

# Efficient decoding of code-modulated evoked responses

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- **(Spontaneous) oscillations**

- Not time-locked, internally generated (endogenous)
- Change in power at a specific frequency, e.g., SMR



- **Evoked responses**

- Time-locked to an external event (exogenous)
- Change in amplitude at a specific latency, e.g., P300



[Blankertz (2014) *BBCI Winter School*]

# Evoked responses

- **Transient responses**

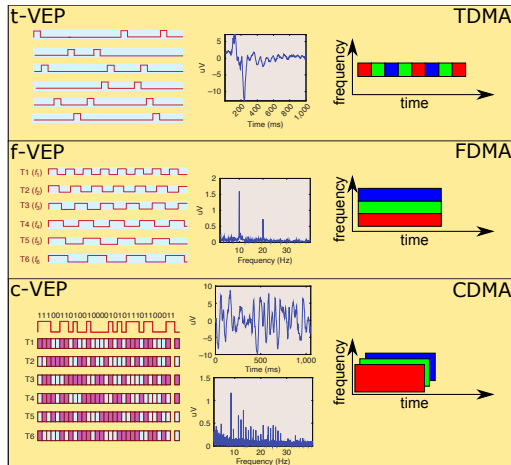
- Response to a *single* event
- Protocol: e.g., oddball
- Examples: P300, ERN, MMN

- **Steady-state responses**

- Response to *periodic* sequence of events
- Protocol: frequency-tagging
- Examples: SSVEP, ASSR, SSSEP

- **Broad-band responses**

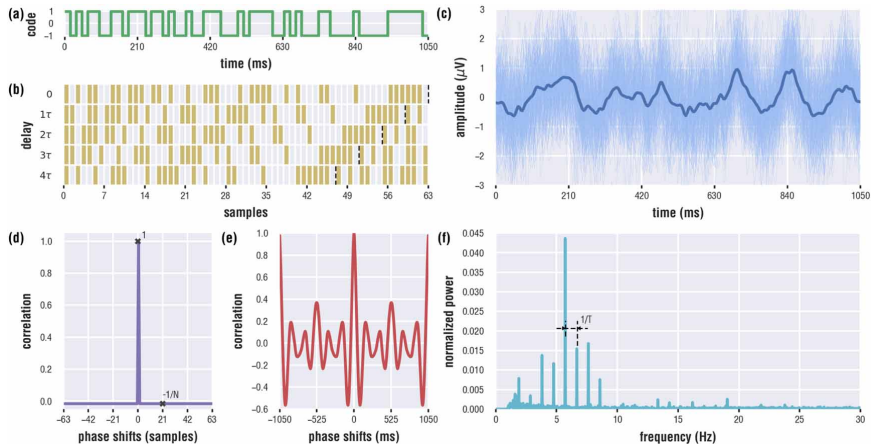
- Response to *pseudo-random* sequence of events
- Protocol: noise-tagging
- Examples: c-VEP, c-AEP, c-SEP



[Bin et al. (2009) *IEEE Comput Intell M*] [Gao et al. (2014) *IEEE T Bio-Med Eng*]

# Code-modulated visual evoked potential (c-VEP)

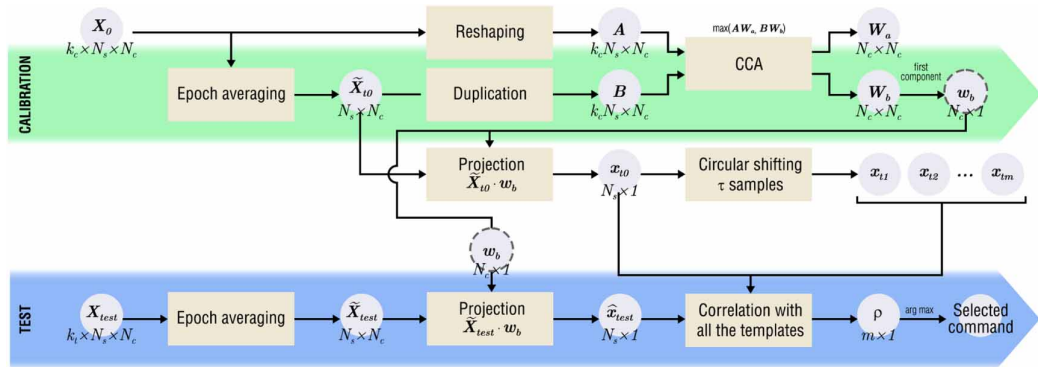
|    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|
| 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 0  |
| 31 | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  |
| 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
| 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 0  |
| 31 | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  |



[Spüler et al. (2012) *PLOS ONE*]

[Martinez-Cagigal et al. (2021) *J Neural Eng*]

# Reference c-VEP analysis pipeline

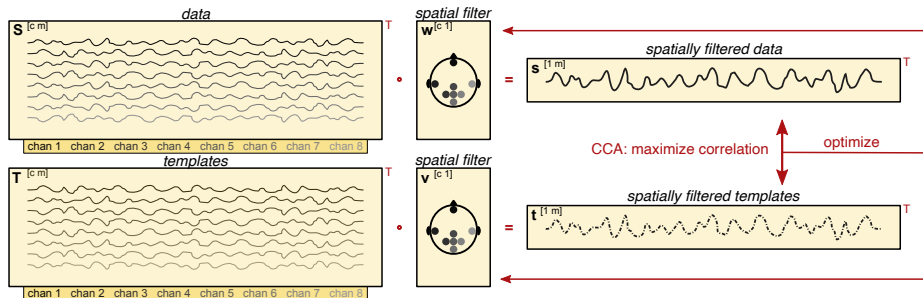


$$\hat{y} = \arg \max_i \rho(\mathbf{w}^\top \mathbf{X}, \mathbf{w}^\top \mathbf{T}_i)$$

[Martinez-Cagigal et al. (2021) *J Neural Eng*]

# Canonical correlation analysis (CCA)

- 1 For each of  $i = 1 \dots n$  classes, compute the template  $\mathbf{R}_i \in \mathbb{R}^{c \times m}$
- 2 Stack all epochs/trials:  $\mathbf{S} = [\mathbf{X}_0, \dots, \mathbf{X}_k]$
- 3 Stack all templates:  $\mathbf{T} = [\mathbf{R}_{y_0}, \dots, \mathbf{R}_{y_k}]$
- 4 Apply CCA( $\mathbf{S}, \mathbf{T}$ ) to find spatial filters  $\mathbf{W} \in \mathbb{R}^{c \times c}$  and  $\mathbf{V} \in \mathbb{R}^{c \times c}$



[Hotelling (1936) *Biometrika*] [Spüler et al. (2012) *ESANN*] [Spüler et al. (2013) *IEEE T Neur Sys Reh*]

# Downside of the reference analysis pipeline

## Requires a large training dataset!

- Depends on [averaging epochs/trials](#) to obtain templates
- Even worse when there is no relation between classes (i.e., sequences)

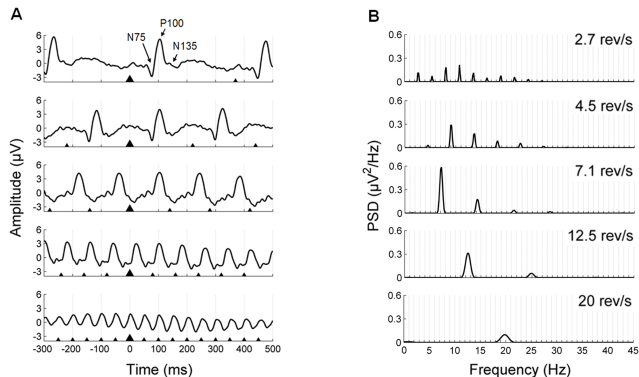
## How can one reduce the required amount of data?

- Exploit the repeating structure in the data
- [Average events](#) within and across epochs/trials

# Linear superposition hypothesis

The response to a sequence of events is the addition of the responses to the individual events.

$$x(t) = \sum_i \sum_{\tau} l_i(t) r_i(t - \tau)$$

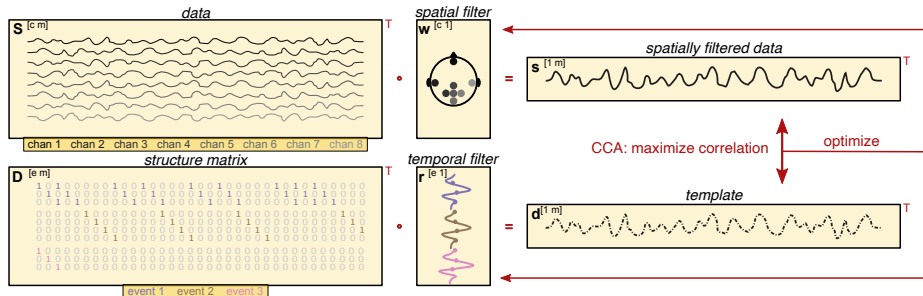


[Capilla et al. (2011) *PLOS ONE*]



# CCA for spatio-temporal decomposition (reconvolution)

- 1 Stack all epochs/trials  $\mathbf{S} = [\mathbf{X}_0, \dots, \mathbf{X}_k]$
- 2 Stack all design matrices  $\mathbf{D} = [\mathbf{M}_{y_0}, \dots, \mathbf{M}_{y_k}]$
- 3 Apply CCA( $\mathbf{S}, \mathbf{D}$ ) to find **spatial filters**  $\mathbf{W} \in \mathbb{R}^{c \times z}$  and **temporal filters**  $\mathbf{R} \in \mathbb{R}^{e \times z}$



[Thielen et al. (2015) *PLOS ONE*] [Thielen et al. (2021) *J Neural Eng*]

# From supervised to semi-supervised with reconvolution

**Supervised** (calibration):

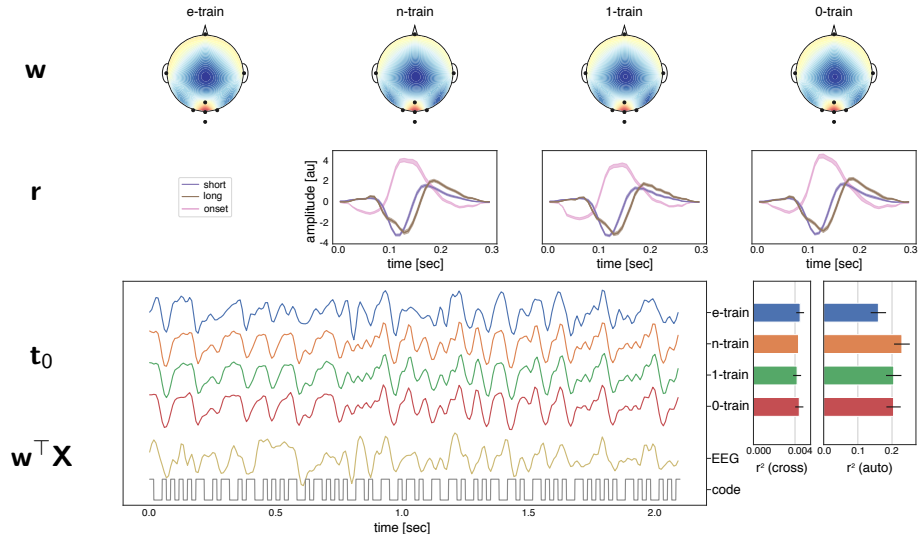
$$\max_{\mathbf{w}, \mathbf{r}} \rho(\mathbf{w}^\top \mathbf{S}, \mathbf{r}^\top \mathbf{D}_i)$$
$$\hat{y} = \arg \max_i \rho(\mathbf{w}^\top \mathbf{X}, \mathbf{r}^\top \mathbf{M}_i)$$

**Semi-supervised** (calibration-free):

$$\max_{\mathbf{w}_i, \mathbf{r}_i} \rho(\mathbf{w}_i^\top \mathbf{X}, \mathbf{r}_i^\top \mathbf{M}_i)$$
$$\hat{y} = \arg \max_i \rho(\mathbf{w}_i^\top \mathbf{X}, \mathbf{r}_i^\top \mathbf{M}_i)$$

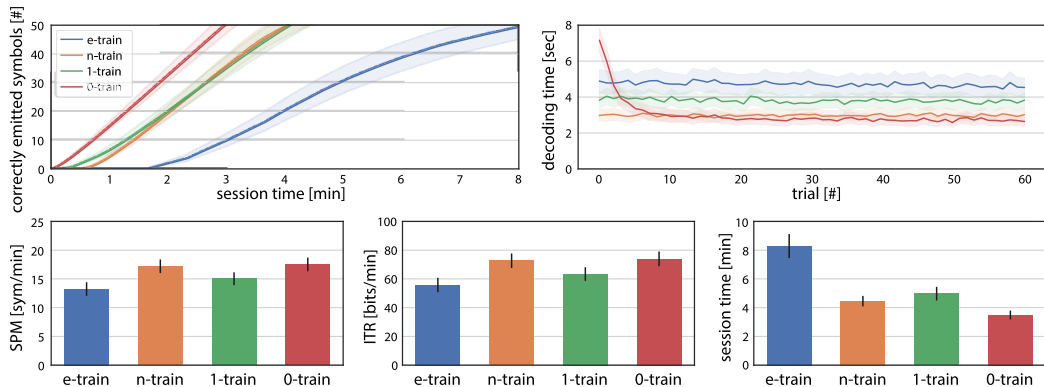
[Thielen et al. (2015) *PLOS ONE*] [Thielen et al. (2021) *J Neural Eng*]

# Reconvolution finds a similar model using limited data



[Thielen et al. (2021) *J Neural Eng*]

# Reconvolution achieves state-of-the-art performance with limited data



[Thielen et al. (2021) *J Neural Eng*]

## Exploiting **structure in neural data**

- Forward model assuming linear superposition hypothesis
  - Limits number of model parameters
  - Increases number of repetitions per parameter
- Limits as well as eliminates the need for training data
  - Achieves high explained variance and decoding performance
  - Generalizes to unseen data/sequences

## Reconvolution CCA (rCCA)

- Tutorial at the end of the workshop
- <https://neurotechlab.socsci.ru.nl/resources/cvep/>
- Python Noise-Tagging ([pynt](#)) library compatible with the scikit-learn API
- Matlab Noise-Tagging ([mant](#)) library



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## The role of code-modulated evoked potentials in next-generation brain-computer interfacing

<https://www.frontiersin.org/research-topics/50998/>

the-role-of-code-modulated-evoked-potentials-in-next-generation-brain-computer-interfacing

# Acknowledgements

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## **BCI lab**

- Peter Desain
- Jason Farquhar
- Pieter Marsman
- Philip van den Broek

## **Primer on posters:**

- 1-F-57: A model-based **dynamic stopping** method for c-VEP BCI (*Ahmadi*)
- 3-C-22: A comparison of **stimulus sequences** for c-VEP BCI (*Thielen*)