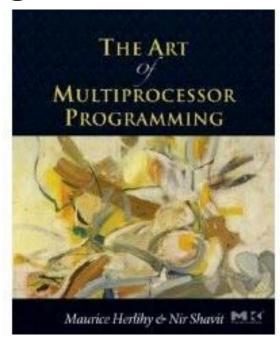


COS 226

Chapter 2
Mutual Exclusion

Acknowledgement



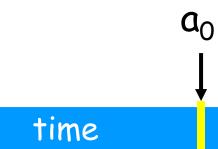
 Some of the slides are taken from the companion slides for "The Art of Multiprocessor Programming" by Maurice Herlihy & Nir Shavit

Why is Concurrent Programming so Hard?

- Try preparing a seven-course banquet
 - By yourself
 - With one friend
 - With twenty-seven friends ...
- Before we can talk about programs
 - Need a language
 - Describing time and concurrency

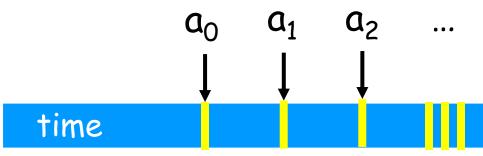
Events

- An *event* a₀ of thread A is
 - Instantaneous
 - No simultaneous events (break ties)



Threads

- A thread A is (formally) a sequence a₀, a₁, ... of events
 - □ "Trace" model
 - □ Notation: $a_0 \rightarrow a_1$ indicates order



Concurrency

Thread A

time

Thread B

time

Interleavings

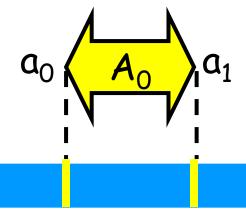
- Events of two or more threads
 - Interleaved
 - Not necessarily independent

time

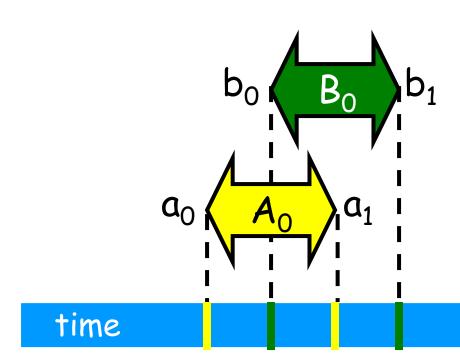
Intervals

time

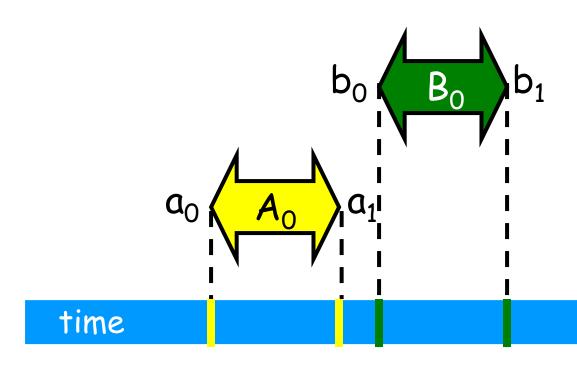
- An *interval* $A_0 = (a_0, a_1)$ is
 - □ Time between events a₀ and a₁





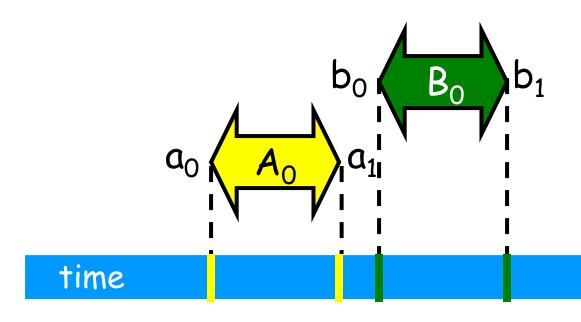




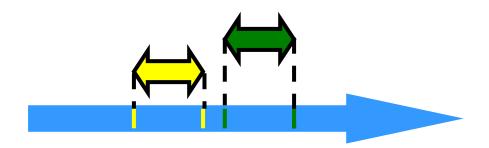


Precedence

Interval A₀ precedes interval B₀

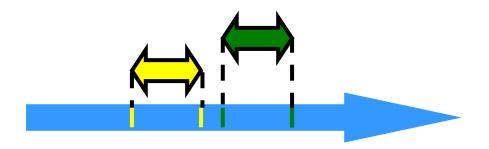


Precedence



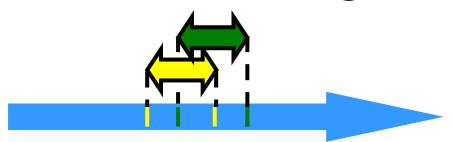
- Notation: $A_0 \rightarrow B_0$
- Formally,
 - □ End event of A₀ before start event of B₀
 - □ Also called "happens before" or "precedes"

Precedence Ordering



- Remark: $A_0 \rightarrow B_0$ is just like saying
 - \square 1066 AD \rightarrow 1492 AD,
 - Middle Ages → Renaissance,

Precedence Ordering



- Never true that A → A
- If A→B then not true that B→A
- If $A \rightarrow B \& B \rightarrow C$ then $A \rightarrow C$
- Funny thing: A→B & B → A might both be false!

Repeated Events

```
while (mumble) { a_0; a_1; } 
 k-th occurrence of event a_0
```

 a_0^k

 A_0^k

k-th occurrence of interval $A_0 = (a_0, a_1)$



Implementing a Counter

```
public class Counter {
  private long value;

  public long getAndIncrement() {
    value++;
  }
}
```



Implementing a Counter

```
public class Counter {
   private long value;

   public long getAndIncrement() {
     temp = value;
     value = temp + 1;
     return value;
   }
}
```



Critical Section

- Block of code that can be executed by only one thread at a time
- Needs Mutual Exclusion
- Standard way to approach mutual exclusion is through locks



Locks (Mutual Exclusion)

```
public interface Lock {
  public void lock();
  public void unlock();
}
```



Locks (Mutual Exclusion)

```
public interface Lock {

public void lock();

public void unlock();
}
```

M

Locks (Mutual Exclusion)

```
public interface Lock {

public void lock();

public void unlock();

release lock
```

м

```
public class Counter {
  private long value;
  private Lock lock;
  public long getAndIncrement() {
   lock.lock();
   try {
    int temp = value;
    value = value + 1;
   } finally {
     lock.unlock();
   return temp;
  }}
```

```
public class Counter {
  private long value;
  private Lock lock;
  public long getAndIncrement() {
  lock.lock();
                               acquire Lock
    int temp = value;
    value = value + 1;
   } finally {
     lock.unlock();
   return temp;
  }}
```

```
public class Counter {
  private long value;
  private Lock lock;
  public long getAndIncrement() {
  lock.lock();
   try {
    int temp = value;
    value = value + 1;
    finally {
                               Release lock
     lock.unlock();
                            (no matter what)
   return temp;
```

```
public class Counter {
  private long value;
  private Lock lock;
  public long getAndIncrement() {
   lock.lock();
                                         Critical
    int temp = value;
                                         section
    value = value + 1;
   } Tinally {
     lock.unlock();
   return temp;
  }}
```



Properties of a good Lock algorithm

- Mutual Exclusion
- Deadlock-free
- Starvation-free



Mutual Exclusion

Threads do not access critical section at same time



Deadlock-free

If some thread attempts to acquire the lock, some thread will succeed in acquiring the lock

Deadlock-free

- If <u>some</u> thread attempts to acquire the lock, <u>some</u> thread will succeed in acquiring the lock
 - ☐ System as a whole makes progress
 - Even if individuals starve
 - ☐ At least one thread is completing



Starvation-free

Every thread that attempts to acquire the lock will eventually succeed



Starvation-free

- Every thread that attempts to acquire the lock will eventually succeed
 - If a thread calls lock() it will eventually acquire the lock
 - □ Individual threads make progress



Locks

■ Let's start with lock solutions for 2 concurrent threads...



Two-Thread Conventions

```
class ... implements Lock {
  // thread-local index, 0 or 1
  public void lock() {
    int i = ThreadID.get();
    int j = 1 - i;
```

Two-Thread Conventions

```
class ... implements Lock {
    ...
    // thread-local index, 0 or 1
    public void lock() {
        int i = ThreadID.get();
        int j = 1 - i;
        ...
    }
}
```

Henceforth: i is current thread, j is other thread

LockOne

- Basic idea:
 - □ Thread indicates interest in acquiring lock
 - Checks to see if other thread is currently in critical section
 - If true, waits until other thread finishes
 - If not, enters critical section

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LockOne

```
class LockOne implements Lock {
private boolean[] flag = new boolean[2];
public void lock() {
 flag[i] = true;
 while (flag[j]) {}
public void unlock() {
 flag[i] = false;
```

LockOne

```
class LockOne implements Lock {
private boolean[] flag =
                         new boolean[2];
public void lock() {
 flag[i] = true;
  while (flag[j]) {}
                            Set my flag
public void unlock() {
  flag[i] = false;
```

LockOne

```
class LockOne implements Lock {
private boolean[] flag =
                         new boolean[2];
public void lock() {
 flag[i] = true;
  while (flag[j]) {}
                            Set my flag
public void unlock
  flag[i] = false;
                      Wait for other
                      flag to go false
```

LockOne

```
class LockOne implements Lock {
private boolean[] flag =
                         new boolean[2];
public void lock() {
  flag[i] = true;
  while (flag[j]) {}
                      When release lock
                       set my flag again
public void unlo
 flag[i] = false;
```

×

Deadlock Freedom?

Concurrent execution:

- If each thread sets its flag to true and waits for the other, they will wait forever
- No deadlock freedom

LockOne Summary

- LockOne offers mutual exclusion
- When accessed sequentially, LockOne works fine
- However with concurrent threads, LockOne is not Deadlock-free

- Basic idea:
 - When attempting to acquire lock, offer to be the victim that has to defer to other thread
 - While current thread is the victim, wait until other thread becomes the victim
 - When current thread no longer the victim, enter the critical section

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```
public class LockTwo implements Lock {
  private int victim;
  public void lock() {
   victim = i;
   while (victim == i) {};
  }
  public void unlock() {}
}
```

```
public class LockTwo implements Lock {
  private int victim;
  public void lock() {
    victim = i;
    while (victim == i) {};
  }
  public void unlock() {}
}
```

```
public class LockTwo implements Lock {
  private int victim;
  public void lock() {
  victim = i:
    while (victim == i) {};
  public void unlock() {}
}
```

```
public class Lock2 implements Lock {
  private int victim;
  public void lock() {
    victim = i;
    while (victim == i) {};
  }
  public void unlock() {}
```



LockTwo Claims

- Satisfies mutual exclusion
 - ☐ If thread i in CS
 - □ Then victim == j
 - Cannot be both 0 and 1

```
public void LockTwo() {
  victim = i;
  while (victim == i) {};
}
```

LockTwo Summary

- LockTwo offers Mutual Exclusion
- Works fine with concurrent threads
- However results in Deadlock with sequential threads
- LockOne and LockTwo thus complement each other

Peterson Lock

- Combine LockOne and LockTwo
 - Enable successful sequential access provided by LockOne
 - Enables successful concurrent access provided by LockTwo



Peterson Lock

- Basic idea:
 - Current thread indicates interest in acquiring the lock
 - Current thread offers to be the victim
 - If no interest from other thread and no longer the victim, then continue to critical section



```
public void lock() {
  flag[i] = true;
  victim = i;
  while (flag[j] && victim == i) {};
}
public void unlock() {
  flag[i] = false;
}
```

7

Peterson's Algorithm

Announce I'm

```
public void lock() {
  flag[i] = true;
  victim = i;
  while (flag[j] && victim == i) {};
}
public void unlock() {
  flag[i] = false;
}
```



```
Announce I'm
                           interested
public void locks
        = true;
                          Defer to other
 victim
while (flag[j] && victim == i) {};
public void unlock() {
flag[i] = false;
```

```
Announce I'm
                           interested
public void lock
        = true;
                          Defer to other
 victim
while (flag[j] && victim == i) {};
public void unlock()
                       Wait while other
 flag[i] = false;
                       interested & I'm
                           the victim
```

```
Announce I'm
                           interested
public void locks
flag[i]
        = true;
                          Defer to other
 victim
while (flag[j] && victim == i) {};
public void unlock()
                        Wait while other
flag[i] = false;
                        interested & I'm
         No longer
                           the victim
         interested
```

м

Mutual Exclusion

```
public void lock() {
  flag[i] = true;
  victim = i;
  while (flag[j] && victim == i) {};
```

- If thread 0 in critical section,
 - -flag[0] = true,
 - victim = 1

- If thread 1 in critical section,
 - \Box flag[1] = true,
 - \square victim = 0

Cannot both be true

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Deadlock Free

```
public void lock() {
    ...
    while (flag[j] && victim == i) {};
```

- Thread blocked
 - □ only at while loop
 - □ Only if other's flag is true
 - □ only if it is the **victim**
- Solo: other's flag is false
- Both: one or the other must not be the victim

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Starvation Free

Thread i would be blocked only if j repeatedly re-enters so that

```
flag[j] == true and
victim == i
```

- When j re-enters
 - \square it sets victim to j.
 - □ So i gets in
- Thus: Starvation free

```
public void lock() {
   flag[i] = true;
   victim = i;
   while (flag[j] && victim == i) {};
}

public void unlock() {
   flag[i] = false;
}
```



Locks

Moving on to solutions for n concurrent threads



Filter Lock

- Peterson lock adapted to work with n threads instead of just 2
- Thread has to traverse n-1 waiting rooms in order to acquire the lock

The Filter Algorithm for *n*Threads

There are **n-1** "waiting rooms" called levels

ncs

- At each level
 - ☐ At least one enters level
 - At least one blocked if many try
- Only one thread makes it through



```
class Filter implements Lock {
   int[] level; // level[i] for thread i
   int[] victim; // victim[L] for level L
 public Filter(int n) {
     level = new int[n];
     victim = new int[n];
     for (int i = 1; i < n; i++) {
         level[i] = 0;
     }}
```



```
class Filter implements Lock {
  public void lock(){
    for (int L = 1; L < n; L++) {
      level[i] = L;
      victim[L] = i:
      while (\exists k != i) level[k] >= L) \&\&
             victim[L] == i );
    }}
  public void unlock() {
    level[i] = 0;
  }}
```

M

```
class Filter implements Lock {
  public void lock() {
   for (int L = 1; L < n; L++) {
      ieveilij = L;
      victim[L] = i;
      while ((\exists k != i) level[k] >= L) \&\&
             victim[L] == i);
    }}
  public void release(int i) {
    level[i] = 0;
                          One level at a time
  }}
```

```
class Filter implements Lock {
  public void lock() {
    for (int L = 1; L < n; L++) {
      level[i] = L;
      victim[L] = 1;
      while (\exists k != 1) \exists evel[k] >= L) \&\&
             victim[L] == i); // busy wait
    }}
                                     Announce
  public void release(int i) {
                                   intention to
    level[i] = 0;
  }}
                                  enter level L
```

7

```
class Filter implements Lock {
  int level[n];
  int victim[n];
  public void lock() {
    for (int L = 1; L < n; L++) {
      level[i] = L;
      victim[L] = i;
      while ((\exists k \neq i) \text{ level[k]} >= L) \&\&
              victim[L] == i);
    }}
  public void release(int i) (Give priority to
    level[i] = 0;
                                 anyone but me
  }}
```

Filter

Wait as long as someone else is at same or higher level, and I'm designated victim

```
class Filter implements Lock {
  int level[n];
  int victim[n];
  public void lock() {
    for (int L = 1; L < n; L_{++})
      level[i] = L;
      victim[L] = i;
      while (\exists k != i) level[k] >= L) \&\&
              victim[L] == i);
  public void release(int i) {
    level[i] = 0;
  }}
```

Filter

```
class Filter implements Lock {
  int level[n];
  int victim[n];
  public void lock() {
    for (int L = 1; L < n; L++) {
      level[i] = L;
      victim[L] = i;
      while ((\exists k != i) level[k] >= L) \&\&
             victim[L] == i);
  public void release(int i) {
    level[i] \neq 0
  }}
```

Thread enters level L when it completes the loop

.

No Starvation

- Filter Lock satisfies properties:
 - □ Just like Peterson Algorithm at any level
 - □ So no one starves
- But what about fairness?
 - □ Threads can be overtaken by others



Waiting

- Starvation freedom guarantees that every thread that calls lock() eventually enters the critical section
- It however makes no guarantee about how long that can take



Waiting

- Ideally if A calls lock() before B, then A should enter critical section before B
- However this does not currently work since we cannot determine which thread called lock() first
- Locks should thus be further defined



Fairness

Locks should be first-some-first served

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Filter Lock again

- Filter Lock satisfies properties:
 - No one starves
 - But very weak fairness
 - Can be overtaken arbitrary # of times
 - □ That's pretty lame...

- Provides First-Come-First-Served
- How?
 - □ Take a "number"
 - Wait until lower numbers have been served

Each thread takes a number when attempting to acquire the lock and waits until no thread with an earlier number is trying to acquire it



```
class Bakery implements Lock {
   boolean[] flag;
   Label[] label;
  public Bakery (int n) {
    flag = new boolean[n];
    label = new Label[n];
    for (int i = 0; i < n; i++) {
       flag[i] = false; label[i] = 0;
```

.

- flag[A] is a boolean flag indicating whether A wants to enter the critical section
- label[A] is an integer that contains thread A's "number" when entering the bakery



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Bakery Algorithm

Label is created as one greater than the maximum of the other thread's labels

W

And someone has a smaller number than me

THEORETICALLY



- If two threads try to acquire the lock concurrently, they may read the same maximum number
- Threads thus have unique pairs consisting of number as well as thread ID

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Bakery Algorithm

(label[i],i) << (label[j],j)

If and only if

label[i] < label[j] OR label[i] = label[j] and i < j

With lower (label,i) in lexicographic order

- In other words:
- Thread A must wait if:
 - □ Another thread is interested AND the other thread's number is lower than thread A
 - OR
 - Another thread is interested AND the two threads have the same number but the other's threads ID is smaller than A



```
class Bakery implements Lock {
    ...
    public void unlock() {
       flag[i] = false;
    }
}
```

100

```
class Bakery implements Lock {
    No longer
    interested

public void unlock() {
    flag[i] = false;
}
```

- Does the lock provide:
 - Mutual exclusion?
 - YES two threads cannot be in the critical section at the same time since one of them will have an earlier label pair

- ☐ Starvation freedom?
 - YES if a thread exists the critical section and immediately wants to reacquire the lock, he will first have to take a new, later number allowing the other waiting threads to gain access first

- □ Deadlock freedom?
 - YES there is always one thread with the earliest label, ties are not possible because of labels consist of number and order in array



- The Bakery algorithm also provides Firstcome-first-served
 - □ If A calls lock() before B, then A's number is smaller than B's number
 - □ So B is locked out while flag[A] is true



Potential issue:

- With the current Bakery algorithm we are assuming that we have an infinite amount of numbers to use
- In practice this is not the case

Bounded timestamps

- Labels in the Bakery lock grow without bounds
- In a long-lived system we may have to worry about overflow
- If a thread's label silently rolled over from a large number to zero, the first-come-firstserved property no longer holds



Bounded timestamps

- In the Bakery algorithm, the idea of labels can be replaced by timestamps
- Timestamps can ensure order among the contending threads
- We will thus need to ensure that if one thread takes a label after another, then the latter has the higher timestamp



Bounded timestamps

- Timestamps need the ability to:
 - □ Scan read the other thread's timestamps
 - □ Label assign itself a larger timestamp

Possible solution

- To construct a Sequential timestamping system
- Each thread perform scan-and-label completely one after the other
- Uses mutual exclusion

- The Bakery algorithm is elegant and fair
- However it is not considered practical
 - □ Why?
 - □ Principal drawback is the need to read *n* distinct location where *n* can be very large