

**HACETTEPE UNIVERSITY**  
**DEPARTMENT OF COMPUTER ENGINEERING**  
**BBM231 LOGIC DESIGN**

**Homework 2 (For all sections)**

**Assigned**

**: 5.11.2018**

**Due**

**: 12.11.2018**

**Hand in your homework solutions in class.**

**QUESTIONS:**

**Q1.** Simplify the following Boolean functions using four-variable maps:

**a)**  $F(w, x, y, z) = \sum(0, 1, 4, 5, 6, 7, 8, 9)$

**b)**  $F(A, B, C, D) = A'B'C'D' + A'CD' + AB'D' + ABCD + A'BD$

**Q2.** Find all the prime implicants for the Boolean functions and determine which are essential:

a)  $F(A, B, C, D) = \sum(1, 3, 4, 5, 10, 11, 12, 13, 14, 15)$

b)  $F(w, x, y, z) = \sum(0, 2, 4, 5, 6, 7, 8, 10, 13, 15)$

**Q3.** Given  $h = f \oplus g$ ,

$$f(w,x,y,z) = \sum(2,3,5,6,7,12,13,15),$$

$$g(w,x,y,z) = \sum(1,3,4,5,6,8,11,12,14,15),$$

find the minimal expression for  $h(w,x,y,z)$  and draw its circuit using minimum number of two-input-gates. You can use AND, OR, NOT, XOR gates with two-inputs.

**Q4.** A majority function has an output value of one if there are more 1s than 0s on its inputs.

- a. Express three input majority function in sum of minterms form after filling the truth table.
- b. Implement the **optimized circuit** with only NAND gates.

**Q5.** Implement the following Boolean function  $F$ , together with the don't-care conditions  $d$ , using no more than two NOR Gates.

$$F(A, B, C, D) = \sum(2, 4, 6, 10, 12)$$

$$d(A, B, C, D) = \sum(0, 8, 9, 13)$$

Assume that both the normal and complement inputs are available.