Linear Algebra and Geometry 1

Systems of equations, matrices, vectors, and geometry

Rules for computations with real numbers

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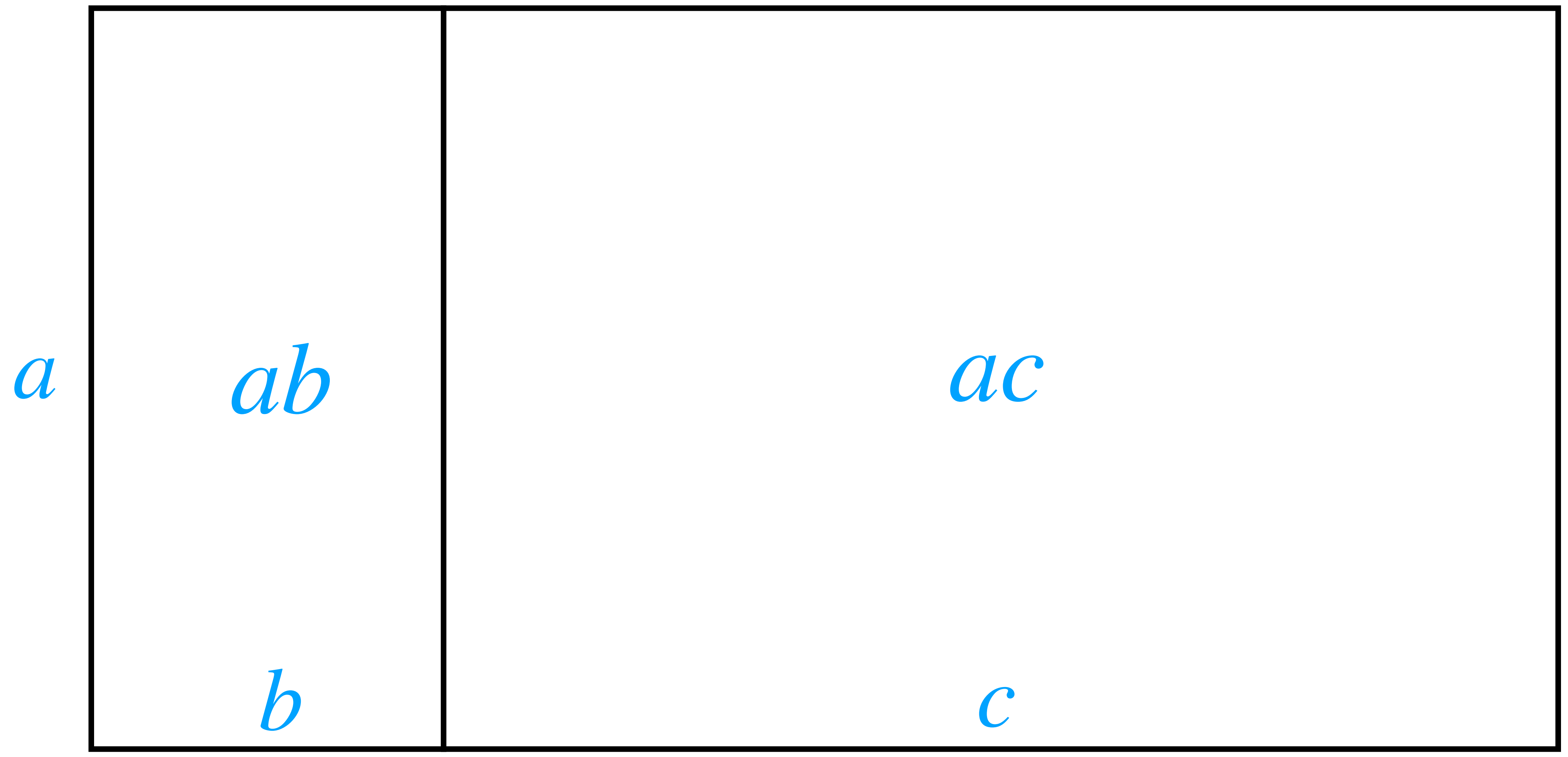

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The inverse element	$a+(-a)=0$	$a\cdot a^{-1}=1 \quad (a\neq 0)$