

# Artificial Intelligence

## Chapter 11: Planning

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# Introduction

- Planning is the task of coming up with a sequence of actions that will achieve the goal
- *Classical planning environments*
  - Fully observable, deterministic, finite, static (change only happens when the agent acts), and discrete (in time, action, objects)

# Introduction

- A plan is **complete** iff every precondition is achieved
- A precondition is **achieved** iff it is the effect of an earlier step and no possibly intervening step undoes it

# Search vs. Planning

- Consider a Internet Buying Agent whose task it is to buy our text book (search based)
  - ISBN# 0137903952
  - $10^9$  possibilities
  - Searched based agent
    - One buying action for each ISBN number
    - Difficult to find a good heuristic
  - Planning based agent
    - Work backwards
    - Goal is *Have(0137903952)*
    - *Have(x)* results from *Buy(x)*
    - Therefore *Buy(0137903952)*

# Search vs. Planning

- Now let's buy 4 books...
  - $10^{40}$  plans of just 4 steps using searching
    - Must search with a heuristic
      - Use # books remaining?
      - Not useful for our agent since it sees the goal test only as a black box that returns True or False for each state
      - Lacks autonomy; requires a human to supply a heuristic function for each new problem

# Search vs. Planning

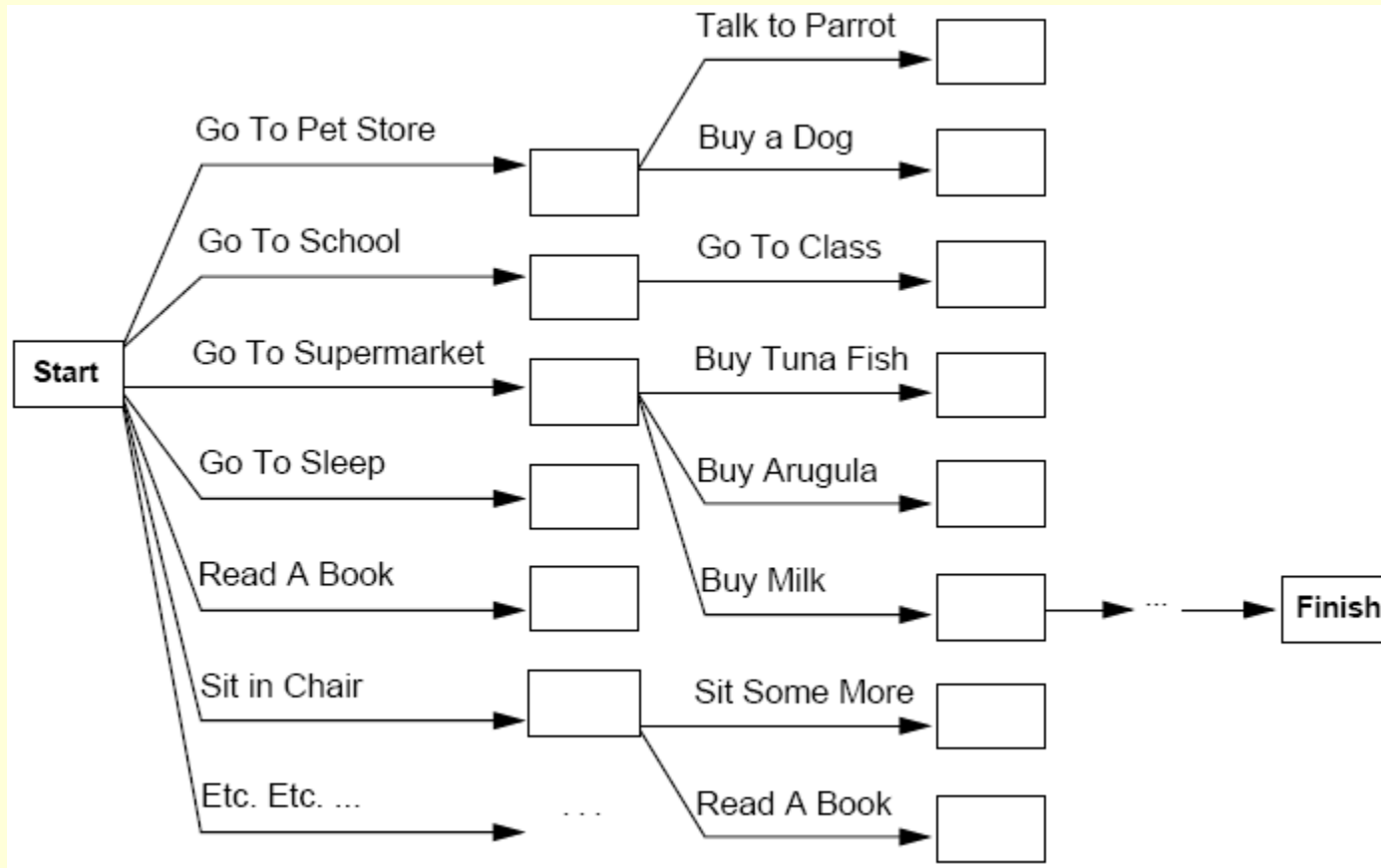
- If our planning agent could use a conjunction of subgoals
  - Then it could use a single domain-independent heuristic
    - The number of unsatisfied conjuncts
  - $\text{Have}(A) \wedge \text{Have}(B) \wedge \text{Have}(C) \wedge \text{Have}(D)$
  - A state containing  $\text{Have}(A) \wedge \text{Have}(B)$  would have a cost 2

# Search vs. Planning

- Another example:
  - Consider the task of getting milk, bananas, and a cordless drill
    - Really want to go to supermarket and then go to the hardware store
    - But we could get sidetracked!
      - By irrelevant actions



# Search vs. Planning



# Search vs. Planning

- Planning Systems do the following:
  - Open up action and goal representation to allow selection
  - Divide-and-conquer by sub-goaling
  - Relax requirement for sequential construction of solutions

# The Language of Planning Problems

- Representation of states
  - Decompose the world into logical conditions and represent a state as a conjunction of positive literals
  - Must be ground and function-free
  - Examples:
    - $\text{Poor} \wedge \text{Unknown}$
    - $\text{At}(\text{Plane}_1, \text{CLE}) \wedge \text{At}(\text{Plane}_2, \text{LAS})$
    - $\text{At}(x,y)$  or  $\text{At}(\text{Father}(\text{Fred}), \text{CLE})$  (not allowed)

# The Language of Planning Problems

- Representation of goals
  - A partially specified state
  - Represented as a conjunction of ground literals
  - Examples
    - $At(Plane_1, LAS)$
    - $Rich \wedge Famous$
  - State  $\mathbf{s}$  satisfies goal  $\mathbf{g}$  if  $\mathbf{s}$  contains all the atoms in  $\mathbf{g}$  (and possibly others)
    - $Rich \wedge Famous \wedge Miserable$  satisfies  $Rich \wedge Famous$

# The Language of Planning Problems

- Representation of actions
  - Specified in terms of the preconditions that must hold before it can be executed and the effects that ensue when it is executed
  - Action( Fly( p, from, to ))
    - Precond:  $\text{At}(p, \text{from}) \wedge \text{Plane}(p) \wedge \text{Airport}(\text{from}) \wedge \text{Airport}(\text{to})$
    - Effect:  $\neg \text{At}(p, \text{from}) \wedge \text{At}(p, \text{to})$
  - This is also known as an **action schema**

# Search vs. Planning Again

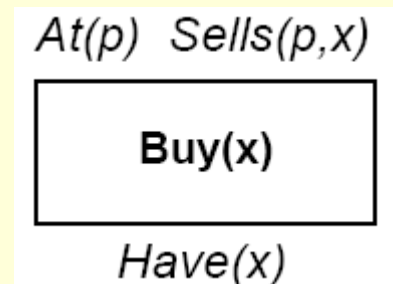
- Search
  - States: program data structures
  - Actions: program code
  - Goal: program code
  - Plan: sequence from  $S_0$
- Planning
  - States: logical sentences
  - Actions: preconditions and outcomes
  - Goal: logical sentences (conjunction)
  - Plan: constraints on actions

# Example

- Suppose our current state is:
  - $At(P1, CLE) \wedge At(P2, LAS) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(CLE) \wedge Airport(LAS)$
- This state satisfies the precondition
  - $At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$
- Using the substitution
  - $\{p/P1, from/CLE, to/LAS\}$
- The following concrete action is applicable
  - $Fly(P1, CLE, LAS)$

# STRIPS

- Stanford Research Institute Problem Solver
- A restricted language for planning that describes actions and descriptions of objects in a system
- Example
  - Action:  $Buy(x)$
  - Precondition:  $At(p), Sells(p, x)$
  - Effect:  $Have(x)$





# STRIPS

- This abstracts away many important details!
- Restricted language -> efficient algorithm
  - Precondition: conjunction of positive literals
  - Effect: conjunction of literals
- A complete set of STRIPS operators can be translated into a set of successor-state axioms

# STRIPS

- Only positive literals in states:  
*Poor  $\wedge$  Unknown*
- Closed world assumption:  
*Unmentioned literals are false*
- Effect  $P \wedge \neg Q$ :  
*Add  $P$  and delete  $Q$*
- Only ground literals in goals:  
*Rich  $\wedge$  Famous*

# STRIPS

- Goals are conjunctions:  
*Rich*  $\wedge$  *Famous*
- Effects are conjunctions:
- No support for equality
- No support for types

# ADL

- Positive and negative literals in states:  
 *$\neg Rich \wedge \neg Famous$*
- Open world assumption:  
*Unmentioned literals are unknown*
- Effect  $P \wedge \neg Q$ :  
*Add  $P$  and  $\neg Q$  and delete  $\neg P$  and  $Q$*
- Quantified variables in goals:  
 *$\exists x At(P_1, x) \wedge At(P_2, x)$  is the goal of having  $P_1$  and  $P_2$  in the same place*

# ADL

- Goals allow conjunction and disjunction:  
 $\neg \textit{Poor} \wedge (\textit{Famous} \vee \textit{Smart})$
- Conditional Effects are allowed:  
***when**  $P$ :  $E$  means  $E$  is an effect only if  $P$  is satisfied*
- Equality predicate built in:  
 $(x = y)$
- Variables can have types:  
 $(p : \textit{Plane})$

# Example: Air Cargo Transport

- $\text{Init}(\text{At}(C_1, \text{CLE}) \wedge \text{At}(C_2, \text{LAS}) \wedge \text{At}(P_1, \text{CLE}) \wedge \text{At}(P_2, \text{LAS}) \wedge \text{Cargo}(C_1) \wedge \text{Cargo}(C_2) \wedge \text{Plane}(P_1) \wedge \text{Plane}(P_2) \wedge \text{Airport}(\text{CLE}) \wedge \text{Airport}(\text{LAS}))$
- $\text{Goal}(\text{At}(C_1, \text{LAS}) \wedge \text{At}(C_2, \text{CLE}))$

# Example: Air Cargo Transport

- *Action( Load( $c, p, a$ ),*  
*Precond:  $At(c, a) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$*   
*Effect:  $\neg At(c, a) \wedge In(c, p)$* )
- *Action( Unload( $c, p, a$ ),*  
*Precond:  $In(c, p) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$*   
*Effect:  $At(c, a) \wedge \neg In(c, p)$* )
- *Action( Fly( $p, from, to$ ),*  
*Precond:  $At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$*   
*Effect:  $\neg At(p, from) \wedge At(p, to)$* )

# Example: Air Cargo Transport

[ Load( $C_1$ ,  $P_1$ , CLE), Fly( $P_1$ , CLE, LAS),  
Unload(  $C_1$ ,  $P_1$ , LAS),  
Load( $C_2$ ,  $P_2$ , LAS), Fly( $P_2$ , LAS, CLE),  
Unload(  $C_2$ ,  $P_2$ , CLE)]

- Is it possible for a plane to fly to and from the same airport?



# Example: The Spare Tire Problem

- $\text{Init}(\text{At}(\text{Flat}, \text{Axle}) \wedge \text{At}(\text{Spare}, \text{Trunk}))$
- $\text{Goal}(\text{At}(\text{Spare}, \text{Axle}))$

# Example: The Spare Tire Problem

- *Action( Remove( Spare, Trunk ),*  
    *Precond: At( Spare, Trunk )*  
    *Effect:  $\neg \text{At( Spare, Trunk )} \wedge \text{At( Spare, Ground )}$*
- *Action( Remove( Flat, Axle ),*  
    *Precond: At( Flat, Axle )*  
    *Effect:  $\neg \text{At( Flat, Axle )} \wedge \text{At( Flat, Ground )}$*
- *Action( PutOn( Spare, Axle ),*  
    *Precond:  $\text{At( Spare, Ground )} \wedge \neg \text{At( Flat, Axle )}$*   
    *Effect:  $\neg \text{At( Spare, Ground )} \wedge \text{At( Spare, Axle )}$*
- *Action( LeaveOvernight,*  
    *Precond:*  
    *Effect:  $\neg \text{At( Spare, Ground )} \wedge \neg \text{At( Spare, Axle )} \wedge \neg \text{At( Spare, Trunk )} \wedge \neg \text{At( Flat, Ground )} \wedge \neg \text{At( Flat, Axle )}$*

# Example: The Blocks World

- Init(  $\text{On}(A, \text{Table}) \wedge \text{On}(B, \text{Table}) \wedge \text{On}(C, \text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(B) \wedge \text{Clear}(C)$  )
- Goal(  $\text{On}(A, B) \wedge \text{On}(B, C)$  )

# Example: The Blocks World

- *Action( Move(  $b, x, y$  ),*  
*Precond:  $On(b, x) \wedge Clear(b) \wedge Clear(y) \wedge Block(b) \wedge$*   
 *$(b \neq x) \wedge (b \neq y) \wedge (x \neq y)$*   
*Effect:  $On(b, y) \wedge Clear(x) \wedge \neg On(b, x) \wedge \neg Clear(y)$ )*
- *Action( MoveToTable(  $b, x$  ),*  
*Precond:  $On(b, x) \wedge Clear(b) \wedge Block(b) \wedge (b \neq x)$*   
*Effect:  $On(b, Table) \wedge Clear(x) \wedge \neg On(b, x)$ )*

# Example: The Blocks World

- A plan for building a three block tower
- [Move(B, Table, C), Move(A, Table, B)]

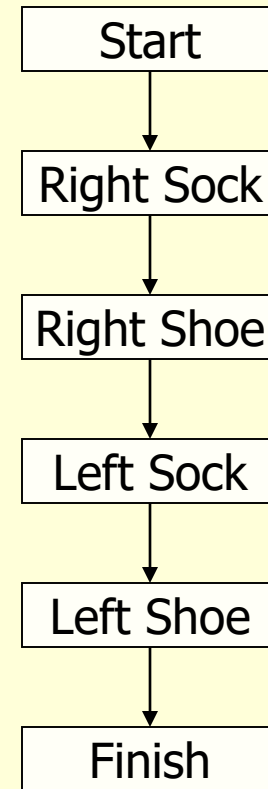
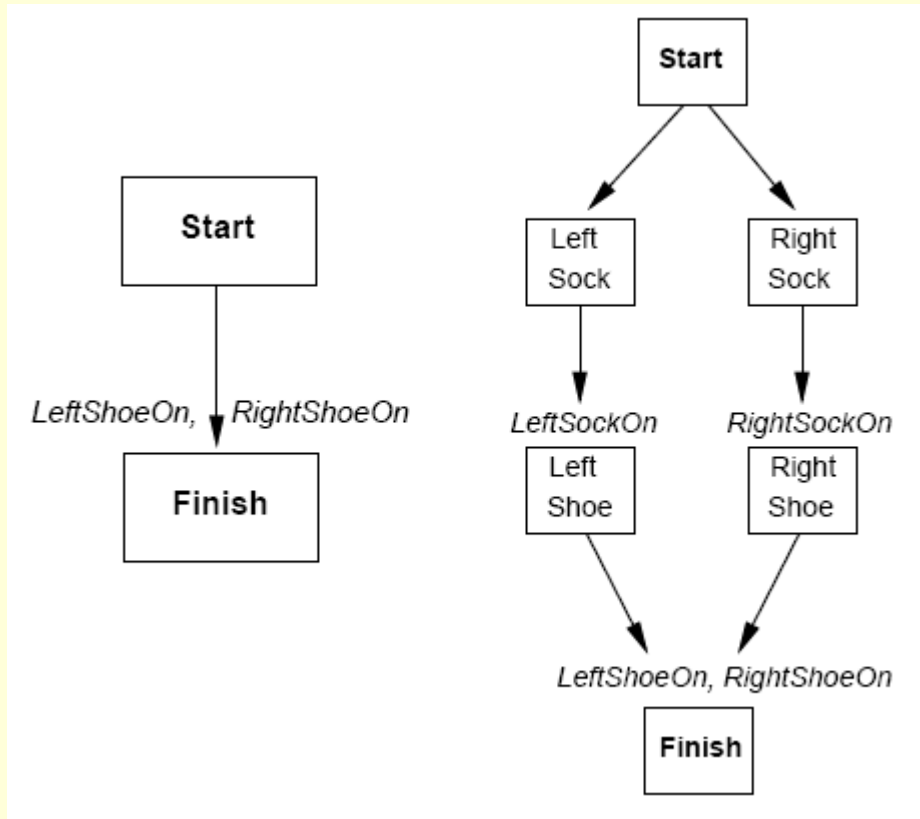
# Partially Ordered Plans

- Partially Ordered Plan
  - A partially ordered collection of steps
    - **Start step** has the initial state description and its effect
    - **Finish step** has the goal description as its precondition
    - **Causal links** from outcome of one step to precondition of another step
    - **Temporal ordering** between pairs of steps

# Partial Ordered Plans

- An open condition is a precondition of a step not yet causally linked
- A plan is **complete** iff every precondition is achieved
- A precondition is **achieved** iff it is the effect of an earlier step and no possibly intervening step undoes it

# Partially Ordered Plans

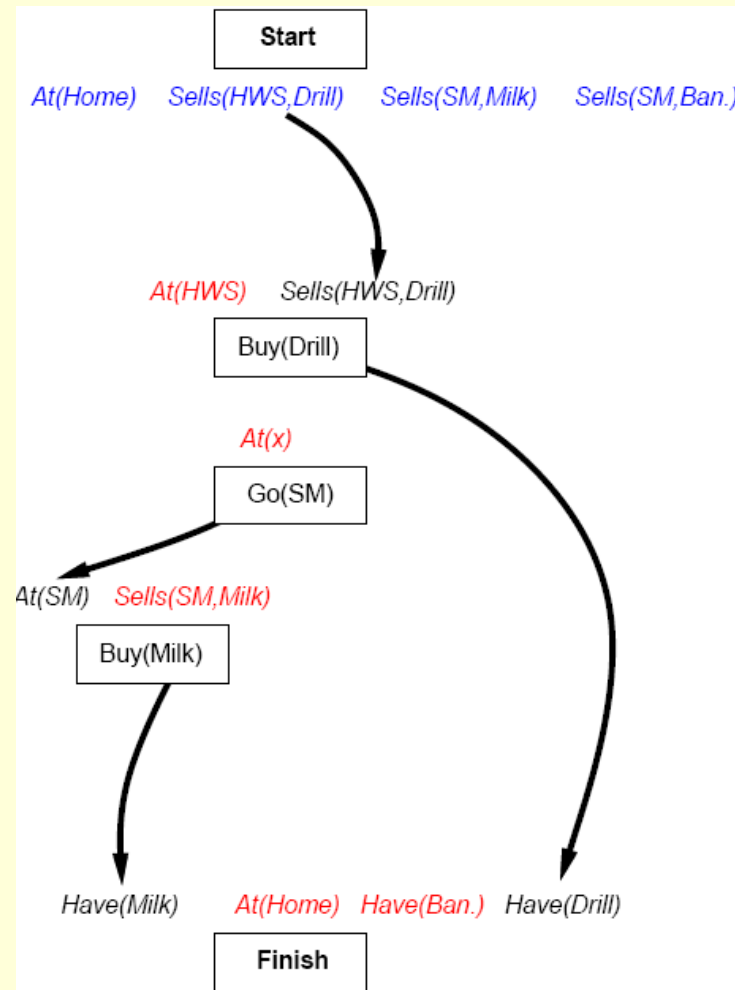




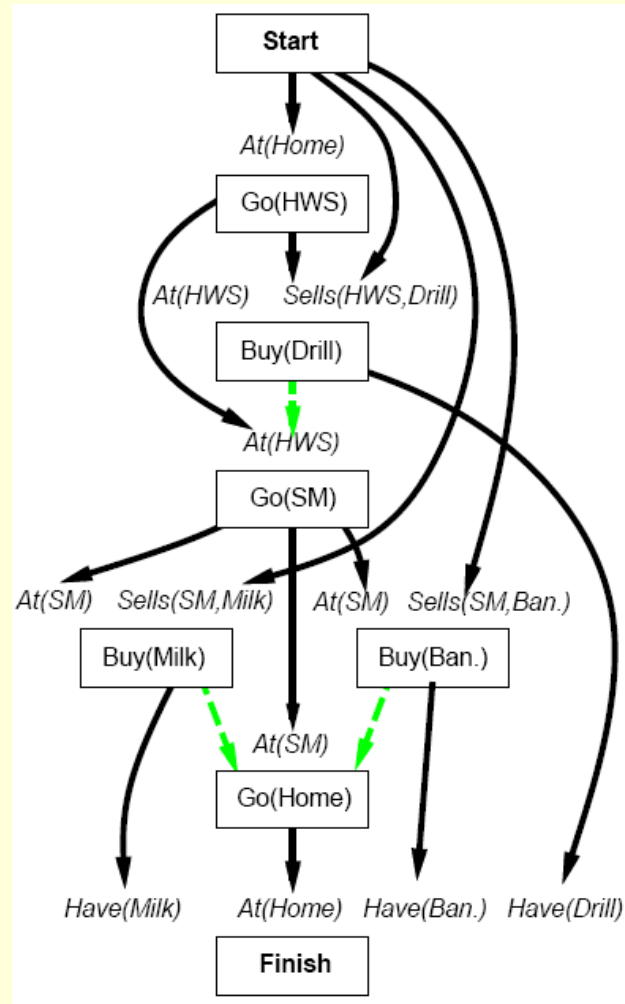
# Partially Ordered Plans



# Partially Ordered Plans



# Partially Ordered Plans



# POP Algorithm

**function** POP(*initial*, *goal*, *operators*) **returns** *plan*

*plan*  $\leftarrow$  MAKE-MINIMAL-PLAN(*initial*, *goal*)

**loop do**

**if** SOLUTION?(*plan*) **then return** *plan*

$S_{need}, c \leftarrow$  SELECT-SUBGOAL(*plan*)

    CHOOSE-OPERATOR(*plan*, *operators*,  $S_{need}$ ,  $c$ )

    RESOLVE-THREATS(*plan*)

**end**

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**function** SELECT-SUBGOAL(*plan*) **returns**  $S_{need}, c$

    pick a plan step  $S_{need}$  from STEPS(*plan*)

        with a precondition  $c$  that has not been achieved

**return**  $S_{need}, c$

# POP Algorithm

**procedure** CHOOSE-OPERATOR( $plan, operators, S_{need}, c$ )

**choose** a step  $S_{add}$  from  $operators$  or  $STEPS(plan)$  that has  $c$  as an effect  
  **if** there is no such step **then fail**  
  add the causal link  $S_{add} \xrightarrow{c} S_{need}$  to  $LINKS(plan)$   
  add the ordering constraint  $S_{add} \prec S_{need}$  to  $ORDERINGS(plan)$   
  **if**  $S_{add}$  is a newly added step from  $operators$  **then**  
    add  $S_{add}$  to  $STEPS(plan)$   
    add  $Start \prec S_{add} \prec Finish$  to  $ORDERINGS(plan)$

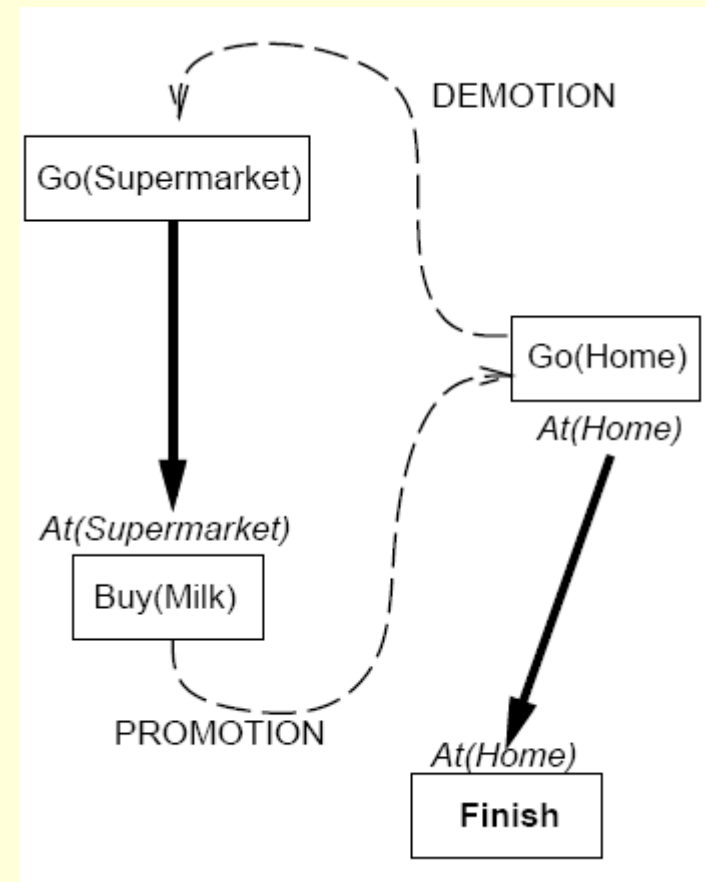
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**procedure** RESOLVE-THREATS( $plan$ )

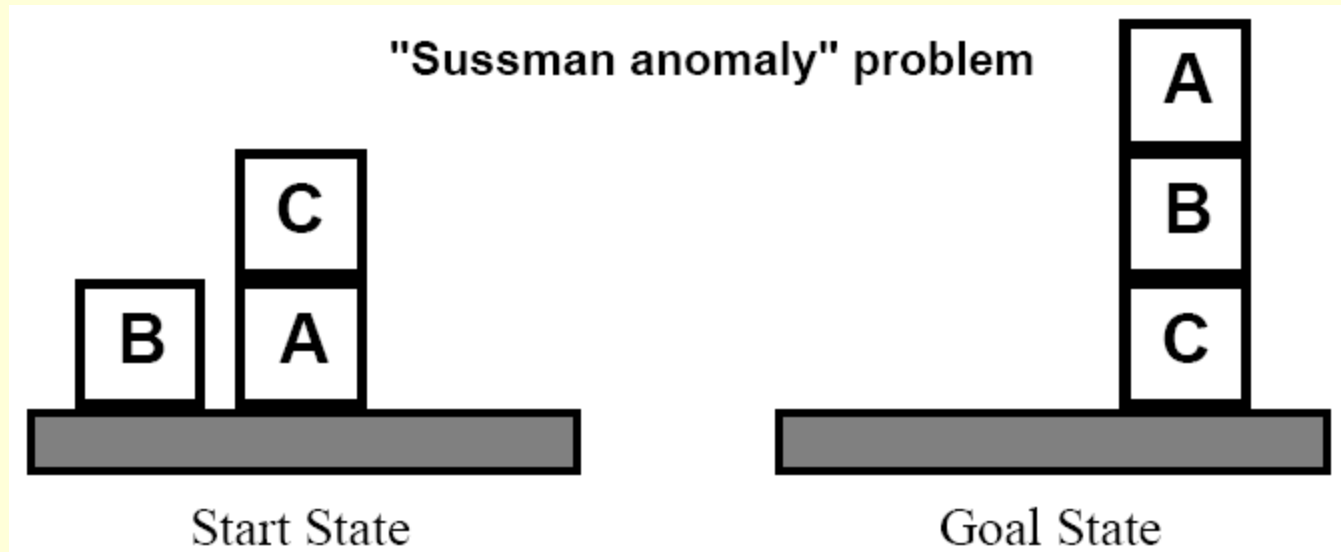
**for each**  $S_{threat}$  that threatens a link  $S_i \xrightarrow{c} S_j$  in  $LINKS(plan)$  **do**  
    **choose** either  
      *Demotion:* Add  $S_{threat} \prec S_i$  to  $ORDERINGS(plan)$   
      *Promotion:* Add  $S_j \prec S_{threat}$  to  $ORDERINGS(plan)$   
    **if not** CONSISTENT( $plan$ ) **then fail**  
  **end**

# Clobbering

- A **clobberer** is a potentially intervening step that destroys the condition achieved by a causal link
  - Example Go(Home) clobbers At(Supermarket)
- Demotion
  - Put before Go(Supermarket)
- Promotion
  - Put after Buy(Milk)



# Example: Blocks World



$Clear(x) \ On(x,z) \ Clear(y)$

PutOn(x,y)

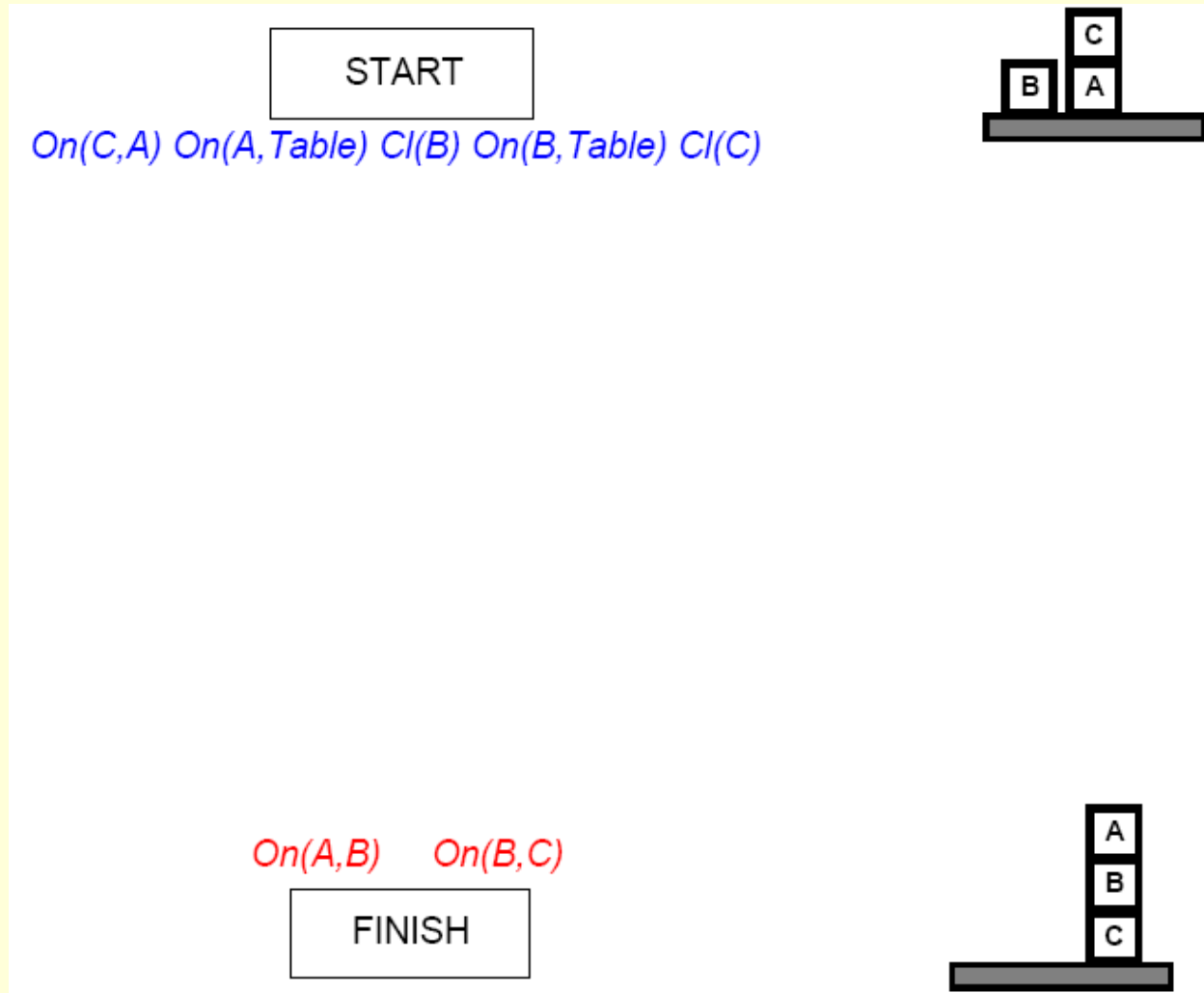
$\sim On(x,z) \ \sim Clear(y)$   
 $Clear(z) \ On(x,y)$

$Clear(x) \ On(x,z)$

PutOnTable(x)

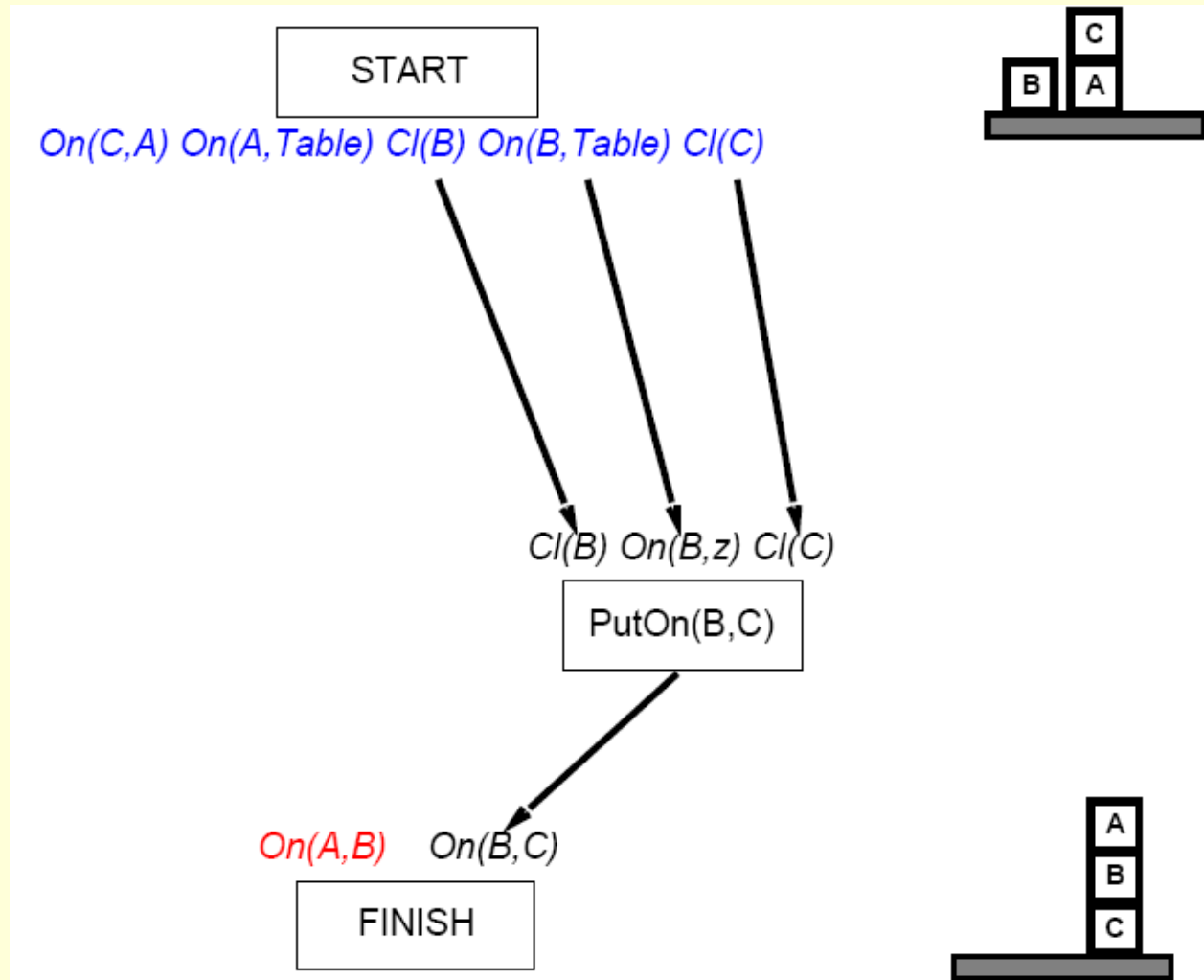
$\sim On(x,z) \ Clear(z) \ On(x, Table)$

# Example: Blocks World

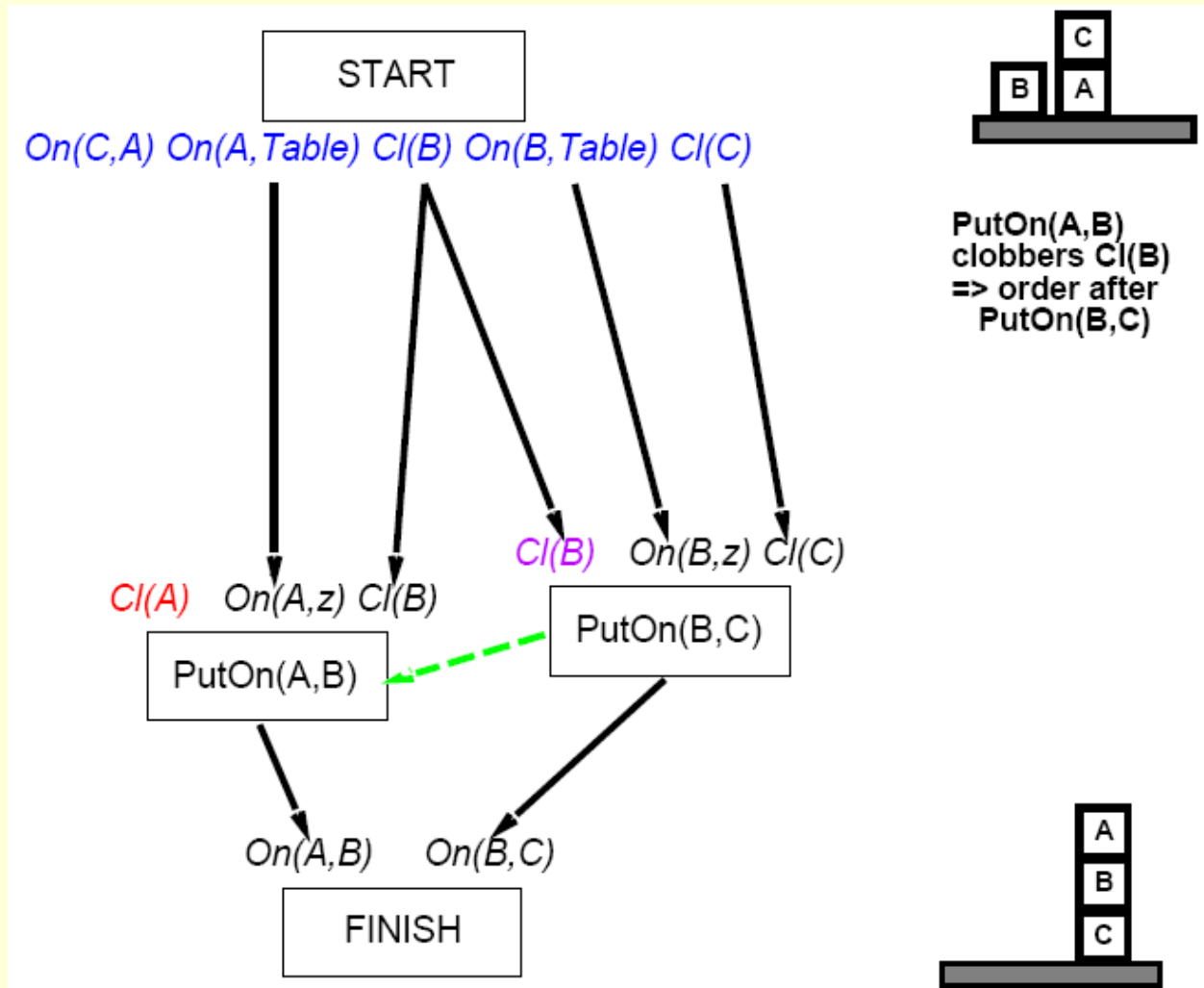




# Example: Blocks World



# Example: Blocks World



# Example: Blocks World

