WWW, WIKIPEDIA AND OSNS

AP

NETWORKS OF HUMANS

Theme: no one controls the evolution of the network, which is selforganizing

What is represented (self, news, opinion, concept) and its **lifecycle** determines the structure and the research questions

look at how they connect and when

Direction of communication is important

```
1 import networkx as nx
2
3 eu_DG = nx.DiGraph()
```

GETTING DATA

WWW

- a Networkx digraph will represent connectivity
- a companion dictionary maps vertices to URLs of the relative pages
- source: a scrape of the 2005 ".eu" domain

TWITTER

- supported by the Twython module
- requires Twitter registration/API token
- alternative platforms exist, e.g. Tweety (+NLTK)
- interesting: the network of mentions as a voting system

WIKIPEDIA

- a network of concepts (lemmas/lemmata) maintained by humans (and some bot)
- time-stamped evolution of the network is available [here]
- contrary to curated taxonomies, e.g., [Linnaeus, 1735], this is not a tree

a directed acyclic graph is the reference model

RANKING ALGORITHMS: PAGERANK

PAGERANK IDEA

Assign a **rank** to each vertex (page) on the basis of its *importance* in the navigation of the network.

Importance will then be captured by the relative value of the dominant Eigenvector of a new matrix P that represents *navigation*

VARIABLES USED

A: directed adjacency matrix (admits dangling ends)

 $K0^{-1}$: 0 everywhere but $rac{1}{k_j}$ on the main diagonal

$$N = A \cdot K0^{-1}$$

E: 0 everywhere but $\frac{1}{|V|}$ on the main diagonal

$$P = \alpha N + (1 - \alpha)E$$

Experimentally, set $\alpha=0.85$

I.e., $1-\alpha$ times navigation will *jump out* of a path and into an arbitrary restart node.

RANKING ALGORITHMS: HITS

HITS IDEA

Hyperlink-Induced Topic Search [Kleinberg, 1999]

Sees importance of a node in a more nuanced way:

Pages that are important for consultation, e.g., train schedules, have authority and tend to be terminal

Well-connected *hub* pages that facilitate navigation, e.g., Time Out, are useful but not authoritative per se

- 1. authority score au(i)
- 2. hub score $\mathbf{h}(\mathbf{i})$

HITS AS MUTUAL RECURSION

Hub-iness influences authority which in turns influences hub-iness:

$$au(i) \propto \sum_{j
ightarrow i} h(j)$$

page *i* is authoritative proportionally to the sum of the hub-iness of the pages that link to it.

$$h(i) \propto \sum_{i
ightarrow j} au(j)$$

page *i* is hub proportionally to the sum of the authoritativeness of pages that it links to.

COMPUTING HITS SCORES

We could start with assigning 1 everywhere and hoping that mutual recursion will converge to stable *au* and *h* values.

As with Von Mises' method, we normalise vectors to 1 at each iteration.

LINEAR ALGEBRA DERIVATIONS

$$\mathbf{h} \propto AA^T\mathbf{h} = \lambda_h AA^T\mathbf{h}$$

$$\mathbf{au} \propto A^T A \mathbf{au} = \lambda_{au} A^T A \mathbf{au}$$

I.e., we can find ${f h}$ and ${f au}$ separately by solving the eigenvalue problem for the matrices AA^T and A^TA

MAIN RESULT

For primitive matrices (i.e., connected networks, no dead-ends/sinks)

$$\mathbf{h} \propto AA^T\mathbf{h} = \lambda_h AA^T\mathbf{h}$$
 $\mathbf{au} \propto A^TA\mathbf{au} = \lambda_{au}A^TA\mathbf{au}$

- convergence is assured;
- dominant λ is unique and
- values for h and au will be all positive, as desired.

(negative values have no interpretation here)

COMMUNITY DETECTION

FINDING SOCIAL STRUCTURES

this is an example of Provost-Fawcett's problems

- 4: Clustering
- 5: co-occurrence grouping

For homogeneous networks, eg., country-to-county of Ch. 2

Community: nodes that are closely connected with each other by strenght or density

Resolution limit: communities with less than $\sqrt{|V|}$ members cannot be properly identified.

GIVAN-NEWMAN

- 1. Rank edges by their help to connectivity
- 2. remove the top-ranking edge
- 3. repeat until loss of connection
- 4. now-isolated areas are called communities

Hyp: Betweenness centrality captures help to connectivity

MODULARITY

AS AN OPTIMIZATION PROB.

Istance: an adj. matrix A, a small integer g

Solution: a partition of V into g groups

Measure: maximise Q: the overall modularity measure

Interpretation: how likely is a random walker to leave the community?

THE Q FACTOR

Let $E_{g imes g}$ be the cross-group matrix and f_i the sum of col. i

Electrical conductance:

$$Q=\sum_{i=1}^g e_{ii}-f_i^2$$

Complexity: NP-complete

Even random networks might exibit densifications that might look as c.