Topic: Dot products

Question: Find the dot product.

$$\overrightarrow{x} = (5, -1)$$

$$\overrightarrow{y} = (3,2)$$

Answer choices:

$$\mathbf{A} \qquad \overrightarrow{x} \cdot \overrightarrow{y} = 11$$

$$\mathbf{B} \qquad \overrightarrow{x} \cdot \overrightarrow{y} = 13$$

$$\mathbf{C} \qquad \overrightarrow{x} \cdot \overrightarrow{y} = 9$$

Solution: B

To find the dot product of two vectors, we multiply corresponding components, then add the products. So the dot product of $\vec{x} = (5, -1)$ and $\vec{y} = (3,2)$ is

$$\overrightarrow{x} \cdot \overrightarrow{y} = (5)(3) + (-1)(2)$$

$$\overrightarrow{x} \cdot \overrightarrow{y} = 15 - 2$$

$$\overrightarrow{x} \cdot \overrightarrow{y} = 13$$



Topic: Dot products

Question: Find the dot product.

$$\vec{x} = (-4,0,12)$$

$$\vec{y} = (9, -12,8)$$

Answer choices:

$$\mathbf{A} \qquad \overrightarrow{x} \cdot \overrightarrow{y} = 48$$

$$\mathbf{B} \qquad \overrightarrow{x} \cdot \overrightarrow{y} = 132$$

$$\mathbf{C} \qquad \overrightarrow{x} \cdot \overrightarrow{y} = 72$$

$$D \qquad \overrightarrow{x} \cdot \overrightarrow{y} = 60$$

Solution: D

To find the dot product of two vectors, we multiply corresponding components, then add the products. So the dot product of $\vec{x} = (-4,0,12)$ and $\vec{y} = (9, -12,8)$ is

$$\overrightarrow{x} \cdot \overrightarrow{y} = (-4)(9) + (0)(-12) + (12)(8)$$

$$\overrightarrow{x} \cdot \overrightarrow{y} = -36 + 0 + 96$$

$$\overrightarrow{x} \cdot \overrightarrow{y} = 60$$



Topic: Dot products

Question: Use the dot product to find $3\vec{x} \cdot (-2\vec{y} - \vec{z})$.

$$\overrightarrow{x} = (-4, -2, 7)$$

$$\overrightarrow{y} = (6, -1, -10)$$

$$\vec{z} = (3, -2, 0)$$

Answer choices:

$$A \qquad 3\overrightarrow{x} \cdot (-2\overrightarrow{y} - \overrightarrow{z}) = 96$$

$$B 3\overrightarrow{x} \cdot (-2\overrightarrow{y} - \overrightarrow{z}) = 576$$

$$\mathbf{C} \qquad 3\overrightarrow{x} \cdot (-2\overrightarrow{y} - \overrightarrow{z}) = -92$$

$$D \qquad 3\overrightarrow{x} \cdot (-2\overrightarrow{y} - \overrightarrow{z}) = -434$$

Solution: B

To simplify $3\overrightarrow{x} \cdot (-2\overrightarrow{y} \cdot \overrightarrow{z})$, start by finding $3\overrightarrow{x}$,

$$\vec{x} = (-4, -2, 7)$$

$$3\overrightarrow{x} = 3(-4, -2,7)$$

$$3\vec{x} = (-12, -6,21)$$

and $-2\overrightarrow{y}$.

$$\vec{y} = (6, -1, -10)$$

$$-2\overrightarrow{y} = -2(6, -1, -10)$$

$$-2\overrightarrow{y} = (-12,2,20)$$

Then the difference $-2\overrightarrow{y} - \overrightarrow{z}$ is

$$-2\overrightarrow{y} - \overrightarrow{z} = \begin{bmatrix} -12\\2\\20 \end{bmatrix} - \begin{bmatrix} 3\\-2\\0 \end{bmatrix}$$

$$-2\vec{y} - \vec{z} = \begin{bmatrix} -12 - 3\\ 2 - (-2)\\ 20 - 0 \end{bmatrix}$$

$$-2\overrightarrow{y} - \overrightarrow{z} = \begin{bmatrix} -15\\4\\20 \end{bmatrix}$$

The dot product is then

$$3\overrightarrow{x} \cdot (-2\overrightarrow{y} - \overrightarrow{z})$$



$$\begin{bmatrix} -12 & -6 & 21 \end{bmatrix} \cdot \begin{bmatrix} -15 \\ 4 \\ 20 \end{bmatrix}$$

$$-12(-15) - 6(4) + 21(20)$$

$$180 - 24 + 420$$