

Self-Assessment Quiz

Discrete Mathematics

Recursion and Recurrence Relations

Instructions: This is a **self-assessment quiz**. It is **not graded**. Select the most appropriate answer for each question. Answers are provided at the end for self-checking.

Multiple Choice Questions

Q1. The process of defining an object in terms of smaller versions of itself is called:

- (A) Induction
- (B) Recursion
- (C) Iteration
- (D) Enumeration

Q2. A recursive definition always consists of:

- (A) A rule and a formula
- (B) A base case and a recursive step
- (C) A sequence and a series
- (D) A function and its inverse

Q3. Which of the following is a base case for the factorial function?

- (A) $n! = n(n - 1)!$
- (B) $1! = 1$
- (C) $0! = 1$
- (D) $n! = (n + 1)!$

Q4. If a function is defined recursively, then:

- (A) It never refers to itself
- (B) It refers to smaller input values

- (C) It has no base value
- (D) It must be linear

Q5. Given $f(0) = 3$ and $f(n + 1) = 2f(n) + 3$, what is $f(1)$?

- (A) 6
- (B) 7
- (C) 9
- (D) 12

Q6. A recurrence relation expresses:

- (A) A term directly as a formula
- (B) A term using its previous terms
- (C) Only the first term of a sequence
- (D) A constant function

Q7. Which of the following defines the Fibonacci sequence?

- (A) $F_n = 2n$
- (B) $F_n = F_{n-1}$
- (C) $F_n = F_{n-1} + F_{n-2}$
- (D) $F_n = n!$

Q8. The initial conditions in a recurrence relation are needed to:

- (A) Solve integrals
- (B) Find unique values of the sequence
- (C) Prove continuity
- (D) Reduce computation time

Q9. Which recurrence relation represents $b_n = 5^n$?

- (A) $b_n = b_{n-1} + 5$
- (B) $b_n = 5b_{n-1}$
- (C) $b_n = b_{n-1}^5$
- (D) $b_n = 5 + b_{n-1}$

Q10. If $S(n)$ is the sum of first n positive integers, then the recursive definition is:

- (A) $S(n) = nS(n - 1)$
- (B) $S(n) = S(n - 1) - n$
- (C) $S(n) = n + S(n - 1)$

(D) $S(n) = 2n + S(n - 1)$

Q11. A recursively defined function must eventually reach:

- (A) A maximum value
- (B) A base case
- (C) A closed form
- (D) An infinite loop

Q12. Which of the following is an example of recursion?

- (A) Solving a quadratic equation
- (B) Factorial computation
- (C) Matrix addition
- (D) Linear search

Q13. In the Fibonacci sequence, $F_0 = 1$ and $F_1 = 1$. What is F_2 ?

- (A) 1
- (B) 2
- (C) 3
- (D) 0

Q14. The purpose of a recursive definition is to:

- (A) Avoid mathematical formulas
- (B) Define complex objects using simpler ones
- (C) Replace functions with graphs
- (D) Eliminate base cases

Q15. A recurrence relation with order 2 depends on:

- (A) One previous term
- (B) Two previous terms
- (C) Only the first term
- (D) All previous terms

Answer Key (For Self-Assessment)

Q1. B

Q2. B

Q3. C

Q4. B

Q5. C

Q6. B

Q7. C

Q8. B

Q9. B

Q10. C

Q11. B

Q12. B

Q13. B

Q14. B

Q15. B