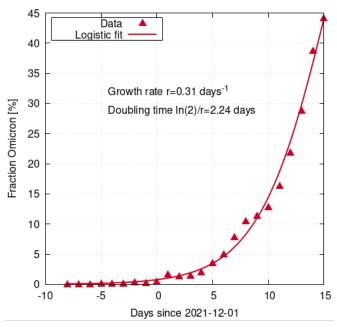


- Data from Danmark and London
- The Delta and Omicron variants coexist without directly affecting each other
- Indirect interaction via competing for common ressources, i,e., first come, first served

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#### Latest observation 2

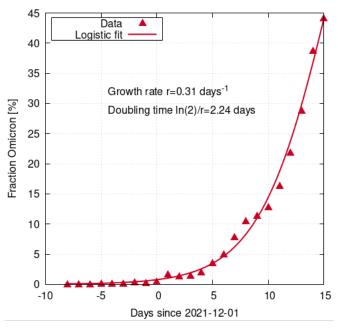


- ► The share of Omicron can be well described by a logistic function with growth rate *r*
- First transform the observed Omicron share p into the **odds ratio** y = p/(1-p)
- From Observation 1 (coexistence), is follows that the odds ratio grows exponentially:

$$y(t) = y_0 e^{rt}$$

➤ Transforming back gives the s-shaped predicted Omicron share (logistic function)

$$p(t) = \frac{y(t)}{1 + y(t)}$$

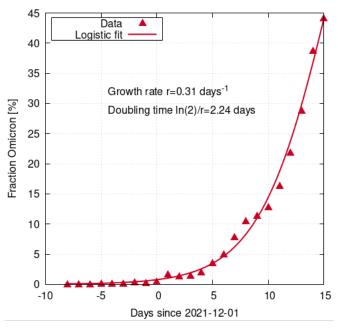


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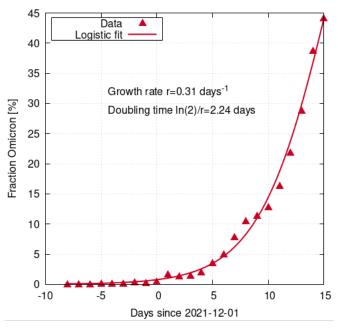


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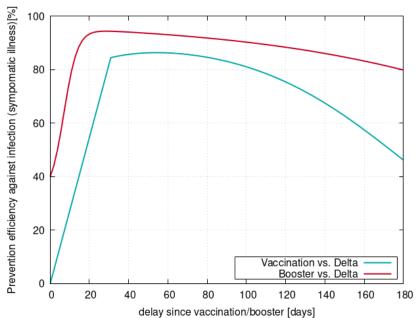
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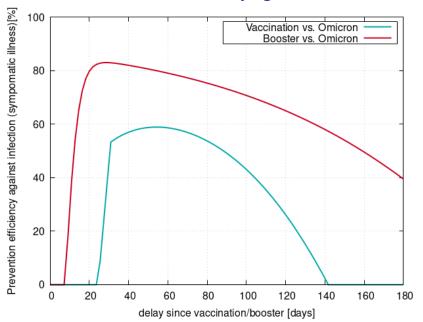
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# **Assumed efficiency against Delta infections**



"First vaccinatedfirst boostered" principle

# Assumed efficiency against Omicron infections



Only fresh full vaccinations or boosters help against Omicron



# **Assumed immunity by infections**

- ▶ 100 % immunity of Delta against Delta reinfections
- ▶ 100 % immunity of Omicron against Omicron reinfections
- ▶ 100 % no cross immunity (people can get both Delta and Omicron infections)



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(1) The spreading of the fraction p new variant (Omicron) at the cost of the old variants (Delta) is logistic:

$$p(t) = \frac{y_0 e^{rt}}{1 + y_0 e^{rt}}, \quad y_0 = \frac{p_0}{1 - p_0}$$

- (2) The growth rate r of the logistic growth depends or
  - ▶ the base reproduction numbers  $R_{10}$  and  $R_{20}$ ,
  - be the total population immunities (vaccination, boosters, infections)  $I_1$  and  $I_2$  against each variant,
  - ightharpoonup the generation time T of the infections (assumed to be equal, 5 days):

according to

$$r = \frac{1}{T} \left[ \frac{R_{20}(1 - I_2)}{R_{10}(1 - I_1)} - 1 \right]$$

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- (3) Assuming no cross effects, the effective  $R_t$  value caused by the mixture of the Delta and Omicron viruses depends on
  - the Omicron percentage p
  - $\blacktriangleright$  the base reproduction numbers  $R_{10}$  and  $R_{20}$  of Delta and Omicron, respectively,
  - the immunity escape fractions  $(1 I_1)$  and  $(1 I_2)$ ,
  - the seasonal multiplicator f<sup>season</sup>
  - the stringency (lockdown) multiplicator f<sup>stringency</sup>:

$$R_t = [(1-p)R_{10}(1-I_1) + pR_{20}(1-I_2)] f_{\text{season}} f_{\text{stringency}}$$
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- Notice: Both the growth rate r of the increase of the Delta share and the growth rate  $(R_t-1)/T$  of the actual infection wave depend on  $P_1=R_{10}(1-I_1)$  and  $P_2=R_{20}(1-I_2)$  such that a positive (negative) value of r implies an increase (decrease) of  $R_t$
- A positive Omicron spreading r does not imply that the new variant is more infectious; only the products  $P_1$  and  $P_2$  matter
- A positive spreading r can be related to a negative infection growth  $(R_t 1)/T$  both before and after the new variant dominates since, for given  $I_1$  and  $I_2$ , r is only related to the ratio  $R_{20}/R_{10}$  of the base immunities  $\Rightarrow$  next slide

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Assume at time  $t=t^*$  given population immunities  $I_1^*$  and  $I_2^*$  (see later), and estimations of the Omega share  $p^*$ , Omicron spreading rate  $r^*$ , and effective reproduction number  $R_t^*$  of the mixture. Then, we can use Eq (1) to obtain the ratio

$$\frac{R_{20}}{R_{10}} = \frac{(r^*T+1)(1-I_1^*)}{1-I_2^*} \tag{3}$$

and, with Eq (2) determine the base reproduction numbers individually:

$$R_{10} = \frac{R_t^*}{(1 + p^*r^*T)f_{\text{season}}f_{\text{stringency}}} \tag{4}$$

For  $t > t^*$ , I assume fixed base reproduction numbers and calculate the future Omicron spreading and the future wave using (1) and (2) with time varying  $I_1$ ,  $I_2$ , p,  $f_{\text{season}}$ , and  $f_{\text{stringency}}$ 



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#### Here, I make following assumptions

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- ► First vaccinated-first boostered

Since the protection depends on the vaccination times, I sum up the different histories weighted with the past daily vaccination and booster rates  $r_{t'}^v$  and  $r_{t'}^b$  (fraction of the population per day):

$$I_1^{\mathsf{vacc}}(t) = \sum_{t'=t_v}^t r_{t'}^v I_1^{\mathsf{v}}(t-t') + \sum_{t'=t_v}^t r_{t'}^b I_1^{\mathsf{b}}(t-t')$$

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# Determining the population immunities II: infections and total

Everybody can only be infected once with any variant but there is no cross immunity, so the immunity is just equal to the total percentage  $X_1$  and  $X_2$  of people infected with either variant:

$$I_1^x = X_1, \quad I_2^x = X_2$$

*Notice*:  $X_i$  is not just the cumulated number of cases divided by the population because any infection, whether detected or not detected, counts

There is no correlation between vaccinations and infections:

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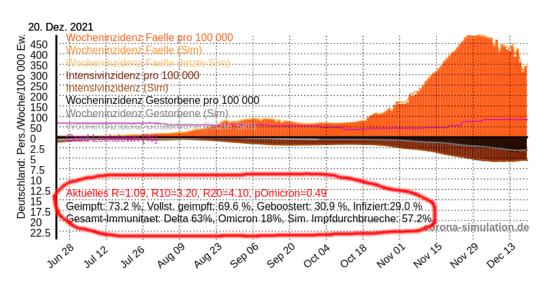
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#### **Simulation**



All items  $I_1$ ,  $I_2$ , p,  $R_{10}$ ,  $R_{20}$ ,  $f_{\text{season}}$  and  $f_{\text{stringency}}$  are displayed in the simulation