M/CS 375 HW 11

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March 1, 2023

Problem 8

If a system of 3000 equations in 3000 unknowns can be solved by Gaussian elimination in 5 seconds on a given computer, how many back substitutions of the same size can be done per second?

$$\frac{s_b^2}{2 \cdot s_e^3/3} = \frac{t_b}{t_e}$$

$$s_e = 3000$$

$$t_e = ?$$

$$s_b = 3000$$

$$t_b = 5$$

$$\frac{3000^2}{2 \cdot 3000^3/3} = \frac{t_b}{5}$$

Simplifying the above, we get $t_b = \frac{1}{400}$ seconds, meaning it would take 1/400th of a second to do one back substitution. (I.e: we can do 400 back substitutions / second).