

# Theory Walk Through for Cross-Correlating Redshift-Free Standard Candles

Mukherjee and Wandelt (2018) Paper

Megan Tabbutt

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## 1 Abstract:

LSST will supply up to  $10^6$  supernovae (SNe) to constrain dark energy through the distance - redshift ( $D_L - z$ ) test. Obtaining spectroscopic SN redshifts (spec-zs) is unfeasible; alternatives are suboptimal and may be biased. We propose a powerful multi-tracer generalization of the Alcock- Paczynski test that pairs redshift-free distance tracers and an overlapping galaxy redshift survey. Cross-correlating  $5 \times 10^4$  redshift-free SNe with DESI or Euclid outperforms the classical  $D_L L - z$  test with spec-zs for all SN. Our method also applies to gravitational wave sirens or any redshift-free distance tracer.

## 2 Introduction:

- Accurate trace of the expansion history, e.g. through the  $D_L - z$  relation, is one of the foremost goals of current and next-generation surveys such as SDSS-IV, DES, DESI, EUCLID, LSST, and WFIRST
- LSST going to generate large type Ia SN sample at a rate of  $\geq 10^4 yr^{-1}$ . Already now, the  $\geq 10^3 yr^{-1}$  SNe being observed over a wide redshift range make it impossible to obtain time-consuming spectroscopic follow-up for every SN, (the traditional approach underlying the success of cosmology with standard candles over the last two decades).
- Alternative approach combines photometric types with spectroscopic redshift measurements of the presumed SN host galaxy, Errors may lead to biases and loss of information in the inferred cosmological parameters.
- Future galaxy redshift surveys (DESI, EUCLID) going to measure tens of millions of galaxy redshifts over large fractions of sky. It is realistic to expect a galaxy catalog with  $10^7$  spectroscopic redshifts overlapping SN data

sets over a wide redshift range on the time scale of LSST.

### 3 Idea:

Propose a new method to infer cosmological parameters accurately from distance tracers (e.g. SNe) without redshifts:

- Exploit fact that both distance tracers and galaxies are tracers of the matter density, and therefore spatially correlated through the underlying matter field
- Can tightly constrain cosmology by maximizing the spatial cross-correlation of overlapping distance catalog and redshift catalogs
- Approach shows a classical cosmological test in a new light as a limit of a multi-tracer generalization of the Alcock-Paczynski (A-P) test
- Particular feature of this cross-correlation approach is its robustness to both data systematics and modeling assumptions

### 4 Set-Up:

#### 4.1 Apparent Magnitude:

Constrain Luminosity Distance,  $D_L$  through relationship between apparent,  $m$ , and absolute,  $M$ , magnitudes calibrated from light curves:

$$m = 5 \log_{10} \left( \frac{D_L(z)}{pc} \right) + M - 5 \quad (1)$$

- Get light-curves from photometric observations, then calibrate the relationship and get  $D_L$ . For some data might already have this, like for DES-Sn.

- Equation is a definition of  $D_L$ , which is the thing you want to get and carry forward.

-  $m$  is the apparent magnitude, this comes from observations, at what point in the light curve do you pick for  $m$

???

-  $M$  is the absolute magnitude, this is gotten from fitting the light curve

## 4.2 Luminosity Distance:

The luminosity distance is related to the cosmological model and redshift through this equation:

$$D_L(z) = \frac{c}{H} (1+z) \int_0^z \frac{dz'}{\sqrt{\mathcal{E}(z')}} \quad (2)$$

$$\mathcal{E}(z) \equiv \Omega_m (1+z')^3 + \Omega_{de} \exp(3 \int_0^z d \ln(1+z')(1+\omega(z')))) \quad (3)$$

- Assume a flat universe ( $\Omega_K = 0$ , or  $\Omega_{de} = 1 - \Omega_m$ ) with dark energy equation of state:  $\omega(z) = \omega_0 + \omega_a(z/(1+z))$ )

## 4.3 Isotropic Two-Point Correlation Function:

At a separation,  $r$ , between two tracers ( $x$  and  $y$ ) of the density fluctuations, e.g.  $1 + \delta_x(\mathbf{s}) = \rho_x(\mathbf{s})/\bar{\rho}$ , with respect to the background density,  $\bar{\rho}$ , can be written as:

$$\xi_{x-y}^{iso}(r) = \frac{1}{2\pi^2} \int k^2 dk b_x(z) b_y(z) P(k) j_0(kr) e^{-k^2/k_{max}^2} \quad (4)$$

-  $P(k)$  is the non-linear power spectrum obtained from the ensemble average of the density fluctuations in the Fourier domain for wavenumber  $\mathbf{k}$

-  $j_0(kr)$  is the spherical Bessel function

-  $b_x = \delta_x/\delta_{dm}$  is the bias of the tracer  $x$  WRT Dark Matter - Things Ross has talked about before

- The cutoff  $k_{max}$  is introduced for a numerical convergence at high  $k$ , to avoid the oscillatory behavior of  $j_0(kr)$

- For galaxies:  $x = g$ , with galaxy bias  $b_g \approx 1.6$ ,

- For SNe:  $x = sn$  and  $b_{sn} = \delta_{sn}/\delta_{sdm}$ . While  $b_{sn}$  is uncertain there are studies which indicate that the  $b_{sn}$  may exceed  $b_g$  by around 60%. We will conservatively take  $b_{sn} \approx 1.6$  as a fiducial value

## 4.4 Red-Shift Space Distortions:

RSD's will affect galaxy positions in redshift space (not SNe because no red-shift label for us). Need to add a single Kaiser factor to the galaxy-SN cross-power spectrum:

$$P_{gs}(k) = (1 + f\mu_k^2/b_g)P_k \quad (5)$$

-  $f \equiv d \ln G / d \ln a$  is dimensionless growth rate -  $G$  is growth factor,  $\mu_k$  is the cosine of the angle between the Fourier modes and the line of sight

Keith Suggestions:

- Kaiser 1987 - this seems to be the seminar work in the field: *Clustering in real space and in red shift space* - Kaiser, 1987
- Hamilton 1992 - fairly technical, similar in spirit to the Kaiser 1987: Measuring Omega and the Real Correlation Function from the Redshift Correlation Function - Hamilton, 1991
- Percival et al. 2011 - more accessible review article: *Redshift-Space Distortions* - Percival et al., 2011

#### 4.5 Anisotropic Cross Correlation Function:

$$\xi_{g-sn}(\mathbf{r}) = \left(1 + \frac{f}{3b_g}\right) \xi_{g-sn}^{iso}(r) \mathcal{P}_0(\mu_r) + \frac{2f}{3b_g} (\xi_{g-sn}^{iso}(r) - \bar{\xi}_{gs}(r)) \mathcal{P}_2(\mu_r) \quad (6)$$

$$- \bar{\xi}_{gs}(r) = \frac{3}{r^3} \int_0^r \xi_{g-sn}^{iso}(s) s^2 ds$$

-  $\mu_r$  is the cosine of the angle between the line of sight and  $\mathbf{r}$

-  $\mathcal{P}_\ell(\mu_r)$  is the  $\ell$ th order Legendre Polynomial.

#### 4.6 Giant Equation:

$$\xi_{g-sn}(\mathbf{r}) = \left(1 + \frac{f}{3b_g}\right) \xi_{g-sn}^{iso}(r) \mathcal{P}_0(\mu_r) + \frac{2f}{3b_g} (\xi_{g-sn}^{iso}(r) - \frac{3}{r^3} \int_0^r \xi_{g-sn}^{iso}(s) s^2 ds) \mathcal{P}_2(\mu_r) \quad (7)$$

$$\xi_{x-y}^{iso}(r) = \frac{1}{2\pi^2} \int k^2 dk b_x(z) b_y(z) P(k) j_0(kr) e^{-k^2/k_{max}^2} \quad (8)$$