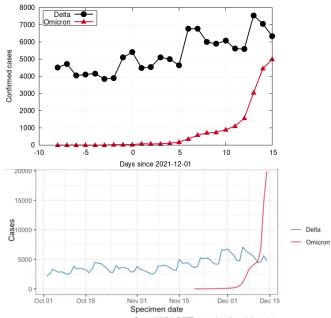
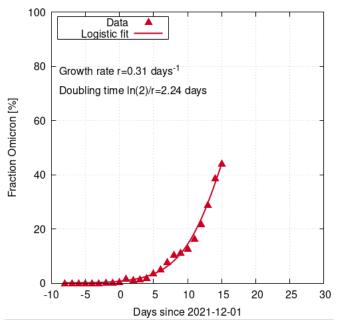
#### Latest observation 1

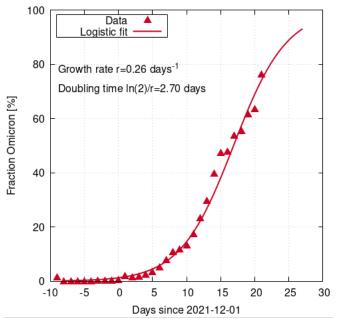


- Data from Danmark and London
- The Delta and Omicron variants coexist without directly affecting each other
- Indirect interaction via competing for common ressources, i,e., first come, first served

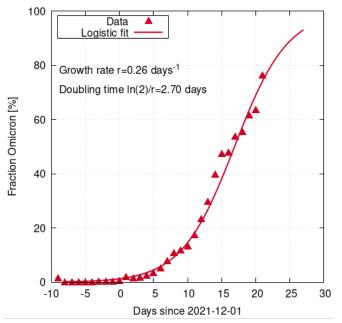
### Latest observation 2



► The share of Omicron can be well described by a logistic function with growth rate *r* 

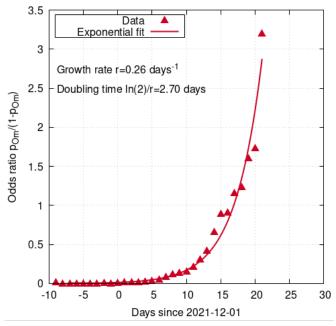


Data update.



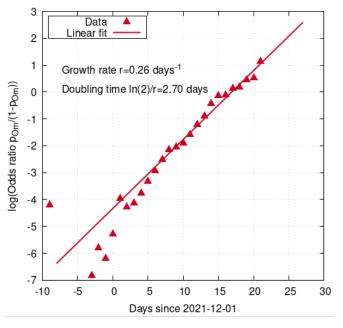
▶ Data update. How to get the curve?





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- Transform the observed Omicron share p into the odds ratio y = p/(1-p)
- ► From Observation 1 (coexistence), it follows that the odds ratio grows exponentially:

$$y(t) = y_0 e^{rt}$$

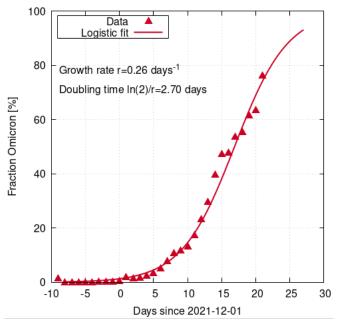


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 Transforming back gives the s-shaped predicted Omicron share (logistic function)

$$p(t) = \frac{y(t)}{1 + y(t)}$$

### Assumptions:

- ▶ Neither positive nor negative **cross effects**: Each variant acts on its own (using common ressources of susceptible humans)
- ▶ The Delta and Omicron variants have different base reproduction numbers  $R_{10}$  and  $R_{20}$  and different generation times  $T_1$  and  $T_2$ , respectively (e.g.,  $R_{10} = 5$ ,  $T_1 = 5 \, \text{days}$ ,  $T_2 = 4 \, \text{days}$ )
- The immunities  $I_1$  and  $I_2$  (including vaccinations and past infections) against Delta and Omicron are generally different
- ightharpoonup The reduction factors  $f_{
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- lacktriangle All factors influencing the effective reproduction number R are multiplicative

 $\Rightarrow \begin{array}{l} x_1(t_0+T_1) = R_1x_1(t_0) = R_{10}(1-I_1)f_{\rm m}f_{\rm s}x_1(t_0), \\ x_2(t_0+T_2) = R_2x_2(t_0) = R_{20}(1-I_2)f_{\rm m}f_{\rm s}x_2(t_0) \end{array}$ 

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Assuming continuous infections (slowly varying rates), we can write (1) as

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# Determining the Omicron base reproduction rate from the logistic growth rate $\it r$

Just use Relation (3) and insert the definitions of  $R_1$  and  $R_2$  from (1)

After some manipulations ..

$$R_{20} = \exp(rT_2) f_{\rm m}^{\gamma - 1} f_{\rm s}^{\gamma - 1} \frac{(R_{10}(1 - I_1))^{\gamma}}{1 - I_2}, \quad \gamma = \frac{T_2}{T_1}$$
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For equal generation times  $T_1 = T_2 = T$ , the measures and the seasonal effects drop out and r depends only on the past infection and vacination immunities (remains time dependent since the immunities change):

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The **effective growth rate**  $r_{\text{eff}}$  of the infection dynamics (not to be confused with the logistic growth rate r of the Omicron shares p) comes directly from (2):

$$\dot{x} = \dot{x}_1 + \dot{x}_2 = r_1 x_1 + r_2 x_2 = [(1-p)r_1 + pr_2]x \equiv r_{\text{eff}}x$$

$$\ln R_{\text{eff}} = (1 - p) \ln R_1 + \frac{p}{\gamma} \ln R_2 \tag{5}$$

- Because  $1/\gamma=T_1/T_2>1$ , influence factors, e.g., measures, have a more sensitive effect on Omicron than om Delta: If  $T_1/T_2=2$  and measures lead to a factor  $1/\sqrt{2}\approx 0.7$  on Delta  $(R_1)$ , they simultaneously lead to a factor 1/2 on Omicron  $(R_2)$
- If, at a certain time, the true Omicron share p, the effective reproduction number  $R_{\rm eff}$ , and the logistic growth rate r are known (all three can be estimated), and the generation time ratio  $\gamma = T_2/T_1$  as well as the total immunities  $I_1$  and  $I_2$  and the effects of the measures and the season at this time can be estimated, the Eqs (1), (5), and (4) allow for a simultaneous estimation of  $R_{10}$  and  $R_{20}$  are

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- Because  $1/\gamma=T_1/T_2>1$ , influence factors, e.g., measures, have a more sensitive effect on Omicron than om Delta: If  $T_1/T_2=2$  and measures lead to a factor  $1/\sqrt{2}\approx 0.7$  on Delta  $(R_1)$ , they simultaneously lead to a factor 1/2 on Omicron  $(R_2)$
- If, at a certain time, the true Omicron share p, the effective reproduction number  $R_{\rm eff}$ , and the logistic growth rate r are known (all three can be estimated), and the generation time ratio  $\gamma = T_2/T_1$  as well as the total immunities  $I_1$  and  $I_2$  and the effects of the measures and the season at this time can be estimated, the Eqs (1), (5), and (4) allow for a simultaneous estimation of  $R_{10}$  and  $R_{20}$  and  $R_{20}$  and  $R_{20}$  are  $R_{20}$  and  $R_{20}$  and  $R_{20}$  and  $R_{20}$  and  $R_{20}$  are  $R_{20}$  and  $R_{20}$  and  $R_{20}$  and  $R_{20}$  are  $R_{20}$  and  $R_{20}$  and  $R_{20}$  are  $R_{20}$  and  $R_{20}$  are  $R_{20}$  and  $R_{20}$  and  $R_{20}$  are  $R_{20}$

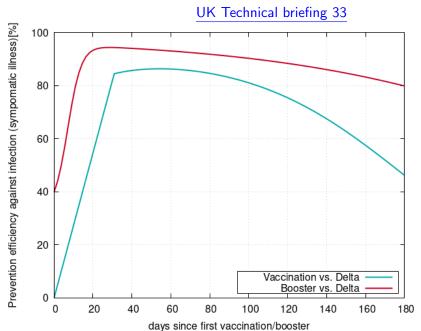
The **effective growth rate**  $r_{\text{eff}}$  of the infection dynamics (not to be confused with the logistic growth rate r of the Omicron shares p) comes directly from (2):

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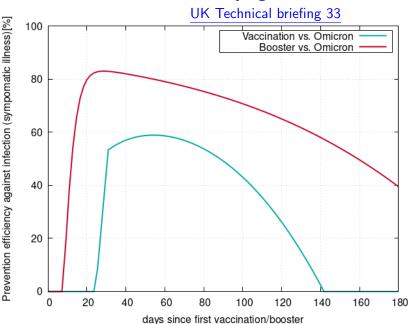
### Assumed efficiency against Delta infections



"First vaccinatedfirst boostered" principle



### Assumed efficiency against Omicron infections



Only fresh full vaccinations or boosters help against Omicron



### **Assumed immunity by infections**

- ▶ 100 % immunity of Delta against Delta reinfections
- ▶ 100 % immunity of Omicron against Omicron reinfections
- 100 % no cross immunity (people can get both Delta and Omicron infections)



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### Here, I make following assumptions

- $lackbox{ Vaccination efficiency curves } I_1^{
  m v}( au)$  and  $I_2^{
  m v}( au)$  against Delta and Omega as shown,
- lacktriangle corresponding booster efficiencies  $I_1^{\mathrm{b}}( au)$  and  $I_2^{\mathrm{b}}( au)$
- ► First vaccinated-first boostered

Since the protection depends on the vaccination times, I sum up the different histories weighted with the past daily vaccination and booster rates  $r_{t'}^v$  and  $r_{t'}^b$  (fraction of the population per day):

$$I_1^{\sf vacc}(t) = \sum_{t'=t_v}^t r_{t'}^v I_1^{\sf v}(t-t') + \sum_{t'=t_b}^t r_{t'}^b I_1^{\sf b}(t-t')$$

where  $t_b$  is the time of the first booster shot, and  $t_v$  the oldest time of the first vaccination of any person who is not yet boostered.

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### Determining the population immunities II: infections and total

Everybody can only be infected once with any variant but there is no cross immunity, so the immunity is just equal to the total percentage  $X_1$  and  $X_2$  of people infected with either variant:

$$I_1^x = X_1, \quad I_2^x = X_2$$

*Notice*:  $X_i$  is not just the cumulated number of cases divided by the population because any infection, whether detected or not detected, counts

There is no correlation between vaccinations and infections:

$$1 - I_1 = (1 - I_1^v)(1 - I_1^x), \quad 1 - I_2 = (1 - I_2^v)(1 - I_2^x)$$
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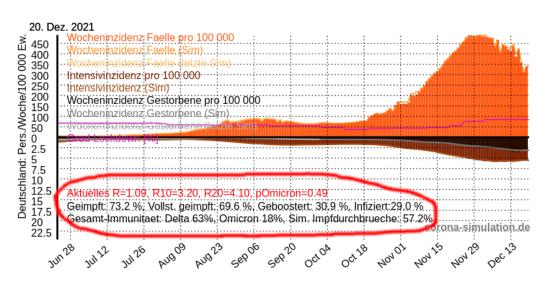
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#### **Simulation**



All items  $I_1$ ,  $I_2$ , p,  $R_{10}$ ,  $R_{20}$ ,  $f_{\text{season}}$  and  $f_{\text{stringency}}$  are displayed in the simulation