

**HACETTEPE UNIVERSITY**  
**DEPARTMENT OF COMPUTER ENGINEERING**  
**BBM231 LOGIC DESIGN**

**Homework 4 (For all sections)**

**Assigned : 12.12.2018**

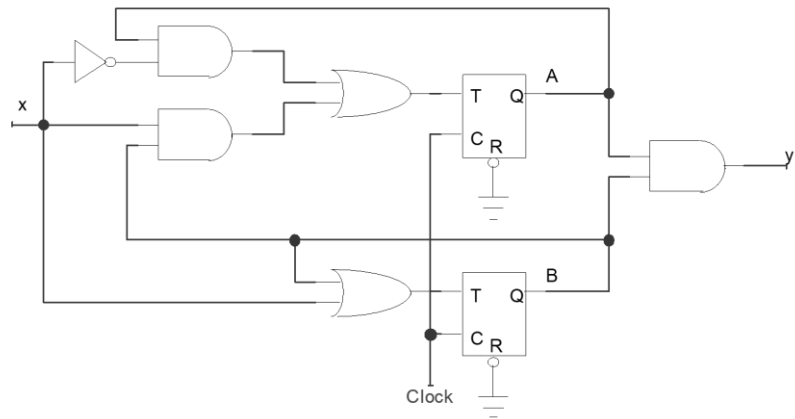
**Due : 17.12.2018**

**Hand in your homework solutions in class.**

**QUESTIONS:**

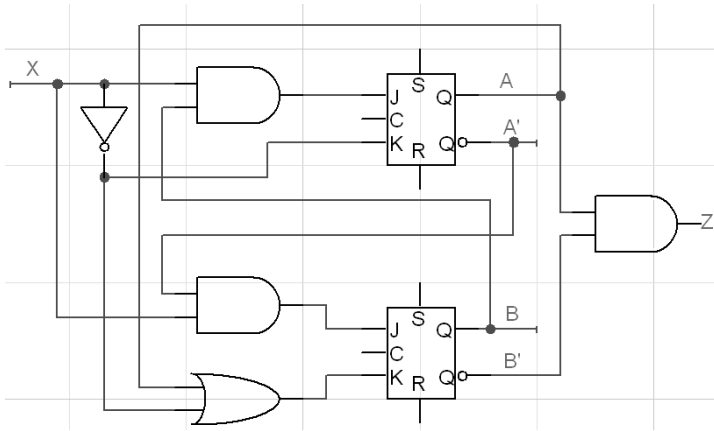
**Q1.** For the sequential circuit given at right, find:

- a. Input equations and state table.
- b. State equations and output equation.
- c. State diagram.

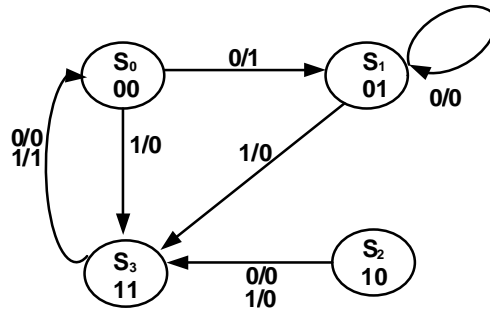


**Q2.** For the sequential circuit below:

- Find flip-flop input equations ( $J_A$ ,  $K_A$ ,  $J_B$ ,  $K_B$ ) and fill the state table.
- Write state equations and output equation.
- Draw its state diagram.



**Q3.** A Mealy type state diagram is given in the figure below. Using JK type flip-flops and gates, design and draw the circuit for this sequential system. (In the diagram  $X(\text{input}) / Y(\text{output})$ )



**Q4.** Design a Mealy type state machine with input X and output Y. Y should be 1 whenever the sequence **110 or 101** has been detected on X on the last 3 consecutive rising clock edges (or ticks). Otherwise, Y=0. Use at most two D flip-flops. An example input–output combination is given below:

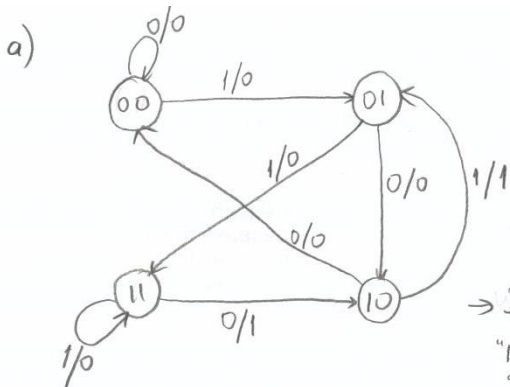
X	0	0	1	1	0	0	1	0	1	0	0	1	1	1	0	1	0	0	1	0	1	1	0	0	1	1	0	0	1	1
Y	0	0	0	0	1	0	0	0	1	0	0	0	0	0	1	1	0	0	0	0	1	0	1	0	0	0	1	0	0	0

You should show: a) State diagram. b) State table. c) Flip flop input equations and output equation.

**Q5.** A *PN* flip-flop has four functions given below:

<b><i>PN</i></b>	<b>Functions</b>
00	Reset to 0
01	No change
10	Complement
11	Set to 1

- Derive the characteristic equation for *PN* flip-flop. Show your work.
- Draw the Mealy type state diagram of a sequence detector that detects the sequence 1101. You must have at most four states. When the sequence 1101 is detected, the output *Z* becomes 1.
- Design the sequence detector using two *PN* flip-flops. (Hint: You should determine the flip-flop input equations,  $P_A$ ,  $N_A$ ,  $P_B$ ,  $N_B$ , and the output equation.)



00 → No sequence  
 01 → 1 is found  
 10 → 10 is found  
 11 → 11 is found

→ If "1" comes in state  
 "10", output becomes one,  
 and "1" sequence is found.  
 → If "0" comes in state  
 "11", output becomes one,  
 and "10" sequence is found.

b)

A	B	x	A*	B*	y
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	1	0	0
0	1	1	1	1	0
1	0	0	0	0	0
1	0	1	0	1	1
1	1	0	1	0	1
1	1	1	1	1	0

c)

A \ Bx	00	01	11	10
0			1	1
1			1	1

$$D_A = A^* = B$$

A \ Bx	00	01	11	10
0		1	1	
1		1	1	

$$D_B = B^* = x$$

A \ Bx	00	01	11	10
0				
1		1		1

$$\begin{aligned}
 y &= AB'x + ABx' \\
 &= A(B \oplus x)
 \end{aligned}$$