

Project 1

7 6 5 4 3 2 1 0
1 1 1 0 0 1 0 0

1: A. 0110 0001 1111
 $= \underset{6}{0} \underset{1}{1} \underset{F}{1} = 61F$

B. 1000 1111 1100
 $\underset{8}{1} \underset{F}{1} \underset{C}{1} = 8FC$

C. 0001 0110 0100 0101
 $\underset{1}{0} \underset{6}{1} \underset{4}{0} \underset{5}{1} = 1645$

2.1: A. $\bar{1}1\bar{0}0^4 \bar{1}0^2 \bar{1}0^0 = -[2^6 + 0 + 0 + 2^3 + 0 + 2 + 0] = 64 + 8 + 2$
 $= (-74)_d$

B. $\bar{1}1\bar{1}1^4 00\bar{1}0^0 = -[2^6 + 2^5 + 2^4 + 0 + 0 + 2^1 + 0] = 64 + 32 + 16 + 2$
 $= (-114)_d$

C. $1000^5 011\bar{1}^0 = -[0 + 0 + 0 + 0 + 2^2 + 2 + 1] = 4 + 2 + 1$
 $= (-7)_d$

2.2: A. $1100 1010 \rightarrow 1's \text{ complement} \Rightarrow 00\bar{1}\bar{1} 0\bar{1}0\bar{1}^0$
 $= -[2^5 + 2^4 + 2^2 + 1] \Rightarrow (-53)_d$

*Negative because original LMB is 1

B. $1111 0010 \rightarrow 0000 1\bar{1}0\bar{1}^0$
 $= -[2^3 + 2^2 + 1] \Rightarrow (-13)_d$

C. $1000 0111 \rightarrow 0\bar{1}\bar{1}\bar{1}^4 100\bar{1}0^0$
 $= -[2^6 + 2^5 + 2^4 + 2^3] \Rightarrow (-120)_d$

2.3: A. $1100 1010 \rightarrow 2's \text{ complement} \Rightarrow 00\bar{1}\bar{1} 0\bar{1}\bar{1}0^0$
 $= -[2^5 + 2^4 + 2^2 + 2] \Rightarrow (-54)_d$

B. $1111 0010 \rightarrow 0000 1\bar{1}\bar{1}0^0$
 $= -[2^3 + 2^2 + 2] \Rightarrow (-14)_d$

C. $1000 0111 \rightarrow 01\bar{1}\bar{1} 100\bar{1}$
 $= -[2^6 + 2^5 + 2^4 + 2^3 + 1] \Rightarrow (-121)_d$

1. 1010101

= 100 = 16 = 21 = 8

$\begin{array}{r} 2 \overline{) 100} \\ 2 \overline{) 50} \\ 2 \overline{) 25} \\ 2 \overline{) 12} \\ 2 \overline{) 6} \\ 2 \overline{) 3} \\ 2 \overline{) 1} \end{array}$	$\begin{array}{r} 2 \overline{) 16} \\ 2 \overline{) 8} \\ 2 \overline{) 4} \\ 2 \overline{) 2} \\ 2 \overline{) 1} \end{array}$	$\begin{array}{r} 2 \overline{) 21} \\ 2 \overline{) 10} \\ 2 \overline{) 5} \\ 2 \overline{) 2} \\ 2 \overline{) 1} \end{array}$	$\begin{array}{r} 2 \overline{) 8} \\ 2 \overline{) 4} \\ 2 \overline{) 2} \\ 2 \overline{) 1} \end{array}$
0	0	1	0
0	0	0	0
1	0	0	0
0	0	0	0
0	0	1	0
1	1	1	0

3. A. $(-100)_d = 1110\ 0100$

1's $\Rightarrow 1001\ 1011$

2's $\Rightarrow 1001\ 1100$

B. $(-16)_d = 1001\ 0000$

1's $\Rightarrow 1110\ 1111$

2's $\Rightarrow 1111\ 0000$

C. $(-21)_d = 1\ 001\ 0101$

1's $= 1110\ 1010$

2's $= 1110\ 1011$

D. $(-0)_d = 1000\ 0000$

1's $= 1111\ 1111$

2's $= 1000\ 0000$

4. A. $= 0 \text{ to } 2^F - 1$

$= 0 \text{ to } 127$

B. $= -2^{F-1} \text{ to } 2^{F-1} - 1$

$= -64 \text{ to } 63$

5. A. $1000 \text{ AND } 1110$

$= 1000$

B. $1000 \text{ OR } 1110$

$= 1110$

C. $(1000 \text{ AND } 1110) \text{ OR } (1001 \text{ AND } 1110)$

This means $1000 \text{ OR } 1001$

$= 1001$

$$64 + 8 + 8$$

6. First convert to binary:

$$(25)_{10} = 00011001$$

$$(65)_{10} = 01000001, \text{ To make negative } \Rightarrow \text{ then two's complement}$$

then we add in binary:

$$\begin{aligned} &\text{one's complement} \\ &= 10111111 \end{aligned}$$

$$\begin{array}{r} 00011001 \\ + 10111111 \\ \hline \end{array}$$

$$= 11010100 \Rightarrow \text{to one's complement} \Rightarrow \text{then two's:}$$

$$= 1's: 00100111 \Rightarrow 00101000$$

$$00101000 = (40)_{10}$$

$$= (-40)_{10}$$

7. ~~Convert to binary~~

$$(+40)_{10} = 00101000$$

$$1's \text{ complement} \Rightarrow 11010111$$

$$2's \text{ complement} \Rightarrow 11011000$$

$$\begin{array}{r} 2 \overline{) 40} \\ 2 \overline{) 20} \ 0 \\ 2 \overline{) 10} \ 0 \\ 2 \overline{) 5} \ 0 \\ 2 \overline{) 2} \ 1 \\ 2 \overline{) 1} \ 0 \\ \hline 1 \end{array} \quad \begin{array}{l} \text{Right} \\ \text{to} \\ \text{left} \end{array}$$