**CALCULATE ENTROPY** 

AP

# THE SETUP

### **WEATHER NEWS**

 $X_{LDN} \in \{$  snow, showers, light rain, wet, misty, cloudy, breezy, bright, sunny $\}$ 

$$Pr[X_{LDN} = x_i] = [\frac{1}{16}, \frac{1}{8}, \dots \frac{1}{8}, \frac{1}{16}]$$

 $X_{WH} \in \{ \text{ cloudy w. light rain, sunny} \}$ 

$$Pr[X_{WH}=y_i]=[rac{1}{8},rac{7}{8}]$$

## LET'S CALCULATE

#### **ENTROPY IN WADI HALFA**

$$egin{aligned} H[X_{WH}] &= \sum Pr[X_{WH} = y_i] \cdot I[y_i] \ H[X_{WH}] &= -\sum Pr[X_{WH} = y_i] \cdot \log_2 Pr[X_{WH} = y_i] \ H[X_{WH}] &= -rac{1}{8} \cdot \log rac{1}{8} - rac{7}{8} \cdot \log rac{7}{8} \end{aligned}$$

$$=-\frac{1}{8} \cdot \log \frac{1}{8} - \frac{7}{8} [\log 7 - \log 8]$$

$$=\frac{1}{8} \cdot \log 8 + \frac{7}{8} [\log 8 - \log 7]$$

$$=\frac{1}{8}\cdot 3+\frac{7}{8}[3-2.8073]$$

$$=\frac{3}{8}+\frac{7}{8}\cdot 0.2$$
 (let's round it)

$$=\frac{3}{8}+\frac{7}{8}\cdot\frac{1}{5}$$

$$= \left[\frac{3}{8} \cdot 5 + \frac{7}{8}\right] \frac{1}{5}$$

$$= \frac{22}{8} \cdot \frac{1}{5}$$

$$=2.75\cdot0.2=0.55pprox1$$
 bit needed.

### **ENTROPY IN LONDON**

$$egin{aligned} H[X_{LDN}] &= \sum Pr[X_{LDN} = x_i] \cdot I[x_i] \ H[X_{LDN}] &= -\sum Pr[X_{LDN} = x_i] \cdot \log_2 Pr[X_{LDN} = x_i] \ H[X_{LDN}] &= -rac{1}{16} \cdot \log rac{1}{16} - rac{1}{8} \cdot \log rac{1}{8} \ldots \end{aligned}$$

$$=-2\frac{1}{16}\cdot\log\frac{1}{16}-7\frac{1}{8}\log\frac{1}{8}$$

$$=2\frac{1}{16}\cdot \log 16 + 7\frac{1}{8}\log 8$$

$$= \frac{1}{8} \cdot \log 16 + \frac{7}{8} \log 8$$

$$= \frac{1}{8} \cdot 4 + \frac{7}{8} \cdot 3$$

$$=rac{25}{8}=3.125pprox4$$
 bits needed.