

## Question 1

```
import itertools

tasks = ['a1', 'a2', 'b1', 'b2', 'b3', 'c1', 'c2', 'c3', 'd1', 'd2']

def main():
    perms = itertools.permutations(tasks)
    perms = filter(is_in_order, perms)
    permList = list(perms)
    valid_order = len(permList)
    print("Ordered permutations: ", valid_order)
    print(permList[0])
    permList = list(filter(is_valid, permList))
    print(permList[0])
    valid_constraint = len(permList)
    print("Valid permutations: ", valid_constraint)

    print(valid_constraint / valid_order)

def is_in_order(perm: list[str]) -> bool:
    if perm.index('a1') > perm.index('a2'):
        return False
    if perm.index('b1') > perm.index('b2') or perm.index('b2') > perm.index('b3'):
        return False
    if perm.index('c1') > perm.index('c2') or perm.index('c2') > perm.index('c3'):
        return False
    if perm.index('d1') > perm.index('d2'):
        return False
    return True

def is_valid(perm: list[str]) -> bool:
    if perm.index('a1') > perm.index('b3'):
        return False
    if perm.index('c2') > perm.index('a2'):
        return False
    if perm.index('d1') > perm.index('b2'):
        return False
    return True

if __name__ == '__main__':
    main()
```

## Output

Ordered permutations: 25200

```

('a1', 'a2', 'b1', 'b2', 'b3', 'c1', 'c2', 'c3', 'd1', 'd2')
('a1', 'b1', 'c1', 'c2', 'a2', 'c3', 'd1', 'b2', 'b3', 'd2')
Valid permutations: 11144
0.4422222222222224

```

Thus, with 25200 ordered permutations, only 11144 are valid. This means that 44.22% of the ordered permutations are valid.

## Question 2

Thread A		Thread B		Thread C	
IA1	<code>x = x + 1</code>	IB2	<code>x = x - 2</code>	IC1	<code>x = x + 2</code>
IA2	<code>print(x)</code>	IB2	<code>print(x)</code>	IC2	<code>print(x)</code>

  

Thread A		Thread B		Thread C	
IA1.1	<code>y &lt;- x</code>	IB2.1	<code>y &lt;- x</code>	IC1.1	<code>y &lt;- x</code>
IA1.2	<code>y += 1</code>	IB2.2	<code>y -= 2</code>	IC1.2	<code>y += 2</code>
IA1.3	<code>x &lt;- y</code>	IB2.3	<code>x &lt;- y</code>	IC1.3	<code>x &lt;- y</code>
IA2	<code>print(x)</code>	IB2	<code>print(x)</code>	IC2	<code>print(x)</code>

A and B are impossible due to the instructions never lining up to both decrease and then increase by 1 (or vice-versa).

All of them except D is impossible.

D (223) is possible, initialize  $x = 4$

Thread	Instruction	x	output
B	Get 4	4	
C	Get 4	4	
B	<code>2 = 4 - 2</code>	4	
C	<code>6 = 4 + 2</code>	4	
C	Set 6	6	
B	Set 2	2	
B	Print x	2	2
C	Print x	2	22
A	Get 2	2	22
A	<code>3 = 2 + 1</code>	2	22
A	Set 3	3	22
A	Print x	3	223

The rest are similarly possible, though I do not care enough to figure out the correct ordering <sup>1</sup>.

## Question 3

### Advantages

Simpler to construct and debug.

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<sup>1</sup>Points for honesty though?

## **Disadvantages**

Requires thoughtful planning and design of what each layer does and what layers are needed. Each layer adds some overhead when passing data between layers.

## **Question 4**

Calling 3 forks would result in 8 processes.

## **Question 5**

Only the Shared Memory Segments are shared.

## **Question 6**

For 2 processing cores with a 65% parallel component we get a speedup of 1.48. For 4 processing cores with a 65% parallel component we get a speedup of 1.95.