

$$\int \frac{1}{x^5} dx \quad \int \frac{1}{x^5 + 1} dx$$




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**Example 6** Find  $\int \frac{1}{\sqrt{1-x^2}} dx$  using the substitution  $x = \sin \theta$ .

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**Example 7** Use a trigonometric substitution to find  $\int \frac{1}{\sqrt{4-x^2}} dx$ .

To simplify  $\sqrt{a^2 - x^2}$ , for constant  $a$ , try  $x = a \sin \theta$ , with  $-\pi/2 \leq \theta \leq \pi/2$ .

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**Example 10** Find  $\int \frac{1}{x^2 + 9} dx$  using the substitution  $x =$  .

To simplify  $a^2 + x^2$  or  $\sqrt{a^2 + x^2}$ , for constant  $a$ , try  $x = a \tan \theta$ , with  $-\pi/2 < \theta < \pi/2$ .

### Completing the Square to Use a Trigonometric Substitution

To make a trigonometric substitution, we may first need to complete the square.

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**Example 12** Find  $\int \frac{3}{\sqrt{2x - x^2}} dx$ .