

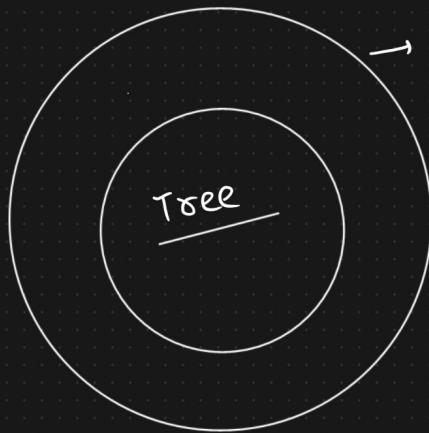
Tree Data Structure

Tree → 1) Non-Linear Data Structure, Hierarchy based
 ↓
 2) Application - Database (Indexing, file system)

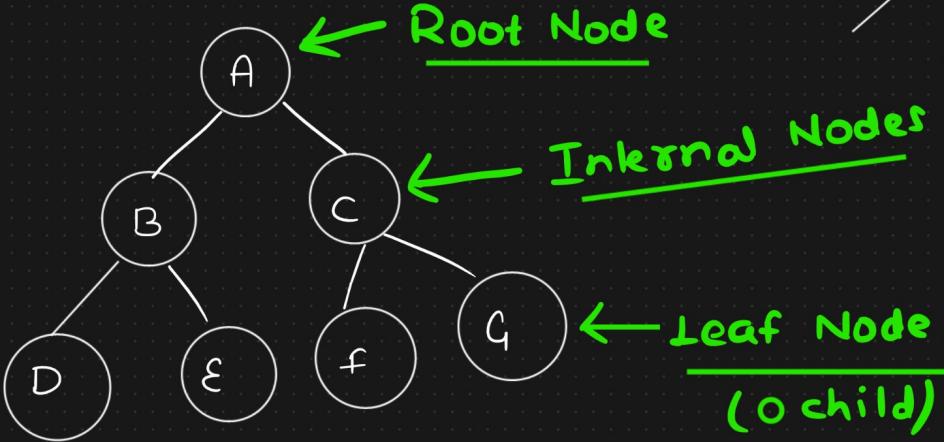
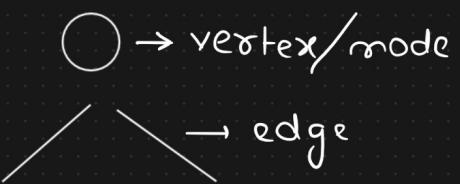
acyclic
 (No cycle)

- Networking
- Google Maps

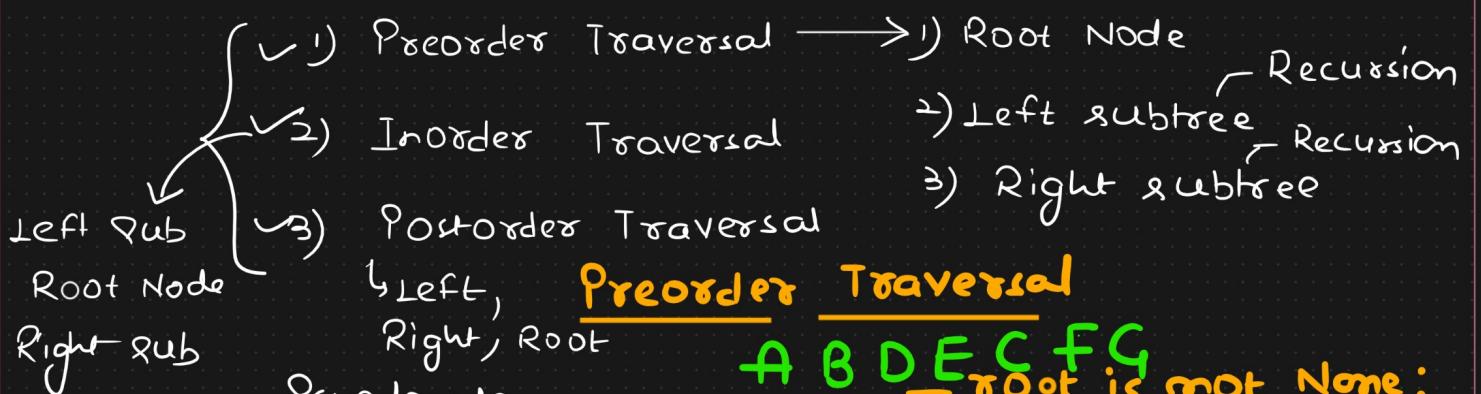
Graph → cycle as well cycle acyclic
 ↓
 → Graph



↳ Binary Tree → at most 2 child nodes
 (0, 1, 2)



Traversal → Traverse every node inside the tree

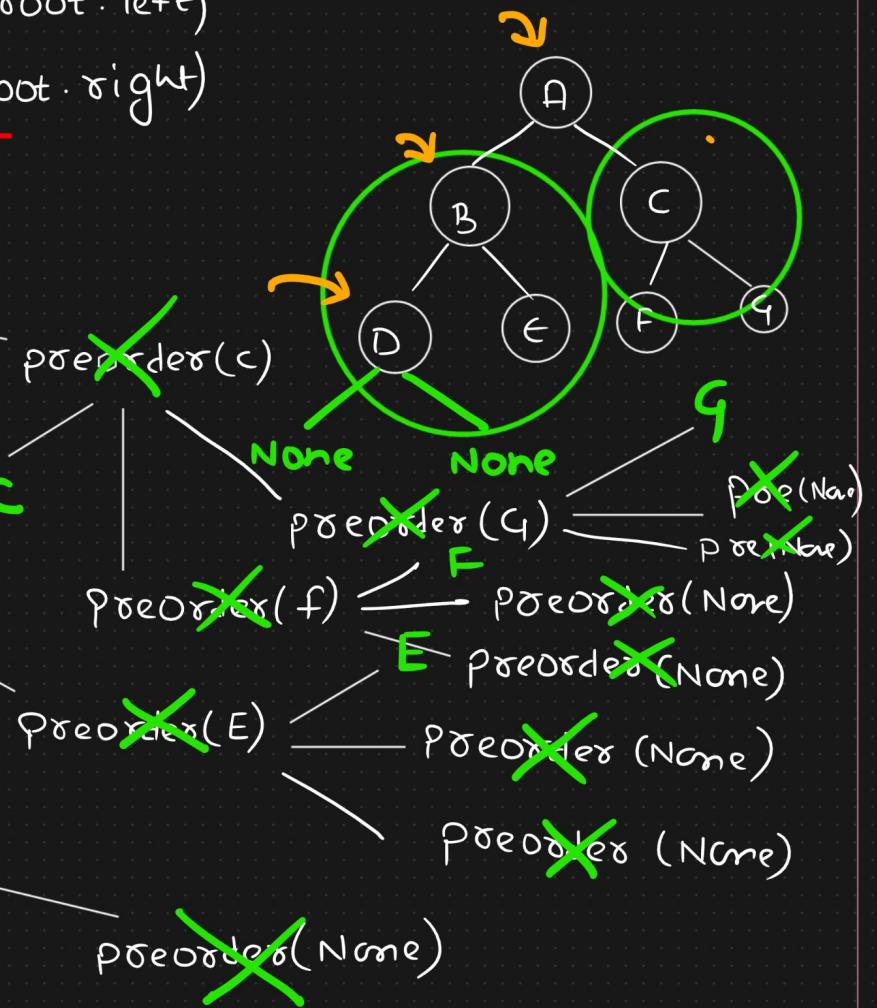
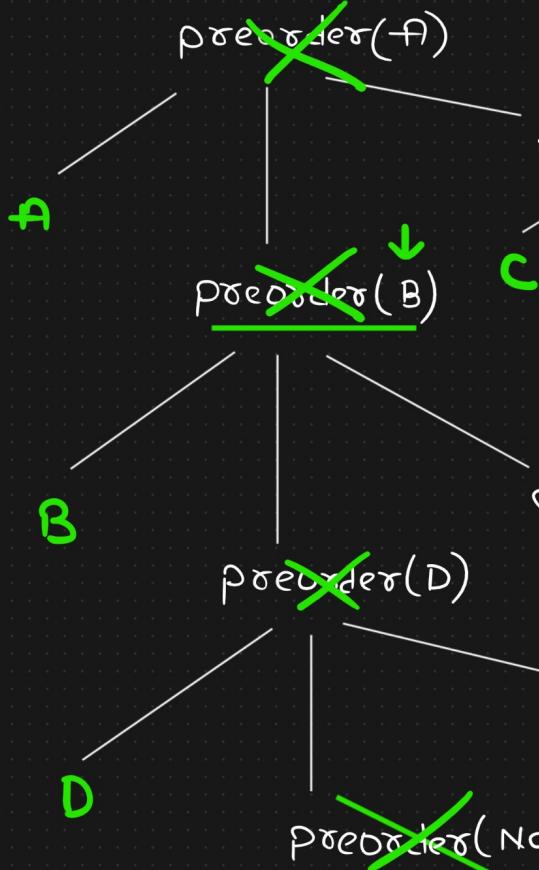


Psuedocode

- ```

Preorder(root):
 ① — print(root.data)
 ② — Preorder(root.left)
 ③ — Preorder(root.right)

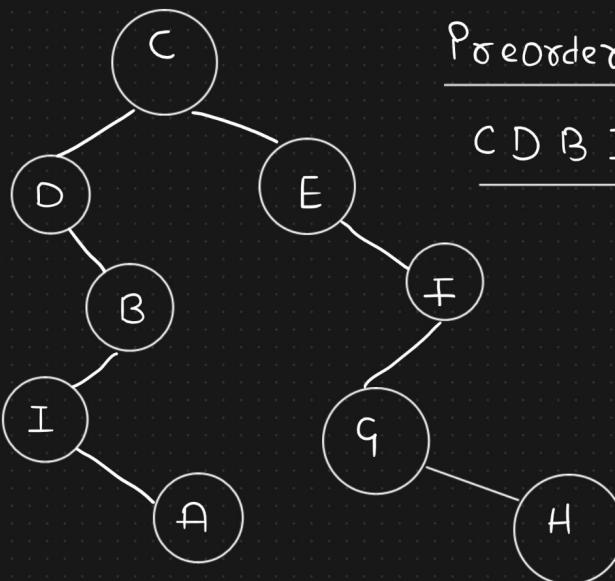
```



Practice  
problem

Inorder

DIA B C E G + F



Postorder

C D B I A E F G H

Inorder Traversal

D B E A F C G

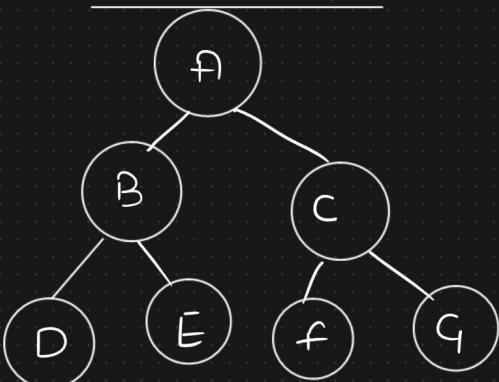
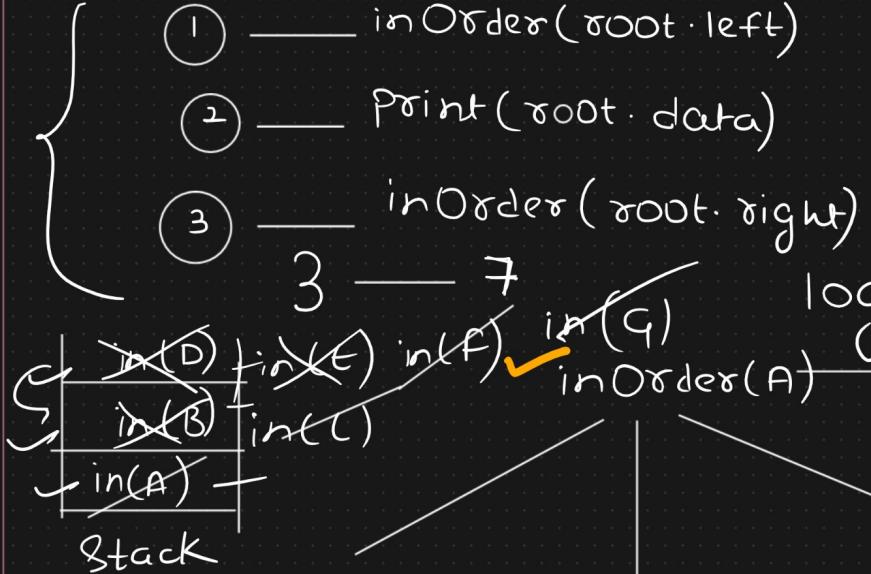
inOrder( $\text{root}$ ):

if  $\text{root}$  :

    ① — inOrder( $\text{root} \cdot \text{left}$ )

    ② — print( $\text{root} \cdot \text{data}$ )

    ③ — inOrder( $\text{root} \cdot \text{right}$ )



$\log_2 n$

D B E A F C G

✓ inOrder(B)

A

✓ inOrder(C)

✓ inOrder(F)

✓ inOrder(G)

✓ inOrder(D)

None

D ✓

None

B ✓

✓ inOrder(E)

None

E ✓

None

None

f

None

C ✓

None

G ✓

None

C

## Recursive Tree

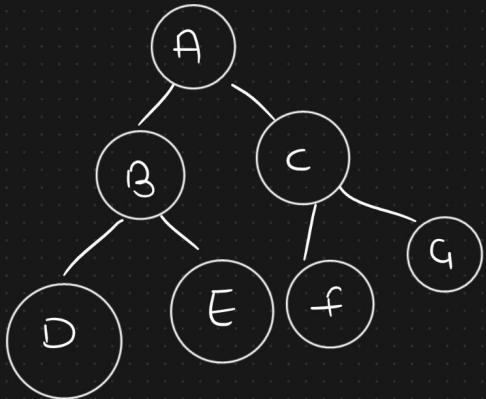
↳ Postorder fashion

### Postorder

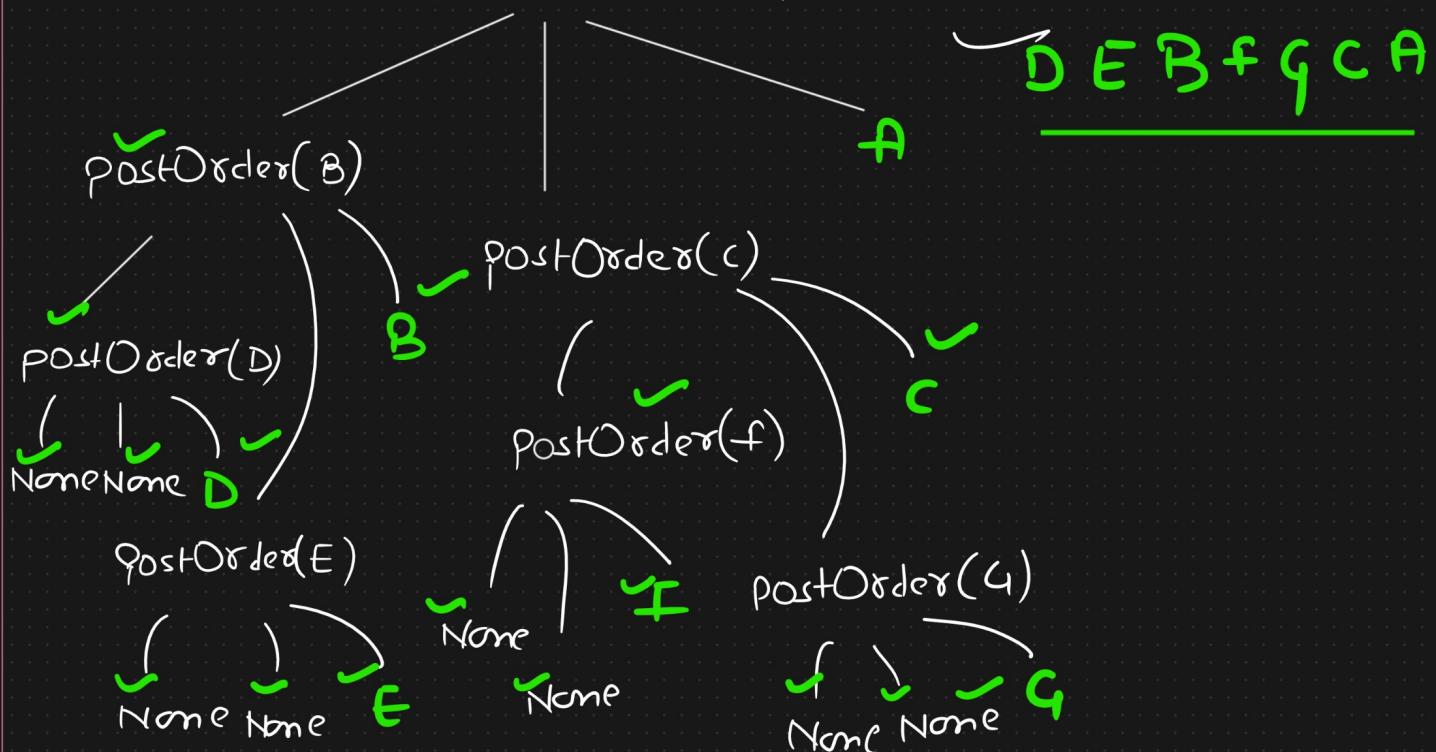
postOrder( $\text{root}$ ):

- ```
if  $\text{root}$  :  
    ① —— postOrder( $\text{root.left}$ )  
    ② —— postOrder( $\text{root.right}$ )  
    ③ —— print( $\text{root.data}$ )
```

DEBFGCA



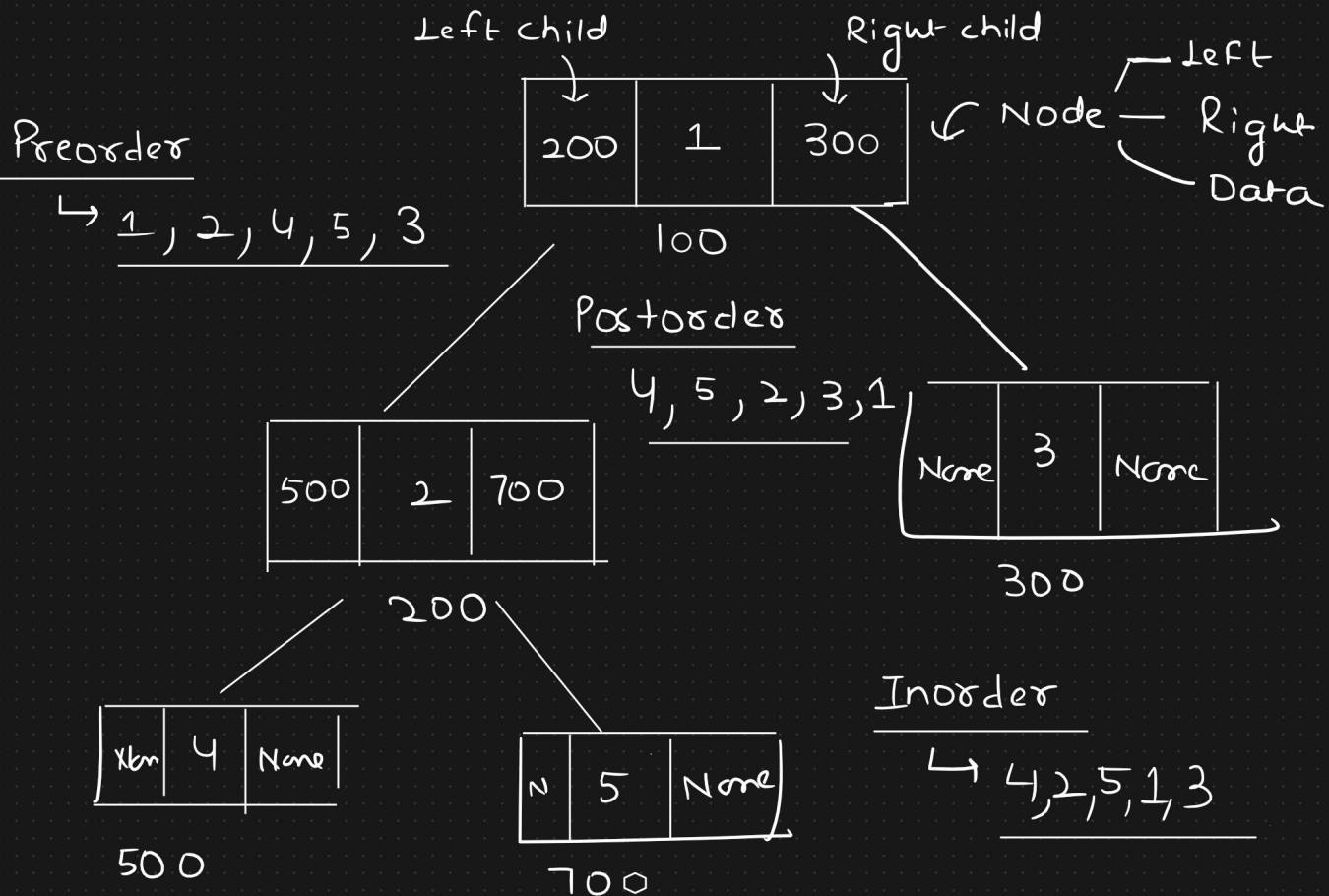
✓ postOrder(A)



PostOrder → Root Node (End)

PreOrder → Root Node (Start)

InOrder → Root Node (In between)



Time complexity

Preorder — if τ_{root} :

$$T(n)$$

$$T\left(\frac{n}{2}\right)$$

Balanced Tree

Best case scenario

Print($\text{root}.\text{data}$)

c

1

Preorder($\text{root}.\text{left}$)

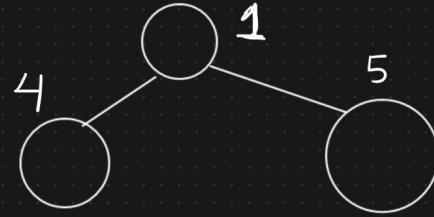
2

Preorder($\text{root}.\text{right}$)

3

$$T\left(\frac{n}{2}\right)$$

Balanced Tree



Recurrence Relation

$$T(n) = 2T\left(\frac{n}{2}\right) + c$$

$$a=2$$

$$b=2$$

$$\log_b a = \log_2 2 = 1$$

$$T(n) = \Theta(n)$$

Equal distribution of elements on

left & Right subtree

Worst case scenario

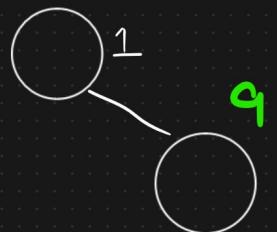
Skewed tree

→ unbalanced tree

Worst case scenario

$$T(n) = T(n-1) + c$$

$$T(n) = \Theta(n)$$



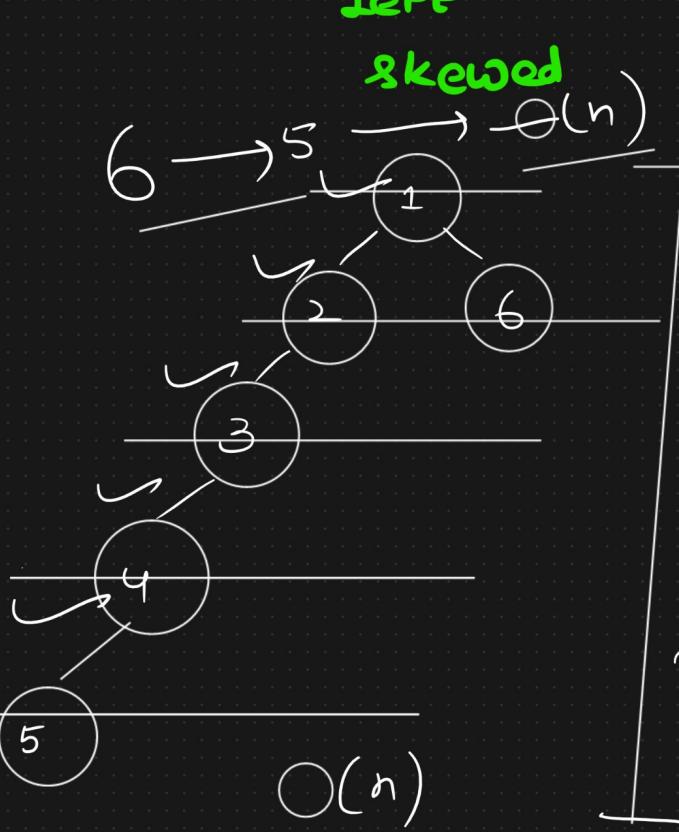
{ Space complexity → $\Theta(\log n)$

→ Best case Scenario

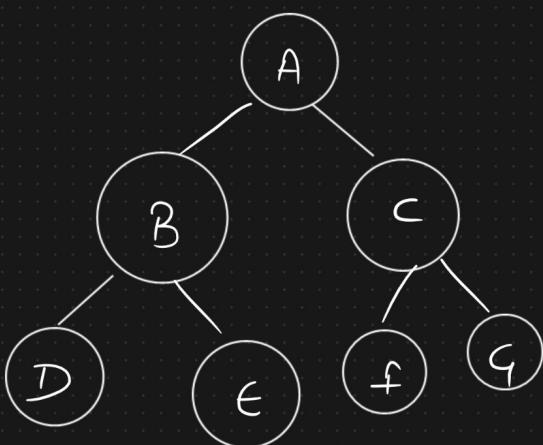
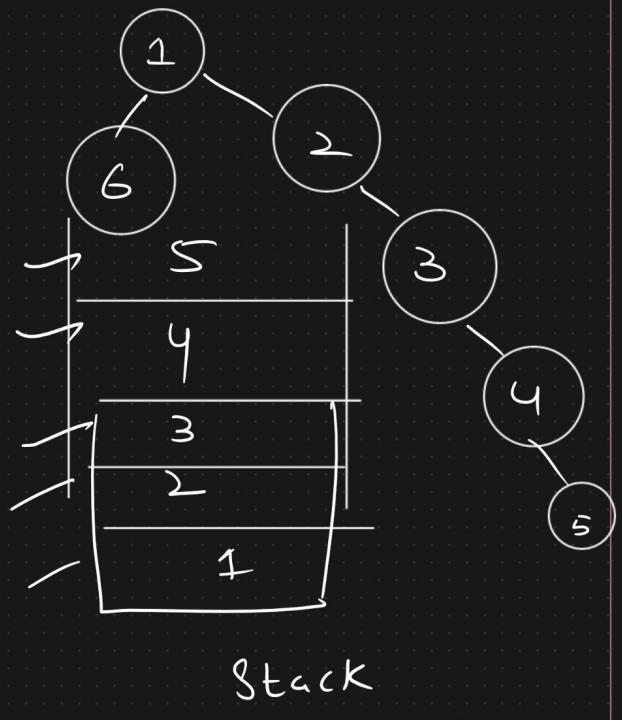
Space complexity → $\Theta(n)$

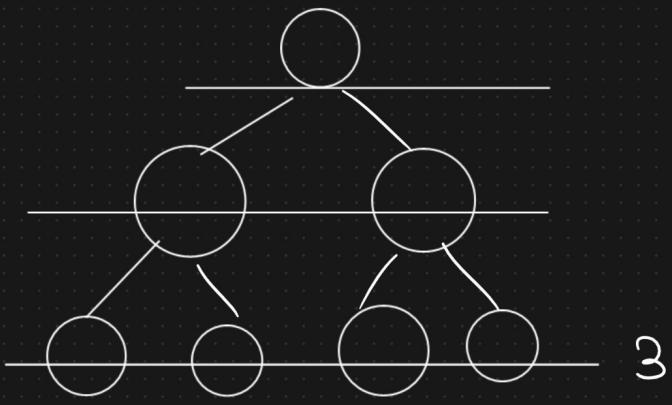
→ Worst case scenario

Skewed Tree



Right Skewed





$$\frac{\log n}{\log_2}$$

3