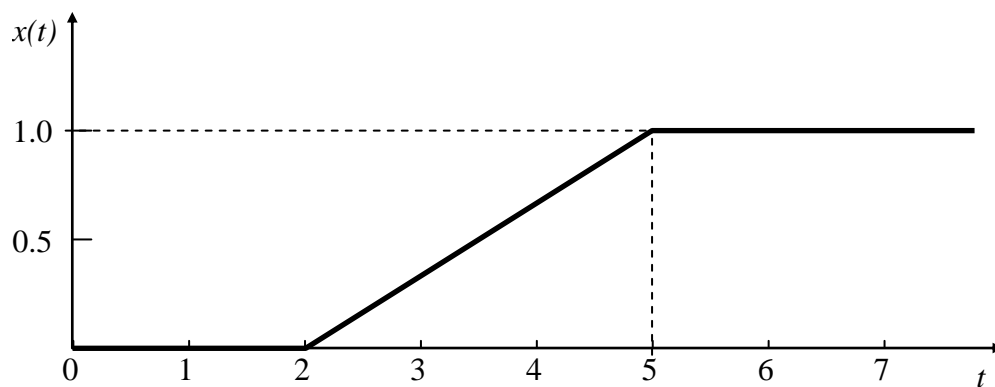
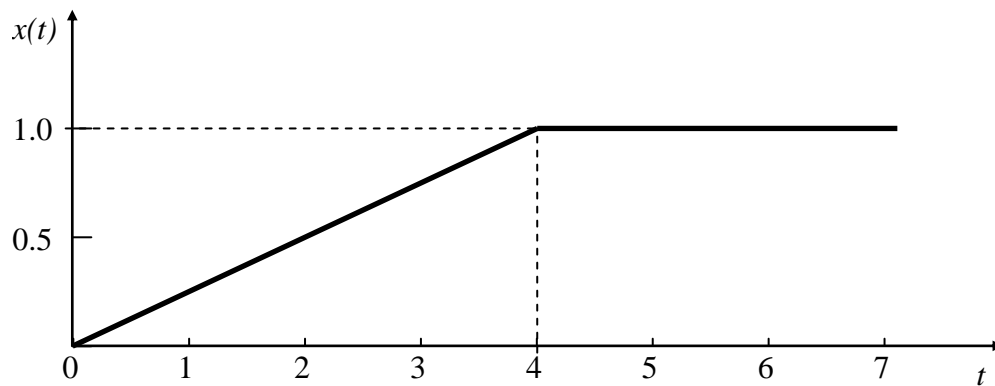


## MECH9211 - MODELLING AND CONTROL OF MECHATRONIC SYSTEMS

### TUTORIAL 3

1. Find the z-transforms of the unit impulse (Kronecker Delta), step input and the two curves shown below.



2. Use the partial fraction expansion method (use **residue** function) to obtain closed form solutions to the following.

$$\frac{z^{-1}(0.5 - z^{-1})}{(1 - 1.5z^{-1})(1 - z^{-1})^2}$$

$$\frac{2 + z^{-2}}{(1 - 0.5z^{-1})^2(1 - z^{-1})}$$

$$\frac{0.368z^2 + 0.478z + 0.154}{z^2(z - 1)}$$

$$\frac{z^{-3}}{(1 - z^{-1})(1 - 0.2z^{-1})}$$

verify your results by using **dimpulse** function of MATLAB.

3. Obtain the solutions for the following two difference equations.

$$x(k) = 0 \text{ for } k < 0 \text{ and } u(k) = \begin{cases} 0; & k < 0 \\ 1; & k \geq 0 \end{cases}$$

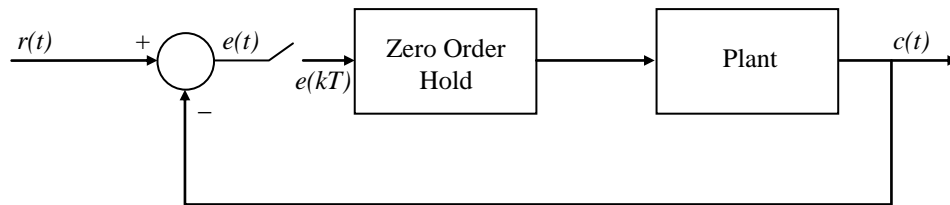
The difference equations are:

$$x(k+2) - x(k+1) + 0.25x(k) = u(k+2) \quad \text{and}$$

$$x(k+2) - 3x(k+1) + 2x(k) = u(k)$$

Compare your results with those obtained using **dstep** function.

Obtain the pulse transfer function for the system shown below, where the transfer function of the plant is  $K/(s+1)$ .



4. Obtain the pulse transfer functions of the two systems shown below. Assume the samplers to be synchronised with a sampling interval of T seconds.

