**CLASSIFICATION: THE NEAREST-NEIGHBORS ALGORITHM (K-NN)** 

AP

# FROM THE INTRODUCTION:

1. Classification and class probability

#### **Instance:**

a collection (dataset) of datapoints from X

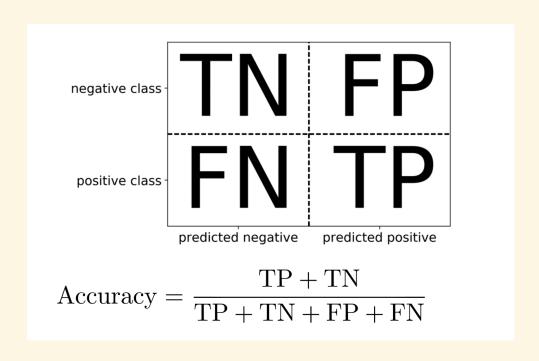
ullet a classification system  $C=\{c_1,c_2,\ldots c_r\}$ 

**Solution:** classification function  $\gamma: \mathbf{X} o C$ 

Measure: misclassification

# MISCLASSIFICATION WHEN R=2

- it's described by the *confusion matrix*, which scores the result of classification against labeled examples.
- often one class is of more interest than the other: better measures are needed.
- accuracy on the given examples does not automatically translate into accuracy on new, previously-unseen data



# **BINARY CLASSIFICATION IN 2D**

With just two numerical dimensions, datapoint similarity can be interpreted as simple Euclideian distance.

Being very close ← being very similar

Q: are 4 and 6 more similar to each other than -1 and +1?

Assumption: small changes in the values won't alter the classification, close points will receive the same classification

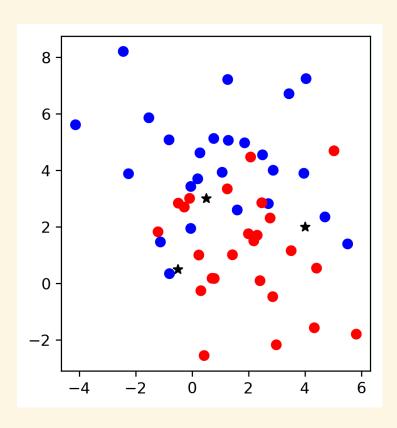
if a point is in close distance to a labeled one then assign the same class

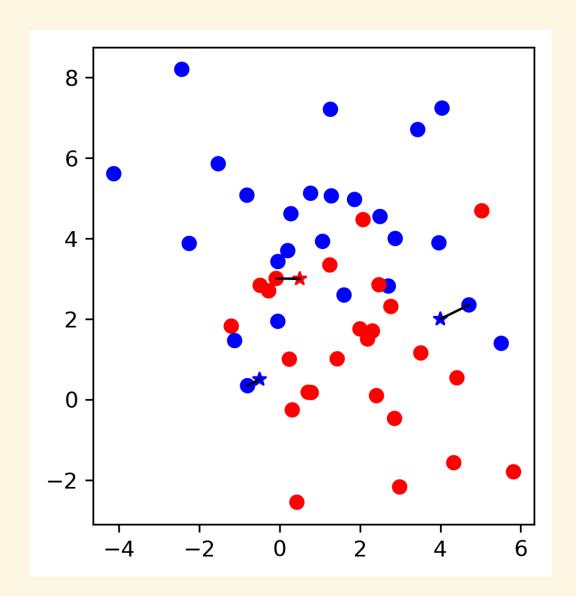
# THE NEAREST NEIGH. ALGORITHM

Take a set of labeled points (the examples), all others are *blank* at the moment.

Whenever a blank point has a nearest neighbor datapoint which is labeled, give it the same label

This is the NN, or 1-NN algorithm.





$$\gamma(\mathbf{x}) = y_i, i = \operatorname{argmin}_j ||\mathbf{x}_j - \mathbf{x}||$$

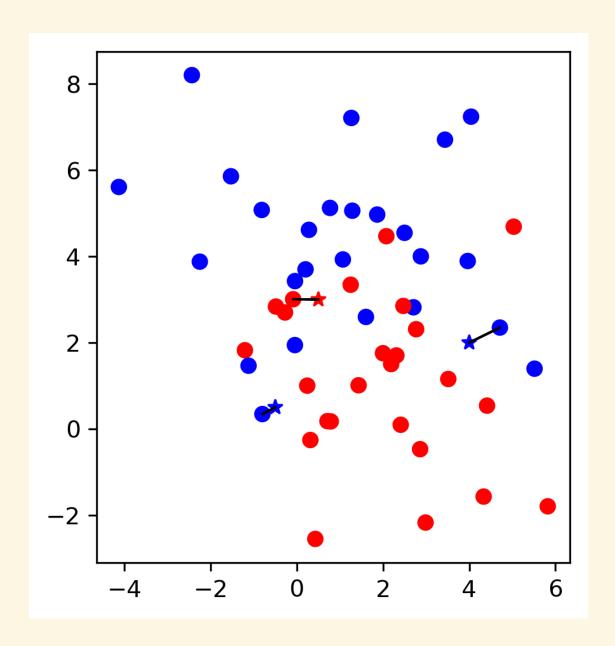
## FROM 1-NN TO K-NN

Consider the *k* nearest neighbors

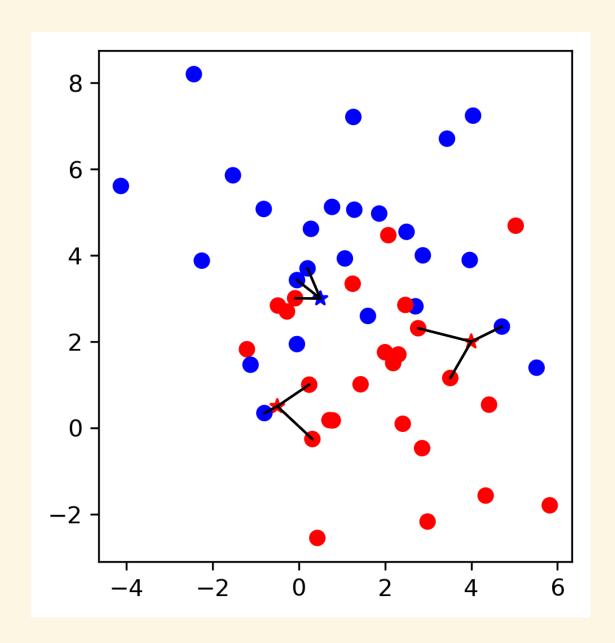
Assign the class that is the most common among them

Variation: consider each label relative to the effective distance of the neighbor.

### **1-NN**



# **3-NN**



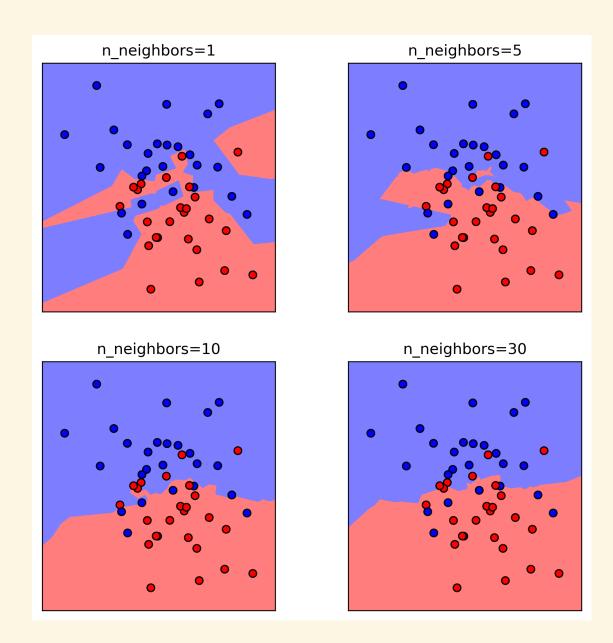
# **LEARNING**

Given the labeled examples, k-NN determines the areas around each example which give a certain class.

k-NN learns an area or *surface* and applies it in classification

A larger k does not always mean a better classification

# **INFLUENCE OF K**



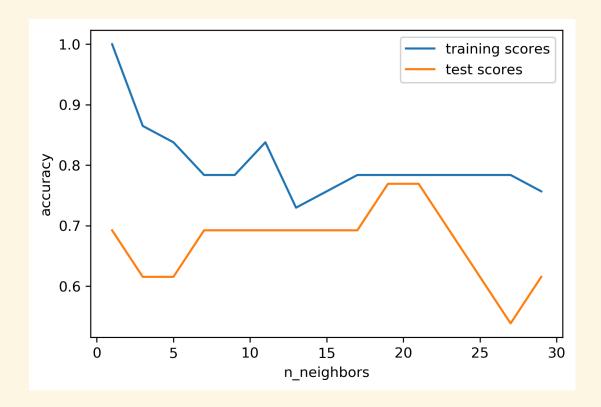
# **OBSERVATIONS**

#### k-NN

- introduces us to voting systems
- is effective when the two classes are balanced, i.e., not *skewed*, in the dataset
- there is no standard way to choose k, yet it may greatly influence the outcome:
  - we face hyperparameter optimization.
- on large training data, even 1-NN approaches the *irreducible\_error\_rate* (2x).

# **TRADE-OFFS**

Sometimes improving accuracy on the training data does not translate into improved accuracy in testing against *unseen* data



1-NN is perfect on training but 0.7 on test.

Increasing k does not improve much and overfitting creeps in.