_index], X[test_index]
. . .
        y_train, y_test = y[train_index], y[test_index]
. . .
. . .
TRAIN: [1 2] TEST: [0 3]
TRAIN: [0 3] TEST: [1 2]
TRAIN: [1 3] TEST: [0 2]
TRAIN: [0 2] TEST: [1 3]
```

#### Methods

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-validator
split(self, X[, y, groups])	Generates indices to split data into training and test set.

```
__init__ (self, n_splits=5, n_repeats=10, random_state=None)
get_n_splits (self, X=None, y=None, groups=None)
```

Returns the number of splitting iterations in the cross-validator

## **Parameters**

- X [object] Always ignored, exists for compatibility. np.zeros(n\_samples) may be used as a placeholder.
- y [object] Always ignored, exists for compatibility. np.zeros(n\_samples) may be used as a placeholder.

**groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set.

# Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X, y=None, groups=None)
```

Generates indices to split data into training and test set.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.

y [array-like, of length n\_samples] The target variable for supervised learning problems.

**groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set.

#### **Yields**

train [ndarray] The training set indices for that split.

**test** [ndarray] The testing set indices for that split.

# sklearn.model\_selection.ShuffleSplit

Random permutation cross-validator

Yields indices to split data into training and test sets.

Note: contrary to other cross-validation strategies, random splits do not guarantee that all folds will be different, although this is still very likely for sizeable datasets.

Read more in the *User Guide*.

## **Parameters**

**n\_splits** [int, default 10] Number of re-shuffling & splitting iterations.

test\_size [float, int, None, default=None] If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is set to the complement of the train size. If train\_size is also None, it will be set to 0.1.

**train\_size** [float, int, or None, default=None] If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the train split. If int, represents the absolute number of train samples. If None, the value is automatically set to the complement of the test size.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

```
>>> import numpy as np
>>> from sklearn.model_selection import ShuffleSplit
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8], [3, 4], [5, 6]])
>>> y = np.array([1, 2, 1, 2, 1, 2])
>>> rs = ShuffleSplit(n_splits=5, test_size=.25, random_state=0)
>>> rs.get_n_splits(X)
5
>>> print(rs)
ShuffleSplit(n_splits=5, random_state=0, test_size=0.25, train_size=None)
>>> for train_index, test_index in rs.split(X):
...     print("TRAIN:", train_index, "TEST:", test_index)
...
TRAIN: [1 3 0 4] TEST: [5 2]
TRAIN: [4 0 2 5] TEST: [1 3]
```

```
TRAIN: [1 2 4 0] TEST: [3 5]
TRAIN: [3 4 1 0] TEST: [5 2]
TRAIN: [3 5 1 0] TEST: [2 4]

>>> rs = ShuffleSplit(n_splits=5, train_size=0.5, test_size=.25,
... random_state=0)

>>> for train_index, test_index in rs.split(X):
... print("TRAIN:", train_index, "TEST:", test_index)

...

TRAIN: [1 3 0] TEST: [5 2]
TRAIN: [4 0 2] TEST: [1 3]
TRAIN: [4 0 2] TEST: [3 5]
TRAIN: [3 4 1] TEST: [5 2]
TRAIN: [3 5 1] TEST: [5 4]
```

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-validator
split(self, X[, y, groups])	Generate indices to split data into training and test set.

```
__init__ (self, n_splits=10, test_size=None, train_size=None, random_state=None)
```

# get\_n\_splits (self, X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

## **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.

groups [object] Always ignored, exists for compatibility.

## Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

## **split** (*self*, *X*, *y=None*, *groups=None*)

Generate indices to split data into training and test set.

# **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape (n\_samples,)] The target variable for supervised learning problems.
- **groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set.

## **Yields**

train [ndarray] The training set indices for that split.

**test** [ndarray] The testing set indices for that split.

## **Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random\_state to an integer.

## Examples using sklearn.model\_selection.ShuffleSplit

- Visualizing cross-validation behavior in scikit-learn
- Plotting Learning Curves
- Scaling the regularization parameter for SVCs

### sklearn.model selection.StratifiedKFold

Stratified K-Folds cross-validator

Provides train/test indices to split data in train/test sets.

This cross-validation object is a variation of KFold that returns stratified folds. The folds are made by preserving the percentage of samples for each class.

Read more in the User Guide.

### **Parameters**

**n\_splits** [int, default=3] Number of folds. Must be at least 2.

Changed in version 0.20: n\_splits default value will change from 3 to 5 in v0.22.

**shuffle** [boolean, optional] Whether to shuffle each class's samples before splitting into batches.

random\_state [int, RandomState instance or None, optional, default=None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when shuffle == True.

### See also:

RepeatedStratifiedKFold Repeats Stratified K-Fold n times.

## **Notes**

Train and test sizes may be different in each fold, with a difference of at most n\_classes.

```
>>> import numpy as np
>>> from sklearn.model_selection import StratifiedKFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> skf = StratifiedKFold(n_splits=2)
>>> skf.get_n_splits(X, y)
2
```

```
>>> print(skf)
StratifiedKFold(n_splits=2, random_state=None, shuffle=False)
>>> for train_index, test_index in skf.split(X, y):
... print("TRAIN:", train_index, "TEST:", test_index)
... X_train, X_test = X[train_index], X[test_index]
... y_train, y_test = y[train_index], y[test_index]
TRAIN: [1 3] TEST: [0 2]
TRAIN: [0 2] TEST: [1 3]
```

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-validator
split(self, X, y[, groups])	Generate indices to split data into training and test set.

```
___init___(self, n_splits='warn', shuffle=False, random_state=None)
```

# get\_n\_splits (self, X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

### **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.
- groups [object] Always ignored, exists for compatibility.

# Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

# split (self, X, y, groups=None)

Generate indices to split data into training and test set.

# **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.

Note that providing y is sufficient to generate the splits and hence np. zeros (n\_samples) may be used as a placeholder for X instead of actual training data.

y [array-like, shape (n\_samples,)] The target variable for supervised learning problems. Stratification is done based on the y labels.

groups [object] Always ignored, exists for compatibility.

## **Yields**

train [ndarray] The training set indices for that split.

test [ndarray] The testing set indices for that split.

## **Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random\_state to an integer.

# Examples using sklearn.model\_selection.StratifiedKFold

- Recursive feature elimination with cross-validation
- Test with permutations the significance of a classification score
- GMM covariances
- Receiver Operating Characteristic (ROC) with cross validation
- Visualizing cross-validation behavior in scikit-learn

# sklearn.model\_selection.StratifiedShuffleSplit

Stratified ShuffleSplit cross-validator

Provides train/test indices to split data in train/test sets.

This cross-validation object is a merge of StratifiedKFold and ShuffleSplit, which returns stratified randomized folds. The folds are made by preserving the percentage of samples for each class.

Note: like the ShuffleSplit strategy, stratified random splits do not guarantee that all folds will be different, although this is still very likely for sizeable datasets.

Read more in the User Guide.

#### **Parameters**

**n\_splits** [int, default 10] Number of re-shuffling & splitting iterations.

test\_size [float, int, None, optional (default=None)] If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is set to the complement of the train size. If train\_size is also None, it will be set to 0.1.

**train\_size** [float, int, or None, default is None] If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the train split. If int, represents the absolute number of train samples. If None, the value is automatically set to the complement of the test size.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

```
>>> import numpy as np
>>> from sklearn.model_selection import StratifiedShuffleSplit
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 0, 1, 1, 1])
>>> sss = StratifiedShuffleSplit(n_splits=5, test_size=0.5, random_state=0)
>>> sss.get_n_splits(X, y)
5
>>> print(sss)
StratifiedShuffleSplit(n_splits=5, random_state=0, ...)
```

```
>>> for train_index, test_index in sss.split(X, y):
...    print("TRAIN:", train_index, "TEST:", test_index)
...    X_train, X_test = X[train_index], X[test_index]
...    y_train, y_test = y[train_index], y[test_index]
TRAIN: [5 2 3] TEST: [4 1 0]
TRAIN: [5 1 4] TEST: [0 2 3]
TRAIN: [5 0 2] TEST: [4 3 1]
TRAIN: [4 1 0] TEST: [2 3 5]
TRAIN: [0 5 1] TEST: [3 4 2]
```

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-validator
split(self, X, y[, groups])	Generate indices to split data into training and test set.

```
___init__ (self, n_splits=10, test_size=None, train_size=None, random_state=None)
```

# get\_n\_splits (self, X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

## **Parameters**

- **X** [object] Always ignored, exists for compatibility.
- y [object] Always ignored, exists for compatibility.

groups [object] Always ignored, exists for compatibility.

# Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

```
split (self, X, y, groups=None)
```

Generate indices to split data into training and test set.

# **Parameters**

X [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.

Note that providing y is sufficient to generate the splits and hence np. zeros (n\_samples) may be used as a placeholder for X instead of actual training data.

**y** [array-like, shape (n\_samples,)] The target variable for supervised learning problems. Stratification is done based on the y labels.

groups [object] Always ignored, exists for compatibility.

#### **Yields**

**train** [ndarray] The training set indices for that split.

test [ndarray] The testing set indices for that split.

# **Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random\_state to an integer.

## Examples using sklearn.model\_selection.StratifiedShuffleSplit

- Visualizing cross-validation behavior in scikit-learn
- RBF SVM parameters

# sklearn.model\_selection.TimeSeriesSplit

```
class sklearn.model_selection.TimeSeriesSplit (n_splits='warn', max_train_size=None)
    Time Series cross-validator
```

Provides train/test indices to split time series data samples that are observed at fixed time intervals, in train/test sets. In each split, test indices must be higher than before, and thus shuffling in cross validator is inappropriate.

This cross-validation object is a variation of KFold. In the kth split, it returns first k folds as train set and the (k+1)th fold as test set.

Note that unlike standard cross-validation methods, successive training sets are supersets of those that come before them.

Read more in the *User Guide*.

# **Parameters**

```
n_splits [int, default=3] Number of splits. Must be at least 2.
```

Changed in version 0.20: n\_splits default value will change from 3 to 5 in v0.22.

max\_train\_size [int, optional] Maximum size for a single training set.

#### **Notes**

The training set has size i  $\star$  n\_samples // (n\_splits + 1) + n\_samples % (n\_splits + 1) in the i`th split, with a test set of size ``n\_samples//(n\_splits + 1), where n\_samples is the number of samples.

```
>>> import numpy as np
>>> from sklearn.model_selection import TimeSeriesSplit
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([1, 2, 3, 4, 5, 6])
>>> tscv = TimeSeriesSplit(n_splits=5)
>>> print(tscv)
TimeSeriesSplit(max_train_size=None, n_splits=5)
>>> for train_index, test_index in tscv.split(X):
       print("TRAIN:", train_index, "TEST:", test_index)
       X_train, X_test = X[train_index], X[test_index]
      y_train, y_test = y[train_index], y[test_index]
. . .
TRAIN: [0] TEST: [1]
TRAIN: [0 1] TEST: [2]
TRAIN: [0 1 2] TEST: [3]
TRAIN: [0 1 2 3] TEST: [4]
TRAIN: [0 1 2 3 4] TEST: [5]
```

<pre>get_n_splits(self[, X, y, groups])</pre>	Returns the number of splitting iterations in the cross-validator
split(self, X[, y, groups])	Generate indices to split data into training and test set.

```
___init___(self, n_splits='warn', max_train_size=None)
```

get\_n\_splits (self, X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

## **Parameters**

**X** [object] Always ignored, exists for compatibility.

y [object] Always ignored, exists for compatibility.

groups [object] Always ignored, exists for compatibility.

# Returns

**n\_splits** [int] Returns the number of splitting iterations in the cross-validator.

split (self, X, y=None, groups=None)

Generate indices to split data into training and test set.

# **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training data, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape (n\_samples,)] Always ignored, exists for compatibility.

**groups** [array-like, with shape (n\_samples,)] Always ignored, exists for compatibility.

# **Yields**

train [ndarray] The training set indices for that split.

**test** [ndarray] The testing set indices for that split.

## Examples using sklearn.model\_selection.TimeSeriesSplit

• Visualizing cross-validation behavior in scikit-learn

# 6.26.2 Splitter Functions

<pre>model_selection.check_cv([cv, y, classifier])</pre>	Input checker utility for building a cross-validator		
<pre>model_selection.train_test_split(\*arrays,</pre>	Split arrays or matrices into random train and test subsets		
)			

# sklearn.model selection.check cv

sklearn.model\_selection.check\_cv (cv='warn', y=None, classifier=False)
Input checker utility for building a cross-validator

## **Parameters**

- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross-validation,
  - integer, to specify the number of folds.
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if classifier is True and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value will change from 3-fold to 5-fold in v0.22.

 $\mathbf{y}$  [array-like, optional] The target variable for supervised learning problems.

**classifier** [boolean, optional, default False] Whether the task is a classification task, in which case stratified KFold will be used.

#### Returns

**checked\_cv** [a cross-validator instance.] The return value is a cross-validator which generates the train/test splits via the split method.

## sklearn.model\_selection.train\_test\_split

```
sklearn.model_selection.train_test_split(*arrays, **options)
```

Split arrays or matrices into random train and test subsets

Quick utility that wraps input validation and next (ShuffleSplit().split(X, y)) and application to input data into a single call for splitting (and optionally subsampling) data in a oneliner.

Read more in the User Guide.

# **Parameters**

- \*arrays [sequence of indexables with same length / shape[0]] Allowed inputs are lists, numpy arrays, scipy-sparse matrices or pandas dataframes.
- **test\_size** [float, int or None, optional (default=None)] If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is set to the complement of the train size. If train size is also None, it will be set to 0.25.
- **train\_size** [float, int, or None, (default=None)] If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the train split. If int, represents the absolute number of train samples. If None, the value is automatically set to the complement of the test size.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- **shuffle** [boolean, optional (default=True)] Whether or not to shuffle the data before splitting. If shuffle=False then stratify must be None.
- **stratify** [array-like or None (default=None)] If not None, data is split in a stratified fashion, using this as the class labels.

## Returns

```
splitting [list, length=2 * len(arrays)] List containing train-test split of inputs.
```

New in version 0.16: If the input is sparse, the output will be a scipy.sparse.csr\_matrix. Else, output type is the same as the input type.

# **Examples**

```
>>> train_test_split(y, shuffle=False)
[[0, 1, 2], [3, 4]]
```

# Examples using sklearn.model\_selection.train\_test\_split

- Faces recognition example using eigenfaces and SVMs
- Prediction Latency
- Probability Calibration curves
- Probability calibration of classifiers
- Classifier comparison
- Column Transformer with Mixed Types
- Effect of transforming the targets in regression model
- Comparing random forests and the multi-output meta estimator
- Early stopping of Gradient Boosting

- Feature transformations with ensembles of trees
- Gradient Boosting Out-of-Bag estimates
- Pipeline Anova SVM
- Comparing various online solvers
- MNIST classfification using multinomial logistic + L1
- Multiclass sparse logisitic regression on newgroups20
- Early stopping of Stochastic Gradient Descent
- Parameter estimation using grid search with cross-validation
- Confusion matrix
- Receiver Operating Characteristic (ROC)
- Precision-Recall
- Classifier Chain
- Comparing Nearest Neighbors with and without Neighborhood Components Analysis
- Dimensionality Reduction with Neighborhood Components Analysis
- Restricted Boltzmann Machine features for digit classification
- Varying regularization in Multi-layer Perceptron
- Using FunctionTransformer to select columns
- Importance of Feature Scaling
- Map data to a normal distribution
- Feature discretization
- Understanding the decision tree structure

# 6.26.3 Hyper-parameter optimizers

model_selection.GridSearchCV(estimator,)	Exhaustive search over specified parameter values for an
	estimator.
model_selection.ParameterGrid(param_grid)	Grid of parameters with a discrete number of values for
	each.
$model\_selection.ParameterSampler([,])$	Generator on parameters sampled from given distributions.
model_selection.RandomizedSearchCV([,	Randomized search on hyper parameters.
])	

# sklearn.model selection.GridSearchCV

```
class sklearn.model_selection.GridSearchCV (estimator, param_grid, scoring=None, n\_jobs=None, iid='warn', refit=True, cv='warn', verbose=0, pre\_dispatch='2*n\_jobs', error\_score='raise-deprecating', return\_train\_score=False)
```

Exhaustive search over specified parameter values for an estimator.

Important members are fit, predict.

GridSearchCV implements a "fit" and a "score" method. It also implements "predict", "predict\_proba", "decision\_function", "transform" and "inverse\_transform" if they are implemented in the estimator used.

The parameters of the estimator used to apply these methods are optimized by cross-validated grid-search over a parameter grid.

Read more in the User Guide.

#### **Parameters**

- **estimator** [estimator object.] This is assumed to implement the scikit-learn estimator interface. Either estimator needs to provide a score function, or scoring must be passed.
- param\_grid [dict or list of dictionaries] Dictionary with parameters names (string) as keys and lists of parameter settings to try as values, or a list of such dictionaries, in which case the grids spanned by each dictionary in the list are explored. This enables searching over any sequence of parameter settings.
- **scoring** [string, callable, list/tuple, dict or None, default: None] A single string (see *The scoring parameter: defining model evaluation rules*) or a callable (see *Defining your scoring strategy from metric functions*) to evaluate the predictions on the test set.

For evaluating multiple metrics, either give a list of (unique) strings or a dict with names as keys and callables as values.

NOTE that when using custom scorers, each scorer should return a single value. Metric functions returning a list/array of values can be wrapped into multiple scorers that return one value each.

See Specifying multiple metrics for evaluation for an example.

If None, the estimator's score method is used.

- n\_jobs [int or None, optional (default=None)] Number of jobs to run in parallel. None means 1
   unless in a joblib.parallel\_backend context. -1 means using all processors. See
   Glossary for more details.
- **pre\_dispatch** [int, or string, optional] Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:
  - None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
  - An int, giving the exact number of total jobs that are spawned
  - A string, giving an expression as a function of n jobs, as in '2\*n jobs'
- **iid** [boolean, default='warn'] If True, return the average score across folds, weighted by the number of samples in each test set. In this case, the data is assumed to be identically distributed across the folds, and the loss minimized is the total loss per sample, and not the mean loss across the folds. If False, return the average score across folds. Default is True, but will change to False in version 0.22, to correspond to the standard definition of cross-validation.

Changed in version 0.20: Parameter iid will change from True to False by default in version 0.22, and will be removed in 0.24.

- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross validation,

- integer, to specify the number of folds in a (Stratified) KFold,
- CV splitter,
- An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

**refit** [boolean, string, or callable, default=True] Refit an estimator using the best found parameters on the whole dataset.

For multiple metric evaluation, this needs to be a string denoting the scorer that would be used to find the best parameters for refitting the estimator at the end.

Where there are considerations other than maximum score in choosing a best estimator, refit can be set to a function which returns the selected best\_index\_ given cv\_results\_.

The refitted estimator is made available at the best\_estimator\_ attribute and permits using predict directly on this GridSearchCV instance.

Also for multiple metric evaluation, the attributes best\_index\_, best\_score\_ and best\_params\_ will only be available if refit is set and all of them will be determined w.r.t this specific scorer. best\_score\_ is not returned if refit is callable.

See scoring parameter to know more about multiple metric evaluation.

Changed in version 0.20: Support for callable added.

**verbose** [integer] Controls the verbosity: the higher, the more messages.

**error\_score** ['raise' or numeric] Value to assign to the score if an error occurs in estimator fitting. If set to 'raise', the error is raised. If a numeric value is given, FitFailedWarning is raised. This parameter does not affect the refit step, which will always raise the error. Default is 'raise' but from version 0.22 it will change to np.nan.

**return\_train\_score** [boolean, default=False] If False, the cv\_results\_ attribute will not include training scores. Computing training scores is used to get insights on how different parameter settings impact the overfitting/underfitting trade-off. However computing the scores on the training set can be computationally expensive and is not strictly required to select the parameters that yield the best generalization performance.

## **Attributes**

**cv\_results**\_ [dict of numpy (masked) ndarrays] A dict with keys as column headers and values as columns, that can be imported into a pandas DataFrame.

For instance the below given table

param_kernel	param_gamma	param_degree	split0_test_score	 rank_t
'poly'	_	2	0.80	 2
'poly'	_	3	0.70	 4
'rbf'	0.1	_	0.80	 3
'rbf'	0.2	_	0.93	 1

will be represented by a cv\_results\_dict of:

```
'param_kernel': masked_array(data = ['poly', 'poly', 'rbf', 'rbf'],
                            mask = [False False False]...)
'param_gamma': masked_array(data = [-- -- 0.1 0.2],
                           mask = [ True True False False]...),
'param_degree': masked_array(data = [2.0 3.0 -- --],
                            mask = [False False True True]...),
'split0_test_score' : [0.80, 0.70, 0.80, 0.93],
'split1_test_score' : [0.82, 0.50, 0.70, 0.78],
'mean_test_score' : [0.81, 0.60, 0.75, 0.85],
'std_test_score'
                   : [0.01, 0.10, 0.05, 0.08],
'rank_test_score' : [2, 4, 3, 1],
'split0_train_score' : [0.80, 0.92, 0.70, 0.93],
'split1_train_score' : [0.82, 0.55, 0.70, 0.87],
                   : [0.81, 0.74, 0.70, 0.90],
'mean_train_score'
'std_train_score' : [0.01, 0.19, 0.00, 0.03],
'mean_fit_time'
'std_fit_time'
                   : [0.73, 0.63, 0.43, 0.49],
                   : [0.01, 0.02, 0.01, 0.01],
'mean_score_time' : [0.01, 0.06, 0.04, 0.04],
'std_score_time'
                   : [0.00, 0.00, 0.00, 0.01],
'params'
                   : [{'kernel': 'poly', 'degree': 2}, ...],
```

#### NOTE

The key 'params' is used to store a list of parameter settings dicts for all the parameter candidates.

The mean\_fit\_time, std\_fit\_time, mean\_score\_time and std\_score\_time are all in seconds.

For multi-metric evaluation, the scores for all the scorers are available in the cv\_results\_ dict at the keys ending with that scorer's name ('\_<scorer\_name>') instead of '\_score' shown above. ('split0\_test\_precision', 'mean\_train\_precision' etc.)

best\_estimator\_ [estimator or dict] Estimator that was chosen by the search, i.e. estimator
which gave highest score (or smallest loss if specified) on the left out data. Not available if
refit=False.

See refit parameter for more information on allowed values.

**best score** [float] Mean cross-validated score of the best estimator

For multi-metric evaluation, this is present only if refit is specified.

**best\_params\_** [dict] Parameter setting that gave the best results on the hold out data.

For multi-metric evaluation, this is present only if refit is specified.

**best\_index**\_ [int] The index (of the cv\_results\_ arrays) which corresponds to the best candidate parameter setting.

The dict at search.cv\_results\_['params'][search.best\_index\_] gives the parameter setting for the best model, that gives the highest mean score (search.best\_score\_).

For multi-metric evaluation, this is present only if refit is specified.

**scorer**\_ [function or a dict] Scorer function used on the held out data to choose the best parameters for the model.

For multi-metric evaluation, this attribute holds the validated scoring dict which maps the scorer key to the scorer callable.

**n\_splits\_** [int] The number of cross-validation splits (folds/iterations).

refit\_time\_ [float] Seconds used for refitting the best model on the whole dataset.

This is present only if refit is not False.

#### See also:

**ParameterGrid** generates all the combinations of a hyperparameter grid.

**sklearn.model\_selection.train\_test\_split** utility function to split the data into a development set usable for fitting a GridSearchCV instance and an evaluation set for its final evaluation.

sklearn.metrics.make\_scorer Make a scorer from a performance metric or loss function.

## **Notes**

The parameters selected are those that maximize the score of the left out data, unless an explicit score is passed in which case it is used instead.

If  $n\_jobs$  was set to a value higher than one, the data is copied for each point in the grid (and not  $n\_jobs$  times). This is done for efficiency reasons if individual jobs take very little time, but may raise errors if the dataset is large and not enough memory is available. A workaround in this case is to set pre\_dispatch. Then, the memory is copied only pre\_dispatch many times. A reasonable value for pre\_dispatch is 2 \* n\_jobs.

```
>>> from sklearn import svm, datasets
>>> from sklearn.model_selection import GridSearchCV
>>> iris = datasets.load_iris()
>>> parameters = {'kernel':('linear', 'rbf'), 'C':[1, 10]}
>>> svc = svm.SVC(gamma="scale")
>>> clf = GridSearchCV(svc, parameters, cv=5)
>>> clf.fit(iris.data, iris.target)
GridSearchCV(cv=5, error_score=...,
       estimator=SVC(C=1.0, cache_size=..., class_weight=..., coef0=...,
                     decision_function_shape='ovr', degree=..., gamma=...,
                     kernel='rbf', max_iter=-1, probability=False,
                     random_state=None, shrinking=True, tol=...,
                     verbose=False),
       iid=..., n_jobs=None,
      param_grid=..., pre_dispatch=..., refit=..., return_train_score=...,
      scoring=..., verbose=...)
>>> sorted(clf.cv_results_.keys())
['mean_fit_time', 'mean_score_time', 'mean_test_score',...
 'param_C', 'param_kernel', 'params',...
 'rank_test_score', 'split0_test_score',...
 'split2_test_score', ...
 'std_fit_time', 'std_score_time', 'std_test_score']
```

decision_function(self, X)	Call decision_function on the estimator with the best		
_ , , ,	found parameters.		
fit(self, X[, y, groups])	Run fit with all sets of parameters.		
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.		
inverse_transform(self, Xt)	Call inverse_transform on the estimator with the best		
	found params.		
predict(self, X)	Call predict on the estimator with the best found param-		
	eters.		
predict_log_proba(self, X)	Call predict_log_proba on the estimator with the best		
	found parameters.		
predict_proba(self, X)	Call predict_proba on the estimator with the best found		
	parameters.		
score(self, X[, y])	Returns the score on the given data, if the estimator has		
	been refit.		
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.		
transform(self, X)	Call transform on the estimator with the best found pa-		
	rameters.		

\_\_init\_\_(self, estimator, param\_grid, scoring=None, n\_jobs=None, iid='warn', refit=True, cv='warn', verbose=0, pre\_dispatch='2\*n\_jobs', error\_score='raise-deprecating', return\_train\_score=False)

## $decision\_function(self, X)$

Call decision\_function on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports decision\_function.

## **Parameters**

X [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

**fit** (*self*, *X*, *y=None*, *groups=None*, \*\**fit\_params*) Run fit with all sets of parameters.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vector, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array-like, shape = [n\_samples] or [n\_samples, n\_output], optional] Target relative to X for classification or regression; None for unsupervised learning.
- **groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set. Only used in conjunction with a "Group" *cv* instance (e.g., *GroupKFold*).
- \*\*fit\_params [dict of string -> object] Parameters passed to the fit method of the estimator

# get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# inverse\_transform(self, Xt)

Call inverse\_transform on the estimator with the best found params.

Only available if the underlying estimator implements inverse\_transform and refit=True.

#### **Parameters**

**Xt** [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

## predict (self, X)

Call predict on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports predict.

## **Parameters**

X [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator

## predict\_log\_proba (self, X)

Call predict\_log\_proba on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports predict\_log\_proba.

#### **Parameters**

**X** [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

# predict\_proba (self, X)

Call predict\_proba on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports predict\_proba.

## **Parameters**

X [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

# score(self, X, y=None)

Returns the score on the given data, if the estimator has been refit.

This uses the score defined by scoring where provided, and the best\_estimator\_.score method otherwise.

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Input data, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array-like, shape = [n\_samples] or [n\_samples, n\_output], optional] Target relative to X for classification or regression; None for unsupervised learning.

## **Returns**

score [float]

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

## transform(self, X)

Call transform on the estimator with the best found parameters.

Only available if the underlying estimator supports transform and refit=True.

## **Parameters**

X [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

# Examples using sklearn.model\_selection.GridSearchCV

- Comparison of kernel ridge regression and SVR
- Faces recognition example using eigenfaces and SVMs
- Feature agglomeration vs. univariate selection
- Concatenating multiple feature extraction methods
- Pipelining: chaining a PCA and a logistic regression
- Column Transformer with Mixed Types
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood
- Model selection with Probabilistic PCA and Factor Analysis (FA)
- Cross-validation on diabetes Dataset Exercise
- Comparison of kernel ridge and Gaussian process regression
- Parameter estimation using grid search with cross-validation
- Comparing randomized search and grid search for hyperparameter estimation
- Nested versus non-nested cross-validation
- Demonstration of multi-metric evaluation on cross\_val\_score and GridSearchCV
- Balance model complexity and cross-validated score
- Sample pipeline for text feature extraction and evaluation
- Kernel Density Estimation
- Feature discretization
- Scaling the regularization parameter for SVCs
- RBF SVM parameters

### sklearn.model selection.ParameterGrid

```
class sklearn.model_selection.ParameterGrid (param_grid)
```

Grid of parameters with a discrete number of values for each.

Can be used to iterate over parameter value combinations with the Python built-in function iter.

Read more in the User Guide.

#### **Parameters**

**param\_grid** [dict of string to sequence, or sequence of such] The parameter grid to explore, as a dictionary mapping estimator parameters to sequences of allowed values.

An empty dict signifies default parameters.

A sequence of dicts signifies a sequence of grids to search, and is useful to avoid exploring parameter combinations that make no sense or have no effect. See the examples below.

## See also:

*GridSearchCV* Uses *ParameterGrid* to perform a full parallelized parameter search.

# **Examples**

```
>>> from sklearn.model_selection import ParameterGrid
>>> param_grid = {'a': [1, 2], 'b': [True, False]}
>>> list(ParameterGrid(param_grid)) == (
...    [{'a': 1, 'b': True}, {'a': 1, 'b': False},
...    {'a': 2, 'b': True}, {'a': 2, 'b': False}])
True
```

\_\_init\_\_ (self, param\_grid)

## sklearn.model selection.ParameterSampler

Generator on parameters sampled from given distributions.

Non-deterministic iterable over random candidate combinations for hyper- parameter search. If all parameters are presented as a list, sampling without replacement is performed. If at least one parameter is given as a distribution, sampling with replacement is used. It is highly recommended to use continuous distributions for continuous parameters.

Note that before SciPy 0.16, the scipy.stats.distributions do not accept a custom RNG instance and always use the singleton RNG from numpy.random. Hence setting random\_state will not guarantee a deterministic iteration whenever scipy.stats distributions are used to define the parameter search space. Deterministic behavior is however guaranteed from SciPy 0.16 onwards.

Read more in the User Guide.

#### **Parameters**

**param\_distributions** [dict] Dictionary where the keys are parameters and values are distributions from which a parameter is to be sampled. Distributions either have to provide a rvs function to sample from them, or can be given as a list of values, where a uniform distribution is assumed.

**n iter** [integer] Number of parameter settings that are produced.

random\_state [int, RandomState instance or None, optional (default=None)] Pseudo random number generator state used for random uniform sampling from lists of possible values instead of scipy.stats distributions. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

## Returns

**params** [dict of string to any] **Yields** dictionaries mapping each estimator parameter to as sampled value.

# **Examples**

```
>>> from sklearn.model_selection import ParameterSampler
>>> from scipy.stats.distributions import expon
>>> import numpy as np
>>> rng = np.random.RandomState(0)
>>> param_grid = {'a':[1, 2], 'b': expon()}
>>> param_list = list(ParameterSampler(param_grid, n_iter=4,
                                        random_state=rng))
>>> rounded_list = [dict((k, round(v, 6)) for (k, v) in d.items())
                    for d in param_list]
>>> rounded_list == [{'b': 0.89856, 'a': 1},
                     {'b': 0.923223, 'a': 1},
. . .
                     {'b': 1.878964, 'a': 2},
. . .
                      {'b': 1.038159, 'a': 2}]
. . .
True
```

**\_\_\_init\_\_** (*self*, *param\_distributions*, *n\_iter*, *random\_state=None*)

# sklearn.model selection.RandomizedSearchCV

Randomized search on hyper parameters.

RandomizedSearchCV implements a "fit" and a "score" method. It also implements "predict", "predict\_proba", "decision\_function", "transform" and "inverse\_transform" if they are implemented in the estimator used.

The parameters of the estimator used to apply these methods are optimized by cross-validated search over parameter settings.

In contrast to GridSearchCV, not all parameter values are tried out, but rather a fixed number of parameter settings is sampled from the specified distributions. The number of parameter settings that are tried is given by n\_iter.

If all parameters are presented as a list, sampling without replacement is performed. If at least one parameter is given as a distribution, sampling with replacement is used. It is highly recommended to use continuous distributions for continuous parameters.

Note that before SciPy 0.16, the scipy.stats.distributions do not accept a custom RNG instance and always use the singleton RNG from numpy.random. Hence setting random\_state will not guarantee a deterministic iteration whenever scipy.stats distributions are used to define the parameter search space.

Read more in the *User Guide*.

## **Parameters**

**estimator** [estimator object.] A object of that type is instantiated for each grid point. This is assumed to implement the scikit-learn estimator interface. Either estimator needs to provide a score function, or scoring must be passed.

**param\_distributions** [dict] Dictionary with parameters names (string) as keys and distributions or lists of parameters to try. Distributions must provide a rvs method for sampling (such as those from scipy.stats.distributions). If a list is given, it is sampled uniformly.

**n\_iter** [int, default=10] Number of parameter settings that are sampled. n\_iter trades off runtime vs quality of the solution.

**scoring** [string, callable, list/tuple, dict or None, default: None] A single string (see *The scoring parameter: defining model evaluation rules*) or a callable (see *Defining your scoring strategy from metric functions*) to evaluate the predictions on the test set.

For evaluating multiple metrics, either give a list of (unique) strings or a dict with names as keys and callables as values.

NOTE that when using custom scorers, each scorer should return a single value. Metric functions returning a list/array of values can be wrapped into multiple scorers that return one value each.

See Specifying multiple metrics for evaluation for an example.

If None, the estimator's score method is used.

- **n\_jobs** [int or None, optional (default=None)] Number of jobs to run in parallel. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- **pre\_dispatch** [int, or string, optional] Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:
  - None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
  - An int, giving the exact number of total jobs that are spawned
  - A string, giving an expression as a function of n\_jobs, as in '2\*n\_jobs'

iid [boolean, default='warn'] If True, return the average score across folds, weighted by the number of samples in each test set. In this case, the data is assumed to be identically distributed across the folds, and the loss minimized is the total loss per sample, and not the mean loss across the folds. If False, return the average score across folds. Default is True, but will change to False in version 0.22, to correspond to the standard definition of cross-validation.

Changed in version 0.20: Parameter iid will change from True to False by default in version 0.22, and will be removed in 0.24.

- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross validation,
  - integer, to specify the number of folds in a (Stratified) KFold,
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, *StratifiedKFold* is used. In all other cases, *KFold* is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

**refit** [boolean, string, or callable, default=True] Refit an estimator using the best found parameters on the whole dataset.

For multiple metric evaluation, this needs to be a string denoting the scorer that would be used to find the best parameters for refitting the estimator at the end.

Where there are considerations other than maximum score in choosing a best estimator, refit can be set to a function which returns the selected best\_index\_ given the cv\_results.

The refitted estimator is made available at the best\_estimator\_ attribute and permits using predict directly on this RandomizedSearchCV instance.

Also for multiple metric evaluation, the attributes best\_index\_, best\_score\_ and best\_params\_ will only be available if refit is set and all of them will be determined w.r.t this specific score. When refit is callable, best\_score\_ is disabled.

See scoring parameter to know more about multiple metric evaluation.

Changed in version 0.20: Support for callable added.

**verbose** [integer] Controls the verbosity: the higher, the more messages.

random\_state [int, RandomState instance or None, optional, default=None] Pseudo random number generator state used for random uniform sampling from lists of possible values instead of scipy.stats distributions. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**error\_score** ['raise' or numeric] Value to assign to the score if an error occurs in estimator fitting. If set to 'raise', the error is raised. If a numeric value is given, FitFailedWarning is raised. This parameter does not affect the refit step, which will always raise the error. Default is 'raise' but from version 0.22 it will change to np.nan.

**return\_train\_score** [boolean, default=False] If False, the cv\_results\_ attribute will not include training scores. Computing training scores is used to get insights on how different parameter settings impact the overfitting/underfitting trade-off. However computing the scores on the training set can be computationally expensive and is not strictly required to select the parameters that yield the best generalization performance.

## **Attributes**

**cv\_results\_** [dict of numpy (masked) ndarrays] A dict with keys as column headers and values as columns, that can be imported into a pandas DataFrame.

For instance the below given table

param_kernel	param_gamma	split0_test_score	 rank_test_score
'rbf'	0.1	0.80	 2
'rbf'	0.2	0.90	 1
'rbf'	0.3	0.70	 1

will be represented by a cv\_results\_dict of:

## NOTE

The key 'params' is used to store a list of parameter settings dicts for all the parameter candidates.

```
The mean_fit_time, std_fit_time, mean_score_time and std score time are all in seconds.
```

For multi-metric evaluation, the scores for all the scorers are available in the cv\_results\_ dict at the keys ending with that scorer's name ('\_<scorer\_name>') instead of '\_score' shown above. ('split0\_test\_precision', 'mean\_train\_precision' etc.)

**best\_estimator\_** [estimator or dict] Estimator that was chosen by the search, i.e. estimator which gave highest score (or smallest loss if specified) on the left out data. Not available if refit=False.

For multi-metric evaluation, this attribute is present only if refit is specified.

See refit parameter for more information on allowed values.

**best score** [float] Mean cross-validated score of the best estimator.

For multi-metric evaluation, this is not available if refit is False. See refit parameter for more information.

best\_params\_ [dict] Parameter setting that gave the best results on the hold out data.

For multi-metric evaluation, this is not available if refit is False. See refit parameter for more information.

**best\_index**\_ [int] The index (of the cv\_results\_ arrays) which corresponds to the best candidate parameter setting.

The dict at search.cv\_results\_['params'][search.best\_index\_] gives the parameter setting for the best model, that gives the highest mean score (search.best\_score\_).

For multi-metric evaluation, this is not available if refit is False. See refit parameter for more information.

**scorer**\_ [function or a dict] Scorer function used on the held out data to choose the best parameters for the model.

For multi-metric evaluation, this attribute holds the validated scoring dict which maps the scorer key to the scorer callable.

**n\_splits\_** [int] The number of cross-validation splits (folds/iterations).

refit\_time\_ [float] Seconds used for refitting the best model on the whole dataset.

This is present only if refit is not False.

#### See also:

**GridSearchCV** Does exhaustive search over a grid of parameters.

ParameterSampler A generator over parameter settings, constructed from param\_distributions.

## **Notes**

The parameters selected are those that maximize the score of the held-out data, according to the scoring parameter.

If  $n\_jobs$  was set to a value higher than one, the data is copied for each parameter setting(and not  $n\_jobs$  times). This is done for efficiency reasons if individual jobs take very little time, but may raise errors if the dataset is large and not enough memory is available. A workaround in this case is to set pre\_dispatch. Then, the memory is copied only pre\_dispatch many times. A reasonable value for pre\_dispatch is 2 \* n\_jobs.

## **Methods**

found parameters.  fit(self, X[, y, groups])  get_params(self[, deep])  inverse_transform(self, Xt)  found parameters.  Run fit with all sets of parameters.  Get parameters for this estimator.  Call inverse_transform on the estimator with the found params.	decision_function(self, X)	Call decision_function on the estimator with the best
get_params(self[, deep])Get parameters for this estimator.inverse_transform(self, Xt)Call inverse_transform on the estimator with the		found parameters.
inverse_transform (self, Xt) Call inverse_transform on the estimator with the	fit(self, X[, y, groups])	Run fit with all sets of parameters.
	<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
found params.	inverse_transform(self, Xt)	Call inverse_transform on the estimator with the best
1		found params.

Continued on next page

Table 6.206 –	continued	from	previous page
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predict(self, X)Call predict on the estimator with the best found parameters.predict_log_proba(self, X)Call predict_log_proba on the estimator with the best found parameters.predict_proba(self, X)Call predict_proba on the estimator with the best found parameters.score(self, X[, y])Returns the score on the given data, if the estimator has been refit.set_params(self, \*\*params)Set the parameters of this estimator.transform(self, X)Call transform on the estimator with the best found parameters.		, , ,
predict_log_proba(self, X)Call predict_log_proba on the estimator with the best found parameters.predict_proba(self, X)Call predict_proba on the estimator with the best found parameters.score(self, X[, y])Returns the score on the given data, if the estimator has been refit.set_params(self, \*\*params)Set the parameters of this estimator.transform(self, X)Call transform on the estimator with the best found pa-	predict(self, X)	Call predict on the estimator with the best found param-
found parameters.  predict_proba(self, X)  Call predict_proba on the estimator with the best found parameters.  score(self, X[, y])  Returns the score on the given data, if the estimator has been refit.  set_params(self, \*\*params)  Set the parameters of this estimator.  transform(self, X)  Call transform on the estimator with the best found pa-		eters.
predict_proba(self, X)       Call predict_proba on the estimator with the best found parameters.         score(self, X[, y])       Returns the score on the given data, if the estimator has been refit.         set_params(self, \*\*params)       Set the parameters of this estimator.         transform(self, X)       Call transform on the estimator with the best found pa-	predict_log_proba(self, X)	Call predict_log_proba on the estimator with the best
parameters.  score(self, X[, y])  Returns the score on the given data, if the estimator has been refit.  set_params(self, \*\*params)  Set the parameters of this estimator.  transform(self, X)  Call transform on the estimator with the best found pa-		found parameters.
score(self, X[, y])       Returns the score on the given data, if the estimator has been refit.         set_params(self, \*\*params)       Set the parameters of this estimator.         transform(self, X)       Call transform on the estimator with the best found pa-	predict_proba(self, X)	Call predict_proba on the estimator with the best found
been refit.  set_params(self, \*\*params)  Set the parameters of this estimator.  transform(self, X)  Call transform on the estimator with the best found pa-		parameters.
set_params(self, \*\*params)Set the parameters of this estimator.transform(self, X)Call transform on the estimator with the best found pa-	score(self, X[, y])	Returns the score on the given data, if the estimator has
transform(self, X) Call transform on the estimator with the best found pa-		been refit.
•	<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
rameters.	transform(self, X)	Call transform on the estimator with the best found pa-
		rameters.

\_\_init\_\_\_(self, estimator, param\_distributions, n\_iter=10, scoring=None, n\_jobs=None, iid='warn', refit=True, cv='warn', verbose=0, pre\_dispatch='2\*n\_jobs', random\_state=None, error\_score='raise-deprecating', return\_train\_score=False)

## $decision_function(self, X)$

Call decision\_function on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports decision\_function.

#### **Parameters**

X [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

**fit** (*self*, *X*, *y=None*, *groups=None*, \*\*fit\_params)

Run fit with all sets of parameters.

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Training vector, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array-like, shape = [n\_samples] or [n\_samples, n\_output], optional] Target relative to X for classification or regression; None for unsupervised learning.
- **groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set. Only used in conjunction with a "Group" *cv* instance (e.g., *GroupKFold*).
- \*\*fit\_params [dict of string -> object] Parameters passed to the fit method of the estimator

#### get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## inverse\_transform(self, Xt)

Call inverse\_transform on the estimator with the best found params.

Only available if the underlying estimator implements inverse\_transform and refit=True.

#### **Parameters**

Xt [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

## predict (self, X)

Call predict on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports predict.

#### **Parameters**

X [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

## predict\_log\_proba (self, X)

Call predict\_log\_proba on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports predict\_loq\_proba.

#### **Parameters**

X [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

## predict\_proba (self, X)

Call predict\_proba on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports predict\_proba.

#### **Parameters**

X [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

```
score(self, X, y=None)
```

Returns the score on the given data, if the estimator has been refit.

This uses the score defined by scoring where provided, and the best\_estimator\_.score method otherwise.

#### **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] Input data, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape = [n\_samples] or [n\_samples, n\_output], optional] Target relative to X for classification or regression; None for unsupervised learning.

#### Returns

score [float]

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, X)

Call transform on the estimator with the best found parameters.

Only available if the underlying estimator supports transform and refit=True.

#### **Parameters**

X [indexable, length n\_samples] Must fulfill the input assumptions of the underlying estimator.

## Examples using sklearn.model\_selection.RandomizedSearchCV

Comparing randomized search and grid search for hyperparameter estimation

```
model\_selection.fit\_grid\_point(X, y, ...[, Run fit on one set of parameters. ...])
```

## sklearn.model\_selection.fit\_grid\_point

Run fit on one set of parameters.

# **Parameters**

**X** [array-like, sparse matrix or list] Input data.

y [array-like or None] Targets for input data.

**estimator** [estimator object] A object of that type is instantiated for each grid point. This is assumed to implement the scikit-learn estimator interface. Either estimator needs to provide a score function, or scoring must be passed.

**parameters** [dict] Parameters to be set on estimator for this grid point.

**train** [ndarray, dtype int or bool] Boolean mask or indices for training set.

test [ndarray, dtype int or bool] Boolean mask or indices for test set.

**scorer** [callable or None] The scorer callable object / function must have its signature as scorer (estimator, X, y).

If None the estimator's score method is used.

verbose [int] Verbosity level.

\*\*fit\_params [kwargs] Additional parameter passed to the fit function of the estimator.

**error\_score** ['raise' or numeric] Value to assign to the score if an error occurs in estimator fitting. If set to 'raise', the error is raised. If a numeric value is given, FitFailedWarning is raised. This parameter does not affect the refit step, which will always raise the error. Default is 'raise' but from version 0.22 it will change to np.nan.

## Returns

score [float] Score of this parameter setting on given test split.

parameters [dict] The parameters that have been evaluated.

**n\_samples\_test** [int] Number of test samples in this split.

## 6.26.4 Model validation

model_selection.cross_validate(estimator,	Evaluate metric(s) by cross-validation and also record
X)	fit/score times.
model_selection.cross_val_predict(estimator,	Generate cross-validated estimates for each input data point
X)	
model_selection.cross_val_score(estimator,	Evaluate a score by cross-validation
X)	
model_selection.learning_curve(estimator, X,	Learning curve.
y)	
model_selection.permutation_test_score(	Evaluate the significance of a cross-validated score with
	permutations
model_selection.validation_curve(estimator,	Validation curve.
)	

## sklearn.model\_selection.cross validate

```
sklearn.model_selection.cross_validate(estimator, X, y=None, groups=None, scor-
ing=None, cv='warn', n_jobs=None, verbose=0,
fit_params=None, pre_dispatch='2*n_jobs', re-
turn_train_score=False, return_estimator=False,
error score='raise-deprecating')
```

Evaluate metric(s) by cross-validation and also record fit/score times.

Read more in the *User Guide*.

#### **Parameters**

estimator [estimator object implementing 'fit'] The object to use to fit the data.

- **X** [array-like] The data to fit. Can be for example a list, or an array.
- **y** [array-like, optional, default: None] The target variable to try to predict in the case of supervised learning.
- **groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set. Only used in conjunction with a "Group" *cv* instance (e.g., *GroupKFold*).
- **scoring** [string, callable, list/tuple, dict or None, default: None] A single string (see *The scoring parameter: defining model evaluation rules*) or a callable (see *Defining your scoring strategy from metric functions*) to evaluate the predictions on the test set.

For evaluating multiple metrics, either give a list of (unique) strings or a dict with names as keys and callables as values.

NOTE that when using custom scorers, each scorer should return a single value. Metric functions returning a list/array of values can be wrapped into multiple scorers that return one value each.

See Specifying multiple metrics for evaluation for an example.

If None, the estimator's score method is used.

- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross validation,
  - integer, to specify the number of folds in a (Stratified) KFold,
  - CV splitter,

• An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

**n\_jobs** [int or None, optional (default=None)] The number of CPUs to use to do the computation. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

**verbose** [integer, optional] The verbosity level.

fit\_params [dict, optional] Parameters to pass to the fit method of the estimator.

- **pre\_dispatch** [int, or string, optional] Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:
  - None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
  - An int, giving the exact number of total jobs that are spawned
  - A string, giving an expression as a function of n\_jobs, as in '2\*n\_jobs'

**return\_train\_score** [boolean, default=False] Whether to include train scores. Computing training scores is used to get insights on how different parameter settings impact the overfitting/underfitting trade-off. However computing the scores on the training set can be computationally expensive and is not strictly required to select the parameters that yield the best generalization performance.

return\_estimator [boolean, default False] Whether to return the estimators fitted on each split.

error\_score ['raise' | 'raise-deprecating' or numeric] Value to assign to the score if an error occurs in estimator fitting. If set to 'raise', the error is raised. If set to 'raise-deprecating', a FutureWarning is printed before the error is raised. If a numeric value is given, FitFailed-Warning is raised. This parameter does not affect the refit step, which will always raise the error. Default is 'raise-deprecating' but from version 0.22 it will change to np.nan.

#### Returns

**scores** [dict of float arrays of shape=(n\_splits,)] Array of scores of the estimator for each run of the cross validation.

A dict of arrays containing the score/time arrays for each scorer is returned. The possible keys for this dict are:

test\_score The score array for test scores on each cv split.

**train\_score** The score array for train scores on each cv split. This is available only if return\_train\_score parameter is True.

**fit\_time** The time for fitting the estimator on the train set for each cv split.

score\_time The time for scoring the estimator on the test set for each cv
split. (Note time for scoring on the train set is not included even if
return\_train\_score is set to True

**estimator** The estimator objects for each cv split. This is available only if return estimator parameter is set to True.

#### See also:

sklearn.model\_selection.cross\_val\_score Run cross-validation for single metric evaluation.

**sklearn.model\_selection.cross\_val\_predict** Get predictions from each split of cross-validation for diagnostic purposes.

sklearn.metrics.make\_scorer Make a scorer from a performance metric or loss function.

# **Examples**

```
>>> from sklearn import datasets, linear_model
>>> from sklearn.model_selection import cross_validate
>>> from sklearn.metrics.scorer import make_scorer
>>> from sklearn.metrics import confusion_matrix
>>> from sklearn.svm import LinearSVC
>>> diabetes = datasets.load_diabetes()
>>> X = diabetes.data[:150]
>>> y = diabetes.target[:150]
>>> lasso = linear_model.Lasso()
```

Single metric evaluation using cross\_validate

```
>>> cv_results = cross_validate(lasso, X, y, cv=3)
>>> sorted(cv_results.keys())
['fit_time', 'score_time', 'test_score']
>>> cv_results['test_score']
array([0.33150734, 0.08022311, 0.03531764])
```

Multiple metric evaluation using cross\_validate (please refer the scoring parameter doc for more information)

#### sklearn.model\_selection.cross val predict

Generate cross-validated estimates for each input data point

The data is split according to the cv parameter. Each sample belongs to exactly one test set, and its prediction is computed with an estimator fitted on the corresponding training set.

Passing these predictions into an evaluation metric may not be a valid way to measure generalization performance. Results can differ from <code>cross\_validate</code> and <code>cross\_val\_score</code> unless all tests sets have equal size and the metric decomposes over samples.

Read more in the *User Guide*.

#### **Parameters**

estimator [estimator object implementing 'fit' and 'predict'] The object to use to fit the data.

- **X** [array-like] The data to fit. Can be, for example a list, or an array at least 2d.
- **y** [array-like, optional, default: None] The target variable to try to predict in the case of supervised learning.
- **groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set. Only used in conjunction with a "Group" *cv* instance (e.g., *GroupKFold*).
- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross validation,
  - integer, to specify the number of folds in a (Stratified) KFold,
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, *StratifiedKFold* is used. In all other cases, *KFold* is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

**n\_jobs** [int or None, optional (default=None)] The number of CPUs to use to do the computation. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

verbose [integer, optional] The verbosity level.

**fit\_params** [dict, optional] Parameters to pass to the fit method of the estimator.

- **pre\_dispatch** [int, or string, optional] Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:
  - None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
  - An int, giving the exact number of total jobs that are spawned
  - A string, giving an expression as a function of n\_jobs, as in '2\*n\_jobs'

**method** [string, optional, default: 'predict'] Invokes the passed method name of the passed estimator. For method='predict\_proba', the columns correspond to the classes in sorted order.

#### Returns

**predictions** [ndarray] This is the result of calling method

# See also:

cross val score calculate score for each CV split

cross\_validate calculate one or more scores and timings for each CV split

#### **Notes**

In the case that one or more classes are absent in a training portion, a default score needs to be assigned to all instances for that class if method produces columns per class, as in {'decision\_function', 'predict\_proba', 'predict\_log\_proba'}. For predict\_proba this value is 0. In order to ensure finite output, we approximate negative infinity by the minimum finite float value for the dtype in other cases.

## **Examples**

```
>>> from sklearn import datasets, linear_model
>>> from sklearn.model_selection import cross_val_predict
>>> diabetes = datasets.load_diabetes()
>>> X = diabetes.data[:150]
>>> y = diabetes.target[:150]
>>> lasso = linear_model.Lasso()
>>> y_pred = cross_val_predict(lasso, X, y, cv=3)
```

## Examples using sklearn.model\_selection.cross\_val\_predict

• Plotting Cross-Validated Predictions

```
sklearn.model_selection.cross_val_score
```

```
sklearn.model_selection.cross_val_score (estimator, X, y=None, groups=None, scoring=None, cv='warn', n\_jobs=None, verbose=0, fit\_params=None, pre\_dispatch='2*n\_jobs', error\_score='raise-deprecating')
```

Evaluate a score by cross-validation

Read more in the User Guide.

## **Parameters**

estimator [estimator object implementing 'fit'] The object to use to fit the data.

- **X** [array-like] The data to fit. Can be for example a list, or an array.
- **y** [array-like, optional, default: None] The target variable to try to predict in the case of supervised learning.
- **groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set. Only used in conjunction with a "Group" *cv* instance (e.g., *GroupKFold*).
- scoring [string, callable or None, optional, default: None] A string (see model evaluation documentation) or a scorer callable object / function with signature scorer (estimator, X, y) which should return only a single value.

Similar to cross\_validate but only a single metric is permitted.

If None, the estimator's default scorer (if available) is used.

- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross validation,
  - integer, to specify the number of folds in a (Stratified) KFold,
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

**n\_jobs** [int or None, optional (default=None)] The number of CPUs to use to do the computation. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

verbose [integer, optional] The verbosity level.

fit\_params [dict, optional] Parameters to pass to the fit method of the estimator.

- **pre\_dispatch** [int, or string, optional] Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:
  - None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
  - An int, giving the exact number of total jobs that are spawned
  - A string, giving an expression as a function of n\_jobs, as in '2\*n\_jobs'

error\_score ['raise' | 'raise-deprecating' or numeric] Value to assign to the score if an error occurs in estimator fitting. If set to 'raise', the error is raised. If set to 'raise-deprecating', a FutureWarning is printed before the error is raised. If a numeric value is given, FitFailed-Warning is raised. This parameter does not affect the refit step, which will always raise the error. Default is 'raise-deprecating' but from version 0.22 it will change to np.nan.

#### Returns

**scores** [array of float, shape=(len(list(cv)),)] Array of scores of the estimator for each run of the cross validation.

## See also:

- **sklearn.model\_selection.cross\_validate** To run cross-validation on multiple metrics and also to return train scores, fit times and score times.
- **sklearn.model\_selection.cross\_val\_predict** Get predictions from each split of cross-validation for diagnostic purposes.
- **sklearn.metrics.make\_scorer** Make a scorer from a performance metric or loss function.

# **Examples**

```
>>> from sklearn import datasets, linear_model
>>> from sklearn.model_selection import cross_val_score
>>> diabetes = datasets.load_diabetes()
>>> X = diabetes.data[:150]
>>> y = diabetes.target[:150]
>>> lasso = linear_model.Lasso()
>>> print(cross_val_score(lasso, X, y, cv=3))
[0.33150734 0.08022311 0.03531764]
```

# Examples using sklearn.model selection.cross val score

- Model selection with Probabilistic PCA and Factor Analysis (FA)
- Cross-validation on Digits Dataset Exercise
- Imputing missing values with variants of IterativeImputer
- Imputing missing values before building an estimator
- Underfitting vs. Overfitting
- Nested versus non-nested cross-validation
- SVM-Anova: SVM with univariate feature selection

## sklearn.model\_selection.learning\_curve

```
sklearn.model_selection.learning_curve (estimator, X, y, groups=None, train_sizes=array([0.1, 0.325, 0.55, 0.775, 1. ]), cv='warn', scoring=None, exploit_incremental_learning=False, n_jobs=None, pre_dispatch='all', verbose=0, shuffle=False, random_state=None, error_score='raise-deprecating')
```

Learning curve.

Determines cross-validated training and test scores for different training set sizes.

A cross-validation generator splits the whole dataset k times in training and test data. Subsets of the training set with varying sizes will be used to train the estimator and a score for each training subset size and the test set will be computed. Afterwards, the scores will be averaged over all k runs for each training subset size.

Read more in the *User Guide*.

## **Parameters**

**estimator** [object type that implements the "fit" and "predict" methods] An object of that type which is cloned for each validation.

- **X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array-like, shape (n\_samples) or (n\_samples, n\_features), optional] Target relative to X for classification or regression; None for unsupervised learning.

**groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set. Only used in conjunction with a "Group" *cv* instance (e.g., *GroupKFold*).

- **train\_sizes** [array-like, shape (n\_ticks,), dtype float or int] Relative or absolute numbers of training examples that will be used to generate the learning curve. If the dtype is float, it is regarded as a fraction of the maximum size of the training set (that is determined by the selected validation method), i.e. it has to be within (0, 1]. Otherwise it is interpreted as absolute sizes of the training sets. Note that for classification the number of samples usually have to be big enough to contain at least one sample from each class. (default: np.linspace(0.1, 1.0, 5))
- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross validation,
  - integer, to specify the number of folds in a (Stratified) KFold,
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, *StratifiedKFold* is used. In all other cases, *KFold* is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

- **exploit\_incremental\_learning** [boolean, optional, default: False] If the estimator supports incremental learning, this will be used to speed up fitting for different training set sizes.
- **n\_jobs** [int or None, optional (default=None)] Number of jobs to run in parallel. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- **pre\_dispatch** [integer or string, optional] Number of predispatched jobs for parallel execution (default is all). The option can reduce the allocated memory. The string can be an expression like '2\*n\_jobs'.
- **verbose** [integer, optional] Controls the verbosity: the higher, the more messages.
- **shuffle** [boolean, optional] Whether to shuffle training data before taking prefixes of it based on 'train sizes'.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when shuffle is True.
- **error\_score** ['raise' | 'raise-deprecating' or numeric] Value to assign to the score if an error occurs in estimator fitting. If set to 'raise', the error is raised. If set to 'raise-deprecating', a FutureWarning is printed before the error is raised. If a numeric value is given, FitFailed-Warning is raised. This parameter does not affect the refit step, which will always raise the error. Default is 'raise-deprecating' but from version 0.22 it will change to np.nan.

## Returns

**train\_sizes\_abs** [array, shape (n\_unique\_ticks,), dtype int] Numbers of training examples that has been used to generate the learning curve. Note that the number of ticks might be less than n ticks because duplicate entries will be removed.

**train\_scores** [array, shape (n\_ticks, n\_cv\_folds)] Scores on training sets. **test\_scores** [array, shape (n\_ticks, n\_cv\_folds)] Scores on test set.

## **Notes**

See examples/model selection/plot learning curve.py

# Examples using sklearn.model\_selection.learning\_curve

- Comparison of kernel ridge regression and SVR
- Plotting Learning Curves

## sklearn.model\_selection.permutation test score

Evaluate the significance of a cross-validated score with permutations

Read more in the *User Guide*.

#### **Parameters**

estimator [estimator object implementing 'fit'] The object to use to fit the data.

- **X** [array-like of shape at least 2D] The data to fit.
- **y** [array-like] The target variable to try to predict in the case of supervised learning.
- **groups** [array-like, with shape (n\_samples,), optional] Labels to constrain permutation within groups, i.e. y values are permuted among samples with the same group identifier. When not specified, y values are permuted among all samples.

When a grouped cross-validator is used, the group labels are also passed on to the split method of the cross-validator. The cross-validator uses them for grouping the samples while splitting the dataset into train/test set.

**scoring** [string, callable or None, optional, default: None] A single string (see *The scoring parameter: defining model evaluation rules*) or a callable (see *Defining your scoring strategy from metric functions*) to evaluate the predictions on the test set.

If None the estimator's score method is used.

- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross validation,
  - integer, to specify the number of folds in a (Stratified) KFold,
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

- **n\_permutations** [integer, optional] Number of times to permute y.
- **n\_jobs** [int or None, optional (default=None)] The number of CPUs to use to do the computation. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- random\_state [int, RandomState instance or None, optional (default=0)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**verbose** [integer, optional] The verbosity level.

#### Returns

**score** [float] The true score without permuting targets.

**permutation\_scores** [array, shape (n\_permutations,)] The scores obtained for each permutations.

**pvalue** [float] The p-value, which approximates the probability that the score would be obtained by chance. This is calculated as:

```
(C + 1) / (n_permutations + 1)
```

Where C is the number of permutations whose score >= the true score.

The best possible p-value is  $1/(n_permutations + 1)$ , the worst is 1.0.

## **Notes**

This function implements Test 1 in:

Ojala and Garriga. Permutation Tests for Studying Classifier Performance. The Journal of Machine Learning Research (2010) vol. 11

## Examples using sklearn.model\_selection.permutation\_test\_score

• *Test with permutations the significance of a classification score* 

## sklearn.model\_selection.validation curve

Validation curve.

Determine training and test scores for varying parameter values.

Compute scores for an estimator with different values of a specified parameter. This is similar to grid search with one parameter. However, this will also compute training scores and is merely a utility for plotting the results

Read more in the User Guide.

#### **Parameters**

- **estimator** [object type that implements the "fit" and "predict" methods] An object of that type which is cloned for each validation.
- **X** [array-like, shape (n\_samples, n\_features)] Training vector, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array-like, shape (n\_samples) or (n\_samples, n\_features), optional] Target relative to X for classification or regression; None for unsupervised learning.

param\_name [string] Name of the parameter that will be varied.

param\_range [array-like, shape (n\_values,)] The values of the parameter that will be evaluated.

- **groups** [array-like, with shape (n\_samples,), optional] Group labels for the samples used while splitting the dataset into train/test set. Only used in conjunction with a "Group" *cv* instance (e.g., *GroupKFold*).
- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross validation,
  - integer, to specify the number of folds in a (Stratified) KFold,
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

- scoring [string, callable or None, optional, default: None] A string (see model evaluation documentation) or a scorer callable object / function with signature scorer (estimator, X, y).
- **n\_jobs** [int or None, optional (default=None)] Number of jobs to run in parallel. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- **pre\_dispatch** [integer or string, optional] Number of predispatched jobs for parallel execution (default is all). The option can reduce the allocated memory. The string can be an expression like '2\*n\_jobs'.

**verbose** [integer, optional] Controls the verbosity: the higher, the more messages.

**error\_score** ['raise' | 'raise-deprecating' or numeric] Value to assign to the score if an error occurs in estimator fitting. If set to 'raise', the error is raised. If set to 'raise-deprecating', a FutureWarning is printed before the error is raised. If a numeric value is given, FitFailed-Warning is raised. This parameter does not affect the refit step, which will always raise the error. Default is 'raise-deprecating' but from version 0.22 it will change to np.nan.

#### Returns

**train\_scores** [array, shape (n\_ticks, n\_cv\_folds)] Scores on training sets. **test\_scores** [array, shape (n\_ticks, n\_cv\_folds)] Scores on test set.

## **Notes**

See Plotting Validation Curves

# Examples using sklearn.model\_selection.validation\_curve

• Plotting Validation Curves

# 6.27 sklearn.multiclass: Multiclass and multilabel classification

# 6.27.1 Multiclass and multilabel classification strategies

## This module implements multiclass learning algorithms:

- one-vs-the-rest / one-vs-all
- one-vs-one
- error correcting output codes

The estimators provided in this module are meta-estimators: they require a base estimator to be provided in their constructor. For example, it is possible to use these estimators to turn a binary classifier or a regressor into a multiclass classifier. It is also possible to use these estimators with multiclass estimators in the hope that their accuracy or runtime performance improves.

All classifiers in scikit-learn implement multiclass classification; you only need to use this module if you want to experiment with custom multiclass strategies.

The one-vs-the-rest meta-classifier also implements a *predict\_proba* method, so long as such a method is implemented by the base classifier. This method returns probabilities of class membership in both the single label and multilabel case. Note that in the multilabel case, probabilities are the marginal probability that a given sample falls in the given class. As such, in the multilabel case the sum of these probabilities over all possible labels for a given sample *will not* sum to unity, as they do in the single label case.

**User guide:** See the *Multiclass and multilabel algorithms* section for further details.

multiclass.OneVsRestClassifier(estimator[,	One-vs-the-rest (OvR) multiclass/multilabel strategy
])	
multiclass.OneVsOneClassifier(estimator[,	One-vs-one multiclass strategy
])	
multiclass.OutputCodeClassifier(estimator[,	(Error-Correcting) Output-Code multiclass strategy
])	

## 6.27.2 sklearn.multiclass.OneVsRestClassifier

class sklearn.multiclass.OneVsRestClassifier (estimator, n\_jobs=None)
 One-vs-the-rest (OvR) multiclass/multilabel strategy

Also known as one-vs-all, this strategy consists in fitting one classifier per class. For each classifier, the class is

fitted against all the other classes. In addition to its computational efficiency (only n\_classes classifiers are needed), one advantage of this approach is its interpretability. Since each class is represented by one and one classifier only, it is possible to gain knowledge about the class by inspecting its corresponding classifier. This is the most commonly used strategy for multiclass classification and is a fair default choice.

This strategy can also be used for multilabel learning, where a classifier is used to predict multiple labels for instance, by fitting on a 2-d matrix in which cell [i, j] is 1 if sample i has label j and 0 otherwise.

In the multilabel learning literature, OvR is also known as the binary relevance method.

Read more in the User Guide.

#### **Parameters**

**estimator** [estimator object] An estimator object implementing fit and one of decision\_function or predict\_proba.

**n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### Attributes

**estimators**\_ [list of n\_classes estimators] Estimators used for predictions.

classes\_ [array, shape = [n\_classes]] Class labels.

**label\_binarizer**\_ [LabelBinarizer object] Object used to transform multiclass labels to binary labels and vice-versa.

multilabel [boolean] Whether this is a multilabel classifier

#### **Methods**

$decision\_function(self, X)$	Returns the distance of each sample from the decision
	boundary for each class.
fit(self, X, y)	Fit underlying estimators.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X, y[, classes])</pre>	Partially fit underlying estimators
predict(self, X)	Predict multi-class targets using underlying estimators.
$predict\_proba(self, X)$	Probability estimates.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
___init___(self, estimator, n_jobs=None)
```

## $decision_function(self, X)$

Returns the distance of each sample from the decision boundary for each class. This can only be used with estimators which implement the decision\_function method.

#### **Parameters**

X [array-like, shape = [n samples, n features]]

## Returns

**T** [array-like, shape = [n\_samples, n\_classes]]

**fit** (self, X, y)

Fit underlying estimators.

#### **Parameters**

- **X** [(sparse) array-like, shape = [n\_samples, n\_features]] Data.
- y [(sparse) array-like, shape = [n\_samples, ], [n\_samples, n\_classes]] Multi-class targets. An indicator matrix turns on multilabel classification.

#### Returns

self

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

#### multilabel

Whether this is a multilabel classifier

## partial\_fit (self, X, y, classes=None)

Partially fit underlying estimators

Should be used when memory is inefficient to train all data. Chunks of data can be passed in several iteration.

## **Parameters**

- **X** [(sparse) array-like, shape = [n\_samples, n\_features]] Data.
- y [(sparse) array-like, shape = [n\_samples, ], [n\_samples, n\_classes]] Multi-class targets. An indicator matrix turns on multilabel classification.

**classes** [array, shape (n\_classes, )] Classes across all calls to partial\_fit. Can be obtained via np.unique(y\_all), where y\_all is the target vector of the entire dataset. This argument is only required in the first call of partial\_fit and can be omitted in the subsequent calls.

#### **Returns**

self

#### predict (self, X)

Predict multi-class targets using underlying estimators.

#### **Parameters**

**X** [(sparse) array-like, shape = [n\_samples, n\_features]] Data.

#### **Returns**

**y** [(sparse) array-like, shape = [n\_samples, ], [n\_samples, n\_classes].] Predicted multi-class targets.

## $predict_proba(self, X)$

Probability estimates.

The returned estimates for all classes are ordered by label of classes.

Note that in the multilabel case, each sample can have any number of labels. This returns the marginal probability that the given sample has the label in question. For example, it is entirely consistent that two labels both have a 90% probability of applying to a given sample.

In the single label multiclass case, the rows of the returned matrix sum to 1.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

#### Returns

**T** [(sparse) array-like, shape = [n\_samples, n\_classes]] Returns the probability of the sample for each class in the model, where classes are ordered as they are in self.classes\_.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
\mathbf{X} [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## **Returns**

self

## Examples using sklearn.multiclass.OneVsRestClassifier

- Multilabel classification
- Receiver Operating Characteristic (ROC)
- Precision-Recall
- Classifier Chain

# 6.27.3 sklearn.multiclass.OneVsOneClassifier

class sklearn.multiclass.OneVsOneClassifier (estimator, n\_jobs=None)
 One-vs-one multiclass strategy

This strategy consists in fitting one classifier per class pair. At prediction time, the class which received the most votes is selected. Since it requires to fit  $n_{classes} * (n_{classes} - 1) / 2$  classifiers, this method is usually slower than one-vs-the-rest, due to its  $O(n_{classes}^2)$  complexity. However, this method may be advantageous for algorithms such as kernel algorithms which don't scale well with  $n_{samples}$ . This is because

each individual learning problem only involves a small subset of the data whereas, with one-vs-the-rest, the complete dataset is used n\_classes times.

Read more in the *User Guide*.

#### **Parameters**

**estimator** [estimator object] An estimator object implementing fit and one of decision\_function or predict\_proba.

**n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### **Attributes**

**estimators**\_ [list of n\_classes \* (n\_classes - 1) / 2 estimators] Estimators used for predictions.

classes\_ [numpy array of shape [n\_classes]] Array containing labels.

pairwise\_indices\_ [list, length = len(estimators\_), or None] Indices of samples used
 when training the estimators. None when estimator does not have \_pairwise at tribute.

#### **Methods**

decision_function(self, X)	Decision function for the OneVsOneClassifier.
fit(self, X, y)	Fit underlying estimators.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X, y[, classes])</pre>	Partially fit underlying estimators
predict(self, X)	Estimate the best class label for each sample in X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_\_init\_\_\_(self, estimator, n\_jobs=None)

## $decision_function(self, X)$

Decision function for the OneVsOneClassifier.

The decision values for the samples are computed by adding the normalized sum of pair-wise classification confidence levels to the votes in order to disambiguate between the decision values when the votes for all the classes are equal leading to a tie.

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

## Returns

**Y** [array-like, shape = [n\_samples, n\_classes]]

# fit (self, X, y)

Fit underlying estimators.

#### **Parameters**

**X** [(sparse) array-like, shape = [n\_samples, n\_features]] Data.

y [array-like, shape = [n\_samples]] Multi-class targets.

#### Returns

self

# get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

**params** [mapping of string to any] Parameter names mapped to their values.

```
partial_fit (self, X, y, classes=None)
```

Partially fit underlying estimators

Should be used when memory is inefficient to train all data. Chunks of data can be passed in several iteration, where the first call should have an array of all target variables.

#### **Parameters**

```
X [(sparse) array-like, shape = [n_samples, n_features]] Data.
```

y [array-like, shape = [n\_samples]] Multi-class targets.

**classes** [array, shape (n\_classes, )] Classes across all calls to partial\_fit. Can be obtained via np.unique(y\_all), where y\_all is the target vector of the entire dataset. This argument is only required in the first call of partial\_fit and can be omitted in the subsequent calls.

#### **Returns**

self

## predict (self, X)

Estimate the best class label for each sample in X.

This is implemented as argmax (decision\_function(X), axis=1) which will return the label of the class with most votes by estimators predicting the outcome of a decision for each possible class pair.

# **Parameters**

**X** [(sparse) array-like, shape = [n\_samples, n\_features]] Data.

#### **Returns**

y [numpy array of shape [n\_samples]] Predicted multi-class targets.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

## **Parameters**

X [array-like, shape = (n\_samples, n\_features)] Test samples.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# 6.27.4 sklearn.multiclass.OutputCodeClassifier

(Error-Correcting) Output-Code multiclass strategy

Output-code based strategies consist in representing each class with a binary code (an array of 0s and 1s). At fitting time, one binary classifier per bit in the code book is fitted. At prediction time, the classifiers are used to project new points in the class space and the class closest to the points is chosen. The main advantage of these strategies is that the number of classifiers used can be controlled by the user, either for compressing the model (0 < code\_size < 1) or for making the model more robust to errors (code\_size > 1). See the documentation for more details.

Read more in the *User Guide*.

#### **Parameters**

**estimator** [estimator object] An estimator object implementing fit and one of decision\_function or predict\_proba.

**code\_size** [float] Percentage of the number of classes to be used to create the code book. A number between 0 and 1 will require fewer classifiers than one-vs-the-rest. A number greater than 1 will require more classifiers than one-vs-the-rest.

random\_state [int, RandomState instance or None, optional, default: None] The generator used to initialize the codebook. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**n\_jobs** [int or None, optional (default=None)] The number of jobs to use for the computation. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

## Attributes

estimators\_ [list of int (n\_classes \* code\_size) estimators] Estimators used for predictions.

classes\_ [numpy array of shape [n\_classes]] Array containing labels.

code\_book\_ [numpy array of shape [n\_classes, code\_size]] Binary array containing the code of each class.

#### References

[R2eddaeec0849-1], [R2eddaeec0849-2], [R2eddaeec0849-3]

# **Methods**

fit(self, X, y)	Fit underlying estimators.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict multi-class targets using underlying estimators.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_ (self, estimator, code\_size=1.5, random\_state=None, n\_jobs=None)

## **fit** (self, X, y)

Fit underlying estimators.

#### **Parameters**

- **X** [(sparse) array-like, shape = [n\_samples, n\_features]] Data.
- y [numpy array of shape [n\_samples]] Multi-class targets.

#### Returns

self

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict multi-class targets using underlying estimators.

## **Parameters**

**X** [(sparse) array-like, shape = [n\_samples, n\_features]] Data.

## Returns

y [numpy array of shape [n\_samples]] Predicted multi-class targets.

## score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

## **Parameters**

- X [array-like, shape = (n\_samples, n\_features)] Test samples.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.
- **sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

# Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# 6.28 sklearn.multioutput: Multioutput regression and classification

This module implements multioutput regression and classification.

The estimators provided in this module are meta-estimators: they require a base estimator to be provided in their constructor. The meta-estimator extends single output estimators to multioutput estimators.

User guide: See the Multiclass and multilabel algorithms section for further details.

multioutput.ClassifierChain(base_estimator)	A multi-label model that arranges binary classifiers into a
	chain.
multioutput.MultiOutputRegressor(estimator)	Multi target regression
multioutput.MultiOutputClassifier(estimator)	Multi target classification
multioutput.RegressorChain(base_estimator[,	A multi-label model that arranges regressions into a chain.
])	

# 6.28.1 sklearn.multioutput.ClassifierChain

class sklearn.multioutput.ClassifierChain(base\_estimator, order=None, cv=None, random state=None)

A multi-label model that arranges binary classifiers into a chain.

Each model makes a prediction in the order specified by the chain using all of the available features provided to the model plus the predictions of models that are earlier in the chain.

Read more in the *User Guide*.

## **Parameters**

**base\_estimator** [estimator] The base estimator from which the classifier chain is built.

**order** [array-like, shape=[n\_outputs] or 'random', optional] By default the order will be determined by the order of columns in the label matrix Y.:

```
order = [0, 1, 2, ..., Y.shape[1] - 1]
```

The order of the chain can be explicitly set by providing a list of integers. For example, for a chain of length 5.:

```
order = [1, 3, 2, 4, 0]
```

means that the first model in the chain will make predictions for column 1 in the Y matrix, the second model will make predictions for column 3, etc.

If order is 'random' a random ordering will be used.

- cv [int, cross-validation generator or an iterable, optional (default=None)] Determines whether to use cross validated predictions or true labels for the results of previous estimators in the chain. If cv is None the true labels are used when fitting. Otherwise possible inputs for cv are:
  - integer, to specify the number of folds in a (Stratified)KFold,
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

The random number generator is used to generate random chain orders.

# **Attributes**

**classes**\_ [list] A list of arrays of length len(estimators\_) containing the class labels for each estimator in the chain.

estimators\_ [list] A list of clones of base\_estimator.

**order**\_ [list] The order of labels in the classifier chain.

#### See also:

RegressorChain Equivalent for regression

MultioutputClassifier Classifies each output independently rather than chaining.

#### References

Jesse Read, Bernhard Pfahringer, Geoff Holmes, Eibe Frank, "Classifier Chains for Multi-label Classification", 2009.

#### Methods

decision_function(self, X)	Evaluate the decision_function of the models in the
	chain.
fit(self, X, Y)	Fit the model to data matrix X and targets Y.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict on the data matrix X using the ClassifierChain
	model.
predict_proba(self, X)	Predict probability estimates.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

**\_\_\_init\_\_** (*self*, *base\_estimator*, *order=None*, *cv=None*, *random\_state=None*)

## $decision_function(self, X)$

Evaluate the decision\_function of the models in the chain.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

## Returns

**Y\_decision** [array-like, shape (n\_samples, n\_classes )] Returns the decision function of the sample for each model in the chain.

#### fit (self, X, Y)

Fit the model to data matrix X and targets Y.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data.

Y [array-like, shape (n\_samples, n\_classes)] The target values.

## Returns

self [object]

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict on the data matrix X using the ClassifierChain model.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data.

## Returns

**Y\_pred** [array-like, shape (n\_samples, n\_classes)] The predicted values.

# $predict_proba(self, X)$

Predict probability estimates.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)]

## Returns

**Y\_prob** [array-like, shape (n\_samples, n\_classes)]

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

# **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples.

y [array-like, shape = (n samples) or (n samples, n outputs)] True labels for X.

**sample weight** [array-like, shape = [n samples], optional] Sample weights.

## **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### **Returns**

self

# Examples using sklearn.multioutput.ClassifierChain

· Classifier Chain

# 6.28.2 sklearn.multioutput.MultiOutputRegressor

This strategy consists of fitting one regressor per target. This is a simple strategy for extending regressors that do not natively support multi-target regression.

#### **Parameters**

**estimator** [estimator object] An estimator object implementing fit and predict.

**n\_jobs** [int or None, optional (default=None)] The number of jobs to run in parallel for fit. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

When individual estimators are fast to train or predict using n\_jobs>1 can result in slower performance due to the overhead of spawning processes.

## **Attributes**

**estimators** [list of n\_output estimators] Estimators used for predictions.

## **Methods**

fit(self, X, y[, sample_weight])	Fit the model to data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X, y[, sample_weight])</pre>	Incrementally fit the model to data.
predict(self, X)	Predict multi-output variable using a model trained for
	each target variable.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, estimator, n\_jobs=None)

 ${\tt fit} \ (self, X, y, sample\_weight=None)$ 

Fit the model to data. Fit a separate model for each output variable.

#### **Parameters**

- **X** [(sparse) array-like, shape (n\_samples, n\_features)] Data.
- y [(sparse) array-like, shape (n\_samples, n\_outputs)] Multi-output targets. An indicator matrix turns on multilabel estimation.

**sample\_weight** [array-like, shape = (n\_samples) or None] Sample weights. If None, then samples are equally weighted. Only supported if the underlying regressor supports sample weights.

#### **Returns**

self [object]

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

## partial\_fit (self, X, y, sample\_weight=None)

Incrementally fit the model to data. Fit a separate model for each output variable.

#### **Parameters**

- **X** [(sparse) array-like, shape (n\_samples, n\_features)] Data.
- y [(sparse) array-like, shape (n\_samples, n\_outputs)] Multi-output targets.

**sample\_weight** [array-like, shape = (n\_samples) or None] Sample weights. If None, then samples are equally weighted. Only supported if the underlying regressor supports sample weights.

## **Returns**

self [object]

predict (self, X)

**Predict multi-output variable using a model** trained for each target variable.

## **Parameters**

**X** [(sparse) array-like, shape (n samples, n features)] Data.

## Returns

**y** [(sparse) array-like, shape (n\_samples, n\_outputs)] Multi-output targets predicted across multiple predictors. Note: Separate models are generated for each predictor.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the regression sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). Best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Test samples.

y [array-like, shape (n\_samples) or (n\_samples, n\_outputs)] True values for X.

sample\_weight [array-like, shape [n\_samples], optional] Sample weights.

## Returns

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

R^2 is calculated by weighting all the targets equally using multioutput='uniform\_average'.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## Examples using sklearn.multioutput.MultiOutputRegressor

• Comparing random forests and the multi-output meta estimator

# 6.28.3 sklearn.multioutput.MultiOutputClassifier

This strategy consists of fitting one classifier per target. This is a simple strategy for extending classifiers that do not natively support multi-target classification

## **Parameters**

estimator [estimator object] An estimator object implementing fit, score and predict\_proba.

n\_jobs [int or None, optional (default=None)] The number of jobs to use for the computation. It does each target variable in y in parallel. None means 1 unless in a joblib.
parallel\_backend context. -1 means using all processors. See Glossary for more
details.

## **Attributes**

**estimators**\_ [list of n\_output estimators] Estimators used for predictions.

## **Methods**

fit(self, X, y[, sample_weight])	Fit the model to data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X, y[, classes, sample_weight])</pre>	Incrementally fit the model to data.

Continued on next page

Table 6.216 – continued from previous page

predict(self, X)	Predict multi-output variable using a model trained for
	each target variable.
predict_proba(self, X)	Probability estimates.
score(self, X, y)	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, estimator, n\_jobs=None)

fit (self, X, y, sample\_weight=None)

Fit the model to data. Fit a separate model for each output variable.

#### **Parameters**

- **X** [(sparse) array-like, shape (n\_samples, n\_features)] Data.
- y [(sparse) array-like, shape (n\_samples, n\_outputs)] Multi-output targets. An indicator matrix turns on multilabel estimation.

**sample\_weight** [array-like, shape = (n\_samples) or None] Sample weights. If None, then samples are equally weighted. Only supported if the underlying regressor supports sample weights.

## Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

partial\_fit (self, X, y, classes=None, sample\_weight=None)

Incrementally fit the model to data. Fit a separate model for each output variable.

## **Parameters**

- **X** [(sparse) array-like, shape (n\_samples, n\_features)] Data.
- y [(sparse) array-like, shape (n\_samples, n\_outputs)] Multi-output targets.

classes [list of numpy arrays, shape (n\_outputs)] Each array is unique classes for one output in str/int Can be obtained by via [np.unique(y[:, i]) for i in range(y. shape[1])], where y is the target matrix of the entire dataset. This argument is required for the first call to partial\_fit and can be omitted in the subsequent calls. Note that y doesn't need to contain all labels in classes.

**sample\_weight** [array-like, shape = (n\_samples) or None] Sample weights. If None, then samples are equally weighted. Only supported if the underlying regressor supports sample weights.

## Returns

self [object]

predict (self, X)

Predict multi-output variable using a model trained for each target variable.

#### **Parameters**

**X** [(sparse) array-like, shape (n\_samples, n\_features)] Data.

## Returns

**y** [(sparse) array-like, shape (n\_samples, n\_outputs)] Multi-output targets predicted across multiple predictors. Note: Separate models are generated for each predictor.

## predict\_proba (self, X)

Probability estimates. Returns prediction probabilities for each class of each output.

This method will raise a ValueError if any of the estimators do not have predict\_proba.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Data

#### **Returns**

p [array of shape = [n\_samples, n\_classes], or a list of n\_outputs such arrays if n\_outputs >
 1.] The class probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes* .

## score(self, X, y)

Returns the mean accuracy on the given test data and labels.

#### **Parameters**

- **X** [array-like, shape [n\_samples, n\_features]] Test samples
- y [array-like, shape [n\_samples, n\_outputs]] True values for X

## Returns

scores [float] accuracy\_score of self.predict(X) versus y

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# 6.28.4 sklearn.multioutput.RegressorChain

A multi-label model that arranges regressions into a chain.

Each model makes a prediction in the order specified by the chain using all of the available features provided to the model plus the predictions of models that are earlier in the chain.

Read more in the User Guide.

#### **Parameters**

base\_estimator [estimator] The base estimator from which the classifier chain is built.

**order** [array-like, shape=[n\_outputs] or 'random', optional] By default the order will be determined by the order of columns in the label matrix Y.:

```
order = [0, 1, 2, ..., Y.shape[1] - 1]
```

The order of the chain can be explicitly set by providing a list of integers. For example, for a chain of length 5.:

```
order = [1, 3, 2, 4, 0]
```

means that the first model in the chain will make predictions for column 1 in the Y matrix, the second model will make predictions for column 3, etc.

If order is 'random' a random ordering will be used.

- cv [int, cross-validation generator or an iterable, optional (default=None)] Determines whether to use cross validated predictions or true labels for the results of previous estimators in the chain. If cv is None the true labels are used when fitting. Otherwise possible inputs for cv are:
  - integer, to specify the number of folds in a (Stratified)KFold,
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

The random number generator is used to generate random chain orders.

## Attributes

estimators\_ [list] A list of clones of base\_estimator.

**order**\_ [list] The order of labels in the classifier chain.

## See also:

ClassifierChain Equivalent for classification

MultioutputRegressor Learns each output independently rather than chaining.

## **Methods**

fit(self, X, Y)	Fit the model to data matrix X and targets Y.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict on the data matrix X using the ClassifierChain
	model.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

**\_\_\_init\_\_** (*self*, *base\_estimator*, *order=None*, *cv=None*, *random\_state=None*)

fit (self, X, Y)

Fit the model to data matrix X and targets Y.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data.

Y [array-like, shape (n\_samples, n\_classes)] The target values.

## Returns

self [object]

get params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

predict (self, X)

Predict on the data matrix X using the ClassifierChain model.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data.

#### **Returns**

Y pred [array-like, shape (n samples, n classes)] The predicted values.

score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

## **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

 $\mathbf{y}$  [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for  $\mathbf{X}$ .

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## **Returns**

**score** [float] R^2 of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# 6.29 sklearn.naive\_bayes: Naive Bayes

The sklearn.naive\_bayes module implements Naive Bayes algorithms. These are supervised learning methods based on applying Bayes' theorem with strong (naive) feature independence assumptions.

**User guide:** See the *Naive Bayes* section for further details.

naive_bayes.BernoulliNB([alpha, binarize,])	Naive Bayes classifier for multivariate Bernoulli models.
<pre>naive_bayes.GaussianNB([priors, var_smoothing])</pre>	Gaussian Naive Bayes (GaussianNB)
naive_bayes.MultinomialNB([alpha,])	Naive Bayes classifier for multinomial models
naive_bayes.ComplementNB([alpha, fit_prior,])	The Complement Naive Bayes classifier described in Ren-
	nie et al.

# 6.29.1 sklearn.naive\_bayes.BernoulliNB

Naive Bayes classifier for multivariate Bernoulli models.

Like MultinomialNB, this classifier is suitable for discrete data. The difference is that while MultinomialNB works with occurrence counts, BernoulliNB is designed for binary/boolean features.

Read more in the *User Guide*.

## **Parameters**

**alpha** [float, optional (default=1.0)] Additive (Laplace/Lidstone) smoothing parameter (0 for no smoothing).

**binarize** [float or None, optional (default=0.0)] Threshold for binarizing (mapping to booleans) of sample features. If None, input is presumed to already consist of binary vectors.

**fit\_prior** [boolean, optional (default=True)] Whether to learn class prior probabilities or not. If false, a uniform prior will be used.

**class\_prior** [array-like, size=[n\_classes,], optional (default=None)] Prior probabilities of the classes. If specified the priors are not adjusted according to the data.

#### **Attributes**

**class\_log\_prior\_** [array, shape = [n\_classes]] Log probability of each class (smoothed).

**feature\_log\_prob\_** [array, shape =  $[n_{classes}, n_{features}]$ ] Empirical log probability of features given a class,  $P(x_{il})$ .

**class\_count\_** [array, shape = [n\_classes]] Number of samples encountered for each class during fitting. This value is weighted by the sample weight when provided.

**feature\_count\_** [array, shape = [n\_classes, n\_features]] Number of samples encountered for each (class, feature) during fitting. This value is weighted by the sample weight when provided.

#### References

C.D. Manning, P. Raghavan and H. Schuetze (2008). Introduction to Information Retrieval. Cambridge University Press, pp. 234-265. https://nlp.stanford.edu/IR-book/html/htmledition/the-bernoulli-model-1.html

A. McCallum and K. Nigam (1998). A comparison of event models for naive Bayes text classification. Proc. AAAI/ICML-98 Workshop on Learning for Text Categorization, pp. 41-48.

V. Metsis, I. Androutsopoulos and G. Paliouras (2006). Spam filtering with naive Bayes – Which naive Bayes? 3rd Conf. on Email and Anti-Spam (CEAS).

# **Examples**

```
>>> import numpy as np
>>> X = np.random.randint(2, size=(6, 100))
>>> Y = np.array([1, 2, 3, 4, 4, 5])
>>> from sklearn.naive_bayes import BernoulliNB
>>> clf = BernoulliNB()
>>> clf.fit(X, Y)
BernoulliNB(alpha=1.0, binarize=0.0, class_prior=None, fit_prior=True)
>>> print(clf.predict(X[2:3]))
[3]
```

## **Methods**

fit(self, X, y[, sample_weight])	Fit Naive Bayes classifier according to X, y
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>partial_fit(self, X, y[, classes, sample_weight])</pre>	Incremental fit on a batch of samples.
predict(self, X)	Perform classification on an array of test vectors X.
predict_log_proba(self, X)	Return log-probability estimates for the test vector X.
predict_proba(self, X)	Return probability estimates for the test vector X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, alpha=1.0, binarize=0.0, fit_prior=True, class_prior=None)
```

**fit** (*self*, *X*, *y*, *sample\_weight=None*)

Fit Naive Bayes classifier according to X, y

# **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vectors, where n samples is the number of samples and n features is the number of features.
- y [array-like, shape = [n\_samples]] Target values.

**sample\_weight** [array-like, shape = [n\_samples], (default=None)] Weights applied to individual samples (1. for unweighted).

#### Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

partial\_fit (self, X, y, classes=None, sample\_weight=None)

Incremental fit on a batch of samples.

This method is expected to be called several times consecutively on different chunks of a dataset so as to implement out-of-core or online learning.

This is especially useful when the whole dataset is too big to fit in memory at once.

This method has some performance overhead hence it is better to call partial\_fit on chunks of data that are as large as possible (as long as fitting in the memory budget) to hide the overhead.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.

y [array-like, shape = [n\_samples]] Target values.

**classes** [array-like, shape = [n\_classes] (default=None)] List of all the classes that can possibly appear in the y vector.

Must be provided at the first call to partial\_fit, can be omitted in subsequent calls.

**sample\_weight** [array-like, shape = [n\_samples] (default=None)] Weights applied to individual samples (1. for unweighted).

#### Returns

self [object]

predict (self, X)

Perform classification on an array of test vectors X.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

## Returns

 $\mathbf{C}$  [array, shape = [n\_samples]] Predicted target values for  $\mathbf{X}$ 

# $predict_log_proba(self, X)$

Return log-probability estimates for the test vector X.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

## Returns

**C** [array-like, shape = [n\_samples, n\_classes]] Returns the log-probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

# predict\_proba (self, X)

Return probability estimates for the test vector X.

## **Parameters**

X [array-like, shape = [n samples, n features]]

# Returns

**C** [array-like, shape = [n\_samples, n\_classes]] Returns the probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

# score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
\mathbf{X} [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# Examples using sklearn.naive\_bayes.BernoulliNB

- Hashing feature transformation using Totally Random Trees
- · Classification of text documents using sparse features

# 6.29.2 sklearn.naive\_bayes.GaussianNB

class sklearn.naive\_bayes.GaussianNB (priors=None, var\_smoothing=1e-09)
Gaussian Naive Bayes (GaussianNB)

Can perform online updates to model parameters via <code>partial\_fit</code> method. For details on algorithm used to update feature means and variance online, see Stanford CS tech report STAN-CS-79-773 by Chan, Golub, and LeVeque:

http://i.stanford.edu/pub/cstr/reports/cs/tr/79/773/CS-TR-79-773.pdf

Read more in the User Guide.

### **Parameters**

**priors** [array-like, shape (n\_classes,)] Prior probabilities of the classes. If specified the priors are not adjusted according to the data.

**var\_smoothing** [float, optional (default=1e-9)] Portion of the largest variance of all features that is added to variances for calculation stability.

## **Attributes**

```
class_prior_ [array, shape (n_classes,)] probability of each class.
class_count_ [array, shape (n_classes,)] number of training samples observed in each class.
theta_ [array, shape (n_classes, n_features)] mean of each feature per class
sigma_ [array, shape (n_classes, n_features)] variance of each feature per class
epsilon_ [float] absolute additive value to variances
```

# **Examples**

```
>>> import numpy as np
>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> Y = np.array([1, 1, 1, 2, 2, 2])
>>> from sklearn.naive_bayes import GaussianNB
>>> clf = GaussianNB()
>>> clf.fit(X, Y)
GaussianNB(priors=None, var_smoothing=1e-09)
>>> print(clf.predict([[-0.8, -1]]))
[1]
>>> clf_pf = GaussianNB()
>>> clf_pf.partial_fit(X, Y, np.unique(Y))
GaussianNB(priors=None, var_smoothing=1e-09)
>>> print(clf_pf.predict([[-0.8, -1]]))
[1]
```

# **Methods**

fit(self, X, y[, sample_weight]) Fit Gaussian Naive Bayes according to X, y		
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.	
<pre>partial_fit(self, X, y[, classes, sample_weight])</pre>	Incremental fit on a batch of samples.	
predict(self, X)	Perform classification on an array of test vectors X.	
predict_log_proba(self, X) Return log-probability estimates for the test v		
predict_proba(self, X)	Return probability estimates for the test vector X.	
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and	
	labels.	
set_params(self, \*\*params)	Set the parameters of this estimator.	

```
__init__ (self, priors=None, var_smoothing=1e-09)

fit (self, X, y, sample_weight=None)

Fit Gaussian Naive Bayes according to X, y
```

# **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape (n\_samples,)] Target values.
- **sample\_weight** [array-like, shape (n\_samples,), optional (default=None)] Weights applied to individual samples (1. for unweighted).

New in version 0.17: Gaussian Naive Bayes supports fitting with *sample\_weight*.

## Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

partial\_fit (self, X, y, classes=None, sample\_weight=None)

Incremental fit on a batch of samples.

This method is expected to be called several times consecutively on different chunks of a dataset so as to implement out-of-core or online learning.

This is especially useful when the whole dataset is too big to fit in memory at once.

This method has some performance and numerical stability overhead, hence it is better to call partial\_fit on chunks of data that are as large as possible (as long as fitting in the memory budget) to hide the overhead.

## **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape (n\_samples,)] Target values.
- **classes** [array-like, shape (n\_classes,), optional (default=None)] List of all the classes that can possibly appear in the y vector.

Must be provided at the first call to partial\_fit, can be omitted in subsequent calls.

**sample\_weight** [array-like, shape (n\_samples,), optional (default=None)] Weights applied to individual samples (1. for unweighted).

New in version 0.17.

# Returns

self [object]

predict (self, X)

Perform classification on an array of test vectors X.

# **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

# Returns

 $\mathbb{C}$  [array, shape = [n samples]] Predicted target values for X

# predict\_log\_proba (self, X)

Return log-probability estimates for the test vector X.

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

## **Returns**

**C** [array-like, shape = [n\_samples, n\_classes]] Returns the log-probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

# predict\_proba (self, X)

Return probability estimates for the test vector X.

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

## Returns

**C** [array-like, shape = [n\_samples, n\_classes]] Returns the probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

## **Parameters**

```
\mathbf{X} [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# Examples using sklearn.naive\_bayes.GaussianNB

- Comparison of Calibration of Classifiers
- Probability Calibration curves
- Probability calibration of classifiers
- Classifier comparison
- Plot class probabilities calculated by the Voting Classifier

- Plotting Learning Curves
- Importance of Feature Scaling

# 6.29.3 sklearn.naive\_bayes.MultinomialNB

class sklearn.naive\_bayes.MultinomialNB(alpha=1.0, fit\_prior=True, class\_prior=None)
 Naive Bayes classifier for multinomial models

The multinomial Naive Bayes classifier is suitable for classification with discrete features (e.g., word counts for text classification). The multinomial distribution normally requires integer feature counts. However, in practice, fractional counts such as tf-idf may also work.

Read more in the *User Guide*.

### **Parameters**

- **alpha** [float, optional (default=1.0)] Additive (Laplace/Lidstone) smoothing parameter (0 for no smoothing).
- **fit\_prior** [boolean, optional (default=True)] Whether to learn class prior probabilities or not. If false, a uniform prior will be used.
- **class\_prior** [array-like, size (n\_classes,), optional (default=None)] Prior probabilities of the classes. If specified the priors are not adjusted according to the data.

### Attributes

- class\_log\_prior\_ [array, shape (n\_classes, )] Smoothed empirical log probability for each class.
- intercept\_ [array, shape (n\_classes, )] Mirrors class\_log\_prior\_ for interpreting MultinomialNB as a linear model.
- **feature\_log\_prob\_** [array, shape (n\_classes, n\_features)] Empirical log probability of features given a class,  $P(x_i|y)$ .
- coef\_ [array, shape (n\_classes, n\_features)] Mirrors feature\_log\_prob\_ for interpreting
   MultinomialNB as a linear model.
- **class\_count\_** [array, shape (n\_classes,)] Number of samples encountered for each class during fitting. This value is weighted by the sample weight when provided.
- **feature\_count\_** [array, shape (n\_classes, n\_features)] Number of samples encountered for each (class, feature) during fitting. This value is weighted by the sample weight when provided.

## **Notes**

For the rationale behind the names *coef\_* and intercept\_, i.e. naive Bayes as a linear classifier, see J. Rennie et al. (2003), Tackling the poor assumptions of naive Bayes text classifiers, ICML.

# References

C.D. Manning, P. Raghavan and H. Schuetze (2008). Introduction to Information Retrieval. Cambridge University Press, pp. 234-265. https://nlp.stanford.edu/IR-book/html/htmledition/naive-bayes-text-classification-1. html

# **Examples**

```
>>> import numpy as np
>>> X = np.random.randint(5, size=(6, 100))
>>> y = np.array([1, 2, 3, 4, 5, 6])
>>> from sklearn.naive_bayes import MultinomialNB
>>> clf = MultinomialNB()
>>> clf.fit(X, y)
MultinomialNB(alpha=1.0, class_prior=None, fit_prior=True)
>>> print(clf.predict(X[2:3]))
[3]
```

## Methods

fit(self, X, y[, sample_weight])	Fit Naive Bayes classifier according to X, y	
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.	
partial_fit(self, X, y[, classes, sample_weight]) Incremental fit on a batch of samples.		
predict(self, X) Perform classification on an array of test vectors		
<pre>predict_log_proba(self, X)</pre>	Return log-probability estimates for the test vector X.	
<pre>predict_proba(self, X)</pre>	Return probability estimates for the test vector X.	
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and	
	labels.	
set_params(self, \*\*params)	Set the parameters of this estimator.	

```
__init__ (self, alpha=1.0, fit_prior=True, class_prior=None)
```

fit (self, X, y, sample\_weight=None)

Fit Naive Bayes classifier according to X, y

## **Parameters**

**X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.

**y** [array-like, shape = [n\_samples]] Target values.

**sample\_weight** [array-like, shape = [n\_samples], (default=None)] Weights applied to individual samples (1. for unweighted).

# Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

partial\_fit (self, X, y, classes=None, sample\_weight=None)

Incremental fit on a batch of samples.

This method is expected to be called several times consecutively on different chunks of a dataset so as to implement out-of-core or online learning.

This is especially useful when the whole dataset is too big to fit in memory at once.

This method has some performance overhead hence it is better to call partial\_fit on chunks of data that are as large as possible (as long as fitting in the memory budget) to hide the overhead.

## **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape = [n\_samples]] Target values.

**classes** [array-like, shape = [n\_classes] (default=None)] List of all the classes that can possibly appear in the y vector.

Must be provided at the first call to partial\_fit, can be omitted in subsequent calls.

**sample\_weight** [array-like, shape = [n\_samples] (default=None)] Weights applied to individual samples (1. for unweighted).

#### Returns

self [object]

# predict (self, X)

Perform classification on an array of test vectors X.

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

# Returns

 $\mathbb{C}$  [array, shape = [n\_samples]] Predicted target values for X

# $predict_log_proba(self, X)$

Return log-probability estimates for the test vector X.

# **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

# Returns

**C** [array-like, shape = [n\_samples, n\_classes]] Returns the log-probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

# predict proba(self, X)

Return probability estimates for the test vector X.

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

## **Returns**

**C** [array-like, shape = [n\_samples, n\_classes]] Returns the probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## **Returns**

self

# Examples using sklearn.naive bayes.MultinomialNB

- Out-of-core classification of text documents
- · Classification of text documents using sparse features

# 6.29.4 sklearn.naive\_bayes.ComplementNB

The Complement Naive Bayes classifier described in Rennie et al. (2003).

The Complement Naive Bayes classifier was designed to correct the "severe assumptions" made by the standard Multinomial Naive Bayes classifier. It is particularly suited for imbalanced data sets.

Read more in the User Guide.

# **Parameters**

**alpha** [float, optional (default=1.0)] Additive (Laplace/Lidstone) smoothing parameter (0 for no smoothing).

**fit\_prior** [boolean, optional (default=True)] Only used in edge case with a single class in the training set.

**class\_prior** [array-like, size (n\_classes,), optional (default=None)] Prior probabilities of the classes. Not used.

**norm** [boolean, optional (default=False)] Whether or not a second normalization of the weights is performed. The default behavior mirrors the implementations found in Mahout and Weka, which do not follow the full algorithm described in Table 9 of the paper.

# **Attributes**

**class\_log\_prior\_** [array, shape (n\_classes, )] Smoothed empirical log probability for each class. Only used in edge case with a single class in the training set.

- **feature\_log\_prob\_** [array, shape (n\_classes, n\_features)] Empirical weights for class complements.
- **class\_count\_** [array, shape (n\_classes,)] Number of samples encountered for each class during fitting. This value is weighted by the sample weight when provided.
- **feature\_count\_** [array, shape (n\_classes, n\_features)] Number of samples encountered for each (class, feature) during fitting. This value is weighted by the sample weight when provided.
- **feature\_all\_** [array, shape (n\_features,)] Number of samples encountered for each feature during fitting. This value is weighted by the sample weight when provided.

## References

Rennie, J. D., Shih, L., Teevan, J., & Karger, D. R. (2003). Tackling the poor assumptions of naive bayes text classifiers. In ICML (Vol. 3, pp. 616-623). https://people.csail.mit.edu/jrennie/papers/icml03-nb.pdf

# **Examples**

```
>>> import numpy as np
>>> X = np.random.randint(5, size=(6, 100))
>>> y = np.array([1, 2, 3, 4, 5, 6])
>>> from sklearn.naive_bayes import ComplementNB
>>> clf = ComplementNB()
>>> clf.fit(X, y)
ComplementNB(alpha=1.0, class_prior=None, fit_prior=True, norm=False)
>>> print(clf.predict(X[2:3]))
[3]
```

# **Methods**

fit(self, X, y[, sample_weight])	Fit Naive Bayes classifier according to X, y	
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.	
<pre>partial_fit(self, X, y[, classes, sample_weight])</pre>	Incremental fit on a batch of samples.	
predict(self, X)	Perform classification on an array of test vectors X.	
predict_log_proba(self, X)	roba(self, X) Return log-probability estimates for the test vector X.	
Predict_proba(self, X) Return probability estimates for the test vector X		
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and	
	labels.	
set_params(self, \*\*params)	Set the parameters of this estimator.	

```
__init__ (self, alpha=1.0, fit_prior=True, class_prior=None, norm=False)

fit (self, X, y, sample_weight=None)

Fit Naive Bayes classifier according to X, y
```

## **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.
- y [array-like, shape = [n\_samples]] Target values.

**sample\_weight** [array-like, shape = [n\_samples], (default=None)] Weights applied to individual samples (1. for unweighted).

## Returns

self [object]

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
partial_fit (self, X, y, classes=None, sample_weight=None)
```

Incremental fit on a batch of samples.

This method is expected to be called several times consecutively on different chunks of a dataset so as to implement out-of-core or online learning.

This is especially useful when the whole dataset is too big to fit in memory at once.

This method has some performance overhead hence it is better to call partial\_fit on chunks of data that are as large as possible (as long as fitting in the memory budget) to hide the overhead.

### **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vectors, where n\_samples is the number of samples and n\_features is the number of features.
- **y** [array-like, shape = [n\_samples]] Target values.

**classes** [array-like, shape =  $[n_{classes}]$  (default=None)] List of all the classes that can possibly appear in the y vector.

Must be provided at the first call to partial\_fit, can be omitted in subsequent calls.

**sample\_weight** [array-like, shape = [n\_samples] (default=None)] Weights applied to individual samples (1. for unweighted).

## Returns

self [object]

# predict (self, X)

Perform classification on an array of test vectors X.

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

## Returns

 $\mathbf{C}$  [array, shape = [n\_samples]] Predicted target values for  $\mathbf{X}$ 

## predict\_log\_proba (self, X)

Return log-probability estimates for the test vector X.

# **Parameters**

X [array-like, shape = [n samples, n features]]

## Returns

**C** [array-like, shape = [n\_samples, n\_classes]] Returns the log-probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

# predict\_proba (self, X)

Return probability estimates for the test vector X.

### **Parameters**

X [array-like, shape = [n samples, n features]]

# Returns

**C** [array-like, shape = [n\_samples, n\_classes]] Returns the probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

# score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# Examples using sklearn.naive\_bayes.ComplementNB

• Classification of text documents using sparse features

# 6.30 sklearn.neighbors: Nearest Neighbors

The sklearn.neighbors module implements the k-nearest neighbors algorithm.

User guide: See the *Nearest Neighbors* section for further details.

neighbors.BallTree	BallTree for fast generalized N-point problems
neighbors.DistanceMetric	DistanceMetric class
neighbors.KDTree	KDTree for fast generalized N-point problems

Continued on next page

Table 6.223 – continued from previous page

Tallion Chillips			
neighbors.KernelDensity([bandwidth,])	Kernel Density Estimation		
neighbors.KNeighborsClassifier([])	Classifier implementing the k-nearest neighbors vote.		
neighbors.KNeighborsRegressor([n_neighbors,	Regression based on k-nearest neighbors.		
])			
neighbors.LocalOutlierFactor([n_neighbors,	Unsupervised Outlier Detection using Local Outlier Factor		
])	(LOF)		
neighbors.RadiusNeighborsClassifier([])	Classifier implementing a vote among neighbors within a		
	given radius		
neighbors.RadiusNeighborsRegressor([radius,	Regression based on neighbors within a fixed radius.		
])			
neighbors.NearestCentroid([metric,])	Nearest centroid classifier.		
neighbors.NearestNeighbors([n_neighbors,	Unsupervised learner for implementing neighbor searches.		
])			
neighbors.NeighborhoodComponentsAnalysis([Ne]ghborhood Components Analysis			

# 6.30.1 sklearn.neighbors.BallTree

class sklearn.neighbors.BallTree

BallTree for fast generalized N-point problems

BallTree(X, leaf\_size=40, metric='minkowski', \*\*kwargs)

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] n\_samples is the number of points in the data set, and n\_features is the dimension of the parameter space. Note: if X is a C-contiguous array of doubles then data will not be copied. Otherwise, an internal copy will be made.

leaf\_size [positive integer (default = 40)] Number of points at which to switch to brute-force.
 Changing leaf\_size will not affect the results of a query, but can significantly impact the speed of a query and the memory required to store the constructed tree. The amount of memory needed to store the tree scales as approximately n\_samples / leaf\_size. For a specified leaf\_size, a leaf node is guaranteed to satisfy leaf\_size <= n\_points <= 2 \* leaf\_size, except in the case that n\_samples < leaf\_size.</pre>

metric [string or DistanceMetric object] the distance metric to use for the tree. Default='minkowski' with p=2 (that is, a euclidean metric). See the documentation of the DistanceMetric class for a list of available metrics. ball\_tree.valid\_metrics gives a list of the metrics which are valid for BallTree.

Additional keywords are passed to the distance metric class.

## Attributes

data [memory view] The training data

# **Examples**

Query for k-nearest neighbors

```
>>> import numpy as np
>>> rng = np.random.RandomState(0)
>>> X = rng.random_sample((10, 3)) # 10 points in 3 dimensions
>>> tree = BallTree(X, leaf_size=2)
>>> dist, ind = tree.query(X[:1], k=3)
```

```
>>> print(ind)  # indices of 3 closest neighbors
[0 3 1]
>>> print(dist)  # distances to 3 closest neighbors
[0. 0.19662693 0.29473397]
```

Pickle and Unpickle a tree. Note that the state of the tree is saved in the pickle operation: the tree needs not be rebuilt upon unpickling.

```
>>> import numpy as np
>>> import pickle
>>> rng = np.random.RandomState(0)
>>> X = rng.random_sample((10, 3)) # 10 points in 3 dimensions
>>> tree = BallTree(X, leaf_size=2)
>>> s = pickle.dumps(tree)
>>> tree_copy = pickle.loads(s)
>>> dist, ind = tree_copy.query(X[:1], k=3)
>>> print(ind) # indices of 3 closest neighbors
[0 3 1]
>>> print(dist) # distances to 3 closest neighbors
[0 0.19662693 0.29473397]
```

Query for neighbors within a given radius

```
>>> import numpy as np
>>> rng = np.random.RandomState(0)
>>> X = rng.random_sample((10, 3)) # 10 points in 3 dimensions
>>> tree = BallTree(X, leaf_size=2)
>>> print(tree.query_radius(X[:1], r=0.3, count_only=True))
3
>>> ind = tree.query_radius(X[:1], r=0.3)
>>> print(ind) # indices of neighbors within distance 0.3
[3 0 1]
```

Compute a gaussian kernel density estimate:

```
>>> import numpy as np
>>> rng = np.random.RandomState(42)
>>> X = rng.random_sample((100, 3))
>>> tree = BallTree(X)
>>> tree.kernel_density(X[:3], h=0.1, kernel='gaussian')
array([ 6.94114649, 7.83281226, 7.2071716 ])
```

Compute a two-point auto-correlation function

```
>>> import numpy as np
>>> rng = np.random.RandomState(0)
>>> X = rng.random_sample((30, 3))
>>> r = np.linspace(0, 1, 5)
>>> tree = BallTree(X)
>>> tree.two_point_correlation(X, r)
array([ 30, 62, 278, 580, 820])
```

**Methods** 

kernel_density(self, X, h[, kernel, atol,])	Compute the kernel density estimate at points X with the given kernel, using the distance metric specified at tree creation.
query(X[, k, return_distance, dualtree,])	query the tree for the k nearest neighbors
query_radius()	query_radius(self, X, r, count_only = False):
two_point_correlation()	Compute the two-point correlation function

	_
get_arrays	
get_n_calls	
get_tree_stats	
reset_n_calls	

\_\_\_init\_\_\_(self, /, \*args, \*\*kwargs)

Initialize self. See help(type(self)) for accurate signature.

**kernel\_density** (self, X, h, kernel='gaussian', atol=0, rtol=1E-8,  $breadth\_first=True$ ,  $return\_log=False$ )

Compute the kernel density estimate at points X with the given kernel, using the distance metric specified at tree creation.

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] An array of points to query. Last dimension should match dimension of training data.

**h** [float] the bandwidth of the kernel

**kernel** [string] specify the kernel to use. Options are - 'gaussian' - 'tophat' - 'epanechnikov' - 'exponential' - 'linear' - 'cosine' Default is kernel = 'gaussian'

atol, rtol [float (default = 0)] Specify the desired relative and absolute tolerance of the result. If the true result is K\_true, then the returned result K\_ret satisfies abs (K\_true K\_ret) < atol + rtol \* K\_ret The default is zero (i.e. machine precision) for
both.</pre>

breadth\_first [boolean (default = False)] if True, use a breadth-first search. If False (default)
use a depth-first search. Breadth-first is generally faster for compact kernels and/or high
tolerances.

**return\_log** [boolean (default = False)] return the logarithm of the result. This can be more accurate than returning the result itself for narrow kernels.

## Returns

**density** [ndarray] The array of (log)-density evaluations, shape = X.shape[:-1]

**query**  $(X, k=1, return\_distance=True, dualtree=False, breadth\_first=False)$  query the tree for the k nearest neighbors

# **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] An array of points to query

 $\mathbf{k}$  [integer (default = 1)] The number of nearest neighbors to return

**return\_distance** [boolean (default = True)] if True, return a tuple (d, i) of distances and indices if False, return array i

- **dualtree** [boolean (default = False)] if True, use the dual tree formalism for the query: a tree is built for the query points, and the pair of trees is used to efficiently search this space. This can lead to better performance as the number of points grows large.
- **breadth\_first** [boolean (default = False)] if True, then query the nodes in a breadth-first manner. Otherwise, query the nodes in a depth-first manner.
- **sort\_results** [boolean (default = True)] if True, then distances and indices of each point are sorted on return, so that the first column contains the closest points. Otherwise, neighbors are returned in an arbitrary order.

## **Returns**

- i [if return\_distance == False]
- (**d,i**) [if return\_distance == True]
- **d** [array of doubles shape: x.shape[:-1] + (k,)] each entry gives the list of distances to the neighbors of the corresponding point
- i [array of integers shape: x.shape[:-1] + (k,)] each entry gives the list of indices of neighbors of the corresponding point

# query radius()

```
query_radius(self, X, r, count_only = False):
```

query the tree for neighbors within a radius r

# **Parameters**

- $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] An array of points to query
- r [distance within which neighbors are returned] r can be a single value, or an array of values of shape x.shape[:-1] if different radii are desired for each point.
- return\_distance [boolean (default = False)] if True, return distances to neighbors of each point if False, return only neighbors Note that unlike the query() method, setting return\_distance=True here adds to the computation time. Not all distances need to be calculated explicitly for return\_distance=False. Results are not sorted by default: see sort\_results keyword.
- **count\_only** [boolean (default = False)] if True, return only the count of points within distance r if False, return the indices of all points within distance r If return\_distance==True, setting count\_only=True will result in an error.
- **sort\_results** [boolean (default = False)] if True, the distances and indices will be sorted before being returned. If False, the results will not be sorted. If return\_distance == False, setting sort\_results = True will result in an error.

# Returns

```
count [if count_only == True]
```

ind [if count\_only == False and return\_distance == False]

(ind, dist) [if count\_only == False and return\_distance == True]

**count** [array of integers, shape = X.shape[:-1]] each entry gives the number of neighbors within a distance r of the corresponding point.

ind [array of objects, shape = X.shape[:-1]] each element is a numpy integer array listing the indices of neighbors of the corresponding point. Note that unlike the results of a kneighbors query, the returned neighbors are not sorted by distance by default.

**dist** [array of objects, shape = X.shape[:-1]] each element is a numpy double array listing the distances corresponding to indices in i.

# two\_point\_correlation()

Compute the two-point correlation function

# **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] An array of points to query. Last dimension should match dimension of training data.
- r [array\_like] A one-dimensional array of distances

**dualtree** [boolean (default = False)] If true, use a dualtree algorithm. Otherwise, use a single-tree algorithm. Dual tree algorithms can have better scaling for large N.

## **Returns**

**counts** [ndarray] counts[i] contains the number of pairs of points with distance less than or equal to r[i]

# 6.30.2 sklearn.neighbors.DistanceMetric

class sklearn.neighbors.DistanceMetric

DistanceMetric class

This class provides a uniform interface to fast distance metric functions. The various metrics can be accessed via the <code>get\_metric</code> class method and the metric string identifier (see below). For example, to use the Euclidean distance:

Available Metrics

The following lists the string metric identifiers and the associated distance metric classes:

Metrics intended for real-valued vector spaces:

identifier	class name	args	distance function
"euclidean"	EuclideanDistance		sqrt(sum((x -
		•	y)^2))
"manhattan"	ManhattanDistance		sum( x - y )
		•	
"chebyshev"	ChebyshevDistance		max( x - y )
		•	
"minkowski"	MinkowskiDistance	p	sum( x -
			y ^p)^(1/p)
"wminkowski"	WMinkowskiDistance	p, w	sum( w * (x -
			y)  ^p)^(1/p)
"seuclidean"	SEuclideanDistance	V	sqrt(sum((x -
			y)^2 / V))
"mahalanobis"	MahalanobisDistance	V or VI	sqrt((x - y)'
			V^-1 (x - y))

**Metrics intended for two-dimensional vector spaces:** Note that the haversine distance metric requires data in the form of [latitude, longitude] and both inputs and outputs are in units of radians.

identifier	class name	distance function
"haver-	HaversineDis-	2 arcsin(sqrt(sin^2(0.5*dx) +
sine"	tance	$cos(x1)cos(x2)sin^2(0.5*dy)))$

**Metrics intended for integer-valued vector spaces:** Though intended for integer-valued vectors, these are also valid metrics in the case of real-valued vectors.

identifier	class name	distance function	
"hamming"	HammingDistance	N_unequal(x, y) / N_tot	
"canberra"	CanberraDistance	sum( x - y  / ( x  +  y ))	
"braycurtis"	BrayCurtisDistance	sum( x - y ) / (sum( x ) + sum( y ))	

**Metrics intended for boolean-valued vector spaces:** Any nonzero entry is evaluated to "True". In the listings below, the following abbreviations are used:

- N : number of dimensions
- NTT: number of dims in which both values are True
- NTF: number of dims in which the first value is True, second is False
- NFT: number of dims in which the first value is False, second is True
- · NFF: number of dims in which both values are False
- NNEQ : number of non-equal dimensions, NNEQ = NTF + NFT
- NNZ : number of nonzero dimensions, NNZ = NTF + NFT + NTT

identifier	class name	distance function
"jaccard"	JaccardDistance	NNEQ / NNZ
"matching"	MatchingDistance	NNEQ / N
"dice"	" DiceDistance NNEQ / (NTT + NNZ)	
"kulsinski"	KulsinskiDistance	(NNEQ + N - NTT) / (NNEQ + N)
"rogerstanimoto"	RogersTanimotoDistance	2 * NNEQ / (N + NNEQ)
"russellrao"	RussellRaoDistance	NNZ / N
"sokalmichener"	SokalMichenerDistance	2 * NNEQ / (N + NNEQ)
"sokalsneath"	SokalSneathDistance	NNEQ / (NNEQ + 0.5 * NTT)

# **User-defined distance:**

identifier	class name	args
"pyfunc"	PyFuncDistance	func

Here func is a function which takes two one-dimensional numpy arrays, and returns a distance. Note that in order to be used within the BallTree, the distance must be a true metric: i.e. it must satisfy the following properties

- 1. Non-negativity: d(x, y) >= 0
- 2. Identity: d(x, y) = 0 if and only if x == y
- 3. Symmetry: d(x, y) = d(y, x)
- 4. Triangle Inequality: d(x, y) + d(y, z) >= d(x, z)

Because of the Python object overhead involved in calling the python function, this will be fairly slow, but it will have the same scaling as other distances.

# **Methods**

dist_to_rdist()	Convert the true distance to the reduced distance.
<pre>get_metric()</pre>	Get the given distance metric from the string identifier.
pairwise()	Compute the pairwise distances between X and Y
rdist_to_dist()	Convert the Reduced distance to the true distance.

\_\_init\_\_ (self, /, \*args, \*\*kwargs)

Initialize self. See help(type(self)) for accurate signature.

## dist\_to\_rdist()

Convert the true distance to the reduced distance.

The reduced distance, defined for some metrics, is a computationally more efficient measure which preserves the rank of the true distance. For example, in the Euclidean distance metric, the reduced distance is the squared-euclidean distance.

## get metric()

Get the given distance metric from the string identifier.

See the docstring of DistanceMetric for a list of available metrics.

# **Parameters**

metric [string or class name] The distance metric to use

\*\*kwargs additional arguments will be passed to the requested metric

## pairwise()

Compute the pairwise distances between X and Y

This is a convenience routine for the sake of testing. For many metrics, the utilities in scipy.spatial.distance.cdist and scipy.spatial.distance.pdist will be faster.

## **Parameters**

- **X** [array like] Array of shape (Nx, D), representing Nx points in D dimensions.
- **Y** [array\_like (optional)] Array of shape (Ny, D), representing Ny points in D dimensions. If not specified, then Y=X.

#### Returns

dist [ndarray] The shape (Nx, Ny) array of pairwise distances between points in X and Y.

# rdist\_to\_dist()

Convert the Reduced distance to the true distance.

The reduced distance, defined for some metrics, is a computationally more efficient measure which preserves the rank of the true distance. For example, in the Euclidean distance metric, the reduced distance is the squared-euclidean distance.

# 6.30.3 sklearn.neighbors.KDTree

```
class sklearn.neighbors.KDTree
```

KDTree for fast generalized N-point problems

KDTree(X, leaf\_size=40, metric='minkowski', \*\*kwargs)

# **Parameters**

- X [array-like, shape = [n\_samples, n\_features]] n\_samples is the number of points in the data set, and n\_features is the dimension of the parameter space. Note: if X is a C-contiguous array of doubles then data will not be copied. Otherwise, an internal copy will be made.
- leaf\_size [positive integer (default = 40)] Number of points at which to switch to brute-force.
   Changing leaf\_size will not affect the results of a query, but can significantly impact the speed of a query and the memory required to store the constructed tree. The amount of memory needed to store the tree scales as approximately n\_samples / leaf\_size. For a specified leaf\_size, a leaf node is guaranteed to satisfy leaf\_size <= n\_points <= 2 \* leaf\_size, except in the case that n\_samples < leaf\_size.</pre>
- metric [string or DistanceMetric object] the distance metric to use for the tree. Default='minkowski' with p=2 (that is, a euclidean metric). See the documentation of the DistanceMetric class for a list of available metrics. kd\_tree.valid\_metrics gives a list of the metrics which are valid for KDTree.

Additional keywords are passed to the distance metric class.

# **Attributes**

data [memory view] The training data

# **Examples**

Query for k-nearest neighbors

```
>>> import numpy as np
>>> rng = np.random.RandomState(0)
>>> X = rng.random_sample((10, 3)) # 10 points in 3 dimensions
>>> tree = KDTree(X, leaf_size=2)
>>> dist, ind = tree.query(X[:1], k=3)
>>> print(ind) # indices of 3 closest neighbors
[0 3 1]
>>> print(dist) # distances to 3 closest neighbors
[0 0.19662693 0.29473397]
```

Pickle and Unpickle a tree. Note that the state of the tree is saved in the pickle operation: the tree needs not be rebuilt upon unpickling.

```
>>> import numpy as np
>>> import pickle
>>> rng = np.random.RandomState(0)
>>> X = rng.random_sample((10, 3)) # 10 points in 3 dimensions
>>> tree = KDTree(X, leaf_size=2)
>>> s = pickle.dumps(tree)
>>> tree_copy = pickle.loads(s)
>>> dist, ind = tree_copy.query(X[:1], k=3)
>>> print(ind) # indices of 3 closest neighbors
[0 3 1]
>>> print(dist) # distances to 3 closest neighbors
[0 0.19662693 0.29473397]
```

Query for neighbors within a given radius

```
>>> import numpy as np
>>> rng = np.random.RandomState(0)
>>> X = rng.random_sample((10, 3)) # 10 points in 3 dimensions
>>> tree = KDTree(X, leaf_size=2)
>>> print(tree.query_radius(X[:1], r=0.3, count_only=True))
3
>>> ind = tree.query_radius(X[:1], r=0.3)
>>> print(ind) # indices of neighbors within distance 0.3
[3 0 1]
```

Compute a gaussian kernel density estimate:

```
>>> import numpy as np
>>> rng = np.random.RandomState(42)
>>> X = rng.random_sample((100, 3))
>>> tree = KDTree(X)
>>> tree.kernel_density(X[:3], h=0.1, kernel='gaussian')
array([ 6.94114649, 7.83281226, 7.2071716 ])
```

Compute a two-point auto-correlation function

```
>>> import numpy as np
>>> rng = np.random.RandomState(0)
>>> X = rng.random_sample((30, 3))
>>> r = np.linspace(0, 1, 5)
>>> tree = KDTree(X)
```

```
>>> tree.two_point_correlation(X, r) array([ 30, 62, 278, 580, 820])
```

# **Methods**

kernel_density(self, X, h[, kernel, atol,])	Compute the kernel density estimate at points X with the given kernel, using the distance metric specified at tree creation.
query(X[, k, return_distance, dualtree,])	query the tree for the k nearest neighbors
query_radius()	query_radius(self, X, r, count_only = False):
two_point_correlation()	Compute the two-point correlation function

get_arrays	
get_n_calls	
get_tree_stats	
reset_n_calls	

```
___init___(self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

**kernel\_density**(self, X, h, kernel='gaussian', atol=0, rtol=1E-8, breadth\_first=True, return log=False)

Compute the kernel density estimate at points X with the given kernel, using the distance metric specified at tree creation.

# **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] An array of points to query. Last dimension should match dimension of training data.

**h** [float] the bandwidth of the kernel

**kernel** [string] specify the kernel to use. Options are - 'gaussian' - 'tophat' - 'epanechnikov' - 'exponential' - 'linear' - 'cosine' Default is kernel = 'gaussian'

atol, rtol [float (default = 0)] Specify the desired relative and absolute tolerance of the result. If the true result is K\_true, then the returned result K\_ret satisfies abs (K\_true K\_ret) < atol + rtol \* K\_ret The default is zero (i.e. machine precision) for
both.</pre>

**breadth\_first** [boolean (default = False)] if True, use a breadth-first search. If False (default) use a depth-first search. Breadth-first is generally faster for compact kernels and/or high tolerances.

**return\_log** [boolean (default = False)] return the logarithm of the result. This can be more accurate than returning the result itself for narrow kernels.

## Returns

**density** [ndarray] The array of (log)-density evaluations, shape = X.shape[:-1]

**query**  $(X, k=1, return\_distance=True, dualtree=False, breadth\_first=False)$  query the tree for the k nearest neighbors

## **Parameters**

- $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] An array of points to query
- $\mathbf{k}$  [integer (default = 1)] The number of nearest neighbors to return
- **return\_distance** [boolean (default = True)] if True, return a tuple (d, i) of distances and indices if False, return array i
- **dualtree** [boolean (default = False)] if True, use the dual tree formalism for the query: a tree is built for the query points, and the pair of trees is used to efficiently search this space. This can lead to better performance as the number of points grows large.
- **breadth\_first** [boolean (default = False)] if True, then query the nodes in a breadth-first manner. Otherwise, query the nodes in a depth-first manner.
- **sort\_results** [boolean (default = True)] if True, then distances and indices of each point are sorted on return, so that the first column contains the closest points. Otherwise, neighbors are returned in an arbitrary order.

## Returns

- i [if return\_distance == False]
- (**d,i**) [if return\_distance == True]
- **d** [array of doubles shape: x.shape[:-1] + (k,)] each entry gives the list of distances to the neighbors of the corresponding point
- i [array of integers shape: x.shape[:-1] + (k,)] each entry gives the list of indices of neighbors of the corresponding point

## query radius()

```
query_radius(self, X, r, count_only = False):
```

query the tree for neighbors within a radius r

# **Parameters**

- $\mathbf{X}$  [array-like, shape = [n\_samples, n\_features]] An array of points to query
- r [distance within which neighbors are returned] r can be a single value, or an array of values of shape x.shape[:-1] if different radii are desired for each point.
- **return\_distance** [boolean (default = False)] if True, return distances to neighbors of each point if False, return only neighbors Note that unlike the query() method, setting return\_distance=True here adds to the computation time. Not all distances need to be calculated explicitly for return\_distance=False. Results are not sorted by default: see sort results keyword.
- **count\_only** [boolean (default = False)] if True, return only the count of points within distance r if False, return the indices of all points within distance r If return\_distance==True, setting count\_only=True will result in an error.
- **sort\_results** [boolean (default = False)] if True, the distances and indices will be sorted before being returned. If False, the results will not be sorted. If return\_distance == False, setting sort\_results = True will result in an error.

## **Returns**

```
count [if count_only == True]
ind [if count_only == False and return_distance == False]
(ind, dist) [if count_only == False and return_distance == True]
```

- **count** [array of integers, shape = X.shape[:-1]] each entry gives the number of neighbors within a distance r of the corresponding point.
- ind [array of objects, shape = X.shape[:-1]] each element is a numpy integer array listing the indices of neighbors of the corresponding point. Note that unlike the results of a kneighbors query, the returned neighbors are not sorted by distance by default.
- **dist** [array of objects, shape = X.shape[:-1]] each element is a numpy double array listing the distances corresponding to indices in i.

# two\_point\_correlation()

Compute the two-point correlation function

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] An array of points to query. Last dimension should match dimension of training data.
- r [array\_like] A one-dimensional array of distances
- **dualtree** [boolean (default = False)] If true, use a dualtree algorithm. Otherwise, use a single-tree algorithm. Dual tree algorithms can have better scaling for large N.

### Returns

**counts** [ndarray] counts[i] contains the number of pairs of points with distance less than or equal to r[i]

# 6.30.4 sklearn.neighbors.KernelDensity

Kernel Density Estimation

Read more in the *User Guide*.

# **Parameters**

bandwidth [float] The bandwidth of the kernel.

**algorithm** [string] The tree algorithm to use. Valid options are ['kd\_tree'l'ball\_tree'l'auto']. Default is 'auto'.

- **kernel** [string] The kernel to use. Valid kernels are ['gaussian'l'tophat'l'epanechnikov'l'exponential'l'linear'l'cosine'] Default is 'gaussian'.
- **metric** [string] The distance metric to use. Note that not all metrics are valid with all algorithms. Refer to the documentation of <code>BallTree</code> and <code>KDTree</code> for a description of available algorithms. Note that the normalization of the density output is correct only for the Euclidean distance metric. Default is 'euclidean'.
- **atol** [float] The desired absolute tolerance of the result. A larger tolerance will generally lead to faster execution. Default is 0.
- **rtol** [float] The desired relative tolerance of the result. A larger tolerance will generally lead to faster execution. Default is 1E-8.
- **breadth\_first** [boolean] If true (default), use a breadth-first approach to the problem. Otherwise use a depth-first approach.
- **leaf\_size** [int] Specify the leaf size of the underlying tree. See BallTree or KDTree for details. Default is 40.

**metric\_params** [dict] Additional parameters to be passed to the tree for use with the metric. For more information, see the documentation of BallTree or KDTree.

# **Methods**

fit(self, X[, y, sample_weight])	Fit the Kernel Density model on the data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
sample(self[, n_samples, random_state])	Generate random samples from the model.
score(self, X[, y])	Compute the total log probability density under the
	model.
score_samples(self, X)	Evaluate the density model on the data.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, bandwidth=1.0, algorithm='auto', kernel='gaussian', metric='euclidean', atol=0, rtol=0, breadth\_first=True, leaf\_size=40, metric\_params=None)

fit (self, X, y=None, sample\_weight=None)

Fit the Kernel Density model on the data.

## **Parameters**

**X** [array\_like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

**sample\_weight** [array\_like, shape (n\_samples,), optional] List of sample weights attached to the data X.

get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

sample (self, n\_samples=1, random\_state=None)

Generate random samples from the model.

Currently, this is implemented only for gaussian and tophat kernels.

## **Parameters**

**n\_samples** [int, optional] Number of samples to generate. Defaults to 1.

random\_state [int, RandomState instance or None. default to None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

## **Returns**

**X** [array\_like, shape (n\_samples, n\_features)] List of samples.

score(self, X, y=None)

Compute the total log probability density under the model.

## **Parameters**

**X** [array\_like, shape (n\_samples, n\_features)] List of n\_features-dimensional data points. Each row corresponds to a single data point.

## Returns

**logprob** [float] Total log-likelihood of the data in X. This is normalized to be a probability density, so the value will be low for high-dimensional data.

# $score\_samples(self, X)$

Evaluate the density model on the data.

# **Parameters**

**X** [array\_like, shape (n\_samples, n\_features)] An array of points to query. Last dimension should match dimension of training data (n\_features).

## **Returns**

**density** [ndarray, shape (n\_samples,)] The array of log(density) evaluations. These are normalized to be probability densities, so values will be low for high-dimensional data.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# Examples using sklearn.neighbors.KernelDensity

- Kernel Density Estimation
- Kernel Density Estimate of Species Distributions
- Simple 1D Kernel Density Estimation

# 6.30.5 sklearn.neighbors.KNeighborsClassifier

Classifier implementing the k-nearest neighbors vote.

Read more in the *User Guide*.

## **Parameters**

**n\_neighbors** [int, optional (default = 5)] Number of neighbors to use by default for *kneighbors* queries.

weights [str or callable, optional (default = 'uniform')] weight function used in prediction. Possible values:

- 'uniform' : uniform weights. All points in each neighborhood are weighted equally.
- 'distance': weight points by the inverse of their distance. in this case, closer neighbors of a query point will have a greater influence than neighbors which are further away.

- [callable]: a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights.
- **algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] Algorithm used to compute the nearest neighbors:
  - 'ball tree' will use BallTree
  - 'kd tree' will use KDTree
  - 'brute' will use a brute-force search.
  - 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.

- **leaf\_size** [int, optional (default = 30)] Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.
- **p** [integer, optional (default = 2)] Power parameter for the Minkowski metric. When p = 1, this is equivalent to using manhattan\_distance (11), and euclidean\_distance (12) for p = 2. For arbitrary p, minkowski\_distance (1\_p) is used.
- **metric** [string or callable, default 'minkowski'] the distance metric to use for the tree. The default metric is minkowski, and with p=2 is equivalent to the standard Euclidean metric. See the documentation of the DistanceMetric class for a list of available metrics.
- **metric\_params** [dict, optional (default = None)] Additional keyword arguments for the metric function.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details. Doesn't affect *fit* method.

## See also:

RadiusNeighborsClassifier KNeighborsRegressor RadiusNeighborsRegressor NearestNeighbors

# **Notes**

See *Nearest Neighbors* in the online documentation for a discussion of the choice of algorithm and leaf\_size.

**Warning:** Regarding the Nearest Neighbors algorithms, if it is found that two neighbors, neighbor k+1 and k, have identical distances but different labels, the results will depend on the ordering of the training data.

https://en.wikipedia.org/wiki/K-nearest neighbor algorithm

# **Examples**

```
>>> X = [[0], [1], [2], [3]]
>>> y = [0, 0, 1, 1]
>>> from sklearn.neighbors import KNeighborsClassifier
>>> neigh = KNeighborsClassifier(n_neighbors=3)
>>> neigh.fit(X, y)
KNeighborsClassifier(...)
>>> print(neigh.predict([[1.1]]))
[0]
>>> print(neigh.predict_proba([[0.9]]))
[[0.666666667 0.333333333]]
```

# **Methods**

fit(self, X, y)	Fit the model using X as training data and y as target
	values
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
kneighbors(self[, X, n_neighbors,])	Finds the K-neighbors of a point.
kneighbors_graph(self[, X, n_neighbors, mode])	Computes the (weighted) graph of k-Neighbors for
	points in X
predict(self, X)	Predict the class labels for the provided data
predict_proba(self, X)	Return probability estimates for the test data X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__(self, n_neighbors=5, weights='uniform', algorithm='auto', leaf_size=30, p=2, met-
ric='minkowski', metric_params=None, n_jobs=None, **kwargs)
```

# **fit** (self, X, y)

Fit the model using X as training data and y as target values

# **Parameters**

- **X** [{array-like, sparse matrix, BallTree, KDTree}] Training data. If array or matrix, shape [n\_samples, n\_features], or [n\_samples, n\_samples] if metric='precomputed'.
- y [{array-like, sparse matrix}] Target values of shape = [n\_samples] or [n\_samples, n\_outputs]

# get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

 $\verb+kneighbors+ (self, X=None, n\_neighbors=None, return\_distance=True)$ 

Finds the K-neighbors of a point. Returns indices of and distances to the neighbors of each point.

# **Parameters**

- **X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.
- n\_neighbors [int] Number of neighbors to get (default is the value passed to the constructor).
- **return\_distance** [boolean, optional. Defaults to True.] If False, distances will not be returned

## **Returns**

**dist** [array] Array representing the lengths to points, only present if return\_distance=True **ind** [array] Indices of the nearest points in the population matrix.

# **Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who's the closest point to [1,1,1]

```
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=1)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> print(neigh.kneighbors([[1., 1., 1.]]))
(array([[0.5]]), array([[2]]))
```

As you can see, it returns [[0.5]], and [[2]], which means that the element is at distance 0.5 and is the third element of samples (indexes start at 0). You can also query for multiple points:

**kneighbors\_graph** (*self*, *X=None*, *n\_neighbors=None*, *mode='connectivity'*)

Computes the (weighted) graph of k-Neighbors for points in X

## **Parameters**

- **X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.
- **n\_neighbors** [int] Number of neighbors for each sample. (default is value passed to the constructor).
- **mode** [{'connectivity', 'distance'}, optional] Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, in 'distance' the edges are Euclidean distance between points.

# Returns

A [sparse matrix in CSR format, shape = [n\_samples, n\_samples\_fit]] n\_samples\_fit is the number of samples in the fitted data A[i, j] is assigned the weight of edge that connects i to j.

See also:

# NearestNeighbors.radius\_neighbors\_graph

# **Examples**

## predict (self, X)

Predict the class labels for the provided data

## **Parameters**

**X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] Test samples.

### Returns

y [array of shape [n\_samples] or [n\_samples, n\_outputs]] Class labels for each data sample.

# predict\_proba (self, X)

Return probability estimates for the test data X.

## **Parameters**

**X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] Test samples.

## **Returns**

p [array of shape = [n\_samples, n\_classes], or a list of n\_outputs] of such arrays if n\_outputs
 > 1. The class probabilities of the input samples. Classes are ordered by lexicographic order.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

# **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

 $\mathbf{y}$  [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for  $\mathbf{X}$ .

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

# Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# Examples using sklearn.neighbors.KNeighborsClassifier

- Classifier comparison
- Plot the decision boundaries of a VotingClassifier
- Digits Classification Exercise
- Nearest Neighbors Classification
- Comparing Nearest Neighbors with and without Neighborhood Components Analysis
- Dimensionality Reduction with Neighborhood Components Analysis
- Classification of text documents using sparse features

# 6.30.6 sklearn.neighbors.KNeighborsRegressor

```
class sklearn.neighbors.KNeighborsRegressor (n\_neighbors=5, weights='uniform', algorithm='auto', leaf_size=30, p=2, metric='minkowski', metric_params=None, n\_iobs=None, **kwargs)
```

Regression based on k-nearest neighbors.

The target is predicted by local interpolation of the targets associated of the nearest neighbors in the training set. Read more in the *User Guide*.

## **Parameters**

**n\_neighbors** [int, optional (default = 5)] Number of neighbors to use by default for *kneighbors* queries.

weights [str or callable] weight function used in prediction. Possible values:

- 'uniform': uniform weights. All points in each neighborhood are weighted equally.
- 'distance': weight points by the inverse of their distance. in this case, closer neighbors of a query point will have a greater influence than neighbors which are further away.
- [callable]: a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights.

Uniform weights are used by default.

**algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] Algorithm used to compute the nearest neighbors:

- 'ball tree' will use BallTree
- 'kd tree' will use KDTree
- 'brute' will use a brute-force search.
- 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.

- **leaf\_size** [int, optional (default = 30)] Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.
- **p** [integer, optional (default = 2)] Power parameter for the Minkowski metric. When p = 1, this is equivalent to using manhattan\_distance (11), and euclidean\_distance (12) for p = 2. For arbitrary p, minkowski\_distance (1\_p) is used.
- **metric** [string or callable, default 'minkowski'] the distance metric to use for the tree. The default metric is minkowski, and with p=2 is equivalent to the standard Euclidean metric. See the documentation of the DistanceMetric class for a list of available metrics.
- **metric\_params** [dict, optional (default = None)] Additional keyword arguments for the metric function.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details. Doesn't affect *fit* method.

## See also:

*NearestNeighbors* 

RadiusNeighborsRegressor

**KN**eighborsClassifier

RadiusNeighborsClassifier

## **Notes**

See *Nearest Neighbors* in the online documentation for a discussion of the choice of algorithm and leaf\_size.

**Warning:** Regarding the Nearest Neighbors algorithms, if it is found that two neighbors, neighbor k+1 and k, have identical distances but different labels, the results will depend on the ordering of the training data.

https://en.wikipedia.org/wiki/K-nearest\_neighbor\_algorithm

# **Examples**

```
>>> X = [[0], [1], [2], [3]]
>>> y = [0, 0, 1, 1]
>>> from sklearn.neighbors import KNeighborsRegressor
>>> neigh = KNeighborsRegressor(n_neighbors=2)
>>> neigh.fit(X, y)
KNeighborsRegressor(...)
>>> print(neigh.predict([[1.5]]))
[0.5]
```

# **Methods**

fit(self, X, y)	Fit the model using X as training data and y as target
	values
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
kneighbors(self[, X, n_neighbors,])	Finds the K-neighbors of a point.
kneighbors_graph(self[, X, n_neighbors, mode])	Computes the (weighted) graph of k-Neighbors for
	points in X
predict(self, X)	Predict the target for the provided data
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, n\_neighbors=5, weights='uniform', algorithm='auto', leaf\_size=30, p=2, metric='minkowski', metric\_params=None, n\_jobs=None, \*\*kwargs)

# **fit** (self, X, y)

Fit the model using X as training data and y as target values

## **Parameters**

- **X** [{array-like, sparse matrix, BallTree, KDTree}] Training data. If array or matrix, shape [n\_samples, n\_features], or [n\_samples, n\_samples] if metric='precomputed'.
- y [{array-like, sparse matrix}]

**Target values, array of float values, shape = [n\_samples]** or [n\_samples, n\_outputs]

# get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

kneighbors (self, X=None, n\_neighbors=None, return\_distance=True)

Finds the K-neighbors of a point. Returns indices of and distances to the neighbors of each point.

# **Parameters**

- **X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.
- n\_neighbors [int] Number of neighbors to get (default is the value passed to the constructor).

**return\_distance** [boolean, optional. Defaults to True.] If False, distances will not be returned

## Returns

**dist** [array] Array representing the lengths to points, only present if return\_distance=True **ind** [array] Indices of the nearest points in the population matrix.

# **Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who's the closest point to [1,1,1]

```
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=1)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> print(neigh.kneighbors([[1., 1., 1.]]))
(array([[0.5]]), array([[2]]))
```

As you can see, it returns [[0.5]], and [[2]], which means that the element is at distance 0.5 and is the third element of samples (indexes start at 0). You can also query for multiple points:

kneighbors\_graph (self, X=None, n\_neighbors=None, mode='connectivity')

Computes the (weighted) graph of k-Neighbors for points in X

## **Parameters**

- **X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.
- **n\_neighbors** [int] Number of neighbors for each sample. (default is value passed to the constructor).
- **mode** [{'connectivity', 'distance'}, optional] Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, in 'distance' the edges are Euclidean distance between points.

## Returns

A [sparse matrix in CSR format, shape = [n\_samples, n\_samples\_fit]] n\_samples\_fit is the number of samples in the fitted data A[i, j] is assigned the weight of edge that connects i to j.

## See also:

NearestNeighbors.radius\_neighbors\_graph

# **Examples**

```
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=2)
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.kneighbors_graph(X)
>>> A.toarray()
array([[1., 0., 1.],
```

```
[0., 1., 1.],
[1., 0., 1.]])
```

# predict (self, X)

Predict the target for the provided data

## **Parameters**

**X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] Test samples.

## **Returns**

y [array of int, shape = [n\_samples] or [n\_samples, n\_outputs]] Target values

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

## **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] R^2 of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

# set params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

# Examples using sklearn.neighbors.KNeighborsRegressor

• Face completion with a multi-output estimators

- Imputing missing values with variants of IterativeImputer
- Nearest Neighbors regression

# 6.30.7 sklearn.neighbors.LocalOutlierFactor

```
 \begin{array}{ll} \textbf{class} \text{ sklearn.neighbors.LocalOutlierFactor} (\textit{n\_neighbors=20}, & \textit{algorithm='auto'}, \\ \textit{leaf\_size=30}, & \textit{metric='minkowski'}, & \textit{p=2}, & \textit{metric\_params=None}, \\ \textit{ric\_params=None}, & \textit{contamination='legacy'}, \\ \textit{novelty=False}, \textit{n\_jobs=None}) \end{array}
```

Unsupervised Outlier Detection using Local Outlier Factor (LOF)

The anomaly score of each sample is called Local Outlier Factor. It measures the local deviation of density of a given sample with respect to its neighbors. It is local in that the anomaly score depends on how isolated the object is with respect to the surrounding neighborhood. More precisely, locality is given by k-nearest neighbors, whose distance is used to estimate the local density. By comparing the local density of a sample to the local densities of its neighbors, one can identify samples that have a substantially lower density than their neighbors. These are considered outliers.

## **Parameters**

**n\_neighbors** [int, optional (default=20)] Number of neighbors to use by default for *kneighbors* queries. If n\_neighbors is larger than the number of samples provided, all samples will be used.

**algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] Algorithm used to compute the nearest neighbors:

- 'ball tree' will use BallTree
- 'kd tree' will use KDTree
- 'brute' will use a brute-force search.
- 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.

**leaf\_size** [int, optional (default=30)] Leaf size passed to *BallTree* or *KDTree*. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

**metric** [string or callable, default 'minkowski'] metric used for the distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.

If 'precomputed', the training input X is expected to be a distance matrix.

If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating the distance between them. This works for Scipy's metrics, but is less efficient than passing the metric name as a string.

Valid values for metric are:

- from scikit-learn: ['cityblock', 'cosine', 'euclidean', '11', '12', 'manhattan']
- from scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule']

- See the documentation for scipy.spatial.distance for details on these metrics: https://docs.scipy.org/doc/scipy/reference/spatial.distance.html
- **p** [integer, optional (default=2)] Parameter for the Minkowski metric from sklearn. metrics.pairwise.pairwise\_distances. When p=1, this is equivalent to using manhattan\_distance (l1), and euclidean\_distance (l2) for p=2. For arbitrary p, minkowski\_distance (l\_p) is used.
- **metric\_params** [dict, optional (default=None)] Additional keyword arguments for the metric function.
- **contamination** [float in (0., 0.5), optional (default=0.1)] The amount of contamination of the data set, i.e. the proportion of outliers in the data set. When fitting this is used to define the threshold on the decision function. If "auto", the decision function threshold is determined as in the original paper.
  - Changed in version 0.20: The default value of contamination will change from 0.1 in 0.20 to 'auto' in 0.22.
- **novelty** [boolean, default False] By default, LocalOutlierFactor is only meant to be used for outlier detection (novelty=False). Set novelty to True if you want to use LocalOutlierFactor for novelty detection. In this case be aware that that you should only use predict, decision\_function and score\_samples on new unseen data and not on the training set.
- n\_jobs [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1
  means using all processors. See Glossary for more details. Affects only kneighbors and
  kneighbors\_graph methods.

## **Attributes**

negative\_outlier\_factor\_ [numpy array, shape (n\_samples,)] The opposite LOF of the training samples. The higher, the more normal. Inliers tend to have a LOF score close to 1
 (negative\_outlier\_factor\_close to -1), while outliers tend to have a larger LOF
score.

The local outlier factor (LOF) of a sample captures its supposed 'degree of abnormality'. It is the average of the ratio of the local reachability density of a sample and those of its k-nearest neighbors.

- **n\_neighbors\_** [integer] The actual number of neighbors used for *kneighbors* queries.
- offset\_ [float] Offset used to obtain binary labels from the raw scores. Observations having a negative\_outlier\_factor smaller than offset\_ are detected as abnormal. The offset is set to -1.5 (inliers score around -1), except when a contamination parameter different than "auto" is provided. In that case, the offset is defined in such a way we obtain the expected number of outliers in training.

## References

[Rca479bb49841-1]

## **Methods**

fit(self, X[, y])	Fit the model using X as training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.

Continued on next page

Table 6.230 - continued from previous page

kneighbors(self[, X, n_neighbors,])	Finds the K-neighbors of a point.
kneighbors_graph(self[, X, n_neighbors, mode])	Computes the (weighted) graph of k-Neighbors for
kneighbors_graph(sch[, A, n_heighbors, mode])	
	points in X
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_ (self, n\_neighbors=20, algorithm='auto', leaf\_size=30, metric='minkowski', p=2, metric\_params=None, contamination='legacy', novelty=False, n\_jobs=None)

### decision\_function

Shifted opposite of the Local Outlier Factor of X.

Bigger is better, i.e. large values correspond to inliers.

The shift offset allows a zero threshold for being an outlier. Only available for novelty detection (when novelty is set to True). The argument X is supposed to contain *new data*: if X contains a point from training, it considers the later in its own neighborhood. Also, the samples in X are not considered in the neighborhood of any point.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The query sample or samples to compute the Local Outlier Factor w.r.t. the training samples.

### **Returns**

**shifted\_opposite\_lof\_scores** [array, shape (n\_samples,)] The shifted opposite of the Local Outlier Factor of each input samples. The lower, the more abnormal. Negative scores represent outliers, positive scores represent inliers.

## **fit** (*self*, *X*, *y*=*None*)

Fit the model using X as training data.

### **Parameters**

- **X** [{array-like, sparse matrix, BallTree, KDTree}] Training data. If array or matrix, shape [n\_samples, n\_features], or [n\_samples, n\_samples] if metric='precomputed'.
- y [Ignored] not used, present for API consistency by convention.

#### Returns

self [object]

## fit\_predict

"Fits the model to the training set X and returns the labels.

Label is 1 for an inlier and -1 for an outlier according to the LOF score and the contamination parameter.

### **Parameters**

- X [array-like, shape (n\_samples, n\_features), default=None] The query sample or samples to compute the Local Outlier Factor w.r.t. to the training samples.
- y [Ignored] not used, present for API consistency by convention.

### Returns

is\_inlier [array, shape (n\_samples,)] Returns -1 for anomalies/outliers and 1 for inliers.

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

**kneighbors** (*self*, *X*=*None*, *n*\_*neighbors*=*None*, *return*\_*distance*=*True*)

Finds the K-neighbors of a point. Returns indices of and distances to the neighbors of each point.

#### **Parameters**

**X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

**n\_neighbors** [int] Number of neighbors to get (default is the value passed to the constructor).

**return\_distance** [boolean, optional. Defaults to True.] If False, distances will not be returned

#### Returns

**dist** [array] Array representing the lengths to points, only present if return\_distance=True **ind** [array] Indices of the nearest points in the population matrix.

## **Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who's the closest point to [1,1,1]

```
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=1)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> print(neigh.kneighbors([[1., 1., 1.]]))
(array([[0.5]]), array([[2]]))
```

As you can see, it returns [[0.5]], and [[2]], which means that the element is at distance 0.5 and is the third element of samples (indexes start at 0). You can also query for multiple points:

 $\verb+kneighbors_graph+ (self, X=None, n\_neighbors=None, mode='connectivity')$ 

Computes the (weighted) graph of k-Neighbors for points in X

## **Parameters**

**X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

n\_neighbors [int] Number of neighbors for each sample. (default is value passed to the constructor).

**mode** [{'connectivity', 'distance'}, optional] Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, in 'distance' the edges are Euclidean distance between points.

### **Returns**

A [sparse matrix in CSR format, shape = [n\_samples, n\_samples\_fit]] n\_samples\_fit is the number of samples in the fitted data A[i, j] is assigned the weight of edge that connects i to j.

### See also:

NearestNeighbors.radius\_neighbors\_graph

## **Examples**

## predict

Predict the labels (1 inlier, -1 outlier) of X according to LOF.

This method allows to generalize prediction to *new observations* (not in the training set). Only available for novelty detection (when novelty is set to True).

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The query sample or samples to compute the Local Outlier Factor w.r.t. to the training samples.

## Returns

**is\_inlier** [array, shape (n\_samples,)] Returns -1 for anomalies/outliers and +1 for inliers.

## score\_samples

Opposite of the Local Outlier Factor of X.

It is the opposite as bigger is better, i.e. large values correspond to inliers.

Only available for novelty detection (when novelty is set to True). The argument X is supposed to contain *new data*: if X contains a point from training, it considers the later in its own neighborhood. Also, the samples in X are not considered in the neighborhood of any point. The score\_samples on training data is available by considering the the negative\_outlier\_factor\_attribute.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The query sample or samples to compute the Local Outlier Factor w.r.t. the training samples.

## Returns

**opposite\_lof\_scores** [array, shape (n\_samples,)] The opposite of the Local Outlier Factor of each input samples. The lower, the more abnormal.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## Examples using sklearn.neighbors.LocalOutlierFactor

- Comparing anomaly detection algorithms for outlier detection on toy datasets
- Outlier detection with Local Outlier Factor (LOF)
- Novelty detection with Local Outlier Factor (LOF)

# 6.30.8 sklearn.neighbors.RadiusNeighborsClassifier

Classifier implementing a vote among neighbors within a given radius

Read more in the User Guide.

## **Parameters**

**radius** [float, optional (default = 1.0)] Range of parameter space to use by default for radius\_neighbors queries.

weights [str or callable] weight function used in prediction. Possible values:

- 'uniform' : uniform weights. All points in each neighborhood are weighted equally.
- 'distance': weight points by the inverse of their distance. in this case, closer neighbors of a query point will have a greater influence than neighbors which are further away.
- [callable]: a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights.

Uniform weights are used by default.

**algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] Algorithm used to compute the nearest neighbors:

- 'ball\_tree' will use BallTree
- 'kd\_tree' will use KDTree
- 'brute' will use a brute-force search.
- 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.

- **leaf\_size** [int, optional (default = 30)] Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.
- **p** [integer, optional (default = 2)] Power parameter for the Minkowski metric. When p = 1, this is equivalent to using manhattan\_distance (11), and euclidean\_distance (12) for p = 2. For arbitrary p, minkowski\_distance (1\_p) is used.
- **metric** [string or callable, default 'minkowski'] the distance metric to use for the tree. The default metric is minkowski, and with p=2 is equivalent to the standard Euclidean metric. See the documentation of the DistanceMetric class for a list of available metrics.
- outlier\_label [int, optional (default = None)] Label, which is given for outlier samples (samples with no neighbors on given radius). If set to None, ValueError is raised, when outlier is detected.
- **metric\_params** [dict, optional (default = None)] Additional keyword arguments for the metric function.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### See also:

KNeighborsClassifier

RadiusNeighborsRegressor

**KNeighborsRegressor** 

*NearestNeighbors* 

## **Notes**

See *Nearest Neighbors* in the online documentation for a discussion of the choice of algorithm and leaf\_size.

https://en.wikipedia.org/wiki/K-nearest\_neighbor\_algorithm

## **Examples**

```
>>> X = [[0], [1], [2], [3]]
>>> y = [0, 0, 1, 1]
>>> from sklearn.neighbors import RadiusNeighborsClassifier
>>> neigh = RadiusNeighborsClassifier(radius=1.0)
>>> neigh.fit(X, y)
RadiusNeighborsClassifier(...)
>>> print(neigh.predict([[1.5]]))
[0]
```

## **Methods**

fit(self, X, y)	Fit the model using X as training data and y as target
	values
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict the class labels for the provided data
radius_neighbors(self[, X, radius,])	Finds the neighbors within a given radius of a point or
	points.
radius_neighbors_graph(self[, X, radius,	Computes the (weighted) graph of Neighbors for points
mode])	in X
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, radius=1.0, weights='uniform', algorithm='auto', leaf\_size=30, p=2, metric='minkowski', outlier\_label=None, metric\_params=None, n\_jobs=None, \*\*kwargs)

## fit (self, X, y)

Fit the model using X as training data and y as target values

#### **Parameters**

- **X** [{array-like, sparse matrix, BallTree, KDTree}] Training data. If array or matrix, shape [n\_samples, n\_features], or [n\_samples, n\_samples] if metric='precomputed'.
- **y** [{array-like, sparse matrix}] Target values of shape = [n\_samples] or [n\_samples, n\_outputs]

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict the class labels for the provided data

## **Parameters**

 $\mathbf{X}$  [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] Test samples.

## **Returns**

y [array of shape [n\_samples] or [n\_samples, n\_outputs]] Class labels for each data sample.

## radius\_neighbors (self, X=None, radius=None, return\_distance=True)

Finds the neighbors within a given radius of a point or points.

Return the indices and distances of each point from the dataset lying in a ball with size radius around the points of the query array. Points lying on the boundary are included in the results.

The result points are *not* necessarily sorted by distance to their query point.

## **Parameters**

**X** [array-like, (n\_samples, n\_features), optional] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

**radius** [float] Limiting distance of neighbors to return. (default is the value passed to the constructor).

**return\_distance** [boolean, optional. Defaults to True.] If False, distances will not be returned

### **Returns**

**dist** [array, shape (n\_samples,) of arrays] Array representing the distances to each point, only present if return\_distance=True. The distance values are computed according to the metric constructor parameter.

ind [array, shape (n\_samples,) of arrays] An array of arrays of indices of the approximate nearest points from the population matrix that lie within a ball of size radius around the query points.

## **Notes**

Because the number of neighbors of each point is not necessarily equal, the results for multiple query points cannot be fit in a standard data array. For efficiency, <code>radius\_neighbors</code> returns arrays of objects, where each object is a 1D array of indices or distances.

## **Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who's the closest point to [1, 1, 1]:

```
>>> import numpy as np
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(radius=1.6)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> rng = neigh.radius_neighbors([[1., 1., 1.]])
>>> print(np.asarray(rng[0][0]))
[1.5 0.5]
>>> print(np.asarray(rng[1][0]))
[1 2]
```

The first array returned contains the distances to all points which are closer than 1.6, while the second array returned contains their indices. In general, multiple points can be queried at the same time.

```
radius_neighbors_graph (self, X=None, radius=None, mode='connectivity')
Computes the (weighted) graph of Neighbors for points in X
```

Neighborhoods are restricted the points at a distance lower than radius.

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features], optional] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

**radius** [float] Radius of neighborhoods. (default is the value passed to the constructor).

**mode** [{'connectivity', 'distance'}, optional] Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, in 'distance' the edges are Euclidean distance between points.

### **Returns**

**A** [sparse matrix in CSR format, shape = [n\_samples, n\_samples]] A[i, j] is assigned the weight of edge that connects i to j.

#### See also:

kneighbors\_graph

## **Examples**

### score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

 $\boldsymbol{score} \hspace{0.2cm} \textbf{[float] Mean accuracy of self.predict}(X) \hspace{0.1cm} wrt. \hspace{0.1cm} y.$ 

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### **Returns**

self

# 6.30.9 sklearn.neighbors.RadiusNeighborsRegressor

Regression based on neighbors within a fixed radius.

The target is predicted by local interpolation of the targets associated of the nearest neighbors in the training set. Read more in the *User Guide*.

### **Parameters**

**radius** [float, optional (default = 1.0)] Range of parameter space to use by default for radius neighbors queries.

weights [str or callable] weight function used in prediction. Possible values:

- 'uniform' : uniform weights. All points in each neighborhood are weighted equally.
- 'distance': weight points by the inverse of their distance. in this case, closer neighbors of a query point will have a greater influence than neighbors which are further away.
- [callable]: a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights.

Uniform weights are used by default.

**algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] Algorithm used to compute the nearest neighbors:

- 'ball tree' will use BallTree
- 'kd tree' will use KDTree
- 'brute' will use a brute-force search.
- 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.

- **leaf\_size** [int, optional (default = 30)] Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.
- **p** [integer, optional (default = 2)] Power parameter for the Minkowski metric. When p = 1, this is equivalent to using manhattan\_distance (11), and euclidean\_distance (12) for p = 2. For arbitrary p, minkowski\_distance (l\_p) is used.
- **metric** [string or callable, default 'minkowski'] the distance metric to use for the tree. The default metric is minkowski, and with p=2 is equivalent to the standard Euclidean metric. See the documentation of the DistanceMetric class for a list of available metrics.
- **metric\_params** [dict, optional (default = None)] Additional keyword arguments for the metric function.
- **n jobs** [int or None, optional (default=None)]

The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context.

−1 means using all processors. See *Glossary* for more details.

See also:

*NearestNeighbors* 

*KNeighborsRegressor* 

**KN**eighborsClassifier

RadiusNeighborsClassifier

### **Notes**

See *Nearest Neighbors* in the online documentation for a discussion of the choice of algorithm and leaf\_size.

https://en.wikipedia.org/wiki/K-nearest\_neighbor\_algorithm

## **Examples**

```
>>> X = [[0], [1], [2], [3]]
>>> y = [0, 0, 1, 1]
>>> from sklearn.neighbors import RadiusNeighborsRegressor
>>> neigh = RadiusNeighborsRegressor(radius=1.0)
>>> neigh.fit(X, y)
RadiusNeighborsRegressor(...)
>>> print(neigh.predict([[1.5]]))
[0.5]
```

## **Methods**

fit(self, X, y)	Fit the model using X as training data and y as target
	values
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict the target for the provided data
radius_neighbors(self[, X, radius,])	Finds the neighbors within a given radius of a point or
	points.
radius_neighbors_graph(self[, X, radius,	Computes the (weighted) graph of Neighbors for points
mode])	in X
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__(self, radius=1.0, weights='uniform', algorithm='auto', leaf_size=30, p=2, metric='minkowski', metric_params=None, n_jobs=None, **kwargs)
```

fit (self, X, y)

Fit the model using X as training data and y as target values

# **Parameters**

- **X** [{array-like, sparse matrix, BallTree, KDTree}] Training data. If array or matrix, shape [n\_samples, n\_features], or [n\_samples, n\_samples] if metric='precomputed'.
- y [{array-like, sparse matrix}]

**Target values, array of float values, shape = [n\_samples]** or [n\_samples, n\_outputs]

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### predict (self, X)

Predict the target for the provided data

#### **Parameters**

**X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] Test samples.

### Returns

y [array of float, shape = [n\_samples] or [n\_samples, n\_outputs]] Target values

radius\_neighbors (self, X=None, radius=None, return\_distance=True)

Finds the neighbors within a given radius of a point or points.

Return the indices and distances of each point from the dataset lying in a ball with size radius around the points of the query array. Points lying on the boundary are included in the results.

The result points are *not* necessarily sorted by distance to their query point.

### **Parameters**

**X** [array-like, (n\_samples, n\_features), optional] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

**radius** [float] Limiting distance of neighbors to return. (default is the value passed to the constructor).

**return\_distance** [boolean, optional. Defaults to True.] If False, distances will not be returned

## Returns

**dist** [array, shape (n\_samples,) of arrays] Array representing the distances to each point, only present if return\_distance=True. The distance values are computed according to the metric constructor parameter.

ind [array, shape (n\_samples,) of arrays] An array of arrays of indices of the approximate nearest points from the population matrix that lie within a ball of size radius around the query points.

## Notes

Because the number of neighbors of each point is not necessarily equal, the results for multiple query points cannot be fit in a standard data array. For efficiency, <code>radius\_neighbors</code> returns arrays of objects, where each object is a 1D array of indices or distances.

## **Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who's the closest point to [1, 1, 1]:

```
>>> import numpy as np
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(radius=1.6)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> rng = neigh.radius_neighbors([[1., 1., 1.]])
>>> print(np.asarray(rng[0][0]))
[1.5 0.5]
>>> print(np.asarray(rng[1][0]))
[1 2]
```

The first array returned contains the distances to all points which are closer than 1.6, while the second array returned contains their indices. In general, multiple points can be queried at the same time.

```
radius_neighbors_graph (self, X=None, radius=None, mode='connectivity')
Computes the (weighted) graph of Neighbors for points in X
```

Neighborhoods are restricted the points at a distance lower than radius.

#### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features], optional] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

radius [float] Radius of neighborhoods. (default is the value passed to the constructor).

**mode** [{'connectivity', 'distance'}, optional] Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, in 'distance' the edges are Euclidean distance between points.

## Returns

**A** [sparse matrix in CSR format, shape = [n\_samples, n\_samples]] A[i, j] is assigned the weight of edge that connects i to j.

### See also:

kneighbors\_graph

## **Examples**

### **score** (*self*, *X*, *y*, *sample weight=None*)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R<sup>2</sup> is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R<sup>2</sup> score of 0.0.

### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### **Returns**

**score** [float] R^2 of self.predict(X) wrt. y.

### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# 6.30.10 sklearn.neighbors.NearestCentroid

class sklearn.neighbors.NearestCentroid(metric='euclidean', shrink\_threshold=None)
 Nearest centroid classifier.

Each class is represented by its centroid, with test samples classified to the class with the nearest centroid.

Read more in the User Guide.

## **Parameters**

metric [string, or callable] The metric to use when calculating distance between instances in a feature array. If metric is a string or callable, it must be one of the options allowed by metrics.pairwise.pairwise\_distances for its metric parameter. The centroids for the samples corresponding to each class is the point from which the sum of the distances (according to the metric) of all samples that belong to that particular class are minimized. If the "manhattan" metric is provided, this centroid is the median and for all other metrics, the centroid is now set to be the mean.

**shrink\_threshold** [float, optional (default = None)] Threshold for shrinking centroids to remove features.

#### **Attributes**

**centroids**\_ [array-like, shape = [n\_classes, n\_features]] Centroid of each class

### See also:

sklearn.neighbors.KNeighborsClassifier nearest neighbors classifier

#### **Notes**

When used for text classification with tf-idf vectors, this classifier is also known as the Rocchio classifier.

### References

Tibshirani, R., Hastie, T., Narasimhan, B., & Chu, G. (2002). Diagnosis of multiple cancer types by shrunken centroids of gene expression. Proceedings of the National Academy of Sciences of the United States of America, 99(10), 6567-6572. The National Academy of Sciences.

## **Examples**

```
>>> from sklearn.neighbors.nearest_centroid import NearestCentroid
>>> import numpy as np
>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> y = np.array([1, 1, 1, 2, 2, 2])
>>> clf = NearestCentroid()
>>> clf.fit(X, y)
NearestCentroid(metric='euclidean', shrink_threshold=None)
>>> print(clf.predict([[-0.8, -1]]))
[1]
```

#### **Methods**

fit(self, X, y)	Fit the NearestCentroid model according to the given
	training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Perform classification on an array of test vectors X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
___init__ (self, metric='euclidean', shrink_threshold=None)
```

fit (self, X, y)

Fit the NearestCentroid model according to the given training data.

### **Parameters**

X [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vector, where n\_samples is the number of samples and n\_features is the number of features. Note that

centroid shrinking cannot be used with sparse matrices.

y [array, shape = [n\_samples]] Target values (integers)

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Perform classification on an array of test vectors X.

The predicted class C for each sample in X is returned.

### **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]]

#### Returns

**C** [array, shape = [n\_samples]]

### **Notes**

If the metric constructor parameter is "precomputed", X is assumed to be the distance matrix between the data to be predicted and self.centroids\_.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

# **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

 $\mathbf{y}$  [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for  $\mathbf{X}$ .

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## Examples using sklearn.neighbors.NearestCentroid

- Nearest Centroid Classification
- Classification of text documents using sparse features

# 6.30.11 sklearn.neighbors.NearestNeighbors

```
class sklearn.neighbors.NearestNeighbors (n_neighbors=5, radius=1.0, algorithm='auto', leaf\_size=30, metric='minkowski', p=2, metric\_params=None, n\_jobs=None, **kwargs)
```

Unsupervised learner for implementing neighbor searches.

Read more in the *User Guide*.

## **Parameters**

**n\_neighbors** [int, optional (default = 5)] Number of neighbors to use by default for *kneighbors* queries.

**radius** [float, optional (default = 1.0)] Range of parameter space to use by default for radius\_neighbors queries.

**algorithm** [{'auto', 'ball\_tree', 'kd\_tree', 'brute'}, optional] Algorithm used to compute the nearest neighbors:

- 'ball tree' will use BallTree
- 'kd\_tree' will use KDTree
- 'brute' will use a brute-force search.
- 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.

**leaf\_size** [int, optional (default = 30)] Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

**metric** [string or callable, default 'minkowski'] metric to use for distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.

If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating the distance between them. This works for Scipy's metrics, but is less efficient than passing the metric name as a string.

Distance matrices are not supported.

Valid values for metric are:

- from scikit-learn: ['cityblock', 'cosine', 'euclidean', '11', '12', 'manhattan']
- from scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule']

See the documentation for scipy.spatial.distance for details on these metrics.

- **p** [integer, optional (default = 2)] Parameter for the Minkowski metric from sklearn.metrics.pairwise\_distances. When p = 1, this is equivalent to using manhattan\_distance (11), and euclidean\_distance (12) for p = 2. For arbitrary p, minkowski\_distance (l\_p) is used.
- **metric\_params** [dict, optional (default = None)] Additional keyword arguments for the metric function.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

### See also:

```
KNeighborsClassifier
RadiusNeighborsClassifier
KNeighborsRegressor
RadiusNeighborsRegressor
BallTree
```

## **Notes**

See *Nearest Neighbors* in the online documentation for a discussion of the choice of algorithm and leaf size.

 $https://en.wikipedia.org/wiki/K-nearest\_neighbor\_algorithm$ 

### **Examples**

```
>>> import numpy as np
>>> from sklearn.neighbors import NearestNeighbors
>>> samples = [[0, 0, 2], [1, 0, 0], [0, 0, 1]]
```

```
>>> neigh = NearestNeighbors(2, 0.4)
>>> neigh.fit(samples)
NearestNeighbors(...)
```

```
>>> neigh.kneighbors([[0, 0, 1.3]], 2, return_distance=False)
...
array([[2, 0]]...)
```

```
>>> nbrs = neigh.radius_neighbors([[0, 0, 1.3]], 0.4, return_distance=False)
>>> np.asarray(nbrs[0][0])
array(2)
```

## **Methods**

fit(self, X[, y])

Fit the model using X as training data

Continued on next page

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<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
kneighbors(self[, X, n_neighbors,])	Finds the K-neighbors of a point.
kneighbors_graph(self[, X, n_neighbors, mode])	Computes the (weighted) graph of k-Neighbors for points in X
radius_neighbors(self[, X, radius,])	Finds the neighbors within a given radius of a point or
	points.
radius_neighbors_graph(self[, X, radius,	Computes the (weighted) graph of Neighbors for points
mode])	in X
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, n\_neighbors=5, radius=1.0, algorithm='auto', leaf\_size=30, metric='minkowski', p=2, metric\_params=None, n\_jobs=None, \*\*kwargs)

## **fit** (self, X, y=None)

Fit the model using X as training data

#### **Parameters**

**X** [{array-like, sparse matrix, BallTree, KDTree}] Training data. If array or matrix, shape [n\_samples, n\_features], or [n\_samples, n\_samples] if metric='precomputed'.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

kneighbors (self, X=None, n\_neighbors=None, return\_distance=True)

Finds the K-neighbors of a point. Returns indices of and distances to the neighbors of each point.

#### **Parameters**

**X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

n\_neighbors [int] Number of neighbors to get (default is the value passed to the constructor).

**return\_distance** [boolean, optional. Defaults to True.] If False, distances will not be returned

## Returns

dist [array] Array representing the lengths to points, only present if return\_distance=True

ind [array] Indices of the nearest points in the population matrix.

## **Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who's the closest point to [1,1,1]

```
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=1)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> print(neigh.kneighbors([[1., 1., 1.]]))
(array([[0.5]]), array([[2]]))
```

As you can see, it returns [[0.5]], and [[2]], which means that the element is at distance 0.5 and is the third element of samples (indexes start at 0). You can also query for multiple points:

**kneighbors\_graph** (*self*, *X=None*, *n\_neighbors=None*, *mode='connectivity'*)

Computes the (weighted) graph of k-Neighbors for points in X

## **Parameters**

- **X** [array-like, shape (n\_query, n\_features), or (n\_query, n\_indexed) if metric == 'precomputed'] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.
- **n\_neighbors** [int] Number of neighbors for each sample. (default is value passed to the constructor).
- **mode** [{'connectivity', 'distance'}, optional] Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, in 'distance' the edges are Euclidean distance between points.

## Returns

A [sparse matrix in CSR format, shape = [n\_samples, n\_samples\_fit]] n\_samples\_fit is the number of samples in the fitted data A[i, j] is assigned the weight of edge that connects i to j.

## See also:

NearestNeighbors.radius\_neighbors\_graph

## **Examples**

radius\_neighbors (self, X=None, radius=None, return\_distance=True)

Finds the neighbors within a given radius of a point or points.

Return the indices and distances of each point from the dataset lying in a ball with size radius around the points of the query array. Points lying on the boundary are included in the results.

The result points are *not* necessarily sorted by distance to their query point.

#### **Parameters**

X [array-like, (n\_samples, n\_features), optional] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

**radius** [float] Limiting distance of neighbors to return. (default is the value passed to the constructor).

**return\_distance** [boolean, optional. Defaults to True.] If False, distances will not be returned

#### Returns

**dist** [array, shape (n\_samples,) of arrays] Array representing the distances to each point, only present if return\_distance=True. The distance values are computed according to the metric constructor parameter.

ind [array, shape (n\_samples,) of arrays] An array of arrays of indices of the approximate nearest points from the population matrix that lie within a ball of size radius around the query points.

#### **Notes**

Because the number of neighbors of each point is not necessarily equal, the results for multiple query points cannot be fit in a standard data array. For efficiency, <code>radius\_neighbors</code> returns arrays of objects, where each object is a 1D array of indices or distances.

## **Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who's the closest point to [1, 1, 1]:

```
>>> import numpy as np
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(radius=1.6)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> rng = neigh.radius_neighbors([[1., 1., 1.]])
>>> print(np.asarray(rng[0][0]))
[1.5 0.5]
>>> print(np.asarray(rng[1][0]))
[1 2]
```

The first array returned contains the distances to all points which are closer than 1.6, while the second array returned contains their indices. In general, multiple points can be queried at the same time.

```
radius_neighbors_graph (self, X=None, radius=None, mode='connectivity')

Computes the (weighted) graph of Neighbors for points in X
```

Neighborhoods are restricted the points at a distance lower than radius.

## Parameters

**X** [array-like, shape = [n\_samples, n\_features], optional] The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

radius [float] Radius of neighborhoods. (default is the value passed to the constructor).

**mode** [{'connectivity', 'distance'}, optional] Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, in 'distance' the edges are Euclidean distance between points.

## Returns

**A** [sparse matrix in CSR format, shape = [n\_samples, n\_samples]] A[i, j] is assigned the weight of edge that connects i to j.

#### See also:

kneighbors\_graph

## **Examples**

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# 6.30.12 sklearn.neighbors.NeighborhoodComponentsAnalysis

```
 \begin{array}{ll} \textbf{class} \; \texttt{sklearn.neighbors.NeighborhoodComponentsAnalysis} \; (n\_components=None, \\ & init='auto', \; warm\_start=False, \\ & max\_iter=50, \qquad tol=1e-05, \\ & callback=None, \qquad verbose=0, \\ & random\_state=None) \end{array}
```

Neighborhood Components Analysis

Neighborhood Component Analysis (NCA) is a machine learning algorithm for metric learning. It learns a linear transformation in a supervised fashion to improve the classification accuracy of a stochastic nearest neighbors rule in the transformed space.

Read more in the *User Guide*.

### **Parameters**

- **n\_components** [int, optional (default=None)] Preferred dimensionality of the projected space. If None it will be set to n\_features.
- init [string or numpy array, optional (default='auto')] Initialization of the linear transformation. Possible options are 'auto', 'pca', 'lda', 'identity', 'random', and a numpy array of shape (n\_features\_a, n\_features\_b).
  - 'auto' Depending on n\_components, the most reasonable initialization will be chosen. If n\_components <= n\_classes we use 'lda', as it uses labels information. If not, but n\_components < min(n\_features, n\_samples), we use 'pca', as it projects data in meaningful directions (those of higher variance). Otherwise, we just use 'identity'.
  - 'pca' n\_components principal components of the inputs passed to fit will be used to initialize the transformation. (See decomposition.PCA)
  - 'lda' min(n\_components, n\_classes) most discriminative components of the inputs passed to fit will be used to initialize the transformation. (If n\_components > n\_classes, the rest of the components will be zero.) (See discriminant\_analysis.LinearDiscriminantAnalysis)
  - 'identity' If n\_components is strictly smaller than the dimensionality of the inputs passed to fit, the identity matrix will be truncated to the first n\_components rows.
  - **'random'** The initial transformation will be a random array of shape (n\_components, n\_features). Each value is sampled from the standard normal distribution.
  - **numpy array** n\_features\_b must match the dimensionality of the inputs passed to fit and n\_features\_a must be less than or equal to that. If n\_components is not None, n\_features\_a must match it.
- warm\_start [bool, optional, (default=False)] If True and fit has been called before, the solution of the previous call to fit is used as the initial linear transformation (n\_components and init will be ignored).
- max\_iter [int, optional (default=50)] Maximum number of iterations in the optimization.
- tol [float, optional (default=1e-5)] Convergence tolerance for the optimization.
- **callback** [callable, optional (default=None)] If not None, this function is called after every iteration of the optimizer, taking as arguments the current solution (flattened transformation matrix) and the number of iterations. This might be useful in case one wants to examine or store the transformation found after each iteration.
- **verbose** [int, optional (default=0)] If 0, no progress messages will be printed. If 1, progress messages will be printed to stdout. If > 1, progress messages will be printed and the disp parameter of scipy.optimize.minimize will be set to verbose 2.
- random\_state [int or numpy.RandomState or None, optional (default=None)] A pseudo random number generator object or a seed for it if int. If init='random', random\_state
  is used to initialize the random transformation. If init='pca', random\_state is
  passed as an argument to PCA when initializing the transformation.

# Attributes

- **components**\_ [array, shape (n\_components, n\_features)] The linear transformation learned during fitting.
- **n iter** [int] Counts the number of iterations performed by the optimizer.

### References

[Rf9b6baee8229-1], [Rf9b6baee8229-2]

## **Examples**

```
>>> from sklearn.neighbors.nca import NeighborhoodComponentsAnalysis
>>> from sklearn.neighbors import KNeighborsClassifier
>>> from sklearn.datasets import load_iris
>>> from sklearn.model_selection import train_test_split
>>> X, y = load_iris(return_X_y=True)
>>> X_train, X_test, y_train, y_test = train_test_split(X, y,
... stratify=y, test_size=0.7, random_state=42)
>>> nca = NeighborhoodComponentsAnalysis(random_state=42)
>>> nca.fit(X_train, y_train)
NeighborhoodComponentsAnalysis(...)
>>> knn = KNeighborsClassifier(n_neighbors=3)
>>> knn.fit(X_train, y_train)
KNeighborsClassifier(...)
>>> print(knn.score(X_test, y_test))
0.933333...
>>> knn.fit(nca.transform(X_train), y_train)
KNeighborsClassifier(...)
>>> print(knn.score(nca.transform(X_test), y_test))
0.961904...
```

## **Methods**

fit(self, X, y)	Fit the model according to the given training data.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Applies the learned transformation to the given data.

```
__init__ (self, n_components=None, init='auto', warm_start=False, max_iter=50, tol=1e-05, call-back=None, verbose=0, random_state=None)
```

## fit (self, X, y)

Fit the model according to the given training data.

### **Parameters**

- **X** [array-like, shape (n\_samples, n\_features)] The training samples.
- y [array-like, shape (n\_samples,)] The corresponding training labels.

#### Returns

**self** [object] returns a trained NeighborhoodComponentsAnalysis model.

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

## Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## **Returns**

self

### transform(self, X)

Applies the learned transformation to the given data.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Data samples.

### Returns

**X\_embedded:** array, shape (n\_samples, n\_components) The data samples transformed.

## **Raises**

**NotFittedError** If fit has not been called before.

## Examples using sklearn.neighbors.NeighborhoodComponentsAnalysis

- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...
- Comparing Nearest Neighbors with and without Neighborhood Components Analysis
- Dimensionality Reduction with Neighborhood Components Analysis
- Neighborhood Components Analysis Illustration

neighbors.kneighbors_graph(X, n_neighbors[,	Computes the (weighted) graph of k-Neighbors for points
])	in X
neighbors.radius_neighbors_graph(X, radius)	Computes the (weighted) graph of Neighbors for points in
	X

# 6.30.13 sklearn.neighbors.kneighbors\_graph

```
sklearn.neighbors.kneighbors_graph (X, n_neighbors, mode='connectivity', metric='minkowski', p=2, metric\_params=None, include\_self=False, n_pobs=None)
```

Computes the (weighted) graph of k-Neighbors for points in X

Read more in the User Guide.

## **Parameters**

- **X** [array-like or BallTree, shape = [n\_samples, n\_features]] Sample data, in the form of a numpy array or a precomputed BallTree.
- **n\_neighbors** [int] Number of neighbors for each sample.
- **mode** [{'connectivity', 'distance'}, optional] Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, and 'distance' will return the distances between neighbors according to the given metric.
- **metric** [string, default 'minkowski'] The distance metric used to calculate the k-Neighbors for each sample point. The DistanceMetric class gives a list of available metrics. The default distance is 'euclidean' ('minkowski' metric with the p param equal to 2.)
- **p** [int, default 2] Power parameter for the Minkowski metric. When p = 1, this is equivalent to using manhattan\_distance (11), and euclidean\_distance (12) for p = 2. For arbitrary p, minkowski\_distance (l\_p) is used.
- metric\_params [dict, optional] additional keyword arguments for the metric function.
- include\_self [bool, default=False.] Whether or not to mark each sample as the first near-est neighbor to itself. If None, then True is used for mode='connectivity' and False for mode='distance' as this will preserve backwards compatibility.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

### Returns

A [sparse matrix in CSR format, shape =  $[n_samples, n_samples]$ ] A[i, j] is assigned the weight of edge that connects i to j.

## See also:

radius\_neighbors\_graph

## **Examples**

## Examples using sklearn.neighbors.kneighbors\_graph

- Agglomerative clustering with and without structure
- Hierarchical clustering: structured vs unstructured ward
- Comparing different clustering algorithms on toy datasets

# 6.30.14 sklearn.neighbors.radius\_neighbors\_graph

```
sklearn.neighbors.radius_neighbors_graph(X, radius, mode='connectivity', metric='minkowski', p=2, metric_params=None, include self=False, n jobs=None)
```

Computes the (weighted) graph of Neighbors for points in X

Neighborhoods are restricted the points at a distance lower than radius.

Read more in the *User Guide*.

### **Parameters**

**X** [array-like or BallTree, shape = [n\_samples, n\_features]] Sample data, in the form of a numpy array or a precomputed BallTree.

radius [float] Radius of neighborhoods.

- **mode** [{'connectivity', 'distance'}, optional] Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, and 'distance' will return the distances between neighbors according to the given metric.
- metric [string, default 'minkowski'] The distance metric used to calculate the neighbors within a given radius for each sample point. The DistanceMetric class gives a list of available metrics. The default distance is 'euclidean' ('minkowski' metric with the param equal to 2.)
- **p** [int, default 2] Power parameter for the Minkowski metric. When p = 1, this is equivalent to using manhattan\_distance (11), and euclidean\_distance (12) for p = 2. For arbitrary p, minkowski distance (1 p) is used.

metric\_params [dict, optional] additional keyword arguments for the metric function.

- include\_self [bool, default=False] Whether or not to mark each sample as the first nearest neighbor to itself. If None, then True is used for mode='connectivity' and False for mode='distance' as this will preserve backwards compatibility.
- **n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run for neighbors search. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

## Returns

A [sparse matrix in CSR format, shape =  $[n_samples, n_samples]$ ] A[i, j] is assigned the weight of edge that connects i to j.

### See also:

kneighbors\_graph

## **Examples**

# 6.31 sklearn.neural\_network: Neural network models

The sklearn.neural\_network module includes models based on neural networks.

**User guide:** See the *Neural network models (supervised)* and *Neural network models (unsupervised)* sections for further details.

neural_network.BernoulliRBM([n_components, Bernoulli Restricted Boltzmann Machine (RBM).	
])	
$neural\_network. exttt{MLPClassifier}([\dots])$	Multi-layer Perceptron classifier.
$neural\_network. exttt{MLPRegressor}([\dots])$	Multi-layer Perceptron regressor.

# 6.31.1 sklearn.neural network.BernoulliRBM

```
 \begin{array}{ll} \textbf{class} \; \texttt{sklearn.neural\_network.BernoulliRBM} \; (\textit{n\_components} = 256, & \textit{learning\_rate} = 0.1, \\ \textit{batch\_size} = 10, & \textit{n\_iter} = 10, & \textit{verbose} = 0, & \textit{random\_state} = None) \end{array}
```

Bernoulli Restricted Boltzmann Machine (RBM).

A Restricted Boltzmann Machine with binary visible units and binary hidden units. Parameters are estimated using Stochastic Maximum Likelihood (SML), also known as Persistent Contrastive Divergence (PCD) [2].

The time complexity of this implementation is O(d \*\* 2) assuming d \* n\_features \* n\_components.

Read more in the *User Guide*.

## **Parameters**

**n\_components** [int, optional] Number of binary hidden units.

**learning\_rate** [float, optional] The learning rate for weight updates. It is *highly* recommended to tune this hyper-parameter. Reasonable values are in the 10\*\*[0., -3.] range.

batch\_size [int, optional] Number of examples per minibatch.

**n\_iter** [int, optional] Number of iterations/sweeps over the training dataset to perform during training.

**verbose** [int, optional] The verbosity level. The default, zero, means silent mode.

**random\_state** [integer or RandomState, optional] A random number generator instance to define the state of the random permutations generator. If an integer is given, it fixes the seed. Defaults to the global numpy random number generator.

**Attributes** 

**intercept\_hidden\_** [array-like, shape (n\_components,)] Biases of the hidden units.

intercept\_visible\_ [array-like, shape (n\_features,)] Biases of the visible units.

**components**\_ [array-like, shape (n\_components, n\_features)] Weight matrix, where n\_features in the number of visible units and n\_components is the number of hidden units.

### References

- [1] Hinton, G. E., Osindero, S. and Teh, Y. A fast learning algorithm for deep belief nets. Neural Computation 18, pp 1527-1554. https://www.cs.toronto.edu/~hinton/absps/fastnc.pdf
- [2] Tieleman, T. Training Restricted Boltzmann Machines using Approximations to the Likelihood Gradient. International Conference on Machine Learning (ICML) 2008

## **Examples**

```
>>> import numpy as np
>>> from sklearn.neural_network import BernoulliRBM
>>> X = np.array([[0, 0, 0], [0, 1, 1], [1, 0, 1], [1, 1, 1]])
>>> model = BernoulliRBM(n_components=2)
>>> model.fit(X)
BernoulliRBM(batch_size=10, learning_rate=0.1, n_components=2, n_iter=10, random_state=None, verbose=0)
```

#### **Methods**

fit(self, X[, y])	Fit the model to the data X.	
$fit\_transform(self, X[, y])$	Fit to data, then transform it.	
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.	
gibbs(self, v)	Perform one Gibbs sampling step.	
partial_fit(self, X[, y])	Fit the model to the data X which should contain a par-	
	tial segment of the data.	
score_samples(self, X)	Compute the pseudo-likelihood of X.	
set_params(self, \*\*params)	Set the parameters of this estimator.	
transform(self, X)	Compute the hidden layer activation probabilities,	
	P(h=1 v=X).	

```
__init__ (self, n_components=256, learning_rate=0.1, batch_size=10, n_iter=10, verbose=0, ran-dom_state=None)
```

**fit** (self, X, y=None)

Fit the model to the data X.

### **Parameters**

**X** [{array-like, sparse matrix} shape (n\_samples, n\_features)] Training data.

## Returns

self [BernoulliRBM] The fitted model.

**fit\_transform** (*self*, *X*, *y=None*, \*\**fit\_params*)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X new** [numpy array of shape [n samples, n features new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

### gibbs(self, v)

Perform one Gibbs sampling step.

### **Parameters**

v [array-like, shape (n\_samples, n\_features)] Values of the visible layer to start from.

#### Returns

**v\_new** [array-like, shape (n\_samples, n\_features)] Values of the visible layer after one Gibbs step.

## partial\_fit (self, X, y=None)

Fit the model to the data X which should contain a partial segment of the data.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Training data.

## Returns

self [BernoulliRBM] The fitted model.

# $score\_samples(self, X)$

Compute the pseudo-likelihood of X.

## **Parameters**

**X** [{array-like, sparse matrix} shape (n\_samples, n\_features)] Values of the visible layer. Must be all-boolean (not checked).

## Returns

**pseudo\_likelihood** [array-like, shape (n\_samples,)] Value of the pseudo-likelihood (proxy for likelihood).

## **Notes**

This method is not deterministic: it computes a quantity called the free energy on X, then on a randomly corrupted version of X, and returns the log of the logistic function of the difference.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## transform(self, X)

Compute the hidden layer activation probabilities, P(h=1|v=X).

### **Parameters**

**X** [{array-like, sparse matrix} shape (n\_samples, n\_features)] The data to be transformed.

### Returns

**h** [array, shape (n\_samples, n\_components)] Latent representations of the data.

## Examples using sklearn.neural\_network.BernoulliRBM

• Restricted Boltzmann Machine features for digit classification

# 6.31.2 sklearn.neural\_network.MLPClassifier

```
class sklearn.neural_network.MLPClassifier(hidden_layer_sizes=(100,
                                                                                          activa-
                                                                                   alpha = 0.0001,
                                                    tion='relu',
                                                                  solver='adam',
                                                    batch_size='auto',
                                                                         learning_rate='constant',
                                                    learning_rate_init=0.001,
                                                                                    power_t=0.5,
                                                    max_iter=200,
                                                                        shuffle=True,
                                                                                            ran-
                                                    dom_state=None,
                                                                           tol=0.0001,
                                                                                            ver-
                                                    bose=False, warm_start=False,
                                                                                        momen-
                                                    tum = 0.9,
                                                                       nesterovs_momentum=True,
                                                    early stopping=False, validation fraction=0.1,
                                                    beta 1=0.9,
                                                                 beta 2=0.999,
                                                                                  epsilon=1e-08,
                                                    n iter no change=10)
```

Multi-layer Perceptron classifier.

This model optimizes the log-loss function using LBFGS or stochastic gradient descent.

New in version 0.18.

### **Parameters**

**hidden\_layer\_sizes** [tuple, length =  $n_{layers}$  - 2, default (100,)] The ith element represents the number of neurons in the ith hidden layer.

activation [{'identity', 'logistic', 'tanh', 'relu'}, default 'relu'] Activation function for the hidden layer.

- 'identity', no-op activation, useful to implement linear bottleneck, returns f(x) = x
- 'logistic', the logistic sigmoid function, returns  $f(x) = 1 / (1 + \exp(-x))$ .
- 'tanh', the hyperbolic tan function, returns  $f(x) = \tanh(x)$ .
- 'relu', the rectified linear unit function, returns f(x) = max(0, x)

**solver** [{'lbfgs', 'sgd', 'adam'}, default 'adam'] The solver for weight optimization.

- 'lbfgs' is an optimizer in the family of quasi-Newton methods.
- 'sgd' refers to stochastic gradient descent.
- 'adam' refers to a stochastic gradient-based optimizer proposed by Kingma, Diederik, and Jimmy Ba

Note: The default solver 'adam' works pretty well on relatively large datasets (with thousands of training samples or more) in terms of both training time and validation score. For small datasets, however, 'lbfgs' can converge faster and perform better.

alpha [float, optional, default 0.0001] L2 penalty (regularization term) parameter.

**batch\_size** [int, optional, default 'auto'] Size of minibatches for stochastic optimizers. If the solver is 'lbfgs', the classifier will not use minibatch. When set to "auto", batch\_size=min(200, n\_samples)

**learning\_rate** [{'constant', 'invscaling', 'adaptive'}, default 'constant'] Learning rate schedule for weight updates.

- 'constant' is a constant learning rate given by 'learning\_rate\_init'.
- 'invscaling' gradually decreases the learning rate at each time step 't' using an inverse scaling exponent of 'power\_t'. effective\_learning\_rate = learning\_rate\_init / pow(t, power\_t)
- 'adaptive' keeps the learning rate constant to 'learning\_rate\_init' as long as training loss keeps decreasing. Each time two consecutive epochs fail to decrease training loss by at least tol, or fail to increase validation score by at least tol if 'early\_stopping' is on, the current learning rate is divided by 5.

Only used when solver='sqd'.

- **learning\_rate\_init** [double, optional, default 0.001] The initial learning rate used. It controls the step-size in updating the weights. Only used when solver='sgd' or 'adam'.
- **power\_t** [double, optional, default 0.5] The exponent for inverse scaling learning rate. It is used in updating effective learning rate when the learning\_rate is set to 'invscaling'. Only used when solver='sgd'.
- max\_iter [int, optional, default 200] Maximum number of iterations. The solver iterates until convergence (determined by 'tol') or this number of iterations. For stochastic solvers ('sgd', 'adam'), note that this determines the number of epochs (how many times each data point will be used), not the number of gradient steps.
- **shuffle** [bool, optional, default True] Whether to shuffle samples in each iteration. Only used when solver='sgd' or 'adam'.
- random\_state [int, RandomState instance or None, optional, default None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- tol [float, optional, default 1e-4] Tolerance for the optimization. When the loss or score is not improving by at least tol for n\_iter\_no\_change consecutive iterations, unless learning\_rate is set to 'adaptive', convergence is considered to be reached and training stops.

verbose [bool, optional, default False] Whether to print progress messages to stdout.

warm\_start [bool, optional, default False] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.

- **momentum** [float, default 0.9] Momentum for gradient descent update. Should be between 0 and 1. Only used when solver='sgd'.
- **nesterovs\_momentum** [boolean, default True] Whether to use Nesterov's momentum. Only used when solver='sgd' and momentum > 0.
- early\_stopping [bool, default False] Whether to use early stopping to terminate training when validation score is not improving. If set to true, it will automatically set aside 10% of training data as validation and terminate training when validation score is not improving by at least tol for n\_iter\_no\_change consecutive epochs. The split is stratified, except in a multilabel setting. Only effective when solver='sgd' or 'adam'
- **validation\_fraction** [float, optional, default 0.1] The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if early\_stopping is True
- **beta\_1** [float, optional, default 0.9] Exponential decay rate for estimates of first moment vector in adam, should be in [0, 1). Only used when solver='adam'
- **beta\_2** [float, optional, default 0.999] Exponential decay rate for estimates of second moment vector in adam, should be in [0, 1). Only used when solver='adam'
- epsilon [float, optional, default 1e-8] Value for numerical stability in adam. Only used when solver='adam'
- **n\_iter\_no\_change** [int, optional, default 10] Maximum number of epochs to not meet tol improvement. Only effective when solver='sgd' or 'adam'

New in version 0.20.

### Attributes

- classes\_ [array or list of array of shape (n\_classes,)] Class labels for each output.
- **loss**\_ [float] The current loss computed with the loss function.
- **coefs**\_ [list, length n\_layers 1] The ith element in the list represents the weight matrix corresponding to layer i.
- **intercepts** [list, length n\_layers 1] The ith element in the list represents the bias vector corresponding to layer i + 1.
- **n\_iter\_** [int,] The number of iterations the solver has ran.
- **n\_layers**\_ [int] Number of layers.
- **n outputs** [int] Number of outputs.
- **out activation** [string] Name of the output activation function.

## **Notes**

MLPClassifier trains iteratively since at each time step the partial derivatives of the loss function with respect to the model parameters are computed to update the parameters.

It can also have a regularization term added to the loss function that shrinks model parameters to prevent overfitting.

This implementation works with data represented as dense numpy arrays or sparse scipy arrays of floating point values.

### References

Hinton, Geoffrey E. "Connectionist learning procedures." Artificial intelligence 40.1 (1989): 185-234.

**Glorot, Xavier, and Yoshua Bengio. "Understanding the difficulty of** training deep feedforward neural networks." International Conference on Artificial Intelligence and Statistics. 2010.

He, Kaiming, et al. "Delving deep into rectifiers: Surpassing human-level performance on imagenet classification." arXiv preprint arXiv:1502.01852 (2015).

**Kingma, Diederik, and Jimmy Ba. "Adam: A method for stochastic** optimization." arXiv preprint arXiv:1412.6980 (2014).

## **Methods**

fit(self, X, y)	Fit the model to data matrix X and target(s) y.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the multi-layer perceptron classifier
predict_log_proba(self, X)	Return the log of probability estimates.
predict_proba(self, X)	Probability estimates.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, hidden\_layer\_sizes=(100, ), activation='relu', solver='adam', al-pha=0.0001, batch\_size='auto', learning\_rate='constant', learning\_rate\_init=0.001, power\_t=0.5, max\_iter=200, shuffle=True, random\_state=None, tol=0.0001, ver-bose=False, warm\_start=False, momentum=0.9, nesterovs\_momentum=True, early\_stopping=False, validation\_fraction=0.1, beta\_1=0.9, beta\_2=0.999, epsilon=1e-08, n\_iter\_no\_change=10)

## fit (self, X, y)

Fit the model to data matrix X and target(s) y.

## **Parameters**

- **X** [array-like or sparse matrix, shape (n\_samples, n\_features)] The input data.
- y [array-like, shape (n\_samples,) or (n\_samples, n\_outputs)] The target values (class labels in classification, real numbers in regression).

## Returns

self [returns a trained MLP model.]

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

### partial fit

Update the model with a single iteration over the given data.

### **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data.
- y [array-like, shape (n\_samples,)] The target values.

classes [array, shape (n\_classes), default None] Classes across all calls to partial\_fit. Can be obtained via np.unique(y\_all), where y\_all is the target vector of the entire dataset. This argument is required for the first call to partial\_fit and can be omitted in the subsequent calls. Note that y doesn't need to contain all labels in classes.

### **Returns**

self [returns a trained MLP model.]

## predict (self, X)

Predict using the multi-layer perceptron classifier

### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data.

#### Returns

y [array-like, shape (n\_samples,) or (n\_samples, n\_classes)] The predicted classes.

## $predict_log_proba(self, X)$

Return the log of probability estimates.

#### **Parameters**

**X** [array-like, shape (n samples, n features)] The input data.

#### Returns

 $log\_y\_prob$  [array-like, shape (n\_samples, n\_classes)] The predicted log-probability of the sample for each class in the model, where classes are ordered as they are in self. classes\_. Equivalent to log(predict\_proba(X))

# $predict\_proba$ (self, X)

Probability estimates.

### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data.

### **Returns**

**y\_prob** [array-like, shape (n\_samples, n\_classes)] The predicted probability of the sample for each class in the model, where classes are ordered as they are in self.classes\_.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

- $\mathbf{X}$  [array-like, shape = (n\_samples, n\_features)] Test samples.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## Examples using sklearn.neural\_network.MLPClassifier

- Classifier comparison
- Visualization of MLP weights on MNIST
- Varying regularization in Multi-layer Perceptron
- Compare Stochastic learning strategies for MLPClassifier

# 6.31.3 sklearn.neural\_network.MLPRegressor

```
class sklearn.neural network.MLPRegressor(hidden layer sizes=(100,
                                                                                             activa-
                                                     tion='relu'.
                                                                   solver='adam'.
                                                                                     alpha = 0.0001.
                                                     batch size='auto',
                                                                           learning_rate='constant',
                                                     learning rate init=0.001,
                                                                                      power t=0.5,
                                                     max_iter=200, shuffle=True, random_state=None,
                                                     tol=0.0001, verbose=False, warm_start=False,
                                                     momentum=0.9,
                                                                         nesterovs momentum=True,
                                                     early_stopping=False,
                                                                             validation fraction=0.1,
                                                                    beta_2=0.999,
                                                                                     epsilon=1e-08,
                                                     beta_1 = 0.9,
                                                     n_iter_no_change=10)
```

Multi-layer Perceptron regressor.

This model optimizes the squared-loss using LBFGS or stochastic gradient descent.

New in version 0.18.

## **Parameters**

**hidden\_layer\_sizes** [tuple, length =  $n_layers - 2$ , default (100,)] The ith element represents the number of neurons in the ith hidden layer.

activation [{'identity', 'logistic', 'tanh', 'relu'}, default 'relu'] Activation function for the hidden layer.

- 'identity', no-op activation, useful to implement linear bottleneck, returns f(x) = x
- 'logistic', the logistic sigmoid function, returns  $f(x) = 1 / (1 + \exp(-x))$ .
- 'tanh', the hyperbolic tan function, returns  $f(x) = \tanh(x)$ .
- 'relu', the rectified linear unit function, returns f(x) = max(0, x)

solver [{'lbfgs', 'sgd', 'adam'}, default 'adam'] The solver for weight optimization.

- 'lbfgs' is an optimizer in the family of quasi-Newton methods.
- 'sgd' refers to stochastic gradient descent.

 'adam' refers to a stochastic gradient-based optimizer proposed by Kingma, Diederik, and Jimmy Ba

Note: The default solver 'adam' works pretty well on relatively large datasets (with thousands of training samples or more) in terms of both training time and validation score. For small datasets, however, 'lbfgs' can converge faster and perform better.

- **alpha** [float, optional, default 0.0001] L2 penalty (regularization term) parameter.
- batch\_size [int, optional, default 'auto'] Size of minibatches for stochastic optimizers. If
  the solver is 'lbfgs', the classifier will not use minibatch. When set to "auto",
  batch\_size=min(200, n\_samples)
- **learning\_rate** [{'constant', 'invscaling', 'adaptive'}, default 'constant'] Learning rate schedule for weight updates.
  - 'constant' is a constant learning rate given by 'learning\_rate\_init'.
  - 'invscaling' gradually decreases the learning rate learning\_rate\_ at each time step
     't' using an inverse scaling exponent of 'power\_t'. effective\_learning\_rate = learning\_rate\_init / pow(t, power\_t)
  - 'adaptive' keeps the learning rate constant to 'learning\_rate\_init' as long as training loss keeps decreasing. Each time two consecutive epochs fail to decrease training loss by at least tol, or fail to increase validation score by at least tol if 'early\_stopping' is on, the current learning rate is divided by 5.

Only used when solver='sgd'.

- **learning\_rate\_init** [double, optional, default 0.001] The initial learning rate used. It controls the step-size in updating the weights. Only used when solver='sgd' or 'adam'.
- **power\_t** [double, optional, default 0.5] The exponent for inverse scaling learning rate. It is used in updating effective learning rate when the learning\_rate is set to 'invscaling'. Only used when solver='sgd'.
- max\_iter [int, optional, default 200] Maximum number of iterations. The solver iterates until convergence (determined by 'tol') or this number of iterations. For stochastic solvers ('sgd', 'adam'), note that this determines the number of epochs (how many times each data point will be used), not the number of gradient steps.
- **shuffle** [bool, optional, default True] Whether to shuffle samples in each iteration. Only used when solver='sgd' or 'adam'.
- random\_state [int, RandomState instance or None, optional, default None] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- tol [float, optional, default 1e-4] Tolerance for the optimization. When the loss or score is not improving by at least tol for n\_iter\_no\_change consecutive iterations, unless learning\_rate is set to 'adaptive', convergence is considered to be reached and training stops.
- verbose [bool, optional, default False] Whether to print progress messages to stdout.
- warm\_start [bool, optional, default False] When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. See *the Glossary*.
- **momentum** [float, default 0.9] Momentum for gradient descent update. Should be between 0 and 1. Only used when solver='sgd'.

- **nesterovs\_momentum** [boolean, default True] Whether to use Nesterov's momentum. Only used when solver='sgd' and momentum > 0.
- early\_stopping [bool, default False] Whether to use early stopping to terminate training when validation score is not improving. If set to true, it will automatically set aside 10% of training data as validation and terminate training when validation score is not improving by at least tol for n\_iter\_no\_change consecutive epochs. Only effective when solver='sgd' or 'adam'
- **validation\_fraction** [float, optional, default 0.1] The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if early\_stopping is True
- **beta\_1** [float, optional, default 0.9] Exponential decay rate for estimates of first moment vector in adam, should be in [0, 1). Only used when solver='adam'
- **beta\_2** [float, optional, default 0.999] Exponential decay rate for estimates of second moment vector in adam, should be in [0, 1). Only used when solver='adam'
- **epsilon** [float, optional, default 1e-8] Value for numerical stability in adam. Only used when solver='adam'
- **n\_iter\_no\_change** [int, optional, default 10] Maximum number of epochs to not meet tol improvement. Only effective when solver='sgd' or 'adam'

New in version 0.20.

#### Attributes

- **loss**\_ [float] The current loss computed with the loss function.
- **coefs**\_ [list, length n\_layers 1] The ith element in the list represents the weight matrix corresponding to layer i.
- **intercepts**\_ [list, length n\_layers 1] The ith element in the list represents the bias vector corresponding to layer i + 1.
- **n\_iter\_** [int,] The number of iterations the solver has ran.
- **n\_layers**\_ [int] Number of layers.
- **n\_outputs\_** [int] Number of outputs.
- **out\_activation\_** [string] Name of the output activation function.

# **Notes**

MLPRegressor trains iteratively since at each time step the partial derivatives of the loss function with respect to the model parameters are computed to update the parameters.

It can also have a regularization term added to the loss function that shrinks model parameters to prevent overfitting.

This implementation works with data represented as dense and sparse numpy arrays of floating point values.

### References

- Hinton, Geoffrey E. "Connectionist learning procedures." Artificial intelligence 40.1 (1989): 185-234.
- **Glorot, Xavier, and Yoshua Bengio. "Understanding the difficulty of training deep feedforward neural networks."** International Conference on Artificial Intelligence and Statistics. 2010.

**He, Kaiming, et al. "Delving deep into rectifiers: Surpassing human-level** performance on imagenet classification." arXiv preprint arXiv:1502.01852 (2015).

**Kingma, Diederik, and Jimmy Ba. "Adam: A method for stochastic** optimization." arXiv preprint arXiv:1412.6980 (2014).

### **Methods**

fit(self, X, y)	Fit the model to data matrix X and target(s) y.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the multi-layer perceptron model.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, hidden\_layer\_sizes=(100, ), activation='relu', solver='adam', al-pha=0.0001, batch\_size='auto', learning\_rate='constant', learning\_rate\_init=0.001, power\_t=0.5, max\_iter=200, shuffle=True, random\_state=None, tol=0.0001, ver-bose=False, warm\_start=False, momentum=0.9, nesterovs\_momentum=True, early\_stopping=False, validation\_fraction=0.1, beta\_1=0.9, beta\_2=0.999, epsilon=1e-08, n\_iter\_no\_change=10)

# **fit** (self, X, y)

Fit the model to data matrix X and target(s) y.

#### **Parameters**

- **X** [array-like or sparse matrix, shape (n\_samples, n\_features)] The input data.
- **y** [array-like, shape (n\_samples,) or (n\_samples, n\_outputs)] The target values (class labels in classification, real numbers in regression).

#### Returns

self [returns a trained MLP model.]

### get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

**params** [mapping of string to any] Parameter names mapped to their values.

# partial fit

Update the model with a single iteration over the given data.

#### **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data.
- y [array-like, shape (n\_samples,)] The target values.

# Returns

self [returns a trained MLP model.]

#### predict (self, X)

Predict using the multi-layer perceptron model.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] The input data.

#### Returns

y [array-like, shape (n\_samples, n\_outputs)] The predicted values.

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with <code>metrics.r2\_score</code>. This will influence the score method of all the multioutput regressors (except for <code>multioutput.MultiOutputRegressor</code>). To specify the default value manually and avoid the warning, please either call <code>metrics.r2\_score</code> directly or make a custom scorer with <code>metrics.make\_scorer</code> (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# Examples using sklearn.neural\_network.MLPRegressor

• Partial Dependence Plots

# 6.32 sklearn.pipeline: Pipeline

The *sklearn.pipeline* module implements utilities to build a composite estimator, as a chain of transforms and estimators.

pipeline.FeatureUnion(transformer_list[,])	Concatenates results of multiple transformer objects.
<pre>pipeline.Pipeline(steps[, memory, verbose])</pre>	Pipeline of transforms with a final estimator.

# 6.32.1 sklearn.pipeline.FeatureUnion

Concatenates results of multiple transformer objects.

This estimator applies a list of transformer objects in parallel to the input data, then concatenates the results. This is useful to combine several feature extraction mechanisms into a single transformer.

Parameters of the transformers may be set using its name and the parameter name separated by a '\_\_'. A transformer may be replaced entirely by setting the parameter with its name to another transformer, or removed by setting to 'drop' or None.

Read more in the *User Guide*.

#### **Parameters**

**transformer\_list** [list of (string, transformer) tuples] List of transformer objects to be applied to the data. The first half of each tuple is the name of the transformer.

**n\_jobs** [int or None, optional (default=None)] Number of jobs to run in parallel. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

**transformer\_weights** [dict, optional] Multiplicative weights for features per transformer. Keys are transformer names, values the weights.

**verbose** [boolean, optional(default=False)] If True, the time elapsed while fitting each transformer will be printed as it is completed.

### See also:

sklearn.pipeline.make\_union convenience function for simplified feature union construction.

# **Examples**

# **Methods**

fit(self, X[, y])	Fit all transformers using X.
<pre>fit_transform(self, X[, y])</pre>	Fit all transformers, transform the data and concatenate
	results.
<pre>get_feature_names(self)</pre>	Get feature names from all transformers.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*kwargs)	Set the parameters of this estimator.
transform(self, X)	Transform X separately by each transformer, concate-
	nate results.

**\_\_\_init\_\_**(*self, transformer\_list, n\_jobs=None, transformer\_weights=None, verbose=False*)

# **fit** (*self*, *X*, *y=None*)

Fit all transformers using X.

#### **Parameters**

- **X** [iterable or array-like, depending on transformers] Input data, used to fit transformers.
- y [array-like, shape (n\_samples, ...), optional] Targets for supervised learning.

### Returns

**self** [FeatureUnion] This estimator

### **fit** transform (self, X, y=None, \*\*fit params)

Fit all transformers, transform the data and concatenate results.

## **Parameters**

- X [iterable or array-like, depending on transformers] Input data to be transformed.
- y [array-like, shape (n\_samples, ...), optional] Targets for supervised learning.

### Returns

**X\_t** [array-like or sparse matrix, shape (n\_samples, sum\_n\_components)] hstack of results of transformers. sum\_n\_components is the sum of n\_components (output dimension) over transformers.

# get\_feature\_names (self)

Get feature names from all transformers.

### Returns

feature\_names [list of strings] Names of the features produced by transform.

# get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

# set\_params (self, \*\*kwargs)

Set the parameters of this estimator.

Valid parameter keys can be listed with get\_params().

#### Returns

self

# transform(self, X)

Transform X separately by each transformer, concatenate results.

#### **Parameters**

**X** [iterable or array-like, depending on transformers] Input data to be transformed.

### Returns

**X\_t** [array-like or sparse matrix, shape (n\_samples, sum\_n\_components)] hstack of results of transformers. sum\_n\_components is the sum of n\_components (output dimension) over transformers.

# Examples using sklearn.pipeline.FeatureUnion

• Concatenating multiple feature extraction methods

# 6.32.2 sklearn.pipeline.Pipeline

class sklearn.pipeline.Pipeline(steps, memory=None, verbose=False)

Pipeline of transforms with a final estimator.

Sequentially apply a list of transforms and a final estimator. Intermediate steps of the pipeline must be 'transforms', that is, they must implement fit and transform methods. The final estimator only needs to implement fit. The transformers in the pipeline can be cached using memory argument.

The purpose of the pipeline is to assemble several steps that can be cross-validated together while setting different parameters. For this, it enables setting parameters of the various steps using their names and the parameter name separated by a '\_\_', as in the example below. A step's estimator may be replaced entirely by setting the parameter with its name to another estimator, or a transformer removed by setting it to 'passthrough' or None.

Read more in the *User Guide*.

#### **Parameters**

**steps** [list] List of (name, transform) tuples (implementing fit/transform) that are chained, in the order in which they are chained, with the last object an estimator.

memory [None, str or object with the joblib.Memory interface, optional] Used to cache the fitted transformers of the pipeline. By default, no caching is performed. If a string is given, it is the path to the caching directory. Enabling caching triggers a clone of the transformers before fitting. Therefore, the transformer instance given to the pipeline cannot be inspected directly. Use the attribute named\_steps or steps to inspect estimators within the pipeline. Caching the transformers is advantageous when fitting is time consuming.

**verbose** [boolean, optional] If True, the time elapsed while fitting each step will be printed as it is completed.

### **Attributes**

**named\_steps** [bunch object, a dictionary with attribute access] Read-only attribute to access any step parameter by user given name. Keys are step names and values are steps parameters.

See also:

sklearn.pipeline.make\_pipeline convenience function for simplified pipeline construction.

# **Examples**

```
>>> from sklearn import svm
>>> from sklearn.datasets import samples_generator
>>> from sklearn.feature_selection import SelectKBest
>>> from sklearn.feature_selection import f_regression
>>> from sklearn.pipeline import Pipeline
>>> # generate some data to play with
>>> X, y = samples_generator.make_classification(
       n_informative=5, n_redundant=0, random_state=42)
>>> # ANOVA SVM-C
>>> anova_filter = SelectKBest(f_regression, k=5)
>>> clf = svm.SVC(kernel='linear')
>>> anova_svm = Pipeline([('anova', anova_filter), ('svc', clf)])
>>> # You can set the parameters using the names issued
>>> # For instance, fit using a k of 10 in the SelectKBest
>>> # and a parameter 'C' of the svm
>>> anova_svm.set_params(anova__k=10, svc__C=.1).fit(X, y)
Pipeline (memory=None,
         steps=[('anova', SelectKBest(...)),
               ('svc', SVC(...))], verbose=False)
>>> prediction = anova_svm.predict(X)
>>> anova_svm.score(X, y)
0.83
>>> # getting the selected features chosen by anova filter
>>> anova_svm['anova'].get_support()
array([False, False, True, True, False, False, True, True, False,
       True, False, True, True, False, True, False, True, True,
       False, False])
>>> # Another way to get selected features chosen by anova_filter
>>> anova_svm.named_steps.anova.get_support()
array([False, False, True, True, False, False, True, True, False,
       True, False, True, True, False, True, False, True, True,
       False, False])
>>> # Indexing can also be used to extract a sub-pipeline.
>>> sub_pipeline = anova_svm[:1]
>>> sub pipeline
Pipeline(memory=None, steps=[('anova', ...)], verbose=False)
>>> coef = anova_svm[-1].coef_
>>> anova_svm['svc'] is anova_svm[-1]
True
>>> coef.shape
>>> sub_pipeline.inverse_transform(coef).shape
(1, 20)
```

## **Methods**

decision_function(self, X)	Apply transforms, and decision_function of the final es-
	timator
fit(self, X[, y])	Fit the model
fit_predict(self, X[, y])	Applies fit_predict of last step in pipeline after trans-
	forms.
<pre>fit_transform(self, X[, y])</pre>	Fit the model and transform with the final estimator
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X, \*\*predict_params)</pre>	Apply transforms to the data, and predict with the final
	estimator
predict_log_proba(self, X)	Apply transforms, and predict_log_proba of the final es-
	timator
predict_proba(self, X)	Apply transforms, and predict_proba of the final estima-
	tor
score(self, X[, y, sample_weight])	Apply transforms, and score with the final estimator
set_params(self, \*\*kwargs)	Set the parameters of this estimator.

\_\_init\_\_ (self, steps, memory=None, verbose=False)

# $decision_function(self, X)$

Apply transforms, and decision\_function of the final estimator

#### **Parameters**

X [iterable] Data to predict on. Must fulfill input requirements of first step of the pipeline.

### Returns

**y score** [array-like, shape = [n samples, n classes]]

**fit** (*self*, *X*, *y=None*, \*\**fit\_params*)

Fit the model

Fit all the transforms one after the other and transform the data, then fit the transformed data using the final estimator.

#### **Parameters**

- X [iterable] Training data. Must fulfill input requirements of first step of the pipeline.
- y [iterable, default=None] Training targets. Must fulfill label requirements for all steps of the pipeline.
- \*\*fit\_params [dict of string -> object] Parameters passed to the fit method of each step, where each parameter name is prefixed such that parameter p for step s has key s\_p.

# Returns

self [Pipeline] This estimator

fit\_predict (self, X, y=None, \*\*fit\_params)

Applies fit\_predict of last step in pipeline after transforms.

Applies fit\_transforms of a pipeline to the data, followed by the fit\_predict method of the final estimator in the pipeline. Valid only if the final estimator implements fit\_predict.

### **Parameters**

- **X** [iterable] Training data. Must fulfill input requirements of first step of the pipeline.
- y [iterable, default=None] Training targets. Must fulfill label requirements for all steps of the pipeline.

\*\*fit\_params [dict of string -> object] Parameters passed to the fit method of each step, where each parameter name is prefixed such that parameter p for step s has key s\_p.

#### Returns

**y\_pred** [array-like]

fit\_transform(self, X, y=None, \*\*fit\_params)

Fit the model and transform with the final estimator

Fits all the transforms one after the other and transforms the data, then uses fit\_transform on transformed data with the final estimator.

#### **Parameters**

- X [iterable] Training data. Must fulfill input requirements of first step of the pipeline.
- y [iterable, default=None] Training targets. Must fulfill label requirements for all steps of the pipeline.
- \*\*fit\_params [dict of string -> object] Parameters passed to the fit method of each step, where each parameter name is prefixed such that parameter p for step s has key s\_p.

#### Returns

**Xt** [array-like, shape = [n\_samples, n\_transformed\_features]] Transformed samples

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

### inverse\_transform

Apply inverse transformations in reverse order

All estimators in the pipeline must support inverse\_transform.

## **Parameters**

**Xt** [array-like, shape = [n\_samples, n\_transformed\_features]] Data samples, where n\_samples is the number of samples and n\_features is the number of features. Must fulfill input requirements of last step of pipeline's inverse\_transform method.

### **Returns**

**Xt** [array-like, shape = [n\_samples, n\_features]]

predict (self, X, \*\*predict\_params)

Apply transforms to the data, and predict with the final estimator

#### **Parameters**

X [iterable] Data to predict on. Must fulfill input requirements of first step of the pipeline.

\*\*predict\_params [dict of string -> object] Parameters to the predict called at the end of all transformations in the pipeline. Note that while this may be used to return uncertainties from some models with return\_std or return\_cov, uncertainties that are generated by the transformations in the pipeline are not propagated to the final estimator.

#### Returns

```
y_pred [array-like]
```

# predict\_log\_proba (self, X)

Apply transforms, and predict\_log\_proba of the final estimator

### **Parameters**

X [iterable] Data to predict on. Must fulfill input requirements of first step of the pipeline.

#### Returns

```
y_score [array-like, shape = [n_samples, n_classes]]
```

# predict\_proba (self, X)

Apply transforms, and predict\_proba of the final estimator

#### **Parameters**

X [iterable] Data to predict on. Must fulfill input requirements of first step of the pipeline.

### Returns

```
y_proba [array-like, shape = [n_samples, n_classes]]
```

```
score (self, X, y=None, sample_weight=None)
```

Apply transforms, and score with the final estimator

### **Parameters**

- **X** [iterable] Data to predict on. Must fulfill input requirements of first step of the pipeline.
- **y** [iterable, default=None] Targets used for scoring. Must fulfill label requirements for all steps of the pipeline.

**sample\_weight** [array-like, default=None] If not None, this argument is passed as sample\_weight keyword argument to the score method of the final estimator.

#### Returns

score [float]

# set\_params (self, \*\*kwargs)

Set the parameters of this estimator.

Valid parameter keys can be listed with get\_params().

### Returns

self

### transform

Apply transforms, and transform with the final estimator

This also works where final estimator is None: all prior transformations are applied.

## **Parameters**

X [iterable] Data to transform. Must fulfill input requirements of first step of the pipeline.

### **Returns**

**Xt** [array-like, shape = [n\_samples, n\_transformed\_features]]

# Examples using sklearn.pipeline.Pipeline

- Explicit feature map approximation for RBF kernels
- Feature agglomeration vs. univariate selection
- Concatenating multiple feature extraction methods
- Pipelining: chaining a PCA and a logistic regression
- Column Transformer with Mixed Types
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Column Transformer with Heterogeneous Data Sources
- Underfitting vs. Overfitting
- Balance model complexity and cross-validated score
- Sample pipeline for text feature extraction and evaluation
- Comparing Nearest Neighbors with and without Neighborhood Components Analysis
- Restricted Boltzmann Machine features for digit classification
- SVM-Anova: SVM with univariate feature selection
- Classification of text documents using sparse features

pipeline.make_pipeline(\*steps, \*\*kwargs)	Construct a Pipeline from the given estimators.
<pre>pipeline.make_union(\*transformers, \*\*kwargs)</pre>	Construct a FeatureUnion from the given transformers.

# 6.32.3 sklearn.pipeline.make\_pipeline

```
sklearn.pipeline.make_pipeline(*steps, **kwargs)
```

Construct a Pipeline from the given estimators.

This is a shorthand for the Pipeline constructor; it does not require, and does not permit, naming the estimators. Instead, their names will be set to the lowercase of their types automatically.

## Parameters

\*steps [list of estimators.]

memory [None, str or object with the joblib.Memory interface, optional] Used to cache the fitted transformers of the pipeline. By default, no caching is performed. If a string is given, it is the path to the caching directory. Enabling caching triggers a clone of the transformers before fitting. Therefore, the transformer instance given to the pipeline cannot be inspected directly. Use the attribute named\_steps or steps to inspect estimators within the pipeline. Caching the transformers is advantageous when fitting is time consuming.

**verbose** [boolean, optional] If True, the time elapsed while fitting each step will be printed as it is completed.

#### Returns

**p** [Pipeline]

# See also:

**sklearn.pipeline**. Pipeline Class for creating a pipeline of transforms with a final estimator.

# **Examples**

# Examples using sklearn.pipeline.make\_pipeline

- Feature transformations with ensembles of trees
- Pipeline Anova SVM
- Imputing missing values with variants of IterativeImputer
- Imputing missing values before building an estimator
- Polynomial interpolation
- Robust linear estimator fitting
- Dimensionality Reduction with Neighborhood Components Analysis
- Using FunctionTransformer to select columns
- Importance of Feature Scaling
- Feature discretization
- Clustering text documents using k-means

# 6.32.4 sklearn.pipeline.make union

```
sklearn.pipeline.make_union(*transformers, **kwargs)
```

Construct a FeatureUnion from the given transformers.

This is a shorthand for the FeatureUnion constructor; it does not require, and does not permit, naming the transformers. Instead, they will be given names automatically based on their types. It also does not allow weighting.

#### **Parameters**

\*transformers [list of estimators]

n\_jobs [int or None, optional (default=None)] Number of jobs to run in parallel. None means 1
 unless in a joblib.parallel\_backend context. -1 means using all processors. See
 Glossary for more details.

**verbose** [boolean, optional(default=False)] If True, the time elapsed while fitting each transformer will be printed as it is completed.

### Returns

f [FeatureUnion]

### See also:

**sklearn**. **pipeline**. **FeatureUnion** Class for concatenating the results of multiple transformer objects.

# **Examples**

# Examples using sklearn.pipeline.make\_union

• Imputing missing values before building an estimator

# 6.33 sklearn.inspection: inspection

The sklearn.inspection module includes tools for model inspection.

```
inspection.partial_dependence(estimator, X, Partial dependence of features.
...)
inspection.plot_partial_dependence(...[, Partial dependence plots.
...])
```

# 6.33.1 sklearn.inspection.partial dependence

```
sklearn.inspection.partial_dependence (estimator, X, features, response_method='auto', percentiles=(0.05, 0.95), grid_resolution=100, method='auto')
```

Partial dependence of features.

Partial dependence of a feature (or a set of features) corresponds to the average response of an estimator for each possible value of the feature.

Read more in the *User Guide*.

### **Parameters**

**estimator** [BaseEstimator] A fitted estimator object implementing *predict*, *predict\_proba*, or *decision\_function*. Multioutput-multiclass classifiers are not supported.

**X** [array-like, shape (n\_samples, n\_features)] X is used both to generate a grid of values for the features, and to compute the averaged predictions when method is 'brute'.

- **features** [list or array-like of int] The target features for which the partial dependency should be computed.
- **response\_method** ['auto', 'predict\_proba' or 'decision\_function', optional (default='auto')] Specifies whether to use *predict\_proba* or *decision\_function* as the target response. For regressors this parameter is ignored and the response is always the output of *predict*. By default, *predict\_proba* is tried first and we revert to *decision\_function* if it doesn't exist. If method is 'recursion', the response is always the output of *decision\_function*.
- **percentiles** [tuple of float, optional (default=(0.05, 0.95))] The lower and upper percentile used to create the extreme values for the grid. Must be in [0, 1].
- **grid\_resolution** [int, optional (default=100)] The number of equally spaced points on the grid, for each target feature.

**method** [str, optional (default='auto')] The method used to calculate the averaged predictions:

- 'recursion' is only supported for objects inheriting from BaseGradientBoosting, but is more efficient in terms of speed. With this method, X is only used to build the grid and the partial dependences are computed using the training data. This method does not account for the init predicor of the boosting process, which may lead to incorrect values (see warning below). With this method, the target response of a classifier is always the decision function, not the predicted probabilities.
- 'brute' is supported for any estimator, but is more computationally intensive.
- If 'auto', then 'recursion' will be used for BaseGradientBoosting estimators with init=None, and 'brute' for all other.

#### Returns

- averaged\_predictions [ndarray, shape (n\_outputs, len(values[0]), len(values[1]), ...)] The predictions for all the points in the grid, averaged over all samples in X (or over the training data if method is 'recursion'). n\_outputs corresponds to the number of classes in a multi-class setting, or to the number of tasks for multi-output regression. For classical regression and binary classification n\_outputs==1. n\_values\_feature\_j corresponds to the size values[j].
- values [seq of 1d ndarrays] The values with which the grid has been created. The generated grid
  is a cartesian product of the arrays in values. len(values) == len(features).
  The size of each array values[j] is either grid\_resolution, or the number of
  unique values in X[:, j], whichever is smaller.

**Warning:** The 'recursion' method only works for gradient boosting estimators, and unlike the 'brute' method, it does not account for the init predictor of the boosting process. In practice this will produce the same values as 'brute' up to a constant offset in the target response, provided that init is a consant estimator (which is the default). However, as soon as init is not a constant estimator, the partial dependence values are incorrect for 'recursion'.

## See also:

sklearn.inspection.plot\_partial\_dependence Plot partial dependence

# **Examples**

# Examples using sklearn.inspection.partial\_dependence

• Partial Dependence Plots

# 6.33.2 sklearn.inspection.plot\_partial\_dependence

```
sklearn.inspection.plot_partial_dependence (estimator, X, features, feature_names=None, target=None, response_method='auto', n\_cols=3, grid\_resolution=100, percentiles=(0.05, 0.95), method='auto', n\_jobs=None, verbose=0, fig=None, line \ kw=None, contour \ kw=None)
```

Partial dependence plots.

The len (features) plots are arranged in a grid with n\_cols columns. Two-way partial dependence plots are plotted as contour plots.

Read more in the *User Guide*.

### **Parameters**

**estimator** [BaseEstimator] A fitted estimator object implementing *predict*, *predict\_proba*, or *decision\_function*. Multioutput-multiclass classifiers are not supported.

**X** [array-like, shape (n\_samples, n\_features)] The data to use to build the grid of values on which the dependence will be evaluated. This is usually the training data.

**features** [list of {int, str, pair of int, pair of str}] The target features for which to create the PDPs. If features[i] is an int or a string, a one-way PDP is created; if features[i] is a tuple, a two-way PDP is created. Each tuple must be of size 2. if any entry is a string, then it must be in feature\_names.

**feature\_names** [seq of str, shape (n\_features,), optional] Name of each feature; feature\_names[i] holds the name of the feature with index i. By default, the name of the feature corresponds to their numerical index.

target [int, optional (default=None)]

- In a multiclass setting, specifies the class for which the PDPs should be computed. Note that for binary classification, the positive class (index 1) is always used.
- In a multioutput setting, specifies the task for which the PDPs should be computed

Ignored in binary classification or classical regression settings.

**response\_method** ['auto', 'predict\_proba' or 'decision\_function', optional (default='auto'):] Specifies whether to use *predict\_proba* or *decision\_function* as the target response. For regressors this parameter is ignored and the response is always the output of *predict*. By

default, *predict\_proba* is tried first and we revert to *decision\_function* if it doesn't exist. If method is 'recursion', the response is always the output of *decision\_function*.

**n\_cols** [int, optional (default=3)] The maximum number of columns in the grid plot.

**grid\_resolution** [int, optional (default=100)] The number of equally spaced points on the axes of the plots, for each target feature.

**percentiles** [tuple of float, optional (default=(0.05, 0.95))] The lower and upper percentile used to create the extreme values for the PDP axes. Must be in [0, 1].

**method** [str, optional (default='auto')] The method to use to calculate the partial dependence predictions:

- 'recursion' is only supported for objects inheriting from BaseGradientBoosting, but is more efficient in terms of speed. With this method, X is optional and is only used to build the grid and the partial dependences are computed using the training data. This method does not account for the init predictor of the boosting process, which may lead to incorrect values (see warning below. With this method, the target response of a classifier is always the decision function, not the predicted probabilities.
- 'brute' is supported for any estimator, but is more computationally intensive.
- If 'auto', then 'recursion' will be used for BaseGradientBoosting estimators with init=None, and 'brute' for all other.

Unlike the 'brute' method, 'recursion' does not account for the init predictor of the boosting process. In practice this still produces the same plots, up to a constant offset in the target response.

**n\_jobs** [int, optional (default=None)] The number of CPUs to use to compute the partial dependences. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

**verbose** [int, optional (default=0)] Verbose output during PD computations.

**fig** [Matplotlib figure object, optional (default=None)] A figure object onto which the plots will be drawn, after the figure has been cleared. By default, a new one is created.

**line\_kw** [dict, optional] Dict with keywords passed to the matplotlib.pyplot.plot call. For one-way partial dependence plots.

contour\_kw [dict, optional] Dict with keywords passed to the matplotlib.pyplot.plot
call. For two-way partial dependence plots.

**Warning:** The 'recursion' method only works for gradient boosting estimators, and unlike the 'brute' method, it does not account for the init predictor of the boosting process. In practice this will produce the same values as 'brute' up to a constant offset in the target response, provided that init is a consant estimator (which is the default). However, as soon as init is not a constant estimator, the partial dependence values are incorrect for 'recursion'.

### See also:

sklearn.inspection.partial\_dependence Return raw partial dependence values

# **Examples**

```
>>> from sklearn.datasets import make_friedman1
>>> from sklearn.ensemble import GradientBoostingRegressor
>>> X, y = make_friedman1()
>>> clf = GradientBoostingRegressor(n_estimators=10).fit(X, y)
>>> plot_partial_dependence(clf, X, [0, (0, 1)])
```

# **Examples using** sklearn.inspection.plot\_partial\_dependence

• Partial Dependence Plots

# 6.34 sklearn.preprocessing: Preprocessing and Normalization

The *sklearn.preprocessing* module includes scaling, centering, normalization, binarization and imputation methods.

**User guide:** See the *Preprocessing data* section for further details.

preprocessing.Binarizer([threshold, copy])	Binarize data (set feature values to 0 or 1) according to a threshold
<pre>preprocessing.FunctionTransformer([func,])</pre>	Constructs a transformer from an arbitrary callable.
<pre>preprocessing.KBinsDiscretizer([n_bins,])</pre>	Bin continuous data into intervals.
preprocessing.KernelCenterer()	Center a kernel matrix
<pre>preprocessing.LabelBinarizer([neg_label,])</pre>	Binarize labels in a one-vs-all fashion
preprocessing.LabelEncoder	Encode labels with value between 0 and n_classes-1.
preprocessing.MultiLabelBinarizer([classes,	Transform between iterable of iterables and a multilabel
])	format
preprocessing.MaxAbsScaler([copy])	Scale each feature by its maximum absolute value.
preprocessing.MinMaxScaler([feature_range,	Transforms features by scaling each feature to a given
copy])	range.
<pre>preprocessing.Normalizer([norm, copy])</pre>	Normalize samples individually to unit norm.
<pre>preprocessing.OneHotEncoder([n_values,])</pre>	Encode categorical integer features as a one-hot numeric array.
preprocessing.OrdinalEncoder([categories,	Encode categorical features as an integer array.
dtype])	
<pre>preprocessing.PolynomialFeatures([degree,])</pre>	Generate polynomial and interaction features.
<pre>preprocessing.PowerTransformer([method,])</pre>	Apply a power transform featurewise to make data more Gaussian-like.
<pre>preprocessing.QuantileTransformer([])</pre>	Transform features using quantiles information.
<pre>preprocessing.RobustScaler([with_centering,])</pre>	Scale features using statistics that are robust to outliers.
preprocessing.StandardScaler([copy,])	Standardize features by removing the mean and scaling to unit variance

# 6.34.1 sklearn.preprocessing.Binarizer

class sklearn.preprocessing.Binarizer(threshold=0.0, copy=True)

Binarize data (set feature values to 0 or 1) according to a threshold

Values greater than the threshold map to 1, while values less than or equal to the threshold map to 0. With the default threshold of 0, only positive values map to 1.

Binarization is a common operation on text count data where the analyst can decide to only consider the presence or absence of a feature rather than a quantified number of occurrences for instance.

It can also be used as a pre-processing step for estimators that consider boolean random variables (e.g. modelled using the Bernoulli distribution in a Bayesian setting).

Read more in the User Guide.

#### **Parameters**

**threshold** [float, optional (0.0 by default)] Feature values below or equal to this are replaced by 0, above it by 1. Threshold may not be less than 0 for operations on sparse matrices.

**copy** [boolean, optional, default True] set to False to perform inplace binarization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR matrix).

### See also:

binarize Equivalent function without the estimator API.

# **Notes**

If the input is a sparse matrix, only the non-zero values are subject to update by the Binarizer class.

This estimator is stateless (besides constructor parameters), the fit method does nothing but is useful when used in a pipeline.

# **Examples**

#### **Methods**

fit(self, X[, y])	Do nothing and return the estimator unchanged
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
	0 11 1

Continued on next page

Table 6.247 – continued from previous page

set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X[, copy])	Binarize each element of X

\_\_init\_\_ (self, threshold=0.0, copy=True)

### **fit** (self, X, y=None)

Do nothing and return the estimator unchanged

This method is just there to implement the usual API and hence work in pipelines.

#### **Parameters**

X [array-like]

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_<parameter> so that it's possible to update each component of a nested object.

### **Returns**

self

# transform (self, X, copy=None)

Binarize each element of X

#### **Parameters**

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] The data to binarize, element by element. scipy.sparse matrices should be in CSR format to avoid an un-necessary copy.

**copy** [bool] Copy the input X or not.

# 6.34.2 sklearn.preprocessing.FunctionTransformer

Constructs a transformer from an arbitrary callable.

A FunctionTransformer forwards its X (and optionally y) arguments to a user-defined function or function object and returns the result of this function. This is useful for stateless transformations such as taking the log of frequencies, doing custom scaling, etc.

Note: If a lambda is used as the function, then the resulting transformer will not be pickleable.

New in version 0.17.

Read more in the *User Guide*.

#### **Parameters**

**func** [callable, optional default=None] The callable to use for the transformation. This will be passed the same arguments as transform, with args and kwargs forwarded. If func is None, then func will be the identity function.

**inverse\_func** [callable, optional default=None] The callable to use for the inverse transformation. This will be passed the same arguments as inverse transform, with args and kwargs forwarded. If inverse\_func is None, then inverse\_func will be the identity function.

**validate** [bool, optional default=True] Indicate that the input X array should be checked before calling func. The possibilities are:

- If False, there is no input validation.
- If True, then X will be converted to a 2-dimensional NumPy array or sparse matrix. If the conversion is not possible an exception is raised.

Deprecated since version 0.20: validate=True as default will be replaced by validate=False in 0.22.

**accept\_sparse** [boolean, optional] Indicate that func accepts a sparse matrix as input. If validate is False, this has no effect. Otherwise, if accept\_sparse is false, sparse matrix inputs will cause an exception to be raised.

pass\_y [bool, optional default=False] Indicate that transform should forward the y argument to the inner callable.

Deprecated since version 0.19.

**check\_inverse** [bool, default=True] Whether to check that or func followed by inverse\_func leads to the original inputs. It can be used for a sanity check, raising a warning when the condition is not fulfilled.

New in version 0.20.

kw\_args [dict, optional] Dictionary of additional keyword arguments to pass to func.

inv\_kw\_args [dict, optional] Dictionary of additional keyword arguments to pass to inverse func.

# **Methods**

fit(self, X[, y])	Fit transformer by checking X.
$fit_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Transform X using the inverse function.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform X using the forward function.

\_\_init\_\_ (self, func=None, inverse\_func=None, validate=None, accept\_sparse=False, pass\_y='deprecated', check\_inverse=True, kw\_args=None, inv\_kw\_args=None)

# fit (self, X, y=None)

Fit transformer by checking X.

If validate is True, X will be checked.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Input array.

#### Returns

self

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit params and returns a transformed version of X.

# **Parameters**

**X** [numpy array of shape [n\_samples, n\_features]] Training set.

y [numpy array of shape [n\_samples]] Target values.

# Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

# $inverse\_transform(self, X)$

Transform X using the inverse function.

# **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Input array.

### **Returns**

**X\_out** [array-like, shape (n\_samples, n\_features)] Transformed input.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, X)

Transform X using the forward function.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] Input array.

### Returns

**X\_out** [array-like, shape (n\_samples, n\_features)] Transformed input.

# Examples using sklearn.preprocessing.FunctionTransformer

• Using FunctionTransformer to select columns

# 6.34.3 sklearn.preprocessing.KBinsDiscretizer

Bin continuous data into intervals.

Read more in the User Guide.

### **Parameters**

**n\_bins** [int or array-like, shape (n\_features,) (default=5)] The number of bins to produce. Raises ValueError if n\_bins < 2.

**encode** [{'onehot', 'onehot-dense', 'ordinal'}, (default='onehot')] Method used to encode the transformed result.

**onehot** Encode the transformed result with one-hot encoding and return a sparse matrix. Ignored features are always stacked to the right.

**onehot-dense** Encode the transformed result with one-hot encoding and return a dense array. Ignored features are always stacked to the right.

**ordinal** Return the bin identifier encoded as an integer value.

**strategy** [{'uniform', 'quantile', 'kmeans'}, (default='quantile')] Strategy used to define the widths of the bins.

**uniform** All bins in each feature have identical widths.

quantile All bins in each feature have the same number of points.

**kmeans** Values in each bin have the same nearest center of a 1D k-means cluster.

### **Attributes**

**n\_bins**\_ [int array, shape (n\_features,)] Number of bins per feature. Bins whose width are too small (i.e., <= 1e-8) are removed with a warning.

**bin\_edges\_** [array of arrays, shape (n\_features, )] The edges of each bin. Contain arrays of varying shapes (n\_bins\_, ) Ignored features will have empty arrays.

#### See also:

**sklearn.preprocessing.Binarizer** class used to bin values as 0 or 1 based on a parameter threshold.

# **Notes**

In bin edges for feature i, the first and last values are used only for inverse\_transform. During transform, bin edges are extended to:

```
np.concatenate([-np.inf, bin_edges_[i][1:-1], np.inf])
```

You can combine KBinsDiscretizer with sklearn.compose.ColumnTransformer if you only want to preprocess part of the features.

KBinsDiscretizer might produce constant features (e.g., when encode = 'onehot' and certain bins do not contain any data). These features can be removed with feature selection algorithms (e.g., sklearn. feature selection. VarianceThreshold).

# **Examples**

```
>>> X = [[-2, 1, -4, -1],
... [-1, 2, -3, -0.5],
... [ 0, 3, -2, 0.5],
... [ 1, 4, -1, 2]]
>>> est = KBinsDiscretizer(n_bins=3, encode='ordinal', strategy='uniform')
>>> est.fit(X)
KBinsDiscretizer(...)
>>> Xt = est.transform(X)
>>> Xt
array([[ 0., 0., 0., 0.],
        [ 1., 1., 1., 0.],
        [ 2., 2., 2., 1.],
        [ 2., 2., 2., 2.]])
```

Sometimes it may be useful to convert the data back into the original feature space. The inverse\_transform function converts the binned data into the original feature space. Each value will be equal to the mean of the two bin edges.

# **Methods**

fit(self, X[, y])	Fits the estimator.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, Xt)	Transforms discretized data back to original feature
	space.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Discretizes the data.

\_\_init\_\_ (self, n\_bins=5, encode='onehot', strategy='quantile')

**fit** (*self*, *X*, *y=None*)

Fits the estimator.

### **Parameters**

**X** [numeric array-like, shape (n\_samples, n\_features)] Data to be discretized.

y [ignored]

### Returns

self

fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

### get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

# $inverse\_transform(self, Xt)$

Transforms discretized data back to original feature space.

Note that this function does not regenerate the original data due to discretization rounding.

### **Parameters**

**Xt** [numeric array-like, shape (n\_sample, n\_features)] Transformed data in the binned space.

# Returns

**Xinv** [numeric array-like] Data in the original feature space.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, X)

Discretizes the data.

#### **Parameters**

**X** [numeric array-like, shape (n\_samples, n\_features)] Data to be discretized.

### Returns

**Xt** [numeric array-like or sparse matrix] Data in the binned space.

# Examples using sklearn.preprocessing.KBinsDiscretizer

- Using KBinsDiscretizer to discretize continuous features
- Demonstrating the different strategies of KBinsDiscretizer
- Feature discretization

# 6.34.4 sklearn.preprocessing.KernelCenterer

class sklearn.preprocessing.KernelCenterer

Center a kernel matrix

Let K(x, z) be a kernel defined by  $phi(x)^T phi(z)$ , where phi is a function mapping x to a Hilbert space. KernelCenterer centers (i.e., normalize to have zero mean) the data without explicitly computing phi(x). It is equivalent to centering phi(x) with sklearn.preprocessing.StandardScaler(with\_std=False).

Read more in the User Guide.

# **Examples**

```
[ 0., 14., -14.],
[ -5., -14., 19.]])
```

# **Methods**

fit(self, K[, y])	Fit KernelCenterer
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, K[, copy])	Center kernel matrix.

```
__init__ (self)
fit (self, K, y=None)
```

Fit KernelCenterer

#### **Parameters**

**K** [numpy array of shape [n\_samples, n\_samples]] Kernel matrix.

### Returns

self [returns an instance of self.]

# fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

# Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

### get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

```
transform (self, K, copy=True)
```

Center kernel matrix.

#### **Parameters**

**K** [numpy array of shape [n\_samples1, n\_samples2]] Kernel matrix.

**copy** [boolean, optional, default True] Set to False to perform inplace computation.

#### **Returns**

**K\_new** [numpy array of shape [n\_samples1, n\_samples2]]

# 6.34.5 sklearn.preprocessing.LabelBinarizer

Binarize labels in a one-vs-all fashion

Several regression and binary classification algorithms are available in scikit-learn. A simple way to extend these algorithms to the multi-class classification case is to use the so-called one-vs-all scheme.

At learning time, this simply consists in learning one regressor or binary classifier per class. In doing so, one needs to convert multi-class labels to binary labels (belong or does not belong to the class). LabelBinarizer makes this process easy with the transform method.

At prediction time, one assigns the class for which the corresponding model gave the greatest confidence. LabelBinarizer makes this easy with the inverse\_transform method.

Read more in the *User Guide*.

## **Parameters**

**neg\_label** [int (default: 0)] Value with which negative labels must be encoded.

**pos\_label** [int (default: 1)] Value with which positive labels must be encoded.

**sparse\_output** [boolean (default: False)] True if the returned array from transform is desired to be in sparse CSR format.

### Attributes

classes\_ [array of shape [n\_class]] Holds the label for each class.

**y\_type\_** [str,] Represents the type of the target data as evaluated by utils.multiclass.type\_of\_target. Possible type are 'continuous', 'continuous-multioutput', 'binary', 'multiclass', 'multiclass-multioutput', 'multilabel-indicator', and 'unknown'.

**sparse\_input\_** [boolean,] True if the input data to transform is given as a sparse matrix, False otherwise.

### See also:

label binarize function to perform the transform operation of LabelBinarizer with fixed classes.

sklearn.preprocessing.OneHotEncoder encode categorical features using a one-hot aka one-of-K scheme.

# **Examples**

# Binary targets transform to a column vector

```
>>> lb = preprocessing.LabelBinarizer()
>>> lb.fit_transform(['yes', 'no', 'no', 'yes'])
array([[1],
        [0],
        [0],
        [1]])
```

# Passing a 2D matrix for multilabel classification

### **Methods**

fit(self, y)	Fit label binarizer
fit_transform(self, y)	Fit label binarizer and transform multi-class labels to
	binary labels.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>inverse_transform(self, Y[, threshold])</pre>	Transform binary labels back to multi-class labels
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, y)	Transform multi-class labels to binary labels

```
__init__ (self, neg_label=0, pos_label=1, sparse_output=False)

fit (self, y)

Fit label binarizer
```

# **Parameters**

**y** [array of shape [n\_samples,] or [n\_samples, n\_classes]] Target values. The 2-d matrix should only contain 0 and 1, represents multilabel classification.

# Returns

**self** [returns an instance of self.]

### fit transform(self, y)

Fit label binarizer and transform multi-class labels to binary labels.

The output of transform is sometimes referred to as the 1-of-K coding scheme.

# **Parameters**

y [array or sparse matrix of shape [n\_samples,] or [n\_samples, n\_classes]] Target values. The 2-d matrix should only contain 0 and 1, represents multilabel classification. Sparse matrix can be CSR, CSC, COO, DOK, or LIL.

### **Returns**

Y [array or CSR matrix of shape [n\_samples, n\_classes]] Shape will be [n\_samples, 1] for binary problems.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

# inverse\_transform(self, Y, threshold=None)

Transform binary labels back to multi-class labels

#### **Parameters**

Y [numpy array or sparse matrix with shape [n\_samples, n\_classes]] Target values. All sparse matrices are converted to CSR before inverse transformation.

threshold [float or None] Threshold used in the binary and multi-label cases.

Use 0 when Y contains the output of decision\_function (classifier). Use 0.5 when Y contains the output of predict\_proba.

If None, the threshold is assumed to be half way between neg\_label and pos\_label.

### Returns

y [numpy array or CSR matrix of shape [n\_samples] Target values.]

# **Notes**

In the case when the binary labels are fractional (probabilistic), inverse\_transform chooses the class with the greatest value. Typically, this allows to use the output of a linear model's decision\_function method directly as the input of inverse\_transform.

# set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

#### self

#### transform (self, y)

Transform multi-class labels to binary labels

The output of transform is sometimes referred to by some authors as the 1-of-K coding scheme.

# **Parameters**

**y** [array or sparse matrix of shape [n\_samples,] or [n\_samples, n\_classes]] Target values. The 2-d matrix should only contain 0 and 1, represents multilabel classification. Sparse matrix can be CSR, CSC, COO, DOK, or LIL.

### **Returns**

Y [numpy array or CSR matrix of shape [n\_samples, n\_classes]] Shape will be [n\_samples, 1] for binary problems.

# 6.34.6 sklearn.preprocessing.LabelEncoder

```
class sklearn.preprocessing.LabelEncoder
```

Encode labels with value between 0 and n classes-1.

Read more in the *User Guide*.

#### **Attributes**

**classes**\_ [array of shape (n\_class,)] Holds the label for each class.

### See also:

**sklearn.preprocessing.OrdinalEncoder** encode categorical features using a one-hot or ordinal encoding scheme.

# **Examples**

LabelEncoder can be used to normalize labels.

```
>>> from sklearn import preprocessing
>>> le = preprocessing.LabelEncoder()
>>> le.fit([1, 2, 2, 6])
LabelEncoder()
>>> le.classes_
array([1, 2, 6])
>>> le.transform([1, 1, 2, 6])
array([0, 0, 1, 2]...)
>>> le.inverse_transform([0, 0, 1, 2])
array([1, 1, 2, 6])
```

It can also be used to transform non-numerical labels (as long as they are hashable and comparable) to numerical labels.

```
>>> le = preprocessing.LabelEncoder()
>>> le.fit(["paris", "paris", "tokyo", "amsterdam"])
LabelEncoder()
>>> list(le.classes_)
['amsterdam', 'paris', 'tokyo']
>>> le.transform(["tokyo", "tokyo", "paris"])
array([2, 2, 1]...)
```

```
>>> list(le.inverse_transform([2, 2, 1]))
['tokyo', 'tokyo', 'paris']
```

# **Methods**

fit(self, y)	Fit label encoder
fit_transform(self, y)	Fit label encoder and return encoded labels
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, y)	Transform labels back to original encoding.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, y)	Transform labels to normalized encoding.

```
__init__ (self, /, *args, **kwargs)
```

Initialize self. See help(type(self)) for accurate signature.

# **fit** (self, y)

Fit label encoder

### **Parameters**

y [array-like of shape (n\_samples,)] Target values.

### Returns

self [returns an instance of self.]

# $fit_tmnsform(self, y)$

Fit label encoder and return encoded labels

## **Parameters**

y [array-like of shape [n\_samples]] Target values.

#### Returns

y [array-like of shape [n\_samples]]

## get\_params (self, deep=True)

Get parameters for this estimator.

# **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

### inverse transform(self, y)

Transform labels back to original encoding.

# **Parameters**

y [numpy array of shape [n\_samples]] Target values.

# Returns

y [numpy array of shape [n\_samples]]

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform (self, y)

Transform labels to normalized encoding.

#### **Parameters**

y [array-like of shape [n\_samples]] Target values.

### **Returns**

y [array-like of shape [n\_samples]]

# 6.34.7 sklearn.preprocessing.MultiLabelBinarizer

class sklearn.preprocessing.MultiLabelBinarizer(classes=None, sparse\_output=False)
 Transform between iterable of iterables and a multilabel format

Although a list of sets or tuples is a very intuitive format for multilabel data, it is unwieldy to process. This transformer converts between this intuitive format and the supported multilabel format: a (samples x classes) binary matrix indicating the presence of a class label.

#### **Parameters**

**classes** [array-like of shape [n\_classes] (optional)] Indicates an ordering for the class labels. All entries should be unique (cannot contain duplicate classes).

**sparse\_output** [boolean (default: False),] Set to true if output binary array is desired in CSR sparse format

### **Attributes**

**classes** [array of labels] A copy of the classes parameter where provided, or otherwise, the sorted set of classes found when fitting.

# See also:

sklearn.preprocessing.OneHotEncoder encode categorical features using a one-hot aka one-of-K scheme.

# **Examples**

### **Methods**

fit(self, y)	Fit the label sets binarizer, storing <i>classes</i> _
fit_transform(self, y)	Fit the label sets binarizer and transform the given label
	sets
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, yt)	Transform the given indicator matrix into label sets
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, y)	Transform the given label sets

```
___init__ (self, classes=None, sparse_output=False)
```

# fit(self, y)

Fit the label sets binarizer, storing *classes*\_

### **Parameters**

y [iterable of iterables] A set of labels (any orderable and hashable object) for each sample. If the classes parameter is set, y will not be iterated.

#### **Returns**

self [returns this MultiLabelBinarizer instance]

# fit\_transform(self, y)

Fit the label sets binarizer and transform the given label sets

### **Parameters**

y [iterable of iterables] A set of labels (any orderable and hashable object) for each sample. If the classes parameter is set, y will not be iterated.

# Returns

y\_indicator [array or CSR matrix, shape (n\_samples, n\_classes)] A matrix such that y\_indicator[i, j] = 1 iff classes\_[j] is in y[i], and 0 otherwise.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

# inverse\_transform(self, yt)

Transform the given indicator matrix into label sets

# **Parameters**

yt [array or sparse matrix of shape (n\_samples, n\_classes)] A matrix containing only 1s ands 0s.

#### Returns

y [list of tuples] The set of labels for each sample such that y[i] consists of classes\_[j] for each yt[i, j] == 1.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# transform(self, y)

Transform the given label sets

#### **Parameters**

y [iterable of iterables] A set of labels (any orderable and hashable object) for each sample. If the classes parameter is set, y will not be iterated.

### **Returns**

```
y_indicator [array or CSR matrix, shape (n_samples, n_classes)] A matrix such that
y_indicator[i, j] = 1 iff classes_[j] is in y[i], and 0 otherwise.
```

# 6.34.8 sklearn.preprocessing.MaxAbsScaler

```
class sklearn.preprocessing.MaxAbsScaler(copy=True)
```

Scale each feature by its maximum absolute value.

This estimator scales and translates each feature individually such that the maximal absolute value of each feature in the training set will be 1.0. It does not shift/center the data, and thus does not destroy any sparsity.

This scaler can also be applied to sparse CSR or CSC matrices.

New in version 0.17.

# Parameters

**copy** [boolean, optional, default is True] Set to False to perform inplace scaling and avoid a copy (if the input is already a numpy array).

### **Attributes**

**scale\_** [ndarray, shape (n\_features,)] Per feature relative scaling of the data.

New in version 0.17: *scale*\_ attribute.

max\_abs\_ [ndarray, shape (n\_features,)] Per feature maximum absolute value.

**n\_samples\_seen\_** [int] The number of samples processed by the estimator. Will be reset on new calls to fit, but increments across partial\_fit calls.

### See also:

maxabs\_scale Equivalent function without the estimator API.

# **Notes**

NaNs are treated as missing values: disregarded in fit, and maintained in transform.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

# **Examples**

### **Methods**

fit(self, X[, y])	Compute the maximum absolute value to be used for
	later scaling.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Scale back the data to the original representation
<pre>partial_fit(self, X[, y])</pre>	Online computation of max absolute value of X for later
	scaling.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Scale the data

```
__init__ (self, copy=True)
```

# fit (self, X, y=None)

Compute the maximum absolute value to be used for later scaling.

### **Parameters**

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] The data used to compute the per-feature minimum and maximum used for later scaling along the features axis.

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

# **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- **y** [numpy array of shape [n\_samples]] Target values.

#### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

### inverse\_transform(self, X)

Scale back the data to the original representation

#### **Parameters**

**X** [{array-like, sparse matrix}] The data that should be transformed back.

```
partial_fit (self, X, y=None)
```

Online computation of max absolute value of X for later scaling. All of X is processed as a single batch. This is intended for cases when fit is not feasible due to very large number of  $n\_samples$  or because X is read from a continuous stream.

### **Parameters**

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] The data used to compute the mean and standard deviation used for later scaling along the features axis.

y Ignored

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# transform(self, X)

Scale the data

#### **Parameters**

**X** [{array-like, sparse matrix}] The data that should be scaled.

# Examples using sklearn.preprocessing.MaxAbsScaler

• Compare the effect of different scalers on data with outliers

# 6.34.9 sklearn.preprocessing.MinMaxScaler

```
class sklearn.preprocessing.MinMaxScaler (feature_range=(0, 1), copy=True)
```

Transforms features by scaling each feature to a given range.

This estimator scales and translates each feature individually such that it is in the given range on the training set, e.g. between zero and one.

The transformation is given by:

```
X_std = (X - X.min(axis=0)) / (X.max(axis=0) - X.min(axis=0))
X_scaled = X_std * (max - min) + min
```

where min,  $max = feature\_range$ .

The transformation is calculated as:

```
X_scaled = scale * X + min - X.min(axis=0) * scale
where scale = (max - min) / (X.max(axis=0) - X.min(axis=0))
```

This transformation is often used as an alternative to zero mean, unit variance scaling.

Read more in the *User Guide*.

### **Parameters**

**feature\_range** [tuple (min, max), default=(0, 1)] Desired range of transformed data.

**copy** [boolean, optional, default True] Set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array).

#### **Attributes**

```
min_ [ndarray, shape (n_features,)] Per feature adjustment for minimum. Equivalent to min - X.min(axis=0) * self.scale_
```

New in version 0.17: *scale\_* attribute.

data\_min\_ [ndarray, shape (n\_features,)] Per feature minimum seen in the data

New in version 0.17: data\_min\_

data\_max\_ [ndarray, shape (n\_features,)] Per feature maximum seen in the data

New in version 0.17: data max

data\_range\_ [ndarray, shape (n\_features,)] Per feature range (data\_max\_ data\_min\_) seen in the data

New in version 0.17: data\_range\_

## See also:

minmax\_scale Equivalent function without the estimator API.

## **Notes**

NaNs are treated as missing values: disregarded in fit, and maintained in transform.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## **Examples**

### **Methods**

fit(self, X[, y])	Compute the minimum and maximum to be used for
	later scaling.
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Undo the scaling of X according to feature_range.
<pre>partial_fit(self, X[, y])</pre>	Online computation of min and max on X for later scal-
	ing.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Scaling features of X according to feature_range.

```
__init__ (self, feature_range=(0, 1), copy=True)
```

## fit (self, X, y=None)

Compute the minimum and maximum to be used for later scaling.

#### Parameters

**X** [array-like, shape [n\_samples, n\_features]] The data used to compute the per-feature minimum and maximum used for later scaling along the features axis.

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- $\boldsymbol{X}$  [numpy array of shape [n\_samples, n\_features]] Training set.
- $\boldsymbol{y} \;$  [numpy array of shape [n\_samples]] Target values.

## Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## inverse\_transform(self, X)

Undo the scaling of X according to feature\_range.

#### **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] Input data that will be transformed. It cannot be sparse.

## partial\_fit (self, X, y=None)

Online computation of min and max on X for later scaling. All of X is processed as a single batch. This is intended for cases when fit is not feasible due to very large number of  $n\_samples$  or because X is read from a continuous stream.

### **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] The data used to compute the mean and standard deviation used for later scaling along the features axis.

y Ignored

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## transform(self, X)

Scaling features of X according to feature\_range.

## **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] Input data that will be transformed.

## Examples using sklearn.preprocessing.MinMaxScaler

- Compare Stochastic learning strategies for MLPClassifier
- Compare the effect of different scalers on data with outliers

## 6.34.10 sklearn.preprocessing.Normalizer

class sklearn.preprocessing.Normalizer(norm='l2', copy=True)

Normalize samples individually to unit norm.

Each sample (i.e. each row of the data matrix) with at least one non zero component is rescaled independently of other samples so that its norm (11 or 12) equals one.

This transformer is able to work both with dense numpy arrays and scipy.sparse matrix (use CSR format if you want to avoid the burden of a copy / conversion).

Scaling inputs to unit norms is a common operation for text classification or clustering for instance. For instance the dot product of two 12-normalized TF-IDF vectors is the cosine similarity of the vectors and is the base similarity metric for the Vector Space Model commonly used by the Information Retrieval community.

Read more in the User Guide.

## **Parameters**

**norm** ['11', '12', or 'max', optional ('12' by default)] The norm to use to normalize each non zero sample.

**copy** [boolean, optional, default True] set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR matrix).

### See also:

normalize Equivalent function without the estimator API.

#### **Notes**

This estimator is stateless (besides constructor parameters), the fit method does nothing but is useful when used in a pipeline.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## **Examples**

### Methods

fit(self, X[, y])	Do nothing and return the estimator unchanged
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X[, copy])	Scale each non zero row of X to unit norm

```
__init__ (self, norm='l2', copy=True)
```

**fit** (self, X, y=None)

Do nothing and return the estimator unchanged

This method is just there to implement the usual API and hence work in pipelines.

## **Parameters**

X [array-like]

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

## transform(self, X, copy=None)

Scale each non zero row of X to unit norm

## **Parameters**

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] The data to normalize, row by row. scipy.sparse matrices should be in CSR format to avoid an un-necessary copy.

**copy** [bool, optional (default: None)] Copy the input X or not.

## Examples using sklearn.preprocessing.Normalizer

- Compare the effect of different scalers on data with outliers
- Clustering text documents using k-means

## 6.34.11 sklearn.preprocessing.OneHotEncoder

Encode categorical integer features as a one-hot numeric array.

The input to this transformer should be an array-like of integers or strings, denoting the values taken on by categorical (discrete) features. The features are encoded using a one-hot (aka 'one-of-K' or 'dummy') encoding scheme. This creates a binary column for each category and returns a sparse matrix or dense array.

By default, the encoder derives the categories based on the unique values in each feature. Alternatively, you can also specify the categories manually. The OneHotEncoder previously assumed that the input features take on values in the range [0, max(values)). This behaviour is deprecated.

This encoding is needed for feeding categorical data to many scikit-learn estimators, notably linear models and SVMs with the standard kernels.

Note: a one-hot encoding of y labels should use a LabelBinarizer instead.

Read more in the User Guide.

### **Parameters**

**categories** ['auto' or a list of lists/arrays of values, default='auto'.] Categories (unique values) per feature:

- 'auto' : Determine categories automatically from the training data.
- list: categories[i] holds the categories expected in the ith column. The passed categories should not mix strings and numeric values within a single feature, and should be sorted in case of numeric values.

The used categories can be found in the categories\_attribute.

- **drop** ['first' or a list/array of shape (n\_features,), default=None.] Specifies a methodology to use to drop one of the categories per feature. This is useful in situations where perfectly collinear features cause problems, such as when feeding the resulting data into a neural network or an unregularized regression.
  - None: retain all features (the default).
  - 'first': drop the first category in each feature. If only one category is present, the feature will be dropped entirely.
  - array : drop[i] is the category in feature X[:, i] that should be dropped.

sparse [boolean, default=True] Will return sparse matrix if set True else will return an array.

**dtype** [number type, default=np.float] Desired dtype of output.

handle\_unknown ['error' or 'ignore', default='error'.] Whether to raise an error or ignore if an unknown categorical feature is present during transform (default is to raise). When this parameter is set to 'ignore' and an unknown category is encountered during transform, the resulting one-hot encoded columns for this feature will be all zeros. In the inverse transform, an unknown category will be denoted as None.

**n values** ['auto', int or array of ints, default='auto'] Number of values per feature.

- 'auto' : determine value range from training data.
- int [number of categorical values per feature.] Each feature value should be in range (n\_values)

• array [n\_values[i] is the number of categorical values in] X[:, i]. Each feature value should be in range (n\_values[i])

Deprecated since version 0.20: The n\_values keyword was deprecated in version 0.20 and will be removed in 0.22. Use categories instead.

- **categorical\_features** ['all' or array of indices or mask, default='all'] Specify what features are treated as categorical.
  - 'all': All features are treated as categorical.
  - array of indices: Array of categorical feature indices.
  - mask: Array of length n\_features and with dtype=bool.

Non-categorical features are always stacked to the right of the matrix.

Deprecated since version 0.20: The categorical\_features keyword was deprecated in version 0.20 and will be removed in 0.22. You can use the ColumnTransformer instead.

#### Attributes

- **categories**\_ [list of arrays] The categories of each feature determined during fitting (in order of the features in X and corresponding with the output of transform). This includes the category specified in drop (if any).
- drop\_idx\_ [array of shape (n\_features,)] drop\_idx\_[i] is the index in categories\_[i]
   of the category to be dropped for each feature. None if all the transformed features will be
   retained.
- **active\_features\_** [array] Indices for active features, meaning values that actually occur in the training set. Only available when n\_values is 'auto'.

Deprecated since version 0.20: The active\_features\_attribute was deprecated in version 0.20 and will be removed in 0.22.

feature\_indices\_ [array of shape (n\_features,)] Indices to feature ranges. Feature
 i in the original data is mapped to features from feature\_indices\_[i] to
 feature\_indices\_[i+1] (and then potentially masked by active\_features\_afterwards)

Deprecated since version 0.20: The feature\_indices\_attribute was deprecated in version 0.20 and will be removed in 0.22.

**n\_values\_** [array of shape (n\_features,)] Maximum number of values per feature.

Deprecated since version 0.20: The n\_values\_ attribute was deprecated in version 0.20 and will be removed in 0.22.

## See also:

- **sklearn.preprocessing.OrdinalEncoder** performs an ordinal (integer) encoding of the categorical features.
- **sklearn.feature\_extraction.DictVectorizer** performs a one-hot encoding of dictionary items (also handles string-valued features).
- **sklearn. feature\_extraction. FeatureHasher** performs an approximate one-hot encoding of dictionary items or strings.
- sklearn.preprocessing.LabelBinarizer binarizes labels in a one-vs-all fashion.

**sklearn.preprocessing.MultiLabelBinarizer** transforms between iterable of iterables and a multilabel format, e.g. a (samples x classes) binary matrix indicating the presence of a class label.

## **Examples**

Given a dataset with two features, we let the encoder find the unique values per feature and transform the data to a binary one-hot encoding.

```
>>> enc.categories_
[array(['Female', 'Male'], dtype=object), array([1, 2, 3], dtype=object)]
>>> enc.transform([['Female', 1], ['Male', 4]]).toarray()
array([[1., 0., 1., 0., 0.],
       [0., 1., 0., 0., 0.]])
>>> enc.inverse_transform([[0, 1, 1, 0, 0], [0, 0, 0, 1, 0]])
array([['Male', 1],
       [None, 2]], dtype=object)
>>> enc.get_feature_names()
array(['x0_Female', 'x0_Male', 'x1_1', 'x1_2', 'x1_3'], dtype=object)
>>> drop_enc = OneHotEncoder(drop='first').fit(X)
>>> drop_enc.categories_
[array(['Female', 'Male'], dtype=object), array([1, 2, 3], dtype=object)]
>>> drop_enc.transform([['Female', 1], ['Male', 2]]).toarray()
array([[0., 0., 0.],
       [1., 1., 0.]])
```

#### **Methods**

fit(self, X[, y])	Fit OneHotEncoder to X.
$fit\_transform(self, X[, y])$	Fit OneHotEncoder to X, then transform X.
<pre>get_feature_names(self[, input_features])</pre>	Return feature names for output features.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Convert the back data to the original representation.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform X using one-hot encoding.

```
__init__ (self, n_values=None, categorical_features=None, categories=None, drop=None, sparse=True, dtype=<class 'numpy.float64'>, handle_unknown='error')
```

```
fit (self, X, y=None)
```

Fit OneHotEncoder to X.

#### **Parameters**

X [array-like, shape [n\_samples, n\_features]] The data to determine the categories of each

feature.

#### Returns

self

## fit\_transform(self, X, y=None)

Fit OneHotEncoder to X, then transform X.

Equivalent to fit(X).transform(X) but more convenient.

## **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] The data to encode.

#### Returns

**X\_out** [sparse matrix if sparse=True else a 2-d array] Transformed input.

## get\_feature\_names (self, input\_features=None)

Return feature names for output features.

#### **Parameters**

**input\_features** [list of string, length n\_features, optional] String names for input features if available. By default, "x0", "x1", ... "xn\_features" is used.

## Returns

**output feature names** [array of string, length n output features]

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

### inverse\_transform(self, X)

Convert the back data to the original representation.

In case unknown categories are encountered (all zeros in the one-hot encoding), None is used to represent this category.

### **Parameters**

**X** [array-like or sparse matrix, shape [n\_samples, n\_encoded\_features]] The transformed data.

### Returns

**X\_tr** [array-like, shape [n\_samples, n\_features]] Inverse transformed array.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

```
transform(self, X)
```

Transform X using one-hot encoding.

#### **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] The data to encode.

### **Returns**

**X\_out** [sparse matrix if sparse=True else a 2-d array] Transformed input.

## Examples using sklearn.preprocessing.OneHotEncoder

- Column Transformer with Mixed Types
- Feature transformations with ensembles of trees

## 6.34.12 sklearn.preprocessing.OrdinalEncoder

Encode categorical features as an integer array.

The input to this transformer should be an array-like of integers or strings, denoting the values taken on by categorical (discrete) features. The features are converted to ordinal integers. This results in a single column of integers (0 to n\_categories - 1) per feature.

Read more in the *User Guide*.

#### **Parameters**

categories ['auto' or a list of lists/arrays of values.] Categories (unique values) per feature:

- 'auto': Determine categories automatically from the training data.
- list: categories[i] holds the categories expected in the ith column. The passed categories should not mix strings and numeric values, and should be sorted in case of numeric values.

The used categories can be found in the categories\_attribute.

**dtype** [number type, default np.float64] Desired dtype of output.

## Attributes

**categories**\_ [list of arrays] The categories of each feature determined during fitting (in order of the features in X and corresponding with the output of transform).

### See also:

```
sklearn.preprocessing.OneHotEncoder performs a one-hot encoding of categorical features.
sklearn.preprocessing.LabelEncoder encodes target labels with values between 0 and n_classes-
1.
```

## **Examples**

Given a dataset with two features, we let the encoder find the unique values per feature and transform the data to an ordinal encoding.

## **Methods**

fit(self, X[, y])	Fit the OrdinalEncoder to X.
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Convert the data back to the original representation.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform X to ordinal codes.

```
__init__ (self, categories='auto', dtype=<class 'numpy.float64'>)
fit (self, X, y=None)
```

Fit the OrdinalEncoder to X.

## **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] The data to determine the categories of each feature.

#### Returns

self

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

## Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

#### inverse\_transform(self, X)

Convert the data back to the original representation.

#### **Parameters**

X [array-like or sparse matrix, shape [n\_samples, n\_encoded\_features]] The transformed data

#### Returns

**X\_tr** [array-like, shape [n\_samples, n\_features]] Inverse transformed array.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### **Returns**

self

## transform(self, X)

Transform X to ordinal codes.

### **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] The data to encode.

#### Returns

**X\_out** [sparse matrix or a 2-d array] Transformed input.

## 6.34.13 sklearn.preprocessing.PolynomialFeatures

Generate polynomial and interaction features.

Generate a new feature matrix consisting of all polynomial combinations of the features with degree less than or equal to the specified degree. For example, if an input sample is two dimensional and of the form [a, b], the degree-2 polynomial features are [1, a, b, a^2, ab, b^2].

#### **Parameters**

**degree** [integer] The degree of the polynomial features. Default = 2.

```
interaction_only [boolean, default = False] If true, only interaction features are produced: features that are products of at most degree distinct input features (so not x[1] ** 2, x[0] * x[2] ** 3, etc.).
```

**include\_bias** [boolean] If True (default), then include a bias column, the feature in which all polynomial powers are zero (i.e. a column of ones - acts as an intercept term in a linear model).

**order** [str in {'C', 'F'}, default 'C'] Order of output array in the dense case. 'F' order is faster to compute, but may slow down subsequent estimators.

New in version 0.21.

## **Attributes**

**powers**\_ [array, shape (n\_output\_features, n\_input\_features)] powers\_[i, j] is the exponent of the jth input in the ith output.

**n\_input\_features\_** [int] The total number of input features.

**n\_output\_features**\_ [int] The total number of polynomial output features. The number of output features is computed by iterating over all suitably sized combinations of input features.

#### **Notes**

Be aware that the number of features in the output array scales polynomially in the number of features of the input array, and exponentially in the degree. High degrees can cause overfitting.

See examples/linear\_model/plot\_polynomial\_interpolation.py

## **Examples**

```
>>> import numpy as np
>>> from sklearn.preprocessing import PolynomialFeatures
>>> X = np.arange(6).reshape(3, 2)
>>> X
array([[0, 1],
       [2, 3],
       [4, 5]])
>>> poly = PolynomialFeatures(2)
>>> poly.fit_transform(X)
array([[ 1., 0., 1., 0., 0., 1.],
      [ 1., 2., 3., 4., 6., 9.],
       [ 1., 4., 5., 16., 20., 25.]])
>>> poly = PolynomialFeatures(interaction_only=True)
>>> poly.fit_transform(X)
array([[ 1., 0., 1., 0.],
       [ 1., 2., 3., 6.],
       [ 1., 4.,
                 5., 20.]])
```

## **Methods**

fit(self, X[, y])	Compute number of output features.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_feature_names(self[, input_features])</pre>	Return feature names for output features
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Transform data to polynomial features

```
__init__ (self, degree=2, interaction_only=False, include_bias=True, order='C')
fit (self, X, y=None)
```

Compute number of output features.

### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The data.

## Returns

**self** [instance]

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

**X** [numpy array of shape [n\_samples, n\_features]] Training set.

y [numpy array of shape [n\_samples]] Target values.

### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_feature\_names (self, input\_features=None)

Return feature names for output features

## **Parameters**

**input\_features** [list of string, length n\_features, optional] String names for input features if available. By default, "x0", "x1", ... "xn\_features" is used.

#### **Returns**

output\_feature\_names [list of string, length n\_output\_features]

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

### transform(self, X)

Transform data to polynomial features

#### **Parameters**

**X** [array-like or CSR/CSC sparse matrix, shape [n\_samples, n\_features]] The data to transform, row by row.

Prefer CSR over CSC for sparse input (for speed), but CSC is required if the degree is 4 or higher. If the degree is less than 4 and the input format is CSC, it will be converted to CSR, have its polynomial features generated, then converted back to CSC.

If the degree is 2 or 3, the method described in "Leveraging Sparsity to Speed Up Polynomial Feature Expansions of CSR Matrices Using K-Simplex Numbers" by Andrew Nystrom and John Hughes is used, which is much faster than the method used on CSC input. For this reason, a CSC input will be converted to CSR, and the output will be converted back to CSC prior to being returned, hence the preference of CSR.

### **Returns**

**XP** [np.ndarray or CSR/CSC sparse matrix, shape [n\_samples, NP]] The matrix of features, where NP is the number of polynomial features generated from the combination of inputs.

## Examples using sklearn.preprocessing.PolynomialFeatures

- Polynomial interpolation
- Robust linear estimator fitting
- Underfitting vs. Overfitting

## 6.34.14 sklearn.preprocessing.PowerTransformer

Apply a power transform featurewise to make data more Gaussian-like.

Power transforms are a family of parametric, monotonic transformations that are applied to make data more Gaussian-like. This is useful for modeling issues related to heteroscedasticity (non-constant variance), or other situations where normality is desired.

Currently, PowerTransformer supports the Box-Cox transform and the Yeo-Johnson transform. The optimal parameter for stabilizing variance and minimizing skewness is estimated through maximum likelihood.

Box-Cox requires input data to be strictly positive, while Yeo-Johnson supports both positive or negative data.

By default, zero-mean, unit-variance normalization is applied to the transformed data.

Read more in the *User Guide*.

## **Parameters**

method [str, (default='yeo-johnson')] The power transform method. Available methods are:

- 'yeo-johnson' [Rf3e1504535de-1], works with positive and negative values
- 'box-cox' [Rf3e1504535de-2], only works with strictly positive values

**standardize** [boolean, default=True] Set to True to apply zero-mean, unit-variance normalization to the transformed output.

**copy** [boolean, optional, default=True] Set to False to perform inplace computation during transformation.

#### **Attributes**

**lambdas**\_ [array of float, shape (n\_features,)] The parameters of the power transformation for the selected features.

See also:

**power\_transform** Equivalent function without the estimator API.

QuantileTransformer Maps data to a standard normal distribution with the parameter output\_distribution='normal'.

#### **Notes**

NaNs are treated as missing values: disregarded in fit, and maintained in transform.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

### References

[Rf3e1504535de-1], [Rf3e1504535de-2]

## **Examples**

```
>>> import numpy as np
>>> from sklearn.preprocessing import PowerTransformer
>>> pt = PowerTransformer()
>>> data = [[1, 2], [3, 2], [4, 5]]
>>> print(pt.fit(data))
PowerTransformer(copy=True, method='yeo-johnson', standardize=True)
>>> print(pt.lambdas_)
[ 1.386... -3.100...]
>>> print(pt.transform(data))
[[-1.316... -0.707...]
[ 0.209... -0.707...]
[ 1.106... 1.414...]]
```

## **Methods**

fit(self, X[, y])	Estimate the optimal parameter lambda for each feature.
$fit_{transform(self, X[, y])}$	
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Apply the inverse power transformation using the fitted
	lambdas.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Apply the power transform to each feature using the fit-
	ted lambdas.

```
__init__ (self, method='yeo-johnson', standardize=True, copy=True)
```

**fit** (self, X, y=None)

Estimate the optimal parameter lambda for each feature.

The optimal lambda parameter for minimizing skewness is estimated on each feature independently using maximum likelihood.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The data used to estimate the optimal transformation parameters.

y [Ignored]

### **Returns**

self [object]

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## $inverse\_transform(self, X)$

Apply the inverse power transformation using the fitted lambdas.

The inverse of the Box-Cox transformation is given by:

```
if lambda == 0:
    X = exp(X_trans)
else:
    X = (X_trans * lambda + 1) ** (1 / lambda)
```

The inverse of the Yeo-Johnson transformation is given by:

```
if X >= 0 and lambda == 0:
    X = exp(X_trans) - 1
elif X >= 0 and lambda != 0:
    X = (X_trans * lambda + 1) ** (1 / lambda) - 1
elif X < 0 and lambda != 2:
    X = 1 - (-(2 - lambda) * X_trans + 1) ** (1 / (2 - lambda))
elif X < 0 and lambda == 2:
    X = 1 - exp(-X_trans)</pre>
```

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The transformed data.

## Returns

X [array-like, shape (n\_samples, n\_features)] The original data

```
set params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

## transform(self, X)

Apply the power transform to each feature using the fitted lambdas.

### **Parameters**

X [array-like, shape (n\_samples, n\_features)] The data to be transformed using a power transformation.

#### Returns

**X trans** [array-like, shape (n samples, n features)] The transformed data.

## Examples using sklearn.preprocessing.PowerTransformer

- Map data to a normal distribution
- Compare the effect of different scalers on data with outliers

## 6.34.15 sklearn.preprocessing.QuantileTransformer

```
class sklearn.preprocessing.QuantileTransformer (n\_quantiles=1000, output_distribution='uniform', ignore_implicit_zeros=False, subsample=100000, random_state=None, copy=True)
```

Transform features using quantiles information.

This method transforms the features to follow a uniform or a normal distribution. Therefore, for a given feature, this transformation tends to spread out the most frequent values. It also reduces the impact of (marginal) outliers: this is therefore a robust preprocessing scheme.

The transformation is applied on each feature independently. First an estimate of the cumulative distribution function of a feature is used to map the original values to a uniform distribution. The obtained values are then mapped to the desired output distribution using the associated quantile function. Features values of new/unseen data that fall below or above the fitted range will be mapped to the bounds of the output distribution. Note that this transform is non-linear. It may distort linear correlations between variables measured at the same scale but renders variables measured at different scales more directly comparable.

Read more in the *User Guide*.

### **Parameters**

- n\_quantiles [int, optional (default=1000 or n\_samples)] Number of quantiles to be computed. It corresponds to the number of landmarks used to discretize the cumulative distribution function. If n\_quantiles is larger than the number of samples, n\_quantiles is set to the number of samples as a larger number of quantiles does not give a better approximation of the cumulative distribution function estimator.
- **output\_distribution** [str, optional (default='uniform')] Marginal distribution for the transformed data. The choices are 'uniform' (default) or 'normal'.
- **ignore\_implicit\_zeros** [bool, optional (default=False)] Only applies to sparse matrices. If True, the sparse entries of the matrix are discarded to compute the quantile statistics. If False, these entries are treated as zeros.
- **subsample** [int, optional (default=1e5)] Maximum number of samples used to estimate the quantiles for computational efficiency. Note that the subsampling procedure may differ for value-identical sparse and dense matrices.
- **random\_state** [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is

the RandomState instance used by np.random. Note that this is used by subsampling and smoothing noise.

**copy** [boolean, optional, (default=True)] Set to False to perform inplace transformation and avoid a copy (if the input is already a numpy array).

## **Attributes**

n\_quantiles\_ [integer] The actual number of quantiles used to discretize the cumulative distribution function.

**quantiles**\_ [ndarray, shape (n\_quantiles, n\_features)] The values corresponding the quantiles of reference.

references\_ [ndarray, shape(n\_quantiles, )] Quantiles of references.

### See also:

quantile\_transform Equivalent function without the estimator API.

**PowerTransformer** Perform mapping to a normal distribution using a power transform.

StandardScaler Perform standardization that is faster, but less robust to outliers.

**RobustScaler** Perform robust standardization that removes the influence of outliers but does not put outliers and inliers on the same scale.

### **Notes**

NaNs are treated as missing values: disregarded in fit, and maintained in transform.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## **Examples**

```
>>> import numpy as np
>>> from sklearn.preprocessing import QuantileTransformer
>>> rng = np.random.RandomState(0)
>>> X = np.sort(rng.normal(loc=0.5, scale=0.25, size=(25, 1)), axis=0)
>>> qt = QuantileTransformer(n_quantiles=10, random_state=0)
>>> qt.fit_transform(X)
array([...])
```

## **Methods**

fit(self, X[, y])	Compute the quantiles used for transforming.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Back-projection to the original space.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Feature-wise transformation of the data.

\_\_init\_\_ (self, n\_quantiles=1000, output\_distribution='uniform', ignore\_implicit\_zeros=False, sub-sample=100000, random\_state=None, copy=True)

### **fit** (self, X, y=None)

Compute the quantiles used for transforming.

#### **Parameters**

X [ndarray or sparse matrix, shape (n\_samples, n\_features)] The data used to scale along the features axis. If a sparse matrix is provided, it will be converted into a sparse csc\_matrix. Additionally, the sparse matrix needs to be nonnegative if ignore\_implicit\_zeros is False.

## Returns

self [object]

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- X [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## $inverse\_transform(self, X)$

Back-projection to the original space.

## **Parameters**

X [ndarray or sparse matrix, shape (n\_samples, n\_features)] The data used to scale along the features axis. If a sparse matrix is provided, it will be converted into a sparse csc\_matrix. Additionally, the sparse matrix needs to be nonnegative if ignore implicit zeros is False.

## Returns

**Xt** [ndarray or sparse matrix, shape (n\_samples, n\_features)] The projected data.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

#### self

## transform(self, X)

Feature-wise transformation of the data.

#### **Parameters**

X [ndarray or sparse matrix, shape (n\_samples, n\_features)] The data used to scale along the features axis. If a sparse matrix is provided, it will be converted into a sparse csc\_matrix. Additionally, the sparse matrix needs to be nonnegative if ignore\_implicit\_zeros is False.

### **Returns**

**Xt** [ndarray or sparse matrix, shape (n\_samples, n\_features)] The projected data.

## Examples using sklearn.preprocessing.QuantileTransformer

- Effect of transforming the targets in regression model
- Map data to a normal distribution
- · Compare the effect of different scalers on data with outliers

## 6.34.16 sklearn.preprocessing.RobustScaler

class sklearn.preprocessing.RobustScaler (with\_centering=True, with\_scaling=True, quantile\_range=(25.0, 75.0), copy=True)

Scale features using statistics that are robust to outliers.

This Scaler removes the median and scales the data according to the quantile range (defaults to IQR: Interquartile Range). The IQR is the range between the 1st quartile (25th quantile) and the 3rd quartile (75th quantile).

Centering and scaling happen independently on each feature by computing the relevant statistics on the samples in the training set. Median and interquartile range are then stored to be used on later data using the transform method.

Standardization of a dataset is a common requirement for many machine learning estimators. Typically this is done by removing the mean and scaling to unit variance. However, outliers can often influence the sample mean / variance in a negative way. In such cases, the median and the interquartile range often give better results.

New in version 0.17.

Read more in the *User Guide*.

## **Parameters**

with\_centering [boolean, True by default] If True, center the data before scaling. This will cause transform to raise an exception when attempted on sparse matrices, because centering them entails building a dense matrix which in common use cases is likely to be too large to fit in memory.

with\_scaling [boolean, True by default] If True, scale the data to interquartile range.

**quantile\_range** [tuple (q\_min, q\_max),  $0.0 < q_min < q_max < 100.0$ ] Default: (25.0, 75.0) = (1st quantile, 3rd quantile) = IQR Quantile range used to calculate scale.

New in version 0.18.

**copy** [boolean, optional, default is True] If False, try to avoid a copy and do inplace scaling instead. This is not guaranteed to always work inplace; e.g. if the data is not a NumPy array or scipy.sparse CSR matrix, a copy may still be returned.

### **Attributes**

center\_ [array of floats] The median value for each feature in the training set.

scale\_ [array of floats] The (scaled) interquartile range for each feature in the training set.

New in version 0.17: *scale\_* attribute.

#### See also:

robust\_scale Equivalent function without the estimator API.

**sklearn.decomposition.PCA** Further removes the linear correlation across features with 'whiten=True'.

### **Notes**

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

https://en.wikipedia.org/wiki/Median https://en.wikipedia.org/wiki/Interquartile\_range

## **Examples**

### **Methods**

fit(self, X[, y])	Compute the median and quantiles to be used for scal-
	ing.
<pre>fit_transform(self, X[, y])</pre>	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
inverse_transform(self, X)	Scale back the data to the original representation
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Center and scale the data.

```
__init__ (self, with_centering=True, with_scaling=True, quantile_range=(25.0, 75.0), copy=True)
```

## **fit** (self, X, y=None)

Compute the median and quantiles to be used for scaling.

## **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] The data used to compute the median and quantiles used for later scaling along the features axis.

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- y [numpy array of shape [n\_samples]] Target values.

### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### **Returns**

params [mapping of string to any] Parameter names mapped to their values.

## inverse transform(self, X)

Scale back the data to the original representation

#### **Parameters**

**X** [array-like] The data used to scale along the specified axis.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## ${\tt transform}\,(\mathit{self},X)$

Center and scale the data.

## **Parameters**

**X** [{array-like, sparse matrix}] The data used to scale along the specified axis.

## Examples using sklearn.preprocessing.RobustScaler

• Compare the effect of different scalers on data with outliers

## 6.34.17 sklearn.preprocessing.StandardScaler

class sklearn.preprocessing.StandardScaler(copy=True, with\_mean=True, with\_std=True)
 Standardize features by removing the mean and scaling to unit variance

The standard score of a sample *x* is calculated as:

$$z = (x - u) / s$$

where u is the mean of the training samples or zero if with\_mean=False, and s is the standard deviation of the training samples or one if with\_std=False.

Centering and scaling happen independently on each feature by computing the relevant statistics on the samples in the training set. Mean and standard deviation are then stored to be used on later data using the transform method.

Standardization of a dataset is a common requirement for many machine learning estimators: they might behave badly if the individual features do not more or less look like standard normally distributed data (e.g. Gaussian with 0 mean and unit variance).

For instance many elements used in the objective function of a learning algorithm (such as the RBF kernel of Support Vector Machines or the L1 and L2 regularizers of linear models) assume that all features are centered around 0 and have variance in the same order. If a feature has a variance that is orders of magnitude larger that others, it might dominate the objective function and make the estimator unable to learn from other features correctly as expected.

This scaler can also be applied to sparse CSR or CSC matrices by passing with\_mean=False to avoid breaking the sparsity structure of the data.

Read more in the *User Guide*.

#### **Parameters**

- **copy** [boolean, optional, default True] If False, try to avoid a copy and do inplace scaling instead. This is not guaranteed to always work inplace; e.g. if the data is not a NumPy array or scipy.sparse CSR matrix, a copy may still be returned.
- with\_mean [boolean, True by default] If True, center the data before scaling. This does not work (and will raise an exception) when attempted on sparse matrices, because centering them entails building a dense matrix which in common use cases is likely to be too large to fit in memory.
- with\_std [boolean, True by default] If True, scale the data to unit variance (or equivalently, unit standard deviation).

## Attributes

**scale\_** [ndarray or None, shape (n\_features,)] Per feature relative scaling of the data. This is calculated using np.sqrt (var\_). Equal to None when with\_std=False.

New in version 0.17: scale

- mean\_ [ndarray or None, shape (n\_features,)] The mean value for each feature in the training set. Equal to None when with mean=False.
- var\_ [ndarray or None, shape (n\_features,)] The variance for each feature in the training set.
  Used to compute scale\_. Equal to None when with\_std=False.
- **n\_samples\_seen\_** [int or array, shape (n\_features,)] The number of samples processed by the estimator for each feature. If there are not missing samples, the n\_samples\_seen will be an integer, otherwise it will be an array. Will be reset on new calls to fit, but increments across partial\_fit calls.

## See also:

scale Equivalent function without the estimator API.

**sklearn.decomposition.PCA** Further removes the linear correlation across features with 'whiten=True'.

### **Notes**

NaNs are treated as missing values: disregarded in fit, and maintained in transform.

We use a biased estimator for the standard deviation, equivalent to numpy.std(x, ddof=0). Note that the choice of ddof is unlikely to affect model performance.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## **Examples**

```
>>> from sklearn.preprocessing import StandardScaler
>>> data = [[0, 0], [0, 0], [1, 1], [1, 1]]
>>> scaler = StandardScaler()
>>> print(scaler.fit(data))
StandardScaler(copy=True, with_mean=True, with_std=True)
>>> print(scaler.mean_)
[0.5 0.5]
>>> print(scaler.transform(data))
[[-1. -1.]
[-1. -1.]
[ 1.  1.]
[ 1.  1.]]
>>> print(scaler.transform([[2, 2]]))
[[3.  3.]]
```

### **Methods**

fit(self, X[, y])	Compute the mean and std to be used for later scaling.
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>inverse_transform(self, X[, copy])</pre>	Scale back the data to the original representation
<pre>partial_fit(self, X[, y])</pre>	Online computation of mean and std on X for later scal-
	ing.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X[, copy])	Perform standardization by centering and scaling

```
__init__ (self, copy=True, with_mean=True, with_std=True)
```

fit (self, X, y=None)

Compute the mean and std to be used for later scaling.

## **Parameters**

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] The data used to compute the mean and standard deviation used for later scaling along the features axis.

y Ignored

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

#### **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- **y** [numpy array of shape [n\_samples]] Target values.

### **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

## inverse\_transform(self, X, copy=None)

Scale back the data to the original representation

#### **Parameters**

 ${f X}$  [array-like, shape [n\_samples, n\_features]] The data used to scale along the features axis.

**copy** [bool, optional (default: None)] Copy the input X or not.

## Returns

**X\_tr** [array-like, shape [n\_samples, n\_features]] Transformed array.

## partial\_fit (self, X, y=None)

Online computation of mean and std on X for later scaling. All of X is processed as a single batch. This is intended for cases when fit is not feasible due to very large number of  $n\_samples$  or because X is read from a continuous stream.

The algorithm for incremental mean and std is given in Equation 1.5a,b in Chan, Tony F., Gene H. Golub, and Randall J. LeVeque. "Algorithms for computing the sample variance: Analysis and recommendations." The American Statistician 37.3 (1983): 242-247:

#### **Parameters**

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] The data used to compute the mean and standard deviation used for later scaling along the features axis.

y Ignored

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## transform (self, X, copy=None)

Perform standardization by centering and scaling

#### **Parameters**

**X** [array-like, shape [n\_samples, n\_features]] The data used to scale along the features axis. **copy** [bool, optional (default: None)] Copy the input X or not.

## Examples using sklearn.preprocessing.StandardScaler

- Prediction Latency
- Classifier comparison
- Demo of DBSCAN clustering algorithm
- Comparing different hierarchical linkage methods on toy datasets
- Comparing different clustering algorithms on toy datasets
- Column Transformer with Mixed Types
- MNIST classfification using multinomial logistic + L1
- L1 Penalty and Sparsity in Logistic Regression
- Comparing Nearest Neighbors with and without Neighborhood Components Analysis
- Dimensionality Reduction with Neighborhood Components Analysis
- Varying regularization in Multi-layer Perceptron
- Importance of Feature Scaling
- Feature discretization
- Compare the effect of different scalers on data with outliers
- SVM-Anova: SVM with univariate feature selection
- RBF SVM parameters

proprogogaina add dummy foaturo(V[ volue])	Augment dataset with an additional dummy feature.
$preprocessing.add\_dummy\_feature(X[, value])$	•
<pre>preprocessing.binarize(X[, threshold, copy])</pre>	Boolean thresholding of array-like or scipy.sparse matrix
<pre>preprocessing.label_binarize(y, classes[,])</pre>	Binarize labels in a one-vs-all fashion
<pre>preprocessing.maxabs_scale(X[, axis, copy])</pre>	Scale each feature to the [-1, 1] range without breaking the
	sparsity.
preprocessing.minmax_scale( $X[,\dots]$ )	Transforms features by scaling each feature to a given
	range.
preprocessing.normalize(X[, norm, axis,])	Scale input vectors individually to unit norm (vector
	length).
$preprocessing.quantile\_transform(X[, axis,$	Transform features using quantiles information.
])	
$preprocessing.robust\_scale(X[,axis,])$	Standardize a dataset along any axis
$preprocessing.scale(X[, axis, with\_mean,])$	Standardize a dataset along any axis
preprocessing.power_transform(X[, method,	Power transforms are a family of parametric, mono-
])	tonic transformations that are applied to make data more
	Gaussian-like.

## 6.34.18 sklearn.preprocessing.add dummy feature

```
sklearn.preprocessing.add_dummy_feature(X, value=1.0)
```

Augment dataset with an additional dummy feature.

This is useful for fitting an intercept term with implementations which cannot otherwise fit it directly.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] Data.

value [float] Value to use for the dummy feature.

## Returns

X [{array, sparse matrix}, shape [n\_samples, n\_features + 1]] Same data with dummy feature added as first column.

## **Examples**

## 6.34.19 sklearn.preprocessing.binarize

sklearn.preprocessing.binarize(X, threshold=0.0, copy=True)

Boolean thresholding of array-like or scipy.sparse matrix

Read more in the User Guide.

## **Parameters**

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] The data to binarize, element by element. scipy.sparse matrices should be in CSR or CSC format to avoid an un-necessary copy.

**threshold** [float, optional (0.0 by default)] Feature values below or equal to this are replaced by 0, above it by 1. Threshold may not be less than 0 for operations on sparse matrices.

**copy** [boolean, optional, default True] set to False to perform inplace binarization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR / CSC matrix and if axis is 1).

### See also:

**Binarizer** Performs binarization using the Transformer API (e.g. as part of a preprocessing sklearn. pipeline.Pipeline).

## 6.34.20 sklearn.preprocessing.label\_binarize

```
sklearn.preprocessing. \textbf{label\_binarize} (y, classes, neg\_label=0, pos\_label=1, sparse\_output=False)
```

Binarize labels in a one-vs-all fashion

Several regression and binary classification algorithms are available in scikit-learn. A simple way to extend these algorithms to the multi-class classification case is to use the so-called one-vs-all scheme.

This function makes it possible to compute this transformation for a fixed set of class labels known ahead of time.

## **Parameters**

```
y [array-like] Sequence of integer labels or multilabel data to encode.
```

classes [array-like of shape [n\_classes]] Uniquely holds the label for each class.

**neg\_label** [int (default: 0)] Value with which negative labels must be encoded.

**pos\_label** [int (default: 1)] Value with which positive labels must be encoded.

**sparse\_output** [boolean (default: False),] Set to true if output binary array is desired in CSR sparse format

### Returns

Y [numpy array or CSR matrix of shape [n\_samples, n\_classes]] Shape will be [n\_samples, 1] for binary problems.

#### See also:

**LabelBinarizer** class used to wrap the functionality of label\_binarize and allow for fitting to classes independently of the transform operation

## **Examples**

The class ordering is preserved:

Binary targets transform to a column vector

## Examples using sklearn.preprocessing.label\_binarize

- Receiver Operating Characteristic (ROC)
- Precision-Recall

## 6.34.21 sklearn.preprocessing.maxabs scale

```
sklearn.preprocessing.maxabs_scale(X, axis=0, copy=True)
```

Scale each feature to the [-1, 1] range without breaking the sparsity.

This estimator scales each feature individually such that the maximal absolute value of each feature in the training set will be 1.0.

This scaler can also be applied to sparse CSR or CSC matrices.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The data.

**axis** [int (0 by default)] axis used to scale along. If 0, independently scale each feature, otherwise (if 1) scale each sample.

**copy** [boolean, optional, default is True] Set to False to perform inplace scaling and avoid a copy (if the input is already a numpy array).

## See also:

**MaxAbsScaler** Performs scaling to the [-1, 1] range using the "Transformer" API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

#### **Notes**

NaNs are treated as missing values: disregarded to compute the statistics, and maintained during the data transformation.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## 6.34.22 sklearn.preprocessing.minmax\_scale

```
sklearn.preprocessing.minmax_scale (X, feature\_range=(0, 1), axis=0, copy=True)

Transforms features by scaling each feature to a given range.
```

This estimator scales and translates each feature individually such that it is in the given range on the training set, i.e. between zero and one.

The transformation is given by (when axis=0):

```
X_std = (X - X.min(axis=0)) / (X.max(axis=0) - X.min(axis=0))
X_scaled = X_std * (max - min) + min
```

where min,  $max = feature\_range$ .

The transformation is calculated as (when axis=0):

```
X_scaled = scale * X + min - X.min(axis=0) * scale
where scale = (max - min) / (X.max(axis=0) - X.min(axis=0))
```

This transformation is often used as an alternative to zero mean, unit variance scaling.

Read more in the User Guide.

New in version 0.17: minmax\_scale function interface to sklearn.preprocessing.MinMaxScaler.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] The data.

**feature range** [tuple (min, max), default=(0, 1)] Desired range of transformed data.

**axis** [int (0 by default)] axis used to scale along. If 0, independently scale each feature, otherwise (if 1) scale each sample.

**copy** [boolean, optional, default is True] Set to False to perform inplace scaling and avoid a copy (if the input is already a numpy array).

#### See also:

**MinMaxScaler** Performs scaling to a given range using the "Transformer" API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

## **Notes**

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## Examples using sklearn.preprocessing.minmax\_scale

• Compare the effect of different scalers on data with outliers

## 6.34.23 sklearn.preprocessing.normalize

sklearn.preprocessing.normalize (*X*, norm='l2', axis=1, copy=True, return\_norm=False)
Scale input vectors individually to unit norm (vector length).

Read more in the *User Guide*.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] The data to normalize, element by element. scipy.sparse matrices should be in CSR format to avoid an un-necessary copy.

**norm** ['11', '12', or 'max', optional ('12' by default)] The norm to use to normalize each non zero sample (or each non-zero feature if axis is 0).

**axis** [0 or 1, optional (1 by default)] axis used to normalize the data along. If 1, independently normalize each sample, otherwise (if 0) normalize each feature.

**copy** [boolean, optional, default True] set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR matrix and if axis is 1).

return\_norm [boolean, default False] whether to return the computed norms

## Returns

**X** [{array-like, sparse matrix}, shape [n\_samples, n\_features]] Normalized input X.

**norms** [array, shape [n\_samples] if axis=1 else [n\_features]] An array of norms along given axis for X. When X is sparse, a NotImplementedError will be raised for norm '11' or '12'.

## See also:

**Normalizer** Performs normalization using the Transformer API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

### **Notes**

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## 6.34.24 sklearn.preprocessing.quantile\_transform

```
sklearn.preprocessing.quantile_transform(X, axis=0, n\_quantiles=1000, output_distribution='uniform', ignore_implicit_zeros=False, subsample=100000, random_state=None, copy='warn')
```

Transform features using quantiles information.

This method transforms the features to follow a uniform or a normal distribution. Therefore, for a given feature, this transformation tends to spread out the most frequent values. It also reduces the impact of (marginal) outliers: this is therefore a robust preprocessing scheme.

The transformation is applied on each feature independently. First an estimate of the cumulative distribution function of a feature is used to map the original values to a uniform distribution. The obtained values are then mapped to the desired output distribution using the associated quantile function. Features values of new/unseen data that fall below or above the fitted range will be mapped to the bounds of the output distribution. Note that this transform is non-linear. It may distort linear correlations between variables measured at the same scale but renders variables measured at different scales more directly comparable.

Read more in the *User Guide*.

#### **Parameters**

- **X** [array-like, sparse matrix] The data to transform.
- **axis** [int, (default=0)] Axis used to compute the means and standard deviations along. If 0, transform each feature, otherwise (if 1) transform each sample.
- n\_quantiles [int, optional (default=1000 or n\_samples)] Number of quantiles to be computed. It corresponds to the number of landmarks used to discretize the cumulative distribution function. If n\_quantiles is larger than the number of samples, n\_quantiles is set to the number of samples as a larger number of quantiles does not give a better approximation of the cumulative distribution function estimator.
- **output\_distribution** [str, optional (default='uniform')] Marginal distribution for the transformed data. The choices are 'uniform' (default) or 'normal'.
- **ignore\_implicit\_zeros** [bool, optional (default=False)] Only applies to sparse matrices. If True, the sparse entries of the matrix are discarded to compute the quantile statistics. If False, these entries are treated as zeros.
- **subsample** [int, optional (default=1e5)] Maximum number of samples used to estimate the quantiles for computational efficiency. Note that the subsampling procedure may differ for value-identical sparse and dense matrices.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Note that this is used by subsampling and smoothing noise.
- **copy** [boolean, optional, (default="warn")] Set to False to perform inplace transformation and avoid a copy (if the input is already a numpy array). If True, a copy of *X* is transformed, leaving the original *X* unchanged

Deprecated since version 0.21: The default value of parameter copy will be changed from False to True in 0.23. The current default of False is being changed to make it more consistent with the default copy values of other functions in sklearn.preprocessing.data. Furthermore, the current default of False may have unexpected side effects by modifying the value of X implace

### Returns

**Xt** [ndarray or sparse matrix, shape (n\_samples, n\_features)] The transformed data.

### See also:

QuantileTransformer Performs quantile-based scaling using the Transformer API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

**power\_transform** Maps data to a normal distribution using a power transformation.

**scale** Performs standardization that is faster, but less robust to outliers.

robust\_scale Performs robust standardization that removes the influence of outliers but does not put outliers and inliers on the same scale.

## **Notes**

NaNs are treated as missing values: disregarded in fit, and maintained in transform.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## **Examples**

```
>>> import numpy as np
>>> from sklearn.preprocessing import quantile_transform
>>> rng = np.random.RandomState(0)
>>> X = np.sort(rng.normal(loc=0.5, scale=0.25, size=(25, 1)), axis=0)
>>> quantile_transform(X, n_quantiles=10, random_state=0, copy=True)
...
array([...])
```

## Examples using sklearn.preprocessing.quantile\_transform

• Effect of transforming the targets in regression model

## 6.34.25 sklearn.preprocessing.robust\_scale

```
sklearn.preprocessing.robust_scale(X, axis=0, with\_centering=True, with\_scaling=True, quantile\_range=(25.0, 75.0), copy=True)
```

Standardize a dataset along any axis

Center to the median and component wise scale according to the interquartile range.

Read more in the User Guide.

## **Parameters**

**X** [array-like] The data to center and scale.

**axis** [int (0 by default)] axis used to compute the medians and IQR along. If 0, independently scale each feature, otherwise (if 1) scale each sample.

with centering [boolean, True by default] If True, center the data before scaling.

with\_scaling [boolean, True by default] If True, scale the data to unit variance (or equivalently, unit standard deviation).

**quantile\_range** [tuple (q\_min, q\_max),  $0.0 < q_min < q_max < 100.0$ ] Default: (25.0, 75.0) = (1st quantile, 3rd quantile) = IQR Quantile range used to calculate scale\_.

New in version 0.18.

**copy** [boolean, optional, default is True] set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR matrix and if axis is 1).

#### See also:

**RobustScaler** Performs centering and scaling using the Transformer API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

### **Notes**

This implementation will refuse to center scipy.sparse matrices since it would make them non-sparse and would potentially crash the program with memory exhaustion problems.

Instead the caller is expected to either set explicitly with\_centering=False (in that case, only variance scaling will be performed on the features of the CSR matrix) or to call X.toarray() if he/she expects the materialized dense array to fit in memory.

To avoid memory copy the caller should pass a CSR matrix.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## 6.34.26 sklearn.preprocessing.scale

sklearn.preprocessing.scale (*X*, axis=0, with\_mean=True, with\_std=True, copy=True)
Standardize a dataset along any axis

Center to the mean and component wise scale to unit variance.

Read more in the User Guide.

#### **Parameters**

**X** [{array-like, sparse matrix}] The data to center and scale.

**axis** [int (0 by default)] axis used to compute the means and standard deviations along. If 0, independently standardize each feature, otherwise (if 1) standardize each sample.

with\_mean [boolean, True by default] If True, center the data before scaling.

with\_std [boolean, True by default] If True, scale the data to unit variance (or equivalently, unit standard deviation).

**copy** [boolean, optional, default True] set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSC matrix and if axis is 1).

### See also:

**StandardScaler** Performs scaling to unit variance using the "Transformer" API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

## **Notes**

This implementation will refuse to center scipy.sparse matrices since it would make them non-sparse and would potentially crash the program with memory exhaustion problems.

Instead the caller is expected to either set explicitly with\_mean=False (in that case, only variance scaling will be performed on the features of the CSC matrix) or to call X.toarray() if he/she expects the materialized dense array to fit in memory.

To avoid memory copy the caller should pass a CSC matrix.

NaNs are treated as missing values: disregarded to compute the statistics, and maintained during the data transformation.

We use a biased estimator for the standard deviation, equivalent to numpy.std(x, ddof=0). Note that the choice of ddof is unlikely to affect model performance.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## Examples using sklearn.preprocessing.scale

• A demo of K-Means clustering on the handwritten digits data

## 6.34.27 sklearn.preprocessing.power transform

sklearn.preprocessing.power\_transform(X, method='warn', standardize=True, copy=True)

Power transforms are a family of parametric, monotonic transformations that are applied to make data more Gaussian-like. This is useful for modeling issues related to heteroscedasticity (non-constant variance), or other situations where normality is desired.

Currently, power\_transform supports the Box-Cox transform and the Yeo-Johnson transform. The optimal parameter for stabilizing variance and minimizing skewness is estimated through maximum likelihood.

Box-Cox requires input data to be strictly positive, while Yeo-Johnson supports both positive or negative data.

By default, zero-mean, unit-variance normalization is applied to the transformed data.

Read more in the *User Guide*.

## Parameters

**X** [array-like, shape (n\_samples, n\_features)] The data to be transformed using a power transformation.

**method** [str] The power transform method. Available methods are:

- 'yeo-johnson' [1], works with positive and negative values
- 'box-cox' [2], only works with strictly positive values

The default method will be changed from 'box-cox' to 'yeo-johnson' in version 0.23. To suppress the FutureWarning, explicitly set the parameter.

**standardize** [boolean, default=True] Set to True to apply zero-mean, unit-variance normalization to the transformed output.

**copy** [boolean, optional, default=True] Set to False to perform inplace computation during transformation.

## Returns

**X\_trans** [array-like, shape (n\_samples, n\_features)] The transformed data.

#### See also:

**PowerTransformer** Equivalent transformation with the Transformer API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

quantile\_transform Maps data to a standard normal distribution with the parameter output\_distribution='normal'.

#### **Notes**

NaNs are treated as missing values: disregarded in fit, and maintained in transform.

For a comparison of the different scalers, transformers, and normalizers, see *exam-ples/preprocessing/plot\_all\_scaling.py*.

## References

[1], [2]

## **Examples**

```
>>> import numpy as np
>>> from sklearn.preprocessing import power_transform
>>> data = [[1, 2], [3, 2], [4, 5]]
>>> print(power_transform(data, method='box-cox'))
[[-1.332... -0.707...]
[ 0.256... -0.707...]
[ 1.076... 1.414...]]
```

# 6.35 sklearn.random\_projection: Random projection

## Random Projection transformers

Random Projections are a simple and computationally efficient way to reduce the dimensionality of the data by trading a controlled amount of accuracy (as additional variance) for faster processing times and smaller model sizes.

The dimensions and distribution of Random Projections matrices are controlled so as to preserve the pairwise distances between any two samples of the dataset.

The main theoretical result behind the efficiency of random projection is the Johnson-Lindenstrauss lemma (quoting Wikipedia):

In mathematics, the Johnson-Lindenstrauss lemma is a result concerning low-distortion embeddings of points from high-dimensional into low-dimensional Euclidean space. The lemma states that a small set of points in a high-dimensional space can be embedded into a space of much lower dimension in such a way that distances between the points are nearly preserved. The map used for the embedding is at least Lipschitz, and can even be taken to be an orthogonal projection.

**User guide:** See the *Random Projection* section for further details.

random_projection.	Reduce dimensionality through Gaussian random projec-
$ extit{GaussianRandomProjection}([\dots])$	tion
random_projection.	Reduce dimensionality through sparse random projection
$ extit{SparseRandomProjection}([\dots])$	

# 6.35.1 sklearn.random\_projection.GaussianRandomProjection

Reduce dimensionality through Gaussian random projection

The components of the random matrix are drawn from  $N(0, 1 / n\_components)$ .

Read more in the User Guide.

## **Parameters**

**n\_components** [int or 'auto', optional (default = 'auto')] Dimensionality of the target projection space.

n\_components can be automatically adjusted according to the number of samples in the dataset and the bound given by the Johnson-Lindenstrauss lemma. In that case the quality of the embedding is controlled by the eps parameter.

It should be noted that Johnson-Lindenstrauss lemma can yield very conservative estimated of the required number of components as it makes no assumption on the structure of the dataset.

**eps** [strictly positive float, optional (default=0.1)] Parameter to control the quality of the embedding according to the Johnson-Lindenstrauss lemma when n\_components is set to 'auto'.

Smaller values lead to better embedding and higher number of dimensions (n\_components) in the target projection space.

random\_state [int, RandomState instance or None, optional (default=None)] Control the pseudo random number generator used to generate the matrix at fit time. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

## **Attributes**

**n component** [int] Concrete number of components computed when n components="auto".

**components**\_ [numpy array of shape [n\_components, n\_features]] Random matrix used for the projection.

## See also:

SparseRandomProjection

## **Examples**

```
>>> import numpy as np
>>> from sklearn.random_projection import GaussianRandomProjection
>>> rng = np.random.RandomState(42)
>>> X = rng.rand(100, 10000)
>>> transformer = GaussianRandomProjection(random_state=rng)
>>> X_new = transformer.fit_transform(X)
>>> X_new.shape
(100, 3947)
```

## **Methods**

fit(self, X[, y])	Generate a sparse random projection matrix
$fit\_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Project the data by using matrix product with the ran-
	dom matrix

```
__init__ (self, n_components='auto', eps=0.1, random_state=None)
```

## **fit** (*self*, *X*, *y=None*)

Generate a sparse random projection matrix

## **Parameters**

**X** [numpy array or scipy.sparse of shape [n\_samples, n\_features]] Training set: only the shape is used to find optimal random matrix dimensions based on the theory referenced in the afore mentioned papers.

y Ignored

## Returns

self

```
fit_transform(self, X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

## **Parameters**

- **X** [numpy array of shape [n\_samples, n\_features]] Training set.
- $\boldsymbol{y}$  [numpy array of shape [n\_samples]] Target values.

## Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## **Returns**

self

## transform(self, X)

Project the data by using matrix product with the random matrix

## **Parameters**

**X** [numpy array or scipy.sparse of shape [n\_samples, n\_features]] The input data to project into a smaller dimensional space.

#### Returns

**X\_new** [numpy array or scipy sparse of shape [n\_samples, n\_components]] Projected array.

## 6.35.2 sklearn.random\_projection.SparseRandomProjection

Reduce dimensionality through sparse random projection

Sparse random matrix is an alternative to dense random projection matrix that guarantees similar embedding quality while being much more memory efficient and allowing faster computation of the projected data.

If we note s = 1 / density the components of the random matrix are drawn from:

- -sqrt(s) / sqrt(n\_components) with probability 1 / 2s
- 0 with probability 1 1 / s
- +sqrt(s) / sqrt(n\_components) with probability 1 / 2s

Read more in the *User Guide*.

#### **Parameters**

**n\_components** [int or 'auto', optional (default = 'auto')] Dimensionality of the target projection space.

n\_components can be automatically adjusted according to the number of samples in the dataset and the bound given by the Johnson-Lindenstrauss lemma. In that case the quality of the embedding is controlled by the eps parameter.

It should be noted that Johnson-Lindenstrauss lemma can yield very conservative estimated of the required number of components as it makes no assumption on the structure of the dataset.

**density** [float in range ]0, 1], optional (default='auto')] Ratio of non-zero component in the random projection matrix.

If density = 'auto', the value is set to the minimum density as recommended by Ping Li et al.: 1 / sqrt(n\_features).

Use density = 1/3.0 if you want to reproduce the results from Achlioptas, 2001.

**eps** [strictly positive float, optional, (default=0.1)] Parameter to control the quality of the embedding according to the Johnson-Lindenstrauss lemma when n\_components is set to 'auto'.

Smaller values lead to better embedding and higher number of dimensions (n\_components) in the target projection space.

**dense\_output** [boolean, optional (default=False)] If True, ensure that the output of the random projection is a dense numpy array even if the input and random projection matrix are both sparse. In practice, if the number of components is small the number of zero components in the projected data will be very small and it will be more CPU and memory efficient to use a dense representation.

If False, the projected data uses a sparse representation if the input is sparse.

random\_state [int, RandomState instance or None, optional (default=None)] Control the pseudo random number generator used to generate the matrix at fit time. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

## **Attributes**

**n\_component\_** [int] Concrete number of components computed when n\_components="auto".

**components**\_ [CSR matrix with shape [n\_components, n\_features]] Random matrix used for the projection.

**density** [float in range 0.0 - 1.0] Concrete density computed from when density = "auto".

## See also:

Gaussian Random Projection

## References

[R0fecf191e4b8-1], [R0fecf191e4b8-2]

## **Examples**

```
>>> import numpy as np
>>> from sklearn.random_projection import SparseRandomProjection
>>> rng = np.random.RandomState(42)
>>> X = rng.rand(100, 10000)
>>> transformer = SparseRandomProjection(random_state=rng)
>>> X_new = transformer.fit_transform(X)
>>> X_new.shape
(100, 3947)
>>> # very few components are non-zero
>>> np.mean(transformer.components_ != 0)
0.0100...
```

## **Methods**

fit(self, X[, y])	Generate a sparse random projection matrix
fit_transform(self, X[, y])	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
set_params(self, \*\*params)	Set the parameters of this estimator.
transform(self, X)	Project the data by using matrix product with the ran-
	dom matrix

## **fit** (self, X, y=None)

Generate a sparse random projection matrix

### **Parameters**

**X** [numpy array or scipy.sparse of shape [n\_samples, n\_features]] Training set: only the shape is used to find optimal random matrix dimensions based on the theory referenced in the afore mentioned papers.

y Ignored

## **Returns**

self

## fit\_transform(self, X, y=None, \*\*fit\_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

## **Parameters**

**X** [numpy array of shape [n samples, n features]] Training set.

**y** [numpy array of shape [n\_samples]] Target values.

## **Returns**

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

### transform(self, X)

Project the data by using matrix product with the random matrix

#### **Parameters**

**X** [numpy array or scipy.sparse of shape [n\_samples, n\_features]] The input data to project into a smaller dimensional space.

#### Returns

**X\_new** [numpy array or scipy sparse of shape [n\_samples, n\_components]] Projected array.

## **Examples using** sklearn.random\_projection.SparseRandomProjection

- The Johnson-Lindenstrauss bound for embedding with random projections
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

```
random_projection.
johnson lindenstrauss min dim(...)
```

Find a 'safe' number of components to randomly project to

# 6.35.3 sklearn.random\_projection.johnson\_lindenstrauss\_min\_dim

sklearn.random\_projection.johnson\_lindenstrauss\_min\_dim(n\_samples, eps=0.1) Find a 'safe' number of components to randomly project to

The distortion introduced by a random projection p only changes the distance between two points by a factor (1 +- eps) in an euclidean space with good probability. The projection p is an eps-embedding as defined by:

```
(1 - eps) \|u - v\|^2 < \|p(u) - p(v)\|^2 < (1 + eps) \|u - v\|^2
```

Where u and v are any rows taken from a dataset of shape  $[n\_samples, n\_features]$ , eps is in ]0, 1[ and p is a projection by a random Gaussian N(0, 1) matrix with shape  $[n\_components, n\_features]$  (or a sparse Achlioptas matrix).

The minimum number of components to guarantee the eps-embedding is given by:

```
n_{\text{components}} >= 4 \log(n_{\text{samples}}) / (eps^2 / 2 - eps^3 / 3)
```

Note that the number of dimensions is independent of the original number of features but instead depends on the size of the dataset: the larger the dataset, the higher is the minimal dimensionality of an eps-embedding.

Read more in the *User Guide*.

#### **Parameters**

- **n\_samples** [int or numpy array of int greater than 0,] Number of samples. If an array is given, it will compute a safe number of components array-wise.
- **eps** [float or numpy array of float in ]0,1[, optional (default=0.1)] Maximum distortion rate as defined by the Johnson-Lindenstrauss lemma. If an array is given, it will compute a safe number of components array-wise.

### Returns

**n\_components** [int or numpy array of int,] The minimal number of components to guarantee with good probability an eps-embedding with n\_samples.

## References

[1], [2]

## **Examples**

```
>>> johnson_lindenstrauss_min_dim(1e6, eps=0.5)
663
```

```
>>> johnson_lindenstrauss_min_dim(1e6, eps=[0.5, 0.1, 0.01])
array([ 663, 11841, 1112658])
```

```
>>> johnson_lindenstrauss_min_dim([1e4, 1e5, 1e6], eps=0.1)
array([ 7894, 9868, 11841])
```

## Examples using sklearn.random\_projection.johnson\_lindenstrauss\_min\_dim

• The Johnson-Lindenstrauss bound for embedding with random projections

# 6.36 sklearn.semi\_supervised Semi-Supervised Learning

The sklearn.semi\_supervised module implements semi-supervised learning algorithms. These algorithms utilized small amounts of labeled data and large amounts of unlabeled data for classification tasks. This module includes Label Propagation.

**User guide:** See the *Semi-Supervised* section for further details.

semi_supervised.LabelPropagation([kernel,	Label Propagation classifier
])	
semi_supervised.LabelSpreading([kernel,	LabelSpreading model for semi-supervised learning
])	

# 6.36.1 sklearn.semi\_supervised.LabelPropagation

Label Propagation classifier

Read more in the *User Guide*.

## **Parameters**

**kernel** [{'knn', 'rbf', callable}] String identifier for kernel function to use or the kernel function itself. Only 'rbf' and 'knn' strings are valid inputs. The function passed should take two inputs, each of shape [n\_samples, n\_features], and return a [n\_samples, n\_samples] shaped weight matrix.

gamma [float] Parameter for rbf kernel

**n\_neighbors** [integer > 0] Parameter for knn kernel

max\_iter [integer] Change maximum number of iterations allowed

tol [float] Convergence tolerance: threshold to consider the system at steady state

**n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

#### **Attributes**

```
X_{\text{le}} [array, shape = [n_samples, n_features]] Input array.
```

**classes** [array, shape =  $[n_{classes}]$ ] The distinct labels used in classifying instances.

**label\_distributions**\_ [array, shape = [n\_samples, n\_classes]] Categorical distribution for each item.

 $transduction_{}$  [array, shape = [n\_samples]] Label assigned to each item via the transduction.

**n\_iter\_** [int] Number of iterations run.

## See also:

LabelSpreading Alternate label propagation strategy more robust to noise

## References

Xiaojin Zhu and Zoubin Ghahramani. Learning from labeled and unlabeled data with label propagation. Technical Report CMU-CALD-02-107, Carnegie Mellon University, 2002 http://pages.cs.wisc.edu/~jerryzhu/pub/CMU-CALD-02-107.pdf

## **Examples**

```
>>> import numpy as np
>>> from sklearn import datasets
>>> from sklearn.semi_supervised import LabelPropagation
>>> label_prop_model = LabelPropagation()
>>> iris = datasets.load_iris()
>>> rng = np.random.RandomState(42)
>>> random_unlabeled_points = rng.rand(len(iris.target)) < 0.3
>>> labels = np.copy(iris.target)
>>> labels[random_unlabeled_points] = -1
>>> label_prop_model.fit(iris.data, labels)
...
LabelPropagation(...)
```

## **Methods**

fit(self, X, y)	
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Performs inductive inference across the model.
predict_proba(self, X)	Predict probability for each possible outcome.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
	Continued on next page

## Table 6.270 - continued from previous page

set params(self, \\*\\*params)

Set the parameters of this estimator.

```
__init__(self, kernel='rbf', gamma=20, n_neighbors=7, max_iter=1000, tol=0.001, n_jobs=None)
```

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Performs inductive inference across the model.

#### **Parameters**

**X** [array\_like, shape = [n\_samples, n\_features]]

#### Returns

y [array\_like, shape = [n\_samples]] Predictions for input data

## $predict_proba(self, X)$

Predict probability for each possible outcome.

Compute the probability estimates for each single sample in X and each possible outcome seen during training (categorical distribution).

## **Parameters**

```
X [array_like, shape = [n_samples, n_features]]
```

## Returns

**probabilities** [array, shape = [n\_samples, n\_classes]] Normalized probability distributions across class labels

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

## **Parameters**

 $\mathbf{X}$  [array-like, shape = (n\_samples, n\_features)] Test samples.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## 6.36.2 sklearn.semi\_supervised.LabelSpreading

```
class sklearn.semi_supervised.LabelSpreading(kernel='rbf', gamma=20, n\_neighbors=7, alpha=0.2, max\_iter=30, tol=0.001, n\_iobs=None)
```

LabelSpreading model for semi-supervised learning

This model is similar to the basic Label Propagation algorithm, but uses affinity matrix based on the normalized graph Laplacian and soft clamping across the labels.

Read more in the User Guide.

## **Parameters**

**kernel** [{'knn', 'rbf', callable}] String identifier for kernel function to use or the kernel function itself. Only 'rbf' and 'knn' strings are valid inputs. The function passed should take two inputs, each of shape [n\_samples, n\_features], and return a [n\_samples, n\_samples] shaped weight matrix

gamma [float] parameter for rbf kernel

**n\_neighbors** [integer > 0] parameter for knn kernel

**alpha** [float] Clamping factor. A value in (0, 1) that specifies the relative amount that an instance should adopt the information from its neighbors as opposed to its initial label. alpha=0 means keeping the initial label information; alpha=1 means replacing all initial information.

max\_iter [integer] maximum number of iterations allowed

tol [float] Convergence tolerance: threshold to consider the system at steady state

**n\_jobs** [int or None, optional (default=None)] The number of parallel jobs to run. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.

## Attributes

```
X_{\text{le}} [array, shape = [n_samples, n_features]] Input array.
```

**classes**\_ [array, shape = [n\_classes]] The distinct labels used in classifying instances.

**label\_distributions**\_ [array, shape = [n\_samples, n\_classes]] Categorical distribution for each item.

**transduction**\_ [array, shape = [n\_samples]] Label assigned to each item via the transduction.

**n iter** [int] Number of iterations run.

## See also:

LabelPropagation Unregularized graph based semi-supervised learning

## References

Dengyong Zhou, Olivier Bousquet, Thomas Navin Lal, Jason Weston, Bernhard Schoelkopf. Learning with local and global consistency (2004) http://citeseer.ist.psu.edu/viewdoc/summary?doi=10.1.1.115.3219

## **Examples**

```
>>> import numpy as np
>>> from sklearn import datasets
>>> from sklearn.semi_supervised import LabelSpreading
>>> label_prop_model = LabelSpreading()
>>> iris = datasets.load_iris()
>>> rng = np.random.RandomState(42)
>>> random_unlabeled_points = rng.rand(len(iris.target)) < 0.3
>>> labels = np.copy(iris.target)
>>> labels[random_unlabeled_points] = -1
>>> label_prop_model.fit(iris.data, labels)
...
LabelSpreading(...)
```

## **Methods**

fit(self, X, y)	Fit a semi-supervised label propagation model based
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Performs inductive inference across the model.
predict_proba(self, X)	Predict probability for each possible outcome.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, kernel='rbf', gamma=20, n_neighbors=7, alpha=0.2, max_iter=30, tol=0.001, n_jobs=None)
```

## fit (self, X, y)

Fit a semi-supervised label propagation model based

All the input data is provided matrix X (labeled and unlabeled) and corresponding label matrix y with a dedicated marker value for unlabeled samples.

## **Parameters**

- **X** [array-like, shape = [n\_samples, n\_features]] A {n\_samples by n\_samples} size matrix will be created from this
- y [array\_like, shape = [n\_samples]] n\_labeled\_samples (unlabeled points are marked as -1) All unlabeled samples will be transductively assigned labels

## Returns

self [returns an instance of self.]

# get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

### predict (self, X)

Performs inductive inference across the model.

#### **Parameters**

**X** [array\_like, shape = [n\_samples, n\_features]]

## Returns

y [array\_like, shape = [n\_samples]] Predictions for input data

## predict\_proba (self, X)

Predict probability for each possible outcome.

Compute the probability estimates for each single sample in X and each possible outcome seen during training (categorical distribution).

## **Parameters**

**X** [array\_like, shape = [n\_samples, n\_features]]

## Returns

**probabilities** [array, shape = [n\_samples, n\_classes]] Normalized probability distributions across class labels

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## **Returns**

self

## Examples using sklearn.semi\_supervised.LabelSpreading

- Decision boundary of label propagation versus SVM on the Iris dataset
- · Label Propagation learning a complex structure
- Label Propagation digits: Demonstrating performance
- Label Propagation digits active learning

# 6.37 sklearn.svm: Support Vector Machines

The sklearn.svm module includes Support Vector Machine algorithms.

**User guide:** See the *Support Vector Machines* section for further details.

## 6.37.1 Estimators

svm.LinearSVC([penalty, loss, dual, tol, C,])	Linear Support Vector Classification.
svm.LinearSVR([epsilon, tol, C, loss,])	Linear Support Vector Regression.
svm.NuSVC([nu, kernel, degree, gamma,])	Nu-Support Vector Classification.
svm. NuSVR([nu, C, kernel, degree, gamma,])	Nu Support Vector Regression.
svm.OneClassSVM([kernel, degree, gamma,])	Unsupervised Outlier Detection.
svm. SVC([C, kernel, degree, gamma, coef0,])	C-Support Vector Classification.
svm. SVR([kernel, degree, gamma, coef0, tol,])	Epsilon-Support Vector Regression.

## sklearn.svm.LinearSVC

Linear Support Vector Classification.

Similar to SVC with parameter kernel='linear', but implemented in terms of liblinear rather than libsym, so it has more flexibility in the choice of penalties and loss functions and should scale better to large numbers of samples.

This class supports both dense and sparse input and the multiclass support is handled according to a one-vs-therest scheme.

Read more in the User Guide.

## **Parameters**

**penalty** [string, '11' or '12' (default='12')] Specifies the norm used in the penalization. The '12' penalty is the standard used in SVC. The '11' leads to coef\_ vectors that are sparse.

**loss** [string, 'hinge' or 'squared\_hinge' (default='squared\_hinge')] Specifies the loss function. 'hinge' is the standard SVM loss (used e.g. by the SVC class) while 'squared\_hinge' is the square of the hinge loss.

**dual** [bool, (default=True)] Select the algorithm to either solve the dual or primal optimization problem. Prefer dual=False when n samples > n features.

tol [float, optional (default=1e-4)] Tolerance for stopping criteria.

C [float, optional (default=1.0)] Penalty parameter C of the error term.

multi\_class [string, 'ovr' or 'crammer\_singer' (default='ovr')] Determines the multi-class strategy if y contains more than two classes. "ovr" trains n\_classes one-vs-rest classifiers, while "crammer\_singer" optimizes a joint objective over all classes. While crammer\_singer is interesting from a theoretical perspective as it is consistent, it is seldom used in practice as it rarely leads to better accuracy and is more expensive to compute. If "crammer\_singer" is chosen, the options loss, penalty and dual will be ignored.

**fit\_intercept** [boolean, optional (default=True)] Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (i.e. data is expected to

be already centered).

- intercept\_scaling [float, optional (default=1)] When self.fit\_intercept is True, instance vector
  x becomes [x, self.intercept\_scaling], i.e. a "synthetic" feature with constant
  value equals to intercept\_scaling is appended to the instance vector. The intercept becomes
  intercept\_scaling \* synthetic feature weight Note! the synthetic feature weight is subject to
  11/12 regularization as all other features. To lessen the effect of regularization on synthetic
  feature weight (and therefore on the intercept) intercept\_scaling has to be increased.
- class\_weight [{dict, 'balanced'}, optional] Set the parameter C of class i to
   class\_weight[i] \*C for SVC. If not given, all classes are supposed to have weight
   one. The "balanced" mode uses the values of y to automatically adjust weights inversely
   proportional to class frequencies in the input data as n\_samples / (n\_classes \*
   np.bincount(y))
- **verbose** [int, (default=0)] Enable verbose output. Note that this setting takes advantage of a perprocess runtime setting in liblinear that, if enabled, may not work properly in a multithreaded context
- random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data for the dual coordinate descent (if dual=True). When dual=False the underlying implementation of LinearSVC is not random and random\_state has no effect on the results. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

max\_iter [int, (default=1000)] The maximum number of iterations to be run.

## **Attributes**

**coef**\_ [array, shape = [n\_features] if n\_classes == 2 else [n\_classes, n\_features]] Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel.

coef\_ is a readonly property derived from raw\_coef\_ that follows the internal memory layout of liblinear.

**intercept**\_ [array, shape = [1] if n\_classes == 2 else [n\_classes]] Constants in decision function.

## See also:

- SVC Implementation of Support Vector Machine classifier using libsvm: the kernel can be non-linear but its SMO algorithm does not scale to large number of samples as LinearSVC does. Furthermore SVC multiclass mode is implemented using one vs one scheme while LinearSVC uses one vs the rest. It is possible to implement one vs the rest with SVC by using the sklearn.multiclass.OneVsRestClassifier wrapper. Finally SVC can fit dense data without memory copy if the input is C-contiguous. Sparse data will still incur memory copy though.
- **sklearn.linear\_model.SGDClassifier** SGDClassifier can optimize the same cost function as LinearSVC by adjusting the penalty and loss parameters. In addition it requires less memory, allows incremental (online) learning, and implements various loss functions and regularization regimes.

## **Notes**

The underlying C implementation uses a random number generator to select features when fitting the model. It is thus not uncommon to have slightly different results for the same input data. If that happens, try with a smaller tol parameter.

The underlying implementation, liblinear, uses a sparse internal representation for the data that will incur a memory copy.

Predict output may not match that of standalone liblinear in certain cases. See *differences from liblinear* in the narrative documentation.

## References

LIBLINEAR: A Library for Large Linear Classification

## **Examples**

## **Methods**

decision_function(self, X)	Predict confidence scores for samples.
densify(self)	Convert coefficient matrix to dense array format.
fit(self, X, y[, sample_weight])	Fit the model according to the given training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict class labels for samples in X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.
sparsify(self)	Convert coefficient matrix to sparse format.

```
__init__ (self, penalty='l2', loss='squared_hinge', dual=True, tol=0.0001, C=1.0, multi_class='ovr', fit_intercept=True, intercept_scaling=1, class_weight=None, verbose=0, random_state=None, max_iter=1000)
```

## decision function (self, X)

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

## **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

## **Returns**

array, shape=(n\_samples,) if n\_classes == 2 else (n\_samples, n\_classes) Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes\_[1] where >0 means this class would be predicted.

## densify (self)

Convert coefficient matrix to dense array format.

Converts the <code>coef\_</code> member (back) to a numpy.ndarray. This is the default format of <code>coef\_</code> and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

#### Returns

**self** [estimator]

**fit** (*self*, *X*, *y*, *sample\_weight=None*)

Fit the model according to the given training data.

### **Parameters**

X [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vector, where n samples in the number of samples and n features is the number of features.

y [array-like, shape = [n\_samples]] Target vector relative to X

**sample\_weight** [array-like, shape = [n\_samples], optional] Array of weights that are assigned to individual samples. If not provided, then each sample is given unit weight.

#### Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Predict class labels for samples in X.

#### **Parameters**

**X** [array like or sparse matrix, shape (n samples, n features)] Samples.

## Returns

C [array, shape [n\_samples]] Predicted class label per sample.

score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

## **Parameters**

X [array-like, shape = (n\_samples, n\_features)] Test samples.

 $\mathbf{y}$  [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for  $\mathbf{X}$ .

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## **Returns**

**score** [float] Mean accuracy of self.predict(X) wrt. y.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## **Returns**

self

## sparsify(self)

Convert coefficient matrix to sparse format.

Converts the coef\_ member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept\_ member is not converted.

#### Returns

**self** [estimator]

## **Notes**

For non-sparse models, i.e. when there are not many zeros in coef, this may actually *increase* memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with (coef == 0). sum(), must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial\_fit method (if any) will not work until you call densify.

## Examples using sklearn.svm.LinearSVC

- Explicit feature map approximation for RBF kernels
- Comparison of Calibration of Classifiers
- Probability Calibration curves
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Column Transformer with Heterogeneous Data Sources
- Pipeline Anova SVM
- Balance model complexity and cross-validated score
- · Precision-Recall
- Feature discretization
- · Plot different SVM classifiers in the iris dataset
- Scaling the regularization parameter for SVCs
- Classification of text documents using sparse features

## sklearn.svm.LinearSVR

```
class sklearn.svm.LinearSVR (epsilon=0.0, tol=0.0001, C=1.0, loss='epsilon_insensitive', fit_intercept=True, intercept_scaling=1.0, dual=True, verbose=0, random_state=None, max_iter=1000)
```

Linear Support Vector Regression.

Similar to SVR with parameter kernel='linear', but implemented in terms of liblinear rather than libsym, so it has more flexibility in the choice of penalties and loss functions and should scale better to large numbers of samples.

This class supports both dense and sparse input.

Read more in the User Guide.

### **Parameters**

- **epsilon** [float, optional (default=0.0)] Epsilon parameter in the epsilon-insensitive loss function. Note that the value of this parameter depends on the scale of the target variable y. If unsure, set epsilon=0.
- tol [float, optional (default=1e-4)] Tolerance for stopping criteria.
- C [float, optional (default=1.0)] Penalty parameter C of the error term. The penalty is a squared 12 penalty. The bigger this parameter, the less regularization is used.
- **loss** [string, optional (default='epsilon\_insensitive')] Specifies the loss function. The epsilon-insensitive loss (standard SVR) is the L1 loss, while the squared epsilon-insensitive loss ('squared\_epsilon\_insensitive') is the L2 loss.
- **fit\_intercept** [boolean, optional (default=True)] Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (i.e. data is expected to be already centered).
- intercept\_scaling [float, optional (default=1)] When self.fit\_intercept is True, instance vector x becomes [x, self.intercept\_scaling], i.e. a "synthetic" feature with constant value equals to intercept\_scaling is appended to the instance vector. The intercept becomes intercept\_scaling \* synthetic feature weight Note! the synthetic feature weight is subject to 11/12 regularization as all other features. To lessen the effect of regularization on synthetic feature weight (and therefore on the intercept) intercept\_scaling has to be increased.
- **dual** [bool, (default=True)] Select the algorithm to either solve the dual or primal optimization problem. Prefer dual=False when n\_samples > n\_features.
- **verbose** [int, (default=0)] Enable verbose output. Note that this setting takes advantage of a perprocess runtime setting in liblinear that, if enabled, may not work properly in a multithreaded context.
- random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- max\_iter [int, (default=1000)] The maximum number of iterations to be run.

## **Attributes**

**coef**\_ [array, shape = [n\_features] if n\_classes == 2 else [n\_classes, n\_features]] Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel.

coef\_ is a readonly property derived from raw\_coef\_ that follows the internal memory
layout of liblinear.

**intercept** [array, shape = [1] if n\_classes == 2 else [n\_classes]] Constants in decision function.

## See also:

- **LinearSVC** Implementation of Support Vector Machine classifier using the same library as this class (liblinear).
- **SVR** Implementation of Support Vector Machine regression using libsvm: the kernel can be non-linear but its SMO algorithm does not scale to large number of samples as LinearSVC does.
- **sklearn.linear\_model.SGDRegressor** SGDRegressor can optimize the same cost function as LinearSVR by adjusting the penalty and loss parameters. In addition it requires less memory, allows incremental (online) learning, and implements various loss functions and regularization regimes.

## **Examples**

## Methods

fit(self, X, y[, sample_weight])	Fit the model according to the given training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Predict using the linear model
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

- \_\_init\_\_ (self, epsilon=0.0, tol=0.0001, C=1.0, loss='epsilon\_insensitive', fit\_intercept=True, intercept\_scaling=1.0, dual=True, verbose=0, random\_state=None, max\_iter=1000)
- **fit** (*self*, *X*, *y*, *sample\_weight=None*)

Fit the model according to the given training data.

## **Parameters**

- **X** [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] Training vector, where n samples in the number of samples and n features is the number of features.
- y [array-like, shape = [n\_samples]] Target vector relative to X

**sample\_weight** [array-like, shape = [n\_samples], optional] Array of weights that are assigned to individual samples. If not provided, then each sample is given unit weight.

#### Returns

self [object]

get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

predict (self, X)

Predict using the linear model

#### **Parameters**

**X** [array\_like or sparse matrix, shape (n\_samples, n\_features)] Samples.

## Returns

C [array, shape (n\_samples,)] Returns predicted values.

score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

### **Parameters**

**X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## sklearn.svm.NuSVC

```
class sklearn.svm.NuSVC (nu=0.5, kernel='rbf', degree=3, gamma='auto\_deprecated', coef0=0.0, shrinking=True, probability=False, tol=0.001, cache\_size=200, class\_weight=None, verbose=False, max\_iter=-1, decision\_function\_shape='ovr', random\_state=None)
```

Nu-Support Vector Classification.

Similar to SVC but uses a parameter to control the number of support vectors.

The implementation is based on libsym.

Read more in the *User Guide*.

#### **Parameters**

- **nu** [float, optional (default=0.5)] An upper bound on the fraction of training errors and a lower bound of the fraction of support vectors. Should be in the interval (0, 1].
- **kernel** [string, optional (default='rbf')] Specifies the kernel type to be used in the algorithm. It must be one of 'linear', 'poly', 'rbf', 'sigmoid', 'precomputed' or a callable. If none is given, 'rbf' will be used. If a callable is given it is used to precompute the kernel matrix.
- **degree** [int, optional (default=3)] Degree of the polynomial kernel function ('poly'). Ignored by all other kernels.
- gamma [float, optional (default='auto')] Kernel coefficient for 'rbf', 'poly' and 'sigmoid'.
  - Current default is 'auto' which uses 1 / n\_features, if gamma='scale' is passed then it uses 1 / (n\_features \* X.var()) as value of gamma. The current default of gamma, 'auto', will change to 'scale' in version 0.22. 'auto\_deprecated', a deprecated version of 'auto' is used as a default indicating that no explicit value of gamma was passed.
- **coef0** [float, optional (default=0.0)] Independent term in kernel function. It is only significant in 'poly' and 'sigmoid'.
- **shrinking** [boolean, optional (default=True)] Whether to use the shrinking heuristic.
- **probability** [boolean, optional (default=False)] Whether to enable probability estimates. This must be enabled prior to calling fit, and will slow down that method.
- tol [float, optional (default=1e-3)] Tolerance for stopping criterion.
- cache\_size [float, optional] Specify the size of the kernel cache (in MB).
- class\_weight [{dict, 'balanced'}, optional] Set the parameter C of class i to class\_weight[i]\*C
   for SVC. If not given, all classes are supposed to have weight one. The "balanced" mode
   uses the values of y to automatically adjust weights inversely proportional to class frequen cies as n\_samples / (n\_classes \* np.bincount(y))

**verbose** [bool, default: False] Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in libsym that, if enabled, may not work properly in a multithreaded context.

max\_iter [int, optional (default=-1)] Hard limit on iterations within solver, or -1 for no limit.

**decision\_function\_shape** ['ovo', 'ovr', default='ovr'] Whether to return a one-vs-rest ('ovr') decision function of shape (n\_samples, n\_classes) as all other classifiers, or the original one-vs-one ('ovo') decision function of libsvm which has shape (n\_samples, n\_classes \* (n\_classes - 1) / 2).

Changed in version 0.19: decision\_function\_shape is 'ovr' by default.

New in version 0.17: decision\_function\_shape='ovr' is recommended.

Changed in version 0.17: Deprecated decision\_function\_shape='ovo' and None.

random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator used when shuffling the data for probability estimates. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### **Attributes**

```
support_ [array-like, shape = [n_SV]] Indices of support vectors.
```

**support\_vectors**\_ [array-like, shape = [n\_SV, n\_features]] Support vectors.

**n\_support\_** [array-like, dtype=int32, shape = [n\_class]] Number of support vectors for each class.

**dual\_coef\_** [array, shape = [n\_class-1, n\_SV]] Coefficients of the support vector in the decision function. For multiclass, coefficient for all 1-vs-1 classifiers. The layout of the coefficients in the multiclass case is somewhat non-trivial. See the section about multi-class classification in the SVM section of the User Guide for details.

**coef**\_ [array, shape = [n\_class \* (n\_class-1) / 2, n\_features]] Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel.

coef\_ is readonly property derived from dual\_coef\_ and support\_vectors\_.

 $intercept_{normal} [array, shape = [n_class * (n_class-1) / 2]] Constants in decision function.$ 

## See also:

SVC Support Vector Machine for classification using libsvm.

**LinearSVC** Scalable linear Support Vector Machine for classification using liblinear.

#### **Notes**

References: LIBSVM: A Library for Support Vector Machines

## **Examples**

```
>>> import numpy as np
>>> X = np.array([[-1, -1], [-2, -1], [1, 1], [2, 1]])
>>> y = np.array([1, 1, 2, 2])
>>> from sklearn.svm import NuSVC
```

```
>>> clf = NuSVC(gamma='scale')
>>> clf.fit(X, y)
NuSVC(cache_size=200, class_weight=None, coef0=0.0,
    decision_function_shape='ovr', degree=3, gamma='scale', kernel='rbf',
    max_iter=-1, nu=0.5, probability=False, random_state=None,
    shrinking=True, tol=0.001, verbose=False)
>>> print(clf.predict([[-0.8, -1]]))
[1]
```

## **Methods**

decision_function(self, X)	Evaluates the decision function for the samples in X.
fit(self, X, y[, sample_weight])	Fit the SVM model according to the given training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Perform classification on samples in X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, nu=0.5, kernel='rbf', degree=3, gamma='auto_deprecated', coef0=0.0, shrink-ing=True, probability=False, tol=0.001, cache_size=200, class_weight=None, verbose=False, max_iter=-1, decision_function_shape='ovr', random_state=None)
```

## $decision\_function(self, X)$

Evaluates the decision function for the samples in X.

## **Parameters**

**X** [array-like, shape (n samples, n features)]

## Returns

**X** [array-like, shape (n\_samples, n\_classes \* (n\_classes-1) / 2)] Returns the decision function of the sample for each class in the model. If decision\_function\_shape='ovr', the shape is (n\_samples, n\_classes).

## **Notes**

If decision\_function\_shape='ovo', the function values are proportional to the distance of the samples X to the separating hyperplane. If the exact distances are required, divide the function values by the norm of the weight vector (coef\_). See also this question for further details. If decision\_function\_shape='ovr', the decision function is a monotonic transformation of ovo decision function.

## fit (self, X, y, sample\_weight=None)

Fit the SVM model according to the given training data.

## **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training vectors, where n\_samples is the number of samples and n\_features is the number of features. For kernel="precomputed", the expected shape of X is (n\_samples, n\_samples).
- y [array-like, shape (n\_samples,)] Target values (class labels in classification, real numbers in regression)

**sample\_weight** [array-like, shape (n\_samples,)] Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.

#### Returns

self [object]

## **Notes**

If X and y are not C-ordered and contiguous arrays of np.float64 and X is not a scipy.sparse.csr\_matrix, X and/or y may be copied.

If X is a dense array, then the other methods will not support sparse matrices as input.

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Perform classification on samples in X.

For an one-class model, +1 or -1 is returned.

### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] For kernel="precomputed", the expected shape of X is [n\_samples\_test, n\_samples\_train]

### **Returns**

**y\_pred** [array, shape (n\_samples,)] Class labels for samples in X.

## predict\_log\_proba

Compute log probabilities of possible outcomes for samples in X.

The model need to have probability information computed at training time: fit with attribute probability set to True.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] For kernel="precomputed", the expected shape of X is [n\_samples\_test, n\_samples\_train]

## Returns

**T** [array-like, shape (n\_samples, n\_classes)] Returns the log-probabilities of the sample for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

## **Notes**

The probability model is created using cross validation, so the results can be slightly different than those obtained by predict. Also, it will produce meaningless results on very small datasets.

## predict\_proba

Compute probabilities of possible outcomes for samples in X.

The model need to have probability information computed at training time: fit with attribute probability set to True.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] For kernel="precomputed", the expected shape of X is [n\_samples test, n\_samples train]

## Returns

**T** [array-like, shape (n\_samples, n\_classes)] Returns the probability of the sample for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

## **Notes**

The probability model is created using cross validation, so the results can be slightly different than those obtained by predict. Also, it will produce meaningless results on very small datasets.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

## **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## **Returns**

self

## Examples using sklearn.svm.NuSVC

• Non-linear SVM

## sklearn.svm.NuSVR

```
class sklearn.svm.NuSVR (nu=0.5, C=1.0, kernel='rbf', degree=3, gamma='auto\_deprecated', coef0=0.0, shrinking=True, tol=0.001, cache\_size=200, verbose=False, max\ iter=-1)
```

Nu Support Vector Regression.

Similar to NuSVC, for regression, uses a parameter nu to control the number of support vectors. However, unlike NuSVC, where nu replaces C, here nu replaces the parameter epsilon of epsilon-SVR.

The implementation is based on libsym.

Read more in the User Guide.

## **Parameters**

- **nu** [float, optional] An upper bound on the fraction of training errors and a lower bound of the fraction of support vectors. Should be in the interval (0, 1]. By default 0.5 will be taken.
- **C** [float, optional (default=1.0)] Penalty parameter C of the error term.
- **kernel** [string, optional (default='rbf')] Specifies the kernel type to be used in the algorithm. It must be one of 'linear', 'poly', 'rbf', 'sigmoid', 'precomputed' or a callable. If none is given, 'rbf' will be used. If a callable is given it is used to precompute the kernel matrix.
- **degree** [int, optional (default=3)] Degree of the polynomial kernel function ('poly'). Ignored by all other kernels.
- gamma [float, optional (default='auto')] Kernel coefficient for 'rbf', 'poly' and 'sigmoid'.
  - Current default is 'auto' which uses 1 / n\_features, if gamma='scale' is passed then it uses 1 / (n\_features \* X.var()) as value of gamma. The current default of gamma, 'auto', will change to 'scale' in version 0.22. 'auto\_deprecated', a deprecated version of 'auto' is used as a default indicating that no explicit value of gamma was passed.
- **coef0** [float, optional (default=0.0)] Independent term in kernel function. It is only significant in 'poly' and 'sigmoid'.
- **shrinking** [boolean, optional (default=True)] Whether to use the shrinking heuristic.
- tol [float, optional (default=1e-3)] Tolerance for stopping criterion.
- **cache\_size** [float, optional] Specify the size of the kernel cache (in MB).
- **verbose** [bool, default: False] Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in libsym that, if enabled, may not work properly in a multithreaded context.
- max\_iter [int, optional (default=-1)] Hard limit on iterations within solver, or -1 for no limit.

### **Attributes**

```
support_ [array-like, shape = [n_SV]] Indices of support vectors.
```

- **support\_vectors**\_ [array-like, shape = [nSV, n\_features]] Support vectors.
- dual\_coef\_ [array, shape = [1, n\_SV]] Coefficients of the support vector in the decision function.
- **coef**\_ [array, shape = [1, n\_features]] Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel.

```
coef_ is readonly property derived from dual_coef_ and support_vectors_.
```

**intercept**\_ [array, shape = [1]] Constants in decision function.

## See also:

**NuSVC** Support Vector Machine for classification implemented with libsym with a parameter to control the number of support vectors.

**SVR** epsilon Support Vector Machine for regression implemented with libsym.

## **Notes**

**References:** LIBSVM: A Library for Support Vector Machines

## **Examples**

```
>>> from sklearn.svm import NuSVR
>>> import numpy as np
>>> n_samples, n_features = 10, 5
>>> np.random.seed(0)
>>> y = np.random.randn(n_samples)
>>> X = np.random.randn(n_samples, n_features)
>>> clf = NuSVR(gamma='scale', C=1.0, nu=0.1)
>>> clf.fit(X, y)
NuSVR(C=1.0, cache_size=200, coef0=0.0, degree=3, gamma='scale', kernel='rbf', max_iter=-1, nu=0.1, shrinking=True, tol=0.001, verbose=False)
```

## **Methods**

fit(self, X, y[, sample_weight])	Fit the SVM model according to the given training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Perform regression on samples in X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, nu=0.5, C=1.0, kernel='rbf', degree=3, gamma='auto_deprecated', coef0=0.0, shrink-ing=True, tol=0.001, cache_size=200, verbose=False, max_iter=-1)
```

fit (self, X, y, sample\_weight=None)

Fit the SVM model according to the given training data.

## **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training vectors, where n\_samples is the number of samples and n\_features is the number of features. For kernel="precomputed", the expected shape of X is (n\_samples, n\_samples).
- y [array-like, shape (n\_samples,)] Target values (class labels in classification, real numbers in regression)

**sample\_weight** [array-like, shape (n\_samples,)] Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.

## **Returns**

self [object]

## **Notes**

If X and y are not C-ordered and contiguous arrays of np.float64 and X is not a scipy.sparse.csr\_matrix, X and/or y may be copied.

If X is a dense array, then the other methods will not support sparse matrices as input.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Perform regression on samples in X.

For an one-class model, +1 (inlier) or -1 (outlier) is returned.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] For kernel="precomputed", the expected shape of X is (n\_samples\_test, n\_samples\_train).

### **Returns**

**y\_pred** [array, shape (n\_samples,)]

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

## **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

## Returns

**score** [float] R^2 of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor).

To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## Examples using sklearn.svm.NuSVR

• Model Complexity Influence

#### sklearn.svm.OneClassSVM

class sklearn.svm.OneClassSVM (kernel='rbf', degree=3,  $gamma='auto\_deprecated'$ , coef0=0.0, tol=0.001, nu=0.5, shrinking=True,  $cache\_size=200$ , verbose=False,  $max\_iter=-1$ ,  $random\_state=None$ )

Unsupervised Outlier Detection.

Estimate the support of a high-dimensional distribution.

The implementation is based on libsym.

Read more in the User Guide.

#### **Parameters**

**kernel** [string, optional (default='rbf')] Specifies the kernel type to be used in the algorithm. It must be one of 'linear', 'poly', 'rbf', 'sigmoid', 'precomputed' or a callable. If none is given, 'rbf' will be used. If a callable is given it is used to precompute the kernel matrix.

**degree** [int, optional (default=3)] Degree of the polynomial kernel function ('poly'). Ignored by all other kernels.

gamma [float, optional (default='auto')] Kernel coefficient for 'rbf', 'poly' and 'sigmoid'.

Current default is 'auto' which uses 1 / n\_features, if gamma='scale' is passed then it uses 1 / (n\_features \* X.var()) as value of gamma. The current default of gamma, 'auto', will change to 'scale' in version 0.22. 'auto\_deprecated', a deprecated version of 'auto' is used as a default indicating that no explicit value of gamma was passed.

**coef0** [float, optional (default=0.0)] Independent term in kernel function. It is only significant in 'poly' and 'sigmoid'.

tol [float, optional] Tolerance for stopping criterion.

**nu** [float, optional] An upper bound on the fraction of training errors and a lower bound of the fraction of support vectors. Should be in the interval (0, 1]. By default 0.5 will be taken.

**shrinking** [boolean, optional] Whether to use the shrinking heuristic.

cache\_size [float, optional] Specify the size of the kernel cache (in MB).

**verbose** [bool, default: False] Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in libsym that, if enabled, may not work properly in a multithreaded context.

max\_iter [int, optional (default=-1)] Hard limit on iterations within solver, or -1 for no limit.

random\_state [int, RandomState instance or None, optional (default=None)] Ignored.

Deprecated since version 0.20: random\_state has been deprecated in 0.20 and will be removed in 0.22.

## **Attributes**

**support** [array-like, shape =  $[n_SV]$ ] Indices of support vectors.

support\_vectors\_ [array-like, shape = [nSV, n\_features]] Support vectors.

**dual\_coef\_** [array, shape = [1, n\_SV]] Coefficients of the support vectors in the decision function.

**coef**\_ [array, shape = [1, n\_features]] Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel.

coef\_ is readonly property derived from dual\_coef\_ and support\_vectors\_

**intercept**\_ [array, shape = [1,]] Constant in the decision function.

**offset**\_ [float] Offset used to define the decision function from the raw scores. We have the relation: decision\_function = score\_samples - offset\_. The offset is the opposite of intercept\_ and is provided for consistency with other outlier detection algorithms.

## **Examples**

```
>>> from sklearn.svm import OneClassSVM
>>> X = [[0], [0.44], [0.45], [0.46], [1]]
>>> clf = OneClassSVM(gamma='auto').fit(X)
>>> clf.predict(X)
array([-1, 1, 1, -1])
>>> clf.score_samples(X)
array([1.7798..., 2.0547..., 2.0556..., 2.0561..., 1.7332...])
```

## **Methods**

decision_function(self, X)	Signed distance to the separating hyperplane.
fit(self, X[, y, sample_weight])	Detects the soft boundary of the set of samples X.
<pre>fit_predict(self, X[, y])</pre>	Performs fit on X and returns labels for X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Perform classification on samples in X.
score_samples(self, X)	Raw scoring function of the samples.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, kernel='rbf', degree=3, gamma='auto\_deprecated', coef0=0.0, tol=0.001, nu=0.5, shrinking=True, cache\_size=200, verbose=False, max\_iter=-1, random\_state=None)

## $decision_function(self, X)$

Signed distance to the separating hyperplane.

Signed distance is positive for an inlier and negative for an outlier.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

## Returns

**dec** [array-like, shape (n samples,)] Returns the decision function of the samples.

 $\label{fit} \textbf{fit} \ (\textit{self}, \textit{X}, \textit{y=None}, \textit{sample\_weight=None}, \ **params)$ 

Detects the soft boundary of the set of samples X.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Set of samples, where n\_samples is the number of samples and n\_features is the number of features.

**sample\_weight** [array-like, shape (n\_samples,)] Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.

y [Ignored] not used, present for API consistency by convention.

## **Returns**

self [object]

#### **Notes**

If X is not a C-ordered contiguous array it is copied.

```
fit_predict (self, X, y=None)
```

Performs fit on X and returns labels for X.

Returns -1 for outliers and 1 for inliers.

## **Parameters**

- **X** [ndarray, shape (n\_samples, n\_features)] Input data.
- y [Ignored] not used, present for API consistency by convention.

## Returns

**y** [ndarray, shape (n\_samples,)] 1 for inliers, -1 for outliers.

## get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Perform classification on samples in X.

For a one-class model, +1 or -1 is returned.

## **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] For kernel="precomputed", the expected shape of X is [n\_samples\_test, n\_samples\_train]

#### Returns

**y\_pred** [array, shape (n\_samples,)] Class labels for samples in X.

#### score\_samples (self, X)

Raw scoring function of the samples.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

## **Returns**

**score\_samples** [array-like, shape (n\_samples,)] Returns the (unshifted) scoring function of the samples.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## Examples using sklearn.svm.OneClassSVM

- Comparing anomaly detection algorithms for outlier detection on toy datasets
- Outlier detection on a real data set
- Species distribution modeling
- Libsvm GUI
- One-class SVM with non-linear kernel (RBF)

## sklearn.svm.SVC

C-Support Vector Classification.

The implementation is based on libsym. The fit time scales at least quadratically with the number of samples and may be impractical beyond tens of thousands of samples. For large datasets consider using sklearn. linear\_model.LinearSVC or sklearn.linear\_model.SGDClassifier instead, possibly after a sklearn.kernel approximation.Nystroem transformer.

The multiclass support is handled according to a one-vs-one scheme.

For details on the precise mathematical formulation of the provided kernel functions and how gamma, coef0 and degree affect each other, see the corresponding section in the narrative documentation: *Kernel functions*.

Read more in the User Guide.

## **Parameters**

C [float, optional (default=1.0)] Penalty parameter C of the error term.

**kernel** [string, optional (default='rbf')] Specifies the kernel type to be used in the algorithm. It must be one of 'linear', 'poly', 'rbf', 'sigmoid', 'precomputed' or a callable. If none is given, 'rbf' will be used. If a callable is given it is used to pre-compute the kernel matrix from data matrices; that matrix should be an array of shape (n\_samples, n\_samples).

**degree** [int, optional (default=3)] Degree of the polynomial kernel function ('poly'). Ignored by all other kernels.

gamma [float, optional (default='auto')] Kernel coefficient for 'rbf', 'poly' and 'sigmoid'.

Current default is 'auto' which uses 1 / n\_features, if gamma='scale' is passed then it uses 1 / (n\_features \* X.var()) as value of gamma. The current default of gamma, 'auto', will change to 'scale' in version 0.22. 'auto\_deprecated', a deprecated version of 'auto' is used as a default indicating that no explicit value of gamma was passed.

**coef0** [float, optional (default=0.0)] Independent term in kernel function. It is only significant in 'poly' and 'sigmoid'.

**shrinking** [boolean, optional (default=True)] Whether to use the shrinking heuristic.

**probability** [boolean, optional (default=False)] Whether to enable probability estimates. This must be enabled prior to calling fit, and will slow down that method.

tol [float, optional (default=1e-3)] Tolerance for stopping criterion.

cache\_size [float, optional] Specify the size of the kernel cache (in MB).

class\_weight [{dict, 'balanced'}, optional] Set the parameter C of class i to class\_weight[i]\*C
 for SVC. If not given, all classes are supposed to have weight one. The "balanced" mode
 uses the values of y to automatically adjust weights inversely proportional to class frequen cies in the input data as n\_samples / (n\_classes \* np.bincount(y))

**verbose** [bool, default: False] Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in libsvm that, if enabled, may not work properly in a multithreaded context.

max\_iter [int, optional (default=-1)] Hard limit on iterations within solver, or -1 for no limit.

**decision\_function\_shape** ['ovo', 'ovr', default='ovr'] Whether to return a one-vs-rest ('ovr') decision function of shape (n\_samples, n\_classes) as all other classifiers, or the original one-vs-one ('ovo') decision function of libsvm which has shape (n\_samples, n\_classes \* (n\_classes - 1) / 2). However, one-vs-one ('ovo') is always used as multi-class strategy.

Changed in version 0.19: decision\_function\_shape is 'ovr' by default.

New in version 0.17: decision\_function\_shape='ovr' is recommended.

Changed in version 0.17: Deprecated decision\_function\_shape='ovo' and None.

random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator used when shuffling the data for probability estimates. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

## Attributes

**support**\_ [array-like, shape = [n\_SV]] Indices of support vectors.

```
support_vectors_ [array-like, shape = [n_SV, n_features]] Support vectors.
```

**n\_support\_** [array-like, dtype=int32, shape = [n\_class]] Number of support vectors for each class.

dual\_coef\_ [array, shape = [n\_class-1, n\_SV]] Coefficients of the support vector in the decision function. For multiclass, coefficient for all 1-vs-1 classifiers. The layout of the coefficients in the multiclass case is somewhat non-trivial. See the section about multi-class classification in the SVM section of the User Guide for details.

**coef**\_ [array, shape = [n\_class \* (n\_class-1) / 2, n\_features]] Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel.

```
coef_ is a readonly property derived from dual_coef_ and support_vectors_.
```

**intercept**\_ [array, shape =  $[n_{class} * (n_{class-1}) / 2]]$  Constants in decision function.

**fit\_status\_** [int] 0 if correctly fitted, 1 otherwise (will raise warning)

```
probA_ [array, shape = [n_{class} * (n_{class-1}) / 2]]
```

**probB**\_ [array, shape = [n\_class \* (n\_class-1) / 2]] If probability=True, the parameters learned in Platt scaling to produce probability estimates from decision values. If probability=False, an empty array. Platt scaling uses the logistic function 1 / (1 + exp(decision\_value \* probA\_ + probB\_)) where probA\_ and probB\_ are learned from the dataset [R20c70293ef72-2]. For more information on the multiclass case and training procedure see section 8 of [R20c70293ef72-1].

#### See also:

**SVR** Support Vector Machine for Regression implemented using libsym.

**LinearSVC** Scalable Linear Support Vector Machine for classification implemented using liblinear. Check the See also section of LinearSVC for more comparison element.

## References

[R20c70293ef72-1], [R20c70293ef72-2]

## **Examples**

```
>>> import numpy as np
>>> X = np.array([[-1, -1], [-2, -1], [1, 1], [2, 1]])
>>> y = np.array([1, 1, 2, 2])
>>> from sklearn.svm import SVC
>>> clf = SVC(gamma='auto')
>>> clf.fit(X, y)
SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0,
    decision_function_shape='ovr', degree=3, gamma='auto', kernel='rbf',
    max_iter=-1, probability=False, random_state=None, shrinking=True,
    tol=0.001, verbose=False)
>>> print(clf.predict([[-0.8, -1]]))
[1]
```

## **Methods**

decision_function(self, X)	Evaluates the decision function for the samples in X.
fit(self, X, y[, sample_weight])	Fit the SVM model according to the given training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Perform classification on samples in X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_init\_\_ (self, C=1.0, kernel='rbf', degree=3, gamma='auto\_deprecated', coef0=0.0, shrink-ing=True, probability=False, tol=0.001, cache\_size=200, class\_weight=None, verbose=False, max\_iter=-1, decision\_function\_shape='ovr', random\_state=None)

## decision\_function(self, X)

Evaluates the decision function for the samples in X.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)]

## **Returns**

**X** [array-like, shape (n\_samples, n\_classes \* (n\_classes-1) / 2)] Returns the decision function of the sample for each class in the model. If decision\_function\_shape='ovr', the shape is (n\_samples, n\_classes).

#### **Notes**

If decision\_function\_shape='ovo', the function values are proportional to the distance of the samples X to the separating hyperplane. If the exact distances are required, divide the function values by the norm of the weight vector (coef\_). See also this question for further details. If decision\_function\_shape='ovr', the decision function is a monotonic transformation of ovo decision function.

## **fit** (*self*, *X*, *y*, *sample\_weight=None*)

Fit the SVM model according to the given training data.

## **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training vectors, where n\_samples is the number of samples and n\_features is the number of features. For kernel="precomputed", the expected shape of X is (n\_samples, n\_samples).
- y [array-like, shape (n\_samples,)] Target values (class labels in classification, real numbers in regression)

**sample\_weight** [array-like, shape (n\_samples,)] Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.

## **Returns**

self [object]

## **Notes**

If X and y are not C-ordered and contiguous arrays of np.float64 and X is not a scipy.sparse.csr\_matrix, X and/or y may be copied.

If X is a dense array, then the other methods will not support sparse matrices as input.

## get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## predict (self, X)

Perform classification on samples in X.

For an one-class model, +1 or -1 is returned.

### **Parameters**

X [{array-like, sparse matrix}, shape (n\_samples, n\_features)] For kernel="precomputed", the expected shape of X is [n\_samples\_test, n\_samples\_train]

#### Returns

**y\_pred** [array, shape (n\_samples,)] Class labels for samples in X.

## predict\_log\_proba

Compute log probabilities of possible outcomes for samples in X.

The model need to have probability information computed at training time: fit with attribute probability set to True.

## **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] For kernel="precomputed", the expected shape of X is [n\_samples\_test, n\_samples\_train]

## **Returns**

**T** [array-like, shape (n\_samples, n\_classes)] Returns the log-probabilities of the sample for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*\_.

## **Notes**

The probability model is created using cross validation, so the results can be slightly different than those obtained by predict. Also, it will produce meaningless results on very small datasets.

## predict\_proba

Compute probabilities of possible outcomes for samples in X.

The model need to have probability information computed at training time: fit with attribute probability set to True.

#### **Parameters**

**X** [array-like, shape (n\_samples, n\_features)] For kernel="precomputed", the expected shape of X is [n\_samples\_test, n\_samples\_train]

## Returns

**T** [array-like, shape (n\_samples, n\_classes)] Returns the probability of the sample for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute *classes*.

#### **Notes**

The probability model is created using cross validation, so the results can be slightly different than those obtained by predict. Also, it will produce meaningless results on very small datasets.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

### Examples using sklearn.svm.SVC

- Multilabel classification
- Explicit feature map approximation for RBF kernels
- Faces recognition example using eigenfaces and SVMs
- Libsvm GUI
- Recognizing hand-written digits
- Plot classification probability
- Classifier comparison
- Concatenating multiple feature extraction methods
- Plot the decision boundaries of a VotingClassifier
- Cross-validation on Digits Dataset Exercise
- SVM Exercise
- Recursive feature elimination

- Recursive feature elimination with cross-validation
- Test with permutations the significance of a classification score
- Univariate Feature Selection
- Plotting Validation Curves
- Parameter estimation using grid search with cross-validation
- Receiver Operating Characteristic (ROC) with cross validation
- Nested versus non-nested cross-validation
- Confusion matrix
- Receiver Operating Characteristic (ROC)
- Plotting Learning Curves
- Feature discretization
- · Decision boundary of label propagation versus SVM on the Iris dataset
- SVM: Maximum margin separating hyperplane
- SVM with custom kernel
- SVM: Weighted samples
- SVM: Separating hyperplane for unbalanced classes
- SVM-Kernels
- SVM-Anova: SVM with univariate feature selection
- SVM Margins Example
- Plot different SVM classifiers in the iris dataset
- RBF SVM parameters

# sklearn.svm.SVR

```
class sklearn.svm.SVR (kernel='rbf', degree=3, gamma='auto\_deprecated', coef0=0.0, tol=0.001, C=1.0, epsilon=0.1, shrinking=True, cache\_size=200, verbose=False, max\_iter=-1)
```

Epsilon-Support Vector Regression.

The free parameters in the model are C and epsilon.

The implementation is based on libsvm. The fit time complexity is more than quadratic with the number of samples which makes it hard to scale to datasets with more than a couple of 10000 samples. For large datasets consider using sklearn.linear\_model.LinearSVR or sklearn.linear\_model.SGDRegressor instead, possibly after a sklearn.kernel\_approximation.Nystroem transformer.

Read more in the User Guide.

### **Parameters**

**kernel** [string, optional (default='rbf')] Specifies the kernel type to be used in the algorithm. It must be one of 'linear', 'poly', 'rbf', 'sigmoid', 'precomputed' or a callable. If none is given, 'rbf' will be used. If a callable is given it is used to precompute the kernel matrix.

**degree** [int, optional (default=3)] Degree of the polynomial kernel function ('poly'). Ignored by all other kernels.

gamma [float, optional (default='auto')] Kernel coefficient for 'rbf', 'poly' and 'sigmoid'.

Current default is 'auto' which uses 1 / n\_features, if gamma='scale' is passed then it uses 1 / (n\_features \* X.var()) as value of gamma. The current default of gamma, 'auto', will change to 'scale' in version 0.22. 'auto\_deprecated', a deprecated version of 'auto' is used as a default indicating that no explicit value of gamma was passed.

**coef0** [float, optional (default=0.0)] Independent term in kernel function. It is only significant in 'poly' and 'sigmoid'.

tol [float, optional (default=1e-3)] Tolerance for stopping criterion.

C [float, optional (default=1.0)] Penalty parameter C of the error term.

**epsilon** [float, optional (default=0.1)] Epsilon in the epsilon-SVR model. It specifies the epsilon-tube within which no penalty is associated in the training loss function with points predicted within a distance epsilon from the actual value.

**shrinking** [boolean, optional (default=True)] Whether to use the shrinking heuristic.

**cache\_size** [float, optional] Specify the size of the kernel cache (in MB).

**verbose** [bool, default: False] Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in libsym that, if enabled, may not work properly in a multithreaded context.

max\_iter [int, optional (default=-1)] Hard limit on iterations within solver, or -1 for no limit.

#### **Attributes**

### See also:

**NuSVR** Support Vector Machine for regression implemented using libsvm using a parameter to control the number of support vectors.

**LinearSVR** Scalable Linear Support Vector Machine for regression implemented using liblinear.

#### **Notes**

References: LIBSVM: A Library for Support Vector Machines

### **Examples**

```
>>> from sklearn.svm import SVR
>>> import numpy as np
>>> n_samples, n_features = 10, 5
>>> rng = np.random.RandomState(0)
```

#### **Methods**

fit(self, X, y[, sample_weight])	Fit the SVM model according to the given training data.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
predict(self, X)	Perform regression on samples in X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

```
__init__ (self, kernel='rbf', degree=3, gamma='auto_deprecated', coef0=0.0, tol=0.001, C=1.0, epsilon=0.1, shrinking=True, cache_size=200, verbose=False, max_iter=-1)
```

fit (self, X, y, sample\_weight=None)

Fit the SVM model according to the given training data.

#### **Parameters**

- **X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Training vectors, where n\_samples is the number of samples and n\_features is the number of features. For kernel="precomputed", the expected shape of X is (n\_samples, n\_samples).
- y [array-like, shape (n\_samples,)] Target values (class labels in classification, real numbers in regression)

**sample\_weight** [array-like, shape (n\_samples,)] Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.

#### Returns

self [object]

#### **Notes**

If X and y are not C-ordered and contiguous arrays of np.float64 and X is not a scipy.sparse.csr\_matrix, X and/or y may be copied.

If X is a dense array, then the other methods will not support sparse matrices as input.

```
get_params (self, deep=True)
```

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

## Returns

params [mapping of string to any] Parameter names mapped to their values.

#### predict (self, X)

Perform regression on samples in X.

For an one-class model, +1 (inlier) or -1 (outlier) is returned.

#### **Parameters**

**X** [{array-like, sparse matrix}, shape (n\_samples, n\_features)] For kernel="precomputed", the expected shape of X is (n\_samples\_test, n\_samples\_train).

#### Returns

```
y_pred [array, shape (n_samples,)]
```

```
score (self, X, y, sample_weight=None)
```

Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### **Returns**

**score** [float] R^2 of self.predict(X) wrt. y.

## **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## Examples using sklearn.svm.SVR

- Comparison of kernel ridge regression and SVR
- Prediction Latency

• Support Vector Regression (SVR) using linear and non-linear kernels

svm.11_min_c(X, y[, loss, fit_intercept,])	Return the lowest bound for C such that for C in (11_min_C,
	infinity) the model is guaranteed not to be empty.

### sklearn.svm.l1 min c

sklearn.svm.l1\_min\_c(X, y, loss='squared\_hinge', fit\_intercept=True, intercept\_scaling=1.0)

Return the lowest bound for C such that for C in (11\_min\_C, infinity) the model is guaranteed not to be empty. This applies to 11 penalized classifiers, such as LinearSVC with penalty='11' and linear model.LogisticRegression with penalty='11'.

This value is valid if class\_weight parameter in fit() is not set.

#### **Parameters**

- **X** [array-like or sparse matrix, shape = [n\_samples, n\_features]] Training vector, where n\_samples in the number of samples and n\_features is the number of features.
- y [array, shape = [n\_samples]] Target vector relative to X
- **loss** [{'squared\_hinge', 'log'}, default 'squared\_hinge'] Specifies the loss function. With 'squared\_hinge' it is the squared hinge loss (a.k.a. L2 loss). With 'log' it is the loss of logistic regression models.
- **fit\_intercept** [bool, default: True] Specifies if the intercept should be fitted by the model. It must match the fit() method parameter.
- **intercept\_scaling** [float, default: 1] when fit\_intercept is True, instance vector x becomes [x, intercept\_scaling], i.e. a "synthetic" feature with constant value equals to intercept\_scaling is appended to the instance vector. It must match the fit() method parameter.

### Returns

11 min c [float] minimum value for C

# Examples using sklearn.svm.l1\_min\_c

• Regularization path of L1- Logistic Regression

## 6.37.2 Low-level methods

svm.libsvm.cross_validation()	Binding of the cross-validation routine (low-level routine)
<pre>svm.libsvm.decision_function()</pre>	Predict margin (libsvm name for this is predict_values)
svm.libsvm.fit()	Train the model using libsvm (low-level method)
<pre>svm.libsvm.predict()</pre>	Predict target values of X given a model (low-level method)
<pre>svm.libsvm.predict_proba()</pre>	Predict probabilities

# sklearn.svm.libsvm.cross\_validation

sklearn.svm.libsvm.cross\_validation()

Binding of the cross-validation routine (low-level routine)

### **Parameters**

```
X [array-like, dtype=float, size=[n_samples, n_features]]
```

Y [array, dtype=float, size=[n\_samples]] target vector

svm\_type [{0, 1, 2, 3, 4}] Type of SVM: C SVC, nu SVC, one class, epsilon SVR, nu SVR

**kernel** [{'linear', 'rbf', 'poly', 'sigmoid', 'precomputed'}] Kernel to use in the model: linear, polynomial, RBF, sigmoid or precomputed.

degree [int] Degree of the polynomial kernel (only relevant if kernel is set to polynomial)

**gamma** [float] Gamma parameter in rbf, poly and sigmoid kernels. Ignored by other kernels. 0.1 by default.

**coef0** [float] Independent parameter in poly/sigmoid kernel.

tol [float] Stopping criteria.

C [float] C parameter in C-Support Vector Classification

**nu** [float]

cache\_size [float]

**random\_seed** [int, optional] Seed for the random number generator used for probability estimates. 0 by default.

### Returns

target [array, float]

### sklearn.svm.libsvm.decision function

```
sklearn.svm.libsvm.decision function()
```

Predict margin (libsvm name for this is predict\_values)

We have to reconstruct model and parameters to make sure we stay in sync with the python object.

### sklearn.svm.libsvm.fit

```
sklearn.svm.libsvm.fit()
```

Train the model using libsvm (low-level method)

# **Parameters**

**X** [array-like, dtype=float64, size=[n\_samples, n\_features]]

Y [array, dtype=float64, size=[n\_samples]] target vector

**svm\_type** [{0, 1, 2, 3, 4}, optional] Type of SVM: C\_SVC, NuSVC, OneClassSVM, EpsilonSVR or NuSVR respectively. 0 by default.

**kernel** [{'linear', 'rbf', 'poly', 'sigmoid', 'precomputed'}, optional] Kernel to use in the model: linear, polynomial, RBF, sigmoid or precomputed. 'rbf' by default.

**degree** [int32, optional] Degree of the polynomial kernel (only relevant if kernel is set to polynomial), 3 by default.

**gamma** [float64, optional] Gamma parameter in rbf, poly and sigmoid kernels. Ignored by other kernels. 0.1 by default.

**coef0** [float64, optional] Independent parameter in poly/sigmoid kernel. 0 by default.

tol [float64, optional] Numeric stopping criterion (WRITEME). 1e-3 by default.

```
C [float64, optional] C parameter in C-Support Vector Classification. 1 by default.
```

**nu** [float64, optional] 0.5 by default.

epsilon [double, optional] 0.1 by default.

**class\_weight** [array, dtype float64, shape (n\_classes,), optional] np.empty(0) by default.

**sample\_weight** [array, dtype float64, shape (n\_samples,), optional] np.empty(0) by default.

**shrinking** [int, optional] 1 by default.

**probability** [int, optional] 0 by default.

cache\_size [float64, optional] Cache size for gram matrix columns (in megabytes). 100 by default.

max\_iter [int (-1 for no limit), optional.] Stop solver after this many iterations regardless of accuracy (XXX Currently there is no API to know whether this kicked in.) -1 by default.

**random\_seed** [int, optional] Seed for the random number generator used for probability estimates. 0 by default.

#### Returns

support [array, shape=[n\_support]] index of support vectors

**support\_vectors** [array, shape=[n\_support, n\_features]] support vectors (equivalent to X[support]). Will return an empty array in the case of precomputed kernel.

n\_class\_SV [array] number of support vectors in each class.

sv\_coef [array] coefficients of support vectors in decision function.

intercept [array] intercept in decision function

**probA**, **probB** [array] probability estimates, empty array for probability=False

#### sklearn.svm.libsvm.predict

```
sklearn.svm.libsvm.predict()
```

Predict target values of X given a model (low-level method)

### **Parameters**

**X** [array-like, dtype=float, size=[n\_samples, n\_features]]

svm\_type [{0, 1, 2, 3, 4}] Type of SVM: C SVC, nu SVC, one class, epsilon SVR, nu SVR

**kernel** [{'linear', 'rbf', 'poly', 'sigmoid', 'precomputed'}] Type of kernel.

**degree** [int] Degree of the polynomial kernel.

**gamma** [float] Gamma parameter in rbf, poly and sigmoid kernels. Ignored by other kernels. 0.1 by default.

**coef0** [float] Independent parameter in poly/sigmoid kernel.

## Returns

dec\_values [array] predicted values.

### sklearn.svm.libsvm.predict proba

```
sklearn.svm.libsvm.predict_proba()
```

Predict probabilities

svm\_model stores all parameters needed to predict a given value.

For speed, all real work is done at the C level in function copy\_predict (libsvm\_helper.c).

We have to reconstruct model and parameters to make sure we stay in sync with the python object.

See sklearn.svm.predict for a complete list of parameters.

#### **Parameters**

```
X [array-like, dtype=float]
kernel [{'linear', 'rbf', 'poly', 'sigmoid', 'precomputed'}]
```

### Returns

dec\_values [array] predicted values.

## 6.38 sklearn tree: Decision Trees

The sklearn.tree module includes decision tree-based models for classification and regression.

User guide: See the *Decision Trees* section for further details.

tree.DecisionTreeClassifier([criterion,])	A decision tree classifier.
tree.DecisionTreeRegressor([criterion,])	A decision tree regressor.
tree.ExtraTreeClassifier([criterion,])	An extremely randomized tree classifier.
<pre>tree.ExtraTreeRegressor([criterion,])</pre>	An extremely randomized tree regressor.

## 6.38.1 sklearn.tree.DecisionTreeClassifier

A decision tree classifier.

Read more in the User Guide.

## **Parameters**

**criterion** [string, optional (default="gini")] The function to measure the quality of a split. Supported criteria are "gini" for the Gini impurity and "entropy" for the information gain.

**splitter** [string, optional (default="best")] The strategy used to choose the split at each node. Supported strategies are "best" to choose the best split and "random" to choose the best random split.

max\_depth [int or None, optional (default=None)] The maximum depth of the tree. If None,

then nodes are expanded until all leaves are pure or until all leaves contain less than min\_samples\_split samples.

min\_samples\_split [int, float, optional (default=2)] The minimum number of samples required to split an internal node:

- If int, then consider min samples split as the minimum number.
- If float, then min\_samples\_split is a fraction and ceil (min\_samples\_split \* n\_samples) are the minimum number of samples for each split.

Changed in version 0.18: Added float values for fractions.

- min\_samples\_leaf [int, float, optional (default=1)] The minimum number of samples required to be at a leaf node. A split point at any depth will only be considered if it leaves at least min\_samples\_leaf training samples in each of the left and right branches. This may have the effect of smoothing the model, especially in regression.
  - If int, then consider min\_samples\_leaf as the minimum number.
  - If float, then min\_samples\_leaf is a fraction and ceil (min\_samples\_leaf \* n\_samples) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for fractions.

- min\_weight\_fraction\_leaf [float, optional (default=0.)] The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample\_weight is not provided.
- max\_features [int, float, string or None, optional (default=None)] The number of features to consider when looking for the best split:
  - If int, then consider max\_features features at each split.
  - If float, then max\_features is a fraction and int(max\_features \* n\_features) features are considered at each split.
  - If "auto", then max\_features=sqrt (n\_features).
  - If "sqrt", then max\_features=sqrt (n\_features).
  - If "log2", then max\_features=log2 (n\_features).
  - If None, then max\_features=n\_features.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than max\_features features.

- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- max\_leaf\_nodes [int or None, optional (default=None)] Grow a tree with max\_leaf\_nodes in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.
- **min\_impurity\_decrease** [float, optional (default=0.)] A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

where N is the total number of samples, N\_t is the number of samples at the current node, N\_t\_L is the number of samples in the left child, and N\_t\_R is the number of samples in the right child.

 $N, N_t, N_t = R$  and  $N_t = L$  all refer to the weighted sum, if sample\_weight is passed.

New in version 0.19.

**min\_impurity\_split** [float, (default=1e-7)] Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: min\_impurity\_split has been deprecated in favor of min\_impurity\_decrease in 0.19. The default value of min\_impurity\_split will change from 1e-7 to 0 in 0.23 and it will be removed in 0.25. Use min\_impurity\_decrease instead.

class\_weight [dict, list of dicts, "balanced" or None, default=None] Weights associated with
 classes in the form {class\_label: weight}. If not given, all classes are supposed
 to have weight one. For multi-output problems, a list of dicts can be provided in the same
 order as the columns of y.

Note that for multioutput (including multilabel) weights should be defined for each class of every column in its own dict. For example, for four-class multilabel classification weights should be [{0: 1, 1: 1}, {0: 1, 1: 5}, {0: 1, 1: 1}, {0: 1, 1: 1}] instead of [{1:1}, {2:5}, {3:1}, {4:1}].

The "balanced" mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as  $n_samples / (n_classes * np. bincount(y))$ 

For multi-output, the weights of each column of y will be multiplied.

Note that these weights will be multiplied with sample\_weight (passed through the fit method) if sample\_weight is specified.

**presort** [bool, optional (default=False)] Whether to presort the data to speed up the finding of best splits in fitting. For the default settings of a decision tree on large datasets, setting this to true may slow down the training process. When using either a smaller dataset or a restricted depth, this may speed up the training.

## Attributes

**classes**\_ [array of shape = [n\_classes] or a list of such arrays] The classes labels (single output problem), or a list of arrays of class labels (multi-output problem).

**feature\_importances\_** [array of shape = [n\_features]] Return the feature importances.

max features [int,] The inferred value of max features.

**n\_classes**\_ [int or list] The number of classes (for single output problems), or a list containing the number of classes for each output (for multi-output problems).

 $n\_features\_$  [int] The number of features when fit is performed.

**n\_outputs\_** [int] The number of outputs when fit is performed.

tree\_ [Tree object] The underlying Tree object. Please refer to help(sklearn.tree.
 \_tree.Tree) for attributes of Tree object and Understanding the decision tree structure
for basic usage of these attributes.

## See also:

DecisionTreeRegressor

#### **Notes**

The default values for the parameters controlling the size of the trees (e.g. max\_depth, min\_samples\_leaf, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

The features are always randomly permuted at each split. Therefore, the best found split may vary, even with the same training data and max\_features=n\_features, if the improvement of the criterion is identical for several splits enumerated during the search of the best split. To obtain a deterministic behaviour during fitting, random\_state has to be fixed.

#### References

[Rb1ec977cd307-1], [Rb1ec977cd307-2], [Rb1ec977cd307-3], [Rb1ec977cd307-4]

### **Examples**

### **Methods**

apply(self, X[, check_input])	Returns the index of the leaf that each sample is pre-
	dicted as.
<pre>decision_path(self, X[, check_input])</pre>	Return the decision path in the tree
$fit(self, X, y[, sample\_weight,])$	Build a decision tree classifier from the training set (X,
	y).
get_depth(self)	Returns the depth of the decision tree.
get_n_leaves(self)	Returns the number of leaves of the decision tree.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, check_input])</pre>	Predict class or regression value for X.
predict_log_proba(self, X)	Predict class log-probabilities of the input samples X.
<pre>predict_proba(self, X[, check_input])</pre>	Predict class probabilities of the input samples X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init___(self, criterion='gini', splitter='best', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features=None, random_state=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, class_weight=None, presort=False)
```

### apply (self, X, check\_input=True)

Returns the index of the leaf that each sample is predicted as.

New in version 0.17.

#### **Parameters**

X [array\_like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

#### **Returns**

X\_leaves [array\_like, shape = [n\_samples,]] For each datapoint x in X, return the index of
 the leaf x ends up in. Leaves are numbered within [0; self.tree\_.node\_count),
 possibly with gaps in the numbering.

# decision\_path (self, X, check\_input=True)

Return the decision path in the tree

New in version 0.18.

#### **Parameters**

X [array\_like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

### Returns

**indicator** [sparse csr array, shape = [n\_samples, n\_nodes]] Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

#### feature\_importances\_

Return the feature importances.

The importance of a feature is computed as the (normalized) total reduction of the criterion brought by that feature. It is also known as the Gini importance.

#### Returns

**feature\_importances\_** [array, shape = [n\_features]]

**fit** (self, X, y,  $sample\_weight=None$ ,  $check\_input=True$ ,  $X\_idx\_sorted=None$ ) Build a decision tree classifier from the training set (X, y).

#### **Parameters**

- X [array-like or sparse matrix, shape = [n\_samples, n\_features]] The training input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csc\_matrix.
- **y** [array-like, shape = [n\_samples] or [n\_samples, n\_outputs]] The target values (class labels) as integers or strings.
- **sample\_weight** [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. Splits are also ignored if they would result in any single class carrying a negative weight in either child node.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

**X\_idx\_sorted** [array-like, shape = [n\_samples, n\_features], optional] The indexes of the sorted training input samples. If many tree are grown on the same dataset, this allows the ordering to be cached between trees. If None, the data will be sorted here. Don't use this parameter unless you know what to do.

#### Returns

self [object]

### get\_depth (self)

Returns the depth of the decision tree.

The depth of a tree is the maximum distance between the root and any leaf.

#### get\_n\_leaves (self)

Returns the number of leaves of the decision tree.

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## predict (self, X, check\_input=True)

Predict class or regression value for X.

For a classification model, the predicted class for each sample in X is returned. For a regression model, the predicted value based on X is returned.

#### **Parameters**

X [array-like or sparse matrix of shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

#### Returns

**y** [array of shape = [n\_samples] or [n\_samples, n\_outputs]] The predicted classes, or the predict values.

# predict\_log\_proba (self, X)

Predict class log-probabilities of the input samples X.

#### **Parameters**

X [array-like or sparse matrix of shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

## Returns

p [array of shape = [n\_samples, n\_classes], or a list of n\_outputs] such arrays if n\_outputs
 > 1. The class log-probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes*.

## predict\_proba (self, X, check\_input=True)

Predict class probabilities of the input samples X.

The predicted class probability is the fraction of samples of the same class in a leaf.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

#### **Parameters**

X [array-like or sparse matrix of shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

check\_input [bool] Run check\_array on X.

#### Returns

p [array of shape = [n\_samples, n\_classes], or a list of n\_outputs] such arrays if n\_outputs
 > 1. The class probabilities of the input samples. The order of the classes corresponds to that in the attribute classes\_.

### score (self, X, y, sample\_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

### **Parameters**

```
\mathbf{X} [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape =  $(n_samples)$  or  $(n_samples, n_outputs)$ ] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

## Examples using sklearn.tree.DecisionTreeClassifier

- Classifier comparison
- Plot the decision boundaries of a VotingClassifier
- Two-class AdaBoost
- Multi-class AdaBoosted Decision Trees

- Discrete versus Real AdaBoost
- Plot the decision surfaces of ensembles of trees on the iris dataset
- Demonstration of multi-metric evaluation on cross\_val\_score and GridSearchCV
- Plot the decision surface of a decision tree on the iris dataset
- Understanding the decision tree structure

# 6.38.2 sklearn.tree.DecisionTreeRegressor

A decision tree regressor.

Read more in the User Guide.

#### **Parameters**

**criterion** [string, optional (default="mse")] The function to measure the quality of a split. Supported criteria are "mse" for the mean squared error, which is equal to variance reduction as feature selection criterion and minimizes the L2 loss using the mean of each terminal node, "friedman\_mse", which uses mean squared error with Friedman's improvement score for potential splits, and "mae" for the mean absolute error, which minimizes the L1 loss using the median of each terminal node.

New in version 0.18: Mean Absolute Error (MAE) criterion.

- **splitter** [string, optional (default="best")] The strategy used to choose the split at each node. Supported strategies are "best" to choose the best split and "random" to choose the best random split.
- **max\_depth** [int or None, optional (default=None)] The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than min samples split samples.
- min\_samples\_split [int, float, optional (default=2)] The minimum number of samples required to split an internal node:
  - If int, then consider min\_samples\_split as the minimum number.
  - If float, then min\_samples\_split is a fraction and ceil (min\_samples\_split
     \* n\_samples) are the minimum number of samples for each split.

Changed in version 0.18: Added float values for fractions.

- min\_samples\_leaf [int, float, optional (default=1)] The minimum number of samples required to be at a leaf node. A split point at any depth will only be considered if it leaves at least min\_samples\_leaf training samples in each of the left and right branches. This may have the effect of smoothing the model, especially in regression.
  - If int, then consider min\_samples\_leaf as the minimum number.
  - If float, then min\_samples\_leaf is a fraction and ceil (min\_samples\_leaf \* n\_samples) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for fractions.

- min\_weight\_fraction\_leaf [float, optional (default=0.)] The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample weight is not provided.
- **max\_features** [int, float, string or None, optional (default=None)] The number of features to consider when looking for the best split:
  - If int, then consider max features features at each split.
  - If float, then max\_features is a fraction and int(max\_features \* n\_features) features are considered at each split.
  - If "auto", then max\_features=n\_features.
  - If "sqrt", then max\_features=sqrt (n\_features).
  - If "log2", then max\_features=log2 (n\_features).
  - If None, then max\_features=n\_features.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than max\_features features.

- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- max\_leaf\_nodes [int or None, optional (default=None)] Grow a tree with max\_leaf\_nodes in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.
- **min\_impurity\_decrease** [float, optional (default=0.)] A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

```
N_t / N * (impurity - N_t_R / N_t * right_impurity - N_t_L / N_t * left_impurity)
```

where N is the total number of samples,  $N_t$  is the number of samples at the current node,  $N_t$  is the number of samples in the left child, and  $N_t$  is the number of samples in the right child.

N, N\_t, N\_t\_R and N\_t\_L all refer to the weighted sum, if sample\_weight is passed. New in version 0.19.

min\_impurity\_split [float, (default=1e-7)] Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: min\_impurity\_split has been deprecated in favor of min\_impurity\_decrease in 0.19. The default value of min\_impurity\_split will change from 1e-7 to 0 in 0.23 and it will be removed in 0.25. Use min\_impurity\_decrease instead.

presort [bool, optional (default=False)] Whether to presort the data to speed up the finding of best splits in fitting. For the default settings of a decision tree on large datasets, setting this to true may slow down the training process. When using either a smaller dataset or a restricted depth, this may speed up the training.

## Attributes

**feature\_importances\_** [array of shape = [n\_features]] Return the feature importances.

```
max_features_ [int,] The inferred value of max_features.
```

**n\_features\_** [int] The number of features when fit is performed.

**n\_outputs\_** [int] The number of outputs when fit is performed.

tree\_ [Tree object] The underlying Tree object. Please refer to help(sklearn.tree.
 \_tree.Tree) for attributes of Tree object and Understanding the decision tree structure
for basic usage of these attributes.

#### See also:

**DecisionTreeClassifier** 

#### **Notes**

The default values for the parameters controlling the size of the trees (e.g. max\_depth, min\_samples\_leaf, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

The features are always randomly permuted at each split. Therefore, the best found split may vary, even with the same training data and max\_features=n\_features, if the improvement of the criterion is identical for several splits enumerated during the search of the best split. To obtain a deterministic behaviour during fitting, random state has to be fixed.

#### References

[Ra37b7e3adb19-1], [Ra37b7e3adb19-2], [Ra37b7e3adb19-3], [Ra37b7e3adb19-4]

## **Examples**

## **Methods**

apply(self, X[, check_input])	Returns the index of the leaf that each sample is pre-
	dicted as.
<pre>decision_path(self, X[, check_input])</pre>	Return the decision path in the tree
$fit(self, X, y[, sample\_weight,])$	Build a decision tree regressor from the training set (X,
	y).
get_depth(self)	Returns the depth of the decision tree.

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get_n_leaves(self)	Returns the number of leaves of the decision tree.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, check_input])</pre>	Predict class or regression value for X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

\_\_init\_\_ (self, criterion='mse', splitter='best', max\_depth=None, min\_samples\_split=2, min\_samples\_leaf=1, min\_weight\_fraction\_leaf=0.0, max\_features=None, random\_state=None, max\_leaf\_nodes=None, min\_impurity\_decrease=0.0, min\_impurity\_split=None, presort=False)

## apply (self, X, check\_input=True)

Returns the index of the leaf that each sample is predicted as.

New in version 0.17.

### **Parameters**

X [array\_like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

#### Returns

**X\_leaves** [array\_like, shape = [n\_samples,]] For each datapoint x in X, return the index of the leaf x ends up in. Leaves are numbered within [0; self.tree\_.node\_count), possibly with gaps in the numbering.

## decision\_path(self, X, check\_input=True)

Return the decision path in the tree

New in version 0.18.

## **Parameters**

X [array\_like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

## Returns

**indicator** [sparse csr array, shape = [n\_samples, n\_nodes]] Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

#### feature\_importances\_

Return the feature importances.

The importance of a feature is computed as the (normalized) total reduction of the criterion brought by that feature. It is also known as the Gini importance.

### Returns

**feature\_importances**\_ [array, shape = [n\_features]]

**fit** (*self*, *X*, *y*, *sample\_weight=None*, *check\_input=True*, *X\_idx\_sorted=None*) Build a decision tree regressor from the training set (X, y).

#### **Parameters**

- X [array-like or sparse matrix, shape = [n\_samples, n\_features]] The training input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csc\_matrix.
- y [array-like, shape = [n\_samples] or [n\_samples, n\_outputs]] The target values (real numbers). Use dtype=np.float64 and order='C' for maximum efficiency.
- **sample\_weight** [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node.
- **check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.
- **X\_idx\_sorted** [array-like, shape = [n\_samples, n\_features], optional] The indexes of the sorted training input samples. If many tree are grown on the same dataset, this allows the ordering to be cached between trees. If None, the data will be sorted here. Don't use this parameter unless you know what to do.

#### Returns

self [object]

### get\_depth (self)

Returns the depth of the decision tree.

The depth of a tree is the maximum distance between the root and any leaf.

### get\_n\_leaves (self)

Returns the number of leaves of the decision tree.

## get\_params (self, deep=True)

Get parameters for this estimator.

### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

```
predict (self, X, check input=True)
```

Predict class or regression value for X.

For a classification model, the predicted class for each sample in X is returned. For a regression model, the predicted value based on X is returned.

#### **Parameters**

- X [array-like or sparse matrix of shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.
- **check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

#### Returns

y [array of shape = [n\_samples] or [n\_samples, n\_outputs]] The predicted classes, or the predict values.

### score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

#### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

## Examples using sklearn.tree.DecisionTreeRegressor

- Decision Tree Regression with AdaBoost
- Single estimator versus bagging: bias-variance decomposition
- Imputing missing values with variants of IterativeImputer
- Using KBinsDiscretizer to discretize continuous features
- Decision Tree Regression
- Multi-output Decision Tree Regression

## 6.38.3 sklearn.tree.ExtraTreeClassifier

An extremely randomized tree classifier.

Extra-trees differ from classic decision trees in the way they are built. When looking for the best split to separate the samples of a node into two groups, random splits are drawn for each of the max\_features randomly selected features and the best split among those is chosen. When max\_features is set 1, this amounts to building a totally random decision tree.

Warning: Extra-trees should only be used within ensemble methods.

Read more in the *User Guide*.

### **Parameters**

- **criterion** [string, optional (default="gini")] The function to measure the quality of a split. Supported criteria are "gini" for the Gini impurity and "entropy" for the information gain.
- **splitter** [string, optional (default="random")] The strategy used to choose the split at each node. Supported strategies are "best" to choose the best split and "random" to choose the best random split.
- max\_depth [int or None, optional (default=None)] The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than min\_samples\_split samples.
- min\_samples\_split [int, float, optional (default=2)] The minimum number of samples required to split an internal node:
  - If int, then consider min\_samples\_split as the minimum number.
  - If float, then min\_samples\_split is a fraction and ceil (min\_samples\_split
     \* n\_samples) are the minimum number of samples for each split.

Changed in version 0.18: Added float values for fractions.

- min\_samples\_leaf [int, float, optional (default=1)] The minimum number of samples required to be at a leaf node. A split point at any depth will only be considered if it leaves at least min\_samples\_leaf training samples in each of the left and right branches. This may have the effect of smoothing the model, especially in regression.
  - If int, then consider min\_samples\_leaf as the minimum number.
  - If float, then min\_samples\_leaf is a fraction and ceil (min\_samples\_leaf \* n\_samples) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for fractions.

- min\_weight\_fraction\_leaf [float, optional (default=0.)] The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample\_weight is not provided.
- max\_features [int, float, string or None, optional (default="auto")] The number of features to consider when looking for the best split:
  - If int, then consider max\_features features at each split.

- If float, then max\_features is a fraction and int(max\_features \* n\_features) features are considered at each split.
- If "auto", then max\_features=sqrt (n\_features).
- If "sqrt", then max features=sqrt (n features).
- If "log2", then max features=log2 (n features).
- If None, then max features=n features.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than max\_features features.

- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- max\_leaf\_nodes [int or None, optional (default=None)] Grow a tree with max\_leaf\_nodes in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.
- min\_impurity\_decrease [float, optional (default=0.)] A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

where N is the total number of samples,  $N_t$  is the number of samples at the current node,  $N_t L$  is the number of samples in the left child, and  $N_t L$  is the number of samples in the right child.

N, N\_t, N\_t\_R and N\_t\_L all refer to the weighted sum, if sample\_weight is passed. New in version 0.19.

**min\_impurity\_split** [float, (default=1e-7)] Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: min\_impurity\_split has been deprecated in favor of min\_impurity\_decrease in 0.19. The default value of min\_impurity\_split will change from 1e-7 to 0 in 0.23 and it will be removed in 0.25. Use min\_impurity\_decrease instead.

class\_weight [dict, list of dicts, "balanced" or None, default=None] Weights associated with
 classes in the form {class\_label: weight}. If not given, all classes are supposed
 to have weight one. For multi-output problems, a list of dicts can be provided in the same
 order as the columns of y.

Note that for multioutput (including multilabel) weights should be defined for each class of every column in its own dict. For example, for four-class multilabel classification weights should be [{0: 1, 1: 1}, {0: 1, 1: 5}, {0: 1, 1: 1}, {0: 1, 1: 1}] instead of [{1:1}, {2:5}, {3:1}, {4:1}].

The "balanced" mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as n\_samples / (n\_classes \* np. bincount(y))

For multi-output, the weights of each column of y will be multiplied.

Note that these weights will be multiplied with sample\_weight (passed through the fit method) if sample\_weight is specified.

#### Attributes

feature\_importances\_ Return the feature importances.

#### See also:

 $\label{lem:extraTreeRegressor} ExtraTreeRegressor, sklearn.ensemble.ExtraTreesClassifier sklearn.ensemble.ExtraTreesRegressor$ 

#### **Notes**

The default values for the parameters controlling the size of the trees (e.g. max\_depth, min\_samples\_leaf, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

### References

[Rdd99a0224c6e-1]

### **Methods**

apply(self, X[, check_input])	Returns the index of the leaf that each sample is pre-
	dicted as.
<pre>decision_path(self, X[, check_input])</pre>	Return the decision path in the tree
fit(self, X, y[, sample_weight,])	Build a decision tree classifier from the training set (X,
	y).
get_depth(self)	Returns the depth of the decision tree.
get_n_leaves(self)	Returns the number of leaves of the decision tree.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, check_input])</pre>	Predict class or regression value for X.
predict_log_proba(self, X)	Predict class log-probabilities of the input samples X.
<pre>predict_proba(self, X[, check_input])</pre>	Predict class probabilities of the input samples X.
score(self, X, y[, sample_weight])	Returns the mean accuracy on the given test data and
	labels.
set_params(self, \*\*params)	Set the parameters of this estimator.

```
__init__ (self, criterion='gini', splitter='random', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', random_state=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, class_weight=None)
```

apply (self, X, check\_input=True)

Returns the index of the leaf that each sample is predicted as.

New in version 0.17.

#### **Parameters**

X [array\_like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Inter-

nally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

### Returns

X\_leaves [array\_like, shape = [n\_samples,]] For each datapoint x in X, return the index of
 the leaf x ends up in. Leaves are numbered within [0; self.tree\_.node\_count),
 possibly with gaps in the numbering.

### decision\_path (self, X, check\_input=True)

Return the decision path in the tree

New in version 0.18.

#### **Parameters**

X [array\_like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

#### Returns

**indicator** [sparse csr array, shape = [n\_samples, n\_nodes]] Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

### feature\_importances\_

Return the feature importances.

The importance of a feature is computed as the (normalized) total reduction of the criterion brought by that feature. It is also known as the Gini importance.

#### Returns

**feature\_importances**\_ [array, shape = [n\_features]]

**fit** (*self*, *X*, *y*, *sample\_weight=None*, *check\_input=True*, *X\_idx\_sorted=None*) Build a decision tree classifier from the training set (X, y).

### **Parameters**

- X [array-like or sparse matrix, shape = [n\_samples, n\_features]] The training input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csc matrix.
- **y** [array-like, shape = [n\_samples] or [n\_samples, n\_outputs]] The target values (class labels) as integers or strings.
- **sample\_weight** [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. Splits are also ignored if they would result in any single class carrying a negative weight in either child node.
- **check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.
- **X\_idx\_sorted** [array-like, shape = [n\_samples, n\_features], optional] The indexes of the sorted training input samples. If many tree are grown on the same dataset, this allows the

ordering to be cached between trees. If None, the data will be sorted here. Don't use this parameter unless you know what to do.

#### Returns

self [object]

#### get\_depth (self)

Returns the depth of the decision tree.

The depth of a tree is the maximum distance between the root and any leaf.

#### get\_n\_leaves (self)

Returns the number of leaves of the decision tree.

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

params [mapping of string to any] Parameter names mapped to their values.

### predict (self, X, check\_input=True)

Predict class or regression value for X.

For a classification model, the predicted class for each sample in X is returned. For a regression model, the predicted value based on X is returned.

#### **Parameters**

X [array-like or sparse matrix of shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

### Returns

**y** [array of shape = [n\_samples] or [n\_samples, n\_outputs]] The predicted classes, or the predict values.

# $predict_log_proba(self, X)$

Predict class log-probabilities of the input samples X.

### **Parameters**

X [array-like or sparse matrix of shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

#### **Returns**

p [array of shape = [n\_samples, n\_classes], or a list of n\_outputs] such arrays if n\_outputs
 > 1. The class log-probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes*\_.

### predict\_proba (self, X, check\_input=True)

Predict class probabilities of the input samples X.

The predicted class probability is the fraction of samples of the same class in a leaf.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

#### **Parameters**

X [array-like or sparse matrix of shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

check input [bool] Run check array on X.

#### **Returns**

p [array of shape = [n\_samples, n\_classes], or a list of n\_outputs] such arrays if n\_outputs
 > 1. The class probabilities of the input samples. The order of the classes corresponds to that in the attribute *classes*\_.

```
score (self, X, y, sample_weight=None)
```

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

#### **Parameters**

```
X [array-like, shape = (n_samples, n_features)] Test samples.
```

y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True labels for X.

**sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] Mean accuracy of self.predict(X) wrt. y.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

# 6.38.4 sklearn.tree.ExtraTreeRegressor

An extremely randomized tree regressor.

Extra-trees differ from classic decision trees in the way they are built. When looking for the best split to separate the samples of a node into two groups, random splits are drawn for each of the max\_features randomly selected features and the best split among those is chosen. When max\_features is set 1, this amounts to building a totally random decision tree.

Warning: Extra-trees should only be used within ensemble methods.

Read more in the *User Guide*.

#### **Parameters**

**criterion** [string, optional (default="mse")] The function to measure the quality of a split. Supported criteria are "mse" for the mean squared error, which is equal to variance reduction as feature selection criterion, and "mae" for the mean absolute error.

New in version 0.18: Mean Absolute Error (MAE) criterion.

- **splitter** [string, optional (default="random")] The strategy used to choose the split at each node. Supported strategies are "best" to choose the best split and "random" to choose the best random split.
- **max\_depth** [int or None, optional (default=None)] The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than min\_samples\_split samples.
- min\_samples\_split [int, float, optional (default=2)] The minimum number of samples required to split an internal node:
  - If int, then consider min\_samples\_split as the minimum number.
  - If float, then min\_samples\_split is a fraction and ceil (min\_samples\_split
     \* n\_samples) are the minimum number of samples for each split.

Changed in version 0.18: Added float values for fractions.

- min\_samples\_leaf [int, float, optional (default=1)] The minimum number of samples required to be at a leaf node. A split point at any depth will only be considered if it leaves at least min\_samples\_leaf training samples in each of the left and right branches. This may have the effect of smoothing the model, especially in regression.
  - If int, then consider min\_samples\_leaf as the minimum number.
  - If float, then min\_samples\_leaf is a fraction and ceil (min\_samples\_leaf \* n\_samples) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for fractions.

- min\_weight\_fraction\_leaf [float, optional (default=0.)] The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample\_weight is not provided.
- max\_features [int, float, string or None, optional (default="auto")] The number of features to consider when looking for the best split:
  - If int, then consider max\_features features at each split.
  - If float, then max\_features is a fraction and int(max\_features \* n\_features) features are considered at each split.
  - If "auto", then max\_features=n\_features.
  - If "sqrt", then max\_features=sqrt (n\_features).
  - If "log2", then max\_features=log2 (n\_features).
  - If None, then max\_features=n\_features.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than max\_features features.

**random\_state** [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance,

random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**min\_impurity\_decrease** [float, optional (default=0.)] A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

```
N_t / N * (impurity - N_t_R / N_t * right_impurity - N_t_L / N_t * left_impurity)
```

where N is the total number of samples, N\_t is the number of samples at the current node, N\_t\_L is the number of samples in the left child, and N\_t\_R is the number of samples in the right child.

N, N\_t, N\_t\_R and N\_t\_L all refer to the weighted sum, if sample\_weight is passed. New in version 0.19.

**min\_impurity\_split** [float, (default=1e-7)] Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: min\_impurity\_split has been deprecated in favor of min\_impurity\_decrease in 0.19. The default value of min\_impurity\_split will change from 1e-7 to 0 in 0.23 and it will be removed in 0.25. Use min\_impurity\_decrease instead.

max\_leaf\_nodes [int or None, optional (default=None)] Grow a tree with max\_leaf\_nodes in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

#### Attributes

feature\_importances\_ Return the feature importances.

### See also:

```
ExtraTreeClassifier, sklearn.ensemble.ExtraTreesClassifier sklearn.ensemble.ExtraTreesRegressor
```

## **Notes**

The default values for the parameters controlling the size of the trees (e.g. max\_depth, min\_samples\_leaf, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

### References

[R4939d63d5a49-1]

### **Methods**

apply(self, X[, check_input])	Returns the index of the leaf that each sample is pre-
	dicted as.
<pre>decision_path(self, X[, check_input])</pre>	Return the decision path in the tree
$fit(self, X, y[, sample\_weight,])$	Build a decision tree regressor from the training set (X,
	y).
get_depth(self)	Returns the depth of the decision tree.
get_n_leaves(self)	Returns the number of leaves of the decision tree.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>predict(self, X[, check_input])</pre>	Predict class or regression value for X.
score(self, X, y[, sample_weight])	Returns the coefficient of determination R^2 of the pre-
	diction.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.

## apply (self, X, check\_input=True)

Returns the index of the leaf that each sample is predicted as.

New in version 0.17.

### **Parameters**

X [array\_like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

## Returns

X\_leaves [array\_like, shape = [n\_samples,]] For each datapoint x in X, return the index of
 the leaf x ends up in. Leaves are numbered within [0; self.tree\_.node\_count),
 possibly with gaps in the numbering.

#### decision path(self, X, check input=True)

Return the decision path in the tree

New in version 0.18.

### **Parameters**

X [array\_like or sparse matrix, shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

### Returns

**indicator** [sparse csr array, shape = [n\_samples, n\_nodes]] Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

### feature importances

Return the feature importances.

The importance of a feature is computed as the (normalized) total reduction of the criterion brought by that feature. It is also known as the Gini importance.

#### Returns

**feature\_importances**\_ [array, shape = [n\_features]]

**fit** (*self*, *X*, *y*, *sample\_weight=None*, *check\_input=True*, *X\_idx\_sorted=None*) Build a decision tree regressor from the training set (X, y).

#### **Parameters**

- X [array-like or sparse matrix, shape = [n\_samples, n\_features]] The training input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csc\_matrix.
- y [array-like, shape = [n\_samples] or [n\_samples, n\_outputs]] The target values (real numbers). Use dtype=np.float64 and order='C' for maximum efficiency.
- **sample\_weight** [array-like, shape = [n\_samples] or None] Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node.
- **check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.
- **X\_idx\_sorted** [array-like, shape = [n\_samples, n\_features], optional] The indexes of the sorted training input samples. If many tree are grown on the same dataset, this allows the ordering to be cached between trees. If None, the data will be sorted here. Don't use this parameter unless you know what to do.

#### **Returns**

self [object]

## get\_depth (self)

Returns the depth of the decision tree.

The depth of a tree is the maximum distance between the root and any leaf.

### get\_n\_leaves (self)

Returns the number of leaves of the decision tree.

### get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

### Returns

params [mapping of string to any] Parameter names mapped to their values.

### predict (self, X, check\_input=True)

Predict class or regression value for X.

For a classification model, the predicted class for each sample in X is returned. For a regression model, the predicted value based on X is returned.

### **Parameters**

X [array-like or sparse matrix of shape = [n\_samples, n\_features]] The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr\_matrix.

**check\_input** [boolean, (default=True)] Allow to bypass several input checking. Don't use this parameter unless you know what you do.

#### Returns

y [array of shape = [n\_samples] or [n\_samples, n\_outputs]] The predicted classes, or the predict values.

## score (self, X, y, sample\_weight=None)

Returns the coefficient of determination R<sup>2</sup> of the prediction.

The coefficient R<sup>2</sup> is defined as (1 - u/v), where u is the residual sum of squares ((y\_true - y\_pred) \*\* 2).sum() and v is the total sum of squares ((y\_true - y\_true.mean()) \*\* 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R<sup>2</sup> score of 0.0.

#### **Parameters**

- **X** [array-like, shape = (n\_samples, n\_features)] Test samples. For some estimators this may be a precomputed kernel matrix instead, shape = (n\_samples, n\_samples\_fitted], where n\_samples\_fitted is the number of samples used in the fitting for the estimator.
- y [array-like, shape = (n\_samples) or (n\_samples, n\_outputs)] True values for X.
- **sample\_weight** [array-like, shape = [n\_samples], optional] Sample weights.

#### Returns

**score** [float] R^2 of self.predict(X) wrt. y.

#### **Notes**

The R2 score used when calling score on a regressor will use multioutput='uniform\_average' from version 0.23 to keep consistent with metrics.r2\_score. This will influence the score method of all the multioutput regressors (except for multioutput.MultiOutputRegressor). To specify the default value manually and avoid the warning, please either call metrics.r2\_score directly or make a custom scorer with metrics.make\_scorer (the built-in scorer 'r2' uses multioutput='uniform\_average').

### set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

### Returns

self

tree.export_graphviz(decision_tree[,])	Export a decision tree in DOT format.
tree.plot_tree(decision_tree[, max_depth,])	Plot a decision tree.
tree.export_text(decision_tree[,])	Build a text report showing the rules of a decision tree.

## 6.38.5 sklearn.tree.export graphviz

```
sklearn.tree.export_graphviz (decision_tree, out_file=None, max_depth=None, fea-
ture_names=None, class_names=None, label='all', filled=False,
leaves_parallel=False, impurity=True, node_ids=False,
proportion=False, rotate=False, rounded=False, spe-
cial_characters=False, precision=3)
```

Export a decision tree in DOT format.

This function generates a GraphViz representation of the decision tree, which is then written into out\_file. Once exported, graphical renderings can be generated using, for example:

```
$ dot -Tps tree.dot -o tree.ps (PostScript format)
$ dot -Tpng tree.dot -o tree.png (PNG format)
```

The sample counts that are shown are weighted with any sample\_weights that might be present.

Read more in the User Guide.

#### **Parameters**

**decision\_tree** [decision tree classifier] The decision tree to be exported to GraphViz.

**out\_file** [file object or string, optional (default=None)] Handle or name of the output file. If None, the result is returned as a string.

Changed in version 0.20: Default of out\_file changed from "tree.dot" to None.

**max\_depth** [int, optional (default=None)] The maximum depth of the representation. If None, the tree is fully generated.

**feature\_names** [list of strings, optional (default=None)] Names of each of the features.

class\_names [list of strings, bool or None, optional (default=None)] Names of each of the target classes in ascending numerical order. Only relevant for classification and not supported for multi-output. If True, shows a symbolic representation of the class name.

**label** [{'all', 'root', 'none'}, optional (default='all')] Whether to show informative labels for impurity, etc. Options include 'all' to show at every node, 'root' to show only at the top root node, or 'none' to not show at any node.

**filled** [bool, optional (default=False)] When set to True, paint nodes to indicate majority class for classification, extremity of values for regression, or purity of node for multi-output.

**leaves\_parallel** [bool, optional (default=False)] When set to True, draw all leaf nodes at the bottom of the tree.

**impurity** [bool, optional (default=True)] When set to True, show the impurity at each node.

**node\_ids** [bool, optional (default=False)] When set to True, show the ID number on each node.

**proportion** [bool, optional (default=False)] When set to True, change the display of 'values' and/or 'samples' to be proportions and percentages respectively.

**rotate** [bool, optional (default=False)] When set to True, orient tree left to right rather than top-down.

**rounded** [bool, optional (default=False)] When set to True, draw node boxes with rounded corners and use Helvetica fonts instead of Times-Roman.

**special\_characters** [bool, optional (default=False)] When set to False, ignore special characters for PostScript compatibility.

**precision** [int, optional (default=3)] Number of digits of precision for floating point in the values of impurity, threshold and value attributes of each node.

#### Returns

**dot\_data** [string] String representation of the input tree in GraphViz dot format. Only returned if out\_file is None.

New in version 0.18.

## **Examples**

```
>>> from sklearn.datasets import load_iris
>>> from sklearn import tree

>>> clf = tree.DecisionTreeClassifier()
>>> iris = load_iris()

>>> clf = clf.fit(iris.data, iris.target)
>>> tree.export_graphviz(clf)
```

# 6.38.6 sklearn.tree.plot\_tree

'digraph Tree {...

```
sklearn.tree.plot_tree (decision_tree, max_depth=None, feature_names=None, class_names=None, label='all', filled=False, impurity=True, node_ids=False, proportion=False, rotate=False, rounded=False, precision=3, ax=None, font-size=None)
```

Plot a decision tree.

The sample counts that are shown are weighted with any sample\_weights that might be present. This function requires matplotlib, and works best with matplotlib  $\geq 1.5$ .

The visualization is fit automatically to the size of the axis. Use the figsize or dpi arguments of plt. figure to control the size of the rendering.

Read more in the *User Guide*.

New in version 0.21.

### **Parameters**

**decision\_tree** [decision tree regressor or classifier] The decision tree to be exported to GraphViz.

**max\_depth** [int, optional (default=None)] The maximum depth of the representation. If None, the tree is fully generated.

**feature\_names** [list of strings, optional (default=None)] Names of each of the features.

class\_names [list of strings, bool or None, optional (default=None)] Names of each of the target classes in ascending numerical order. Only relevant for classification and not supported for multi-output. If True, shows a symbolic representation of the class name.

**label** [{'all', 'root', 'none'}, optional (default='all')] Whether to show informative labels for impurity, etc. Options include 'all' to show at every node, 'root' to show only at the top root node, or 'none' to not show at any node.

**filled** [bool, optional (default=False)] When set to True, paint nodes to indicate majority class for classification, extremity of values for regression, or purity of node for multi-output.

**impurity** [bool, optional (default=True)] When set to True, show the impurity at each node.

node\_ids [bool, optional (default=False)] When set to True, show the ID number on each node.

**proportion** [bool, optional (default=False)] When set to True, change the display of 'values' and/or 'samples' to be proportions and percentages respectively.

**rotate** [bool, optional (default=False)] When set to True, orient tree left to right rather than top-down.

**rounded** [bool, optional (default=False)] When set to True, draw node boxes with rounded corners and use Helvetica fonts instead of Times-Roman.

**precision** [int, optional (default=3)] Number of digits of precision for floating point in the values of impurity, threshold and value attributes of each node.

**ax** [matplotlib axis, optional (default=None)] Axes to plot to. If None, use current axis. Any previous content is cleared.

**fontsize** [int, optional (default=None)] Size of text font. If None, determined automatically to fit figure.

#### Returns

**annotations** [list of artists] List containing the artists for the annotation boxes making up the tree.

# **Examples**

```
>>> from sklearn.datasets import load_iris
>>> from sklearn import tree

>>> clf = tree.DecisionTreeClassifier(random_state=0)
```

```
>>> iris = load_iris()

>>> clf = clf.fit(iris.data, iris.target)
>>> tree.plot_tree(clf)
```

#### Examples using sklearn.tree.plot\_tree

 $[Text(251.5,345.217,'X[3] \le 0.8...$ 

• Plot the decision surface of a decision tree on the iris dataset

# 6.38.7 sklearn.tree.export\_text

```
sklearn.tree.export_text (decision_tree, feature_names=None, max_depth=10, spacing=3, deci-
mals=2, show_weights=False)
```

Build a text report showing the rules of a decision tree.

Note that backwards compatibility may not be supported.

### **Parameters**

**decision\_tree** [object] The decision tree estimator to be exported. It can be an instance of DecisionTreeClassifier or DecisionTreeRegressor.

**feature\_names** [list, optional (default=None)] A list of length n\_features containing the feature names. If None generic names will be used ("feature\_0", "feature\_1", ...).

max\_depth [int, optional (default=10)] Only the first max\_depth levels of the tree are exported. Truncated branches will be marked with "...".

**spacing** [int, optional (default=3)] Number of spaces between edges. The higher it is, the wider the result.

**decimals** [int, optional (default=2)] Number of decimal digits to display.

**show\_weights** [bool, optional (default=False)] If true the classification weights will be exported on each leaf. The classification weights are the number of samples each class.

### Returns

**report** [string] Text summary of all the rules in the decision tree.

## **Examples**

```
>>> from sklearn.datasets import load_iris
>>> from sklearn.tree import DecisionTreeClassifier
>>> from sklearn.tree.export import export_text
>>> iris = load_iris()
>>> X = iris['data']
>>> y = iris['target']
>>> decision_tree = DecisionTreeClassifier(random_state=0, max_depth=2)
>>> decision_tree = decision_tree.fit(X, y)
>>> r = export_text(decision_tree, feature_names=iris['feature_names'])
>>> print(r)
|--- petal width (cm) <= 0.80
  |--- class: 0
|--- petal width (cm) > 0.80
    |--- petal width (cm) \leq 1.75
   | |--- class: 1
   |--- petal width (cm) > 1.75
    | |--- class: 2
```

# 6.39 sklearn.utils: Utilities

The sklearn.utils module includes various utilities.

Developer guide: See the Utilities for Developers page for further details.

utils.arrayfuncs.cholesky_delete(L,	
go_out)	
utils.arrayfuncs.min_pos()	Find the minimum value of an array over positive values
<pre>utils.as_float_array(X[, copy, force_all_finite])</pre>	Converts an array-like to an array of floats.
utils.assert_all_finite(X[, allow_nan])	Throw a ValueError if X contains NaN or infinity.
$utils.check\_X\_y(X, y[, accept\_sparse,])$	Input validation for standard estimators.

Continued on next page

Table 6.288 – continued from previous page

Table 6.288 – continued from previous page		
<pre>utils.check_array(array[, accept_sparse,])</pre>	Input validation on an array, list, sparse matrix or similar.	
utils.check_scalar(x, name, target_type[,])	Validate scalar parameters type and value.	
utils.check_consistent_length(\*arrays)	Check that all arrays have consistent first dimensions.	
utils.check_random_state(seed)	Turn seed into a np.random.RandomState instance	
utils.class_weight.	Estimate class weights for unbalanced datasets.	
<pre>compute_class_weight()</pre>		
utils.class_weight.	Estimate sample weights by class for unbalanced datasets.	
<pre>compute_sample_weight()</pre>		
utils.deprecated([extra])	Decorator to mark a function or class as deprecated.	
utils.estimator_checks.	Check if estimator adheres to scikit-learn conventions.	
<pre>check_estimator(Estimator)</pre>		
utils.extmath.safe_sparse_dot( $a, b[,]$ )	Dot product that handle the sparse matrix case correctly	
utils.extmath.randomized_range_finder(A,	Computes an orthonormal matrix whose range approxi-	
)	mates the range of A.	
utils.extmath.randomized_svd( $\mathbf{M},$	Computes a truncated randomized SVD	
n_components)		
utils.extmath.fast_logdet(A)	Compute log(det(A)) for A symmetric	
utils.extmath.density(w,\*\*kwargs)	Compute density of a sparse vector	
utils.extmath.weighted_mode(a, w[, axis])	Returns an array of the weighted modal (most common) value in a	
utils.gen_even_slices(n, n_packs[, n_samples])	Generator to create n_packs slices going up to n.	
	1 0 1	
utils.graph.single_source_shortest_path_	I Return the shortest path length from source to all reachable nodes.	
utils.graph_shortest_path.	Perform a shortest-path graph search on a positive directed	
graph_shortest_path()	or undirected graph.	
utils.indexable(\*iterables)	Make arrays indexable for cross-validation.	
utils.metaestimators.	Create a decorator for methods that are delegated to a sub-	
if_delegate_has_method()	estimator	
utils.multiclass.type_of_target(y)	Determine the type of data indicated by the target.	
utils.multiclass.is_multilabel(y)	Check if y is in a multilabel format.	
utils.multiclass.unique_labels(\*ys)	Extract an ordered array of unique labels	
utils.murmurhash3_32()	Compute the 32bit murmurhash3 of key at seed.	
utils.resample(\*arrays, \*\*options)	Resample arrays or sparse matrices in a consistent way	
utils.safe_indexing(X, indices)	Return items or rows from X using indices.	
utils.safe_mask(X, mask)	Return a mask which is safe to use on X.	
utils.safe_sqr(X[,copy])	Element wise squaring of array-likes and sparse matrices.	
utils.shuffle(\*arrays, \*\*options)	Shuffle arrays or sparse matrices in a consistent way	
utils.sparsefuncs.	Compute incremental mean and variance along an axix on	
$incr_{mean\_variance\_axis}(X,)$	a CSR or CSC matrix.	
utils.sparsefuncs.	Inplace column scaling of a CSC/CSR matrix.	
inplace_column_scale(X, scale)	inplace column scaning of a Coc/Cox matrix.	
utils.sparsefuncs.inplace_row_scale(X,	Inplace row scaling of a CSR or CSC matrix.	
scale)	inplace fow scanning of a core of coc matrix.	
utils.sparsefuncs.inplace_swap_row(X, m,	Swaps two rows of a CSC/CSR matrix in-place.	
n)	Swaps two lows of a CSC/CSR matrix m-place.	
utils.sparsefuncs.	Swaps two columns of a CSC/CSR matrix in-place.	
<pre>inplace_swap_column(X, m, n)</pre>	5 maps two columns of a COC/Core maura in-place.	
utils.sparsefuncs.mean_variance_axis(X,	Compute mean and variance along an axix on a CSR or	
axis)	CSC matrix	
utils.sparsefuncs.	Inplace column scaling of a CSR matrix.	
inplace_csr_column_scale(X,)	inplace column scaning of a CSN matrix.	
inprace_cor_corumi_scare(A,)	Continued on next page	
	Continued on next page	

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	1 1 5
utils.sparsefuncs_fast.	Inplace row normalize using the 11 norm
inplace_csr_row_normalize_l1()	
utils.sparsefuncs_fast.	Inplace row normalize using the 12 norm
inplace_csr_row_normalize_12()	
<pre>utils.random.sample_without_replacement()</pre>	Sample integers without replacement.
utils.validation.check_is_fitted(estimator,	Perform is_fitted validation for estimator.
)	
utils.validation.check_memory(memory)	Check that memory is joblib.Memory-like.
utils.validation.check_symmetric(array[,	Make sure that array is 2D, square and symmetric.
])	
utils.validation.column_or_1d(y[, warn])	Ravel column or 1d numpy array, else raises an error
utils.validation.has_fit_parameter()	Checks whether the estimator's fit method supports the
	given parameter.
utils.testing.assert_in(member, container[,	Just like self.assertTrue(a in b), but with a nicer default
msg])	message.
utils.testing.assert_not_in(member, con-	Just like self.assertTrue(a not in b), but with a nicer default
tainer)	message.
utils.testing.assert_raise_message()	Helper function to test the message raised in an exception.
utils.testing.all_estimators([])	Get a list of all estimators from sklearn.

# 6.39.1 sklearn.utils.arrayfuncs.cholesky\_delete

# 6.39.2 sklearn.utils.arrayfuncs.min\_pos

sklearn.utils.arrayfuncs.min\_pos()

Find the minimum value of an array over positive values

Returns a huge value if none of the values are positive

# 6.39.3 sklearn.utils.as\_float\_array

sklearn.utils.as\_float\_array (X, copy=True, force\_all\_finite=True)

Converts an array-like to an array of floats.

The new dtype will be np.float32 or np.float64, depending on the original type. The function can create a copy or modify the argument depending on the argument copy.

### **Parameters**

**X** [{array-like, sparse matrix}]

**copy** [bool, optional] If True, a copy of X will be created. If False, a copy may still be returned if X's dtype is not a floating point type.

**force\_all\_finite** [boolean or 'allow-nan', (default=True)] Whether to raise an error on np.inf and np.nan in X. The possibilities are:

- True: Force all values of X to be finite.
- False: accept both np.inf and np.nan in X.
- 'allow-nan': accept only np.nan values in X. Values cannot be infinite.

New in version 0.20: force\_all\_finite accepts the string 'allow-nan'.

#### Returns

XT [{array, sparse matrix}] An array of type np.float

# 6.39.4 sklearn.utils.assert\_all\_finite

sklearn.utils.assert\_all\_finite(X, allow\_nan=False)
Throw a ValueError if X contains NaN or infinity.

#### **Parameters**

X [array or sparse matrix]
allow\_nan [bool]

# 6.39.5 sklearn.utils.check X y

sklearn.utils.check\_X\_y (X, y, accept\_sparse=False, accept\_large\_sparse=True, dtype='numeric', order=None, copy=False, force\_all\_finite=True, ensure\_2d=True, allow\_nd=False, multi\_output=False, ensure\_min\_samples=1, ensure\_min\_features=1, y\_numeric=False, warn\_on\_dtype=None, estimator=None)

Input validation for standard estimators.

Checks X and y for consistent length, enforces X to be 2D and y 1D. By default, X is checked to be non-empty and containing only finite values. Standard input checks are also applied to y, such as checking that y does not have np.nan or np.inf targets. For multi-label y, set multi\_output=True to allow 2D and sparse y. If the dtype of X is object, attempt converting to float, raising on failure.

#### **Parameters**

- **X** [nd-array, list or sparse matrix] Input data.
- y [nd-array, list or sparse matrix] Labels.
- accept\_sparse [string, boolean or list of string (default=False)] String[s] representing allowed
  sparse matrix formats, such as 'csc', 'csr', etc. If the input is sparse but not in the allowed
  format, it will be converted to the first listed format. True allows the input to be any format.
  False means that a sparse matrix input will raise an error.
- accept\_large\_sparse [bool (default=True)] If a CSR, CSC, COO or BSR sparse matrix is supplied and accepted by accept\_sparse, accept\_large\_sparse will cause it to be accepted only if its indices are stored with a 32-bit dtype.

New in version 0.20.

- dtype [string, type, list of types or None (default="numeric")] Data type of result. If None, the dtype of the input is preserved. If "numeric", dtype is preserved unless array.dtype is object. If dtype is a list of types, conversion on the first type is only performed if the dtype of the input is not in the list.
- order ['F', 'C' or None (default=None)] Whether an array will be forced to be fortran or c-style.
- **copy** [boolean (default=False)] Whether a forced copy will be triggered. If copy=False, a copy might be triggered by a conversion.
- **force\_all\_finite** [boolean or 'allow-nan', (default=True)] Whether to raise an error on np.inf and np.nan in X. This parameter does not influence whether y can have np.inf or np.nan values. The possibilities are:
  - True: Force all values of X to be finite.

- False: accept both np.inf and np.nan in X.
- 'allow-nan': accept only np.nan values in X. Values cannot be infinite.

New in version 0.20: force\_all\_finite accepts the string 'allow-nan'.

**ensure\_2d** [boolean (default=True)] Whether to raise a value error if X is not 2D.

**allow\_nd** [boolean (default=False)] Whether to allow X.ndim > 2.

- multi\_output [boolean (default=False)] Whether to allow 2D y (array or sparse matrix).
  If false, y will be validated as a vector. y cannot have np.nan or np.inf values if multi\_output=True.
- **ensure\_min\_samples** [int (default=1)] Make sure that X has a minimum number of samples in its first axis (rows for a 2D array).
- ensure\_min\_features [int (default=1)] Make sure that the 2D array has some minimum number of features (columns). The default value of 1 rejects empty datasets. This check is only enforced when X has effectively 2 dimensions or is originally 1D and ensure\_2d is True. Setting to 0 disables this check.
- **y\_numeric** [boolean (default=False)] Whether to ensure that y has a numeric type. If dtype of y is object, it is converted to float64. Should only be used for regression algorithms.
- warn\_on\_dtype [boolean or None, optional (default=None)] Raise DataConversionWarning if the dtype of the input data structure does not match the requested dtype, causing a memory copy.

Deprecated since version 0.21: warn\_on\_dtype is deprecated in version 0.21 and will be removed in 0.23.

**estimator** [str or estimator instance (default=None)] If passed, include the name of the estimator in warning messages.

### Returns

**X\_converted** [object] The converted and validated X.

**y\_converted** [object] The converted and validated y.

## 6.39.6 sklearn.utils.check array

```
sklearn.utils.\textbf{check\_array} (array, accept\_sparse=False, accept\_large\_sparse=True, \\ dtype='numeric', order=None, copy=False, force\_all\_finite=True, \\ ensure\_2d=True, allow\_nd=False, ensure\_min\_samples=1, ensure\_min\_features=1, warn\_on\_dtype=None, estimator=None)
```

Input validation on an array, list, sparse matrix or similar.

By default, the input is checked to be a non-empty 2D array containing only finite values. If the dtype of the array is object, attempt converting to float, raising on failure.

#### **Parameters**

**array** [object] Input object to check / convert.

accept\_sparse [string, boolean or list/tuple of strings (default=False)] String[s] representing allowed sparse matrix formats, such as 'csc', 'csr', etc. If the input is sparse but not in the allowed format, it will be converted to the first listed format. True allows the input to be any format. False means that a sparse matrix input will raise an error.

**accept\_large\_sparse** [bool (default=True)] If a CSR, CSC, COO or BSR sparse matrix is supplied and accepted by accept\_sparse, accept\_large\_sparse=False will cause it to be accepted only if its indices are stored with a 32-bit dtype.

New in version 0.20.

- **dtype** [string, type, list of types or None (default="numeric")] Data type of result. If None, the dtype of the input is preserved. If "numeric", dtype is preserved unless array.dtype is object. If dtype is a list of types, conversion on the first type is only performed if the dtype of the input is not in the list.
- **order** ['F', 'C' or None (default=None)] Whether an array will be forced to be fortran or c-style. When order is None (default), then if copy=False, nothing is ensured about the memory layout of the output array; otherwise (copy=True) the memory layout of the returned array is kept as close as possible to the original array.
- **copy** [boolean (default=False)] Whether a forced copy will be triggered. If copy=False, a copy might be triggered by a conversion.
- **force\_all\_finite** [boolean or 'allow-nan', (default=True)] Whether to raise an error on np.inf and np.nan in array. The possibilities are:
  - True: Force all values of array to be finite.
  - False: accept both np.inf and np.nan in array.
  - 'allow-nan': accept only np.nan values in array. Values cannot be infinite.

For object dtyped data, only np.nan is checked and not np.inf.

New in version 0.20: force\_all\_finite accepts the string 'allow-nan'.

ensure\_2d [boolean (default=True)] Whether to raise a value error if array is not 2D.

**allow\_nd** [boolean (default=False)] Whether to allow array.ndim > 2.

- **ensure\_min\_samples** [int (default=1)] Make sure that the array has a minimum number of samples in its first axis (rows for a 2D array). Setting to 0 disables this check.
- ensure\_min\_features [int (default=1)] Make sure that the 2D array has some minimum number of features (columns). The default value of 1 rejects empty datasets. This check is only enforced when the input data has effectively 2 dimensions or is originally 1D and ensure\_2d is True. Setting to 0 disables this check.
- warn\_on\_dtype [boolean or None, optional (default=None)] Raise DataConversionWarning if the dtype of the input data structure does not match the requested dtype, causing a memory copy.

Deprecated since version 0.21: warn\_on\_dtype is deprecated in version 0.21 and will be removed in 0.23.

**estimator** [str or estimator instance (default=None)] If passed, include the name of the estimator in warning messages.

#### Returns

**array\_converted** [object] The converted and validated array.

## 6.39.7 sklearn.utils.check scalar

sklearn.utils.check\_scalar(x, name, target\_type, min\_val=None, max\_val=None) Validate scalar parameters type and value.

#### **Parameters**

**x** [object] The scalar parameter to validate.

**name** [str] The name of the parameter to be printed in error messages.

target\_type [type or tuple] Acceptable data types for the parameter.

**min\_val** [float or int, optional (default=None)] The minimum valid value the parameter can take. If None (default) it is implied that the parameter does not have a lower bound.

max\_val [float or int, optional (default=None)] The maximum valid value the parameter can take. If None (default) it is implied that the parameter does not have an upper bound.

#### Raises

**TypeError** If the parameter's type does not match the desired type.

ValueError If the parameter's value violates the given bounds.

# 6.39.8 sklearn.utils.check consistent length

```
sklearn.utils.check_consistent_length(*arrays)
```

Check that all arrays have consistent first dimensions.

Checks whether all objects in arrays have the same shape or length.

#### **Parameters**

\*arrays [list or tuple of input objects.] Objects that will be checked for consistent length.

# 6.39.9 sklearn.utils.check random state

sklearn.utils.check\_random\_state(seed)

Turn seed into a np.random.RandomState instance

### **Parameters**

**seed** [None | int | instance of RandomState] If seed is None, return the RandomState singleton used by np.random. If seed is an int, return a new RandomState instance seeded with seed. If seed is already a RandomState instance, return it. Otherwise raise ValueError.

### Examples using sklearn.utils.check\_random\_state

- Isotonic Regression
- Face completion with a multi-output estimators
- Empirical evaluation of the impact of k-means initialization
- MNIST classification using multinomial logistic + L1
- · Manifold Learning methods on a severed sphere
- Scaling the regularization parameter for SVCs

# 6.39.10 sklearn.utils.class\_weight.compute\_class\_weight

sklearn.utils.class\_weight.compute\_class\_weight (class\_weight, classes, y) Estimate class weights for unbalanced datasets.

#### **Parameters**

class\_weight [dict, 'balanced' or None] If 'balanced', class weights will be given by
n\_samples / (n\_classes \* np.bincount(y)). If a dictionary is given, keys
are classes and values are corresponding class weights. If None is given, the class weights
will be uniform.

**classes** [ndarray] Array of the classes occurring in the data, as given by np.unique (y\_org) with y\_org the original class labels.

y [array-like, shape (n\_samples,)] Array of original class labels per sample;

#### Returns

class\_weight\_vect [ndarray, shape (n\_classes,)] Array with class\_weight\_vect[i] the weight for
 i-th class

### References

The "balanced" heuristic is inspired by Logistic Regression in Rare Events Data, King, Zen, 2001.

# 6.39.11 sklearn.utils.class\_weight.compute\_sample\_weight

sklearn.utils.class\_weight.compute\_sample\_weight (class\_weight, y, indices=None) Estimate sample weights by class for unbalanced datasets.

### **Parameters**

class\_weight [dict, list of dicts, "balanced", or None, optional] Weights associated with classes
in the form {class\_label: weight}. If not given, all classes are supposed to have
weight one. For multi-output problems, a list of dicts can be provided in the same order as
the columns of y.

Note that for multioutput (including multilabel) weights should be defined for each class of every column in its own dict. For example, for four-class multilabel classification weights should be [{0: 1, 1: 1}, {0: 1, 1: 5}, {0: 1, 1: 1}, {0: 1, 1: 1}] instead of [{1:1}, {2:5}, {3:1}, {4:1}].

The "balanced" mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data:  $n_samples / (n_classes * np. bincount(y))$ .

For multi-output, the weights of each column of y will be multiplied.

- **y** [array-like, shape = [n\_samples] or [n\_samples, n\_outputs]] Array of original class labels per sample.
- indices [array-like, shape (n\_subsample,), or None] Array of indices to be used in a subsample. Can be of length less than n\_samples in the case of a subsample, or equal to n\_samples in the case of a bootstrap subsample with repeated indices. If None, the sample weight will be calculated over the full sample. Only "balanced" is supported for class\_weight if this is provided.

## Returns

sample\_weight\_vect [ndarray, shape (n\_samples,)] Array with sample weights as applied to
the original y

# 6.39.12 sklearn.utils.deprecated

```
sklearn.utils.deprecated(extra='')
```

Decorator to mark a function or class as deprecated.

Issue a warning when the function is called/the class is instantiated and adds a warning to the docstring.

The optional extra argument will be appended to the deprecation message and the docstring. Note: to use this with the default value for extra, put in an empty of parentheses:

```
>>> from sklearn.utils import deprecated
>>> deprecated()
<sklearn.utils.deprecation.deprecated object at ...>
```

```
>>> @deprecated()
... def some_function(): pass
```

### **Parameters**

extra [string] to be added to the deprecation messages

## 6.39.13 sklearn.utils.estimator\_checks.check estimator

```
sklearn.utils.estimator_checks.check_estimator(Estimator)
```

Check if estimator adheres to scikit-learn conventions.

This estimator will run an extensive test-suite for input validation, shapes, etc. Additional tests for classifiers, regressors, clustering or transformers will be run if the Estimator class inherits from the corresponding mixin from sklearn.base.

This test can be applied to classes or instances. Classes currently have some additional tests that related to construction, while passing instances allows the testing of multiple options.

### **Parameters**

estimator [estimator object or class] Estimator to check. Estimator is a class object or instance.

## 6.39.14 sklearn.utils.extmath.safe sparse dot

```
sklearn.utils.extmath.safe_sparse_dot(a, b, dense_output=False)
```

Dot product that handle the sparse matrix case correctly

Uses BLAS GEMM as replacement for numpy.dot where possible to avoid unnecessary copies.

# **Parameters**

- a [array or sparse matrix]
- **b** [array or sparse matrix]

**dense\_output** [boolean, default False] When False, either a or b being sparse will yield sparse output. When True, output will always be an array.

## Returns

**dot\_product** [array or sparse matrix] sparse if a or b is sparse and dense\_output=False.

# 6.39.15 sklearn.utils.extmath.randomized\_range\_finder

```
sklearn.utils.extmath.randomized\_range\_finder(A, size, n\_iter, power\_iteration\_normalizer='auto', random\_state=None) \\ Computes an orthonormal matrix whose range approximates the range of A.
```

#### **Parameters**

A [2D array] The input data matrix

size [integer] Size of the return array

**n\_iter** [integer] Number of power iterations used to stabilize the result

**power\_iteration\_normalizer** ['auto' (default), 'QR', 'LU', 'none'] Whether the power iterations are normalized with step-by-step QR factorization (the slowest but most accurate), 'none' (the fastest but numerically unstable when n\_iter is large, e.g. typically 5 or larger), or 'LU' factorization (numerically stable but can lose slightly in accuracy). The 'auto' mode applies no normalization if n\_iter <= 2 and switches to LU otherwise.

New in version 0.18.

random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

#### Returns

**Q** [2D array] A (size x size) projection matrix, the range of which approximates well the range of the input matrix A.

### **Notes**

Follows Algorithm 4.3 of Finding structure with randomness: Stochastic algorithms for constructing approximate matrix decompositions Halko, et al., 2009 (arXiv:909) https://arxiv.org/pdf/0909.4061.pdf

An implementation of a randomized algorithm for principal component analysis A. Szlam et al. 2014

# 6.39.16 sklearn.utils.extmath.randomized\_svd

```
sklearn.utils.extmath. {\bf randomized\_svd} (M, n\_components, n\_oversamples=10, n\_iter='auto', power\_iteration\_normalizer='auto', transpose='auto', flip\_sign=True, random\_state=0)
```

Computes a truncated randomized SVD

#### **Parameters**

- M [ndarray or sparse matrix] Matrix to decompose
- **n\_components** [int] Number of singular values and vectors to extract.
- **n\_oversamples** [int (default is 10)] Additional number of random vectors to sample the range of M so as to ensure proper conditioning. The total number of random vectors used to find

the range of M is n\_components + n\_oversamples. Smaller number can improve speed but can negatively impact the quality of approximation of singular vectors and singular values.

n\_iter [int or 'auto' (default is 'auto')] Number of power iterations. It can be used to deal
with very noisy problems. When 'auto', it is set to 4, unless n\_components is small (<
 .1 \* min(X.shape)) n\_iter in which case is set to 7. This improves precision with few
components.</pre>

Changed in version 0.18.

power\_iteration\_normalizer ['auto' (default), 'QR', 'LU', 'none'] Whether the power iterations are normalized with step-by-step QR factorization (the slowest but most accurate), 'none' (the fastest but numerically unstable when n\_iter is large, e.g. typically 5 or larger), or 'LU' factorization (numerically stable but can lose slightly in accuracy). The 'auto' mode applies no normalization if n\_iter <= 2 and switches to LU otherwise.</pre>

New in version 0.18.

**transpose** [True, False or 'auto' (default)] Whether the algorithm should be applied to M.T instead of M. The result should approximately be the same. The 'auto' mode will trigger the transposition if M.shape[1] > M.shape[0] since this implementation of randomized SVD tend to be a little faster in that case.

Changed in version 0.18.

- **flip\_sign** [boolean, (True by default)] The output of a singular value decomposition is only unique up to a permutation of the signs of the singular vectors. If flip\_sign is set to True, the sign ambiguity is resolved by making the largest loadings for each component in the left singular vectors positive.
- random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

### **Notes**

This algorithm finds a (usually very good) approximate truncated singular value decomposition using randomization to speed up the computations. It is particularly fast on large matrices on which you wish to extract only a small number of components. In order to obtain further speed up, n\_iter can be set <=2 (at the cost of loss of precision).

#### References

- Finding structure with randomness: Stochastic algorithms for constructing approximate matrix decompositions Halko, et al., 2009 https://arxiv.org/abs/0909.4061
- A randomized algorithm for the decomposition of matrices Per-Gunnar Martinsson, Vladimir Rokhlin and Mark Tygert
- An implementation of a randomized algorithm for principal component analysis A. Szlam et al. 2014

# 6.39.17 sklearn.utils.extmath.fast logdet

```
sklearn.utils.extmath.fast_logdet(A)
```

Compute log(det(A)) for A symmetric

 $Equivalent \ to: np.log(nl.det(A)) \ but \ more \ robust. \ It \ returns \ -Inf \ if \ det(A) \ is \ non \ positive \ or \ is \ not \ defined.$ 

#### **Parameters**

A [array\_like] The matrix

# 6.39.18 sklearn.utils.extmath.density

```
sklearn.utils.extmath.density(w, **kwargs)
```

Compute density of a sparse vector

### **Parameters**

w [array\_like] The sparse vector

#### **Returns**

**float** The density of w, between 0 and 1

## Examples using sklearn.utils.extmath.density

• Classification of text documents using sparse features

# 6.39.19 sklearn.utils.extmath.weighted\_mode

```
sklearn.utils.extmath.weighted_mode(a, w, axis=0)
```

Returns an array of the weighted modal (most common) value in a

If there is more than one such value, only the first is returned. The bin-count for the modal bins is also returned.

This is an extension of the algorithm in scipy.stats.mode.

## **Parameters**

- **a** [array\_like] n-dimensional array of which to find mode(s).
- w [array\_like] n-dimensional array of weights for each value

axis [int, optional] Axis along which to operate. Default is 0, i.e. the first axis.

### Returns

```
vals [ndarray] Array of modal values.
```

score [ndarray] Array of weighted counts for each mode.

### See also:

```
scipy.stats.mode
```

## **Examples**

```
>>> from sklearn.utils.extmath import weighted_mode
>>> x = [4, 1, 4, 2, 4, 2]
>>> weights = [1, 1, 1, 1, 1]
>>> weighted_mode(x, weights)
(array([4.]), array([3.]))
```

The value 4 appears three times: with uniform weights, the result is simply the mode of the distribution.

```
>>> weights = [1, 3, 0.5, 1.5, 1, 2] # deweight the 4's
>>> weighted_mode(x, weights)
(array([2.]), array([3.5]))
```

The value 2 has the highest score: it appears twice with weights of 1.5 and 2: the sum of these is 3.5.

# 6.39.20 sklearn.utils.gen\_even\_slices

```
sklearn.utils.gen_even_slices (n, n_packs, n_samples=None)
Generator to create n_packs slices going up to n.
```

#### **Parameters**

n [int]

**n\_packs** [int] Number of slices to generate.

**n\_samples** [int or None (default = None)] Number of samples. Pass n\_samples when the slices are to be used for sparse matrix indexing; slicing off-the-end raises an exception, while it works for NumPy arrays.

### **Yields**

slice

#### **Examples**

```
>>> from sklearn.utils import gen_even_slices
>>> list(gen_even_slices(10, 1))
[slice(0, 10, None)]
>>> list(gen_even_slices(10, 10))
[slice(0, 1, None), slice(1, 2, None), ..., slice(9, 10, None)]
>>> list(gen_even_slices(10, 5))
[slice(0, 2, None), slice(2, 4, None), ..., slice(8, 10, None)]
>>> list(gen_even_slices(10, 3))
[slice(0, 4, None), slice(4, 7, None), slice(7, 10, None)]
```

# 6.39.21 sklearn.utils.graph.single\_source\_shortest\_path\_length

```
sklearn.utils.graph.single_source_shortest_path_length(graph, source, cut-off=None)
```

Return the shortest path length from source to all reachable nodes.

Returns a dictionary of shortest path lengths keyed by target.

## **Parameters**

graph [sparse matrix or 2D array (preferably LIL matrix)] Adjacency matrix of the graph

source [integer] Starting node for path

**cutoff** [integer, optional] Depth to stop the search - only paths of length <= cutoff are returned.

## **Examples**

# 6.39.22 sklearn.utils.graph\_shortest\_path.graph\_shortest\_path

sklearn.utils.graph\_shortest\_path()

Perform a shortest-path graph search on a positive directed or undirected graph.

#### **Parameters**

**dist\_matrix** [arraylike or sparse matrix, shape = (N,N)] Array of positive distances. If vertex i is connected to vertex j, then dist\_matrix[i,j] gives the distance between the vertices. If vertex i is not connected to vertex j, then dist\_matrix[i,j] = 0

**directed** [boolean] if True, then find the shortest path on a directed graph: only progress from a point to its neighbors, not the other way around. if False, then find the shortest path on an undirected graph: the algorithm can progress from a point to its neighbors and vice versa.

**method** [string ['auto'|'FW'|'D']] method to use. Options are 'auto': attempt to choose the best method for the current problem 'FW': Floyd-Warshall algorithm.  $O[N^3]$  'D': Dijkstra's algorithm with Fibonacci stacks.  $O[(k+log(N))N^2]$ 

### Returns

**G** [np.ndarray, float, shape = [N,N]] G[i,j] gives the shortest distance from point i to point j along the graph.

### **Notes**

As currently implemented, Dijkstra's algorithm does not work for graphs with direction-dependent distances when directed == False. i.e., if dist\_matrix[i,j] and dist\_matrix[j,i] are not equal and both are nonzero, method='D' will not necessarily yield the correct result.

Also, these routines have not been tested for graphs with negative distances. Negative distances can lead to infinite cycles that must be handled by specialized algorithms.

# 6.39.23 sklearn.utils.indexable

```
sklearn.utils.indexable(*iterables)
```

Make arrays indexable for cross-validation.

Checks consistent length, passes through None, and ensures that everything can be indexed by converting sparse matrices to csr and converting non-interable objects to arrays.

#### **Parameters**

\*iterables [lists, dataframes, arrays, sparse matrices] List of objects to ensure sliceability.

# 6.39.24 sklearn.utils.metaestimators.if\_delegate\_has\_method

sklearn.utils.metaestimators.if\_delegate\_has\_method(delegate)

Create a decorator for methods that are delegated to a sub-estimator

This enables ducktyping by hasattr returning True according to the sub-estimator.

#### **Parameters**

**delegate** [string, list of strings or tuple of strings] Name of the sub-estimator that can be accessed as an attribute of the base object. If a list or a tuple of names are provided, the first sub-estimator that is an attribute of the base object will be used.

## Examples using sklearn.utils.metaestimators.if\_delegate\_has\_method

• Inductive Clustering

# 6.39.25 sklearn.utils.multiclass.type\_of\_target

```
sklearn.utils.multiclass.type_of_target(y)
```

Determine the type of data indicated by the target.

Note that this type is the most specific type that can be inferred. For example:

- binary is more specific but compatible with multiclass.
- multiclass of integers is more specific but compatible with continuous.
- multilabel-indicator is more specific but compatible with multiclass-multioutput.

#### **Parameters**

y [array-like]

### Returns

## target\_type [string] One of:

- 'continuous': y is an array-like of floats that are not all integers, and is 1d or a column vector.
- 'continuous-multioutput': y is a 2d array of floats that are not all integers, and both dimensions are of size > 1.
- 'binary': y contains <= 2 discrete values and is 1d or a column vector.
- 'multiclass': y contains more than two discrete values, is not a sequence of sequences, and is 1d or a column vector.
- 'multiclass-multioutput': y is a 2d array that contains more than two discrete values, is not a sequence of sequences, and both dimensions are of size > 1.
- 'multilabel-indicator': y is a label indicator matrix, an array of two dimensions with at least two columns, and at most 2 unique values.

• 'unknown': y is array-like but none of the above, such as a 3d array, sequence of sequences, or an array of non-sequence objects.

## **Examples**

```
>>> import numpy as np
>>> type_of_target([0.1, 0.6])
'continuous'
>>> type_of_target([1, -1, -1, 1])
'binary'
>>> type_of_target(['a', 'b', 'a'])
'binary'
>>> type_of_target([1.0, 2.0])
'binary'
>>> type_of_target([1, 0, 2])
'multiclass'
>>> type_of_target([1.0, 0.0, 3.0])
'multiclass'
>>> type_of_target(['a', 'b', 'c'])
'multiclass'
>>> type_of_target(np.array([[1, 2], [3, 1]]))
'multiclass-multioutput'
>>> type_of_target([[1, 2]])
'multiclass-multioutput'
>>> type_of_target(np.array([[1.5, 2.0], [3.0, 1.6]]))
'continuous-multioutput'
>>> type_of_target(np.array([[0, 1], [1, 1]]))
'multilabel-indicator'
```

## 6.39.26 sklearn.utils.multiclass.is\_multilabel

```
sklearn.utils.multiclass.is_multilabel(y)
Check if y is in a multilabel format.
```

## **Parameters**

y [numpy array of shape [n\_samples]] Target values.

### Returns

out [bool,] Return True, if y is in a multilabel format, else `False.

# **Examples**

```
>>> import numpy as np
>>> from sklearn.utils.multiclass import is_multilabel
>>> is_multilabel([0, 1, 0, 1])
False
>>> is_multilabel([[1], [0, 2], []])
False
>>> is_multilabel(np.array([[1, 0], [0, 0]]))
True
>>> is_multilabel(np.array([[1], [0], [0]]))
False
```

```
>>> is_multilabel(np.array([[1, 0, 0]]))
True
```

## 6.39.27 sklearn.utils.multiclass.unique\_labels

```
sklearn.utils.multiclass.unique_labels(*ys)
Extract an ordered array of unique labels
```

#### We don't allow:

- mix of multilabel and multiclass (single label) targets
- mix of label indicator matrix and anything else, because there are no explicit labels)
- mix of label indicator matrices of different sizes
- · mix of string and integer labels

At the moment, we also don't allow "multiclass-multioutput" input type.

### **Parameters**

```
*ys [array-likes]
```

#### Returns

out [numpy array of shape [n\_unique\_labels]] An ordered array of unique labels.

## **Examples**

```
>>> from sklearn.utils.multiclass import unique_labels
>>> unique_labels([3, 5, 5, 5, 7, 7])
array([3, 5, 7])
>>> unique_labels([1, 2, 3, 4], [2, 2, 3, 4])
array([1, 2, 3, 4])
>>> unique_labels([1, 2, 10], [5, 11])
array([ 1,  2,  5, 10, 11])
```

## Examples using sklearn.utils.multiclass.unique\_labels

• Confusion matrix

## 6.39.28 sklearn.utils.murmurhash3 32

```
sklearn.utils.murmurhash3_32()
```

Compute the 32bit murmurhash3 of key at seed.

The underlying implementation is MurmurHash3\_x86\_32 generating low latency 32bits hash suitable for implementing lookup tables, Bloom filters, count min sketch or feature hashing.

### **Parameters**

key [int32, bytes, unicode or ndarray with dtype int32] the physical object to hashseed [int, optional default is 0] integer seed for the hashing algorithm.positive [boolean, optional default is False]

True: the results is casted to an unsigned int from 0 to 2 \*\* 32 - 1

False: the results is casted to a signed int from -(2 \*\* 31) to 2 \*\* 31 - 1

## 6.39.29 sklearn.utils.resample

```
sklearn.utils.resample(*arrays, **options)
```

Resample arrays or sparse matrices in a consistent way

The default strategy implements one step of the bootstrapping procedure.

#### **Parameters**

\*arrays [sequence of indexable data-structures] Indexable data-structures can be arrays, lists, dataframes or scipy sparse matrices with consistent first dimension.

#### Returns

**resampled\_arrays** [sequence of indexable data-structures] Sequence of resampled copies of the collections. The original arrays are not impacted.

### **Other Parameters**

- **replace** [boolean, True by default] Implements resampling with replacement. If False, this will implement (sliced) random permutations.
- **n\_samples** [int, None by default] Number of samples to generate. If left to None this is automatically set to the first dimension of the arrays. If replace is False it should not be larger than the length of arrays.
- random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- **stratify** [array-like or None (default=None)] If not None, data is split in a stratified fashion, using this as the class labels.

### See also:

```
sklearn.utils.shuffle
```

### **Examples**

It is possible to mix sparse and dense arrays in the same run:

# Example using stratification:

```
>>> y = [0, 0, 1, 1, 1, 1, 1, 1, 1]

>>> resample(y, n_samples=5, replace=False, stratify=y,

... random_state=0)

[1, 1, 1, 0, 1]
```

# 6.39.30 sklearn.utils.safe\_indexing

```
sklearn.utils.safe_indexing(X, indices)
```

Return items or rows from X using indices.

Allows simple indexing of lists or arrays.

#### **Parameters**

**X** [array-like, sparse-matrix, list, pandas.DataFrame, pandas.Series.] Data from which to sample rows or items.

**indices** [array-like of int] Indices according to which X will be subsampled.

#### Returns

subset Subset of X on first axis

### **Notes**

CSR, CSC, and LIL sparse matrices are supported. COO sparse matrices are not supported.

# 6.39.31 sklearn.utils.safe\_mask

```
sklearn.utils.safe_mask(X, mask)
```

Return a mask which is safe to use on X.

## Parameters

**X** [{array-like, sparse matrix}] Data on which to apply mask.

mask [array] Mask to be used on X.

#### Returns

#### mask

# 6.39.32 sklearn.utils.safe\_sqr

```
sklearn.utils.safe sqr(X, copy=True)
```

Element wise squaring of array-likes and sparse matrices.

#### **Parameters**

**X** [array like, matrix, sparse matrix]

**copy** [boolean, optional, default True] Whether to create a copy of X and operate on it or to perform inplace computation (default behaviour).

#### Returns

X \*\* 2 [element wise square]

## 6.39.33 sklearn.utils.shuffle

```
sklearn.utils.shuffle(*arrays, **options)
```

Shuffle arrays or sparse matrices in a consistent way

This is a convenience alias to resample (\*arrays, replace=False) to do random permutations of the collections.

### **Parameters**

\*arrays [sequence of indexable data-structures] Indexable data-structures can be arrays, lists, dataframes or scipy sparse matrices with consistent first dimension.

### Returns

**shuffled\_arrays** [sequence of indexable data-structures] Sequence of shuffled copies of the collections. The original arrays are not impacted.

### **Other Parameters**

random\_state [int, RandomState instance or None, optional (default=None)] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**n\_samples** [int, None by default] Number of samples to generate. If left to None this is automatically set to the first dimension of the arrays.

## See also:

```
sklearn.utils.resample
```

## **Examples**

It is possible to mix sparse and dense arrays in the same run:

```
>>> X = np.array([[1., 0.], [2., 1.], [0., 0.]])
>>> y = np.array([0, 1, 2])
>>> from scipy.sparse import coo_matrix
>>> X_sparse = coo_matrix(X)
>>> from sklearn.utils import shuffle
>>> X, X_sparse, y = shuffle(X, X_sparse, y, random_state=0)
>>> X
array([[0., 0.],
       [2., 1.],
       [1., 0.]])
>>> X_sparse
<3x2 sparse matrix of type '<... 'numpy.float64'>'
    with 3 stored elements in Compressed Sparse Row format>
>>> X_sparse.toarray()
array([[0., 0.],
       [2., 1.],
       [1., 0.]])
>>> y
array([2, 1, 0])
>>> shuffle(y, n_samples=2, random_state=0)
array([0, 1])
```

# Examples using sklearn.utils.shuffle

- Model Complexity Influence
- Prediction Latency
- Color Quantization using K-Means
- Empirical evaluation of the impact of k-means initialization
- Gradient Boosting regression
- Early stopping of Stochastic Gradient Descent

## 6.39.34 sklearn.utils.sparsefuncs.incr\_mean\_variance\_axis

sklearn.utils.sparsefuncs.incr\_mean\_variance\_axis (*X*, axis, last\_mean, last\_var, last\_n)
Compute incremental mean and variance along an axix on a CSR or CSC matrix.

last\_mean, last\_var are the statistics computed at the last step by this function. Both must be initialized to 0-arrays of the proper size, i.e. the number of features in X. last\_n is the number of samples encountered until now.

#### **Parameters**

**X** [CSR or CSC sparse matrix, shape (n\_samples, n\_features)] Input data.

axis [int (either 0 or 1)] Axis along which the axis should be computed.

**last\_mean** [float array with shape (n\_features,)] Array of feature-wise means to update with the new data X.

last\_var [float array with shape (n\_features,)] Array of feature-wise var to update with the new data X

**last\_n** [int with shape (n\_features,)] Number of samples seen so far, excluded X.

### Returns

**means** [float array with shape (n\_features,)] Updated feature-wise means.

variances [float array with shape (n\_features,)] Updated feature-wise variances.

n [int with shape (n\_features,)] Updated number of seen samples.

#### **Notes**

NaNs are ignored in the algorithm.

# 6.39.35 sklearn.utils.sparsefuncs.inplace column scale

```
sklearn.utils.sparsefuncs.inplace_column_scale(X, scale)
Inplace column scaling of a CSC/CSR matrix.
```

Scale each feature of the data matrix by multiplying with specific scale provided by the caller assuming a (n\_samples, n\_features) shape.

#### **Parameters**

**X** [CSC or CSR matrix with shape (n\_samples, n\_features)] Matrix to normalize using the variance of the features.

**scale** [float array with shape (n\_features,)] Array of precomputed feature-wise values to use for scaling.

# 6.39.36 sklearn.utils.sparsefuncs.inplace row\_scale

```
sklearn.utils.sparsefuncs.inplace_row_scale(X, scale)
Inplace row scaling of a CSR or CSC matrix.
```

Scale each row of the data matrix by multiplying with specific scale provided by the caller assuming a (n samples, n features) shape.

#### **Parameters**

X [CSR or CSC sparse matrix, shape (n\_samples, n\_features)] Matrix to be scaled.

**scale** [float array with shape (n\_features,)] Array of precomputed sample-wise values to use for scaling.

## 6.39.37 sklearn.utils.sparsefuncs.inplace swap row

```
sklearn.utils.sparsefuncs.inplace_swap_row (X, m, n)
Swaps two rows of a CSC/CSR matrix in-place.
```

#### **Parameters**

**X** [CSR or CSC sparse matrix, shape=(n\_samples, n\_features)] Matrix whose two rows are to be swapped.

- **m** [int] Index of the row of X to be swapped.
- **n** [int] Index of the row of X to be swapped.

# 6.39.38 sklearn.utils.sparsefuncs.inplace\_swap\_column

 $\verb|sklearn.utils.sparsefuncs.inplace_swap_column| (X, m, n)$ 

Swaps two columns of a CSC/CSR matrix in-place.

#### **Parameters**

- **X** [CSR or CSC sparse matrix, shape=(n\_samples, n\_features)] Matrix whose two columns are to be swapped.
- **m** [int] Index of the column of X to be swapped.
- **n** [int] Index of the column of X to be swapped.

# 6.39.39 sklearn.utils.sparsefuncs.mean\_variance\_axis

sklearn.utils.sparsefuncs.mean\_variance\_axis(X, axis)

Compute mean and variance along an axix on a CSR or CSC matrix

#### **Parameters**

X [CSR or CSC sparse matrix, shape (n\_samples, n\_features)] Input data.

axis [int (either 0 or 1)] Axis along which the axis should be computed.

#### Returns

**means** [float array with shape (n\_features,)] Feature-wise means variances [float array with shape (n\_features,)] Feature-wise variances

# 6.39.40 sklearn.utils.sparsefuncs.inplace\_csr\_column\_scale

sklearn.utils.sparsefuncs.inplace\_csr\_column\_scale(X, scale)
Inplace column scaling of a CSR matrix.

Scale each feature of the data matrix by multiplying with specific scale provided by the caller assuming a (n\_samples, n\_features) shape.

### **Parameters**

**X** [CSR matrix with shape (n\_samples, n\_features)] Matrix to normalize using the variance of the features.

**scale** [float array with shape (n\_features,)] Array of precomputed feature-wise values to use for scaling.

# 6.39.41 sklearn.utils.sparsefuncs\_fast.inplace\_csr\_row\_normalize\_l1

```
sklearn.utils.sparsefuncs_fast.inplace_csr_row_normalize_11()
Inplace row normalize using the l1 norm
```

# 6.39.42 sklearn.utils.sparsefuncs\_fast.inplace\_csr\_row\_normalize\_I2

```
sklearn.utils.sparsefuncs_fast.inplace_csr_row_normalize_12()
Inplace row normalize using the l2 norm
```

# 6.39.43 sklearn.utils.random.sample\_without\_replacement

Select n\_samples integers from the set [0, n\_population) without replacement.

### **Parameters**

- **n\_population** [int,] The size of the set to sample from.
- **n\_samples** [int,] The number of integer to sample.
- random\_state [int, RandomState instance or None, optional (default=None)] If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
- method ["auto", "tracking\_selection", "reservoir\_sampling" or "pool"] If method == "auto", the ratio of n\_samples / n\_population is used to determine which algorithm to use: If ratio is between 0 and 0.01, tracking selection is used. If ratio is between 0.01 and 0.99, numpy.random.permutation is used. If ratio is greater than 0.99, reservoir sampling is used. The order of the selected integers is undefined. If a random order is desired, the selected subset should be shuffled.

If method =="tracking\_selection", a set based implementation is used which is suitable for  $n\_samples <<< n\_population$ .

If method == "reservoir\_sampling", a reservoir sampling algorithm is used which is suitable for high memory constraint or when  $O(n\_samples) \sim O(n\_population)$ . The order of the selected integers is undefined. If a random order is desired, the selected subset should be shuffled.

If method == "pool", a pool based algorithm is particularly fast, even faster than the tracking selection method. Hovewer, a vector containing the entire population has to be initialized. If  $n_s$  amples  $\sim n_p$  population, the reservoir sampling method is faster.

## Returns

**out** [array of size (n\_samples, )] The sampled subsets of integer. The subset of selected integer might not be randomized, see the method argument.

# 6.39.44 sklearn.utils.validation.check\_is\_fitted

Perform is\_fitted validation for estimator.

Checks if the estimator is fitted by verifying the presence of "all\_or\_any" of the passed attributes and raises a NotFittedError with the given message.

### **Parameters**

**estimator** [estimator instance.] estimator instance for which the check is performed.

attributes [attribute name(s) given as string or a list/tuple of strings]

```
Eg.: ["coef_", "estimator_", ...], "coef_"
```

**msg** [string] The default error message is, "This %(name)s instance is not fitted yet. Call 'fit' with appropriate arguments before using this method."

For custom messages if "%(name)s" is present in the message string, it is substituted for the estimator name.

Eg.: "Estimator, %(name)s, must be fitted before sparsifying".

**all\_or\_any** [callable, {all, any}, default all] Specify whether all or any of the given attributes must exist.

#### Returns

None

#### Raises

NotFittedError If the attributes are not found.

# 6.39.45 sklearn.utils.validation.check memory

```
sklearn.utils.validation.check_memory(memory)
```

Check that memory is joblib. Memory-like.

joblib.Memory-like means that memory can be converted into a joblib.Memory instance (typically a str denoting the location) or has the same interface (has a cache method).

#### **Parameters**

**memory** [None, str or object with the joblib.Memory interface]

### Returns

**memory** [object with the joblib.Memory interface]

### Raises

ValueError If memory is not joblib.Memory-like.

## 6.39.46 sklearn.utils.validation.check symmetric

```
sklearn.utils.validation.check_symmetric(array, tol=1e-10, raise_warning=True, raise exception=False)
```

Make sure that array is 2D, square and symmetric.

If the array is not symmetric, then a symmetrized version is returned. Optionally, a warning or exception is raised if the matrix is not symmetric.

### **Parameters**

**array** [nd-array or sparse matrix] Input object to check / convert. Must be two-dimensional and square, otherwise a ValueError will be raised.

tol [float] Absolute tolerance for equivalence of arrays. Default = 1E-10.

raise\_warning [boolean (default=True)] If True then raise a warning if conversion is required.

raise\_exception [boolean (default=False)] If True then raise an exception if array is not symmetric.

#### Returns

**array\_sym** [ndarray or sparse matrix] Symmetrized version of the input array, i.e. the average of array and array.transpose(). If sparse, then duplicate entries are first summed and zeros are eliminated.

# 6.39.47 sklearn.utils.validation.column or 1d

```
sklearn.utils.validation.column_or_1d(y, warn=False)
Ravel column or 1d numpy array, else raises an error
```

#### **Parameters**

y [array-like]

warn [boolean, default False] To control display of warnings.

### Returns

y [array]

# 6.39.48 sklearn.utils.validation.has\_fit\_parameter

```
sklearn.utils.validation.has_fit_parameter (estimator, parameter)

Checks whether the estimator's fit method supports the given parameter.
```

### **Parameters**

**estimator** [object] An estimator to inspect.

parameter [str] The searched parameter.

### Returns

**is\_parameter: bool** Whether the parameter was found to be a named parameter of the estimator's fit method.

# **Examples**

```
>>> from sklearn.svm import SVC
>>> has_fit_parameter(SVC(), "sample_weight")
True
```

# 6.39.49 sklearn.utils.testing.assert in

sklearn.utils.testing.assert\_in (member, container, msg=None)

Just like self.assertTrue(a in b), but with a nicer default message.

## 6.39.50 sklearn.utils.testing.assert\_not\_in

```
sklearn.utils.testing.assert_not_in (member, container, msg=None)
Just like self.assertTrue(a not in b), but with a nicer default message.
```

## 6.39.51 sklearn.utils.testing.assert raise message

```
sklearn.utils.testing.assert_raise_message(exceptions, message, function, *args, **kwargs)
```

Helper function to test the message raised in an exception.

Given an exception, a callable to raise the exception, and a message string, tests that the correct exception is raised and that the message is a substring of the error thrown. Used to test that the specific message thrown during an exception is correct.

#### **Parameters**

exceptions [exception or tuple of exception] An Exception object.

**message** [str] The error message or a substring of the error message.

function [callable] Callable object to raise error.

\*args [the positional arguments to function.]

\*\*kwargs [the keyword arguments to function.]

# 6.39.52 sklearn.utils.testing.all estimators

sklearn.utils.testing.all\_estimators(include\_meta\_estimators=None, include\_other=None, type\_filter=None, include\_dont\_test=None)

Get a list of all estimators from sklearn.

This function crawls the module and gets all classes that inherit from BaseEstimator. Classes that are defined in test-modules are not included. By default meta\_estimators such as GridSearchCV are also not included.

### **Parameters**

include\_meta\_estimators [boolean, default=False] Deprecated, ignored. .. deprecated:: 0.21

include\_meta\_estimators has been deprecated and has no effect in 0.21 and will be removed in 0.23.

include\_other [boolean, default=False] Deprecated, ignored. .. deprecated:: 0.21

include\_other has been deprecated and has not effect in 0.21 and will be removed in 0.23.

**type\_filter** [string, list of string, or None, default=None] Which kind of estimators should be returned. If None, no filter is applied and all estimators are returned. Possible values are 'classifier', 'regressor', 'cluster' and 'transformer' to get estimators only of these specific types, or a list of these to get the estimators that fit at least one of the types.

include\_dont\_test [boolean, default=False] Deprecated, ignored. .. deprecated:: 0.21

 $include\_dont\_test$  has been deprecated and has no effect in 0.21 and will be removed in 0.23.

### Returns

**estimators** [list of tuples] List of (name, class), where name is the class name as string and class is the actuall type of the class.

Utilities from joblib:

utils.parallel_backend(backend[, n_jobs])	Change the default backend used by Parallel inside a with
	block.
utils.register_parallel_backend(name, fac-	Register a new Parallel backend factory.
tory)	

## 6.39.53 sklearn.utils.parallel backend

sklearn.utils.parallel\_backend(backend, n\_jobs=-1, \*\*backend\_params)

Change the default backend used by Parallel inside a with block.

If backend is a string it must match a previously registered implementation using the register\_parallel\_backend function.

By default the following backends are available:

- 'loky': single-host, process-based parallelism (used by default),
- 'threading': single-host, thread-based parallelism,
- 'multiprocessing': legacy single-host, process-based parallelism.

'loky' is recommended to run functions that manipulate Python objects. 'threading' is a low-overhead alternative that is most efficient for functions that release the Global Interpreter Lock: e.g. I/O-bound code or CPU-bound code in a few calls to native code that explicitly releases the GIL.

In addition, if the dask and distributed Python packages are installed, it is possible to use the 'dask' backend for better scheduling of nested parallel calls without over-subscription and potentially distribute parallel calls over a networked cluster of several hosts.

Alternatively the backend can be passed directly as an instance.

By default all available workers will be used  $(n_jobs=-1)$  unless the caller passes an explicit value for the  $n_jobs$  parameter.

This is an alternative to passing a backend='backend\_name' argument to the Parallel class constructor. It is particularly useful when calling into library code that uses joblib internally but does not expose the backend argument in its own API.

```
>>> from operator import neg
>>> with parallel_backend('threading'):
... print(Parallel()(delayed(neg)(i + 1) for i in range(5)))
...
[-1, -2, -3, -4, -5]
```

Warning: this function is experimental and subject to change in a future version of joblib.

New in version 0.10.

# 6.39.54 sklearn.utils.register\_parallel\_backend

```
sklearn.utils.register_parallel_backend (name, factory, make_default=False)
Register a new Parallel backend factory.
```

The new backend can then be selected by passing its name as the backend argument to the Parallel class. Moreover, the default backend can be overwritten globally by setting make\_default=True.

The factory can be any callable that takes no argument and return an instance of ParallelBackendBase.

Warning: this function is experimental and subject to change in a future version of joblib.

New in version 0.10.

# 6.40 Recently deprecated

# 6.40.1 To be removed in 0.23

utils.Memory(*args, **kwargs)	Attributes	
utils.Parallel(*args, **kwargs)		
	Methods	

## sklearn.utils.Memory

Warning: DEPRECATED	
---------------------	--

class sklearn.utils.Memory (\*args, \*\*kwargs)

**Attributes** 

cachedir

### **Methods**

cache(self[, func, ignore, verbose, mmap_mode])	Decorates the given function func to only compute its
	return value for input arguments not cached on disk.
clear(self[, warn])	Erase the complete cache directory.
eval(self, func, \*args, \*\*kwargs)	Eval function func with arguments *args and
	**kwargs, in the context of the memory.
<pre>format(self, obj[, indent])</pre>	Return the formatted representation of the object.
reduce_size(self)	Remove cache elements to make cache size fit in
	bytes_limit.

debug	
warn	

\_\_\_init\_\_\_(\*args, \*\*kwargs)

DEPRECATED: deprecated in version 0.20.1 to be removed in version 0.23. Please import this functionality directly from joblib, which can be installed with: pip install joblib.

 $\verb+cache+ (self, func=None, ignore=None, verbose=None, mmap\_mode=False)$ 

Decorates the given function func to only compute its return value for input arguments not cached on disk.

## **Parameters**

func: callable, optional The function to be decorated

**ignore:** list of strings A list of arguments name to ignore in the hashing

**verbose: integer, optional** The verbosity mode of the function. By default that of the memory object is used.

mmap\_mode: {None, 'r+', 'r', 'w+', 'c'}, optional The memmapping mode used when loading from cache numpy arrays. See numpy.load for the meaning of the arguments. By default that of the memory object is used.

### Returns

**decorated\_func:** MemorizedFunc object The returned object is a MemorizedFunc object, that is callable (behaves like a function), but offers extra methods for cache lookup and management. See the documentation for joblib.memory.MemorizedFunc.

## clear (self, warn=True)

Erase the complete cache directory.

## eval (self, func, \*args, \*\*kwargs)

Eval function func with arguments \*args and \*\*kwargs, in the context of the memory.

This method works similarly to the builtin apply, except that the function is called only if the cache is not up to date.

### format (self, obj, indent=0)

Return the formatted representation of the object.

#### reduce\_size (self)

Remove cache elements to make cache size fit in bytes\_limit.

#### sklearn.utils.Parallel

## Warning: DEPRECATED

class sklearn.utils.Parallel(\*args, \*\*kwargs)

### **Methods**

call(self, iterable)	
dispatch_next(self)	Dispatch more data for parallel processing
dispatch_one_batch(self, iterator)	Prefetch the tasks for the next batch and dispatch them.
<pre>format(self, obj[, indent])</pre>	Return the formatted representation of the object.
print_progress(self)	Display the process of the parallel execution only a frac-
	tion of time, controlled by self.verbose.

debug	
retrieve	
warn	

\_\_\_init\_\_\_(\*args, \*\*kwargs)

DEPRECATED: deprecated in version 0.20.1 to be removed in version 0.23. Please import this function-

ality directly from joblib, which can be installed with: pip install joblib.

## dispatch\_next(self)

Dispatch more data for parallel processing

This method is meant to be called concurrently by the multiprocessing callback. We rely on the thread-safety of dispatch\_one\_batch to protect against concurrent consumption of the unprotected iterator.

## dispatch\_one\_batch (self, iterator)

Prefetch the tasks for the next batch and dispatch them.

The effective size of the batch is computed here. If there are no more jobs to dispatch, return False, else return True.

The iterator consumption and dispatching is protected by the same lock so calling this function should be thread safe.

## format (self, obj, indent=0)

Return the formatted representation of the object.

## print\_progress(self)

Display the process of the parallel execution only a fraction of time, controlled by self.verbose.

utils.cpu count()	DEPRECATED: deprecated in version 0.20.1 to be re-
	moved in version 0.23.
<pre>utils.delayed(function[, check_pickle])</pre>	DEPRECATED: deprecated in version 0.20.1 to be re-
	moved in version 0.23.
metrics.calinski_harabaz_score(X, labels)	DEPRECATED: Function 'calinski_harabaz_score' has
	been renamed to 'calinski_harabasz_score' and will be re-
	moved in version 0.23.
metrics.jaccard_similarity_score(y_true,	Jaccard similarity coefficient score
y_pred)	
linear_model.logistic_regression_path(X,	DEPRECATED: logistic_regression_path was deprecated
y)	in version 0.21 and will be removed in version 0.23.0

## sklearn.utils.cpu\_count

# Warning: DEPRECATED

### sklearn.utils.cpu\_count()

DEPRECATED: deprecated in version 0.20.1 to be removed in version 0.23. Please import this functionality directly from joblib, which can be installed with: pip install joblib.

Return the number of CPUs.

## sklearn.utils.delayed

## Warning: DEPRECATED

## sklearn.utils.delayed(function, check\_pickle=None)

DEPRECATED: deprecated in version 0.20.1 to be removed in version 0.23. Please import this functionality directly from joblib, which can be installed with: pip install joblib.

Decorator used to capture the arguments of a function.

### sklearn.metrics.calinski\_harabaz\_score

## Warning: DEPRECATED

sklearn.metrics.calinski\_harabaz\_score(X, labels)

DEPRECATED: Function 'calinski\_harabaz\_score' has been renamed to 'calinski\_harabasz\_score' and will be removed in version 0.23.

# sklearn.metrics.jaccard\_similarity\_score

## Warning: DEPRECATED

sklearn.metrics.jaccard\_similarity\_score(y\_true, y\_pred, normalize=True, sample\_weight=None)

Jaccard similarity coefficient score

Deprecated since version 0.21: This is deprecated to be removed in 0.23, since its handling of binary and multiclass inputs was broken. <code>jaccard\_score</code> has an API that is consistent with precision\_score, f\_score, etc.

Read more in the *User Guide*.

### **Parameters**

- **y\_true** [1d array-like, or label indicator array / sparse matrix] Ground truth (correct) labels.
- **y\_pred** [1d array-like, or label indicator array / sparse matrix] Predicted labels, as returned by a classifier.

**normalize** [bool, optional (default=True)] If False, return the sum of the Jaccard similarity coefficient over the sample set. Otherwise, return the average of Jaccard similarity coefficient.

**sample\_weight** [array-like of shape = [n\_samples], optional] Sample weights.

### Returns

**score** [float] If normalize == True, return the average Jaccard similarity coefficient, else it returns the sum of the Jaccard similarity coefficient over the sample set.

The best performance is 1 with normalize == True and the number of samples with normalize == False.

### See also:

accuracy\_score, hamming\_loss, zero\_one\_loss

### **Notes**

In binary and multiclass classification, this function is equivalent to the accuracy\_score. It differs in the multilabel classification problem.

#### References

[1]

## sklearn.linear\_model.logistic\_regression\_path

### Warning: DEPRECATED

```
sklearn.linear\_model.logistic\_regression\_path (X, y, pos\_class=None, Cs=10, fit\_intercept=True, max\_iter=100, tol=0.0001, verbose=0, solver='lbfgs', coef=None, class\_weight=None, dual=False, penalty='l2', intercept\_scaling=1.0, multi\_class='warn', random\_state=None, check\_input=True, max\_squared\_sum=None, sample weight=None, l1 ratio=None)
```

DEPRECATED: logistic\_regression\_path was deprecated in version 0.21 and will be removed in version 0.23.0

## Compute a Logistic Regression model for a list of regularization parameters.

This is an implementation that uses the result of the previous model to speed up computations along the set of solutions, making it faster than sequentially calling LogisticRegression for the different parameters. Note that there will be no speedup with liblinear solver, since it does not handle warm-starting.

Deprecated since version 0.21: logistic\_regression\_path was deprecated in version 0.21 and will be removed in 0.23.

Read more in the User Guide.

#### **Parameters**

**X** [array-like or sparse matrix, shape (n\_samples, n\_features)]

Input data.

- y [array-like, shape (n\_samples,) or (n\_samples, n\_targets)] Input data, target values.
- **pos\_class** [int, None] The class with respect to which we perform a one-vs-all fit. If None, then it is assumed that the given problem is binary.
- **Cs** [int | array-like, shape (n\_cs,)] List of values for the regularization parameter or integer specifying the number of regularization parameters that should be used. In this case, the parameters will be chosen in a logarithmic scale between 1e-4 and 1e4.
- **fit\_intercept** [bool] Whether to fit an intercept for the model. In this case the shape of the returned array is (n\_cs, n\_features + 1).

max\_iter [int] Maximum number of iterations for the solver.

- tol [float] Stopping criterion. For the newton-cg and lbfgs solvers, the iteration will stop when  $\max\{|g_i| | i = 1, ..., n\} \le tol where g_i is the i-th component of the gradient.$
- **verbose** [int] For the liblinear and lbfgs solvers set verbose to any positive number for verbosity.

**solver** [{'lbfgs', 'newton-cg', 'liblinear', 'sag', 'saga'}] Numerical solver to use.

- **coef** [array-like, shape (n\_features,), default None] Initialization value for coefficients of logistic regression. Useless for liblinear solver.
- class\_weight [dict or 'balanced', optional] Weights associated with classes in the form
  {class\_label: weight}. If not given, all classes are supposed to have weight
  one.

The "balanced" mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as  $n_samples / (n_classes * np.bincount(y))$ .

Note that these weights will be multiplied with sample\_weight (passed through the fit method) if sample\_weight is specified.

- **dual** [bool] Dual or primal formulation. Dual formulation is only implemented for 12 penalty with liblinear solver. Prefer dual=False when n\_samples > n\_features.
- **penalty** [str, '11', '12', or 'elasticnet'] Used to specify the norm used in the penalization. The 'newton-cg', 'sag' and 'lbfgs' solvers support only 12 penalties. 'elasticnet' is only supported by the 'saga' solver.
- intercept\_scaling [float, default 1.] Useful only when the solver 'liblinear' is used and
   self.fit\_intercept is set to True. In this case, x becomes [x, self.intercept\_scaling],
   i.e. a "synthetic" feature with constant value equal to intercept\_scaling is ap pended to the instance vector. The intercept becomes intercept\_scaling \*
   synthetic\_feature\_weight.

Note! the synthetic feature weight is subject to 11/12 regularization as all other features. To lessen the effect of regularization on synthetic feature weight (and therefore on the intercept) intercept\_scaling has to be increased.

multi\_class [str, {'ovr', 'multinomial', 'auto'}, default: 'ovr'] If the option chosen is 'ovr', then a binary problem is fit for each label. For 'multinomial' the loss minimised is the multinomial loss fit across the entire probability distribution, even when the data is binary. 'multinomial' is unavailable when solver='liblinear'. 'auto' selects 'ovr' if the data is binary, or if solver='liblinear', and otherwise selects 'multinomial'.

New in version 0.18: Stochastic Average Gradient descent solver for 'multinomial' case.

Changed in version 0.20: Default will change from 'ovr' to 'auto' in 0.22.

- random\_state [int, RandomState instance or None, optional, default None] The seed of the pseudo random number generator to use when shuffling the data. If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == 'sag' or 'liblinear'.
- **check\_input** [bool, default True] If False, the input arrays X and y will not be checked.
- max\_squared\_sum [float, default None] Maximum squared sum of X over samples. Used only in SAG solver. If None, it will be computed, going through all the samples. The value should be precomputed to speed up cross validation.
- **sample\_weight** [array-like, shape(n\_samples,) optional] Array of weights that are assigned to individual samples. If not provided, then each sample is given unit weight.
- I1\_ratio [float or None, optional (default=None)] The Elastic-Net mixing parameter,
  with 0 <= l1\_ratio <= 1. Only used if penalty='elasticnet'. Setting
  l1\_ratio=0 is equivalent to using penalty='l2', while setting l1\_ratio=1 is
  equivalent to using penalty='l1'. For 0 < l1\_ratio <1, the penalty is a combination of L1 and L2.</pre>

#### Returns

```
coefs [ndarray, shape (n_cs, n_features) or (n_cs, n_features + 1)]
```

List of coefficients for the Logistic Regression model. If fit\_intercept is set to True then the second dimension will be  $n_{\text{features}} + 1$ , where the last item represents the intercept. For multiclass='multinomial', the shape is  $(n_{\text{classes}}, n_{\text{cs}}, n_{\text{features}})$  or  $(n_{\text{classes}}, n_{\text{cs}}, n_{\text{features}} + 1)$ .

Cs [ndarray] Grid of Cs used for cross-validation.

**n\_iter** [array, shape (n\_cs,)] Actual number of iteration for each Cs.

#### **Notes**

You might get slightly different results with the solver liblinear than with the others since this uses LIBLINEAR which penalizes the intercept.

Changed in version 0.19: The "copy" parameter was removed.

<pre>ensemble.partial_dependence. partial_dependence()</pre>	DEPRECATED: The function ensemble.partial_dependence has been deprecated in favour of inspection.partial_dependence in 0.21 and will be removed in 0.23.
ensemble.partial_dependence.	DEPRECATED: The function ensem-
<pre>plot_partial_dependence()</pre>	ble.plot_partial_dependence has been deprecated in
	favour of sklearn.inspection.plot_partial_dependence in
	0.21 and will be removed in 0.23.

# sklearn.ensemble.partial\_dependence.partial\_dependence

```
sklearn.ensemble.partial_dependence.partial_dependence(gbrt, target\_variables, grid=None, X=None, percentiles=(0.05, 0.95), grid resolution=100)
```

DEPRECATED: The function ensemble.partial\_dependence has been deprecated in favour of inspection.partial\_dependence in 0.21 and will be removed in 0.23.

Partial dependence of target\_variables.

Partial dependence plots show the dependence between the joint values of the target\_variables and the function represented by the gbrt.

Read more in the *User Guide*.

Deprecated since version 0.21: This function was deprecated in version 0.21 in favor of sklearn. inspection.partial\_dependence and will be removed in 0.23.

## **Parameters**

gbrt [BaseGradientBoosting]

A fitted gradient boosting model.

**target\_variables** [array-like, dtype=int] The target features for which the partial dependency should be computed (size should be smaller than 3 for visual renderings).

- grid [array-like, shape=(n\_points, len(target\_variables))] The grid of
   target\_variables values for which the partial dependency should be evaluated (either grid or X must be specified).
- X [array-like, shape=(n\_samples, n\_features)] The data on which gbrt was trained. It is used to generate a grid for the target\_variables. The grid comprises grid\_resolution equally spaced points between the two percentiles.

**percentiles** [(low, high), default=(0.05, 0.95)] The lower and upper percentile used create the extreme values for the grid. Only if X is not None.

grid\_resolution [int, default=100] The number of equally spaced points on the grid.

#### Returns

```
pdp [array, shape=(n_classes, n_points)]
```

The partial dependence function evaluated on the grid. For regression and binary classification  $n\_classes==1$ .

**axes** [seq of ndarray or None] The axes with which the grid has been created or None if the grid has been given.

# **Examples**

```
>>> samples = [[0, 0, 2], [1, 0, 0]]
>>> labels = [0, 1]
>>> from sklearn.ensemble import GradientBoostingClassifier
>>> gb = GradientBoostingClassifier(random_state=0).fit(samples, labels)
>>> kwargs = dict(X=samples, percentiles=(0, 1), grid_resolution=2)
>>> partial_dependence(gb, [0], **kwargs)
(array([[-4.52..., 4.52...]]), [array([ 0., 1.])])
```

## sklearn.ensemble.partial\_dependence.plot\_partial\_dependence

```
sklearn.ensemble.partial_dependence.plot_partial_dependence (gbrt, X, features, feature_names=None, label=None, n_cols=3, grid_resolution=100, percentiles=(0.05, 0.95), n_jobs=None, verbose=0, ax=None, line_kw=None, contour_kw=None, contour_kw=None, *fig_kw)

DEPRECATED: The function ensemble plot partial dependence has been deprecated in favour of the function of
```

DEPRECATED: The function ensemble.plot\_partial\_dependence has been deprecated in favour of sklearn.inspection.plot\_partial\_dependence in 0.21 and will be removed in 0.23.

Partial dependence plots for features.

The len(features) plots are arranged in a grid with n\_cols columns. Two-way partial dependence plots are plotted as contour plots.

Read more in the User Guide.

Deprecated since version 0.21: This function was deprecated in version 0.21 in favor of sklearn. inspection.plot\_partial\_dependence and will be removed in 0.23.

### **Parameters**

gbrt [BaseGradientBoosting]

A fitted gradient boosting model.

**X** [array-like, shape=(n\_samples, n\_features)] The data on which gbrt was trained.

**features** [seq of ints, strings, or tuples of ints or strings] If seq[i] is an int or a tuple with one int value, a one-way PDP is created; if seq[i] is a tuple of two ints, a two-way PDP is created. If feature\_names is specified and seq[i] is an int, seq[i] must be < len(feature\_names). If seq[i] is a string, feature\_names must be specified, and seq[i] must be in feature\_names.

**feature\_names** [seq of str] Name of each feature; feature\_names[i] holds the name of the feature with index i.

**label** [object] The class label for which the PDPs should be computed. Only if gbrt is a multi-class model. Must be in gbrt.classes\_.

**n\_cols** [int] The number of columns in the grid plot (default: 3).

grid\_resolution [int, default=100] The number of equally spaced points on the axes.

**percentiles** [(low, high), default=(0.05, 0.95)] The lower and upper percentile used to create the extreme values for the PDP axes.

n\_jobs [int or None, optional (default=None)] None means 1 unless in a joblib.
parallel\_backend context. -1 means using all processors. See Glossary for more
details.

verbose [int] Verbose output during PD computations. Defaults to 0.

ax [Matplotlib axis object, default None] An axis object onto which the plots will be drawn.

line\_kw [dict] Dict with keywords passed to the matplotlib.pyplot.plot call. For one-way partial dependence plots.

contour\_kw [dict] Dict with keywords passed to the matplotlib.pyplot.plot call.
For two-way partial dependence plots.

\*\*fig\_kw [dict] Dict with keywords passed to the figure() call. Note that all keywords not recognized above will be automatically included here.

### Returns

**fig** [figure]

The Matplotlib Figure object.

axs [seq of Axis objects] A seq of Axis objects, one for each subplot.

# **Examples**

```
>>> from sklearn.datasets import make_friedman1
>>> from sklearn.ensemble import GradientBoostingRegressor
>>> X, y = make_friedman1()
>>> clf = GradientBoostingRegressor(n_estimators=10).fit(X, y)
```

```
>>> fig, axs = plot_partial_dependence(clf, X, [0, (0, 1)])
...
```

# 6.40.2 To be removed in 0.22

covariance.GraphLasso(*args, **kwargs)	Sparse inverse covariance estimation with an 11-penalized estimator.
covariance.GraphLassoCV(*args, **kwargs)	Sparse inverse covariance w/ cross-validated choice of the
	11 penalty.
preprocessing.Imputer(*args, **kwargs)	Imputation transformer for completing missing values.
utils.testing.mock_mldata_urlopen(*args,	Object that mocks the urlopen function to fake requests to
)	mldata.

# sklearn.covariance.GraphLasso

# Warning: DEPRECATED

class sklearn.covariance.GraphLasso(\*args, \*\*kwargs)

Sparse inverse covariance estimation with an 11-penalized estimator.

This class implements the Graphical Lasso algorithm.

Read more in the *User Guide*.

## **Parameters**

**alpha** [positive float, default 0.01] The regularization parameter: the higher alpha, the more regularization, the sparser the inverse covariance.

**mode** [{'cd', 'lars'}, default 'cd'] The Lasso solver to use: coordinate descent or LARS. Use LARS for very sparse underlying graphs, where p > n. Elsewhere prefer cd which is more numerically stable.

**tol** [positive float, default 1e-4] The tolerance to declare convergence: if the dual gap goes below this value, iterations are stopped.

enet\_tol [positive float, optional] The tolerance for the elastic net solver used to calculate the descent direction. This parameter controls the accuracy of the search direction for a given column update, not of the overall parameter estimate. Only used for mode='cd'.

max\_iter [integer, default 100] The maximum number of iterations.

**verbose** [boolean, default False] If verbose is True, the objective function and dual gap are plotted at each iteration.

**assume\_centered** [boolean, default False] If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data are centered before computation.

## **Attributes**

covariance\_ [array-like, shape (n\_features, n\_features)] Estimated covariance matrix
 precision\_ [array-like, shape (n\_features, n\_features)] Estimated pseudo inverse matrix.
 n\_iter\_ [int] Number of iterations run.

## See also:

graph\_lasso, GraphLassoCV

#### **Methods**

<pre>error_norm(self, comp_cov[, norm, scaling,])</pre>	Computes the Mean Squared Error between two covari-
	ance estimators.
fit(self, X[, y])	Fits the GraphicalLasso model to X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Getter for the precision matrix.
mahalanobis(self, X)	Computes the squared Mahalanobis distances of given
	observations.
score(self, X_test[, y])	Computes the log-likelihood of a Gaussian data set with
	self.covariance_ as an estimator of its covari-
	ance matrix.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_\_init\_\_\_(\*args, \*\*kwargs)

DEPRECATED: The 'GraphLasso' was renamed to 'GraphicalLasso' in version 0.20 and will be removed in 0.22.

error\_norm(self, comp\_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

# **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

norm [str] The type of norm used to compute the error. Available error types: - 'frobenius'
 (default): sqrt(tr(A^t.A)) - 'spectral': sqrt(max(eigenvalues(A^t.A)) where A is the error
 (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

**squared** [bool] Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

#### Returns

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp\_cov covariance estimators.

**fit** (self, X, y=None)

Fits the GraphicalLasso model to X.

## **Parameters**

- **X** [ndarray, shape (n\_samples, n\_features)] Data from which to compute the covariance estimate
- y [(ignored)]

get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

#### Returns

**params** [mapping of string to any] Parameter names mapped to their values.

## get\_precision(self)

Getter for the precision matrix.

## **Returns**

precision\_ [array-like] The precision matrix associated to the current covariance object.

# mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

#### Returns

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

```
score (self, X_test, y=None)
```

Computes the log-likelihood of a Gaussian data set with self.covariance\_ as an estimator of its covariance matrix.

## **Parameters**

**X\_test** [array-like, shape = [n\_samples, n\_features]] Test data of which we compute the likelihood, where n\_samples is the number of samples and n\_features is the number of features. X\_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y not used, present for API consistence purpose.

# Returns

**res** [float] The likelihood of the data set with self.covariance\_ as an estimator of its covariance matrix.

```
set_params (self, **params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

## Returns

self

# sklearn.covariance.GraphLassoCV

Warning: DEPRECATED

class sklearn.covariance.GraphLassoCV(\*args, \*\*kwargs)

Sparse inverse covariance w/ cross-validated choice of the 11 penalty.

See glossary entry for cross-validation estimator.

This class implements the Graphical Lasso algorithm.

Read more in the *User Guide*.

#### **Parameters**

- **alphas** [integer, or list positive float, optional] If an integer is given, it fixes the number of points on the grids of alpha to be used. If a list is given, it gives the grid to be used. See the notes in the class docstring for more details.
- **n\_refinements** [strictly positive integer] The number of times the grid is refined. Not used if explicit values of alphas are passed.
- **cv** [int, cross-validation generator or an iterable, optional] Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross-validation,
  - integer, to specify the number of folds.
  - CV splitter,
  - An iterable yielding (train, test) splits as arrays of indices.

For integer/None inputs KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

Changed in version 0.20: cv default value if None will change from 3-fold to 5-fold in v0.22.

- **tol** [positive float, optional] The tolerance to declare convergence: if the dual gap goes below this value, iterations are stopped.
- enet\_tol [positive float, optional] The tolerance for the elastic net solver used to calculate the descent direction. This parameter controls the accuracy of the search direction for a given column update, not of the overall parameter estimate. Only used for mode='cd'.
- max\_iter [integer, optional] Maximum number of iterations.
- **mode** [{'cd', 'lars'}] The Lasso solver to use: coordinate descent or LARS. Use LARS for very sparse underlying graphs, where number of features is greater than number of samples. Elsewhere prefer cd which is more numerically stable.
- **n\_jobs** [int or None, optional (default=None)] number of jobs to run in parallel. None means 1 unless in a joblib.parallel\_backend context. -1 means using all processors. See *Glossary* for more details.
- **verbose** [boolean, optional] If verbose is True, the objective function and duality gap are printed at each iteration.
- **assume\_centered** [Boolean] If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data are centered before computation.

# Attributes

**covariance** [numpy.ndarray, shape (n\_features, n\_features)] Estimated covariance matrix.

**precision**\_ [numpy.ndarray, shape (n\_features, n\_features)] Estimated precision matrix (inverse covariance).

**alpha**\_ [float] Penalization parameter selected.

cv\_alphas\_ [list of float] All penalization parameters explored.

**grid\_scores**\_ [2D numpy.ndarray (n\_alphas, n\_folds)] Log-likelihood score on left-out data across folds.

**n\_iter\_** [int] Number of iterations run for the optimal alpha.

## See also:

graph\_lasso, GraphLasso

# **Notes**

The search for the optimal penalization parameter (alpha) is done on an iteratively refined grid: first the cross-validated scores on a grid are computed, then a new refined grid is centered around the maximum, and so on.

One of the challenges which is faced here is that the solvers can fail to converge to a well-conditioned estimate. The corresponding values of alpha then come out as missing values, but the optimum may be close to these missing values.

# **Methods**

error_norm(self, comp_cov[, norm, scaling,])	Computes the Mean Squared Error between two covari-
	ance estimators.
fit(self, X[, y])	Fits the GraphicalLasso covariance model to X.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
get_precision(self)	Getter for the precision matrix.
mahalanobis(self, X)	Computes the squared Mahalanobis distances of given
	observations.
score(self, X_test[, y])	Computes the log-likelihood of a Gaussian data set with
	self.covariance_ as an estimator of its covari-
	ance matrix.
set_params(self, \*\*params)	Set the parameters of this estimator.

\_\_\_init\_\_\_(\*args, \*\*kwargs)

DEPRECATED: The 'GraphLassoCV' was renamed to 'GraphicalLassoCV' in version 0.20 and will be removed in 0.22.

error\_norm(self, comp\_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

# **Parameters**

**comp\_cov** [array-like, shape = [n\_features, n\_features]] The covariance to compare with.

norm [str] The type of norm used to compute the error. Available error types: - 'frobenius'
 (default): sqrt(tr(A^t.A)) - 'spectral': sqrt(max(eigenvalues(A^t.A)) where A is the error
 (comp\_cov - self.covariance\_).

**scaling** [bool] If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.

squared [bool] Whether to compute the squared error norm or the error norm. If True

(default), the squared error norm is returned. If False, the error norm is returned.

# Returns

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp\_cov covariance estimators.

**fit** (self, X, y=None)

Fits the Graphical Lasso covariance model to X.

## **Parameters**

**X** [ndarray, shape (n\_samples, n\_features)] Data from which to compute the covariance estimate

y [(ignored)]

# get\_params (self, deep=True)

Get parameters for this estimator.

#### **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

# get\_precision(self)

Getter for the precision matrix.

#### Returns

precision\_ [array-like] The precision matrix associated to the current covariance object.

# mahalanobis(self, X)

Computes the squared Mahalanobis distances of given observations.

## **Parameters**

**X** [array-like, shape = [n\_samples, n\_features]] The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

## **Returns**

**dist** [array, shape = [n\_samples,]] Squared Mahalanobis distances of the observations.

```
score(self, X test, y=None)
```

Computes the log-likelihood of a Gaussian data set with self.covariance\_ as an estimator of its covariance matrix.

### **Parameters**

**X\_test** [array-like, shape = [n\_samples, n\_features]] Test data of which we compute the likelihood, where n\_samples is the number of samples and n\_features is the number of features. X\_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y not used, present for API consistence purpose.

# Returns

**res** [float] The likelihood of the data set with self.covariance\_ as an estimator of its covariance matrix.

## set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

#### Returns

self

# sklearn.preprocessing.lmputer

# Warning: DEPRECATED

class sklearn.preprocessing.Imputer(\*args, \*\*kwargs)

Imputation transformer for completing missing values.

Read more in the *User Guide*.

## **Parameters**

missing\_values [integer or "NaN", optional (default="NaN")] The placeholder for the missing values. All occurrences of missing\_values will be imputed. For missing values encoded as np.nan, use the string value "NaN".

strategy [string, optional (default="mean")] The imputation strategy.

- If "mean", then replace missing values using the mean along the axis.
- If "median", then replace missing values using the median along the axis.
- If "most\_frequent", then replace missing using the most frequent value along the axis.

**axis** [integer, optional (default=0)] The axis along which to impute.

- If axis=0, then impute along columns.
- If axis=1, then impute along rows.

**verbose** [integer, optional (default=0)] Controls the verbosity of the imputer.

**copy** [boolean, optional (default=True)] If True, a copy of X will be created. If False, imputation will be done in-place whenever possible. Note that, in the following cases, a new copy will always be made, even if copy=False:

- If X is not an array of floating values;
- If X is sparse and missing\_values=0;
- If axis=0 and X is encoded as a CSR matrix;
- If axis=1 and X is encoded as a CSC matrix.

## **Attributes**

statistics\_ [array of shape (n\_features,)] The imputation fill value for each feature if axis == 0.

# **Notes**

- When axis=0, columns which only contained missing values at fit are discarded upon transform.
- When axis=1, an exception is raised if there are rows for which it is not possible to fill in the missing values (e.g., because they only contain missing values).

## **Methods**

fit(self, X[, y])	Fit the imputer on X.
$fit_transform(self, X[, y])$	Fit to data, then transform it.
<pre>get_params(self[, deep])</pre>	Get parameters for this estimator.
<pre>set_params(self, \*\*params)</pre>	Set the parameters of this estimator.
transform(self, X)	Impute all missing values in X.

\_\_\_init\_\_\_(\*args, \*\*kwargs)

DEPRECATED: Imputer was deprecated in version 0.20 and will be removed in 0.22. Import impute. SimpleImputer from sklearn instead.

**fit** (*self*, *X*, *y=None*)

Fit the imputer on X.

#### **Parameters**

X [{array-like, sparse matrix}, shape (n\_samples, n\_features)] Input data, where n\_samples is the number of samples and n\_features is the number of features.

# Returns

**self** [Imputer]

**fit** transform(self, X, y=None, \*\*fit params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit\_params and returns a transformed version of X.

## **Parameters**

**X** [numpy array of shape [n\_samples, n\_features]] Training set.

y [numpy array of shape [n\_samples]] Target values.

# Returns

**X\_new** [numpy array of shape [n\_samples, n\_features\_new]] Transformed array.

get\_params (self, deep=True)

Get parameters for this estimator.

## **Parameters**

**deep** [boolean, optional] If True, will return the parameters for this estimator and contained subobjects that are estimators.

# Returns

params [mapping of string to any] Parameter names mapped to their values.

set\_params (self, \*\*params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_\_<parameter> so that it's possible to update each component of a nested object.

# Returns

self

transform(self, X)

Impute all missing values in X.

## **Parameters**

X [{array-like, sparse matrix}, shape = [n\_samples, n\_features]] The input data to complete.

# sklearn.utils.testing.mock\_mldata\_urlopen

# Warning: DEPRECATED

class sklearn.utils.testing.mock\_mldata\_urlopen(\*args, \*\*kwargs)

Object that mocks the urlopen function to fake requests to mldata.

When requesting a dataset with a name that is in mock\_datasets, this object creates a fake dataset in a StringIO object and returns it. Otherwise, it raises an HTTPError.

Deprecated since version 0.20: Will be removed in version 0.22

## **Parameters**

mock\_datasets [dict] A dictionary of {dataset\_name: data\_dict}, or {dataset\_name: (data\_dict, ordering). data\_dict itself is a dictionary of {column\_name: data\_array}, and ordering is a list of column\_names to determine the ordering in the data set (see fake\_mldata for details).

# **Methods**

call(self, urlname)	Parameters		
init(*args, **kwargs)  DEPRECATED: deprecated in version 0.20 to be removed in version 0.22			
covariance.graph_lasso(emp_cov, alpha[,])	DEPRECATED: The 'graph_lasso' was renamed to		
	'graphical_lasso' in version 0.20 and will be removed in		
	0.22.		
datasets.fetch_mldata(dataname[,])	DEPRECATED: fetch_mldata was deprecated in version		
	0.20 and will be removed in version 0.22.		
datasets.mldata_filename(dataname)	DEPRECATED: mldata_filename was deprecated in ver-		
	sion 0.20 and will be removed in version 0.22.		

# sklearn.covariance.graph lasso

# Warning: DEPRECATED

```
sklearn.covariance.graph_lasso(emp_cov, alpha, cov_init=None, mode='cd', tol=0.0001, enet_tol=0.0001, max_iter=100, verbose=False, return_costs=False, eps=2.220446049250313e-16, return n iter=False)
```

DEPRECATED: The 'graph\_lasso' was renamed to 'graphical\_lasso' in version 0.20 and will be removed in 0.22.

11-penalized covariance estimator

Read more in the *User Guide*.

#### **Parameters**

```
emp_cov [2D ndarray, shape (n_features, n_features)]
```

Empirical covariance from which to compute the covariance estimate.

**alpha** [positive float] The regularization parameter: the higher alpha, the more regularization, the sparser the inverse covariance.

**cov\_init** [2D array (n\_features, n\_features), optional] The initial guess for the covariance.

**mode** [{'cd', 'lars'}] The Lasso solver to use: coordinate descent or LARS. Use LARS for very sparse underlying graphs, where p > n. Elsewhere prefer cd which is more numerically stable.

**tol** [positive float, optional] The tolerance to declare convergence: if the dual gap goes below this value, iterations are stopped.

**enet\_tol** [positive float, optional] The tolerance for the elastic net solver used to calculate the descent direction. This parameter controls the accuracy of the search direction for a given column update, not of the overall parameter estimate. Only used for mode='cd'.

max\_iter [integer, optional] The maximum number of iterations.

**verbose** [boolean, optional] If verbose is True, the objective function and dual gap are printed at each iteration.

**return\_costs** [boolean, optional] If return\_costs is True, the objective function and dual gap at each iteration are returned.

**eps** [float, optional] The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems.

return\_n\_iter [bool, optional] Whether or not to return the number of iterations.

# Returns

```
covariance [2D ndarray, shape (n_features, n_features)]
```

The estimated covariance matrix.

**precision** [2D ndarray, shape (n\_features, n\_features)] The estimated (sparse) precision matrix.

**costs** [list of (objective, dual\_gap) pairs] The list of values of the objective function and the dual gap at each iteration. Returned only if return\_costs is True.

**n\_iter** [int] Number of iterations. Returned only if return\_n\_iter is set to True.

#### **Notes**

The algorithm employed to solve this problem is the GLasso algorithm, from the Friedman 2008 Biostatistics paper. It is the same algorithm as in the R glasso package.

One possible difference with the glasso R package is that the diagonal coefficients are not penalized.

# sklearn.datasets.fetch\_mldata

# Warning: DEPRECATED

sklearn.datasets.fetch\_mldata(dataname, target\_name='label', data\_name='data', transpose\_data=True, data\_home=None)

DEPRECATED: fetch\_mldata was deprecated in version 0.20 and will be removed in version 0.22. Please use fetch\_openml.

Fetch an mldata.org data set

mldata.org is no longer operational.

If the file does not exist yet, it is downloaded from mldata.org.

mldata.org does not have an enforced convention for storing data or naming the columns in a data set. The default behavior of this function works well with the most common cases:

- 1. data values are stored in the column 'data', and target values in the column 'label'
- 2. alternatively, the first column stores target values, and the second data values
- 3. the data array is stored as n\_features x n\_samples, and thus needs to be transposed to match the sklearn standard

Keyword arguments allow to adapt these defaults to specific data sets (see parameters target\_name, data\_name, transpose\_data, and the examples below).

mldata.org data sets may have multiple columns, which are stored in the Bunch object with their original name.

Deprecated since version 0.20: Will be removed in version 0.22

#### **Parameters**

## dataname [str]

Name of the data set on mldata.org, e.g.: "leukemia", "Whistler Daily Snowfall", etc. The raw name is automatically converted to a mldata.org URL.

**target\_name** [optional, default: 'label'] Name or index of the column containing the target values.

data\_name [optional, default: 'data'] Name or index of the column containing the data.

**transpose\_data** [optional, default: True] If True, transpose the downloaded data array.

**data\_home** [optional, default: None] Specify another download and cache folder for the data sets. By default all scikit-learn data is stored in '~/scikit\_learn\_data' subfolders.

## Returns

data [Bunch] Dictionary-like object, the interesting attributes are: 'data', the data to learn, 'target', the classification labels, 'DESCR', the full description of the dataset, and 'COL\_NAMES', the original names of the dataset columns.

# sklearn.datasets.mldata\_filename

# Warning: DEPRECATED

# sklearn.datasets.mldata\_filename(dataname)

DEPRECATED: mldata\_filename was deprecated in version 0.20 and will be removed in version 0.22. Please use fetch\_openml.

Convert a raw name for a data set in a mldata.org filename.

Deprecated since version 0.20: Will be removed in version 0.22

# **Parameters**

dataname [str] Name of dataset

## Returns

**fname** [str] The converted dataname.