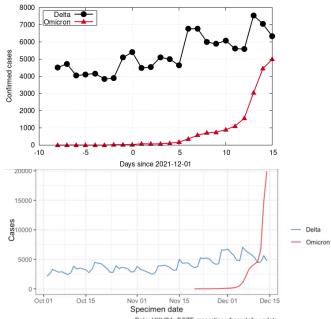
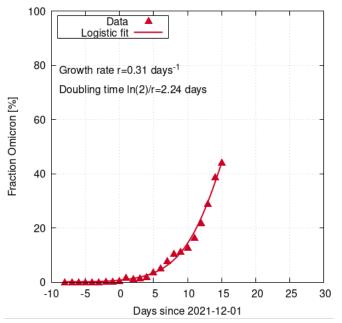
1. Delta and Omicron: Observations

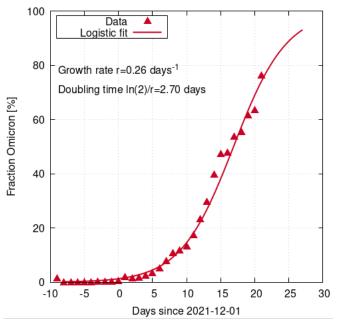


- Data from Danmark and London
- The Delta and Omicron variants coexist without directly affecting each other
- Indirect interaction via competing for common ressources, i,e., first come, first served

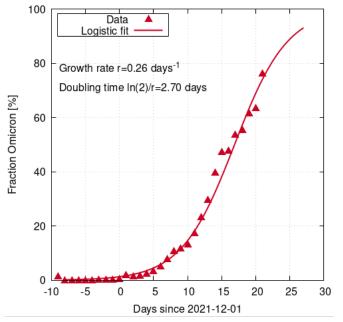
2. Rate r of the logistic growth of the Omicron share



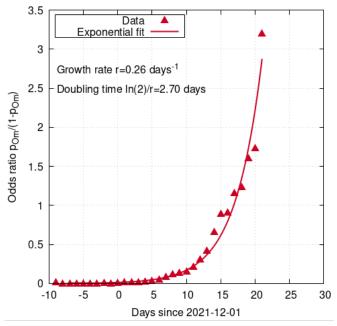
► The share of Omicron can be well described by a logistic function with growth rate *r*



Data update.

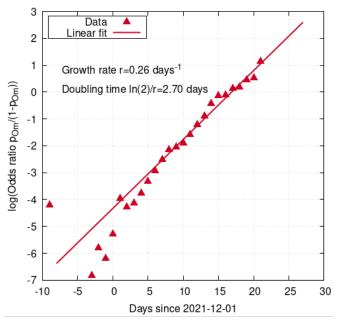


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$$y(t) = y_0 e^{rt}$$

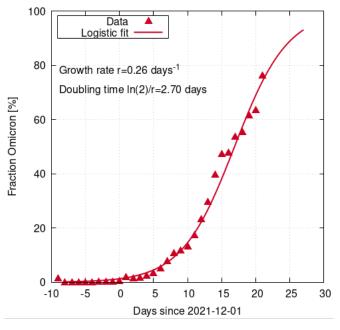


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 Transforming back gives the s-shaped predicted Omicron share (logistic function)

$$p(t) = \frac{y(t)}{1 + y(t)}$$

- Neither positive nor negative **cross effects**: Each variant acts on its own (using common ressources of susceptible humans)
- The Delta and Omicron variants have different base reproduction numbers R_{10} and R_{20} and different generation times T_1 and T_2 , respectively (e.g., $R_{10} = 5$, $T_1 = 5 \, \text{days}$, $T_2 = 4 \, \text{days}$)
- The **immunities** I_1 and I_2 (including vaccinations and past infections) against Delta and Omicron are generally different
- The reduction factors f_m by isolation measures and the seasonal factor f_s are common
- All factors influencing the effective reproduction number R are multiplicative. Daily new infections x_1 (Delta) and x_2 (Omicron) develop according to following

Infection dynamics $x_1(t_0+T_1)=R_1x_1(t_0)=R_{10}(1-I_1)f_mf_sx_1(t_0),$ as $f(R_{01},\ R_{02},\ \text{factors})$: $x_2(t_0+T_2)=R_2x_2(t_0)=R_{20}(1-I_2)f_mf_sx_2(t_0)$

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Assuming continuous infections (slowly varying rates), we can write (1) as

$$x_1(t) = x_1(0)R_1^{t/T_1} = x_1(0)\exp\left(\frac{t}{T_1}\ln R_1\right) \equiv x_1(0)\exp(r_1t),$$

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special case $x_1 = x_2 = x_3$ $x_1 = x_2 + x_3 + x_4 = x_4$ the spreading rate is proportional to the ratio of the actual reproduction numbers



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Special case $T_1 = T_2 = T$: $r = 1/T \ln(R_2/R_1)$: the spreading rate is proportional to the ratio of the actual reproduction numbers $\bullet \square \bullet \bullet \square \bullet$



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After some manipulations ...

Observed Omicron
$$R_{02}$$
: $R_{20} = e^{rT_2} f_{\rm m}^{\gamma-1} f_{\rm s}^{\gamma-1} \frac{(R_{10}(1-I_1))^{\gamma}}{1-I_2}, \quad \gamma = \frac{T_2}{T_1}$ (4)

For equal generation times $T_1 = T_2 = T$, the measures and the seasonal effects drop out and r depends only on the past infection and vacination immunities (remains time dependent since the immunities change):

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The **effective growth rate** r_{eff} of the infection dynamics (not to be confused with the logistic growth rate r of the Omicron shares p) comes directly from (2):

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Associating r_{eff} with $\ln R_{\text{eff}}/T_1$, we get the

Effective reproduction number:
$$R_{\text{eff}} = R_1^{1-p} R_2^{p/\gamma}$$
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The effective growth rate r_{eff} of the infection dynamics (not to be confused with the logistic growth rate r of the Omicron shares p) comes directly from (2):

$$\dot{x} = \dot{x}_1 + \dot{x}_2 = r_1 x_1 + r_2 x_2 = [(1-p)r_1 + pr_2]x \equiv r_{\text{eff}}x$$

Effective reproduction number:
$$R_{\text{eff}} = R_1^{1-p} R_2^{p/\gamma}$$
 (5)

- ▶ Because $1/\gamma = T_1/T_2 > 1$, influence factors influencing R_1 and R_2 according to (1) have a more sensitive effect on Omicron than on Delta: If $T_1/T_2 = 1/\gamma = 2$ and measures lead to a factor $1/\sqrt{2} \approx 0.7$ on Delta (R_1) , they simultaneously lead to a factor 1/2 on Omicron (R_2)
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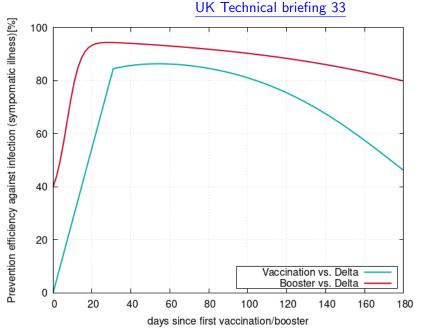
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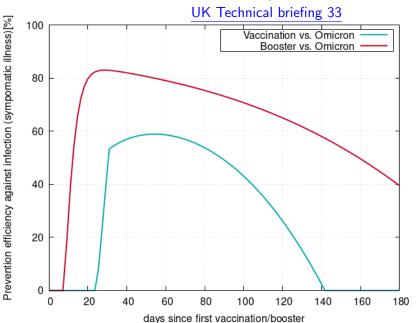
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6. Immunity I: vaccinations/boosters vs. Delta variant



"First vaccinatedfirst boostered" principle

6. Immunity II: vaccinations/boosters vs. Omicron variant



Only fresh full vaccinations or boosters help against Omicron



6. Immunity III: past infections

- ▶ 100 % immunity of Delta against Delta reinfections
- ▶ 100 % immunity of Omicron against Omicron reinfections
- ▶ 100 % no cross immunity (people can get both Delta and Omicron infections)



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Here, I make following assumptions

- lacktriangle Vaccination efficiency curves $I_1^{
 m v}(au)$ and $I_2^{
 m v}(au)$ against Delta and Omega as shown,
- lacktriangle corresponding booster efficiencies $I_1^{
 m b}(au)$ and $I_2^{
 m b}(au)$
- ► First vaccinated-first boostered

Since the protection depends on the vaccination times, I sum up the different histories weighted with the past daily vaccination and booster rates $r_{t'}^v$ and $r_{t'}^b$ (fraction of the population per day):

$$I_1^{\mathsf{vacc}}(t) = \sum_{t'=t_v}^t r_{t'}^v I_1^{\mathsf{v}}(t-t') + \sum_{t'=t_b}^t r_{t'}^b I_1^{\mathsf{b}}(t-t')$$

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Determining the population immunities in the simulator II: infections and total

Everybody can only be infected once with any variant but there is no cross immunity, so the immunity is just equal to the total percentage X_1 and X_2 of people infected with either variant:

$$I_1^x = X_1, \quad I_2^x = X_2$$

Notice: X_i is not just the cumulated number of cases divided by the population because any infection, whether detected or not detected, counts

► There is no correlation between vaccinations and infections:

$$1 - I_1 = (1 - I_1^v)(1 - I_1^x), \quad 1 - I_2 = (1 - I_2^v)(1 - I_2^x)$$
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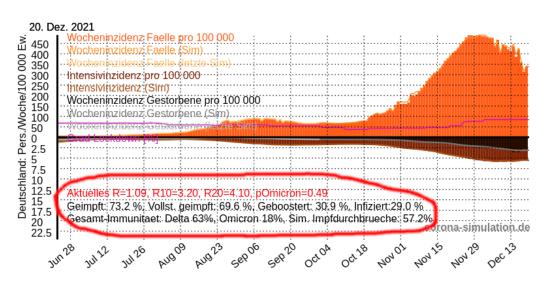
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Simulation



All items I_1 , I_2 , p, R_{10} , R_{20} , f_{season} and $f_{\text{stringency}}$ are displayed in the simulation