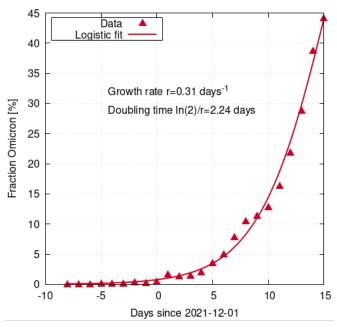


- ► The Delta and Omicron variants coexist without directly affecting each other
- Indirect interaction via competing for common ressources, i,e., first come, first served

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Latest observation 2

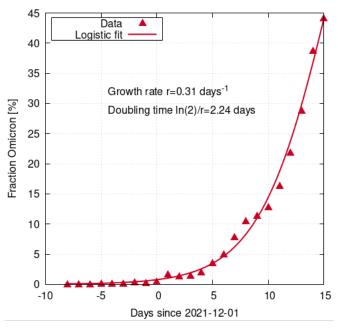


- ► The share of Omicron can be well described by a logistic function with growth rate *r*
- First transform the observed Omicron share p into the **odds ratio** y = p/(1-p)
- From Observation 1 (coexistence), is follows that the odds ratio grows exponentially:

$$y(t) = y_0 e^{rt}$$

➤ Transforming back gives the s-shaped predicted Omicron share (logistic function)

$$p(t) = \frac{y(t)}{1 + y(t)}$$

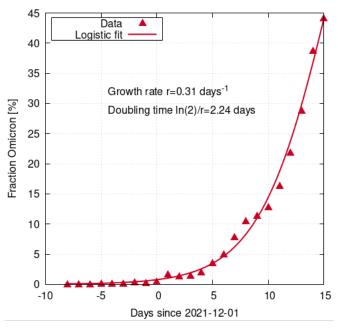


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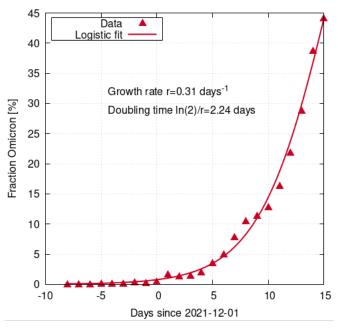


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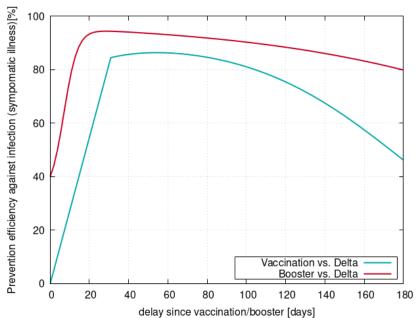
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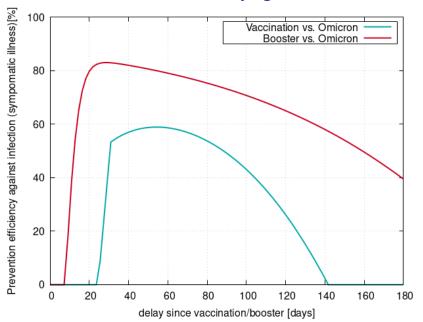
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Assumed efficiency against Delta infections



"First vaccinatedfirst boostered" principle

Assumed efficiency against Omicron infections



Only fresh full vaccinations or boosters help against Omicron



Assumed immunity by infections

- ▶ 100 % immunity of Delta against Delta reinfections
- ▶ 100 % immunity of Omicron against Omicron reinfections
- ▶ 100 % no cross immunity (people can get both Delta and Omicron infections)



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$$p(t) = \frac{y_0 e^{rt}}{1 + y_0 e^{rt}}, \quad y_0 = \frac{p_0}{1 - p_0}$$

- (2) The growth rate r of the logistic growth depends or
 - ▶ the base reproduction numbers R_{10} and R_{20} ,
 - be the total population immunities (vaccination, boosters, infections) I_1 and I_2 against each variant,
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according to

$$r = \frac{1}{T} \left[\frac{R_{20}(1 - I_2)}{R_{10}(1 - I_1)} - 1 \right]$$

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 - the Omicron percentage p
 - \blacktriangleright the base reproduction numbers R_{10} and R_{20} of Delta and Omicron, respectively,
 - the immunity escape fractions $(1 I_1)$ and $(1 I_2)$,
 - the seasonal multiplicator f^{season}
 - the stringency (lockdown) multiplicator f^{stringency}:

$$R_t = [(1-p)R_{10}(1-I_1) + pR_{20}(1-I_2)] f_{\text{season}} f_{\text{stringency}}$$
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- Notice: Both the growth rate r of the increase of the Delta share and the growth rate $(R_t-1)/T$ of the actual infection wave depend on $P_1=R_{10}(1-I_1)$ and $P_2=R_{20}(1-I_2)$ such that a positive (negative) value of r implies an increase (decrease) of R_t
- A positive Omicron spreading r does not imply that the new variant is more infectious; only the products P_1 and P_2 matter
- A positive spreading r can be related to a negative infection growth $(R_t 1)/T$ both before and after the new variant dominates since, for given I_1 and I_2 , r is only related to the ratio R_{20}/R_{10} of the base immunities \Rightarrow next slide

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Estimating the base reproduction numbers

Assume at time $t=t^*$ given population immunities I_1^* and I_2^* (see later), and estimatios of the Omega share p^* , Omicron spreading rate r^* , and effective reproduction number R_t^* of the mixture. Then, we can use Eq (1) to obtain the ratio

$$\frac{R_{20}}{R_{10}} = \frac{(r^*T+1)(1-I_1^*)}{1-I_2^*} \tag{3}$$

and, with Eq (2) determine the base reproduction numbers individually:

$$R_{10} = \frac{R_t^*}{(1 + p^*r^*T)f_{\text{season}}f_{\text{stringency}}} \tag{4}$$

For $t > t^*$, I assume fixed base reproduction numbers and calculate the future Omicron spreading and the future wave using (1) and (2) with time varying I_1 , I_2 , p, f_{season} , and $f_{\text{stringency}}$



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Here, I make following assumptions

- $lackbox{ Vaccination efficiency curves }I_1^{
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- lacktriangle corresponding booster efficiencies $I_1^{
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- ► First vaccinated-first boostered

Since the protection depends on the vaccination times, I sum up the different histories weighted with the past daily vaccination and booster rates $r_{t'}^v$ and $r_{t'}^b$ (fraction of the population per day):

$$I_1^{\mathsf{vacc}}(t) = \sum_{t'=t_v}^t r_{t'}^v I_1^{\mathsf{v}}(t-t') + \sum_{t'=t_v}^t r_{t'}^b I_1^{\mathsf{b}}(t-t')$$

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Determining the population immunities II: infections and total

Everybody can only be infected once with any variant but there is no cross immunity, so the immunity is just equal to the total percentage X_1 and X_2 of people infected with either variant:

$$I_1^x = X_1, \quad I_2^x = X_2$$

Notice: X_i is not just the cumulated number of cases divided by the population because any infection, whether detected or not detected, counts

There is no correlation between vaccinations and infections:

$$1 - I_1 = (1 - I_1^v)(1 - I_1^x), \quad 1 - I_2 = (1 - I_2^v)(1 - I_2^x)$$
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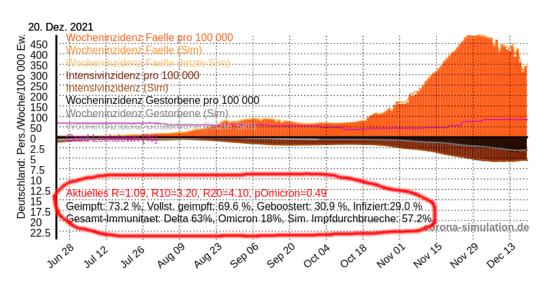
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Simulation



All items I_1 , I_2 , p, R_{10} , R_{20} , f_{season} and $f_{\text{stringency}}$ are displayed in the simulation