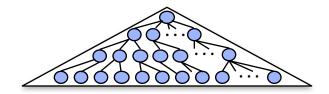


# Multiway Search Trees

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#### Multiway search trees

A multiway search tree (M-way tree) is a tree of order M > 2 in which the search property (total order) holds on every node and in which all leaves are at the same depth.

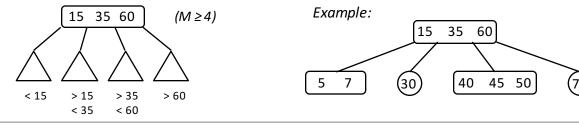


In an M-way tree:

Each node holds between 1 and M-1 values in sorted order.

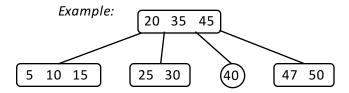
A non-leaf node with K values has K+1 non-empty subtrees that are M-way search trees.

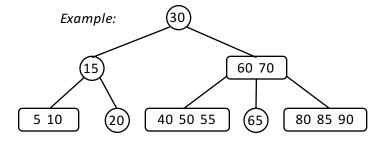
The i-th subtree of a node that holds values  $[v_0..v_k]$  ( $0 \le i \le K$ ) can only store values  $v_{i-1} < v < v_i$ .



### 2-4 trees

A 2-4 tree is a 4-way search tree where each non-leaf node must have at least two non-empty subtrees.



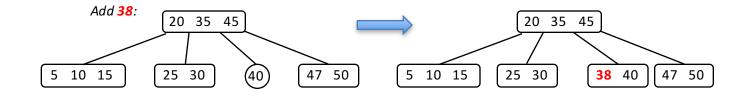


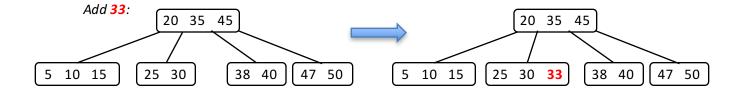
To add a new value, use the total order to find the **leaf** that should hold this value.

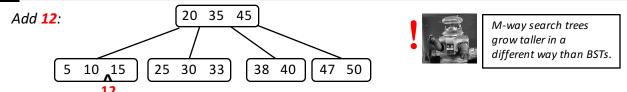
New values are always added in the context of an existing leaf node.



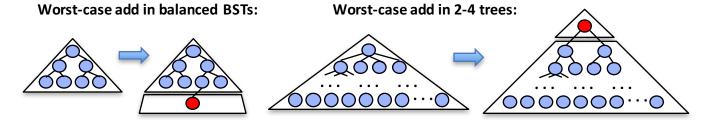
New values in a BST went into a **new leaf** in a currently empty subtree.







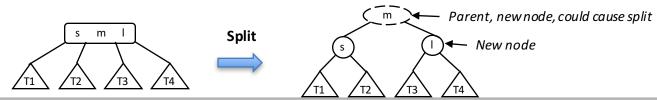
A node in a 2-4 tree can store up to 3 values, so this leaf is **full**.

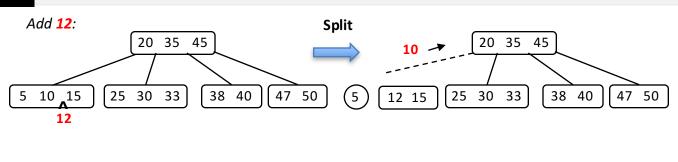


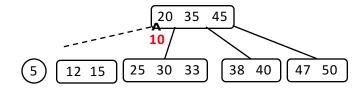
All leaves in a 2-4 tree have to be at the same level.

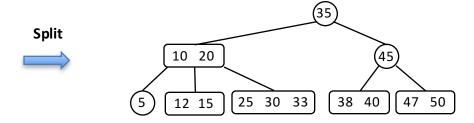
The tree grows "up" by adding a new root rather than down by adding a new (lower) leaf.

When a 2-4 node is full but it needs to store another value, we perform a split.









Insert: 10, 85, 15, 70, 20, 60, 30, 50, 65, 80, 90, 40, 5, 55

